## Package 'isopleuros'

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```
Title Ternary Plots
Version 1.3.0
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Description Ternary plots made simple. This package allows to create
      ternary plots using 'graphics'. It provides functions to display the
      data in the ternary space, to add or tune graphical elements and to
      display statistical summaries. It also includes common ternary
      diagrams which are useful for the archaeologist (e.g. soil texture
      charts, ceramic phase diagram).
License GPL (>= 3)
URL https://packages.tesselle.org/isopleuros/,
      https://github.com/tesselle/isopleuros
BugReports https://github.com/tesselle/isopleuros/issues
Depends R (>= 3.5)
Imports graphics, grDevices, methods, stats, utils
Suggests interp, rsvg, svglite, tinysnapshot, tinytest
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RoxygenNote 7.3.2
Collate 'AllGenerics.R' 'coordinates.R' 'data.R'
      'isopleuros-internal.R' 'isopleuros-package.R'
      'ternary_arrows.R' 'ternary_axes.R' 'ternary_box.R'
      'ternary_contour.R' 'ternary_crosshairs.R' 'ternary_density.R'
      'ternary_ellipse.R' 'ternary_grid.R' 'ternary_hull.R'
      'ternary_image.R' 'ternary_labels.R' 'ternary_lines.R'
      'ternary_mean.R' 'ternary_pairs.R' 'ternary_pca.R'
      'ternary_plot.R' 'ternary_points.R' 'ternary_polygon.R'
      'ternary_segments.R' 'ternary_text.R' 'ternary_title.R'
      'ternary_window.R' 'triangle_phase.R' 'triangle_soil.R' 'zzz.R'
```

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## Description

Sand, silt, clay compositions of 39 sediment samples at different water depths in an Arctic lake.

boxite 3

## Usage

arctic

#### **Format**

A data. frame with 4 variables:

sand

silt

clay

depth Water depth (m).

## Source

Aitchison, J. (1986). *The Statistical Analysis of Compositional Data*. London: Chapman and Hall. doi:10.1007/9789400941090.

#### See Also

Other datasets: boxite, lava

boxite

**Boxite Compositions** 

## Description

Compositions of 25 specimens of boxite.

## Usage

boxite

## **Format**

A data. frame with 5 variables:

- A albite.
- B blandite.
- C cornite.
- D daubite.
- E endite.

#### **Source**

Aitchison, J. (1986). *The Statistical Analysis of Compositional Data*. London: Chapman and Hall. doi:10.1007/9789400941090.

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#### See Also

Other datasets: arctic, lava

lava

Skye Lavas Compositions

## **Description**

AFM compositions of 23 aphyric Skye lavas.

## Usage

lava

#### **Format**

A data. frame with 3 variables:

```
A Na2O + K2O (percent).
```

F Fe2O3 (percent).

M MgO (percent).

#### **Source**

Aitchison, J. (1986). *The Statistical Analysis of Compositional Data*. London: Chapman and Hall. doi:10.1007/9789400941090.

#### See Also

Other datasets: arctic, boxite

ternary\_arrows

Add Arrows to a Ternary Plot

## **Description**

Draw arrows between pairs of points.

```
ternary_arrows(x0, y0, z0, ...)
## S4 method for signature 'numeric, numeric, numeric'
ternary_arrows(x0, y0, z0, x1 = x0, y1 = y0, z1 = z0, ...)
```

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## **Arguments**

x0, y0, z0	A numeric vector giving the x, y and z ternary coordinates of points from which to draw.
	Further arguments to be passed to graphics::arrows().
x1, y1, z1	A numeric vector giving the x, y and z ternary coordinates of points to which to draw.

#### Value

ternary\_arrows() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
graphics::arrows()
Other geometries: ternary_crosshairs(), ternary_image(), ternary_labels(), ternary_lines(),
ternary_points(), ternary_polygon(), ternary_segments(), ternary_text()
```

## **Examples**

ternary\_axis

Add an Axis to a Ternary Plot

## Description

Adds an axis to the current plot.

```
ternary_axis(
    side,
    at = NULL,
    labels = TRUE,
    tick = TRUE,
    center = getOption("isopleuros.center"),
    scale = getOption("isopleuros.scale"),
    font = NA,
    lty = "solid",
    lwd = 1,
```

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```
lwd.ticks = lwd,
col = NULL,
col.ticks = NULL,
...
)
```

## Arguments

side	An integer specifying which side of the plot the axis is to be drawn on. The axis is placed as follows: 1=below, 2=right and 3=left.
at	A numeric vector giving the points at which tick-marks are to be drawn.
labels	A logical scalar specifying whether (numerical) annotations are to be made at the tickmarks, or a character vector of labels to be placed at the tickpoints. If this is not logical, at should also be supplied and of the same length.
tick	A logical scalar: should tickmarks and an axis line be drawn?
center	A numeric vector giving the center. If NULL (the default), data are assumed not centered.
scale	A numeric vector giving the scale factor. If NULL (the default), data are assumed not scaled.
font	font for text. Defaults to par("font.axis").
lty	A character string or numeric value specifying the line type for both the axis line and the tick marks.
lwd, lwd.ticks	A non-negative numeric value specifying the line widths for the axis line and the tick marks.
col,col.ticks	Colors for the axis line and the tick marks respectively. Defaults to par("col.axis").
•••	Other graphical parameters may also be passed as arguments to this function, particularly, cex.axis, col.axis and font.axis for axis annotation.

## Value

ternary\_axis() is called it for its side-effects.

## Author(s)

N. Frerebeau

## See Also

```
Other graphical elements: ternary_box(), ternary_grid(), ternary_pairs(), ternary_plot(), ternary_title()
```

```
## Add axis
ternary_plot(NULL, axes = FALSE)
ternary_axis(side = 1, col = "red")
ternary_axis(side = 2, col = "blue")
```

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```
ternary_axis(side = 3, col = "green")
## Add box and grid
ternary_plot(NULL, axes = FALSE)
ternary_box(lty = "dashed", col = "red")
ternary_grid(lty.primary = "dotted")
```

ternary\_box

Draw a Box around a Ternary Plot

## **Description**

Draw a Box around a Ternary Plot

#### Usage

```
ternary_box(lty = "solid", ...)
```

#### Arguments

1ty A character string or numeric value specifying the line type of the box.... Other graphical parameters may also be passed as arguments to this function, particularly, col or lwd.

#### Value

ternary\_box() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
Other graphical elements: ternary_axis(), ternary_grid(), ternary_pairs(), ternary_plot(), ternary_title()
```

```
## Add axis
ternary_plot(NULL, axes = FALSE)
ternary_axis(side = 1, col = "red")
ternary_axis(side = 2, col = "blue")
ternary_axis(side = 3, col = "green")

## Add box and grid
ternary_plot(NULL, axes = FALSE)
ternary_box(lty = "dashed", col = "red")
ternary_grid(lty.primary = "dotted")
```

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ternary\_contour

Contour Lines

## Description

Computes and draws contour lines.

## Usage

```
ternary_contour(x, y, z, ...)
## S4 method for signature 'numeric, numeric, numeric'
ternary_contour(
 х,
 у,
  Ζ,
  value,
  n = 50,
  nlevels = 10,
  levels = pretty(range(value, na.rm = TRUE), nlevels),
  ilr = TRUE,
 method = "linear",
  extrapolate = FALSE,
  palette = function(i) grDevices::hcl.colors(i, "YlOrRd", rev = TRUE),
)
## S4 method for signature 'ANY, missing, missing'
ternary_contour(
  Х,
  value,
 n = 50,
  nlevels = 10,
  levels = pretty(range(value, na.rm = TRUE), nlevels),
  ilr = TRUE,
 method = "linear",
  extrapolate = FALSE,
 palette = function(i) grDevices::hcl.colors(i, "YlOrRd", rev = TRUE),
)
```

#### **Arguments**

x, y, z A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).

... Further arguments to be passed to ternary\_lines().

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value A	A numeric vector giving the values to be plotted.
n A	A length-one numeric specifying the number of grid points.
	A length-one numeric vector specifying the number of contour levels desired.  Only used if levels is NULL.
levels A	A numeric vector of levels at which to draw contour lines.
	A logical scalar: should interpolation be computed in ILR space? If FALSE, nterpolation is computed in Cartesian space.
method A	A character string: specifying the method for interpolation (see interp::interp()).
·	A logical scalar: should extrapolation be used outside of the convex hull de- ermined by the data points (see interp::interp())?
palette A	A color palette function that takes a single integer argument (the number of

#### **Details**

Contour are computed from a bivariate interpolation onto a grid, after an isometric log ratio transformation of the original data.

levels) and returns a vector of colors.

#### Value

```
ternary_contour() is called it for its side-effects.

Invisibly returns a list with elements levels (the contour levels) and colors (the contour colors) that can be used for a legend.
```

## Note

The **interp** package needs to be installed on your machine.

#### Author(s)

N. Frerebeau

#### See Also

```
interp::interp(), grDevices::contourLines()
Other statistics: ternary_density(), ternary_ellipse(), ternary_hull(), ternary_mean(),
ternary_pca()
```

```
## Add density
## Data from Aitchison 1986
ternary_plot(arctic, panel.first = ternary_grid())
levels <- ternary_contour(arctic, value = arctic$depth, n = 100, nlevels = 10)
## Add a legend
legend_image <- grDevices::as.raster(rev(levels$colors))
graphics::rasterImage(legend_image, 0.85, 0.75, 0.9, 1)
graphics::text(x = 0.9, y = c(0.75, 1), labels = range(levels$levels), pos = 4)</pre>
```

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ternary\_crosshairs

Add Cross-Hairs to a Ternary Plot

#### Description

Draw lines that intersect at a point.

#### Usage

```
ternary_crosshairs(x, y, z, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_crosshairs(x, y, z, x_mark = TRUE, y_mark = TRUE, z_mark = TRUE, ...)
## S4 method for signature 'ANY,missing,missing'
ternary_crosshairs(x, x_mark = TRUE, y_mark = TRUE, z_mark = TRUE, ...)
```

#### **Arguments**

x, y, z

A numeric vector giving the x, y and z ternary coordinates of a set of points.

If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).

Further graphical parameters (see graphics::par()) may also be supplied as arguments, particularly, line type, lty, line width, lwd and color, col. Also the line characteristics lend, ljoin and lmitre.

 $x_mark, y_mark, z_mark$ 

A logical scalar: should the x, y or z axis component be drawn?

#### Value

ternary\_crosshairs() is called it for its side-effects.

#### Author(s)

N. Frerebeau

## See Also

```
Other geometries: ternary_arrows(), ternary_image(), ternary_labels(), ternary_lines(), ternary_points(), ternary_polygon(), ternary_segments(), ternary_text()
```

```
## Add cross-hairs
## Data from Aitchison 1986
ternary_plot(lava, panel.first = ternary_grid())
ternary_crosshairs(lava)
```

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```
ternary_plot(lava, panel.first = ternary_grid())
ternary_crosshairs(lava, y_mark = FALSE, z_mark = FALSE, col = "red")

ternary_plot(lava, panel.first = ternary_grid())
ternary_crosshairs(lava, x_mark = FALSE, z_mark = FALSE, col = "green")

ternary_plot(lava, panel.first = ternary_grid())
ternary_crosshairs(lava, x_mark = FALSE, y_mark = FALSE, col = "blue")
```

ternary\_density

Density Contour Lines

## **Description**

Computes and draws density contour lines.

#### Usage

```
ternary_density(x, y, z, ...)
## S4 method for signature 'numeric, numeric'
ternary_density(
 х,
 у,
 Ζ,
 h = NULL
 n = 25,
 nlevels = 10,
 levels = NULL,
 palette = function(i) grDevices::hcl.colors(i, "YlOrRd", rev = TRUE),
)
## S4 method for signature 'ANY, missing, missing'
ternary_density(
 Х,
 h = NULL,
 n = 25,
 nlevels = 10,
 levels = NULL,
 palette = function(i) grDevices::hcl.colors(i, "YlOrRd", rev = TRUE),
)
```

## Arguments

x, y, z A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).

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	Further arguments to be passed to ternary_lines().
h	A length-one numeric vector giving the bandwidth.
n	A length-one numeric specifying the number of grid points.
nlevels	A length-one numeric vector specifying the number of contour levels desired. Only used if levels is NULL.
levels	A numeric vector of levels at which to draw contour lines.
palette	A color palette function that takes a single integer argument (the number of levels) and returns a vector of colors.

#### **Details**

Two-dimensional kernel density estimation with an axis-aligned bivariate normal kernel. Normal kernel is evaluated on a square grid, after an isometric log ratio transformation of the original data.

#### Value

```
ternary_density() is called it for its side-effects.
```

Invisibly returns a list with elements levels (the contour levels) and colors (the contour colors) that can be used for a legend.

#### Note

This must be considered as experimental and subject to major changes in a future release.

## Author(s)

N. Frerebeau

#### Source

Two-dimensional kernel density estimation is adapted from MASS::kde2d().

#### See Also

```
grDevices::contourLines()
Other statistics: ternary_contour(), ternary_ellipse(), ternary_hull(), ternary_mean(),
ternary_pca()
```

```
## Add density
## Data from Aitchison 1986
ternary_plot(lava, panel.first = ternary_grid())
levels <- ternary_density(lava, n = 500, nlevels = 10)

## Add a legend
legend_image <- grDevices::as.raster(rev(levels$colors))
graphics::rasterImage(legend_image, 0.85, 0.75, 0.9, 1)
graphics::text(x = 0.9, y = c(0.75, 1), labels = range(levels$levels), pos = 4)</pre>
```

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ternary\_ellipse

Add an Ellipse to a Ternary Plot

## **Description**

Computes and draws a confidence/tolerance ellipse.

#### Usage

```
ternary_ellipse(x, y, z, ...)

ternary_confidence(x, y, z, ...)

## S4 method for signature 'numeric,numeric,numeric'
ternary_ellipse(x, y, z, radius = 1, ...)

## S4 method for signature 'ANY,missing,missing'
ternary_ellipse(x, radius = 1, ...)

## S4 method for signature 'numeric,numeric,numeric'
ternary_confidence(x, y, z, level = 0.95, ...)

## S4 method for signature 'ANY,missing,missing'
ternary_confidence(x, level = 0.95, ...)

## S4 method for signature 'numeric,numeric,numeric'
ternary_tolerance(x, y, z, level = 0.95, ...)

## S4 method for signature 'ANY,missing,missing'
ternary_tolerance(x, level = 0.95, ...)
```

#### **Arguments**

x, y, z	A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
	Further arguments to be passed to graphics::polygon().
radius	A numeric vector specifying the scaling of the half-diameters.
level	A numeric vector specifying the confidence/tolerance level.

#### **Details**

Ellipse coordinates are computed after an isometric log ratio transformation of the original data.

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## Value

ternary\_ellipse() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
graphics::polygon()
Other statistics: ternary_contour(), ternary_density(), ternary_hull(), ternary_mean(),
ternary_pca()
```

## **Examples**

```
## Ellipses
## Data from Aitchison 1986
ternary_plot(lava, panel.first = ternary_grid(5, 10))
ternary_tolerance(lava, level = 0.95, border = "blue", lty = 2)
ternary_confidence(lava, level = 0.95, border = "red", lty = 3)
```

ternary\_grid

Add Grid to a Ternary Plot

## **Description**

Adds a triangular grid to an existing plot.

```
ternary_grid(
  primary = NULL,
  secondary = NULL,
  center = getOption("isopleuros.center"),
  scale = getOption("isopleuros.scale"),
  col.primary = "darkgray",
  col.secondary = "lightgray",
  lty.primary = "dashed",
  lty.secondary = "dotted",
  lwd.primary = 1,
  lwd.secondary = lwd.primary
)
```

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## **Arguments**

primary	An integer specifying the number of cells of the primary grid in x, y and z direction.
secondary	An integer specifying the number of cells of the secondary grid in x, y and z direction.
center	A numeric vector giving the center. If NULL (the default), data are assumed not centered.
scale	A numeric vector giving the scale factor. If NULL (the default), data are assumed not scaled.
col.primary, co	l.secondary
	A character string specifying the color of the grid lines.
lty.primary,lt	y.secondary  A character string or numeric value specifying the line type of the grid lines.
lwd.primary,lwo	

## Value

ternary\_grid() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
Other graphical elements: ternary_axis(), ternary_box(), ternary_pairs(), ternary_plot(), ternary_title()
```

```
## Data from Aitchison 1986
ternary_plot(lava, center = FALSE, scale = FALSE, col = "red", pch = 16)
ternary_grid(5)

## Center
z <- ternary_plot(lava, center = TRUE, col = "blue", pch = 16)
ternary_grid(5, center = z$center)

## Center and scale
z <- ternary_plot(lava, center = TRUE, scale = TRUE, col = "green", pch = 16)
ternary_grid(5, center = z$center, scale = z$scale)</pre>
```

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ternary\_hull

Convex Hull of a Set of Points

## **Description**

Computes and draws the convex hull of the set of points specified.

## Usage

```
ternary_hull(x, y, z, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_hull(x, y, z, center = FALSE, scale = FALSE, ...)
## S4 method for signature 'ANY,missing,missing'
ternary_hull(x, center = FALSE, scale = FALSE, ...)
```

## **Arguments**

x, y, z	A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
	Further arguments to be passed to graphics::polygon().
center	A logical scalar specifying wether the data should be centered, or a numeric vector giving the center.
scale	A logical scalar specifying wether the data should be scaled, or a numeric vector giving the scale factor.

#### Value

ternary\_hull() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
grDevices::chull(), graphics::polygon()
Other statistics: ternary_contour(), ternary_density(), ternary_ellipse(), ternary_mean(),
ternary_pca()
```

```
## Convex hull
## Data from Aitchison 1986
ternary_plot(lava, panel.first = ternary_grid(5, 10))
ternary_hull(lava, border = "red")
```

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ternary\_image

Display a Color Image

#### Description

Creates a grid of colored triangles with colors corresponding to the output of a function.

#### Usage

```
ternary_image(f, ...)
## S4 method for signature 'function'
ternary_image(f, n = 48, palette = NULL, ...)
```

#### **Arguments**

f A function that takes three arguments (x, y and z coordinates) and returns a

numeric vector.

... Further parameters to be passed to f.

n A length-one integer vector specifying the maximum number of tiles on each

axis.

palette A function that takes a single numeric vector (the output of f) as argument

and returns a vector of color. If NULL, the default color scheme will be used. If

FALSE, the output of f is used as colors.

#### Value

ternary\_image() is called it for its side-effects.

## Author(s)

N. Frerebeau

#### See Also

```
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_labels(), ternary_lines(), ternary_points(), ternary_polygon(), ternary_segments(), ternary_text()
```

```
## RGB
ternary_plot(NULL, xlab = "Red", ylab = "Green", zlab = "Blue")
ternary_image(f = rgb, n = 20, palette = FALSE)
```

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ternary\_labels

Non-Overlapping Text Labels

## Description

Optimize the location of text labels to minimize overplotting text.

## Usage

```
ternary_labels(x, y, z, ...)

## S4 method for signature 'numeric,numeric,numeric'
ternary_labels(
    x,
    y,
    z,
    center = FALSE,
    scale = FALSE,
    labels = seq_along(x),
    type = c("text", "shadow"),
    ...
)

## S4 method for signature 'ANY,missing,missing'
ternary_labels(x, center = FALSE, scale = FALSE, labels = seq_along(x$x), ...)
```

## Arguments

x, y, z	A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
	Further graphical parameters (see <pre>graphics::par()</pre> ) may also be supplied as arguments, particularly, character expansion, cex and color, col.
center	A logical scalar specifying wether the data should be centered, or a numeric vector giving the center.
scale	A logical scalar specifying wether the data should be scaled, or a numeric vector giving the scale factor.
labels	A character vector or expression specifying the text to be written.
type	A character string specifying the shape of the field. It must be one of "text" or "shadow". Any unambiguous substring can be given.

#### Value

ternary\_labels() is called it for its side-effects.

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#### Author(s)

N. Frerebeau

#### See Also

```
graphics::text()
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_image(), ternary_lines(),
ternary_points(), ternary_polygon(), ternary_segments(), ternary_text()
```

#### **Examples**

```
## Compositional data
coda <- data.frame(
    X = c(41.0, 40, 39.0),
    Y = c(19.5, 20, 20.5),
    Z = c(39.5, 40, 40.5)
)

## Add text
ternary_plot(NULL, panel.first = ternary_grid())
ternary_points(coda)
ternary_labels(coda, labels = c("A", "B", "C"))</pre>
```

ternary\_lines

Add Connected Line Segments to a Ternary Plot

#### **Description**

Add Connected Line Segments to a Ternary Plot

## Usage

```
ternary_lines(x, y, z, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_lines(x, y, z, type = "l", ...)
## S4 method for signature 'ANY,missing,missing'
ternary_lines(x, type = "l", ...)
```

#### **Arguments**

x, y, z

A numeric vector giving the x, y and z ternary coordinates of a set of points.

If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).

Further graphical parameters (see graphics::par()) may also be supplied as arguments, particularly, line type, lty, line width, lwd, color, col and for type = "b", pch. Also the line characteristics lend, ljoin and lmitre.

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type

A character string indicating the type of plotting; actually any of the types as in graphics::plot.default().

#### Value

ternary\_lines() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
graphics::lines()
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_image(), ternary_labels(),
ternary_points(), ternary_polygon(), ternary_segments(), ternary_text()
```

## **Examples**

```
## Compositional data
coda <- data.frame(
    X = c(20, 60, 20, 20),
    Y = c(20, 20, 60, 40),
    Z = c(60, 20, 20, 40)
)

## Add lines
ternary_plot(NULL, panel.first = ternary_grid())
ternary_lines(coda, col = "red", lwd = 2)</pre>
```

ternary\_mean

Compositional Mean

#### **Description**

Computes and draws the closed geometric mean of the set of points specified.

```
ternary_mean(x, y, z, ...)
## S4 method for signature 'numeric, numeric, numeric'
ternary_mean(x, y, z, ...)
## S4 method for signature 'ANY, missing, missing'
ternary_mean(x, y, z, ...)
```

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## Arguments

x, y, z A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).

. Further arguments to be passed to graphics::points().

## Value

ternary\_mean() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
Other statistics: ternary_contour(), ternary_density(), ternary_ellipse(), ternary_hull(), ternary_pca()
```

## **Examples**

```
## Mean
## Data from Aitchison 1986
ternary_plot(lava, panel.first = ternary_grid())
ternary_mean(lava, pch = 16, col = "red")
ternary_confidence(lava, level = 0.95, border = "red", lty = 1)
```

ternary\_pairs

Ternary Plot Matrices

## Description

Produces a matrix of ternary plots.

```
ternary_pairs(x, ...)
## S4 method for signature 'matrix'
ternary_pairs(x, margin = NULL, ...)
## S4 method for signature 'data.frame'
ternary_pairs(x, margin = NULL, ...)
```

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## **Arguments**

x A matrix or a data. frame. Columns are converted to numeric in the same way that data.matrix() does.

... Further graphical parameters.

margin A character string or an integer giving the index of the column to be used as

the third part of the ternary plots. If  $\ensuremath{\mathsf{NULL}}$  (the default), marginal compositions

will be used (i.e. the geometric mean of the non-selected parts).

#### Value

ternary\_pairs() is called it for its side-effects: it results in a graphic being displayed. Invisibly returns x.

## Author(s)

N. Frerebeau

#### See Also

```
Other graphical elements: ternary_axis(), ternary_box(), ternary_grid(), ternary_plot(), ternary_title()
```

## Examples

```
## Data from Aitchison 1986
## Ternary plots with marginal compositions
ternary_pairs(boxite)
## Ternary plots with endite
ternary_pairs(boxite, margin = "E")
```

ternary\_pca

Principal Component Analysis

#### **Description**

Computes and draws principal component.

```
ternary_pca(x, y, z, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_pca(x, y, z, axis = 1, ...)
## S4 method for signature 'ANY,missing,missing'
ternary_pca(x, axis = 1, ...)
```

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## **Arguments**

x, y, z
A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
... Further arguments to be passed to graphics::lines().
axis
An integer specifying the dimension to be plotted.

#### Value

ternary\_pca() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
Other statistics: ternary_contour(), ternary_density(), ternary_ellipse(), ternary_hull(), ternary_mean()
```

## **Examples**

```
## PCA
## Data from Aitchison 1986
ternary_plot(lava, panel.first = ternary_grid())
ternary_pca(lava, axis = 1, col = "red", lty = 2)
```

ternary\_plot

Ternary Plot

## Description

Produces a ternary plot.

```
ternary_plot(x, y, z, ...)
## S4 method for signature 'numeric, numeric, numeric'
ternary_plot(
    x,
    y,
    z,
    center = FALSE,
    scale = FALSE,
    xlim = NULL,
    ylim = NULL,
```

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```
zlim = NULL,
 xlab = NULL,
 ylab = NULL,
 zlab = NULL,
 main = NULL,
 sub = NULL,
 ann = graphics::par("ann"),
 axes = TRUE,
  frame.plot = axes,
 panel.first = NULL,
 panel.last = NULL,
)
## S4 method for signature 'ANY, missing, missing'
ternary_plot(
 Х,
 xlim = NULL,
 ylim = NULL,
 zlim = NULL,
 xlab = NULL,
 ylab = NULL,
 zlab = NULL,
 main = NULL,
 sub = NULL,
 ann = graphics::par("ann"),
 axes = TRUE,
 frame.plot = axes,
 panel.first = NULL,
 panel.last = NULL,
)
```

## Arguments

x, y, z	A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
	Other graphical parameters may also be passed as arguments to this function.
center	A logical scalar: should the data be centered?
scale	A logical scalar: should the data be scaled?
xlim	A length-three $numeric$ vector giving the x limits in the range $[0,1]$ .
ylim	A length-three $\operatorname{numeric}$ vector giving the y limits in the range $[0,1]$ .
zlim	A length-three numeric vector giving the z limits in the range $[0,1]$ .
xlab, ylab, zlab	A character string giving a label for the x, y and z axes.
main	A character string giving a main title for the plot.

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sub	A character string giving a subtitle for the plot.
ann	A logical scalar: should the default annotation (title and $x$ , $y$ and $z$ axis labels) appear on the plot?
axes	A logical scalar: should axes be drawn on the plot?
frame.plot	A logical scalar: should a box be drawn around the plot?
panel.first	An an expression to be evaluated after the plot axes are set up but before any plotting takes place. This can be useful for drawing background grids.
panel.last	An expression to be evaluated after plotting has taken place but before the axes, title and box are added.

#### Value

ternary\_plot() is called it for its side-effects: it results in a graphic being displayed. Invisibly returns a list with the components:

```
    x A numeric vector of x values.
    y A numeric vector of y values.
    z A numeric vector of z values.
    center A numeric vector giving the center.
    scale A numeric vector giving the scale factor.
```

## Author(s)

N. Frerebeau

#### See Also

```
Other graphical elements: ternary_axis(), ternary_box(), ternary_grid(), ternary_pairs(), ternary_title()
```

```
## Blank plot
ternary_plot(NULL)

## Compositional data
coda <- data.frame(
    X = c(20, 60, 20, 1/3),
    Y = c(20, 20, 60, 1/3),
    Z = c(60, 20, 20, 1/3)
)

## Ternary plot
ternary_plot(coda, pch = 16, col = "red")

## Add a grid
ternary_plot(coda, panel.first = ternary_grid(5, 10))</pre>
```

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ternary\_points

Add Points to a Ternary Plot

## **Description**

Add Points to a Ternary Plot

#### Usage

```
ternary_points(x, y, z, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_points(x, y, z, center = FALSE, scale = FALSE, type = "p", ...)
## S4 method for signature 'ANY,missing,missing'
ternary_points(x, center = FALSE, scale = FALSE, type = "p", ...)
```

## Arguments

x, y, z	A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
•••	Further graphical parameters (see graphics::par()) may also be supplied as arguments, particularly, plotting character, pch, character expansion, cex and color, col.
center	A logical scalar specifying wether the data should be centered, or a numeric vector giving the center.
scale	A logical scalar specifying wether the data should be scaled, or a numeric vector giving the scale factor.
type	A character string indicating the type of plotting; actually any of the types as in graphics::plot.default().

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#### Value

ternary\_points() is called it for its side-effects. Invisibly returns a list with the components:

```
    x A numeric vector of x values.
    y A numeric vector of y values.
    z A numeric vector of z values.
    center A numeric vector giving the center.
    scale A numeric vector giving the scale factor.
```

## Author(s)

N. Frerebeau

#### See Also

```
graphics::points()
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_image(), ternary_labels(),
ternary_lines(), ternary_polygon(), ternary_segments(), ternary_text()
```

## **Examples**

```
## Add points
## Data from Aitchison 1986
ternary_plot(NULL, panel.first = ternary_grid())
ternary_points(lava, col = "red", pch = 16)

## Center and scale
ternary_plot(NULL, axes = FALSE, frame.plot = TRUE)
ternary_points(lava, col = "red", pch = 16)
ternary_points(lava, center = TRUE, col = "blue", pch = 16)
ternary_points(lava, center = TRUE, scale = TRUE, col = "green", pch = 16)
```

ternary\_polygon

Polygon Drawing

#### **Description**

Draws the polygons whose vertices are given in x, y and z.

```
ternary_polygon(x, y, z, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_polygon(x, y, z, ...)
## S4 method for signature 'ANY,missing,missing'
ternary_polygon(x, y, z, ...)
```

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## Arguments

x, y, z A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).

Further arguments to be passed to graphics::polygon().

#### Value

ternary\_polygon() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
graphics::polygon()
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_image(), ternary_labels(),
ternary_lines(), ternary_points(), ternary_segments(), ternary_text()
```

## **Examples**

```
## Compositional data
coda <- data.frame(
    X = c(20, 60, 20),
    Y = c(20, 20, 60),
    Z = c(60, 20, 20)
)

## Add a polygon
ternary_plot(NULL, panel.first = ternary_grid())
ternary_polygon(coda, density = 5, border = "red")</pre>
```

ternary\_segments

Add Line Segments to a Ternary Plot

#### **Description**

Draw line segments between pairs of points.

```
ternary_segments(x0, y0, z0, ...)
## S4 method for signature 'numeric,numeric,numeric'
ternary_segments(x0, y0, z0, x1 = x0, y1 = y0, z1 = z0, ...)
```

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## **Arguments**

x0, y0, z0	A numeric vector giving the x, y and z ternary coordinates of points from which to draw.
	Further graphical parameters (see graphics::par()) may also be supplied as arguments, particularly, line type, lty, line width, lwd and color, col. Also the line characteristics lend, ljoin and lmitre.
x1, y1, z1	A numeric vector giving the x, y and z ternary coordinates of points to which to draw.

#### Value

ternary\_segments() is called it for its side-effects.

## Author(s)

N. Frerebeau

#### See Also

```
graphics::segments()
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_image(), ternary_labels(),
ternary_lines(), ternary_points(), ternary_polygon(), ternary_text()
```

## **Examples**

ternary\_text

Add Text to a Ternary Plot

## Description

Draws the strings given in the vector labels at the coordinates given by x, y and z.

```
ternary_text(x, y, z, ...)
## S4 method for signature 'numeric, numeric, numeric'
ternary_text(
    x,
    y,
    z,
    center = FALSE,
```

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```
scale = FALSE,
labels = seq_along(x),
...
)

## S4 method for signature 'ANY, missing, missing'
ternary_text(x, center = FALSE, scale = FALSE, labels = seq_along(x$x), ...)
```

## **Arguments**

x, y, z	A numeric vector giving the x, y and z ternary coordinates of a set of points. If y and z are missing, an attempt is made to interpret x in a suitable way (see grDevices::xyz.coords()).
	Further arguments to be passed to graphics::text().
center	A logical scalar specifying wether the data should be centered, or a numeric vector giving the center.
scale	A logical scalar specifying wether the data should be scaled, or a numeric vector giving the scale factor.
labels	A character vector or expression specifying the text to be written.

#### Value

ternary\_text() is called it for its side-effects.

## Author(s)

N. Frerebeau

## See Also

```
graphics::text()
Other geometries: ternary_arrows(), ternary_crosshairs(), ternary_image(), ternary_labels(),
ternary_lines(), ternary_points(), ternary_polygon(), ternary_segments()
```

```
## Compositional data
coda <- data.frame(
    X = c(20, 60, 20),
    Y = c(20, 20, 60),
    Z = c(60, 20, 20)
)

## Add text
ternary_plot(NULL, panel.first = ternary_grid())
ternary_text(coda, labels = c("A", "B", "C"), col = "red", cex = 2)</pre>
```

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ternary\_title

Ternary Plot Annotation

## **Description**

Ternary Plot Annotation

## Usage

```
ternary_title(
  main = NULL,
  sub = NULL,
  xlab = NULL,
  ylab = NULL,
  zlab = NULL,
  line = NA,
  outer = FALSE,
  ...
)
```

## Arguments

main A character string specifying the main title (on top).

sub A character string specifying the sub-title (at bottom).

xlab, ylab, zlab A character string giving a label for the x, y and z axes.

line Specifying a value for line overrides the default placement of labels, and places them this many lines outwards from the plot edge.

outer A logical scalar: should the titles be placed in the outer margins of the plot?

Other graphical parameters may also be passed as arguments to this function, particularly, font.main, cex.main, col.main and font.sub, cex.sub, col.sub for title annotation; font.lab, cex.lab and col.lab for axis label.

#### Value

ternary\_title() is called it for its side-effects.

#### Author(s)

N. Frerebeau

#### See Also

```
Other graphical elements: ternary_axis(), ternary_box(), ternary_grid(), ternary_pairs(), ternary_plot()
```

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#### **Examples**

triangle\_phase\_cas

Ceramic Phase Diagram

#### Description

Ceramic Phase Diagram

#### Usage

```
triangle_phase_cas(labels = TRUE, symbol = FALSE, mol = FALSE, ...)
triangle_phase_ceramic(labels = TRUE, symbol = FALSE, mol = FALSE, ...)
```

#### **Arguments**

labels A logical scalar: should labels be displayed?

Symbol A logical scalar: should symbol be used instead of full labels? Only used if labels is TRUE.

mol A logical scalar: should molarity be used instead of molar mass?

Further arguments to be passed to graphics::polygon().

#### Author(s)

N. Frerebeau

## See Also

```
Other charts: triangle_soil
```

```
## Ceramic phase diagram
ternary_plot(NULL, xlab = "CaO", ylab = "Al2O3", zlab = "SiO2")
triangle_phase_ceramic(symbol = TRUE, mol = TRUE, pch = 16)

ternary_plot(NULL, xlab = "CaO", ylab = "Al2O3", zlab = "SiO2")
triangle_phase_ceramic(symbol = TRUE, mol = FALSE, pch = 16)

## CAS diagram
```

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```
ternary_plot(NULL, axes = FALSE, ann = FALSE, frame.plot = TRUE)
triangle_phase_cas(mol = FALSE, pch = 16)
```

triangle\_soil

Soil Texture Triangle

#### **Description**

Soil Texture Triangle

#### Usage

```
triangle_soil_hypres(labels = TRUE, symbol = FALSE, ...)
triangle_soil_folk(labels = TRUE, symbol = FALSE, ...)
triangle_soil_shepard(labels = TRUE, symbol = FALSE, ...)
triangle_soil_usda(labels = TRUE, symbol = FALSE, ...)
```

## **Arguments**

labels A logical scalar: should labels be displayed?

symbol A logical scalar: should symbol be used instead of full labels? Only used if

labels is TRUE.

... Further arguments to be passed to graphics::polygon().

#### Author(s)

N. Frerebeau

#### See Also

```
Other charts: triangle_phase_cas()
```

```
## HYPRES soil texture
ternary_plot(NULL, xlab = "sand", ylab = "silt", zlab = "clay")
triangle_soil_hypres()

## USDA (1951) soil texture
ternary_plot(NULL, xlab = "sand", ylab = "silt", zlab = "clay")
triangle_soil_usda(symbol = TRUE)

## Folk (1954) soil texture
ternary_plot(NULL, xlab = "sand", ylab = "silt", zlab = "clay")
triangle_soil_folk(symbol = TRUE)
```

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```
## Shepard (1954) soil texture
ternary_plot(NULL, xlab = "sand", ylab = "silt", zlab = "clay")
triangle_soil_shepard()
```

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