Package 'vfcp'

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Type Package

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Title Computation of v Values for U and Copula C(U, v)

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Depends copula, extraDistr, stringr

Suggests knitr, rmarkdown

Description Computation the value of one of two uniformly
distributed marginals if the copula probability value is known
and the value of the second marginal is also known.
Computation and plotting corresponding cumulative
distribution function or survival function.
The numerical definition of a common area limited by lines
of the cumulative distribution function and survival function.
Approximate quantification of the probability of this area.
In addition to 'amh', the copula dimension may be larger than 2.

License GPL (>= 3)

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R topics documented:

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vfcp-package   *Computation of v Values for U and Copula C(U, v)*

Description

Computation v when u and C(u, v) copula are known. Calculation and plotting of cumulative distribution and survival function when u, C(u, v) copula and marginal distributions are known. These calculations can be tabulated as option. The numerical definition of a common area limited by lines of the cumulative distribution function and survival function. Approximate quantification of the probability of this area. In addition to 'amh', the copula dimension may be larger than 2.

Details

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Version:	1.4.0
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License:	GPL (>= 3)

Author(s)

Josef Brejcha

Maintainer: Josef Brejcha <brchjo@gmail.com>

References

A.K. SUZUKI, F. LOUZADA and V.G. CANCHO, On estimation and influence diagnostics for a Bivariate Promotion Lifetime Model Based on the FGM Copula: A Fully Bayesian Computation, *Tendencias em Matematica Aplicada e Computacional, 14, N. 3 (2013), 441-461*, `http://www.scielo.br/pdf/tema/v14n3/a14v14n3.pdf`

M. Mahfoud, "Bivariate Archimedean copulas: an application to two stock market indices", *Vrije Universiteit Amsterdam*, **BMI Paper**, Amsterdam-2012, `http://docplayer.net/24882927-Bivariate-archimedean-co html`

Copula (probability theory), `https://en.wikipedia.org/wiki/Copula_(probability_theory)` Statistical - Distributions - Inverted Beta distribution - Example, `http://www.xycoon.com/ibeta.htm`

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gentruk	*Creating an object for CDF and copula survival*

Description

For given inputs, the coordinates of the object defined by the CDF and the survival function for the copula object are created.

Usage

```
gentruk(tht, fm, C, pro)
```

Arguments

tht	Copula parameter. If fam = "fgm", it must be a vector of size $dm*(dm-1)/2+1$.
fm	Family name copula. These can be: "clayton", "gumbel", "frank", "joe", "amh", "fgm".
C	Probability value of the copula. Single value.
pro	Numeric vector. Its pro[1:k] are upper values of the u. Next pro[-c(1:k)] are then all greater than or equal to 1.

Value

A list with components as [trimeze](#) value.

Author(s)

Josef Brejcha

Examples

```
tht = 0.6
cx = c(0.025, 0.05, 0.1, 0.15, 0.25)
pro = c(0.99999, 0.9999, 0.999, 0.99, 24, 16, 8, 4)
dm = 2
fam = "fgm"
marg = c("weibull", "betapr")
xo = c(200, 2.75, 16.5, 6.60)
e12 = vfenuo(marg, xo)
p = numeric(length(cx))
x12 = qweibull(0.975, scale = xo[1], shape = xo[2])
y12 = qbetapr(0.975, shape1 = xo[3], shape2 = xo[4])
mtit = paste(fam, " ... ", marg[1], "(", xo[1], ", ", xo[2], ")",
 " ", marg[2], "(", xo[3], ", ", xo[4], ")",
 sep = "")
plot(NULL, NULL, xlim = c(0, x12), ylim = c(0, y12),
     xlab = paste("x, E[x] = ", round(e12[1], 2)),
 ylab = paste("y, E[y] = ", round(e12[2], 2)),
 main = mtit)
points(e12[1], e12[2], pch = 20)
abline(h = e12[2], v = e12[1])
grid(col = "grey50")
#===========================
kop2 = kopula(fam, tht, dm)
fmc = c("", "", "clayton", "gumbel", "frank", "joe")
pro = c(0.999999, 0.99999, 0.9999, 16, 8, 4, 2)
tm3 = list()
tmk = list()
for (k in 1:length(cx)){
  tm3 = gentruk(tht, fm=fam, C=cx[k], pro)
  tmk[[k]] = tm3
}
p = prosim(C = cx, fam, tht, dm, no = 100000)
# =============
xa = c("u")
ya = c("v")
for (k in 1:length(cx)){
  mspx = vfmrg(rdj=marg, i=1, cosi=tmk[[k]]$sp$s1, yo=xo, cdf=TRUE)
  mspy = vfmrg(rdj=marg, i=2, cosi=tmk[[k]]$sp$s2, yo=xo, cdf=TRUE)
  mcpx = vfmrg(rdj=marg, i=1, cosi=tmk[[k]]$cp$c1, yo=xo, cdf=TRUE)
  mcpy = vfmrg(rdj=marg, i=2, cosi=tmk[[k]]$cp$c2, yo=xo, cdf=TRUE)
  lines(mspx,mspy, col=k)
  lines(mcpx, mcpy, col = k)
}
  legend("topleft", legend = c("C", cx), text.col = c(1, 1:length(cx)),
         bty = "n")
  legend("topright", legend = c("p", round(p, 4)),
         text.col = c(1, 1:length(cx)), bty = "n")
```

---

kopula   *Copula object*

Description

Generate the copula object.

Usage

```
kopula(fam, tht, dm)
```

Arguments

fam	Family name copula. These can be: "clayton", "gumbel", "frank", "joe", "amh", "fgm".
tht	Copula parameter.
dm	Copula dimension.

Value

Copula object

Author(s)

Josef Brejcha

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prosim	*Monte Carlo method*

Description

Probability of the inside of an object as defined by CDF and survival. For this, the Monte Carlo method is used.

Usage

```
prosim(C, fam, tht, dm, no)
```

Arguments

C	single numeric; CDF value. Survival value is 1 - CDF.
fam	Family name copula. These can be: "clayton", "gumbel", "frank", "joe", "amh", "fgm".
tht	Copula parameter. If fam = "fgm", it must be a vector of size $dm*(dm-1)/2+1$.
dm	Copula dimension
no	Monte Carlo sample size

Value

Probability

Author(s)

Josef Brejcha

Examples

```
tht = 10.6
cx = c(0.05, 0.1, 0.15, 0.25)
pro = c(0.99999, 0.9999, 0.999, 0.99, 24, 16, 8, 4)
dm = 4
fam = "gumbel"
marg = rep(c("weibull", "betapr"), 2)
xo = rep(c(200, 2.75, 16.5, 6.60), 2)
#=========================
kop2 = kopula(fam, tht, dm)
fmc = c("", "", "clayton", "gumbel", "frank", "joe")
pro = c(0.999999, 0.99999, 0.9999, 16, 8, 4, 2)
tm3 = list()
tmk = list()
# di = dm*(dm - 1)/2
for (k in 1:length(cx)){
  tm3 = gentruk(tht, fm=fam, C=cx[k], pro)
  tmk[[k]] = tm3
}
np = 5
no = 100000
ncx = length(cx)
p = array(0, c(np*ncx, 2))
colnames(p) = c("C", "p")
k = 0
for (i in 1:length(cx)){
  for (j in 1:np){
    k = k + 1
    p[k, 1] = cx[i]
    p[k, 2] = prosim(C = cx[i], fam, tht, dm, no)
  }
}
plst = list()
print(paste(fam, "dim =", dm, "tht =", tht, "n =", no, "nrep.", np))
for (k in 1:ncx){
  plst[[k]] = summary(p[p[, 1] == cx[k], 2])
  print(paste("cx =", cx[k]))
  print(plst[[k]])
}
```

---

prunikus   *The coordinates of the intersection lines of the cumulative distribution function and survival function*

Description

The coordinates of the intersection lines of the cumulative distribution function and survival function.

Usage

```
prunikus(x, y)
```

Arguments

x	Numeric vector of size 4. The horizontal coordinates of opposite points.
y	Numeric vector of size 4. The vertical coordinates of opposite points.

Value

Numeric vector size 2.

Author(s)

Josef Brejcha

References

Line-line intersection, https://en.wikipedia.org/wiki/Line-line_intersection

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trimeze	*Coordinates of an object defined by CDF and survival functions*

Description

Calculates the coordinates of the object defined matrices C1 and C23. Both matrices are two-row.

Usage

```
trimeze(C1, C23)
```

Arguments

C1	numerical probability two-row matrix defining survival line
C23	numerical probability two-row matrix defining CDF line

Value

A list with components as follows:

tlc	upper left corner coordinates
brc	bottom right corner coordinates
sp	survival line coordinates
cp	CDF line coordinates

Author(s)

Josef Brejcha

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vfalihaq	*Ali-Mikhail-Haq Copula Variable Given Second One and Copula Probability*

Description

v for Ali-Mikhail-Haq copula `C(u, v)` given probability `C(u, v)` and `u`.

Usage

```
vfalihaq(C, u, tht)
```

Arguments

C	Probability value of the Ali-Mikhail-Haq copula. It can be a vector.
u	The first variable value of the `C(u, v)`. `u` can be a vector if `C` is a single. `u` is a matrix with `nrow = length(C)` if `C` is a vector.
tht	Copula parameter

Details

The value of the `u` must be grater than `C`.

Value

The value of the second variable depending on the first variable and copula probability value.

Author(s)

Josef Brejcha

Examples

```
require(copula)
C = 0.3
tht = 0.5
u = c(0.35, 0.40, 0.45)
v <- vfalihaq(C, u, tht)
kali <- archmCopula(family = "amh", param = tht, dim = 2)
pCopula(cbind(u, v), kali)
#
Cf <- c(0.3, 0.4)
mx <- matrix(c(seq(0.35, 0.45, 0.05), seq(0.5, 0.6, 0.05)),
             nrow = 2, ncol = 3, byrow = TRUE)
rownames(mx) <- Cf
vfalihaq(C = Cf, u = mx , tht=0.5)
#         [,1]      [,2]      [,3]
# 0.3 0.8019802 0.6774194 0.5918367
# 0.4 0.7500000 0.6739130 0.6153846
```

---

vfclayton	*Clayton Copula Variable Given Second One and Copula Probability*

Description

v for Clayton copula C(u, v) given probability C(u, v) and u.

Usage

```
vfclayton(C, u, tht)
```

Arguments

C	Probability value of the Clayton copula. It can be a vector.
u	The first variable value of the C(u, v). u can be a vector if C is a single. u is a matrix with nrow = length(C) if C is a vector.
tht	Copula parameter

Details

The value of the u must be grater than C.

Value

The value of the second variable depending on the first variable and copula probability value.

Author(s)

Josef Brejcha

Examples

```
C <- 0.3
tht <- 6
u <- c(0.35, 0.4, 0.45)
v <- vfclayton(C, u, tht)
kop = claytonCopula(tht)
pCopula(cbind(u, v), kop)
#
Cf <- c(0.3, 0.4)
mx <- matrix(c(seq(0.35, 0.45, 0.05), seq(0.5, 0.6, 0.05)),
  nrow = 2, ncol = 3, byrow = TRUE)
rownames(mx) <- Cf
vfclayton(C = Cf, u = mx , tht=7)
#          [,1]      [,2]      [,3]
# 0.3 0.3183261 0.3061926 0.3025859
# 0.4 0.4135555 0.4064530 0.4033610
```

---

vfenuo   *Expected values of marginal distributions*

Description

Auxiliary function that calculates the expected values of marginal distributions.

Usage

```
vfenuo(marg, xo)
```

Arguments

marg   Character vector size greater than or equal to 2. Its components can now be
                c("weibull", "gamma", "lnorm", "norm", "betapr", "beta").

xo   Vector size 2*length(marg) of parameters of marg.

xo[odd]	scale, meanlog, mean, shape1
xo[even]	shape, sdlog, sd, shape2

Value

Numeric vector size equal to length(marg).

Author(s)

Josef Brejcha

Examples

```
vfenuo(marg = c("betapr", "beta", "norm", "weibull"),
  xo = c(5, 5, 3, 20, 30, 5, 100, 1.5))
```

---

vfex	*Compute vector V for C(u, V)*

Description

A vector `v` is computed for `C` and numeric probability vector `u`.

Usage

```
vfex(C, u, th, fm)
```

Arguments

C	Copula probability. It is a single value.
u	Probability vector. All its components are greater than C.
th	Copula parameter.
fm	character; A name of copula. One of c("clayton", "frank", "gumbel", "amh", "joe", "fgm"). "amh", "joe", "fgm" names are for Ali-Mikhail-Haq, Joe, Farlie-Gumbel-Morgenstern copulas.

Value

Numeric vector.

Author(s)

Josef Brejcha

---

vffgm	*Farlie-Gumbel-Morgenstern Copula Variable Given Second One and Copula Probability*

Description

`v` for Farlie-Gumbel-Morgenstern copula `C(u, v)` given probability `C(u, v)` and `u`.

Usage

```
vffgm(C, u, tht)
```

Arguments

C	Probability value of the Farlie-Gumbel-Morgenstern copula. It can be a vector.
u	The first variable value of the C(u, v). u can be a vector if C is a single. u is a matrix with nrow = length(C) if C is a vector.
tht	Copula parameter

Details

The value of the u must be grater than C.

Value

The value of the second variable depending on the first variable and copula probability value.

Author(s)

Josef Brejcha

References

A.K. SUZUKI, F. LOUZADA and V.G. CANCHO, On estimation and influence diagnostics for a Bivariate Promotion Lifetime Model Based on the FGM Copula: A Fully Bayesian Computation, *Tend^encias em Matem´ atica Aplicada e Computacional, 14, N. 3 (2013), 441-461*, http://www.scielo.br/pdf/tema/v14n3/a14v14n3.pdf

Examples

```
require(copula)
C = 0.3
tht = 0.5
u = c(0.35, 0.40, 0.45)
v <- vffgm(C, u, tht)
kfgm <- fgmCopula(tht)
pCopula(c(u, v), kfgm)
#
Cf <- c(0.3, 0.4)
mx <- matrix(c(seq(0.35, 0.45, 0.05), seq(0.5, 0.6, 0.05)),
             nrow = 2, ncol = 3, byrow = TRUE)
rownames(mx) <- Cf
vffgm(C = Cf, u = mx , tht=0.5)
#          [,1]      [,2]      [,3]
# 0.3 0.8064052 0.6853009 0.6007056
# 0.4 0.7535751 0.6781648 0.6195239
```

---

vffrank   *Frank Copula Variable Given Second One and Copula Probability*

Description

v for Frank copula `C(u, v)` given probability `C(u, v)` and u.

Usage

```
vffrank(C, u, tht)
```

Arguments

C	Probability value of the Frank copula. It can be a vector.
u	The first variable value of the `C(u, v)`. u can be a vector if `C` is a single. u is a matrix with `nrow = length(C)` if `C` is a vector.
tht	Copula parameter

Details

The value of the u must be grater than `C`.

Value

The value of the second variable depending on the first variable and copula probability value.

Author(s)

Josef Brejcha

Examples

```
C <- 0.3
tht <- 6
u <- c(0.35, 0.4, 0.45)
v <- vffrank(C, u, tht)
kop = frankCopula(tht)
pCopula(cbind(u, v), kop)
```

---

vfgumbel   *Gumbel Copula Variable Given Second One and Copula Probability*

Description

v for Gumbel copula `C(u, v)` given probability `C(u, v)` and u.

Usage

```
vfgumbel(C, u, tht)
```

Arguments

C	Probability value of the Gumbel copula. It can be a vector.
u	The first variable value of the `C(u, v)`. u can be a vector if C is a single. u is a matrix with `nrow = length(C)` if C is a vector.
tht	Copula parameter

Details

The value of the u must be grater than C.

Value

The value of the second variable depending on the first variable and copula probability value.

Author(s)

Josef Brejcha

Examples

```
C <- 0.3
tht <- 6
u <- c(0.35, 0.4, 0.45)
v <- vfgumbel(C, u, tht)
kop = gumbelCopula(tht)
pCopula(cbind(u, v), kop)
#
vfgumbel(c(0.3, 0.4), u = rbind(seq(0.35, 0.45, 0.05),
  seq(0.45, 0.55, 0.05)), 8)
#           [,1]      [,2]      [,3]
# [1,] 0.3184504 0.3053987 0.3017235
# [2,] 0.4184819 0.4051936 0.4015295
```

---

vfjoe *Joe Copula Variable Given Second One and Copula Probability*

Description

v for Joe copula C(u, v) given probability C(u, v) and u.

Usage

```
vfjoe(C, u, tht)
```

Arguments

C   Probability value of the Joe copula. It can be a vector.

u   The first variable value of the C(u, v). u can be a vector if C is a single. u is a
                matrix with nrow = length(C) if C is a vector.

tht   Copula parameter

Details

The value of the u must be grater than C.

Value

The value of the second variable depending on the first variable and copula probability value.

Author(s)

Josef Brejcha

Examples

```
C <- 0.3
tht <- 6
u <- c(0.35, 0.4, 0.45)
v <- vfjoe(C, u, tht)
kop = joeCopula(tht)
pCopula(cbind(u, v), kop)
#
Cf <- c(0.3, 0.4)
mx <- matrix(c(seq(0.35, 0.45, 0.05), seq(0.5, 0.6, 0.05)),
             nrow = 2, ncol = 3, byrow = TRUE)
rownames(mx) <- Cf
vfjoe(C = Cf, u = mx , tht=6)
#           [,1]      [,2]      [,3]
# [1,] 0.4021216 0.3513741 0.3274672
# [2,] 0.4379531 0.4184746 0.4087143
```

---

vfmrg   *Auxiliary function*

Description

Auxiliary function used in vfploto. It computes random variable value of the CDF or survival which can be one of the c("weibull", "gamma", "lnorm", "norm", "betapr", "beta").

Usage

```
vfmrg(rdj, i, cosi, yo, cdf)
```

Arguments

rdj   A character vector. Its components are from c("weibull", "gamma", "lnorm", "norm", "betapr", "beta").

i   An index of the rdj

cosi   A vector of probabilities

yo   Vector size 2*length(rdj) of parameters of rdj

yo[1], yo[3]	scale, meanlog, mean, shape1
yo[2], yo[4]	shape, sdlog, sd, shape2

cdf   Cumulative distribution function when TRUE, survival otherwise.

Details

"betapr" is the name of 'BetaPrime' distribution from extrDistr package. The other name 'BetaPrime' is 'Inverted Beta'.

Value

Numeric vector

Author(s)

Josef Brejcha

vfploto	*Plotting the cumulative distribution function or survival function*

Description

Plotting the cumulative distribution function or survival function.

Usage

```
vfploto(cx, pro, fam, marg, xo, tht, cdf=TRUE, plt=TRUE, rtn=FALSE,
  ped = TRUE)
```

Arguments

cx	A vector of copula probabilities.
pro	Numeric vector. Its `pro[1]` is upper value of the u. Next `pro[-1]` are then all greater than or equal to 1. The second case of `pro` is all `pro` less than 1. The first case is an extra calculation of the u values. In the latter case, u values can be pre-selected.
fam	character; A name of copula. One of c("clayton", "frank", "gumbel", "amh", "joe", "fgm"). "amh", "joe", "fgm" names are for Ali-Mikhail-Haq, Joe, Farlie-Gumbel-Morgenstern copulas.
marg	A vector size 2. Combination of these marginals: c("weibull", "gamma", "lnorm", "norm", "betapr", "beta").
xo	A vector of marginal distribution parameters. It is size 4 with these components:

xo[1], xo[3]	scale, meanlog, mean, shape1
xo[2], xo[4]	shape, sdlog, sd, shape2

tht	copula parameter
cdf	logical; Computation for CDF when TRUE. If FALSE is the same for Survival.
plt	Plot only when TRUE.
rtn	Print output value only when TRUE.
ped	Compute and add to plot an expected values o f marginal distributions when $ped = TRUE$.

Details

Must not be `plt` and `rtn` at the same time equal to FALSE.

Value

If `rtn` is TRUE, then a list of these components:

Type	character; `"CDF"` or `"Survival"`
P	numeric; CDF or Survival value
x	numeric vector of the first marginal values for `P`
y	numeric vector of the second marginal values for `P`
u	numeric vector of the first copula marginal values
v	numeric vector of the second copula marginal values

Author(s)

Josef Brejcha

Examples

```
require(copula)
tht = 0.475
cx = c(0.0025, 0.05, seq(0.1, 0.9, 0.1), 0.95, 0.975)
# nC = length(cx)
proh = c(0.9999999, 8, 4, 4, 4)
prod = c(0.999, 8, 4, 4, 4)
fam = "clayton"
marg = c("weibull", "lnorm")
xo = c(100, 1.5, 3, 0.425)
suro = vfploto(cx, proh, fam, marg, xo, tht, cdf=FALSE, plt=TRUE, rtn=FALSE)
cdfo = vfploto(cx, prod, fam, marg, xo, tht, cdf=TRUE, plt=TRUE, rtn=FALSE)
##
cx = 0.4
vfploto(cx, proh, fam, marg, xo, tht, cdf=TRUE, plt=FALSE, rtn=TRUE,
        ped = TRUE)
```

---

vfprifo	*Computation of the vector* u *to compute the second vector* v

---

Description

Auxiliary function. Each vector value u must be greater than the probability of the copula.

Usage

```
vfprifo(ck, pro)
```

Arguments

ck	Copula probability. Single value. Not a vector.
pro	Numeric vector. All its components are less than 1. u can be pre-set in the desired values.

Value

Numeric vector.

Author(s)

Josef Brejcha

---

vfpripo   *Computation of the vector* u *to compute the second vector* v

---

Description

Auxiliary function. Each vector value u must be greater than the probability of the copula.

Usage

```
vfpripo(ck, pro)
```

Arguments

ck	Copula probability. Single value. Not a vector.
pro	Numeric vector. Its pro[1:k] are upper values of the u. Next pro[-c(1:k)] are then all greater than or equal to 1.

Value

Numeric vector.

Author(s)

Josef Brejcha

Examples

```
prk = c(0.99999, 0.9999, 0.999, 0.99, 8, 4, 2)
C = 0.1
u = vfpripo(ck = C, pro = prk)
```

Index