Package 'RobustBayesianCopas'

October 12, 2022

Type Package

Title Robust Bayesian Copas Selection Model
Version 2.0
Date 2021-01-05
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Description Fits the robust Bayesian Copas (RBC) selection model of Bai et al. (2020) <arxiv:2005.02930> for correcting and quantifying publication bias in univariate meta-analysis. Also fits standard random effects meta-analysis and the Copas-like selection model of Ning et al. (2017) <doi:10.1093 biostatistics="" kxx004="">.</doi:10.1093></arxiv:2005.02930>
License GPL-3
LazyData true
Depends R (>= $3.6.0$)
Imports stats, statip, rjags
NeedsCompilation yes
Repository CRAN
RoxygenNote 7.1.1
Date/Publication 2021-01-06 15:10:02 UTC
R topics documented:
Barlow2014
BayesNonBiasCorrected
CopasLikeSelection
Hackshaw1997
RobustBayesianCopas
StandardMetaAnalysis
Index 18

2 antidepressants

antidepressants

A Meta-Analysis on the Efficacy of Antidepressants

Description

This data set contains 73 studies with results on the effectiveness of antidepressants that were reported to the FDA. However, only 50 of these studies were subsequently published. Since studies reported their outcomes on different scales, effect sizes were all expressed as standardized mean differences by means of Hedges' *g* scores, accompanied by corresponding variances. This data set was originally analyzed by Turner et al. (2008).

Usage

data(antidepressants)

Format

A dataframe with 73 studies with the following seven variables.

Drug: Antidepressant name.

Study: Study identifier.

Published: A binary variable indicating whether the study was published: "1"=published, "0"=not published.

Nonstandardized_effect_size: Estimated mean improvement in depression symptoms (non-standardized).

Nonstandardized_SE: Estimated standard error (nonstandardized).

Standardized_effect_size Estimated mean improvement in depression symptoms (standardized). Note that the standardized values are only available for the *published* studies (NA if not published). The *non*-missing data in this column should be used as y in the selection model.

Standardized_SE: Estimated standard error (standardized). Note that the standardized values are only available for the *published* studies (NA if not published). The *non*-missing data in this column should be used as s in the selection model.

Source

Turner, E. H., Matthews, A. M., Linardatos, E., Tell, R. A., and Rosenthal, R. (2008). "Selective publication of antidepressant trials and its influence on apparent efficacy." *New England Journal of Medicine*, **358**(3):252-260.

Barlow2014 3

Barlow2014	A Meta-Analysis on the Effect of Parent Training Programs vs. Control for Improving Parental Psychosocial Health Within 4 Weeks After
	Intervention

Description

This data set contains 26 studies with the standardized mean differences between the improvement in parental psychosocial health for subjects who were enrolled in parent training programs vs. those who were not. This data set is also available in the R package altmeta, along with many other useful data sets.

Usage

data(Barlow2014)

Format

A dataframe with 26 studies with the following five variables within each study.

- y: Standardized mean differences in improvement of parental psychosocial health.
- s: Sample standard errors of standardized mean differences.
- n1: Sample sizes in treatment group 1 (parent training programs).
- n2: Sample sizes in treatment group 2 (control).
- n: Total sample size.

Source

Barlow J, Smailagic N, Huband N, Roloff V, Bennett C (2014). "Group-based parent training programmes for improving parental psychosocial health." *Cochrane Database of Systematic Reviews*,**5**, Art. No.: CD002020. <doi: 10.1002/14651858.CD002020.pub4>

BayesNonBiasCorrected Non-bias-corrected robust Bayesian meta-analysis model

Description

This function implements the *non*-bias-corrected Robust Bayesian Copas selection model of Bai et al. (2020) when there is no publication bias (i.e. $\rho=0$). In this case, the Copas selection model reduces to the standard random effects meta-analysis model:

$$y_i = \theta + \tau u_i + s_i \epsilon_i,$$

where y_i is the reported treatment effect for the *i*th study, s_i is the reported standard error for the *i*th study, θ is the population treatment effect of interest, $\tau > 0$ is a heterogeneity parameter, ϵ_i is distributed as N(0,1), and u_i and ϵ_i are independent.

For the *non*-bias-corrected model, we place noninformative priors on (θ, τ^2) (see Bai et al. (2020) for details). For the random effects $u_i, i = 1, \ldots, n$, we give the option for using normal, Student's t, Laplace, or slash distributions for the random effects. If this function is being run in order to quantify publication bias with the robust Bayesian Copas selection model, then the practitioner should use the *same* random effects distribution that they used for RobustBayesianCopas.

Usage

Arguments

٤	guments		
	У	An $n \times 1$ vector of reported treatment effects.	
	S	An $n \times 1$ vector of reported within-study standard errors.	
	re.dist	Distribution for the between-study random effects $u_i, i=1,\ldots,n$. The user may specify the normal, Student's t, Laplace, or slash distribution. The default is StudentsT with 4 degrees of freedom.	
	t.df	Degrees of freedom for t-distribution. Only used if $StudentsT$ is specified for re.dist. Default is 4.	
	slash.shape	Shape parameter in the slash distribution. Only used if slash is specified for re.dist. Default is 1.	
	init	Optional initialization values for (θ,τ) . If specified, they must be provided in this exact order. If they are not provided, the program estimates initial values from the data.	
	seed	Optional seed. This needs to be specified if you want to reproduce the exact results of your analysis.	
	burn	Number of burn-in samples. Default is burn=10000.	
	nmc	Number of posterior samples to save. Default is nmc=10000.	

Value

The function returns a list containing the following components:

theta.hat posterior mean for θ . theta.samples MCMC samples for θ after burn-in. Used for plotting the posterior for θ and performing inference of θ . tau.hat posterior mean for τ . tau.samples MCMC samples for τ after burn-in. Used for plotting the posterior for τ and performing inference of τ .

CopasLikeSelection 5

References

Bai, R., Lin, L., Boland, M. R., and Chen, Y. (2020). "A robust Bayesian Copas selection model for quantifying and correcting publication bias." *arXiv preprint arXiv:2005.02930*.

Examples

```
# Example on the Barlow2014 data set #
data(Barlow2014)
attach(Barlow2014)
# Observed treatment effect
y.obs = Barlow2014[,1]
# Observed standard error
s.obs = Barlow2014[,2]
# Fit the non-bias-corrected model #
# NOTE: Use default burn-in (burn=10000) and post-burn-in samples (nmc=10000)
# Fit the model with Laplace errors.
RBCNoBias.mod = BayesNonBiasCorrected(y=y.obs, s=s.obs, re.dist="Laplace", burn=500, nmc=500)
# Point estimate for theta
theta.hat.RBCNoBias = RBCNoBias.mod$theta.hat
# Standard error for theta
theta.se.RBCNoBias = sd(RBCNoBias.mod$theta.samples)
# 95% posterior credible interval for theta
theta.cred.int = quantile(RBCNoBias.mod$theta.samples, probs=c(0.025,0.975))
# Display results
theta.hat.RBCNoBias
theta.se.RBCNoBias
theta.cred.int
# Plot the posterior for theta
hist(RBCNoBias.mod$theta.samples)
```

CopasLikeSelection

Copas-like selection model

Description

This function performs maximum likelihood estimation (MLE) of $(\theta, \tau, \rho, \gamma_0, \gamma_1)$ using the EM algorithm of Ning et al. (2017) for the Copas selection model,

6 CopasLikeSelection

$$y_i|(z_i > 0) = \theta + \tau u_i + s_i \epsilon_i,$$

$$z_i = \gamma_0 + \gamma_1/s_i + \delta_i,$$

$$corr(\epsilon_i, \delta_i) = \rho,$$

where y_i is the reported treatment effect for the *i*th study, s_i is the reported standard error for the *i*th study, θ is the population treatment effect of interest, $\tau > 0$ is a heterogeneity parameter, and u_i , ϵ_i , and δ_i are marginally distributed as N(0,1), and u_i and ϵ_i are independent.

In the Copas selection model, y_i is published (selected) if and only if the corresponding propensity score z_i (or the propensity to publish) is greater than zero. The propensity score z_i contains two parameters: γ_0 controls the overall probability of publication, and γ_1 controls how the chance of publication depends on study sample size. The reported treatment effects and propensity scores are correlated through ρ . If $\rho=0$, then there is no publication bias and the Copas selection model reduces to the standard random effects meta-analysis model.

This is called the "Copas-like selection model" because to find the MLE, the EM algorithm utilizes a latent variable m that is treated as missing data. See Ning et al. (2017) for more details. An alternative funtion for implementing the Copas selection model using a grid search for (γ_0, γ_1) is available in the R package metasens.

Usage

CopasLikeSelection(y, s, init = NULL, tol=1e-20, maxit=1000)

Arguments

У	An $n \times 1$ vector of reported treatment effects.
S	An $n \times 1$ vector of reported within-study standard errors.
init	Optional initialization values for $(\theta, \tau, \rho, \gamma_0, \gamma_1)$. If specified, they must be provided in this exact order. If they are not provided, the program estimates initial values from the data.
tol	Convergence criterion for the Copas-like EM algorithm for finding the MLE. Default is tol=1e-20.
maxit	Maximum number of iterations for the Copas-like EM algorithm for finding the MLE. Default is maxit=1000.

Value

The function returns a list containing the following components:

theta.hat	MLE of θ .
tau.hat	MLE of τ .
rho.hat	MLE of ρ .
gamma0.hat	MLE of γ_0 .
gamma1.hat	MLE of γ_1 .

CopasLikeSelection 7

H 5×5 Hessian matrix for the estimates of $(\theta, \tau, \rho, \gamma_0, \gamma_1)$. The square root of the diagonal entries of H can be used to estimate the standard errors for $(\theta, \tau, \rho, \gamma_0, \gamma_1)$.

"1" if the optimization algorithm converged, "0" if algorithm did not converge. If conv=0, then using H to estimate the standard errors may not be reliable.

References

Ning, J., Chen, Y., and Piao, J. (2017). "Maximum likelihood estimation and EM algorithm of Copas-like selection model for publication bias correction." *Biostatistics*, **18**(3):495-504.

```
# Example on the Hackshaw data set #
data(Hackshaw1997)
attach(Hackshaw1997)
# Extract the log OR
y.obs = Hackshaw1997[,2]
# Extract the observed standard error
s.obs = Hackshaw1997[,3]
# Fit Copas-like selection model #
# First fit RBC model with normal errors
RBC.mod = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="normal", seed=123, burn=500, nmc=500)
# Fit CLS model with initial values given from RBC model fit.
# Initialization is not necessary but the algorithm will converge faster with initialization.
CLS.mod = CopasLikeSelection(y=y.obs, s=s.obs, init=c(RBC.mod$theta.hat, RBC.mod$tau.hat,
                                              RBC.mod$rho.hat, RBC.mod$gamma0.hat,
                                               RBC.mod$gamma1.hat))
# Point estimate for theta
CLS.theta.hat = CLS.mod$theta.hat
# Use Hessian to estimate standard error for theta
CLS.Hessian = CLS.mod$H
# Standard error estimate for theta
CLS.theta.se = sqrt(CLS.Hessian[1,1]) #
# 95 percent confidence interval
CLS.interval = c(CLS.theta.hat-1.96*CLS.theta.se, CLS.theta.hat+1.96*CLS.theta.se)
# Display results
CLS.theta.hat
CLS.theta.se
CLS.interval
```

D.measure

```
# Other parameters controlling the publication bias
CLS.mod$rho.hat
CLS.mod$gamma0.hat
CLS.mod$gamma1.hat
```

D.measure

D Measure for Quantifying Publication Bias

Description

This function computes Bai's D measure for quantifying publication bias based on the robust Bayesian Copas (RBC) selection model. Let $\pi_{rbc}(\theta|y)$ be the posterior distribution for θ under the full RBC (bias-corrected) model, and let $\pi_{\rho=0}(\theta|y)$ be the posterior distribution for θ under the non-bias corrected model (when ρ is fixed at $\rho=0$). The D measure is the Hellinger distance H between the bias-corrected and non-bias-corrected posteriors.

$$D = H(\pi_{rbc}(\theta|y), \pi_{\rho=0}(\theta|y)).$$

D is always between 0 and 1, with $D\approx 0$ indicating negligible publication bias and $D\approx 1$ indicating a very high magnitude of publication bias.

The random effects distributions for the bias-corrected and non-bias-corrected models should be the same in order for the D measure to be valid. The posterior densities for $\pi_{rbc}(\theta|y)$ and $\pi_{\rho=0}(\theta|y)$ are approximated using MCMC samples. Numerical integration is used to compute the Hellinger distance between them.

Usage

D.measure(samples.RBCmodel, samples.nobiasmodel)

Arguments

samples.RBCmodel

A vector of the MCMC samples from the RBC model. These can be obtained from the output of the function RobustBayesianCopas.

samples.nobiasmodel

A vector of the MCMC samples from the non-bias-corrected model. These can be obtained from the output of the function BayesNonBiasCorrected. In order for the D measure to be valid, the random effects distribution used in BayesNonBiasCorrected should be the same as the random effects distribution used in RobustBayesianCopas.

Value

The function returns Bai's D measure, a value between 0 and 1. $D \approx 0$ means negligible publication bias, and $D \approx 1$ means a very high magnitude of publication bias.

D.measure 9

References

Bai, R., Lin, L., Boland, M. R., and Chen, Y. (2020). "A robust Bayesian Copas selection model for quantifying and correcting publication bias." *arXiv preprint arXiv:2005.02930*.

```
# Example on the Barlow2014 data set #
data(Barlow2014)
attach(Barlow2014)
# Observed treatment effect
y.obs = Barlow2014[,1]
# Observed standard error
s.obs = Barlow2014[.2]
# Compute D measure using posterior samples #
# Fit RBC (bias-corrected) model with t-distributed random effects.
# NOTE: Use default burn-in (burn=10000) and post-burn-in samples (nmc=10000)
RBC.mod = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="StudentsT", burn=500, nmc=500)
# Fit non-bias-corrected model with t-distributed random effects.
# NOTE: Use default burn-in (burn=10000) and post-burn-in samples (nmc=10000)
RBCNoBias.mod = BayesNonBiasCorrected(y=y.obs, s=s.obs, re.dist="StudentsT", burn=500, nmc=500)
# Compute the D measure based on posterior samples for theta
D = D.measure(RBC.mod$theta.samples, RBCNoBias.mod$theta.samples)
# Example on the antidepressants data set. #
# This is from Section 6.2 of the paper
# by Bai et al. (2020).
# Set seed, so we can reproduce the exact same results as in the paper.
seed = 123
set.seed(seed)
# Load the full data
data(antidepressants)
attach(antidepressants)
# Extract the 50 published studies
published.data = antidepressants[which(antidepressants$Published==1),]
# Observed treatment effect
```

10 Hackshaw1997

```
y.obs = published.data$Standardized_effect_size
 # Observed standard error
 s.obs = published.data$Standardized_SE
 #####################################
 # Compute the D measure for
 # quantifying publication bias #
 # Fit RBC model with different random effects distributions and compare them using DIC.
 RBC.mod.normal = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="normal", seed=seed)
 RBC.mod.normal$DIC # DIC=369.3126
 # Student's t
 RBC.mod.StudentsT = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="StudentsT", seed=seed)
 RBC.mod.StudentsT$DIC # DIC=515.5151
 RBC.mod.laplace = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="Laplace", seed=seed)
 RBC.mod.laplace$DIC # DIC=475.5845
 # Slash
 RBC.mod.slash = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="slash", seed=seed)
 RBC.mod.slash$DIC # DIC=381.2705
 # The model with normal random effects gave the lowest DIC, so we use the model
 # with normal study-specific effects for our final analysis.
 RBC.mod.normal$rho.hat # rho.hat=0.804
 # Plot posterior for rho, which suggests strong publication bias.
 hist(RBC.mod.normal$rho.samples)
 # Fit non-biased-corrected model. Make sure that we specify the random effects as normal.
 RBCNoBias.mod = BayesNonBiasCorrected(y=y.obs, s=s.obs, re.dist="normal", seed=seed)
 # Compute D measure using posterior samples for theta
 D.RBC = D.measure(RBC.mod.normal$theta.samples, RBCNoBias.mod$theta.samples) # D=0.95
Hackshaw1997
                        A Meta-Analysis on the Relationship Between Second-hand Tobacco
                        Smoke and Lung Cancer
```

Description

This data set contains 37 studies analyzed by Hackshaw et al. (1997). Hackshaw et al. (1997) evaluated the risk of developing lung cancer in women who were lifelong nonsmokers but whose husbands smoked, compared to women whose husbands had never smoked.

RobustBayesianCopas

Usage

data(Hackshaw1997)

Format

A dataframe with 37 studies with the following four variables within each study.

Study: Study identifier.

log_OR: The reported log-odds ratio. Use this as the treatment effect in meta-analysis.

SE: The reported standard error.

weight: The percent weight that the study contributes to the pooled log-odds ratio.

Source

Hackshaw, A. K., Law, M. R., and Wald, N. J. (1997). "The accumulated evidence on lung cancer and environmental tobacco smoke." *BMJ*, **315**(7114):980-988.

11

RobustBayesianCopas

Robust Bayesian Copas selection model

Description

This function implements the Robust Bayesian Copas selection model of Bai et al. (2020) for the Copas selection model,

$$y_i|(z_i > 0) = \theta + \tau u_i + s_i \epsilon_i,$$

$$z_i = \gamma_0 + \gamma_1/s_i + \delta_i,$$

$$corr(\epsilon_i, \delta_i) = \rho,$$

where y_i is the reported treatment effect for the *i*th study, s_i is the reported standard error for the *i*th study, θ is the population treatment effect of interest, $\tau > 0$ is a heterogeneity parameter, and ϵ_i , and δ_i are marginally distributed as N(0,1) and u_i , and ϵ_i are independent.

In the Copas selection model, y_i is published (selected) if and only if the corresponding propensity score z_i (or the propensity to publish) is greater than zero. The propensity score z_i contains two parameters: γ_0 controls the overall probability of publication, and γ_1 controls how the probability of publication depends on study sample size. The reported treatment effects and propensity scores are correlated through ρ . If $\rho=0$, then there is no publication bias and the Copas selection model reduces to the standard random effects meta-analysis model.

The RBC model places noninformative priors on $(\theta, \tau^2, \rho, \gamma_0, \gamma_1)$ (see Bai et al. (2020) for details). For the random effects $u_i, i = 1, \ldots, n$, we give the option for using normal, Student's t, Laplace, or slash distributions for the random effects. The function returns the Deviance Information Criterion (DIC), which can be used to select the appropriate distribution to use for the final analysis.

Usage

Arguments

у	An $n \times 1$ vector of reported treatment effects.
S	An $n \times 1$ vector of reported within-study standard errors.
re.dist	Distribution for the between-study random effects $u_i, i = 1,, n$. The user may specify the normal, Student's T, Laplace, or slash distribution. The default is StudentsT with 4 degrees of freedom.
t.df	Degrees of freedom for t-distribution. Only used if StudentsT is specified for re.dist. Default is 4.
slash.shape	Shape parameter in the slash distribution. Only used if slash is specified for re.dist. Default is 1.
init	Optional initialization values for $(\theta, \tau, \rho, \gamma_0, \gamma_1)$. If specified, they must be provided in this exact order. If they are not provided, the program estimates initial values from the data.
seed	Optional seed. This needs to be specified if you want to reproduce the exact results of your analysis.
burn	Number of burn-in samples. Default is burn=10000.
nmc	Number of posterior samples to save. Default is nmc=10000.

Value

The function returns a list containing the following components:

The function returns a list containing the following components:	
DIC	Deviance Information Criterion (DIC), a measure of model fit. This can be used to compare the results for different random effects distributions. The model that gives the lowest DIC gives the best fit to the data.
theta.hat	Posterior mean for θ .
theta.samples	MCMC samples for θ after burn-in. Used for plotting the posterior for θ and performing inference of θ .
tau.hat	Posterior mean for τ .
tau.samples	MCMC samples for τ after burn-in. Used for plotting the posterior for τ and performing inference of τ .
rho.hat	Posterior median for ρ .
rho.samples	MCMC samples for ρ after burn-in. Used for plotting the posterior for ρ and performing inference of ρ .
gamma0.hat	Posterior median for γ_0 .
gamma0.samples	MCMC samples for γ_0 after burn-in. Used for plotting the posterior for γ_0 and performing inference of γ_0 .
gamma1.hat	Posterior median for γ_1 .
gamma1.samples	MCMC samples for γ_1 after burn-in. Used for plotting the posterior for γ_1 and performing inference of γ_1 .

RobustBayesianCopas 13

References

Bai, R., Lin, L., Boland, M. R., and Chen, Y. (2020). "A robust Bayesian Copas selection model for quantifying and correcting publication bias." *arXiv preprint arXiv:2005.02930*.

```
# Example on the Barlow2014 data set #
# Load data
data(Barlow2014)
attach(Barlow2014)
# Observed treatment effect
v.obs = Barlow2014[,1]
# Observed standard error
s.obs = Barlow2014[,2]
# Fit the RBC model with slash random effects #
# NOTE: Use default burn-in (burn=10000) and post-burn-in samples (nmc=10000)
# Fit model with slash errors
RBC.mod = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="slash", burn=500, nmc=500)
# Point estimate for rho
rho.hat.RBC = RBC.mod$rho.hat
rho.hat.RBC
# Plot posterior for rho
hist(RBC.mod$rho.samples)
# Point estimate for theta
theta.hat.RBC = RBC.mod$theta.hat
# Standard error for theta
theta.se.RBC = sd(RBC.mod\$theta.samples)
# 95% posterior credible interval for theta
theta.cred.int = quantile(RBC.mod$theta.samples, probs=c(0.025,0.975))
# Display results
theta.hat.RBC
theta.se.RBC
theta.cred.int
# Plot the posterior for theta
hist(RBC.mod$theta.samples)
# Example on second-hand smoking data set. #
# This is from Section 6.1 of the paper by #
```

```
# Bai et al. (2020).
# Set seed, so we can reproduce the exact same result as in the paper.
seed = 1234
set.seed(seed)
# Load the full data
data(Hackshaw1997)
attach(Hackshaw1997)
# Extract the log OR
y.obs = Hackshaw1997[,2]
# Extract the observed standard error
s.obs = Hackshaw1997[,3]
# Fit the RBC model with different random effects #
# distributions and compare them using the DIC.
RBC.mod.normal = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="normal", seed=seed)
RBC.mod.normal$DIC # DIC=429.7854
# Student's t
RBC.mod.StudentsT = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="StudentsT", seed=seed)
RBC.mod.StudentsT$DIC # DIC=399.1955
# Laplace
RBC.mod.Laplace = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="Laplace", seed=seed)
RBC.mod.Laplace$DIC # DIC=410.9086
RBC.mod.slash = RobustBayesianCopas(y=y.obs, s=s.obs, re.dist="slash", seed=seed)
RBC.mod.slash$DIC # DIC=407.431
# Use the model with t-distributed random errors for #
# the final analysis since it gave the lowest DIC.
# Point estimate for rho
rho.hat.RBC = RBC.mod.StudentsT$rho.hat # rho.hat=0.459 (moderate publication bias)
# Plot posterior for rho
hist(RBC.mod.StudentsT$rho.samples)
# Point estimate for theta
theta.hat.RBC = RBC.mod.StudentsT$theta.hat # theta.hat=0.1672
# 95% posterior credible interval for theta
theta.cred.int = quantile(RBC.mod.StudentsT$theta.samples, probs=c(0.025,0.975))
# Plot the posterior for theta
hist(RBC.mod.StudentsT$theta.samples)
# Obtain odds ratio estimates
```

StandardMetaAnalysis 15

StandardMetaAnalysis Standard meta-analysis

Description

This function performs maximum likelihood estimation (MLE) of (θ, τ) for the standard random effects meta-analysis model,

$$y_i = \theta + \tau u_i + s_i \epsilon_i,$$

where y_i is the reported treatment effect for the *i*th study, s_i is the reported standard error for the *i*th study, θ is the population treatment effect of interest, $\tau > 0$ is a heterogeneity parameter, and u_i and ϵ_i are independent and distributed as N(0,1).

Usage

```
StandardMetaAnalysis(y, s, init = NULL, tol=1e-10, maxit=1000)
```

Arguments

У	An $n \times 1$ vector of reported treatment effects.
S	An $n \times 1$ vector of reported within-study standard errors.
init	Optional initialization values for (θ, τ) . If specified, they must be provided in this order. If they are not provided, the program estimates initial values from the data.
tol	Convergence criterion for the optimization algorithm for finding the MLE. Default is tol=1e-10.
maxit	Maximum number of iterations for the optimization algorithm for finding the MLE. Default is maxit=1000.

Value

The function returns a list containing the following components:

theta.hat MLE of θ . tau.hat MLE of τ .

H 2×2 Hessian matrix for the estimates of (θ, τ) . The square root of the diagonal

entries of H can be used to estimate the standard errors for (θ, τ) .

conv "1" if the optimization algorithm converged, "0" if algorithm did not converge.

If conv=0, then using H to estimate the standard errors may not be reliable.

References

Bai, R., Lin, L., Boland, M. R., and Chen, Y. (2020). "A robust Bayesian Copas selection model for quantifying and correcting publication bias." *arXiv preprint arXiv:2005.02930*.

Ning, J., Chen, Y., and Piao, J. (2017). "Maximum likelihood estimation and EM algorithm of Copas-like selection model for publication bias correction." *Biostatistics*, **18**(3):495-504.

```
# Example on the antidepressants data set. #
# This is from Section 6.2 of the paper by #
# Bai et al. (2020).
# Load the full data
data(antidepressants)
attach(antidepressants)
# Extract the 50 published studies
published.data = antidepressants[which(antidepressants$Published==1),]
# Observed treatment effect
y.obs = published.data$Standardized_effect_size
# Observed standard error
s.obs = published.data$Standardized_SE
####################################
# Fit a standard meta-analysis #
# that ignores publication bias #
# Set seed
set.seed(123)
SMA.mod = StandardMetaAnalysis(y=y.obs, s=s.obs)
# Point estimate for theta
SMA.theta.hat = SMA.mod$theta.hat
# Use Hessian to estimate standard error for theta
SMA.Hessian = SMA.mod$H
```

```
# Standard error estimate for theta
SMA.theta.se = sqrt(SMA.Hessian[1,1])
# 95 percent confidence interval
SMA.interval = c(SMA.theta.hat-1.96*SMA.theta.se, SMA.theta.hat+1.96*SMA.theta.se)
# Display results
SMA.theta.hat
SMA.theta.se
SMA.interval
```

17

Index

```
antidepressants, 2
Barlow2014, 3
BayesNonBiasCorrected, 3
CopasLikeSelection, 5
D.measure, 8
Hackshaw1997, 10
RobustBayesianCopas, 11
StandardMetaAnalysis, 15
```