# Package 'ptmixed'

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Author Mirko Signorelli [aut, cre, cph] ( <a href="https://orcid.org/0000-0002-8102-3356">https://orcid.org/0000-0002-8102-3356</a> ), Pietro Spitali [ctb], Roula Tsonaka [ctb]
Maintainer Mirko Signorelli <msignorelli.rpackages@gmail.com></msignorelli.rpackages@gmail.com>
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df1

Example dataset with longitudinal counts

### **Description**

An example dataset of a study with longitudinal counts, used to illustrate how 'ptmixed()' and 'nbmixed()' work.

### Usage

data(df1)

### Format

A data frame with 18 rows and 5 variables

### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### See Also

examples in the nbmixed and ptmixed help pages

loglik.pt.1re

loglik.pt.1re	Loglikelihood of Poisson-Tweedie generalized linear mixed model with random intercept

### Description

Evaluates the loglikelihood of a Poisson-Tweedie generalized linear mixed model with random intercept, using the adaptive Gauss-Hermite quadrature rule.

### Usage

```
loglik.pt.1re(beta, D, a, Sigma, y, X, Z, id, offset = NULL, GHk = 5,
tol = 9.88131291682493e-324, GHs = NULL)
```

### Arguments

beta	Vector of regression coefficients
D	Dispersion parameter (must be $> 1$ )
а	Power parameter (must be < 1)
Sigma	A matrix with the variance of the random intercept
у	Response vector (discrete)
Χ	Design matrix for the fixed effects
Z	Design matrix for the random effects
id	Id indicator (it should be numeric)
offset	Offset term to be added to the linear predictor
GHk	Number of quadrature points (default is 5)
tol	Tolerance value for the evaluation of the probability mass function of the Poisson-Tweedie distribution
GHs	Quadrature points at which to evaluate the loglikelihood. If NULL (default value), the GH quadrature points are computed internally

#### Value

The loglikelihood value obtained using a Gauss-Hermite quadrature approximation with GHk quadrature points.

### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

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#### See Also

ptmixed and the examples therein

make.spaghetti

Generate a spaghetti plot to visualize longitudinal data

### Description

A spaghetti plot, or trajectory plot, is a plot that allows to compare across individuals or groups the trajectories of a longitudinal outcome

### Usage

```
make.spaghetti(x, y, id, group = NULL, data, col = NULL, pch = 16,
  lty = 1, lwd = 1, title = "", xlab = NA, ylab = NA,
  legend.title = "", xlim = NULL, ylim = NULL, cex.axis = 1,
  cex.title = 1, cex.lab = 1, cex.leg = 1, margins = NULL,
  legend.inset = -0.3, legend.space = 1)
```

### **Arguments**

X	the time variable (numeric vector)
у	the longitudinal outcome (numeric vector)
id	the subject indicator
group	the group that each subject belongs to (optional, do not specify if not relevant)
data	a data frame containing x, y, id and optionally group
col	a vector of colors (optional)
pch	dot type
lty	line type
lwd	line width
title	plot title
xlab	label for the x axis
ylab	label for the y axis
legend.title	legend title
xlim	limits for the x axis
ylim	limits for the y axis
cex.axis	font size for the axes
cex.title	title font size
cex.lab	font size for axis labels
cex.leg	font size for the legend
margins	use this argument if you want to overwrite the default function margins
legend.inset	moves legend more to the left / right (default is -0.3)
legend.space	interspace between lines in the legend (default is 1)

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#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

### **Examples**

```
# generate example data
set.seed(123)
n = 12; t = 6
id = rep(1:n, each = t)
rand.int = rep(rnorm(n, sd = 0.5), each = t)
group = rep(c(0,1), each = n*t/2)
time = rep(0:(t-1), n)
offset = rnorm(n*t, sd = 0.3)
beta = c(3, 0, 0.1, 0.3)
X = model.matrix(~group + time + group*time)
mu = 2^(X %*% beta + rand.int + offset)
y = rpois(n*t, lambda = mu)
group = ifelse(group == 0, 'control', 'treatment')
data.long = data.frame(y, group, time, id, offset)
rm(list = setdiff(ls(), 'data.long'))
# create plot
make.spaghetti(x = time, y, id, group,
data = data.long, title = 'spaghetti plot')
```

nbglm

Negative binomial generalized linear model

#### **Description**

Estimates a negative binomial generalized linear model.

```
nbglm(formula, offset = NULL, data, maxit = c(500, 1e+05), trace = T,
  theta.start = NULL)
```

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### Arguments

formula	A formula for the fixed effects part of the model. It should be in the form $y \sim x1 + x2$
offset	An offset to be added to the linear predictor. Default is NULL.
data	A data frame containing the variables declared in formula.
maxit	Vector containing the maximum number of iterations used in optim by the BFGS method and, if this fails, by the Nelder-Mead method
trace	Logical value. If TRUE, additional information is printed during the optimization. Default is TRUE.
theta.start	Numeric vector comprising initial parameter values for the vector of regression coefficients and the dispersion parameter

#### **Details**

Maximum likelihood estimation of a negative binomial GLM (the NB distribution is obtained as special case of the Poisson-Tweedie distribution when a = 0).

#### Value

A list containing the following elements: function's call (call); maximum likelihood estimate (mle); value of the loglikelihood at the mle (logl); convergence value (if 0, the optimization converged); the observed Fisher information (fisher.info) and the starting values used in the optimization (theta.init)

#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

### See Also

ptmixed for the Poisson-Tweedie GLMM

```
data(df1, package = 'ptmixed')
# estimate the model
fit1 = nbglm(formula = y ~ group*time, data = df1)
# view model summary
summary(fit1)
```

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nbmixed	Negative binomial generalized linear mixed model	

### **Description**

Estimates the negative binomial generalized linear mixed model with random intercept (here, the NB distribution is obtained as special case of the Poisson-Tweedie distribution when a = 0). Likelihood approximation for the model is based on the adaptive Gauss-Hermite quadrature rule.

### Usage

```
nbmixed(fixef.formula, id, offset = NULL, data, npoints = 5, hessian = T,
  trace = T, theta.start = NULL, reltol = 1e-08, maxit = c(10000, 100),
  freq.updates = 200, min.var.init = 0.001)
```

### Arguments

fixef.formula	A formula for the fixed effects part of the model. It should be in the form $y \sim x1 + x2$
id	A variable to distinguish observations from the same subject.
offset	An offset to be added to the linear predictor. Default is NULL.
data	A data frame containing the variables declared in fixef.formula.
npoints	Number of quadrature points employed in the adaptive quadrature. Default is 5.
hessian	Logical value. If TRUE, the hessian matrix is evaluated at the MLE to derive the observed Fisher information matrix. Default is TRUE.
trace	Logical value. If TRUE, additional information is printed during the optimization. Default is TRUE.
theta.start	Numeric vector comprising initial parameter values for the vector of regression coefficients, the dispersion parameter (using the same parametrization of ptmixed) and the variance of the random intercept. Default is NULL: initial parameter estimates are computed automatically by the function.
reltol	Relative tolerance to be used in optim. Default to 1e-8
maxit	Vector containing the maximum number of iterations used in optim by the Nelder-Mead method and, if this fails, by the BFGS method
freq.updates	Number of iterations after which the quadrature points are updated when the Nelder-Mead algorithm is used for the optimization. Default value is 200. To update the quadrature points at every iteration (note that this may make the computation about 10x slower), set freq.updates = 1 or freq.updates = NA. The function first tries to optimize the loglikelihood using the Nelder-Mead algorithm, updating the quadrature points every freq.updates iterations. If this fails to converge, a second attempt is made using the BFGS algorithm, for which the quadrature points are updated at every iteration.
min.var.init	If the initial estimate of the variance of the random intercept is smaller than this value, estimation is stopped and the user is advided to use the simpler Poisson-

Tweedie GLM is used. Default is 1e-3.

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#### Value

A list containing the following elements: function's call (call); maximum likelihood estimate (mle); value of the loglikelihood at the mle (logl); convergence value (if 0, the optimization converged); the observed Fisher information (fisher.info), if hessian = T; the number of quadrature points used (quad.points) and the starting value used in the optimization (theta.init); relevant warnings (warnings).

#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### See Also

```
summary.ptglmm, ranef
```

```
data(df1, package = 'ptmixed')
head(df1)
# 1) Quick example (hessian and SEs not computed)
# estimate the model
fit1 = nbmixed(fixef.formula = y ~ group + time, id = id,
              offset = offset, data = df1, npoints = 5,
              freq.updates = 200, hessian = FALSE, trace = TRUE)
# print summary:
summary(fit1, wald = FALSE)
# 2) Full computation, including computation of SEs
# estimate the model
fit2 = nbmixed(fixef.formula = y ~ group + time, id = id,
              offset = offset, data = df1, npoints = 5,
              freq.updates = 200, hessian = TRUE, trace = TRUE)
# print summary:
summary(fit2)
# extract summary:
results = summary(fit2)
ls(results)
results$coefficients
```

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pmf

Probability mass function plot for a discrete variable

### Description

This function produces a simple plot of the probability mass function of a discrete variable

### Usage

```
pmf(x, absolute = T, xlim = NULL, lwd = 1, col = "black",
  title = NULL, xlab = "x", bty = "l", cex.title = NULL,
  cex.axis = NULL)
```

### Arguments

x	the (discrete) variable of interest
absolute	logical. If TRUE (default) absolute frequencies are plotted, if FALSE relative frequencies $$
xlim	limits for the x axis
lwd	line width
col	color used for the vertical frequency bars
title	plot title
xlab	label for the x axis
bty	box type (default is bty="1")
cex.title	title font size
cex.axis	font size for the axes

### Author(s)

Mirko Signorelli

```
pmf(cars$speed)
pmf(cars$speed, absolute = FALSE)
pmf(cars$speed, lwd = 2, col = 'blue')
```

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ptglm Poisson-Tweedie generalized linear model
--

### **Description**

Estimates a Poisson-Tweedie generalized linear model.

### Usage

```
ptglm(formula, offset = NULL, data, maxit = c(500, 1e+05), trace = T,
    theta.start = NULL)
```

### **Arguments**

formula	A formula for the fixed effects part of the model. It should be in the form $y \sim x1 + x2$
offset	An offset to be added to the linear predictor. Default is NULL.
data	A data frame containing the variables declared in formula.
maxit	Vector containing the maximum number of iterations used in optim by the BFGS method and, if this fails, by the Nelder-Mead method
trace	Logical value. If TRUE, additional information is printed during the optimization. Default is TRUE.
theta.start	Numeric vector comprising initial parameter values for the vector of regression coefficients, the dispersion parameter and the power parameter (to be specified exactlyin this order!).

#### Value

A list containing the following elements: function's call (call); maximum likelihood estimate (mle); value of the loglikelihood at the mle (logl); convergence value (if 0, the optimization converged); the observed Fisher information (fisher.info) and the starting values used in the optimization (theta.init)

### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### See Also

ptmixed for the Poisson-Tweedie GLMM

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#### **Examples**

```
data(df1, package = 'ptmixed')
# estimate the model
fit1 = ptglm(formula = y ~ group*time, data = df1)
# view model summary:
summary(fit1)
```

ptmixed

Poisson-Tweedie generalized linear mixed model

### Description

Estimates the Poisson-Tweedie generalized linear mixed model with random intercept. Likelihood approximation for the model is based on the adaptive Gauss-Hermite quadrature rule.

### Usage

```
ptmixed(fixef.formula, id, offset = NULL, data, npoints = 5, hessian = T,
  trace = T, theta.start = NULL, reltol = 1e-08, maxit = c(10000, 100),
  freq.updates = 200, min.var.init = 0.001)
```

### Arguments

fixef.formula	A formula for the fixed effects part of the model. It should be in the form $y \sim x1 + x2$
id	A variable to distinguish observations from the same subject.
offset	An offset to be added to the linear predictor. Default is NULL.
data	A data frame containing the variables declared in fixef.formula.
npoints	Number of quadrature points employed in the adaptive quadrature. Default is 5.
hessian	Logical value. If TRUE, the hessian matrix is evaluated at the MLE to derive the observed Fisher information matrix. Default is TRUE.
trace	Logical value. If TRUE, additional information is printed during the optimization. Default is TRUE.
theta.start	Numeric vector comprising initial parameter values for the vector of regression coefficients, the dispersion parameter, the power parameter and the variance of the random intercept (to be specified exactlyin this order!). Default is NULL: initial parameter estimates are computed automatically by the function.
reltol	Relative tolerance to be used in optim. Default to 1e-8
maxit	Vector containing the maximum number of iterations used in optim by the Nelder-Mead method and, if this fails, by the BFGS method

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freq.updates

Number of iterations after which the quadrature points are updated when the Nelder-Mead algorithm is used for the optimization. Default value is 200. To update the quadrature points at every iteration (note that this may make the computation about 10x slower), set freq.updates = 1 or freq.updates = NA. The function first tries to optimize the loglikelihood using the Nelder-Mead algorithm, updating the quadrature points every freq.updates iterations. If this fails to converge, a second attempt is made using the BFGS algorithm, for which the quadrature points are updated at every iteration.

min.var.init

If the initial estimate of the variance of the random intercept is smaller than this value, estimation is stopped and the user is advided to use the simpler Poisson-Tweedie GLM is used. Default is 1e-3.

#### Value

A list containing the following elements: function's call (call); maximum likelihood estimate (mle); value of the loglikelihood at the mle (logl); convergence value (if 0, the optimization converged); the observed Fisher information (fisher.info), if hessian = T; the number of quadrature points used (quad.points) and the starting value used in the optimization (theta.init); relevant warnings (warnings).

#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### See Also

```
summary.ptglmm, ranef
```

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ranef

Compute random effects for Poisson-Tweedie and negative binomial mixed model

### **Description**

Compute the BLUP (best linear unbiased predictor) of the random effects for the Poisson-Tweedie and negative binomial generalized linear mixed models (fitted through ptmixed and nbmixed respectively)

### Usage

```
ranef(obj)
```

### **Arguments**

obj

an object of class ptglmm (obtained from ptmixed or nbmixed).

### Value

A vector with the EB estimates of the random effects

#### Author(s)

Mirko Signorelli

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#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### See Also

```
ptmixed, nbmixed
```

### **Examples**

simulate\_ptglmm

Simulate data from the Poisson-Tweedie generalized linear mixed model

### Description

Simulates a dataset comprising t repeated measurements for n subjects from a Poisson-Tweedie GLMM. Subjects are assumed to belong to two different groups. The linear predictor comprises an intercept, main effects of group and of time, and the interaction between time and group; a random intercept; and, optionally, a normally-distributed offset term.

### Usage

```
simulate_ptglmm(n = 20, t = 5, seed = 1, beta = c(3, 0, 0, 0.4), D = 1.5, a = -1, sigma2 = 0.8^2, offset = F)
```

#### **Arguments**

n	number of subjects
t	number of time points (0, 1,, t-1)
seed	seed for random number generation
beta	vector of regression coefficients, to be specified in this order: intercept, group main effect, time main effect, group*time interaction

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D	dispersion parameter of the Poisson-Tweedie distribution $(D > 1)$
a	power parameter of the Poisson-Tweedie distribution (a $< 1$ )
sigma2	Variance of the subject-specific random intercept
offset	Logical value. If TRUE, a normally-distributed offset is added to the linear predictor.

#### Value

A list containing the following elements: a dataframe (data) containing the response y, the subject id, the group indicator and time; a vector with the true random intercept values (true.randint).

#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### **Examples**

```
# simulate a simple, small dataset
example1 = simulate_ptglmm(n = 5, t = 2)
example1$data
# the function allows to set several different parameters
example2 = simulate_ptglmm(n = 20, t = 5, seed = 1,
beta = c(2.2, 1.2, 0.3, -0.5), D = 1.8, a = 0.5,
sigma2 = 0.7, offset = TRUE)
# view the distribution of the response variable:
pmf(example2$data$y)
# visualize the data with a trajectory plot:
make.spaghetti(x = time, y = y, id = id,
group = group, data = example2$data)
```

summary.ptglm

Summarizing Poisson-Tweedie and negative binomial GLM estimation results

### Description

Provides parameter estimates, standard errors and univariate Wald test for the Poisson-Tweedie and the negative binomial generalized linear models (fitted through ptglm and nbglm respectively)

```
## S3 method for class 'ptglm'
summary(object, silent = F, ...)
```

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### **Arguments**

object	an object of class ptglm (obtained from ptglm or nbglm). #' @param silent logical. If TRUE, information on parameter estimates and tests is not printed on screen. Default is FALSE (info is printed)
silent	logical. If TRUE, information on parameter estimates and tests is not printed on screen. Default is FALSE (info is printed)
	Further arguments passed to or from other methods.

### Value

A list with the following elements: logl, coefficients, D, a

### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

### See Also

ptglm, nbglm and the examples therein

summary.ptglmm	Summarizing Poisson-Tweedie and negative binomial mixed model estimation results
	ununon resuns

### Description

Provides parameter estimates, standard errors and univariate Wald test for the Poisson-Tweedie and negative binomial generalized linear mixed models (fitted through ptmixed and nbmixed respectively)

```
## S3 method for class 'ptglmm'
summary(object, wald = T, silent = F, ...)
```

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### Arguments

object	an object of class ptglmm (obtained from ptmixed or nbmixed).
wald	logical. If TRUE, standard errors and univariate Wald test are computed. Default is TRUE.
silent	logical. If TRUE, information on parameter estimates and tests is not printed on screen. Default is FALSE (info is printed)
	Further arguments passed to or from other methods.

#### Value

A list with the following elements: value of the loglikelihood at the MLE (log1), table with maximum likelihood estimates of the regression coefficients, SEs and Wald tests coefficients, and maximum likelihood estimates of the other parameters (D, a and sigma2)

#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

#### See Also

ptmixed, nbmixed and the examples therein

wald.test	Wald test for regression coefficients	
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#### **Description**

Compute a multivariate Wald test for one of the following models: Poisson-Tweedie GLMM, negative binomial GLMM, Poisson-Tweedie GLM, negative binomial GLM. The null hypothesis has to be specified in the (matrix) form L b = k, where b is the vector of regression coefficients and L and k are defined below

```
wald.test(obj, L, k = NULL)
```

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### **Arguments**

obj	an object of class $ptglmm$ (obtained from $ptmixed$ or $nbmixed$ ) or $ptglm$ (obtained from $ptglm$ or $nbglm$ )
L	a matrix used to define the hypothesis to test, in the form $L b = k$
k	a vector used to define the hypothesis to test, in the form $L b = k$ . Default is a null vector ( $L b = 0$ )

#### Value

A data frame with the result of the test

#### Author(s)

Mirko Signorelli

#### References

Signorelli, M., Spitali, P., Tsonaka, R. (2021). Poisson-Tweedie mixed-effects model: a flexible approach for the analysis of longitudinal RNA-seq data. Statistical Modelling, 21 (6), 520-545. URL: https://doi.org/10.1177/1471082X20936017

```
# generate data
data(df1, package = 'ptmixed')

# estimate one of the following models: a Poisson-Tweedie or
# negative binomial GLMM (using ptmixed() or nbmixed()), or
# a Poisson-Tweedie or negative binomial GLM (using ptglm()
# or nbgml())
fit1 = nbglm(formula = y ~ group*time, data = df1)

# define L for beta2 = beta4 = 0
L = matrix(0, nrow = 2, ncol = 4)
L[1, 2] = L[2, 4] = 1

# compute multivariate Wald test
wald.test(obj = fit1, L = L, k = NULL)
```

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