Polyvariant Staging

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Abstract

In staged languages each term is executed at a single *compilation stage* that is determined based on: quotation (e.g., MetaOCaml), or types (e.g., LMS). To ensure *cross-stage persistence* (i.e., correctness) types of next/previous stage terms must annotated. Consequentially staged functions are *monovariant*: their arguments can not vary with respect to a compilation stage.

Type based staged languages require type annotations of all *next stage* terms, as well as implementing reification and code generation logic for all next stage types. Further, when we use staging at host language compile-time, all terms scheduled to execute at runtime require type annotations and all libraries used at runtime require logic for reification and code generation. Annotations are especially noticeable in languages with local type inference as types of method parameters must be provided by the programmer.

We introduce a type based staging extension for Scala where we transparently extend Scala with polymorphic binding-time information. By using this information we enable parametrically polymorphic parameters to also be stage polymorphic. With our scheme defining stage polyvariant functions can be done through existing language features (i.e., bounded parametric polymorphism). Further, terms whose types are monomorphically annotated are executed in the earlier stage of compilation, in our case, at host language compile-time. Annotated types rely on the polymorphic binding time to represent merely *compile-time views* of original types. This obviates the necessity for reification and code generation logic. We compare our framework with LMS and show that in majority of programs we require less type annotations while we achieve same performance improvements.

Categories and Subject Descriptors D.3.3 [Programming Languages]: Language Constructs and Features

Keywords Multi-Stage Programming, Partial Evaluation

1. Introduction

Multi-stage programming (or staging) is a meta-programming technique where compilation is separated in multiple stages. Execution of each stage outputs code that is executed in the next stage of compilation. The first stage of compilation happens at the host language

compile time, the second stage happens at the host language runtime, the third stage happens at runtime of runtime generated code, etc. Different stages of compilation can be executed in the same language [??] or in different languages [??]. In this work we will focus on staging where all stages are in the same language and that, through static typing, assures that terms in the next stage are well typed.

Notable staging systems in statically typed languages are MetaOCaml [??] and LMS [?]. These systems were successfully applied as a *partial evaluatior* [?]: for removing abstraction overheads in high-level programs [??], for domain-specific languages [???], and for converting language interpreters into compilers [??]. Staging originates from research on two-level [??] and multi-level [?] calculi.

We show an example of how staging is used for partial evaluation of a function for computing the inner product of two vectors¹:

```
def dot[T:Numeric](v1: Vector[T], v2: Vector[T]): T =
  (v1 zip v2).foldLeft(zero[T]) {
   case (prod, (cl, cr)) => prod + cl * cr
}
```

In function dot, if vector sizes are constant, the inner product can be partially evaluated into a sum of products of vector components. To achieve partial evaluation, we must communicate to the staging system that operations on values of vector components should be executed in the next stage. The compilation stage in which a term is executed is determined by *code quotation* (in MetaOCaml) or by parametric types Rep (in LMS). In LMS we denote that the vector size is statically known is achieved by annotating only vector elements with a Rep type²:

```
def dot[T:Numeric]
  (v1: Vector[Rep[T]], v2: Vector[Rep[T]]): Rep[T]
```

Here the Rep annotations on Rep[T] denote that elements of vectors will be known only in the next stage (in LMS, this is a stage after run-time compilation). After run-time compilation zip, foldLeft, and pattern matching inside the closure will not exist in the *residual* program as they were evaluated in the previous stage of compilation (host language runtime). Note that in LMS unannotated code is always executed during host-language runtime and type-annotated code is executed after run-time compilation.

Stage monovariance. The dot function in LMS is monovariant: it can only accept vectors that are statically known but their elements are dynamic. In order to support both versions the author of dot would have the body of dot with slightly different stage annotations:

```
def dot[T:Numeric](v1: Vector[T], v2: Vector[T]): T
```

Designers of *binding-time analysis* for offline partial-evaluators had the same difficulties with monovariance. First solutions duplicate code [?] to achieve polyvariance. Duplication is much less

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troublesome with partial evaluation as users do not write the duplicate code. Henglein and Mossin introduce polymorphic binding-time analysis [?] to avoid code duplication, which was further refined to parametric polymorphism [?], and recursion and subtyping [?]. Although effective, these approaches are not used for staging but for offline partial evaluation. Finally, Ofenbeck et al. [?] propose a solution to this problem based on type classes and higher-kinded types. Their solution requires additional annotations and implicit parameters in the type signature of polyvariant methods.

Code Duplication. Staging systems based on type annotations (e.g., LMS and type-directed partial evaluation [?]) inherently require code duplication as, a priory, no operations are defined on Rep annotated types. For example, in the LMS version of the dot function, all numeric types (i.e., Rep[Int], Rep[Double], etc.) must be re-implemented in order to typecheck the programs and achieve code generation for the next stage.

Sujeeth et al. [?] and Jovanovic et al. [?] propose generating code for the next stage computations based on a language specification. These approaches solve the problem, but they require writing additional specification for the libraries, require a large machinery for code generation, and support only restricted parts of Scala.

Staging at host language compile time. How can we use type based staging for programs whose values are statically known at the host language compile-time (the first stage)? Existing staging frameworks treat unannotated terms as runtime values of the host language and annotated terms as values in later stages of compilation. Even if we would take that the first stage is executed at the host language compile time, we would have to annotate all run-time values. Annotating all values is cumbersome since host language run-time values comprise the majority of user programs (§??).

MacroML [?] expresses macros as two-stage computations that start executing from host language compile time. In MacroML, parameters of macros can be annotated as an early stage computation. These parameters can then used in escaped terms for compile-time computation. Terms scheduled for runtime execution, withing the escaped terms, again need to be quoted with brackets. This, in effect, imposes quotation for both escaping and brackets which requiring additional effort.

Polymorphic binding-time information. The main idea of this paper is to use polymorphic binding-time analysis: *i)* to enable stage polivariant code through bounded parametric polymorphism, and *ii)* to allow reusing existing data types in different stages of computation without code duplication.

With bounded parametric polymorphism we can make functions stage polyvariant in their arguments by replacing them with type parameters upperbounded by their original type. For example, polymorphic power function is defined as:

```
@ct def pow[V <: Long](base: Long, exp: V): Long</pre>
```

Annotated types denote terms whose instances and non-polymorphic fields are known, and whose methods can be executed at in the previous stage (i.e., compile time). We call annotated types compiletime views of existing data types. Types are promoted to their compile-time views with type qualifiers [?] expressed with the @ct annotation (e.g., Int@ct). In terms, statically known terms can be promoted their compile time duals with the function ct. By having two views of the same type we obviate the need for introducing reification and code generation logic for existing types.

```
package object scalact {
   final class ct extends StaticAnnotation

def ct[T](body: => T): T = ???
}
```

Figure 1. Interface of ScalaCT.

With compile-time views, to require that vectors v1 and v2 are static and to partially evaluate the function, a programmer needs to make a simple modification of the dot signature:

```
def dot[V: Numeric@ct]
  (v1: Vector[V]@ct, v2: Vector[V]@ct): V
```

Since, vector elements are stage polymorphic the result of the function can be a dynamic value, or a compile-time view that can be further used for compile-time computations. The binding time of the return type of dot will match the binding time of vector elements:

```
// [el1, el2, el3, el4] are dynamic decimals dot(Vector(el1, el2), Vector(el3, el4)) \hookrightarrow (\text{el1} * \text{el3} + \text{el2} * \text{el4}) \colon \text{Double} // ct promotes static terms to compile-time views dot(Vector(ct(2), ct(4)), Vector(ct(1), ct(10))) \hookrightarrow 42 \colon \text{Double@ct}
```

In this paper we contribute to the state of the art:

- By using bounded parametric polymorphism as a vehicle to succinctly achieve polyvariant staging. This allows writing polyvariant stage programs without code duplication or additional language features. Stage annotations passed through type parameters are used by underlying polymorphic binding-time analysis to determine the correct binding-times.
- By obviating the need for reification and code generation logic in type based staging systems. The same binding-time analysis is to allow types defined in monovariant way to be used in multiple stages.
- By introducing compile-time views (§??) as means to achieve type safe type based two-stage programming starting from host language compile time.
- By demonstrating the usefulness of compile-time views in four case studies (§??): inlining, partially evaluating recursion, removing overheads of variable argument functions, and removing overheads of type-classes [???].

We have implemented a staging extension for Scala ScalaCT. ScalaCT has a minimal interface (§??) based on type annotations. We have evaluated performance gains and the validity of ScalaCT on all case studies (§??) and compared them to LMS. In all benchmarks (§??) our evaluator performs the same as LMS and gives significant performance gains compared to original programs.

2. ScalaCT Interface

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In this section we present ScalaCT, a staging extension for Scala based polymorphic binding-time analysis. ScalaCT is a compiler plugin that executes in a phase after the Scala type checker. The plugin takes as input typechecked Scala programs and uses type annotations [?] to track and verify information about the biding-time of terms. It supports only two stages of compilation: host language compile-time (types annotated with @ct) and host language run-time (unannotated code).

To the user, ScalaCT exposes a minimal interface (Figure ??) with a single annotation ct and a single function ct.

¹ All code examples are written in *Scala*. It is necessary to know the basics of Scala to comprehend this paper.

² In this work we use LMS as a representative of type-based staging systems

Annotation ct is used on types (e.g., Int@ct) to promote them to their compile-time views. The annotation is integrated in the Scala's type system and, therefore, can be arbitrarily nested in different variants of types.

Since operations on compile-time views should be executed at compile time, the ct type can be viewed as the original type whose instance is known at compile time with additional methods whose non-generic method parameters and result types also become compile-time views (if possible). Generic parameters remain unchanged as their binding time is defined during corresponding type application. Table ?? shows how the <code>@ct</code> annotation can be placed on types and how it affects method signatures of additional methods. Note that methods are not in fact added to the type but the binding-time polymorphic behavior of original methods can be observed as additional methods.

In Table ??, on Int@ct both parameters and result types of all methods are also compile-time views. On the other hand, Vector[Int]@ct has parameters of all methods transformed except the generic ones. In effect, this, makes higher order combinators of Vector operate on dynamic values, thus, function f passed to map accepts the dynamic value as input. Note that hashCode of Vector[Int]@ct returns a dynamic value—this is due to its implementation that internally operates on generic values that are dynamic. Type Vector[Int@ct]@ct has all additional methods promoted to compile-time. The return type of the function map on Vector[Int@ct]@ct can still be either dynamic or a compile-time view due to the type parameter U.

Annotation ct can also be used to achieve inlining of statically known methods and functions. This is achieved by putting the annotation of the method/function¹ definition:

```
@ct def dot[T: Numeric]
  (v1: Vector[T], v2: Vector[T]): T
```

Annotated methods will have an annotated method type

```
((v1: Vector[T], v2: Vector[T]) => T)@ct
```

which can not be written by the users.

Function ct is used at the term level for promoting literals, modules, and methods/functions into their compile-time views. Table ?? shows how different types of terms are promoted to their compile-time views. An exception for promoting terms to compile-time views is the new construct. Here we use the type annotation on the constructed type.

2.1 Well-Formedness of Compile-Time Views

Earlier stages of computation can not depend on values from later stages. This property—defined as *cross-stage persistence* [??]—imposes that all operations on compile-time views must be known at compile time.

To satisfy cross-stage persistence ScalaCT verifies that binding time of composite types (e.g., polymorphic types, function types, record types, etc.) is always a subtype of the binding time of their components. In the following example, we show malformed types and examples of terms that are inconsistent:

```
xs: List[Int@ct] => ct(Predef).println(xs.head)
fn: (Int@ct=>Int@ct) => ct(Predef).println(fn(ct(1)))
```

In the first example the program would, according to the semantics of @ct, print a head of the list at compile time. However, the head of the list is known only in the runtime stage. In the second example the program should print the result of fn at compile time

but the body of the function will be known only at runtime. By causality such examples are not possible.

On functions/methods the ct annotation requires that function/method bodies are known at compile-time. Otherwise, inlining of such functions/methods would not be possible at compile-time. In Scala, method bodies are statically known in objects and classes with final methods, thus, the ct annotation is only applicable on such methods.

2.2 Minimizing the Number of Annotations

One of the design goals of ScalaCT is to minimize the number of superfluous staging annotations. We achieve this by implicitly adding annotations and term promotions that would with high probability be added by the user.

Adding ct to Functions. Due to cross-stage persistence if a single parameter of a function is annotated with ct the whole function must also be ct. Since forgetting this annotation would only result in an error we implicitly add the ct annotation when at least one parameter type or the result type is marked as ct.

Implicit Conversions. If method parameters require the compiletime view of a type the corresponding arguments in method application would always have to be promoted to ct. In some libraries this could require an inconveniently large number of annotations.

To minimize the number of required annotations we introduce *implicit conversions* from certain static terms to ct terms. Note that we use a custom mechanism for implicit conversions based on type annotations. This is necessary as Scala implicit conversions are oblivious to type annotations (§??).

The conversions support translation of language literals, direct class constructor calls with static arguments, and static method calls with static arguments into their compile-time views. Since our compile-time evaluator does not use Asai's [??] method to keep track of the value of each static term, we disallow implicit conversions of terms with static variables.

For example, for a factorial function

```
def fact(n: Int@ct): Int@ct =
  if (n == 0) 1 else fact(n - 1)
```

we will not require promotions of literals 0, and 1. Furthermore, the function can be invoked without promoting the argument into it's compile-time view:

```
fact(5)
\hookrightarrow 120
```

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Without implicit conversions the factorial functions would be more verbose

```
else fact(n - ct(1))
```

as well as each function application (fact(ct(5))).

Implicit conversions are safe in all cases except when the user should be warned about potential code explosion. For example, a user could accidentally call fact with a very large number and cause code explosion without even knowing that staging is happening. If ct was required it would remind the users about the potential problems. In the design of ScalaCT we decided to prefer less annotations over code-explosion prevention.

3. Polymorphic Binding-Time Analysis

Scala is an object oriented language with numerous features and separate compilation. To avoid a mismatch between the formalization and Scala we describe binding-time analysis on the minimal subset of Scala that gives insights in the actual implementation.

 $^{^{1}}$ This is not the first time that inlining is achieved through partial evaluation [?].

Annotated Type
Annotated Type
Int@ct
Vector[Int]@ct
Vector[Int@ct]
Type's Method Signatures
+(rhs: Int@ct): Int@ct
map[U](f: (Int => U)@ct): Vector[U]@ct
length: Int@ct
hashCode: Int
Vector[Int@ct]@ct
map[U](f: (Int@ct => U)@ct): Vector[U]@ct
length: Int@ct
hashCode: Int
Quadratic Int@ct
length: Int@ct
get(key: Int@ct): Option[Int]@ct

 Table 2. Promotion of terms to their compile-time views.

 Term's Type

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Terms:

Promoted Term

$$\begin{split} t &::= t \ t \mid \lambda x : \tau.t \mid x[\overline{\tau}] \mid x \mid ct \ v \\ v &::= \lambda x : \tau.t \mid c \\ c &::= \mathbf{true} \mid \mathbf{false} \mid 0 \mid 1 \mid \dots \end{split}$$

Types:

$$\begin{split} b &::= \beta \mid rt \mid ct \\ \gamma &::= \forall \overline{\beta} \Rightarrow C.\gamma \mid \sigma' \\ \sigma' &::= \tau \mid \sigma \mid \gamma \langle \overline{b} \rangle \\ \sigma &::= \forall \overline{X^b}.\tau \\ \tau &::= X^b \mid \tau \to^b \tau \mid \sigma[\overline{\tau}] \mid \iota \\ \iota &::= \mathbf{Bool}^b \mid \mathbf{Int}^b \end{split}$$

Well formed types:

$$\frac{\operatorname{wff}(\sigma)|b \quad \operatorname{wff}(\overline{\tau})|\overline{\tau} <: b}{\operatorname{wff}\sigma[\overline{\tau}]|b}$$

$$\frac{\operatorname{wff}(\tau_1)|b_1 \quad \operatorname{wff}(\tau_2)|b_2 \quad b_1 <: b_3 \quad b_2 <: b_3}{\operatorname{wff}(\tau_1) \rightarrow^{b_3} \tau_2)|b_3}$$

$$\frac{\operatorname{wff}(\sigma)|b \quad \operatorname{wff}(\overline{\tau})|\overline{\tau} <: b}{\operatorname{wff}\sigma[\overline{\tau}]|b}$$

$$\operatorname{wff}(X^b)|b$$

$$\operatorname{wff}(Bool^b)|b$$

$$\operatorname{wff}(Int^b)|b$$

Figure 2. Well formed types wff iT

Coaercions:

Subtyping relation:

Deviate from regular underline/overline Context:

Constructors: Methods:

Translation to polymorphic calculus:

generic translations rules

To achieve polyvariant staging we augment Scala with bindingtime annotations. There are two concrete binding time annotations rt and ct (often named D and S in related work). Annotations rtand ct represent run-time binding time and compile time binding time respectively. To achieve binding-time polymorphism we also introduce binding time variables \boldsymbol{b} .

Binding times form a two-point lattice with the ordering operator <:. TODO Binding time variables are introduced with binding time abstraction $\forall \overline{\beta}$ where $\overline{\beta}$ stands for a set of variables. Free binding time variables are tracked in a context B.

To achieve polyvariant staging and cross stage persistence we introduce a set C of constraints on binding time variables. The set C contains assumptions on binding-time variables defined as $B, C \vdash \beta <: b$ where all free variables are in context B. Finally, a polyvariant term is defined as:

$$B, C \vdash \forall \overline{\beta} \Rightarrow \{\overline{\beta_i <: b}\}. t$$

The corresponding application of polymorphic terms is defines as

$$t < \overline{b} >$$

Types. To preserve clarity we will look only at a subset of Scala types that includes functions, rank-1 parametric polymorphism, and base types:

We distinguish our selves from the others by keeping rank-1 and by annotating type parameters separately Mention that for every type variable we have a corresponding binding time variable. Well formedness. For each type we want to assure two things: i) cross-stage persistence, ii) that for each type variable we have a corresponding binding time variable. We assure the cross stage persistence

$$Ccontains wff(\sigma)$$

$$wff(\tau \to \tau) = \cup \cup$$

$$wff(\tau[\tau]) = \cup \cup$$

$$wff(\forall \alpha[\tau]) = \cup \cup$$

- 3.1 Nominal Types and Subtyping
- 3.2 Compile-Time Evaluation
- 3.3 Mutable State

4. Case Studies

In this section we present selected use-cases for compile-time views that, at the same time, demonstrate step-by-step the mechanics behind ScalaCT. We start by inlining a simple function with staging (§??), then do the canonical staging example of the integer power function (§??), then we demonstrate how variable argument functions can be desugared into the core functionality (§??). Finally, we demonstrate how the abstraction overhead of the dot function and all associated type-class related abstraction an be removed (§??).

4.1 Inlining Expressed Through Staging

Function inlining can be expressed as staged computation [?]. Inlining is achieved when a statically known function body is applied with symbolic arguments. In ScalaCT we use the ct annotation on functions and methods to achieve inlining:

4.2 Recursion

The canonical example in staging literature is partial evaluation of the power function where exponent is an integer:

```
def pow(base: Double, exp: Int): Double =
  if (exp == 0) 1 else base * pow(base, exp - 1)
```

When the exponent (exp) is statically known this function can be partially evaluated into exp multiplications of the base argument, significantly improving performance [?].

With compile-time views making pow partially evaluated requires adding only one annotation:

```
def pow(base: Double, exp: Int@ct): Double =
  if (exp == 0) 1 else base * pow(base, exp - 1)
```

To satisfy cross-stage persistence (§??) the pow must be @ct. This annotation is automatically added by ScalaCT as described in §??. In the example, the ct annotation on exp requires that the function must be called with a compile-time view of Int. ScalaCT ensures that the definition of the pow function does not cause infinite recursion at compile-time by invoking the power function only when the value of the ct arguments is known.

The application of the function pow with a constant exponent produces:

```
pow(base, 4) \hookrightarrow base * base * base * 1
```

Constant 4 is promoted to ct by the implicit conversions (§??).

4.3 Variable Argument Functions

Variable argument functions appear in widely used languages like Java, C#, and Scala. Such arguments are typically passed in the function body inside of the data structure (e.g. Seq[T] in Scala). When applied with variable arguments the size of the data-structure is statically known and all operations on them can be partially evaluated. However, sometimes, the function is called with arguments of dynamic size. For example, function min that accepts multiple integers

```
def min(vs: Int*): Int = vs.tail.foldLeft(vs.head) {
```

```
def min(vs: Int*): Int = macro
  if (isVarargs(vs)) q"min_CT(vs)"
  else q"min_D(vs)"

def min_CT(vs: Seq[Int]@ct): Int =
    vs.tail.foldLeft(vs.head) { (min, el) =>
      if (el < min) el else min
  }

def min_D(vs: Seq[Int]): Int =
  vs.tail.foldLeft(vs.head) {
    (min, el) => if (el < min) el else min
  }</pre>
```

Figure 3. Function min is desugared into a min macro that based on the binding time of the arguments dispatches to the partially evaluated version (min_CT) for statically known varargs or to the original min function for dynamic arguments min_D.

```
(min, el) => if (el < min) el else min
```

can be called either with statically known arguments (e.g., min(1,2)) or with dynamic arguments:

```
val values: Seq[Int] = ... // dynamic value
min(values: _*)
```

Ideally, we would be able to achieve partial evaluation if the arguments are of statically known size and avoid partial evaluation in case of dynamic arguments. To this end we translate the method min into a partially evaluated version and a dynamic version. The call to these methods is dispatched, at compile-time, by the min method which checks if arguments are statically known. Desugaring of min is shown in Figure ??.

4.4 Removing Abstraction Overhead of Type-Classes

Type-classes are omnipresent in everyday programming as they allow abstraction over generic parameters (e.g., Numeric abstracts over numeric values). Unfortunately, type-classes introduce *dynamic dispatch* on every call [?] and, thus, impose a performance penalty. Type-classes are in most of the cases statically known. Here we show how with ScalaCT we can remove all abstraction overheads of type classes.

In Scala, type classes are implemented with objects and implicit parameters [?]. In Figure ??, we define a trait Numeric serves as an interface for all numeric types. Then we define a concrete implementation of Numeric for type Double (DoubleNumeric). The DoubleNumeric is than passed as an implicit argument dnum to all methods that use it (e.g., zero).

When zero is applied first the implicit argument (dnum) gets inlined due to the ct annotation of the return type, then the function zero gets inlined. Since dnum returns a compile-time view of DoubleNumerc the method zero on dnum is evaluated at compile time. The constant 0.0 is promoted to ct since DoubleNumeric is a compile time view. Finally the ct (0.0) result is coerced to a dynamic value by the signature of Numeric.zero. The compile-time execution is shown in the following snippet

```
\begin{array}{lll} & \texttt{Numeric.zero} \, [\texttt{Double}] \\ & \hookrightarrow \, \texttt{Numeric.zero} \, [\texttt{Double}] \, (\texttt{DoubleNumeric}) \\ & \hookrightarrow \, \mathsf{ct} \, (\texttt{DoubleNumeric}) \, . \mathsf{zero} \\ & \hookrightarrow \, (\mathsf{ct} \, (0.0) \colon \, \mathsf{Double}) \\ & \hookrightarrow \, 0.0 \end{array}
```

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```
object Numeric {
   implicit def dnum: Numeric[Double]@ct =
      ct(DoubleNumeric)
   def zero[T](implicit num: Numeric[T]@ct): T =
      num.zero
}

trait Numeric[T] {
   def plus(x: T, y: T): T
   def times(x: T, y: T): T
   def zero: T
}

object DoubleNumeric extends Numeric[Double] {
   def plus(x: Double, y: Double): Double = x + y
   def times(x: Double, y: Double): Double = x * y
   def zero: Double = 0.0
}
```

Figure 4. Removing abstraction overheads of type classes.

4.5 Inner Product of Vectors

Here we demonstrate how the introductory example (§??) is partially evaluated through staging. We start with the desugared dot function (i.e., all implicit operations are shown):

```
def dot[V](v1: Vector[V]@ct, v2: Vector[V]@ct)
  (implicit num: Numeric[V]@ct): V =
   (v1 zip v2).foldLeft(zero[V](num)) {
    case (prod, (cl, cr)) => prod + cl * cr
}
```

Function dot is generic in the type of vector elements. This will reflect upon the staging annotations as well (ct and static). When we apply the dot function with static arguments we will get the vector with static elements back:

When dot is evaluated with the ct elements the last step will further execute to a single compile-time value that can further be used in compile-time computations:

5. Discussion

To distinguish terms executed at compile-time from terms executed at runtime with type annotations we have the following possibilities:

- Annotate types of all terms that should be executed at runtime.
 Here all types analyzed LMS and realized that this is not an
 option.
- 2. Annotate types of terms that should be executed at runtime but introduce scopes (e.g., method bodies) for which this rule applies. In this way we would avoid annotating types of all runtime terms. This approach is taken by MacroML where macro functions are executed at compile time and quoted terms

are executed at runtime. First approach is, also, a special case of this approach where there is a single scope for the whole language.

Annotate types of terms that are executed at compile time. This approach is used with ScalaCT and annotated types are called compile-time views.

To compare approach of ScalaCT with the first approach we analyzed 817 functions from the OptiML [?] DSL based on LMS. With the ScalaCT scheme OptiML would require more than 2x less annotations to implement.

Compared to the second approach our solution is simpler to comprehend and communicate. In the second approach there are two things that users need to understand when reasoning about staged programs: *i*) where does the compile time scope start, and *ii*) which terms are annotated. With ScalaCT the comprehension is simple: terms whose types are annotated with ct are executed at compile time.

It is also interesting to the second and third approaches. Here the number of annotations depends on the program. If the programs are mostly partially evaluated the second approach is better. These category of programs could also be regarded as code generators as most of the code is executed at compile time and produces large outputs. When programs are comprised of mostly runtime values the approach of ScalaCT requires less annotations.

6. Evaluation

In this section we evaluate the amount of code that is obviated with ScalaCT compared to existing type directed staging systems (§??). Then we evaluate performance of ScalaCT compared to LMS and hand optimized code (§??)

6.1 Reduction in Code Duplication

Evaluating reduction of duplicated code (for reification and code generation) in type based staging systems is difficult as the factor varies from program to program. To avoid benchmark dependent results we instead calculate the lower bound on the duplication factor

Given that we have a method on a type T whose body contains n lines of code (without the method definition). To introduce the same method on an annotated type Rep [T] we need another method for reification which has at least 1 line of code. Then we need code generation logic, which, if we use the same language should not have less lines than the original method plus at least one line for matching the reified method. For method of n lines we get a lower bound on the code duplication factor of:

$$2n + 3/n + 1$$

For single line methods (n=0) the factor is 3 and for large methods $(n\to\infty)$ it converges to 2.

6.2 Performance of Generated Code

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In this section we compare performance of ScalaCT with LMS and original code. All benchmarks are executed on an Intel Core i7 processor (4960HQ) working frequency of 2.6 GHZ with 16GB of DDR3 with a working frequency of 1600 MHz. For all benchmarks we use Scala 2.11.5 and the HotSpot(TM) 64-Bit Server (24.51-b03) virtual machine. In all benchmarks the virtual machine is warmed up, no garbage collection happens, and all reported numbers are a mean of 5 measurements.

In Table ?? we show execution time normalized to original code for: i) pow(42.0, 10), ii) min(a, b, c, d, e), iii) inner product of two statically known vectors of size 50, and iv) the butterfly network of size 4 for fast Fourier transform fft

(equivalent to code presented by Rompf and Odersky [?]). For all benchmarks the performance results are equivalent to LMS.

Table 3. Speedup of LMS and ScalaCT compared to the naive implementation of the algorithms.

Benchmark	LMS	ScalaCT
pow	221.75	221.70
min	1.82	1.79
dot	246.08	246.08
fft	12.14	12.88

7. Limitations

Type Annotations. Using type annotations for annotating the compilation stage is not ideal. Type annotations are not fully integrated into the Scala language. Major drawbacks are that overloading resolution and implicit search are oblivious about annotations. For example, if two methods have the same signatures but different staging annotations the compiler will report an error. Implicit search will fail in two ways: *i*) if two implicit functions with the same type are in scope but annotations differ the compiler will report an error about ambiguous implicits and *ii*) if a method requires an implicit parameter with the ct annotation the compiler might provide an implicit argument without the annotation. These are not fundamental limitations and, in practice, stage polyvariance can be used to avoid difficulties with annotations.

Type Annotation Position. Annotations in Scala can be used in many different positions and ScalaCT supports only some of them. Annotation ct can not be used in following positions: *i)* on classes, traits, and modules, *ii)* in the list of inherited classes and traits, *iii)* on the right hand side of the type variable definitions, and *iv)* on all terms outside the method definitions (constructors, constructor arguments, etc.).

Access Modifiers. Scala supports access modifiers of members. If methods that use ScalaCT internally access private members of the class ScalaCT will fail as all staged methods are inlined at the call site. Similar limitations exist with inlining functions in Scala. This problem could be circumvented inside Scala, however, the JVM will not allow this in the bytecode verification phase.

Code Explosion. Annotation ct inlines all functions that are annotated and unrolls all loops on compile-time executed data structures. This can, for a staged function, lead to unnaceptable code explosion for some inputs while the code can behave regularly for other inputs. For example, calling pow (0.5, 10000000) on the function from §?? will make unacceptably large code while pow (0.5, 10) will work as expected.

7.1 Nominal Typing, Lower Bounds, and Higher-Kinded Types

8. Related Work

MetaOCaml [??] is a staging extension for OCaml. It uses quotation to determine the stage in which the term is executed. Types of quoted terms are annotated to assure cross-stage persistence. Staging in MetaOCaml starts at host language runtime and can not express compile-time computations. Further, operations on annotated types do not get automatically promoted to the adequate stage of computation as with compile-time views. Finally, there are no implicit conversions so all stage promotions of terms must be explicit.

MacroML [?] is a language that translates macros into MetaML staging executed at compile time to provide a "clean" solution for macros. In MacroML, within the let mac construct function parameters can be annotated as an early stage computation. These parameters can then be used in escaped terms, i.e., terms scheduled

to execute at compile time. Unlike ScalaCT, MacroML uses escapes and early parameters to mark terms scheduled for to execute at compile time. Within escapes terms scheduled for runtime again need to be marked with brackets. This kind of dual annotations are not required as compile-time views are automatically promoted to runtime terms.

In LMS [?] terms that are annotated with Rep types will be executed at the stage after runtime compilation. Therefore, LMS can not directly be used for compile time computation. Furthermore, LMS requires additional reification logic and code generation for all Rep types.

Programming language Idris [?] introduces the static annotation on function parameters to achieve partial evaluation. Annotation static denotes that the term is statically known and that all operations on that term should be executed at compile-time. However, since static is placed on terms rather then types, it can mark only whole terms as static. This restricts the number of programs that can be expressed, e.g., we could not express that vectors in the signature of dot are static only in size. Finally, information about static terms can not be propagated through return types of functions so static in Idris is a partial evaluation construct, i.e., it hints that partial evaluation should be applied if function arguments are static.

Hybrid Partial Evaluation (HPE) [?] is a technique for partial evaluation that does not perform binding time analysis (similarly to online partial evaluators) but relies on the user provided annotation CT². HPE implementations exist for both Java and Scala [?]. Although, CT is used for partial evaluation, it does not affect typing of user programs. Furthermore, behavior of CT in context of generics is not described. ScalaCT can be seen as statically typed version of hybrid partial evaluation with support for parametric polymorphism. Due to the support for parametric polymorphism ScalaCT can express compile-time data structures with dynamic data.

Forge [?], by Sujeeth et al., uses a DSL to declare a specification of the libraries. Forge then generates both unannotated and annotated code based on the specification. Their language also supports generating staged code (comprised of terms different from multiple stages). Forge specification and code generation supports only a subset of Scala guided towards the Delite [??] framework.

The Yin-Yang framework, by Jovanovic et al. [?], solves the problem of code duplication by generating reification and code generation logic based on Scala code of existing types. With their approach there is no code duplication for the supported language features. However, not all of the Scala language is supported and all generated terms are generated for the next stage, thus, making a stage distinction is impossible.

9. Conclusion

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ScalaCT is only the first step towards a staging system for Scala that is fully integrated in the language. For complete integration it would be necessary to allow usage of ct on trait and class definitions as well as abstract types.

In ScalaCT annotation of a term determins the stage where it is computed. When ScalaCT is used only for partial evaluation this can lead to unnecessary code duplication as users need to provide two versions of the same code (one staged and one unstaged). For a practical system it is necessary to extend ScalaCT with annotations which denote that terms should be partially evaluated if they are statically known. We have achieved this for variable argument funcitons in §?? with an ad-hoc mechanism, however, we seek for a principled solution.

² Name ct in ScalaCT is inspired by hybrid partial evaluation.