Package 'blockmodels'

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BM_bernoulli

Perform estimation on blockmodels for bernoulli probability distribution

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## S4 method for signature 'new'
BM_bernoulli(
    membership_type,
    adj,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

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exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration_factor of the object.

explore_min

Explore to the explore_min number of groups even if the exploration_factor rule is satisfied. By default 4. This parameter can be changed by accessing the field \$explore_min of the object.

explore_max

Stop exploration after explore_max number of group in any case. By default Inf. This parameter can be changed by accessing the field \$explore_max of the object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * 0 # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
P<-matrix(runif(Q*Q),Q,Q)
M<-1*(matrix(runif(n*n),n,n)<Z%*%P%*%t(Z)) ## adjacency matrix
## estimation
my_model <- BM_bernoulli("SBM",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## SBM symmetric
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
```

```
n <- npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
P<-matrix(runif(Q*Q),Q,Q)
P[lower.tri(P)]<-t(P)[lower.tri(P)]
M<-1*(matrix(runif(n*n),n,n)<Z%*%P%*%t(Z)) ## adjacency matrix
M[lower.tri(M)]<-t(M)[lower.tri(M)]</pre>
## estimation
my_model <- BM_bernoulli("SBM_sym",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q \leftarrow c(2,3) \# classes
n \leftarrow npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
P<-matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
 M<-1*(matrix(runif(n[1]*n[2]),n[1],n[2])< Z1\%*\%P\%*\%t(Z2)) \ \#\# \ adjacency \ matrix \} 
## estimation
my_model <- BM_bernoulli("LBM",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

BM_bernoulli_covariates

Perform estimation on blockmodels for bernoulli probability distribution aith covariates

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership, and impact vector of covariates.

Usage

```
## $4 method for signature 'new'
BM_bernoulli_covariates(
    membership_type,
    adj,
    covariates,
    verbosity=6,
```

```
autosave='',
plotting=character(0),
exploration_factor=1.5,
exploration_direction=numeric(0),
explore_min=4,
explore_max=Inf,
ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

covariates Covariates matrix, or list of covariates matrices. Covariates matrix must have

the same size than the adjacency matrix.

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave If autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$explo-

ration factor of the object.

explore_min Explore to the explore_min number of groups even if the exploration_factor rule

is satisfied. By default 4. This parameter can be changed by accessing the field

\$explore_min of the object.

explore_max Stop exploration after explore_max number of group in any case. By default

Inf. This parameter can be changed by accessing the field \$explore_max of the

object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided

group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
sigmo <- function(x){1/(1+exp(-x))}
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mg<-8*matrix(runif(Q*Q),Q,Q)-4
Y1 <- matrix(runif(n*n),n,n)-.5
Y2 <- matrix(runif(n*n),n,n)-.5
M_in_expectation < -sigmo(Z%*%Mg%*%t(Z) + 5*Y1-3*Y2)
M<-1*(matrix(runif(n*n),n,n)<M_in_expectation)</pre>
## estimation
my_model <- BM_bernoulli_covariates("SBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
##
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
sigmo \leftarrow function(x)\{1/(1+exp(-x))\}
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mg<-8*matrix(runif(Q*Q),Q,Q)-4
Mg[lower.tri(Mg)]<-t(Mg)[lower.tri(Mg)]</pre>
Y1 <- matrix(runif(n*n),n,n)-.5
Y2 <- matrix(runif(n*n),n,n)-.5
Y1[lower.tri(Y1)]<-t(Y1)[lower.tri(Y1)]
Y2[lower.tri(Y2)]<-t(Y2)[lower.tri(Y2)]
M_in_expectation < -sigmo(Z%*%Mg%*%t(Z) + 5*Y1-3*Y2)
M<-1*(matrix(runif(n*n),n,n)<M_in_expectation)</pre>
```

```
M[lower.tri(M)]<-t(M)[lower.tri(M)]
## estimation
my_model <- BM_bernoulli_covariates("SBM_sym",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q <- c(2,3) # classes
n <- npc * Q # nodes
sigmo \leftarrow function(x)\{1/(1+exp(-x))\}
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
Mg<-8*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])-4
Y1 <- matrix(runif(n[1]*n[2]),n[1],n[2])-.5
Y2 \leftarrow matrix(runif(n[1]*n[2]),n[1],n[2])-.5
\label{eq:m_in_expectation} $$M_in_expectation <-sigmo(Z1%*%Mg%*%t(Z2) + 5*Y1-3*Y2)$
M<-1*(matrix(runif(n[1]*n[2]),n[1],n[2])<M_in_expectation)
## estimation
my_model <- BM_bernoulli_covariates("LBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

BM_bernoulli_covariates_fast

Perform estimation on blockmodels for bernoulli probability distribution aith covariates

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership, and impact vector of covariates.

Usage

```
## S4 method for signature 'new'
BM_bernoulli_covariates_fast(
    membership_type,
    adj,
    covariates,
```

```
verbosity=6,
autosave='',
plotting=character(0),
exploration_factor=1.5,
exploration_direction=numeric(0),
explore_min=4,
explore_max=Inf,
ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

covariates Covariates matrix, or list of covariates matrices. Covariates matrix must have

the same size than the adjacency matrix.

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0) (the default), plots are done on screen, if plotting==", no plot are done, if plot-

ting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$explo-

ration_factor of the object.

explore_min Explore to the explore_min number of groups even if the exploration_factor rule

is satisfied. By default 4. This parameter can be changed by accessing the field

\$explore_min of the object.

explore_max Stop exploration after explore_max number of group in any case. By default

Inf. This parameter can be changed by accessing the field \$explore_max of the

object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided

group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
sigmo <- function(x){1/(1+exp(-x))}
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mg<-8*matrix(runif(Q*Q),Q,Q)-4
Y1 <- matrix(runif(n*n),n,n)-.5
Y2 \leftarrow matrix(runif(n*n),n,n)-.5
\label{eq:m_in_expectation} $$M_in_expectation <-sigmo(Z%*%Mg%*%t(Z) + 5*Y1-3*Y2)$
M<-1*(matrix(runif(n*n),n,n)<M_in_expectation)</pre>
## estimation
my_model <- BM_bernoulli_covariates_fast("SBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
##
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
sigmo \leftarrow function(x)\{1/(1+exp(-x))\}
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mg<-8*matrix(runif(Q*Q),Q,Q)-4
Mg[lower.tri(Mg)]<-t(Mg)[lower.tri(Mg)]</pre>
Y1 <- matrix(runif(n*n),n,n)-.5
Y2 <- matrix(runif(n*n),n,n)-.5
Y1[lower.tri(Y1)]<-t(Y1)[lower.tri(Y1)]
Y2[lower.tri(Y2)]<-t(Y2)[lower.tri(Y2)]
M_in_expectation < -sigmo(Z%*%Mg%*%t(Z) + 5*Y1-3*Y2)
M<-1*(matrix(runif(n*n),n,n)<M_in_expectation)</pre>
```

```
M[lower.tri(M)]<-t(M)[lower.tri(M)]
## estimation
my_model <- BM_bernoulli_covariates_fast("SBM_sym",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q <- c(2,3) # classes
n <- npc * Q # nodes
sigmo \leftarrow function(x)\{1/(1+exp(-x))\}
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
Mg<-8*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])-4
Y1 <- matrix(runif(n[1]*n[2]),n[1],n[2])-.5
Y2 \leftarrow matrix(runif(n[1]*n[2]),n[1],n[2])-.5
M_in_expectation < -sigmo(Z1%*%Mg%*%t(Z2) + 5*Y1-3*Y2)
M<-1*(matrix(runif(n[1]*n[2]),n[1],n[2])<M_in_expectation)
## estimation
my_model <- BM_bernoulli_covariates_fast("LBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

BM_bernoulli_multiplex

Perform estimation on blockmodels for multiplex binary networks

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## S4 method for signature 'new'
BM_bernoulli_multiplex(
    membership_type,
    adj,
    verbosity=6,
```

```
autosave='',
plotting=character(0),
exploration_factor=1.5,
exploration_direction=numeric(0),
explore_min=4,
explore_max=Inf,
ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The list of adjacency matrices. All matrices must have the same size

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration factor.

ration_factor of the object.

explore_min Explore to the explore_min number of groups even if the exploration_factor rule

is satisfied. By default 4. This parameter can be changed by accessing the field

\$explore_min of the object.

explore_max Stop exploration after explore_max number of group in any case. By default

Inf. This parameter can be changed by accessing the field \$explore_max of the

object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group

number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n <- npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
P00<-matrix(runif(Q*Q),Q,Q)
P10 < -matrix(runif(0*0),0,0)
P01<-matrix(runif(Q*Q),Q,Q)
P11<-matrix(runif(Q*Q),Q,Q)
SumP<-P00+P10+P01+P11
P00<-P00/SumP
P01<-P01/SumP
P10<-P10/SumP
P11<-P11/SumP
MU<-matrix(runif(n*n),n,n)
M1<-1*(MU>Z%*%(P00+P01)%*%t(Z))
M2<-1*((MU>Z%*%P00%*%t(Z)) & (MU<Z%*%(P00+P01+P11)%*%t(Z))) ## adjacency matrices
## estimation
my_model <- BM_bernoulli_multiplex("SBM",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## SBM symmetric
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
P00<-matrix(runif(Q*Q),Q,Q)
P10<-matrix(runif(Q*Q),Q,Q)
P01<-matrix(runif(Q*Q),Q,Q)
P11<-matrix(runif(Q*Q),Q,Q)
SumP<-P00+P10+P01+P11
```

```
P00<-P00/SumP
 P01<-P01/SumP
P10<-P10/SumP
P11<-P11/SumP
P00[lower.tri(P00)]<-t(P00)[lower.tri(P00)]
P01[lower.tri(P01)]<-t(P01)[lower.tri(P01)]
P10[lower.tri(P10)]<-t(P10)[lower.tri(P10)]
P11[lower.tri(P11)]<-t(P11)[lower.tri(P11)]
MU<-matrix(runif(n*n),n,n)
MU[lower.tri(MU)]<-t(MU)[lower.tri(MU)]
M1<-1*(MU>Z%*%(P00+P01)%*%t(Z))
 \texttt{M2} < -1 \times ((\texttt{MU} \times \texttt{Z}\% \times \texttt{P00} \% \times \texttt{xt}(\texttt{Z})) \ \& \ (\texttt{MU} < \texttt{Z}\% \times \texttt{X}(\texttt{P00} + \texttt{P01} + \texttt{P11}) \% \times \texttt{xt}(\texttt{Z}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{MU} \times \texttt{Z}\% \times \texttt{P00} \times \texttt{M2} \times \texttt{M2})) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{MU} \times \texttt{Z}\% \times \texttt{P00} \times \texttt{M2} \times \texttt{M2}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{MU} \times \texttt{Z}\% \times \texttt{M2} \times \texttt{M2}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{MU} \times \texttt{Z}\% \times \texttt{M2} \times \texttt{M2}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2})) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}))) \ \# \# \ adjacency \ matrices \ \# \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2})) \ \# \ \# \ (\texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M2} \times \texttt{M2} \times \texttt{M2}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times \texttt{M3}) \ \# \ (\texttt{M3} \times \texttt{M3} \times
 ## estimation
 my_model <- BM_bernoulli_multiplex("SBM_sym",list(M1,M2) )</pre>
 my_model$estimate()
 which.max(my_model$ICL)
 ##
 ## LBM
 ##
 ## generation of one LBM network
 npc \leftarrow c(50,40) \# nodes per class
 Q \leftarrow c(2,3) \# classes
n <- npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
 Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
P00<-matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
P10<-matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
P01<-matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
P11<-matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
 SumP<-P00+P10+P01+P11
 P00<-P00/SumP
P01<-P01/SumP
P10<-P10/SumP
P11<-P11/SumP
MU<-matrix(runif(n[1]*n[2]),n[1],n[2])</pre>
M1<-1*(MU>Z1%*%(P00+P01)%*%t(Z2))
 \texttt{M2} < -1 \times ((\texttt{MU} \times \texttt{Z1}\% \times \texttt{P00}\% \times \texttt{Xt}(\texttt{Z2})) \ \& \ (\texttt{MU} < \texttt{Z1}\% \times \texttt{X}(\texttt{P00} + \texttt{P01} + \texttt{P11})\% \times \texttt{Xt}(\texttt{Z2}))) \ \# \ adjacency \ matrices \ \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M2} < -1 \times ((\texttt{M2} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M2} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M2}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3}))) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ matrices \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ \texttt{M3} < -1 \times ((\texttt{M3} \times \texttt{M3})) \ \# \ adjacency \ \texttt{M3} < 
 ## estimation
 my_model <- BM_bernoulli_multiplex("LBM",list(M1,M2) )</pre>
 my_model$estimate()
 which.max(my_model$ICL)
 ## End(Not run)
```

14 BM_gaussian

BM_gaussian	Perform estimation on blockmodels for gaussian probability distribution
-------------	---

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## $4 method for signature 'new'
BM_gaussian(
    membership_type,
    adj,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave If autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

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exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration_factor of the object.

explore_min

Explore to the explore_min number of groups even if the exploration_factor rule is satisfied. By default 4. This parameter can be changed by accessing the field \$explore_min of the object.

explore_max

Stop exploration after explore_max number of group in any case. By default Inf. This parameter can be changed by accessing the field \$explore_max of the object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * 0 # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu < -20 * matrix(runif(Q*Q),Q,Q)
M<-matrix(rnorm(n*n,sd=10),n,n)+Z%*%Mu%*%t(Z) ## adjacency matrix
## estimation
my_model <- BM_gaussian("SBM",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## SBM symmetric
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
```

```
n <- npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu<-20*matrix(runif(Q*Q),Q,Q)
Mu[lower.tri(Mu)]<-t(Mu)[lower.tri(Mu)]</pre>
M<-matrix(rnorm(n*n,sd=10),n,n)+Z%*%Mu%*%t(Z) ## adjacency matrix
M[lower.tri(M)]<-t(M)[lower.tri(M)]</pre>
## estimation
my_model <- BM_gaussian("SBM_sym",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q \leftarrow c(2,3) \# classes
n \leftarrow npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
Mu<-20*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
## estimation
my_model <- BM_gaussian("LBM",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

BM_gaussian_covariates

Perform estimation on blockmodels for gaussian probability distribution with covariates

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership and impact vector of covariates

Usage

```
## S4 method for signature 'new'
BM_gaussian_covariates(
    membership_type,
    adj,
    covariates,
    verbosity=6,
```

```
autosave='',
plotting=character(0),
exploration_factor=1.5,
exploration_direction=numeric(0),
explore_min=4,
explore_max=Inf,
ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

covariates Covariates matrix, or list of covariates matrices. Covariates matrix must have

the same size than the adjacency matrix.

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$explo-

ration factor of the object.

explore_min Explore to the explore_min number of groups even if the exploration_factor rule

is satisfied. By default 4. This parameter can be changed by accessing the field

\$explore_min of the object.

explore_max Stop exploration after explore_max number of group in any case. By default

Inf. This parameter can be changed by accessing the field \$explore_max of the

object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided

group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu<-20*matrix(runif(Q*Q),Q,Q)
Y1 <- matrix(runif(n*n),n,n)
Y2 <- matrix(runif(n*n),n,n)
M<-matrix(rnorm(n*n,sd=5),n,n)+Z%*%Mu%*%t(Z)+4.2*Y1-1.6*Y2 ## adjacency matrix
## estimation
my_model <- BM_gaussian_covariates("SBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu<-20*matrix(runif(Q*Q),Q,Q)
Mu[lower.tri(Mu)]<-t(Mu)[lower.tri(Mu)]</pre>
Y1 <- matrix(runif(n*n),n,n)
Y2 <- matrix(runif(n*n),n,n)
Y1[lower.tri(Y1)]<-t(Y1)[lower.tri(Y1)]
Y2[lower.tri(Y2)]<-t(Y2)[lower.tri(Y2)]
M<-matrix(rnorm(n*n,sd=5),n,n)+Z%*%Mu%*%t(Z)+4.2*Y1-1.6*Y2 ## adjacency matrix
M[lower.tri(M)]<-t(M)[lower.tri(M)]
## estimation
my_model <- BM_gaussian_covariates("SBM_sym",M,list(Y1,Y2) )</pre>
my_model$estimate()
```

```
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q <- c(2,3) # classes
n <- npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
Mu<-20*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
Y1 <- matrix(runif(n[1]*n[2]),n[1],n[2])
Y2 <- matrix(runif(n[1]*n[2]),n[1],n[2])
 \texttt{M<-matrix(rnorm(n[1]*n[2],sd=5),n[1],n[2])+Z1\%*\%Mu\%*\%t(Z2)+4.2*Y1-1.6*Y2~\# adjacency~matrix ) } \\
## estimation
my_model <- BM_gaussian_covariates("LBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

BM_gaussian_multivariate

Perform estimation on blockmodels for multivariate gaussian probability distribution

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## $4 method for signature 'new'
BM_gaussian_multivariate(
    membership_type,
    adj,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The list of adjacency matrices. All matrices must have the same size

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave If autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$explo-

ration_factor of the object.

explore_min Explore to the explore_min number of groups even if the exploration_factor rule

is satisfied. By default 4. This parameter can be changed by accessing the field

\$explore_min of the object.

explore_max Stop exploration after explore_max number of group in any case. By default

Inf. This parameter can be changed by accessing the field \$explore_max of the

object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group

number and the column group number.

ncores Number of parallel jobs to launch different EM intializations. By default de-

tectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested

on *BSD.)

Examples

Not run:

```
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu1<-4*matrix(runif(Q*Q),Q,Q)
Mu2 < -4*matrix(runif(Q*Q),Q,Q)
Noise1<-matrix(rnorm(n*n,sd=1),n,n)
Noise2<-matrix(rnorm(n*n,sd=1),n,n)
M1 < - Z%*Mu1%*%t(Z) + Noise1
M2 < - Z%*%Mu2%*%t(Z) + 10*Noise1 + Noise2
## estimation
my_model <- BM_gaussian_multivariate("SBM",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## SBM symmetric
##
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n <- npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu1 < -4*matrix(runif(Q*Q),Q,Q)
Mu2<-4*matrix(runif(Q*Q),Q,Q)
Noise1<-matrix(rnorm(n*n,sd=1),n,n)
Noise2<-matrix(rnorm(n*n,sd=1),n,n)
M1 < - Z%*%Mu1%*%t(Z) + Noise1
M2 < - Z%*%Mu2%*%t(Z) + 10*Noise1 + Noise2
M1[lower.tri(M1)]<-t(M1)[lower.tri(M1)]
M2[lower.tri(M2)]<-t(M2)[lower.tri(M2)]
## estimation
my_model <- BM_gaussian_multivariate("SBM_sym",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q \leftarrow c(2,3) \# classes
n \leftarrow npc * Q # nodes
```

```
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)
Mu1<-4*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
Mu2<-4*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
Noise1<-matrix(rnorm(n[1]*n[2],sd=1),n[1],n[2])
Noise2<-matrix(rnorm(n[1]*n[2],sd=1),n[1],n[2])
M1<-Z1%*%Mu1%*%t(Z2) + Noise1 ## adjacency
M2<-Z1%*%Mu2%**xt(Z2) + 10*Noise1 + Noise2 ## adjacency
## estimation
my_model <- BM_gaussian_multivariate("LBM",list(M1,M2) )
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)</pre>
```

BM_gaussian_multivariate_independent

Perform estimation on blockmodels for multivariate independent homoscedastic gaussian probability distribution

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## $4 method for signature 'new'
BM_gaussian_multivariate_independent(
    membership_type,
    adj,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

```
membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj

The list of adjacency matrices. All matrices must have the same size
```

verbosity

The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization. Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to the field \$verbosity of the object.

autosave

If *autosave* != ", after each estimation, the model object is writed into file *autosave*. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can be changed by accessing to the field \$autosave of the object.

plotting

Control plot of ICL values while the estimation is running. If plotting==character(0) (the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration_factor of the object.

explore_min

Explore to the explore_min number of groups even if the exploration_factor rule is satisfied. By default 4. This parameter can be changed by accessing the field \$explore_min of the object.

explore_max

Stop exploration after explore_max number of group in any case. By default Inf. This parameter can be changed by accessing the field \$explore_max of the object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

Examples

Not run:

##

SBM

##

```
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu1 < -8 * matrix(runif(Q*Q),Q,Q)
Mu2<-8*matrix(runif(Q*Q),Q,Q)
M1<-matrix(rnorm(n*n,sd=5),n,n)+Z%*%Mu1%*%t(Z) ## adjacency
M2 < -matrix(rnorm(n*n,sd=10),n,n) + Z%*%Mu2%*%t(Z) ## adjacency
## estimation
my_model <- BM_gaussian_multivariate_independent("SBM",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
##
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu1 < -8*matrix(runif(Q*Q),Q,Q)
Mu2 < -8*matrix(runif(Q*Q),Q,Q)
Mu1[lower.tri(Mu1)]<-t(Mu1)[lower.tri(Mu1)]</pre>
Mu2[lower.tri(Mu2)]<-t(Mu2)[lower.tri(Mu2)]
M1<-matrix(rnorm(n*n,sd=5),n,n)+Z%*%Mu1%*%t(Z) ## adjacency
M2 < -matrix(rnorm(n*n,sd=10),n,n) + Z%*%Mu2%*%t(Z) ## adjacency
M1[lower.tri(M1)]<-t(M1)[lower.tri(M1)]
M2[lower.tri(M2)]<-t(M2)[lower.tri(M2)]
## estimation
my_model <- BM_gaussian_multivariate_independent("SBM_sym",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q \leftarrow c(2,3) \# classes
n \leftarrow npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
Mu1<-8*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
Mu2<-8*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
 \texttt{M1} < -\texttt{matrix}(\texttt{rnorm}(\texttt{n[1]*n[2]}, \texttt{sd=5}), \texttt{n[1]}, \texttt{n[2]}) + \texttt{Z1}\% * \% \texttt{Mu1}\% * \% \texttt{t(Z2)} \ \#\# \ \texttt{adjacency} 
M2 < -matrix(rnorm(n[1]*n[2], sd=10), n[1], n[2]) + Z1%*%Mu2%*%t(Z2) ## adjacency
```

```
## estimation
my_model <- BM_gaussian_multivariate_independent("LBM",list(M1,M2) )
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)</pre>
```

BM_gaussian_multivariate_independent_homoscedastic

Perform estimation on blockmodels for multivariate independent homoscedastic gaussian probability distribution

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## S4 method for signature 'new'
BM_gaussian_multivariate_independent_homoscedastic(
    membership_type,
    adj,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj

The list of adjacency matrices. All matrices must have the same size

verbosity

The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization. Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to the field \$verbosity of the object.

autosave

If *autosave* != ", after each estimation, the model object is writed into file *autosave*. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can be changed by accessing to the field \$autosave of the object.

plotting

Control plot of ICL values while the estimation is running. If plotting==character(0) (the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration_factor of the object.

explore_min

Explore to the explore_min number of groups even if the exploration_factor rule is satisfied. By default 4. This parameter can be changed by accessing the field \$explore_min of the object.

explore_max

Stop exploration after explore_max number of group in any case. By default Inf. This parameter can be changed by accessing the field \$explore_max of the object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
##
## SBM
##
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n <- npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)
Mu1<-4*matrix(runif(Q*Q),Q,Q)
Mu2<-4*matrix(runif(Q*Q),Q,Q)
M1<-matrix(rnorm(n*n,sd=5),n,n)+Z%*%Mu1%*%t(Z) ## adjacency
M2<-matrix(rnorm(n*n,sd=5),n,n)+Z%*%Mu2%*%t(Z) ## adjacency</pre>
```

```
## estimation
my_model <- BM_gaussian_multivariate_independent_homoscedastic("SBM",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
##
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n <- npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
Mu1<-4*matrix(runif(Q*Q),Q,Q)
Mu2 < -4*matrix(runif(Q*Q),Q,Q)
Mu1[lower.tri(Mu1)]<-t(Mu1)[lower.tri(Mu1)]
Mu2[lower.tri(Mu2)]<-t(Mu2)[lower.tri(Mu2)]
M1 < -matrix(rnorm(n*n,sd=5),n,n) + Z%*%Mu1%*%t(Z) ## adjacency
M2 < -matrix(rnorm(n*n,sd=5),n,n) + Z\% *\% Mu2\% *\% t(Z) ## adjacency
M1[lower.tri(M1)]<-t(M1)[lower.tri(M1)]
M2[lower.tri(M2)]<-t(M2)[lower.tri(M2)]
## estimation
my_model <- BM_gaussian_multivariate_independent_homoscedastic("SBM_sym",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q <- c(2,3) # classes
n \leftarrow npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
Mu1<-4*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
Mu2<-4*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
M1<-matrix(rnorm(n[1]*n[2],sd=5),n[1],n[2])+Z1%*%Mu1%*%t(Z2) ## adjacency
\label{eq:matrix} $$M2<-matrix(rnorm(n[1]*n[2],sd=5),n[1],n[2])+Z1%*$$Mu2%*$$t(Z2) $$\#$ adjacency $$Mu2\%*$$t(Z2) $$Mu2\%*$$t(
## estimation
my_model <- BM_gaussian_multivariate_independent_homoscedastic("LBM",list(M1,M2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

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BM_poisson Perform estimation on blockmodels for poisson probation	bility distribu-
--	------------------

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership

Usage

```
## S4 method for signature 'new'
BM_poisson(
    membership_type,
    adj,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave If autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

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exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration_factor of the object.

explore_min

Explore to the explore_min number of groups even if the exploration_factor rule is satisfied. By default 4. This parameter can be changed by accessing the field \$explore_min of the object.

explore_max

Stop exploration after explore_max number of group in any case. By default Inf. This parameter can be changed by accessing the field \$explore_max of the object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group number and the column group number.

ncores

Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested on *BSD.)

```
## Not run:
# SBM
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * 0 # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
L<-70*matrix(runif(Q*Q),Q,Q)
M_in_expectation<-Z%*%L%*%t(Z)
M<-matrix(
    rpois(
        length(as.vector(M_in_expectation)),
        as.vector(M_in_expectation))
    ,n,n)
## estimation
my_model <- BM_poisson("SBM",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
```

```
##
## generation of one SBM_sym network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
L<-70*matrix(runif(Q*Q),Q,Q)
L[lower.tri(L)]<-t(L)[lower.tri(L)]</pre>
M_in_expectation<-Z%*%L%*%t(Z)</pre>
M<-matrix(
    rpois(
        length(as.vector(M_in_expectation)),
        as.vector(M_in_expectation))
    ,n,n)
M[lower.tri(M)]<-t(M)[lower.tri(M)]
## estimation
my_model <- BM_poisson("SBM_sym",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q <- c(2,3) # classes
n <- npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
L<-70*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
M_in_expectation<-Z1%*%L%*%t(Z2)
M<-matrix(
    rpois(
        length(as.vector(M_in_expectation)),
        as.vector(M_in_expectation))
    ,n[1],n[2])
## estimation
my_model <- BM_poisson("LBM",M )</pre>
my_model$estimate()
which.max(my_model$ICL)
## End(Not run)
```

Description

With the provided network and blockmodel type, estimate number of groups, parameters and node membership, and impact vector of covariates

Usage

```
## S4 method for signature 'new'
BM_poisson_covariates(
    membership_type,
    adj,
    covariates,
    verbosity=6,
    autosave='',
    plotting=character(0),
    exploration_factor=1.5,
    exploration_direction=numeric(0),
    explore_min=4,
    explore_max=Inf,
    ncores=detectCores())
```

Arguments

membership_type

The type of node membership, i.e. 'SBM', 'SBM_sym' or 'LBM'

adj The adjacency matrix

covariates Covariates matrix, or list of covariates matrices. Covariates matrix must have

the same size than the adjacency matrix.

verbosity The verbosity level, 0 means quiet. Level 1 display the phase of reinitialization.

Level 2 display the level 1 and the ascending and descending phase for the number of groups. Level 3 display the level 2 and the number current number of groups which is estimated. Level 4 display the level 3 and the steps inside the estimation. Level 5 display the level 4, the current status of parallel running jobs and the current sub-step. Level 6 display level 5 and informations about ICL criteria found. Default is level 6. This parameter can be changed by accessing to

the field \$verbosity of the object.

autosave If autosave != ", after each estimation, the model object is writed into file au-

tosave. The model object is readable by the function *readRDS*. Use-it for long computation to allow restarting the estimation on system crash. You can use it to alanyze the partial results when the estimation is running. This parameter can

be changed by accessing to the field \$autosave of the object.

plotting Control plot of ICL values while the estimation is running. If plotting==character(0)

(the default), plots are done on screen, if plotting==", no plot are done, if plotting is a filename, plots are done in this filename. This parameter can be changed

by accessing the field \$plotting of the object.

exploration_factor

Control the exploration of the number of groups. The exploration is stop when the number of groups reach exploration factor times the current maximum. By default 1.5. This parameter can be changed by accessing the field \$exploration_factor of the object.

explore_min Explore to the explore_min number of groups even if the exploration_factor rule

is satisfied. By default 4. This parameter can be changed by accessing the field

\$explore_min of the object.

explore_max Stop exploration after explore_max number of group in any case. By default

Inf. This parameter can be changed by accessing the field \$explore_max of the

object.

exploration_direction

Only for LBM membership. Control the exploration direction for groups number. When provided, the exploring strategy is made to explore the provided group number. Must be a vector of two integer value representing the row group

number and the column group number.

ncores Number of parallel jobs to launch different EM intializations. By default detectCores(). This parameter can be changed by accessing the field \$ncores of

the object. This parameter can be changed by accessing the field shoores of the object. This parameters is used only on Linux. Parallism is disabled on other plateform. (Not working on Windows, not tested on Mac OS, not tested

on *BSD.)

```
## Not run:
##
## SBM
## generation of one SBM network
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
L<-70*matrix(runif(Q*Q),Q,Q)
M_in_expectation_without_covariates<-Z%*%L%*%t(Z)
Y1 <- matrix(runif(n*n),n,n)
Y2 <- matrix(runif(n*n),n,n)
M_in_expectation<-M_in_expectation_without_covariates*exp(4.2*Y1-1.2*Y2)
M<-matrix(
    rpois(
        length(as.vector(M_in_expectation)),
        as.vector(M_in_expectation))
    ,n,n)
## estimation
my_model <- BM_poisson_covariates("SBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
## SBM symmetric
```

##

```
## generation of one SBM_sym network, we re-use one produced for SBM
npc <- 30 # nodes per class
Q <- 3 # classes
n \leftarrow npc * Q # nodes
Z<-diag(Q)%x%matrix(1,npc,1)</pre>
L<-70*matrix(runif(Q*Q),Q,Q)
L[lower.tri(L)]<-t(L)[lower.tri(L)]
M_in_expectation_without_covariates<-Z%*%L%*%t(Z)</pre>
Y1 <- matrix(runif(n*n),n,n)
Y2 <- matrix(runif(n*n),n,n)
Y1[lower.tri(Y1)]<-t(Y1)[lower.tri(Y1)]
Y2[lower.tri(Y2)]<-t(Y2)[lower.tri(Y2)]
M_in_expectation<-M_in_expectation_without_covariates*exp(4.2*Y1-1.2*Y2)
M<-matrix(
    rpois(
        length(as.vector(M_in_expectation)),
        as.vector(M_in_expectation))
M[lower.tri(M)]<-t(M)[lower.tri(M)]
## estimation
my_model <- BM_poisson_covariates("SBM_sym",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
##
## LBM
##
## generation of one LBM network
npc <- c(50,40) \# nodes per class
Q \leftarrow c(2,3) \# classes
n <- npc * Q # nodes
Z1<-diag(Q[1])%x%matrix(1,npc[1],1)</pre>
Z2<-diag(Q[2])%x%matrix(1,npc[2],1)</pre>
L<-70*matrix(runif(Q[1]*Q[2]),Q[1],Q[2])
M_in_expectation_without_covariates<-Z1%*%L%*%t(Z2)
Y1 <- matrix(runif(n[1]*n[2]),n[1],n[2])
Y2 <- matrix(runif(n[1]*n[2]),n[1],n[2])
M_in_expectation<-M_in_expectation_without_covariates*exp(4.2*Y1-1.2*Y2)
M<-matrix(
    rpois(
        length(as.vector(M_in_expectation)),
        as.vector(M_in_expectation))
    ,n[1],n[2])
## estimation
my_model <- BM_poisson_covariates("LBM",M,list(Y1,Y2) )</pre>
my_model$estimate()
which.max(my_model$ICL)
```

End(Not run)

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