Package 'MultiObjMatch'

July 5, 2024

Type Package
Title Multi-Objective Matching Algorithm
Version 1.0.0
Description Matching algorithm based on network-flow structure. Users are able to modify the emphasis on three different optimization goals: two different distance measures and the number of treated units left unmatched. The method is proposed by Pimentel and Kelz (2019) <doi:10.1080 01621459.2020.1720693="">. The 'rrelaxiv' package, which provides an alternative solver for the underlying network flow problems, carries an academic license and is not available on CRAN, but may be downloaded from Github at <https: github.com="" josherrickson="" rrelaxiv=""></https:>.</doi:10.1080>
License MIT + file LICENSE
Encoding UTF-8
Imports cobalt, dplyr, optmatch, matchMulti, fields, plyr, RCurl, gtools, rcbalance, MASS, stats, methods, ggplot2, utils, rlang, rlemon
RoxygenNote 7.1.2
Suggests testthat (>= 3.0.0), rrelaxiv
Config/testthat/edition 3
NeedsCompilation no
Author Shichao Han [cre, aut], Samuel D. Pimentel [aut]
Maintainer Shichao Han <schan21@berkeley.edu></schan21@berkeley.edu>
Repository CRAN
Date/Publication 2024-07-04 23:10:05 UTC
Contents
addBalance

3

2 Contents

ddExclusion	3
alanceCosts	
uild.dist.struct	. 4
uild.dist.struct_user	. 5
allrelax	. 6
heck_representative	. 6
ombine_dist	. 7
ombine_match_result	
ompare_matching	
ompare_tables	
onvert_index	
onvert names	
ostSkeleton	
ata_precheck	
escr.stats_general	
istanceFunctionHelper	
ist_bal_match	
ummy	
dgelist2ISM	
xcludeCosts	
xtractEdges	
xtractSupply	
lter_match_result	
attenSkeleton	
enerateRhoObj	
enerate_rhos	
etExactOn	
etPropensityScore	
et_balance_table	
et_five_index	
et_pairdist_balance_graph	
et_pairdist_graph	. 25
et_rho_obj	. 26
et_tv_graph	. 26
et_unmatched	. 27
nakeInfinitySparseMatrix	. 28
nakeSparse	. 29
natched_data	. 29
natched_index	. 30
natrix2cost	
natrix2edgelist	. 31
neldMask	
etFlowMatch	
bj.to.match	
airCosts	
no_proposition	
olveP	
olveP1	. 34
U11V1 1	

addBalance 3

lanca	Λd	1 fi	20	ha	lai	nco	200	daz	20																				
two_dist_match .																													. 36
summary.multiObi	Match	١.																											. 35
	two_dist_match . visualize	two_dist_match visualize	two_dist_match visualize	two_dist_match visualize	two_dist_match	summary.multiObjMatch																							

Description

Add fine balance edges

Usage

```
addBalance(net, treatedVals, controlVals, replaceExisting = TRUE)
```

Arguments

net the network object created for the network flow problem

treatedVals the balance value for treated nodes controlVals the balance value for control nodes

replaceExisting

(optional) whether or not to replace the existing net; TRUE by default

Value

the network structure with balance edges added

addExclusion Add exclusion edges

Description

Add exclusion edges

Usage

```
addExclusion(net, remove = FALSE)
```

Arguments

net the input network structure

remove (optional) whether to exclude edges; FALSE by default

Value

the network structure with exclusion edges added to allow for trdeoff for the exclusion cost

4 build.dist.struct

balanceCosts

Create a skeleton representation of the balance edge costs

Description

Create a skeleton representation of the balance edge costs associated with pairings for a given distance and network

Usage

```
balanceCosts(net, balance.penalty = 1)
```

Arguments

```
net the network structure
balance.penalty

(optional) the numeric value for balance; 1 by default
```

Value

the skeleton with balance edge cost

build.dist.struct

An internal helper function that generates the data abstraction for the edge weights of the main network structure.

Description

An internal helper function that generates the data abstraction for the edge weights of the main network structure.

Usage

```
build.dist.struct(
    z,
    X,
    distMat,
    exact = NULL,
    dist.type = "Mahalanobis",
    calip.option = "propensity",
    calip.cov = NULL,
    caliper = 0.2,
    verbose = FALSE
)
```

build.dist.struct_user 5

Arguments

distMat

a vector of treatment and control indicators, 1 for treatment and 0 for control.
 a data frame or a numeric or logical matrix containing covariate information for treated and control units. Its row count must be equal to the length of z.

a matrix of pair-wise distance specified by the user

exact an optional vector of the same length as z. If this argument is specified, treated

units will only be allowed to match to control units that have equal values in the corresponding indices of the exact vector. For example, to match patients within hospitals only, one could set exact equal to a vector of hospital IDs for

each patient.

dist.type one of ('propensity', 'user', 'none'). If 'propensity' is specified (the default op-

tion), the function estimates a propensity score via logistic regression of z on X and imposes a propensity score caliper. If 'user' is specified, the user must provide a vector of values on which a caliper will be enforced using the calip.cov

argument. If 'none' is specified no caliper is used.

calip.option a character indicating the type of caliper used

calip.cov see calip.option.

caliper a numeric value that gives the size of the caliper when the user specifies the

calip.option argument as 'propensity' or 'calip.cov'.

verbose a boolean value whether to print(cat) debug information. Default: FALSE

Value

a distance structure used for constructing the main network flow problem

build.dist.struct_user

An internal helper function that generates the data abstraction for the edge weights of the main network structure using the distance matrix passed by the user.

Description

An internal helper function that generates the data abstraction for the edge weights of the main network structure using the distance matrix passed by the user.

Usage

```
build.dist.struct_user(z, distMat, verbose = FALSE)
```

Arguments

z a vector indicating whether each unit is in treatment or control group

distMat a matrix of pair-wise distance

verbose a boolean value whether to print(cat) debug information. Default: FALSE

6 check_representative

Value

a distance structure used for constructing the main network flow problem

callrelax

Call relax on the network

Description

this function is copied from the rebalance package

Usage

```
callrelax(net, solver = "rlemon")
```

Arguments

net the network structure

solver (optional) the solver; by default, "rlemon"

Value

list of the result from the call to relax solver

check_representative Check the representativeness of matched treated units

Description

Summary function to compare SMD of the key covariates in matched and the full set of treated units.

Usage

```
check_representative(matching_result, match_num = NULL)
```

Arguments

matching_result

the matching result returned by either dist_bal_match or two_dist_match.

match_num

(optional) Integer index of match that the user want to extract paired observations from. NULL by default, which will generate a table for all the matches.

Value

a summary table of SMDs of the key covariates between the whole treated units and the matched treated units.

combine_dist 7

 $combine_dist$

An internal helper function that combines two distance object

Description

An internal helper function that combines two distance object

Usage

```
combine_dist(a, b)
```

Arguments

a a distance structure objectb a distance structure object

Value

a new distance structure object whose edge weights are the sum of the corresponding edge weights in a and b

combine_match_result

Combine two matching result

Description

Combine two matching result

Usage

```
combine_match_result(matching_result1, matching_result2)
```

Arguments

```
matching_result1
the first matching result object.
matching_result2
the second matching result object.
```

Value

a new matching result combining two objects. Note that the matching index for the second matching is the original name plus the maximum match index in the first matching object.

8 compare_matching

compare_matching

Generate covariate balance in different matches

Description

This is a wrapper function for use in evaluating covariate balance across different matches. It only works for 'Basic' version of matching (using dist_bal_match).

Usage

```
compare_matching(
  matching_result,
  cov_list = NULL,
  display_all = TRUE,
  stat = "mean.diff"
)
```

Arguments

matching_result

an object returned by the main matching function dist_bal_match

cov_list (optional) factor of names of covariates that we want to evaluate covariate bal-

ance on; default is NULL. When set to NULL, the program will compare the

covariates that have been used to construct a propensity model.

display_all (optional) boolean value of whether to display all the matches; default is TRUE,

where matches at each quantile is displayed

stat (optional) character of the name of the statistic used for measuring covariate

balance; default is "mean.diff". This argument is the same as used in "cobalt"

package, see: bal.tab

Value

a dataframe that shows covariate balance in different matches

Examples

```
## Generate matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")
treat_val <- "treat"
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")
my_bal_val <- c("race")
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val,
marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s,</pre>
```

compare_tables 9

```
dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)

## Generate table for comparing matches
compare_matching(match_result, display_all = TRUE)
```

compare_tables

Summarize covariate balance table

Description

This function would take the result of get_balance_table function and combine the results in a single table. It only works for 'Basic' version of the matching.

Usage

```
compare_tables(balance_table)
```

Arguments

balance_table a named list, which is the result from the function get_balance_table

Value

a dataframe with combined information

Examples

```
## Generate matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")
treat_val <- "treat"
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")
my_bal_val <- c("race")
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val, marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s, dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)
## Generate summary table for comparing matches
compare_tables(get_balance_table(match_result))</pre>
```

10 convert_names

convert_index	An internal helper function that translates the matching index in the sorted data frame to the original dataframe's row index

Description

An internal helper function that translates the matching index in the sorted data frame to the original dataframe's row index

Usage

```
convert_index(matching_result)
```

Arguments

```
matching_result
```

an object returned by the main matching function dist_bal_match

convert_names	Internal helper function that converts axis name to internal variable
	name

Description

Internal helper function that converts axis name to internal variable name

Usage

```
convert_names(x, y, z = NULL)
```

Arguments

Χ	the user input character for x-axis value
У	the user input character for y-axis value
Z	the user input character for z-axis value

Value

a named list with variable names for visualization for internal use

costSkeleton 11

costSkeleton

Create cost skeleton

Description

Create a more user-friendly data structure to represent the edge costs in a network. Internally the network object used by the optmiization routine represents all the edge costs in a single vector. The "skeleton" structure decomposes this vector into a list of components, each corresponding to a different role in the network: "pairings" are edges between treated and control, exclusion" are direct links between treated units and a sink that allows them to be excluded, "balance" refers to edges that count marginal balance between groups, and "sink" indicates edges that connect control nodes to the sink. Skeletons are created so these various features can be combined (or switched on and off) easily into objective functions, and the interface to the main tradeoff function expects to see each function represented in skeleton format.

Usage

costSkeleton(net)

Arguments

net

the network structure

Value

the skeleton

data_precheck

Data precheck: Handle missing data(mean imputation) and remove redundant columns; it also adds an NA column for indicating whether it's missing

Description

Data precheck: Handle missing data(mean imputation) and remove redundant columns; it also adds an NA column for indicating whether it's missing

Usage

data_precheck(X)

Arguments

Χ

a dataframe that the user initially inputs for matching - dataframe with covariates

Value

a dataframe with modified data if necessary

descr.stats_general

Generate summary statistics for matches

Description

Generate summary statistics for matches

Usage

```
descr.stats_general(matches, df, treatCol, b.vars, pair.vars, extra = FALSE)
```

Arguments

matches One matching result from the main matching function

df the original data frame used for matching

treatCol the character of the column name for treatment vector

b.vars the vector of column names of covariates used for measuring balance pair.vars the vector of column names used for measuring pairwise distance

extra the list of summary statistic; it must be the types that can be taken by cobalt

Value

a named vector of summary statistic

distanceFunctionHelper

Helper function that change input distance matrix

Description

Helper function that change input distance matrix

Usage

distanceFunctionHelper(z, distMat)

Arguments

z the treatment vector

distMat the user input distance matrix

Value

a distance matrix where (i,j) element is the distance between unit i and j in the same order as z

dist_bal_match

dist_bal_match

Optimal tradeoffs among distance, exclusion and marginal imbalance

Description

Explores tradeoffs among three important objective functions in an optimal matching problem: the sum of covariate distances within matched pairs, the number of treated units included in the match, and the marginal imbalance on pre-specified covariates (in total variation distance).

Usage

```
dist_bal_match(
  data,
  treat_col,
 marg_bal_col,
  exclusion_penalty = c(),
  balance_penalty = c(),
  dist_matrix = NULL,
  dist_col = NULL,
  exact_col = NULL,
  propensity_col = NULL,
  pscore_name = NULL,
  ignore_col = NULL,
  max\_unmatched = 0.25,
  caliper_option = NULL,
  tol = 0.01,
 max_iter = 1,
  rho_max_factor = 10,
 max_pareto_search_iter = 5
)
```

Arguments

data data frame that contain columns indicating treatment, outcome and covariates. treat_col character of name of the column indicating treatment assignment. marg_bal_col character of column name of the variable on which to evaluate marginal balance. exclusion_penalty (optional) numeric vector of values of exclusion penalty. Default is c(), which would trigger the auto grid search. balance_penalty (optional) factor of values of marginal balance penalty. Default value is c(), which would trigger the auto grid search. dist_matrix (optional) a matrix that specifies the pair-wise distances between any two obdist_col (optional) character vector of variable names used for calculating within-pair distance.

14 dist_bal_match

exact_col	(optional) character vector, variable names that we want exact matching on; NULL by default.
propensity_col	(optional) character vector, variable names on which to fit a propensity score (to supply a caliper).
pscore_name	(optional) character, giving the variable name for the fitted propensity score.
ignore_col	(optional) character vector of variable names that should be ignored when constructing the internal matching. NULL by default.
max_unmatched	(optional) numeric, the maximum proportion of unmatched units that can be accepted; default is 0.25 .
caliper_option	(optional) numeric, the propensity score caliper value in standard deviations of the estimated propensity scores; default is NULL, which is no caliper.
tol	(optional) numeric, tolerance of close match distance; default is 1e-2.
max_iter	(optional) integer, maximum number of iterations to use in searching for penalty combintions that improve the matching; default is 1, where the algorithm searches for one round.
rho_max_factor	(optional) numeric, the scaling factor used in proposal for penalties; default is 10.
max_pareto_sear	rch_iter
	(optional) numeric, the number of tries to search for the tol that yield pareto optimal solutions; default is 5.

Details

Matched designs generated by this function are Pareto optimal for the three objective functions. The degree of relative emphasis among the three objectives in any specific solution is controlled by the penalties, denoted by Greek letter rho. Larger values of exclusion_penalty corresponds to increased emphasis on retaining treated units (all else being equal), while larger values of balance_penalty corresponds to increased emphasis on marginal balance. Additional details:

- Users may either specify their own distance matrix via the dist_matrix argument or ask the function to create a robust Mahalanobis distance matrix internally on a set of covariates specified by the dist_col argument; if neither argument is specified an error will result. User-specified distance matrices should have row count equal to the number of treated units and column count equal to the number of controls.
- If the caliper_option argument is specified, a propensity score caliper will be imposed, forbidding matches between units more than a fixed distance apart on the propensity score. The caliper will be based either on a user-fit propensity score, identified in the input dataframe by argument pscore_name, or by an internally-fit propensity score based on logistic regression against the variables named in propensity_col. If caliper_option is non-NULL and neither of the other arguments is specified an error will result.
- tol controls the precision at which the objective functions is evaluated. When matching problems are especially large or complex it may be necessary to increase toleranceOption in order to prevent integer overflows in the underlying network flow solver; generally this will be suggested in appropariate warning messages.

dist_bal_match 15

• While by default tradeoffs are only assessed at penalty combinations provided by the user, the user may ask for the algorithm to search over additional penalty values in order to identify additional Pareto optimal solutions. rho_max_factor is a multiplier applied to initial penalties to discover new solutions, and setting it larger leads to wider exploration; similarly, max_iter controls how long the exploration routine runs, with larger values leading to more exploration.

Value

a named list whose elements are: * "rhoList": list of penalty combinations for each match * "match-List": list of matches indexed by number

- "treatmentCol": character of treatment variable
- "covs": character vector of names of the variables used for calculating within-pair distance
- "exactCovs": character vector of names of variables that we want exact or close match on *
 "idMapping": numeric vector of row indices for each observation in the sorted data frame for
 internal use
- "stats": data frame of important statistics (total variation distance) for variable on which marginal balance is measured
- "b.var": character, name of variable on which marginal balance is measured * "dataTable": data frame sorted by treatment value
- "t": a treatment vector
- "df": the original dataframe input by the user
- "pair_cost1": list of pair-wise distance sum using the first distance measure
- "pair_cost2": list of pair-wise distance sum using the second distance measure (left NULL since only one distance measure is used here).
- "version": (for internal use) the version of the matching function called; "Basic" indicates the matching comes from dist bal match and "Advanced" from two dist match.
- "fPair": a vector of values for the first objective function; it corresponds to the pair-wise distance sum according to the first distance measure.
- "fExclude": a vector of values for the second objective function; it corresponds to the number of treated units being unmatched.
- "fMarginal": a vector of values for the third objective function; it corresponds to the marginal balanced distance for the specified variable(s).

See Also

Other main matching function: two_dist_match()

Examples

```
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")
treat_val <- "treat"
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")
my_bal_val <- c("race")</pre>
```

16 dummy

```
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val,
marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s,
dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)</pre>
```

dummy

This is a modified version of the function "dummy" from the R package dummies. Original code Copyright (c) 2011 Decision Patterns.

Description

Change is made to the "model.matrix" function so that the output could be used for the current package.

Usage

```
dummy(
    X,
    data = NULL,
    sep = "",
    drop = TRUE,
    fun = as.integer,
    verbose = FALSE,
    name = NULL
)
```

Arguments

Х	a data.frame, matrix or single variable or variable name
data	(optional) if provided, x is the name of a column on the data
sep	(optional) the separator used between variable name and the value
drop	(optional) whether to drop unused levels
fun	(optional) function to coerce the value in the final matrix; 'as,integer' by default
verbose	(optional) whether to print the number of variables; FALSE by default
name	(optional) the column name to be selected for converting; NULL by default

edgelist2ISM 17

edgelist2ISM

Change the edgelist to the infinity sparse matrix

Description

Change the edgelist to the infinity sparse matrix

Usage

```
edgelist2ISM(elist)
```

Arguments

elist

the vector of the edges

Value

the infinity sparse matrix object

excludeCosts

Create a skeleton representation of the exclusion edge costs

Description

Create a skeleton representation of the exclusion edge costs associated with pairings for a given distance and network

Usage

```
excludeCosts(net, exclude.penalty = 1)
```

Arguments

```
net the network structure exclude.penalty
```

(optional) numeric penalty for excluding a treated unit; 1 by default

Value

the skeleton with exclusion edge cost

18 extractSupply

extractEdges

Extract edges from the network

Description

Extract edges from the network

Usage

```
extractEdges(net)
```

Arguments

net

the network representation

Value

the list of edges

extractSupply

Extract the supply nodes from the net

Description

Extract the supply nodes from the net

Usage

```
extractSupply(net)
```

Arguments

net

the network representation

Value

the vector of the supply nodes

filter_match_result 19

filter_match_result

Filter match result

Description

Filter match result

Usage

```
filter_match_result(matching_result, filter_expr)
```

Arguments

matching_result

the matching result object.

filter_expr

character, the filtering condition based on the summary table returned by get_rho_obj.

Value

the filtered match result

flattenSkeleton

Turns a skeleton representation of edge costs in a network

Description

Turns a skeleton representation of edge costs in a network back into the vector representation expected by the optimization routine. See comment on the costSkeleton function for more details.

Usage

```
flattenSkeleton(skeleton)
```

Arguments

skeleton

the skeleton structure

Value

vector representation expected by the optimization routine.

20 generate_rhos

generateRhoObj

Penalty and objective values summary

Description

Helper function to generate a dataframe with matching number, penalty (rho) values, and objective function values.

Usage

```
generateRhoObj(matchingResult)
```

Arguments

matchingResult matchingResult object that contains information for all matches.

Value

a dataframe that contains objective function values and rho values corresponding coefficients before each objective function.

See Also

Other numerical analysis helper functions: get_balance_table(), get_rho_obj(), get_unmatched()

generate_rhos

Generate rho pairs

Description

An internal helper function that generates the set of rho value pairs used for matching. This function is used when exploring the Pareto optimality of the solutions to the multi-objective optimization in matching.

Usage

```
generate_rhos(rho1.list, rho2.list)
```

Arguments

```
rho1.list a vector of rho 1 values rho2.list a vector of rho 2 values
```

Value

```
a vector of (rho1, rho2) pairs
```

getExactOn 21

|--|

Description

Generate a factor for exact matching.

Usage

```
getExactOn(dat, exactList)
```

Arguments

dataframe containing all the variables in exactList

exactList factor of names of the variables on which we want exact or close matching.

Value

factor on which to match exactly, with labels given by concatenating labels for input variables.

getPropensityScore	Fit propensity scores using logistic regression.	
--------------------	--	--

Description

Fit propensity scores using logistic regression.

Usage

```
getPropensityScore(data, covs)
```

Arguments

data dataframe that contains a column named "treat", the treatment vector, and columns

of covariates specified.

covs factor of column names of covariates used for fitting a propensity score model.

Value

vector of estimated propensity scores (on the probability scale).

22 get_balance_table

get_balance_table

Generate balance table

Description

The helper function can generate tabular analytics that quantify covariate imbalance after matching. It only works for the 'Basic' version of matching (produced by dist_bal_match).

Usage

```
get_balance_table(
  matching_result,
  cov_list = NULL,
  display_all = TRUE,
  stat_list = c("mean.diffs")
)
```

Arguments

matching_result

an object returned by the main matching function dist_bal_match

cov_list (optional) a vector of names of covariates used for evaluating covariate imbal-

ance; NULL by default.

display_all (optional) a boolean value indicating whether or not to show the data for all

possible matches; TRUE by default

stat_list (optional) a vector of statistics that are calculated for evaluating the covariate

imbalance between treated and control group. The types that are supported can

be found here: bal.tab.

Details

The result can be either directly used by indexing into the list, or post-processing by the function compare_tables that summarizes the covariate balance information in a tidier table. Users can specify the arguments as follows: * cov_list: if it is set of NULL, all the covariates are included for the covariate balance table; otherwise, only the specified covariates will be included in the tabular result. * display_all: by default, the summary statistics for each match are included when the argument is set to TRUE. If the user only wants to see the summary statistics for matches with varying performance on three different objective values, the function would only display the matches with number of treated units being excluded at different quantiles. User can switch to the brief version by setting the parameter to FALSE. * stat_list is the list of statistics used for measuring balance. The argument is the same as stats argument in bal.tab, which is the function that is used for calculating the statistics. By default, only standardized difference in means is calculated.

Value

a named list object containing covariate balance table and statistics for numer of units being matched for each match; the names are the character of index for each match in the matchResult.

get_five_index 23

See Also

Other numerical analysis helper functions: generateRhoObj(), get_rho_obj(), get_unmatched()

Examples

```
## Generate matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")</pre>
treat_val <- "treat"</pre>
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")</pre>
my_bal_val <- c("race")</pre>
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val,</pre>
marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s,
dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)
## Generate summary table for balance
balance_tables <- get_balance_table(match_result)</pre>
balance_tables_10 <- balance_tables$'10'</pre>
```

get_five_index

An internal helper function that gives the index of matching with a wide range of number of treated units left unmatched

Description

An internal helper function that gives the index of matching with a wide range of number of treated units left unmatched

Usage

```
get_five_index(matching_result)
```

Arguments

```
matching_result
```

an object returned by the main matching function dist_bal_match

Value

a vector of five matching indices with the number of treated units excluded at 0th, 25th, 50th, 75th and 100th percentiles respectively.

```
get_pairdist_balance_graph
```

Total variation imbalance vs. marginal imbalance

Description

Plotting function that generate sum of pairwise distance vs. total variation imbalance on specified balance variable. This function only works for 'Basic' version of matching (conducted using dist_bal_match).

Usage

```
get_pairdist_balance_graph(matching_result)
```

Arguments

```
matching_result
```

an object returned by the main matching function dist_bal_match

Value

No return value, called for visualization of match result

See Also

Other Graphical helper functions for analysis: get_pairdist_graph(), get_tv_graph()

Examples

```
## Generate matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")</pre>
treat_val <- "treat"</pre>
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")</pre>
my_bal_val <- c("race")</pre>
r1s < c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val,</pre>
marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s,
dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)
## Visualize the tradeoff between the pair-wise distance sum and
## total variation distance
get_pairdist_balance_graph(match_result)
```

get_pairdist_graph 25

Description

Plotting function that generate sum of pair-wise distance vs. number of unmatched treated units

Usage

```
get_pairdist_graph(matching_result)
```

Arguments

```
matching_result
```

an object returned by the main matching function dist_bal_match

Value

No return value, called for visualization of match result

See Also

Other Graphical helper functions for analysis: get_pairdist_balance_graph(), get_tv_graph()

Examples

```
## Generate matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")</pre>
treat_val <- "treat"</pre>
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")</pre>
my_bal_val <- c("race")</pre>
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val,</pre>
marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s,
dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)
## Generate visualization of tradeoff between pari-wise distance sum and
## number of treated units left unmatched
get_pairdist_graph(match_result)
```

26 get_tv_graph

get_rho_obj

Penalty and objective values summary

Description

Helper function to generate a dataframe with matching number, penalty (rho) values, and objective function values.

Usage

```
get_rho_obj(matching_result)
```

Arguments

matching_result

matchingResult object that contains information for all matches.

Value

a dataframe that contains objective function values and rho values corresponding coefficients before each objective function.

See Also

Other numerical analysis helper functions: generateRhoObj(), get_balance_table(), get_unmatched()

get_tv_graph

Marginal imbalance vs. exclusion

Description

Plotting function that visualizes the tradeoff between the total variation imbalance on a specified variable and the number of unmatched treated units. This function only works for the 'Basic' version of matching (conducted using dist_bal_match).

Usage

```
get_tv_graph(matching_result)
```

Arguments

```
matching_result
```

an object returned by the main matching function dist_bal_match

Value

No return value, called for visualization of match result

get_unmatched 27

See Also

Other Graphical helper functions for analysis: get_pairdist_balance_graph(), get_pairdist_graph()

Examples

```
## Generate matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")</pre>
treat_val <- "treat"</pre>
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")</pre>
my_bal_val <- c("race")</pre>
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val,</pre>
marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s,
dist_col = pair_dist_val,
propensity_col = ps_cols, max_iter=0)
## Generate visualization of tradeoff between total variation distance and
## number of treated units left unmatched
get_tv_graph(match_result)
```

get_unmatched

Get unmatched percentage

Description

A function that generate the percentage of unmatched units for each match.

Usage

```
get_unmatched(matching_result)
```

Arguments

```
matching_result
```

matchingResult object that contains information for all matches

Value

data frame with three columns, one containing the matching index, one containing the number of matched units, and one conatining the percentage of matched units (out of original treated group size).

See Also

Other numerical analysis helper functions: generateRhoObj(), get_balance_table(), get_rho_obj()

Examples

```
## Not run:
get_unmatched(match_result)
## End(Not run)
```

 ${\tt makeInfinitySparseMatrix}$

Internal helper to build infinity sparse matrix

Description

Formats the data and make a call to InfinitySparseMatrix-class

Usage

```
makeInfinitySparseMatrix(
  data,
  cols,
  rows,
  colnames = NULL,
  rownames = NULL,
  dimension = NULL,
  call = NULL
)
```

Arguments

data	the input numeric vector of cost
cols	the input numeric vector corresponding to control units
rows	the input numeric vector corresponding to treated units
colnames	(optional) vector containing names for all control units
rownames	(optional) vector containing names for all treated units
dimension	(optional) vector of number of treated and control units
call	(optional) funtion call used to create the InfinitySparseMatrix

Value

an InfinitySparseMatrix object

makeSparse 29

• •

Description

Remove some of the treatment-control edges from a network flow representation of a match (for-bidding those pairings)

Usage

```
makeSparse(net, mask, replaceMask = TRUE)
```

Arguments

net the network object

mask a matrix indicating whether to exclude the corresponding edge

replaceMask (optional) whether to mask

Value

the masked network structure object

matched_data	Get matched dataframe

Description

A function that returns the dataframe that contains only matched pairs from the original data frame with specified match index

Usage

```
matched_data(matching_result, match_num)
```

Arguments

matching_result

an object returned by the main matching function dist_bal_match

match_num Integer index of match that the user want to extract paired observations from

Value

dataframe that contains only matched pair data

30 matrix2cost

Examples

```
## Generate Matches
data("lalonde", package="cobalt")
ps_cols <- c("age", "educ", "married", "nodegree", "race")
treat_val <- "treat"
response_val <- "re78"
pair_dist_val <- c("age", "married", "educ", "nodegree", "race")
my_bal_val <- c("race")
r1s <- c(0.01,1,2,4,4.4,5.2,5.4,5.6,5.8,6)
r2s <- c(0.001)
match_result <- dist_bal_match(data=lalonde, treat_col= treat_val, marg_bal_col = my_bal_val, exclusion_penalty=r1s, balance_penalty=r2s, dist_col = pair_dist_val, propensity_col = ps_cols, max_iter=0)
matched_data(match_result, 1)</pre>
```

matched_index

An internal helper function that translate the matching index in the sorted data frame to the original dataframe's row index

Description

An internal helper function that translate the matching index in the sorted data frame to the original dataframe's row index

Usage

```
matched_index(matchingResult)
```

Arguments

matchingResult an object returned by the main matching function dist_bal_match

matrix2cost

change the distance matrix to cost

Description

change the distance matrix to cost

Usage

```
matrix2cost(net, distance)
```

matrix2edgelist 31

Arguments

net the network structure distance distance matrix

Value

the vector of cost

matrix2edgelist

Helper function to convert matrix to list

Description

Convert between a matrix representation of distances between treated and control units and a list of vectors (default format for build.dist.struct function in rcbalance package)

Usage

```
matrix2edgelist(mat)
```

Arguments

mat

matrix representation of distances between treated and control units

Value

list of vector representation of distances

meldMask

Helper function to combine two sparse distances

Description

Combine two sparse distances, allowing only pairings allowed by both

Usage

```
meldMask(mask1, mask2)
```

Arguments

mask1 matrix of the first mask mask2 matrix of the second mask

Value

combined mask structure

32 obj.to.match

netF	10	ωMa	tcl	า
1100	TO	wiia	LUI	

Create network flow structure

Description

Create network flow structure

Usage

```
netFlowMatch(z, IDs = NULL)
```

Arguments

Z	a vector of treatment vectors
IDs	(optional) the name of the units

Value

a networks structure

obj.to.match	An internal helper function th	at transforms the out
--------------	--------------------------------	-----------------------

tput from the RELAX algorithm to a data structure that is more interpretable for the output

of the main matching function

Description

An internal helper function that transforms the output from the RELAX algorithm to a data structure that is more interpretable for the output of the main matching function

Usage

```
obj.to.match(out.elem, already.done = NULL, prev.obj = NULL)
```

Arguments

a named list whose elements are: (1) the net structure (2) the edge weights of out.elem

pair-wise distance (3) the edge weights of marginal balance (4) the list of rho

value pairs (5) the named list of solutions from the RELAX algorithm

a factor indicating the index of matches already been transformed already.done

prev.obj an object of previously transformed matches

Value

a named list with elements containing matching information useful for the main matching function

pairCosts 33

pairCosts

Create a skeleton representation of the edge costs

Description

Create a skeleton representation of the edge costs

Usage

```
pairCosts(dist.struct, net)
```

Arguments

```
dist.struct the distance structure
net the net structure
```

Value

the skeleton representation of the given distance pairs and the net

rho_proposition

Generate penalty coefficient pairs

Description

An internal helper function used for automatically generating the set of rho values used for grid search in exploring the Pareto optimal set of solutions.

Usage

```
rho_proposition(
  paircosts.list,
  rho.max.factor = 10,
  rho1old,
  rho2old,
  rho.min = 0.01
)
```

Arguments

rho.min

```
paircosts.list a vector of pair-wise distance.

rho.max.factor a numeric value indicating the maximal rho values.

rho1old a vector of numeric values of rho1 used before.

rho2old a vector of numeric values of rho2 used before.
```

smallest rho value to consider.

34 solveP1

Value

a vector of pairs of rho values for future search.

solveP

Solve the network flow problem - basic version

Description

Solve the network flow problem - basic version

Usage

```
solveP(net, f1.list, f2.list, rho, tol = 1e-05)
```

Arguments

net	the network representation
f1.list	the list of the first objective functions values for each node
f2.list	the list of the second objective functions values for each node
rho	the penalty coefficient
tol	the tolerance value for precision

Value

the solution represented in a named list

solveP1

 $Solve \ the \ network \ flow \ problem \ - \ two DistMatch$

Description

Solve the network flow problem - twoDistMatch

Usage

```
solveP1(net, f1.list, f2.list, f3.list, rho1, rho2 = 0, tol = 1e-05)
```

Arguments

net	the network representation
f1.list	the list of the first objective functions values for each node
f2.list	the list of the second objective functions values for each node
f3.list	the list of the third objective functions values for each node
rho1	the penalty coefficient for the second objective
rho2	the penalty coefficient for the third objective
tol	the tolerance value for precision

Value

the solution represented in a named list

summary.multiObjMatch Generate numerical summary

Description

Main summary functions for providing tables of numerical information in matching penalties, objective function values, and balance.

Usage

```
## $3 method for class 'multiObjMatch'
summary(
  object,
  type = "penalty",
  cov_list = NULL,
  display_all = TRUE,
  stat = "mean.diff",
   ...
)
```

Arguments

object	the matching result returned by either dist_bal_match or two_dist_match.
type	(optional) the type of the summary result in c("penalty", "exclusion", "balance").
	When "penalty" is passed in, the objective function values and the penalty values
	are displayed for each match; when "exclusion" is passed in, the number of
	units being matched is displayed for each match; when "balance" is passed in,
	the covariate the covariate balance table from bal.tab function in cobalt function
	is displayed and user can change covList to specify the variables to examine. "penalty" by default.
cov_list	(optional) factor of names of covariates that we want to evaluate covariate bal- ance on if "balance" is passed in for type; default is NULL. When set to NULL, the program will compare the covariates that have been used to construct a propensity model.
display_all	(optional) boolean value of whether to display all the matches if "balance" is passed in for type; default is TRUE, where all matches are displayed.
stat	(optional) character of the name of the statistic used for measuring covariate balance if "balance" is passed in for type; default is "mean.diff". This argument is the same as used in "cobalt" package, see: bal.tab
	ignored.

Value

a summary dataframe of the corresponding type.

two_dist_match

Optimal tradeoffs among two distances and exclusion

Description

Explores tradeoffs among three objective functions in multivariate matching: sums of two different user-specified covariate distances within matched pairs, and the number of treated units included in the match.

Usage

```
two_dist_match(
  dist1_type = "user",
  dist2_type = "user",
  dist1_matrix = NULL,
  data = NULL,
  dist2_matrix = NULL,
  treat_col = NULL,
  dist1_col = NULL,
  dist2_col = NULL,
  exclusion_penalty = c(),
  dist2_penalty = c(),
 marg_bal_col = NULL,
  exact_col = NULL,
  propensity_col = NULL,
  pscore_name = NULL,
  ignore_col = NULL,
 max\_unmatched = 0.25,
  caliper_option = NULL,
  tol = 0.01,
 max_iter = 1,
  rho_max_factor = 10,
 max_pareto_search_iter = 5
)
```

Arguments

dist1_type	One of ("euclidean", "robust_mahalanobis", "user") indicating the type of distance that are used for the first distance objective functions. NULL by default.
dist2_type	One of ("euclidean", "robust_mahalanobis", "user") charactor indicating the type of distance that are used for the second distance objective functions. NULL by default.
dist1_matrix	(optional) matrix object that represents the distance matrix using the first distance measure; dist1_type must be passed in as "user" if dist1_matrix is non-empty

data	(optional) data frame that contain columns indicating treatment, outcome and covariates
dist2_matrix	(optional) matrix object that represents the distance matrix using the second distance measure; dist2_type must be passed in as "user" if dist2_matrix is non-empty
treat_col	(optional) character, name of the column indicating treatment assignment.
dist1_col	(optional) character vector names of the variables used for calculating covariate distance using first distance measure specified by dType
dist2_col	(optional) character vector, names of the variables used for calculating covariate distance using second distance measure specified by dType1
exclusion_pena	
	(optional) numeric vector, penalty values associated with exclusion. Empty by default, where auto grid search is triggered.
dist2_penalty	(optional) numeric vector, penalty values associated with the distance specified by dist2_matrix or dist2_type. Empty by default, where auto grid search is tiggered.
marg_bal_col	(optional) character, column name of the variable on which to evaluate balance.
exact_col	(optional) character vector, names of the variables on which to match exactly; NULL by default.
propensity_col	character vector, names of columns on which to fit a propensity score model.
pscore_name	(optional) character, name of the column containing fitted propensity scores; default is NULL.
ignore_col	(optional) character vector of variable names that should be ignored when constructing the internal matching. NULL by default.
max_unmatched	(optional) numeric, maximum proportion of unmatched units that can be accepted; default is 0.25 .
caliper_option	(optional) numeric, the propensity score caliper value in standard deviations of the estimated propensity scores; default is NULL, which is no caliper.
tol	(optional) numeric, tolerance of close match distance; default is 1e-2.
max_iter	(optional) integer, maximum number of iterations to use in searching for penalty combintions that improve the matching; default is 1, where the algorithm searches for one round.
	(optional) numeric, the scaling factor used in proposal for penalties; default is 10.
max_pareto_sea	
	(optional) numeric, the number of tries to search for the tol that yield pareto optimal solutions; default is 5.

Details

Matched designs generated by this function are Pareto optimal for the three objective functions. The degree of relative emphasis among the three objectives in any specific solution is controlled by the penalties, denoted by Greek letter rho. Larger values for the penalties associated with the two distances correspond to increased emphasis close matching on these distances, at the possible cost of excluding more treated units. Additional details:

Users may either specify their own distance matrices (specifying the User option in dist1_type and/or dist2_type and supplying arguments to dist1_matrix and/or dist2_matrix respectively) or ask the function to create Mahalanobis or Euclidean distances on sets of covariates specified by the dist1_col and dist2_col arguments. If dist1_type or dist2_type is not specified, if one of these is set to user and the corresponding dist1_matrix argument is not provided, or if one is NOT set to User and the corresponding dist1_col argument is not provided, the code would error out.

- User-specified distance matrices passed to dist1_matrix or dist2_matrix should have row count equal to the number of treated units and column count equal to the number of controls.
- If the caliper_option argument is specified, a propensity score caliper will be imposed, forbidding matches between units more than a fixed distance apart on the propensity score. The caliper will be based either on a user-fit propensity score, identified in the input dataframe by argument pscore_name, or by an internally-fit propensity score based on logistic regression against the variables named in propensity_col. If caliper_option is non-NULL and neither of the other arguments is specified an error will result.
- tol controls the precision at which the objective functions is evaluated. When matching problems are especially large or complex it may be necessary to increase toleranceOption in order to prevent integer overflows in the underlying network flow solver; generally this will be suggested in appropariate warning messages.
- While by default tradeoffs are only assessed at penalty combinations provided by the user, the
 user may ask for the algorithm to search over additional penalty values in order to identify
 additional Pareto optimal solutions. rho_max_factor is a multiplier applied to initial penalty
 values to discover new solutions, and setting it larger leads to wider exploration; similarly,
 max_iter controls how long the exploration routine runs, with larger values leading to more
 exploration.

Value

a named list whose elements are:

- "rhoList": list of penalty combinations for each match
- "matchList": list of matches indexed by number
- "treatmentCol": character of treatment variable
- "covs":character vector of names of the variables used for calculating within-pair distance
- "exactCovs": character vector of names of variables that we want exact or close match on
- "idMapping": numeric vector of row indices for each observation in the sorted data frame for internal use
- "stats": data frame of important statistics (total variation distance) for variable on which marginal balance is measured
- "b.var": character, name of variable on which marginal balance is measured (left NULL since no balance constraint is imposed here).
- "dataTable": data frame sorted by treatment value
- "t": a treatment vector
- "df": the original dataframe input by the user
- "pair_cost1": list of pair-wise distance sum using the first distance measure

- "pair_cost2": list of pair-wise distance sum using the second distance measure
- "version": (for internal use) the version of the matching function called; "Basic" indicates the matching comes from dist_bal_match and "Advanced" from two_dist_match.
- "fDist1": a vector of values for the first objective function; it corresponds to the pair-wise distance sum according to the first distance measure.
- "fExclude": a vector of values for the second objective function; it corresponds to the number of treated units being unmatched.
- "fDist2": a vector of values for the third objective function; it corresponds to the pair-wise distance sum corresponds to the

See Also

Other main matching function: dist_bal_match()

Examples

```
x1 = rnorm(100, 0, 0.5)
x2 = rnorm(100, 0, 0.1)
x3 = rnorm(100, 0, 1)
x4 = rnorm(100, x1, 0.1)
r1ss < - seq(0.1,50, 10)
r2ss \leftarrow seq(0.1,50, 10)
x = cbind(x1, x2, x3,x4)
z = sample(c(rep(1, 50), rep(0, 50)))
e1 = rnorm(100, 0, 1.5)
e0 = rnorm(100, 0, 1.5)
y1impute = x1^2 + 0.6*x2^2 + 1 + e1
y0impute = x1^2 + 0.6*x2^2 + e0
treat = (z==1)
y = ifelse(treat, y1impute, y0impute)
names(x) \leftarrow c("x1", "x2", "x3", "x4")
df <- data.frame(cbind(z, y, x))</pre>
df$x5 <- 1
names(x) \leftarrow c("x1", "x2", "x3", "x4")
df <- data.frame(cbind(z, y, x))</pre>
df$x5 <- 1
d1 <- as.matrix(dist(df["x1"]))</pre>
d2 <- as.matrix(dist(df["x2"]))</pre>
idx <- 1:length(z)</pre>
treated_units <- idx[z==1]</pre>
control_units <- idx[z==0]</pre>
d1 <- as.matrix(d1[treated_units, control_units])</pre>
d2 <- as.matrix(d2[treated_units, control_units])</pre>
match_result_1 <- two_dist_match(data=df, treat_col="z", dist1_matrix=d1,</pre>
dist1_type= "User", dist2_matrix=d2,
dist2_type="User", marg_bal_col=c("x5"), exclusion_penalty=r1ss,
dist2_penalty=r2ss,
propensity_col = c("x1"), max_iter = 0,
max_pareto_search_iter = 0)
```

40 visualize

visualize

Visualize tradeoffs

Description

Main visualization functions for showing the tradeoffs between two of the three objective functions. A 3-d plot can be visualized where the third dimension is represented by coloring of the dots.

Usage

```
visualize(
  matching_result,
 x_axis = "dist1",
 y_axis = "dist2",
  z_{axis} = NULL,
 xlab = NULL,
 ylab = NULL,
  zlab = NULL,
 main = NULL,
  display_all = FALSE,
  cond = NULL,
  xlim = NULL,
 ylim = NULL,
  display_index = TRUE,
  average\_cost = FALSE
)
```

Arguments

```
matching_result
                   the matching result returned by either dist_bal_match or two_dist_match.
                   character, naming the objective function shown on x-axis; one of ("pair", "marginal",
x_axis
                   "dist1", "dist2", "exclude", "distance_penalty", "balance_penalty", "dist1_penalty",
                   "dist2_penalty", "exclusion_penalty"), "dist1" by default.
                   character, naming the objective function shown on y-axis; one of ("pair", "marginal",
y_axis
                   "dist1", "dist2", "exclude", "distance_penalty", "balance_penalty", "dist1_penalty",
                   "dist2_penalty", "exclusion_penalty"), "dist1" by default.
                   character, naming the objective function for coloring; one of ("pair", "marginal",
z_axis
                   "dist1", "dist2", "exclude"), "exclude" by default.
xlab
                   (optional) the axis label for x-axis; NULL by default.
                   (optional) the axis label for y-axis; NULL by default.
ylab
zlab
                   (optional) the axis label for z-axis; NULL by default.
                   (optional) the title of the graph; NULL by default.
main
```

visualize 41

display_all	(optional) whether to show all the labels for match index; FALSE by default, which indicates the visualization function only labels matches at quantiles of number of treated units being excluded.
cond	(optional) NULL by default, which denotes all the matches are shown; otherwise, takes a list of boolean values indicating whether to include each match
xlim	(optional) NULL by default; function automatically takes the max of the first objective function values being plotted on x-axis; if specified otherwise, pass in the numeric vector c(lower_bound, upper_bound)
ylim	(optional) NULL by default; function automatically takes the max of the first objective function values being plotted on y-axis; if specified otherwise, pass in the numeric vector c(lower_bound, upper_bound)
display_index	(optional) TRUE by default; whether to display match index
average_cost	(optional) FALSE by default; whether to show mean cost

Details

By default, the plotting function will show the tradeoff between the first distance objective function and the marginal balance (if dist_bal_match) is used; or simply the second distance objective function, if two_dist_match is used.

Value

No return value, called for visualization of match result

Index

* Graphical helper functions for analysis	filter_match_result, 19
<pre>get_pairdist_balance_graph, 24</pre>	flattenSkeleton, 19
<pre>get_pairdist_graph, 25</pre>	
get_tv_graph, 26	generate_rhos, 20
* main matching function	generateRhoObj, 20, 23, 26, 27
dist_bal_match, 13	get_balance_table, 20, 22, 26, 27
two_dist_match, 36	<pre>get_five_index, 23</pre>
* numerical analysis helper functions	<pre>get_pairdist_balance_graph, 24, 25, 27</pre>
generateRhoObj, 20	get_pairdist_graph, 24, 25, 27
get_balance_table, 22	get_rho_obj, 20, 23, 26, 27
get_rho_obj, 26	get_tv_graph, 24, 25, 26
get_unmatched, 27	get_unmatched, 20, 23, 26, 27
	getExactOn, 21
addBalance, 3	getPropensityScore, 21
addExclusion, 3	
	InfinitySparseMatrix-class, 28
bal. tab, 8, 22, 35	1.7.6: 0
balanceCosts, 4	makeInfinitySparseMatrix, 28
build.dist.struct, 4	makeSparse, 29
<pre>build.dist.struct_user, 5</pre>	matched_data, 29
	matched_index, 30
callrelax, 6	matrix2cost, 30
check_representative, 6	matrix2edgelist, 31
combine_dist, 7	meldMask, 31
combine_match_result, 7	· 53 . W · 1 . 22
compare_matching, 8	netFlowMatch, 32
compare_tables, 9	ohi to motoh 22
convert_index, 10	obj.to.match, 32
convert_names, 10	pairCosts, 33
costSkeleton, 11	pull 605 t3, 55
data_precheck, 11	rho_proposition, 33
descr.stats_general, 12	
dist_bal_match, 13, 39	solveP, 34
distanceFunctionHelper, 12	solveP1, 34
	summary.multiObjMatch, 35
dummy, 16	
edgelist2ISM, 17	two_dist_match, 15, 36
excludeCosts, 17	
extractEdges, 18	visualize, 40
extractSupply. 18	