# Package 'robStepSplitReg'

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Type Package

Title Robust Stepwise Split Regularized Regression

<b>Date</b> 2023-06-28
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<b>Description</b> Functions to perform robust stepwise split regularized regression. The approach first uses a robust stepwise algorithm to split the variables into the models of an ensemble. An adaptive robust regularized estimator is then applied to each subset of predictors in the models of an ensemble.
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R topics documented:
coef.robStepSplitReg
Index

coef.robStepSplitReg

coef.robStepSplitReg Coefficients for robStepSplitReg Object

# Description

coef.robStepSplitReg returns the coefficients for a robStepSplitReg object.

# Usage

```
## S3 method for class 'robStepSplitReg'
coef(object, group_index = NULL, ...)
```

### **Arguments**

object An object of class robStepSplitReg

group\_index Groups included in the ensemble. Default setting includes all the groups.

... Additional arguments for compatibility.

#### Value

The coefficients for the robStepSplitReg object.

#### Author(s)

Anthony-Alexander Christidis, <anthony.christidis@stat.ubc.ca>

#### See Also

```
robStepSplitReg
```

# Examples

```
# Required library
library(mvnfast)

# Simulation parameters
n <- 50
p <- 500
rho <- 0.5
p.active <- 100
snr <- 1
contamination.prop <- 0.2

# Setting the seed
set.seed(0)

# Simulation of beta vector
true.beta <- c(runif(p.active, 0, 5)*(-1)^rbinom(p.active, 1, 0.7), rep(0, p - p.active))</pre>
```

coef.robStepSplitReg 3

```
# Simulation of uncontaminated data
sigma.mat <- matrix(0, nrow = p, ncol = p)</pre>
sigma.mat[1:p.active, 1:p.active] <- rho</pre>
diag(sigma.mat) <- 1</pre>
x \leftarrow mvnfast::rmvn(n, mu = rep(0, p), sigma = sigma.mat)
sigma <- as.numeric(sqrt(t(true.beta) %*% sigma.mat %*% true.beta)/sqrt(snr))</pre>
y <- x %*% true.beta + rnorm(n, 0, sigma)
# Contamination of data
contamination_indices <- 1:floor(n*contamination.prop)</pre>
k_lev <- 2
k_slo <- 100
x_train <- x
y_train <- y
beta_cont <- true.beta</pre>
beta_cont[true.beta!=0] <- beta_cont[true.beta!=0]*(1 + k_slo)</pre>
beta_cont[true.beta==0] <- k_slo*max(abs(true.beta))</pre>
for(cont_id in contamination_indices){
  a \leftarrow runif(p, min = -1, max = 1)
  a <- a - as.numeric((1/p)*t(a) %*% rep(1, p))</pre>
  x_{\text{train}}[\text{cont}_{\text{id}}] \leftarrow \text{mvnfast}::\text{rmvn}(1, \text{rep}(0, p), 0.1^2*\text{diag}(p)) +
    k_lev * a / as.numeric(sqrt(t(a) %*% solve(sigma.mat) %*% a))
  y_train[cont_id] <- t(x_train[cont_id,]) %*% beta_cont</pre>
}
# Ensemble models
ensemble_fit <- robStepSplitReg(x_train, y_train,</pre>
                                   n_{models} = 5,
                                    model_saturation = c("fixed", "p-value")[1],
                                    alpha = 0.05, model_size = n - 1,
                                    robust = TRUE,
                                    compute_coef = TRUE,
                                    en_alpha = 1/4)
# Ensemble coefficients
ensemble_coefs <- coef(ensemble_fit, group_index = 1:ensemble_fit$n_models)</pre>
sens_ensemble <- sum(which((ensemble_coefs[-1]!=0)) <= p.active)/p.active
spec_ensemble <- sum(which((ensemble_coefs[-1]!=0)) <= p.active)/sum(ensemble_coefs[-1]!=0)</pre>
# Simulation of test data
m <- 2e3
x_{test} \leftarrow mvnfast::rmvn(m, mu = rep(0, p), sigma = sigma.mat)
y_test <- x_test %*% true.beta + rnorm(m, 0, sigma)</pre>
# Prediction of test samples
ensemble_preds <- predict(ensemble_fit, newx = x_test,</pre>
                             group_index = 1:ensemble_fit$n_models,
                             dynamic = FALSE)
mspe_ensemble <- mean((y_test - ensemble_preds)^2)/sigma^2</pre>
```

```
predict.robStepSplitReg
```

Predictions for robStepSplitReg Object

# **Description**

predict.robStepSplitReg returns the predictions for a robStepSplitReg object.

#### Usage

```
## S3 method for class 'robStepSplitReg'
predict(object, newx, group_index = NULL, dynamic = FALSE, ...)
```

#### **Arguments**

object An object of class robStepSplitReg

newx New data for predictions.

group\_index Groups included in the ensemble. Default setting includes all the groups.

dynamic Argument to determine whether dynamic predictions are used based on deviat-

ing cells. Default is FALSE.

... Additional arguments for compatibility.

#### Value

The predictions for the robStepSplitReg object.

#### Author(s)

Anthony-Alexander Christidis, <anthony.christidis@stat.ubc.ca>

## See Also

```
robStepSplitReg
```

# **Examples**

```
# Required library
library(mvnfast)

# Simulation parameters
n <- 50
p <- 500
rho <- 0.5
p.active <- 100
snr <- 1
contamination.prop <- 0.2</pre>
```

```
# Setting the seed
set.seed(0)
# Simulation of beta vector
true.beta < c(runif(p.active, 0, 5)*(-1)^rbinom(p.active, 1, 0.7), rep(0, p - p.active))
# Simulation of uncontaminated data
sigma.mat <- matrix(0, nrow = p, ncol = p)</pre>
sigma.mat[1:p.active, 1:p.active] <- rho</pre>
diag(sigma.mat) <- 1</pre>
x \leftarrow mvnfast::rmvn(n, mu = rep(0, p), sigma = sigma.mat)
sigma <- as.numeric(sqrt(t(true.beta) %*% sigma.mat %*% true.beta)/sqrt(snr))</pre>
y <- x %*% true.beta + rnorm(n, 0, sigma)
# Contamination of data
contamination_indices <- 1:floor(n*contamination.prop)</pre>
k_lev <- 2
k_slo <- 100
x_train <- x
y_train <- y
beta_cont <- true.beta</pre>
beta_cont[true.beta!=0] <- beta_cont[true.beta!=0]*(1 + k_slo)</pre>
beta_cont[true.beta==0] <- k_slo*max(abs(true.beta))</pre>
for(cont_id in contamination_indices){
  a \leftarrow runif(p, min = -1, max = 1)
  a <- a - as.numeric((1/p)*t(a) %*% rep(1, p))
  x_{\text{train}}[\text{cont}_{\text{id}}] \leftarrow \text{mvnfast}::\text{rmvn}(1, \text{rep}(0, p), 0.1^2*\text{diag}(p)) +
    k_lev * a / as.numeric(sqrt(t(a) %*% solve(sigma.mat) %*% a))
  y_train[cont_id] <- t(x_train[cont_id,]) %*% beta_cont</pre>
}
# Ensemble models
ensemble_fit <- robStepSplitReg(x_train, y_train,</pre>
                                   n_{models} = 5,
                                   model_saturation = c("fixed", "p-value")[1],
                                   alpha = 0.05, model_size = n - 1,
                                   robust = TRUE,
                                   compute_coef = TRUE,
                                   en_alpha = 1/4)
# Ensemble coefficients
ensemble_coefs <- coef(ensemble_fit, group_index = 1:ensemble_fit$n_models)</pre>
sens_ensemble <- sum(which((ensemble_coefs[-1]!=0)) <= p.active)/p.active</pre>
spec_ensemble <- sum(which((ensemble_coefs[-1]!=0)) <= p.active)/sum(ensemble_coefs[-1]!=0)</pre>
# Simulation of test data
m < - 2e3
x_{test} \leftarrow mvnfast::rmvn(m, mu = rep(0, p), sigma = sigma.mat)
y_test <- x_test %*% true.beta + rnorm(m, 0, sigma)</pre>
# Prediction of test samples
ensemble_preds <- predict(ensemble_fit, newx = x_test,</pre>
```

6 robStepSplitReg

robStepSplitReg

Robust Stepwise Split Regularized Regression

### **Description**

robStepSplitReg performs robust stepwise split regularized regression.

#### Usage

```
robStepSplitReg(
    x,
    y,
    n_models = 1,
    model_saturation = c("fixed", "p-value")[1],
    alpha = 0.05,
    model_size = NULL,
    robust = TRUE,
    compute_coef = FALSE,
    en_alpha = 1/4
)
```

#### Arguments

x Design matrix.
y Response vector.

Number of models

n\_models Number of models into which the variables are split.

 $model\_saturation$ 

Criterion to determine if a model is saturated. Must be one of "fixed" (default)

or "p-value".

alpha P-value used to determine when the model is saturated

model\_size Size of the models in the ensemble.

robust Argument to determine if robust measures of location, scale and correlation are

used. Default is TRUE.

compute\_coef Argument to determine if coefficients are computed (via adaptive PENSE) for

each model. Default is FALSE.

en\_alpha Elastic net mixing parmeter for parameters shrinkage. Default is 1/4.

#### Value

An object of class robStepSplitReg.

robStepSplitReg 7

#### Author(s)

Anthony-Alexander Christidis, <anthony.christidis@stat.ubc.ca>

#### See Also

```
coef.robStepSplitReg, predict.robStepSplitReg
```

# Examples

```
# Required library
library(mvnfast)
# Simulation parameters
n <- 50
p <- 500
rho <- 0.5
p.active <- 100
snr <- 1
contamination.prop <- 0.2</pre>
# Setting the seed
set.seed(0)
# Simulation of beta vector
true.beta \leftarrow c(runif(p.active, 0, 5)*(-1)^rbinom(p.active, 1, 0.7), rep(0, p - p.active))
# Simulation of uncontaminated data
sigma.mat <- matrix(0, nrow = p, ncol = p)</pre>
sigma.mat[1:p.active, 1:p.active] <- rho</pre>
diag(sigma.mat) <- 1</pre>
x \leftarrow mvnfast::rmvn(n, mu = rep(0, p), sigma = sigma.mat)
sigma <- as.numeric(sqrt(t(true.beta) %*% sigma.mat %*% true.beta)/sqrt(snr))</pre>
y <- x %*% true.beta + rnorm(n, 0, sigma)
# Contamination of data
contamination_indices <- 1:floor(n*contamination.prop)</pre>
k_lev <- 2
k_slo <- 100
x_train <- x
y_train <- y
beta_cont <- true.beta</pre>
beta_cont[true.beta!=0] <- beta_cont[true.beta!=0]*(1 + k_slo)</pre>
beta_cont[true.beta==0] <- k_slo*max(abs(true.beta))</pre>
for(cont_id in contamination_indices){
  a \leftarrow runif(p, min = -1, max = 1)
  a \leftarrow a - as.numeric((1/p)*t(a) %*% rep(1, p))
  x_{train}[cont_{id}] \leftarrow mvnfast::rmvn(1, rep(0, p), 0.1^2*diag(p)) +
    k_lev * a / as.numeric(sqrt(t(a) %*% solve(sigma.mat) %*% a))
  y_train[cont_id] <- t(x_train[cont_id,]) %*% beta_cont</pre>
}
```

8 robStepSplitReg

```
# Ensemble models
ensemble_fit <- robStepSplitReg(x_train, y_train,</pre>
                                  n_{models} = 5,
                                  model_saturation = c("fixed", "p-value")[1],
                                  alpha = 0.05, model_size = n - 1,
                                  robust = TRUE,
                                  compute_coef = TRUE,
                                  en_alpha = 1/4)
# Ensemble coefficients
ensemble_coefs <- coef(ensemble_fit, group_index = 1:ensemble_fit$n_models)</pre>
sens_ensemble <- sum(which((ensemble_coefs[-1]!=0)) <= p.active)/p.active</pre>
spec_ensemble <- sum(which((ensemble_coefs[-1]!=0)) <= p.active)/sum(ensemble_coefs[-1]!=0)</pre>
# Simulation of test data
m <- 2e3
x_{test} \leftarrow mvnfast::rmvn(m, mu = rep(0, p), sigma = sigma.mat)
y_test <- x_test %*% true.beta + rnorm(m, 0, sigma)</pre>
# Prediction of test samples
ensemble_preds <- predict(ensemble_fit, newx = x_test,</pre>
                            group_index = 1:ensemble_fit$n_models,
                            dynamic = FALSE)
mspe_ensemble <- mean((y_test - ensemble_preds)^2)/sigma^2</pre>
```

# **Index**

```
coef.robStepSplitReg, 2, 7
predict.robStepSplitReg, 4, 7
robStepSplitReg, 2, 4, 6
```