# Package 'Rcapture'

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# **Description**

Estimation of abundance and of other demographic parameters for closed populations, open populations and the robust design in capture-recapture experiments using loglinear models.

This package focuses on closed populations. Since version 1.2-0, no new features have been added to open populations and robust design functions.

### **Details**

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Type: Package
Version: 1.4-4
Date: 2022-05-03
License: GPL-2

# **SUMMARY OF Reapture CONTENTS**

The **Reapture** package contains nine capture-recapture data sets and the following functions:

- Model fitting functions for
  - > closed populations:
    - closedp functions: fit various loglinear models for abundance estimation,
    - closedpCI functions: fit one customized loglinear model and calculate a confidance interval for the abundance estimation,
    - closedpMS.t: fits various hierarchical loglinear models in a perspective of model selection.
    - closedp.bc: performs bias corrections to the abundance estimations from customized loglinear models,

closedp.Mtb: fits model Mtb, which cannot be fitted by any other function, for abundance estimation;

# > open populations:

- openp: computes various demographic parameters using a loglinear model;

### > robust design:

- robustd functions: compute various demographic parameters and capture probabilities per period using a loglinear model.
- Descriptive statistics functions:
  - descriptive: produces basic descriptive statistics for capture-recapture data;
  - uifit: produces fit statistics concerning the  $u_i$ , i.e. the numbers of first captures on each capture occasion, for closed population models.
- Data manipulation functions:
  - histpos functions: builds a matrix of observable capture histories;
  - periodhist: merges capture occasions.

#### DESCRIPTION OF DATA SET FORMATS

In capture-recapture experiments, the data collected consist of capture histories for captured units. A capture history is simply a serie of capture indicators for each capture event in the experiment. The capture history of one unit is expressed as a length t vector  $w = (w_1, \ldots, w_t)$ , where  $w_j = 1$  if the unit is captured at the jth occasion and 0 if not. For closed populations, capture events are named capture occasions, whereas they are named capture periods for open populations.

Capture-recapture data sets are given to **Rcapture** functions through the X argument. X must be a numeric matrix. Arguments dfreq and dtype indicate the format of the matrix. Each have two possible values, meaning that four data set formats are possible with **Rcapture**.

### FORMAT 1 - CAPTURE HISTORY PER UNIT

If dfreq=FALSE and dtype="hist" (the default), X has one row per unit captured in the experiment. Each row is an observed capture history. It must contain only zeros and ones; the number one indicates a capture. In this case, the number of columns in the table represents the number of capture occasions in the experiment (noted t). Here is an example of a data set of this type for t=2:

- 11
- 1 1
- 10
- 10
- 1 0 1 0
- 0 1

### FORMAT 2 - AGGREGATED CAPTURE HISTORIES

If dfreq=TRUE and dtype="hist", X contains one row per observed capture history followed by its frequency. In that case, X has t+1 columns. As for format 1, the first t columns of X, identifying the capture histories, must contain only zeros and ones. The number one indicates a capture. In this format, the example data set is represented by the following matrix:

112

104

If a possible capture history is not observed, it can appear in X with a frequency of zero, or it can simply be omitted.

#### FORMAT 3 - NUMBER OF CAPTURES PER UNIT

If dfreq=FALSE and dtype="nbcap", X is a vector with the number of captures for every captured unit. Therefore, this format does not contain complete capture histories. Instead, capture histories are summarized through the number of captures. In this format, the example data set looks like: 2 2 1 1 1 1 1

#### FORMAT 4 - AGGREGATED NUMBERS OF CAPTURES

If dfreq=TRUE and dtype="nbcap", X is a 2 columns matrix. The first column contains the observed numbers of captures, the second columns contains their frequencies. In this format, the example data is:

22

15

#### DETAILS ABOUT FORMATS WITH NUMBERS OF CAPTURES

Only few functions have the dtype argument. Functions without dtype argument accept only a data matrix X of the form dtype="hist". So the first two formats listed above are the most common.

Formats with dtype="nbcap" are used for captures in continuous time (see below). They are also useful to reduce the size of the data set for experiments with a large number of capture occasions t (often with no units caught a large number of times). For theses formats, the number of capture occasions t cannot be deduced from X as it can be with dtype="hist". One has no garanties that the larger number of captures observed is the total number of capture occasions. Therefore, if one gives a data matrix X with dtype="nbcap", one must also provide t, the number of capture occasions, as an additional argument.

For now, the data formats with dtype="nbcap" are not generalized to the robust design. So dtype is not an argument of the robustd.0 function.

#### CAPTURES IN CONTINUOUS TIME

In some capture-recapture experiments, there is no well defined capture occasions. Captures occur in continuous time. The data set ill comes from such an experiment. Bohning and Schon (2005) call this type of capture-recapture data *repeated counting data*. These data sets always have the format dtype="nbcap".

We can estimate abundance for data of this type using the option t=Inf with the functions closedpCI.0 and closedpCI.0. The function descriptive also accepts t=Inf. It modifies the y coordinate of the exploratory heterogeneity graph.

#### DISTINCTION BETWEEN .t and .0 FUNCTIONS

Capture recapture models for closed population aim at estimating the population size by modelling the probabilities of the different capture histories. The data available to fit these models consist of observed frequencies of capture histories. These frequencies are modeled in Rcapture using loglinear models for frequency tables. For functions with a name ending with .t (closedp.t,

closedpCI.t, closedpMS.t and robustd.t), the observed values of the response variable is the vector of frequencies for every observable capture history. It has length  $2^t - 1$ .

However, for a model without temporal effect (assuming that the probability of capturing a unit does not vary between capture occasions), all the information needed to fit the model can be found in aggregated data. Functions with a name ending with .0 (closedp.0, closedpCI.0 and robustd.0) fit models using as response variable the number of units captured i times, for  $i=1,\ldots,t$ . It is a vector of length t, which is much shorter than  $2^t-1$  for a large t. Because of an appropriate offset added to the model, the results from a .0 function match exactly the results from a .t function for a corresponding capture-recapture model. Because .0 functions deal with smaller design matrix, they run faster than .t functions, but they cannot fit models with a temporal effect.

#### FUNCTIONS USED FOR MODEL FITTING

Most of the **Reapture** functions use the function glm of the **stats** package to fit a loglinear model. However, the function optim, again of the **stats**, is also used by three functions:

- closedpCI.t, closedpCI.0 and closedpMS.t: when a normal heterogeneous models is requested.
- closedp. Mtb: because model Mtb does not have a loglinear form.

#### ERRORS AND WARNINGS MANAGEMENT IN CLOSED POPULATION FUNCTIONS

If an error occurs while executing a function fitting only one closed population model (closedpCI functions, closedp.bc, closedp.Mtb), the execution is stopped and the error message is printed (usual behavior in R). However, if an error occurs while fitting a model in a call to a closedp population function fitting more than one model (closedp functions, closedpMS.t), the execution of the call is not stopped. Instead, the row in the results table for the problematic model is filled with NA and the error message is stored in an output value. This value is called glm.err for closedp functions. It is however called fit.err for closedpMS.t because this function do not always use glm to fit the model (as mentionned above, optim is used for normal heterogeneous models).

Warning messages while fitting a closed population model, if any, are stored in an output value called 'glm.warn', 'fit.warn' or 'optim.warn' depending on the function. They are not printed in the console. To inform the user that a warning occured, the last column of the results table, named infoFit, contains a numerical code giving information about errors or warnings encountered. Here is a description of the meaning of the numerical code:

**0** no error or warning occured while fitting the model;

- -1 an error occured while fitting the model;
- 1 a warning indicating that the model fit is questionnable occured (algorithm did not converge, non-positive sigma estimate for a normal heterogeneous model or large asymptotic bias);
- 2 the warning 'design matrix not of full rank' occured, therefore some model's coefficients are not estimable;
- **3** a warning not of type 1 or 2 occured (the glm warning 'fitted rates nummerically 0 occured' is often encountered with small frequencies, it does not always mean that the model fit is questionnable).

The elements in the column infoFit can contain more than one number since more than one warning can occur. For exemple, if infoFit takes the value 13 for a model, it means that at least one

warning of type 1 and one warning of type 3 have occured. If more than one warning of the same type are encountered, the number representing the type of warning is not repeated in infoFit.

### Author(s)

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#### References

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Rivest, L.P. (2008) Why a time effect often has a limited impact on capture-recapture estimates in closed populations. *Canadian Journal of Statistics*, **36**(1), 75–84.

```
# Here is an example on the lesbian data set.

desc <- descriptive(lesbian, dfreq = TRUE)
desc
plot(desc)

# 1612 out of 2185 individuals (74%) appear on one list only.
# The exploratory heterogeneity graph are not quite linear.
# Some heterogeneity in the units capture probabilities
# seem present in the data set.</pre>
```

BBS2001 7

```
closedp(lesbian, dfreq = TRUE)
 # According to the BIC, the best model is Mth Darroch.
 # Let's see if adding interactions between capture
 # histories to the model could improve the model's fit.
 closedpMS.t(lesbian, dfreq = TRUE, h = "Darroch")
 # According to the BIC, the best heterogeneous Darroch model
 # contains the double interactions 12, 13, 14.
 # Here is the profile likelihood confidence interval for the
 # abundance estimation from this model.
 closedpCI.t(lesbian, dfreq = TRUE, mX = "[12,13,14]", h = "Darroch")
 # Example to illustrate warnings management in closed population functions.
 # Here is a capture-recapture data set one could encounter.
 crdata <- cbind(histpos.t(4), c(0,0,3,0,0,0,0,0,0,0,0,0,1,0,0,2))
 # This data set contains 4 capture occasions but only 6 captured units.
 # Fitting capture-recapture models on this data set is quite useless.
 # The population size should be very close to the sample size.
 # Such small frequencies in a capture-recapture data set should
 # lead to warnings when fitting a loglinear model on it.
 ex <- closedp.t(crdata, dfreq=TRUE)</pre>
 # Many models produce warnings of type 1 indicating that the model fit
 # is questionnable. The very large abundance estimation for some models
 # are another indicator of questionable model fits.
 # Details about the warnings are found in the glm.warn element of the output.
 ex$glm.warn
BBS2001
                        Species Richness Data from the North American Breeding Bird Survey
                        (BBS) in 2001
```

### **Description**

This data set contains species richness data from the North American Breeding Bird Survey (BBS) in 2001. The number of capture occasions t is 50.

8 BBS2001

#### Usage

BBS2001

#### **Format**

36 by 2 numeric matrix, with the following columns:

nbcap Numbers of captures

freq Observed frequencies for each number of captures

#### **Details**

This data set is presented in Dorazio and Royle (2003). It comes from the North American Breeding Bird Survey (BBS). This survey includes more than 4000 39.4 km survey routes throughout North America. Along each survey route an observer stops at 50 equidistant locations and records the species identity and number of all birds heard or seen within a 3-minute period.

The data in BBS2001 was collected along Route 123, in Maryland, in 2001. In this data set a capture occasion is in fact a location and the frequencies represent the number of species detected at i locations out of the 50 locations on that route. The frequencies for  $i = 37, \ldots, 50$  are null and do not appear in the data set.

#### Source

Dorazio, R. M. and Royle, A. J. (2003) Mixture models for estimating the size of a closed population when capture rates vary among individuals. *Biometrics*, **59**, 351–364

```
desc <- descriptive(BBS2001, dfreq = TRUE, dtype = "nbcap", t = 50)</pre>
plot(desc)
   # Note in this plot the convex shape typical of model Mh.
cp < -closedp.0(BBS2001, dfreq = TRUE, dtype = "nbcap", t = 50, t0 = 20)
ср
plot(cp)
   # The Gamma estimator has the smallest deviance and all
   # its residuals are small.
   # Let's calculate a profile confidence interval for the gamma
   # estimator:
closedpCI.0(BBS2001, dfreq = TRUE, dtype = "nbcap", t = 50, t0 = 20,
            m = "Mh", h = "Gamma", h.control = list(theta = 3.5))
   # One can also calculate a profile confidence interval for Chao's
   # lower bound:
closedpCI.0(BBS2001, dfreq = TRUE, dtype = "nbcap", t = 50, t0 = 20,
            m = "Mh", h = "Chao")
```

bunting 9

bunting

Lazuli Bunting Data

### **Description**

This data set contains frequencies of capture histories for 8 years of observation of lazuli buntings.

# Usage

bunting

# **Format**

255 by 9 numeric matrix, with the following columns:

p1, p2, p3, p4, p5, p6, p7, p8 Capture histories from eight periods

freq Observed frequencies for each capture history

### **Details**

The data come from an eight-year (1973 to 1980) study by Allen W. Stokes of lazuli buntings wintering in Logan, Utah. This data set is analyzed in Burnham and al. (1987) and in Cormack (1993).

Each row of this data set represents an observed capture history followed by its frequency.

### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Burnham, K.P., Anderson, D.R., White, G.C., Brownie, C. and Pollock, K.H. (1987) Design and analysis methods for fish survival experiments based on release-recapture. *American Fisheries Society Monographs 5*. Bethesda, Maryland.

Cormack, R. M. (1993) The flexibility of GLIM analyses of multiple recapture or resighting data. In J.D. Lebreton and P. North editors: *Marked Individuals in the Study of Bird Population*. Basel, Switzerland: Birkhauser Verlag, 39–49.

```
descriptive(bunting, dfreq = TRUE)
  # 1430 birds among the 1681 birds seen (85%) were caught only once.
  # This suggests the presence of transient birds at each capture occasion.

op.m1 <- openp(bunting, dfreq = TRUE)
op.m1$model.fit
plot(op.m1)
  # The residuals plot shows large residuals for the birds caught twice or
  # more while the residuals are small for birds caught once. The Jolly-Seber</pre>
```

10 cbird

```
# model does not fit well and the likely presence of transients might
 # cause that. Let's remove the birds caught only once from the analysis.
keep2 <- rowSums(histpos.t(8)) > 1
op.m2<- openp(bunting, dfreq = TRUE, keep = keep2)
op.m2$model.fit
 # The deviance drop of 94 for 6 degrees of freedom is highly significant.
 # The residual plot still shows Pearson residuals larger than 4. We redo
 # the analysis without the transient birds and without the large residuals.
keep3p <- residuals(op.m2$glm, type = "pearson") < 4</pre>
num3 <- ((1:255)[keep2])[keep3p]
keep3 <- rep(FALSE, 255)
keep3[num3] <- TRUE
op.m3 <- openp(bunting, dfreq = TRUE, keep = keep3)
cbind(op.m2$survivals, op.m3$survivals)
 # These changes have little impact on the survival estimates.
 # We now test the equality of the survival probabilities and estimate its
 # common value phi. Least squares estimates of phi and its standard error:
siginv <- solve(op.m2$cov[8:12, 8:12])</pre>
phi <- t(rep(1, 5)) %*% siginv %*% op.m2$survivals[2:6, 1] /</pre>
      (t(rep(1, 5)) %*% siginv %*% rep(1, 5))
se <- 1 / sqrt(t(rep(1, 5)) %*% siginv %*% rep(1, 5))
cbind(estimate = phi, stderr = se)
 # The chi-square goodness of fit statistic for a constant survival
 # and its pvalue are:
\label{eq:chisq4} chisq4 <- t(op.m2\$survivals[2:6, 1] - as.vector(phi)) \ \%*\% \ siginv \ \%*\%
          (op.m2$survivals[2:6, 1] - as.vector(phi))
cbind(chi2stat = chisq4, pvalue = 1 - pchisq(chisq4, df = 4))
 # The hypothesis of a constant survival is accepted.
```

cbird

Catbird Site Occupancy Data

### **Description**

This data set contains site occupancy data for catbirds. The number of capture occasions t is 11.

# Usage

cbird

#### **Format**

6 by 2 numeric matrix, with the following columns:

nbcap Numbers of captures

freq Observed frequencies for each number of captures

#### **Details**

This data set is presented in Royle (2006). It comes from an experiment in which 50 locations have been visited 11 times. The presence or absence of catbirds was noted at each visit. The experiment aims at estimating the number of locations (<=50) at which catbirds are present.

In the data set cbird, the frequencies represent the number of locations at which cbirdirbs have been detected i times, out of t=11 visits. The frequencies for  $i=7,\ldots,11$  are null and do not appear in the data set.

#### Source

Royle, A. J. (2006) Site occupancy models with heterogeneous detection probabilities. *Biometrics*, **62**, 97–102

#### **Examples**

```
desc <- descriptive(cbird, dfreq = TRUE, dtype = "nbcap", t = 11)
plot(desc)
    # The heterogeneity graph is mildly convex, mostly because of
    # 2 sites where catbirds have been seen six times.

closedp.0(cbird, dfreq = TRUE, dtype = "nbcap", t = 11)
    # The residuals are OK. The occupancy rate (N/50) estimate
    # varies between 40.6% for M0 and 49.4% for Mh Gamma.
    # One could also try fitting M0 removing the 2 unusual sites:
closedp.0(cbird, dfreq = TRUE, dtype = "nbcap", t = 11, t0 = 5)
    # M0 fits very well and the occupancy rate estimate is 42.6%.</pre>
```

closedp

Loglinear Models for Closed Population Capture-Recapture Experiments

### **Description**

The functions closedp.t and closedp.0 fit various loglinear models for closed populations in capture-recapture experiments. For back compatibility, closedp.t is also named closedp.

closedp.t fits more models than closedp.0 but for data set with more than 20 capture occasions, the function might fail. However, closedp.0 works with fairly large data sets (see **Details**).

# Usage

```
print(x, ...)
## S3 method for class 'closedp'
boxplot(x, main="Boxplots of Pearson Residuals", ...)
## S3 method for class 'closedp'
plot(x, main="Residual plots for some heterogeneity models", ...)
```

#### **Arguments**

X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
dtype	A characters string, either "hist" or "nbcap", to specify the type of data. "hist", the default, means that X contains complete observed capture histories. "nbcap" means that X contains numbers of captures (see Rcapture-package for details on data formats).
t	Requested only if dtype="nbcap". A numeric specifying the total number of capture occasions in the experiment. For closedp.0, the value t=Inf is accepted. It indicates that captures occur in continuous time (see Rcapture-package).
t0	A numeric. Models are fitted considering only the frequencies of units captured 1 to t0 times. By default, if t is not equal to Inf, t0=t. When t=Inf, the default value of t0 is the larger number of captures observed.
neg	If this option is set to TRUE, negative eta parameters in Chao's lower bound models are set to zero (see <b>Details</b> ).
•••	Further arguments to be passed to glm, print.default, boxplot.default or plot.default.
х	An object, produced by a closedp function, to print or to plot.
main	A main title for the plot.

# Details

closedp.t fits models M0, Mt, Mh Chao (LB), Mh Poisson2, Mh Darroch, Mh Gamma3.5, Mth Chao (LB), Mth Poisson2, Mth Darroch, Mth Gamma3.5, Mb and Mbh. closedp.0 fits only models M0, Mh Chao (LB), Mh Poisson2, Mh Darroch and Mh Gamma3.5. However, closedp.0 can be used with larger data sets than closedp.t. This is explained by the fact that closedp.t fits models using the frequencies of the observable capture histories (vector of size  $2^t-1$ ), whereas closedp.0 uses the numbers of units captured i times, for  $i=1,\ldots,t$  (vector of size t). See Rcapture-package for more details about the distinction between .t and .0 functions.

Multinomial profile confidence intervals for the abundance are constructed by closedpCI.t and closedpCI.0.

To calculate bias corrected abundance estimates, use the closedp.bc function.

CHAO'S LOWER BOUND MODEL

Chao's (or LB) models estimate a lower bound for the abundance, both with a time effect (Mth Chao) and without one (Mh Chao). The estimate obtained under Mh Chao is Chao's (1987) moment estimator. Rivest and Baillargeon (2007) exhibit a loglinear model underlying this estimator and provide a generalization to Mth. For these two models, a small deviance means that there is an heterogeneity in capture probabilities; it does not mean that the lower bound estimate is unbiased. To test whether a certain model for heterogeneity is adequate, one can conduct a likelihood ratio test by subtracting the deviance of Chao's model to the deviance of the heterogeneous model under study. If this heterogeneous model includes a time effect, it must be compared to model Mth Chao. If it does not include a time effect, it must be compared to model Mh Chao. Under the null hypothesis of equivalence between the two models, the difference of deviances follows a chisquare distribution with degrees of freedom equal to the difference between the models' degrees of freedom.

Chao's lower bound models contain t-2 parameters, called eta parameters, for the heterogeneity. These parameters should theoretically be greater or equal to zero (see Rivest and Baillargeon (2007)). When the argument neg is set to TRUE (the default), negative eta parameters are set to zero (to do so, columns are removed from the design matrix of the model). Degrees of freedom of Chao's model increase when eta parameters are set to zero.

#### OTHER MODELS FOR HETEROGENEITY

Other models for heterogeneity are defined as follows:

Model Column for heterogeneity in the design matrix

Poisson2  $2^k - 1$ Darroch  $k^2/2$ 

Gamma3.5  $-\log(3.5+k) + \log(3.5)$ 

where k is the number of captures. Poisson and Gamma models with alternative to the parameter defaults values 2 and 3.5 can be fitted with the closedpCI.t and closedpCI.0 functions.

Darroch's models for Mh and Mth are considered by Darroch et al. (1993) and Agresti (1994). Poisson and Gamma models are discussed in Rivest and Baillargeon (2007). Poisson models typically yield smaller corrections for heterogeneity than Darroch's model since the capture probabilities are bounded from below under these models. On the other hand, Gamma models can lead to very large estimators of abundance. We suggest considering this estimator only in experiments where very small capture probabilities are likely.

### PLOT METHODS AND FUNCTIONS

The boxplot.closedp function produces boxplots of the Pearson residuals of the fitted loglinear models that converged.

The plot.closed function produces scatterplots of the Pearson residuals in terms of  $f_i$  (number of units captured i times) for the heterogeneous models Mh Poisson2, Mh Darroch and Mh Gamma3.5 if they converged.

#### Value

n The number of captured units.

t The total number of capture occasions in the data matrix X. When captures occur in continuous time (input argument t=Inf), this output value is the larger

number of captures observed.

t0 For closedp.0 only: the value of the argument t0 used in the computations.

results A table containing, for every fitted model:

abundance: the estimated population size,

stderr: the standard error of the estimated population size,

deviance: the model's deviance, df: the number of degrees of freedom, AIC: the Akaike's information criterion, BIC: the bayesian information criterion,

infoFit: a numerical code giving information about error or warnings encountered when fitting the model (see Rcapture-package for details).

A vector, the asymptotic bias of the estimated population size for every fitted

model.

glm A list of the 'glm' objects obtained from fitting models.

glm.err A list of character string vectors. If the glm function generates an error when

fitting a model, a copy of the error message is stored in glm.err\$mname where mname is a short name to identify the model. A NULL list element means that no

error occured for the considered model.

glm.warn A list of character string vectors. If the glm function generates one or more warn-

ings when fitting a model, a copy of these warnings are stored in  $glm.warn\mbox{\$mname}$  where mname is a short name to identify the model. A NULL list element means

that glm did not produce any warnings for the considered model.

parameters Capture-recapture parameters estimates. It contains N, the estimated population

size, and p or  $p_1$  to  $p_t$  defined as follows for the different models:

M0: the capture probability at any capture occasion,Mt: the capture probabilities for each capture occasion,

**Mh models:** the average probability of capture,

**Mth models:** the average probabilities of capture for each occasion, **Mb and Mbh:** the probability of first capture at any capture occasion.

For models Mb and Mbh, it also contains c, the recapture probability at any

capture occasion.

neg.eta The position of the eta parameters set to zero in the loglinear parameter vector

of models MhC and MthC. NULL if no parameters are set to zero.

X A copy of the data given as input in the function call.

dfreq A copy of the dfreq argument given in the function call.

#### Note

This function uses the glm function of the stats package.

# Author(s)

bias

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#### References

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#### See Also

closedpCI.t, closedpCI.0, closedp.bc, closedp.Mtb, closedpMS.t, uifit.

```
# hare data set
hare.closedp <- closedp.t(hare)</pre>
hare.closedp
boxplot(hare.closedp)
# Third primary period of mvole data set
period3 <- mvole[, 11:15]</pre>
closedp.t(period3)
# BBS2001 data set
BBS.closedp <- closedp.0(BBS2001, dfreq = TRUE, dtype = "nbcap", t = 50, t0 = 20)
BBS.closedp
plot(BBS.closedp)
### Seber (1982) p.107
# When there is 2 capture occasions, the heterogeneity models cannot be fitted
X \leftarrow matrix(c(1,1,167,1,0,781,0,1,254), byrow = TRUE, ncol = 3)
closedp.t(X, dfreq = TRUE)
### Example of captures in continuous time
# Illegal immigrants data set
closedp.0(ill, dtype = "nbcap", dfreq = TRUE, t = Inf)
```

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 ${\tt closedp.bc}$ 

Bias Correction for Closed Population Loglinear Models

# Description

This function applies a bias correction to the abundance estimations obtained by closed population

# Usage

```
closedp.bc(X, dfreq=FALSE, dtype=c("hist","nbcap"), t=NULL, t0=t,
          m=c("M0","Mt","Mh","Mth","Mb","Mbh"), h=NULL, h.control=list(), ...)
## S3 method for class 'closedp.bc'
print(x, ...)
```

# Arg

rguments	
X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
dtype	A characters string, either "hist" or "nbcap", to specify the type of data. "hist", the default, means that X contains complete observed capture histories. "nbcap" means that X contains numbers of captures (see Rcapture-package for details on data formats). If m is "Mt", "Mth", "Mb" or "Mbh", dtype must be "hist".
t	Requested only if dtype="nbcap". A numeric specifying the total number of capture occasions in the experiment.
t0	A numeric used for model M0 or for an Mh model other than Chao's lower bound model: Models are fitted considering only the frequencies of units captured 1 to t0 times. By default t0=t.
m	A character string indicating the model to fit, either "M0"=M0 model, "Mt"=Mt model, "Mh"=Mh model, "Mth"=Mth model, "Mb"=Mb model, "Mbh"=Mbh model.
h	A character string ("LB", "Chao", "Poisson", "Darroch" or "Gamma") or a numerical R function specifying the form of the column(s) for heterogeneity in the design matrix.  "LB" and "Chao" represents Chao's lower bound model (the default),  "Poisson" represents the function $f(k) = theta^k - 1$ ,  "Darroch" represents the function $f(k) = k^2/2$ ,  and "Gamma" represents the function $f(k) = -\log(theta + k) + \log(theta)$ where $k$ is the number of captures and $theta$ is a parameter specified with the

argument theta.

If an R function is given, it must be the implementation of any convex mathematical function f(k) (it must have only one argument).

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h.control A list of elements to control the heterogeneous part of the model, if any.

For a Poisson or Gamma heterogeneous model:

theta The value of the parameter theta in  $f(k) = theta^k - 1$  for the Poisson model (the default value is 2) and in  $f(k) = -\log(theta + k) + \log(theta)$  for the Gamma model (the default value is 3.5).

For the Chao's lower bound Mth model:

neg If this option is set to TRUE (the default), negative eta parameters in Chao's lower bound models are set to zero.

Further arguments to be passed to glm or print.default.

x An object, produced by the closedp.bc function, to print.

#### **Details**

For the Mt model:

When t=2, closedp.bc returns the Petersen estimator with Chapman's (1951) bias correction and the bias corrected standard error estimator of Seber (1970) and Wittes (1972). For t>2, closedp.bc implements the bias correction of Rivest and Levesque (2001). The estimate for N and its variance are calculated by solving an estimating equation as proposed in Seber (1982), not by fitting a Poisson regression. This approach works for large values of t.

For other models:

The bias correction is done through frequency modifications in Poisson regression as described in Rivest and Levesque (2001). The variances calculated with the modified frequencies are less biased than the standard ones, but they can overestimate the mean squared errors, especially when the data is sparse.

This function works with fairly large data set, except if an "Mth" model is requested. In this case, only heterogeneity of the form "LB", "Chao", "Poisson" with theta=2 or "Darroch" is accepted.

### Value

n	The number of captured units
t	The total number of capture occasions in the data matrix X.
t0	For models M0 and Mh only: the value of the argument $t\theta$ used in the computations.
results	A table containing, for the fitted model:
	abundance: the estimated population size, stderr: the standard error of the estimated population size,
	infoFit: a numerical code giving information about error or warnings encountered when fitting the model (see Rcapture-package for details).
glm.warn	Only if the corrected population size estimation was obtained with glm: A vector of character strings. If the glm function generates one or more warnings when fitting the model, a copy of these warnings are stored in glm.warn. NULL if glm did not produce any warnings.
neg.eta	For Chao's lower bound model Mth only: the position of the eta parameters set to zero in the loglinear parameter vector, if any.

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#### Note

This function uses the glm function of the **stats** package, except for models Mt and Mh Chao's lower bound for which exact calculation is performed.

### Author(s)

Louis-Paul Rivest < Louis - Paul . Rivest@mat.ulaval.ca> and Sophie Baillargeon

#### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Chapman, D. G. (1951) Some properties of the hypergeometric distribution with applications to zoological sample censuses. *University of California Publications in Statistics*, **1**(7), 131-160.

Rivest, L.P. and Levesque, T. (2001) Improved loglinear model estimators of abundance in capture-recapture experiments. *Canadian Journal of Statistics*, **29**, 555-572.

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### See Also

closedp

closedp.custom 19

closedp.custom	Customization of a Loglinear Model for Closed Populations Capture-
	Recapture Experiments

# **Description**

As of version 1.2-0 of **Reapture**, these functions are deprecated, but kept for back compatibility. Please use closedpCI.t instead.

The closedp.mX function fits a loglinear model given a design matrix mX. The closedp.h function fits Mh or Mth models for which the form of the column for heterogeneity in the design matrix is determined by the user.

# Usage

```
closedp.mX(X, dfreq=FALSE, mX, mname="Customized model")
closedp.h(X, dfreq=FALSE, m="Mh", h="Poisson", a=2)
## S3 method for class 'closedp.custom'
print(x, ...)
## S3 method for class 'closedp.custom'
boxplot(x, ...)
```

# **Arguments**

X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
mX	The design matrix of the loglinear model. In this matrix, the order of the capture histories is as defined in the histpos.t function.
mname	A character string specifying the name of the customized model.
m	A character string indicating the model to fit, either "Mh"=Mh model or "Mth"=Mth model
h	The character string "Poisson" $(2^k - 1)$ or a numerical function taking only one argument specifying the form of the column for heterogeneity in the design matrix.
а	The value of the exponent's base for a Poisson model.
x	An object, produced by the closedp.mX or the closedp.h function, to print or to plot. $ \\$
	Further arguments passed to or from other methods.

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#### **Details**

An intercept is added to the model. Therefore, the mX matrix must not contain a column of ones.

The abundance estimation is calculated as the number of captured units plus the exponential of the intercept. Therefore, these functions are not suited for models with a behavioral effect.

In closedp.h, the argument h cannot take the value "Chao" or "Darroch" because these models are already fitted by the closedp function.

The boxplot.closedp.custom function produces a boxplot of the pearson residuals of the customized model.

#### Value

n The number of captured units

results A table containing the estimated population size and its standard error, the de-

viance, the number of degrees of freedom and the Akaike's information crite-

rion.

glm The 'glm' object obtained from fitting the model.

#### Note

These functions use the glm function of the **stats** package.

#### Author(s)

Louis-Paul Rivest <Louis-Paul.Rivest@mat.ulaval.ca> and Sophie Baillargeon

### References

Rivest, L.P. and Baillargeon, S. (2007) Applications and extensions of Chao's moment estimator for the size of a closed population. *Biometrics*, **63**(4), 999–1006.

#### See Also

```
closedp, closedp. Mtb
```

```
# HIV data set
mat <- histpos.t(4)
mX2 <- cbind(mat, mat[, 1] * mat[, 2])
closedp.mX(HIV, dfreq = TRUE, mX = mX2)

# Third primary period of mvole data set
period3 <- mvole[, 11:15]
psi <- function(x) { -log(3.5 + x) + log(3.5) }
closedp.h(period3, h = psi)</pre>
```

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closedp.Mtb	Closed Population Capture-Recapture Model Mtb	

#### **Description**

This function fits model Mtb for closed populations in capture-recapture experiments.

### Usage

```
closedp.Mtb(X, dfreq=FALSE, method = "BFGS", ...)
## S3 method for class 'closedp.Mtb'
print(x, ...)
```

### **Arguments**

X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
method	The method to be used by optim. The default is "BFGS".
	Further arguments to be passed to optim or print.default.
x	An object, produced by the closedp. Mtb function, to print.

### **Details**

The Mtb model is non-linear. It is fitted with the optim function instead of the glm function. Therefore, the abundance estimate can be unstable.

For the model to be identifiable, the parameters are constrained in the following way:  $logit(c_i) = logit(p_i) + b$  for i in  $2, \ldots, l$ .

### Value

n The number of captured units

t The total number of capture occasions in the data matrix X.

results A table containing, for the fitted model:
 abundance: the estimated population size,
 stderr: the standard error of the estimated population size,
 deviance: the model's deviance,
 df: the number of degrees of freedom,
 AIC: the Akaike's information criterion,
 BIC: the bayesian information criterion,
 infoFit: a numerical code giving information about error or warnings encountered when fitting the model (see Rcapture-package for details).

optim The output produced by optim from fitting the model.

optim.warn A vector of character strings. If the optim function generates one or more warn-

ings when fitting the model, a copy of these warnings are stored in optim.warn.

NULL if optim did not produce any warnings.

parMtb Capture-recapture parameters estimates for model Mtb: the abundance N,  $p_1$  to

 $p_t$ , the probabilities of first capture for each capture occasion, and  $c_2$  to  $c_t$ , the

recapture probabilities for each capture occasion.

#### Author(s)

Louis-Paul Rivest <Louis-Paul.Rivest@mat.ulaval.ca> and Sophie Baillargeon

#### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

#### See Also

```
closedp, closedpCI.t
```

### **Examples**

```
# hare data set
closedp.Mtb(hare)

## Example producing an unstable estimate
# Fourth primary period of mvole data set
period4 <- mvole[, 16:20]
closedp.Mtb(period4)</pre>
```

closedpCI

Customization of a Loglinear Model and Confidence Interval for Abundance Estimation in Closed Population Capture-Recapture Experiments

# Description

The closedpCI.t and closedpCI.0 functions fit a loglinear model specified by the user and compute a confidence interval for the abundance estimation. For a normal heterogeneous model, a log-transformed confidence interval (Chao 1987) is produced. For any other model, the multinomial profile likelihood confidence interval (Cormack 1992) is produced.

The model is identified with the argument m or mX. For heterogeneous models, the form of the heterogeneity is specified with the arguments h and h. control. If h is given with mX, heterogeneity is added in mX.

These functions extend closedp.t and closedp.0 as they broaden the range of models one can fit and they compute confidence intervals. Unlike the closedp functions, it fits only one model at a time.

# Usage

### **Arguments**

X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
dtype	A characters string, either "hist" or "nbcap", to specify the type of data. "hist", the default, means that X contains complete observed capture histories. "nbcap" means that X contains numbers of captures (see Rcapture-package for details on data formats).
t	Requested only if dtype="nbcap". A numeric specifying the total number of capture occasions in the experiment. For closedpCI.0, the value t=Inf is accepted. It indicates that captures occur in continuous time (see Rcapture-package).
t0	A numeric. Models are fitted considering only the frequencies of units captured 1 to t0 times. By default, if t is not equal to Inf, t0=t. When t=Inf, the default value of t0 is the larger number of captures observed.
m	A character string indicating the model to fit. For closedpCI.0 it can be either "M0"=M0 model or "Mh"=Mh model. For closedpCI.t it can also be "Mt"=Mt model or "Mth"=Mth model.
mX	The design matrix of the loglinear model. By default, the design matrix is built based on the m argument. If a mX argument is given, it must be a matrix (or an

object that can be coerced to a matrix by as.matrix). The order of the capture

histories in the mX matrix must be as defined in the histpos.t or histpos.0 function.

For the closedpCI.t function only, mX can also be an object of class "formula" or a hierarchical loglinear model name. The details of a formula specification are given under **Details** and the details of a hierarchical loglinear model name specification are given in the closedpMS.t documentation.

An intercept is always added to the model. Therefore, mX must not contain a column of ones if it is a matrix. Also, if the argument h is not NULL, one or more columns for heterogeneity are added to the design matrix.

A character string ("LB", "Chao", "Poisson", "Darroch", "Gamma" or "Normal") or a numerical R function specifying the form of the column(s) for heterogeneity in the design matrix.

"LB" and "Chao" represents Chao's lower bound model (the default),

"Poisson" represents the function  $f(k) = theta^k - 1$ ,

"Darroch" represents the function  $f(k) = k^2/2$ ,

and "Gamma" represents the function  $f(k) = -\log(theta+k) + \log(theta)$  where k is the number of captures and theta is a parameter specified with the h.control element theta.

"Normal" represents heterogeneity modeled with a normal mixing distribution, as presented in Rivest (2011).

If an R function is given, it must be the implementation of any convex mathematical function f(k) (it must have only one argument).

h.control

A list of elements to control the heterogeneous part of the model, if any. For a Poisson or Gamma heterogeneous model:

theta The value of the parameter theta in  $f(k) = theta^k - 1$  for the Poisson model (the default value is 2) and in  $f(k) = -\log(theta + k) + \log(theta)$  for the Gamma model (the default value is 3.5).

For a Chao's lower bound heterogeneous model:

neg If this option is set to TRUE (the default), negative eta parameters in Chao's lower bound models are set to zero.

For a Normal heterogeneous model:

initcoef Initial values for the loglinear coefficients given to optim. The default values are taken from Darroch's model.

initsig Initial value for the sigma parameter of the normal mixing distribution. The default is 0.2.

method The method to be used by optim. The default is "BFGS".

mname

A character string specifying the name of the customized model. By default, it is derived from the arguments specifying the model.

alpha

A confidence interval with confidence level 1-alpha is constructed. The value of alpha must be between 0 and 1; the default is 0.05.

fmaxSupCL

A numeric (by default 3). The upper end point of the interval to be searched by uniroot to find the upper bound of the multinomial profile likelihood confidence interval (Cormack 1992) is defined by fmaxSupCL $\times \hat{N}$ . In this product, fmaxSupCL is a factor multiplying  $\hat{N}$ , the population size estimated by

h

Poisson regression. If the upper bound obtained is equal the upper end point fmaxSupCL $\times \hat{N}$ , the element SupCL of the output value CI will begin with the symbol >. In that case, one could try to increase the value of fmaxSupCL to find the upper bound of the multinomial profile likelihood confidence interval instead of a minimum value for this upper bound.

.. Further arguments to be passed to glm, optim, print.default, plot.default

or boxplot.default.

x.closedpCI An object, produced by a closedpCI function, to produce a plot of the multino-

mial profile likelihood for N.

main A main title for the plot

x An object, produced by a closedpCI function, to print or to plot.

#### **Details**

The closedpCI.t function fits models using the frequencies of the observable capture histories (vector of size  $2^t-1$ ), whereas closedpCI.0 uses the number of units capture i times, for  $i=1,\ldots,t$  (vector of size t). Thus, closedpCI.0 can be used with data sets larger than those for closedpCI.t, but it cannot fit models with a temporal effect. See Rcapture-package for more details about the distinction between .t and .0 functions.

These functions do not work for closed population models featuring a behavioral effect, such as Mb and Mbh. The abundance estimation is calculated as the number of captured units plus the exponential of the Poisson regression intercept. However, models with a behavioral effect can by fitted with closedp.t (Mb and Mbh), closedp.Mtb and closedp.bc.

# CHAO'S LOWER BOUND MODELS

Chao's lower bound models estimate a lower bound for the abundance. Rivest (2011) presents a generalized loglinear model underlying this estimator. To test whether a certain model for heterogeneity is adequate, one can conduct a likelihood ratio test by subtracting the deviance of a Chao's lower bound model to the deviance of the heterogeneous model under study. The two models should have the same mX argument. Under the null hypothesis of equivalence between the two models, the difference of deviances follows a chi-square distribution with degrees of freedom equal to the difference between the models' degrees of freedom.

A Chao's lower bound model contains t-2 parameters, called eta parameters, for the heterogeneity. These parameters should theoretically be greater or equal to zero (see Rivest and Baillargeon (2007)). When the element neg of the argument h.control is set to TRUE (the default), negative eta parameters are set to zero (to do so, columns are removed from the design matrix of the model). Degrees of freedom of Chao's lower bound model increase when eta parameters are set to zero.

### ARGUMENT mX: FORMULA SPECIFICATION

For the closedpCI.t function, mX can be an object of class "formula". The only accepted variables in this formula are c1 to ct. The variable ci represents a capture indicator (1 for a capture, 0 otherwise) for the ith capture occasions. Also, the formula must not contain a response variable since it is only used to construct the design matrix of the model. For example, if t=3, the Mt model is fitted if mX =  $\sim$  . or mX =  $\sim$  c1 + c2 + c3. The symbol . in this formula is a shortcut for c1 + c2 + ... + ct. Formula mX arguments facilitate the addition of interactions between capture occasions in the model. For example, if t=3, the Mt model with an interaction between the first and the second

capture occasion is fitted if mX = ~ . + c1:c2. See formula for more details of allowed formulae.

#### PLOT METHODS AND FUNCTIONS

The boxplot.closedpCI function produces a boxplot of the Pearson residuals of the customized model.

The plot . closedpCI function traces the scatterplot of the Pearson residuals in terms of  $f_i$  (number of units captured i times) for the customized model.

The plotCI function produces a plot of the multinomial profile likelihood for N. The value of N maximizing the profile likelihood and the bounds of the confidence interval are identified.

#### Value

The number of captured units n

t The total number of capture occasions in the data matrix X. When captures occur in continuous time (input argument t=Inf), this output value is the larger

number of captures observed.

t0 For closedpCI.0 only: the value of the argument t0 used in the computations.

results A table containing, for the fitted model:

abundance: the estimated population size,

stderr: the standard error of the estimated population size,

deviance: the model's deviance,

df: the number of degrees of freedom,

AIC: the Akaike's information criterion,

BIC: the bayesian information criterion,

infoFit: a numerical code giving information about error or warnings encountered when fitting the model (see Rcapture-package for details).

bias

Not produced for normal heterogeneous models (h="Normal"): The asymptotic

bias of the estimated population size.

fit

The 'glm' object obtained from fitting the model except for normal heterogeneous models (h="Normal"). These models are not fitted with glm. For them, fit is a list with the following elements:

parameters: the matrix of parameters (loglinear coefficients + sigma parameter) estimates with their standard errors,

varcov: the estimated variance-covariance matrix of the estimated parameters,

y: the y vector used to fit the model,

fitted.values: the model fitted values,

initparam: the initial values for the parameters (loglinear coefficients + sigma parameter) used by optim,

optim: the output produced by optim.

fit.warn

A vector of character strings. If the glm or optim (for normal heterogeneous models) function generates one or more warnings when fitting the model, a copy of these warnings are stored in fit.warn. NULL if no warnings occured.

neg.eta For Chao's lower bound models only: the position of the eta parameters set to zero in the loglinear parameter vector, if any. CI Not produced for normal heterogeneous models (h="Normal"): A table containing the abundance estimation and its multinomial profile likelihood confidence interval. The last column of the table, named infoCI, contains a numerical code giving information about error or warnings encountered when calculating the confidence interval. Here is a description of the meaning of this numerical code: **0** no error or warning occured; -1 an error occured while calculating the multinomial abundance estimation; 4 a warning occured while calculating the multinomial abundance estimation; 5 a warning occured while calculating the lower bound of the multinomial profile likelihood confidence interval; 6 a warning occurred while calculating the upper bound of the multinomial profile likelihood confidence interval. CI.err Not produced for normal heterogeneous models (h="Normal"): If an error occured while calculating the multinomial abundance, a copy of the error message is stored in CI.err. NULL if no error occured. CI.warn Not produced for normal heterogeneous models (h="Normal"): If one or more warnings occur while calculating the multinomial abundance estimation or the profile likelihood confidence interval, a copy of these warnings are stored in CI. warn. NULL if no warnings occured. alpha 1-the confidence level of the interval. N.CI Not produced for normal heterogeneous models (h="Normal"): The x-coordinates for plot.closedpCI.t. Not produced for normal heterogeneous models (h="Normal"): The y-coordinates

#### Note

loglik.CI

For normal heterogeneous models, the closedpCI functions use optim from the **stats** package. Otherwise, models are fitted with glm and the code to compute the multinomial profile likelihood confidence interval calls the functions glm, optimize and uniroot, all from the stats package.

#### Author(s)

Louis-Paul Rivest < Louis - Paul . Rivest@mat.ulaval.ca> and Sophie Baillargeon

for plot.closedpCI.t.

#### References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. Journal of Statistical Software, 19(5), doi:10.18637/jss.v019.i05.

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Rivest, L.P. and Baillargeon, S. (2007) Applications and extensions of Chao's moment estimator for the size of a closed population. *Biometrics*, **63**(4), 999–1006.

#### See Also

```
closedp, closedp. Mtb
```

```
# hare data set
CI <- closedpCI.t(hare, m = "Mth", h = "Poisson", h.control = list(theta = 2))
plotCI(CI)
# HIV data set
mat <- histpos.t(4)</pre>
mX2 <- cbind(mat, mat[, 1] * mat[ ,2])</pre>
closedpCI.t(HIV, dfreq = TRUE, mX = mX2, mname = "Mt interaction 1,2")
# which can be obtained more conveniently with
closedpCI.t(HIV, dfreq = TRUE, mX = ~ . + c1:c2, mname = "Mt interaction 1,2")
# BBS2001 data set
CI0 <- closedpCI.0(BBS2001, dfreq = TRUE, dtype = "nbcap", t = 50, t0 = 20,
                   m = "Mh", h = "Gamma", h.control = list(theta = 3.5))
CI0
plot(CI0)
plotCI(CI0)
### As an alternative to a gamma model, one can fit a negative Poisson model.
### It is appropriate in experiments where very small capture probabilities
### are likely. It can lead to very large estimators of abundance.
# Third primary period of mvole data set
period3 <- mvole[, 11:15]</pre>
psi \leftarrow function(x) { 0.5^x - 1 }
closedpCI.t(period3, m = "Mh", h = psi)
### Example of normal heterogeneous models
### diabetes data of Bruno et al. (1994)
histpos <- histpos.t(4)
diabetes <- cbind(histpos, c(58,157,18,104,46,650,12,709,14,20,7,74,8,182,10))
# chosen interaction set I in Rivest (2011)
closedpCI.t(X = diabetes, dfreq = TRUE, mX = ~ . + c1:c3 + c2:c4 + c3:c4,
            h = "Normal", mname = "Mth normal with I")
### Example of captures in continuous time
# Illegal immigrants data set
closedpCI.0(ill, dtype = "nbcap", dfreq = TRUE, t = Inf, m = "Mh", h = "LB")
```

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closedpMS	Hierarchical	Loglinear	Model	Selection	in	Closed	Population
	Capture-Recap	ture Experii	nents				

### **Description**

The closedpMS.t function fits every possible hierarchical loglinear models for a given closed population capture-recapture data set, under the constraints set by the given maxorder and forced arguments. Parameters for heterogeneity in capture probabilites among units can be added to the models.

The getAllModels function lists every possible hierarchical loglinear models for a certain number of capture occasions t, under the constraints set by the given maxorder and forced arguments.

### Usage

# Arguments

dfreq

h

X The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).

A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.

A character string ("LB", "Chao", "Poisson", "Darroch", "Gamma" or "Normal") or a numerical R function specifying the form of the column(s) for heterogeneity in the design matrix.

"LB" and "Chao" represents Chao's lower bound model (the default),

"Poisson" represents the function  $f(k) = theta^k - 1$ ,

"Darroch" represents the function  $f(k) = k^2/2$ ,

and "Gamma" represents the function  $f(k) = -\log(theta+k) + \log(theta)$  where k is the number of captures and theta is a parameter specified with the h.control element theta.

"Normal" represents heterogeneity modeled with a normal mixing distribution, as presented in Rivest (2011).

If an R function is given, it must be the implementation of any convex mathematical function f(k) (it must have only one argument).

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h.control A list of elements to control the heterogeneous part of the model, if any. For a Poisson or Gamma heterogeneous model:

theta The value of the parameter theta in  $f(k) = theta^k - 1$  for the Poisson model (the default value is 2) and in  $f(k) = -\log(theta + k) + \log(theta)$  for the Gamma model (the default value is 3.5).

For a Chao's lower bound heterogeneous model:

neg If this option is set to TRUE (the default), negative eta parameters in Chao's lower bound models are set to zero.

For a Normal heterogeneous model:

initing Initial value for the sigma parameter of the normal mixing distribution. The default is 0.2.

method The method to be used by optim. The default is "BFGS".

maxorder A numeric specifying the higher order accepted for the terms in the models. It

can take a value between 1 and t - 1 (the default).

forced A vector of the terms forced in the model (by default every first order terms).

NULL if no terms are forced in the model.

stopiflong A logical indicating whether the function execution should be stopped when

the number of possibles models is larger than 10 000, that is when the function

might be long to run (defaut TRUE).

... Further arguments to be passed to glm, optim or print.default.

x An object, produced by the closedpMS. t function, to print or to plot.

main A main title for the plot.

omitOutliers A logical. If TRUE (the default), models with an outlier abundance or BIC value

are removed from the plot. A value is considered an outlier if it is smaller than the first quartile minus 1.5 times the interquartile range, or larger than the third

quartile plus 1.5 times the interquartile range.

t A numeric specifying the number of capture occasions in the experiments. It is

deduced from the data set in the closedpMS.t function. It must be an integer

between 1 and 9 inclusively.

#### **Details**

# HIERARCHICAL LOGLINEAR MODEL NAME SYNTAX

First, a model's term is written using numbers between 1 and 9 to represent the capture occasions it includes (ex.: 134 represents the three-way interaction c1:c3:c4). This syntax limits the maximal number of capture occasion to 9. This is not a problem since from 6 capture occasions upwards, the number of hierarchical models becomes very large and difficult to manage.

A hierarchical model name is a list of the model's terms at the top of the hierarchies in the model. These terms are separated by commas, without spaces. They are surronded by brackets. For example, "[123,34,5]" is the name of the model

```
\sim 1 + c1 + c2 + c3 + c4 + c5 + c1:c2 + c1:c3 + c2:c3 + c3:c4 + c1:c2:c3.
```

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#### Value

getAllModels returns a caracter vector with the models names.

closedpMS. t returns a list with the following elements:

n The number of captured units

t The total number of capture occasions in the data matrix X. When captures oc-

cur in continuous time (input argument t=Inf), this output value is the larger

number of captures observed.

results A table containing, for every fitted model:

abundance the estimated population size,

stderr the standard error of the estimated population size,

deviance the model's deviance, df the number of degrees of freedom, AIC the Akaike's information criterion, BIC the bayesian information criterion,

infoFit a numerical code giving information about error or warnings encoun-

tered when fitting the model (see Rcapture-package for details).

bias A vector, the asymptotic bias of the estimated population size for every fitted

model.

fit.err A list of character string vectors. If an error occurs while fitting a model (with

 ${\tt glm}$  or  ${\tt optim}$ ), a copy of the error message is stored in fit.err\$mname where mname is the name of the hierarchical loglinear model. A NULL list element

means that no error occured for the considered model.

fit.warn A list of character string vectors. If warnings are generated while fitting a model

(with glm or optim), a copy of these warnings are stored in fit.warn\$mname where mname is a the name of the hierarchical model. A NULL list element means

that no warnings were generated for the considered model.

neg.eta For Chao's lower bound models only: the position of the eta parameters set to

zero in the loglinear parameter vector, if any.

#### Note

For normal heterogeneous models, closedpMS.t uses optim from the **stats** package. Otherwise, models are fitted with glm, also from the **stats** package.

### Author(s)

Louis-Paul Rivest <Louis-Paul.Rivest@mat.ulaval.ca> and Sophie Baillargeon

### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Chao, A. (1987) Estimating the population size for capture-recapture data with unequal catchability. *Biometrics*, **43**(4), 783–791.

32 descriptive

Cormack, R. M. (1992) Interval estimation for mark-recapture studies of closed populations. *Biometrics*, **48**, 567–576.

Rivest, L.P. (2011) A lower bound model for multiple record systems estimation with heterogeneous catchability. *The International Journal of Biostatistics*, **7**(1), Article 23.

Rivest, L.P. and Baillargeon, S. (2007) Applications and extensions of Chao's moment estimator for the size of a closed population. *Biometrics*, **63**(4), 999–1006.

#### See Also

```
closedp, closedp. Mtb
```

### **Examples**

```
# The lesbian data set contains 4 capture occasions.
# By default, closedpMB.t fits the 113 following models:
getAllModels(4)
closedpMS.t(lesbian, dfreq = TRUE)
# We could reduce the number of models by omitting
# those with triple interactions.
closedpMS.t(lesbian, dfreq = TRUE, maxorder = 2)
# Models with heterogeneity fits better.
Darr <- closedpMS.t(lesbian, dfreq = TRUE, h = "Darroch")</pre>
Darr
# The plot method allows the visualization of the results
# from models fitted by closedpMS.t().
plot(Darr)
# According to the BIC, the best heterogeneous Darroch model
# for this data set contains the double interactions 12, 13, 14.
# Here is the profile likelihood confidence interval for the
# abundance estimation from this model.
closedpCI.t(lesbian, dfreq = TRUE, mX = "[12,13,14]", h = "Darroch")
```

descriptive

Descriptive Statistics

# Description

This function produces descriptive statistics for capture-recapture data.

descriptive 33

# Usage

```
descriptive(X, dfreq=FALSE, dtype=c("hist","nbcap"), t=NULL)
## S3 method for class 'descriptive'
print(x, ...)
## S3 method for class 'descriptive'
plot(x, main="Exploratory Heterogeneity Graph", ...)
```

# **Arguments**

X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
dtype	A characters string, either "hist" or "nbcap", to specify the type of data. "hist", the default, means that X contains complete observed capture histories. "nbcap" means that X contains numbers of captures (see Rcapture-package for details on data formats).
t	Requested only if dtype="nbcap". A numeric specifying the total number of capture occasions in the experiment. The value t=Inf is accepted. It indicates that captures occur in continuous time. (see Rcapture-package).
х	An object, produced by the descriptive function, to print or to plot.
main	A main title for the plot
	Further arguments to be passed to methods (see print.default and plot.default).

### **Details**

The plot.descriptive function produces an exploratory heterogeneity graph. In the absence of heterogeneity, the relation(s) presented in the graph should be almost linear. Convex functions indicate heterogeneity (Baillargeon and Rivest (2007)).

# Value

n	The total number of captured units.
base.freq	A table of basic descriptive statistics. For $i=1,\ldots,t$ : fi: the number of units captured $i$ times ui: the number of units captured for the first time on occasion $i$ vi: the number of units captured for the last time on occasion $i$ ni: the number of units captured on occasion $i$ If dtype="nbcap", only the number of units captured $i$ times, fi, can be computed.
m.array	Only if dtype="hist": A $t$ by $t$ matrix containing recapture statistics for units released on occasion $i$ , for $i=1,\ldots,t$ : ni: the number of units released on occasion $i$ ; c2: the number of units released on occasion $i$ and recaptured for the first time

34 descriptive

on occasion 2;

. . .

ct: the number of units released on occasion i and recaptured for the first time on occasion t:

not recapt: the number of units released on occasion i and never recaptured again.

The m.array matrix is used in Mark (see White and Burnham 1999) and MSurge (see Choquet, Reboulet, Pradel, Gimenez, and Lebreton 2004) to fit open population models to the data.

call The function call (object of class "call").

### Author(s)

Louis-Paul Rivest <Louis-Paul.Rivest@mat.ulaval.ca> and Sophie Baillargeon

#### References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Choquet, R., Reboulet, A.M., Pradel, R., Gimenez, O. and Lebreton, J.D. (2004). M-Surge: New Software Specifically Designed for Multistate Capture-Recapture Models. *Animal Biodiversity and Conservation*, **27.1**, 207–215.

Hoaglin, D. C. (1980) A Poissonness Plot, The American Statistician, 34, 146-149

Lindsay, B. G. (1986) Exponential family mixture models (with least-squares estimators). *Annals of Statistics*, **14**, 124–137.

Rivest, L.P. (2008) Why a time effect often has a limited impact on capture-recapture estimates in closed populations. *Canadian Journal of Statistics*, **36**(1), 75–84.

White, G. and Burnham, K.P. (1999) Program Mark: Survival Estimation from Populations of Marked Animals. *Bird Study*, **46** (Supplement), 120–138. The software can be downloaded here: http://www.phidot.org/software/mark/.

```
# hare data set
hare.desc <- descriptive(hare)
hare.desc
plot(hare.desc)

# cbird data set
cbird.desc1 <- descriptive(cbird, dfreq = TRUE, dtype = "nbcap", t = 11)
plot(cbird.desc1)
# To illustrate the option t = Inf.
cbird.desc2 <- descriptive(cbird, dfreq = TRUE, dtype = "nbcap", t = Inf)
plot(cbird.desc2)
# The y coordinate has changed.</pre>
```

duck 35

duck

Eider Duck Data

### **Description**

This data set contains capture-recapture data for eider ducks.

### Usage

duck

#### **Format**

```
63 by 7 numeric matrix, with the following columns:
```

```
p1, p2, p3, p4, p5, p6 Capture histories from six periods
```

freq Observed frequencies for each capture history

#### **Details**

The data points are extracted from a 25-year study by Coulson (1984). The capture periods are six consecutive years: years 19-24. This data set is analyzed in Cormack (1989).

Each row of this data set represents an observed capture history followed by its frequency.

### Source

Coulson, J. C. (1984) The population dynamics of the Eider Duck *Somateria mollissima* and evidence of extensive non breeding by adults ducks. *Ibis*, **126**, 525–543.

### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Cormack, R. M. (1989) Loglinear models for capture-recapture. *Biometrics*, 45, 395–413.

```
op.m1 <- openp(duck, dfreq = TRUE)
op.m1$model.fit
    # The pvalue of the goodness of fit test based on the deviance is
1 - pchisq(op.m1$model.fit[1, 1], df = 49)
plot(op.m1)
    # The residual plot shows a large residual for the 13 individuals
    # captured all the times. We redo the analysis without them.

keep2 <- rowSums(histpos.t(6)) != 6
op.m2 <- openp(duck, dfreq = TRUE, keep = keep2)
op.m2$model.fit</pre>
```

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```
1 - pchisq(op.m2$model.fit[1, 1], df = 48)
 # The fit is still not satisfactory.
plot(op.m2)
 # The residual plot has the convex shape characteristic of
 # heterogeneity in the capture probabilities. We also remove the
 # individuals caught at 5 periods out of 6.
keep3 < - rowSums(histpos.t(6)) < 5
op.m3 <- openp(duck, dfreq = TRUE, keep = keep3)
op.m3$model.fit
1 - pchisq(op.m3\$model.fit[1, 1], df = 42)
 # The fit is better but there is still heterogeneity in the data.
 # To investigate whether the capture probabilities are homogeneous,
 # one can fit a model with equal capture probabilities.
op.m4 <- openp(duck, dfreq = TRUE, m = "ep", keep = keep3)
op.m4$model.fit
 # It gives a much larger deviance; this model is not considered anymore.
 # We now investigate models for the growth rate N[i+1]/N[i] of this
 # population using the multivariate normal distribution for the
 # abundance estimates. The growth rates and their standard errors are
growth <- op.m3$N[3:5]/op.m3$N[2:4]
partial <- matrix(c(-op.m3$N[3]/op.m3$N[2]^2, 1/op.m3$N[2], 0, 0,
                   0, -op.m3$N[4]/op.m3$N[3]^2, 1/op.m3$N[3], 0,
               0, 0, -op.m3$N[5]/op.m3$N[4]^2, 1/op.m3$N[4]), 3, 4, byrow = TRUE)
sig <- partial %*% op.m3$cov[9:12, 9:12] %*% t(partial)</pre>
cbind(estimate = growth, stderr = sqrt(diag(sig)))
 # An estimate for the common growth rate is
siginv <- solve(sig)</pre>
growth.e <- t(rep(1, 3)) %*% siginv %*% growth/(t(rep(1, 3)) %*% siginv %*% rep(1, 3))
se <- 1/sqrt(t(rep(1, 3)) %*% siginv %*% rep(1, 3))
cbind(estimate = growth.e, stderr = se)
 # A chi-square statistic for testing the equality of the growth rates
  # and its pvalue
c(chi2stat = chisq2, pvalue = 1 - pchisq(chisq2, df = 2))
 # The hypothesis of a common growth rate is rejected
```

hare

Snowshoe Hare Data

### **Description**

This data set contains capture-recapture data for snowshoe hares.

# Usage

hare

histpos 37

### **Format**

68 by 6 numeric matrix, with the following columns:

c1, c2, c3, c4, c5, c6 Capture histories from the six capture occasions

#### **Details**

This data set is analyzed in Cormack (1989) and Agresti (1994).

Each row of this data set represents the capture history of one animal.

### References

Agresti, A. (1994) Simple capture-recapture models permitting unequal catchability and variable sampling effort. *Biometrics*, **50**, 494–500.

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Cormack, R. M. (1989) Loglinear models for capture-recapture. *Biometrics*, **45**, 395–413.

# **Examples**

```
desc <- descriptive(hare)
plot(desc)
    # The fi plot shows that the two animals caught on all occasions create
    # some heterogeneity in the capture probabilities.

closedp(hare)
    # The best fitting model Mth Poisson2(N = 81.1, s.e. = 5.7) has an AIC of 146.
closedpCI.t(hare, m = "Mth", h = "Poisson", h.control = list(theta = 2))

# One can compare the fit of this model with that obtained by removing the
    # 2 hares caught 6 times. This can be done by adding a column to the design
    # matrix for Mt taking the value 1 for the capture history (1,1,1,1,1).
col <- rep(0, 2^6-1)
mat <- histpos.t(6)
col[rowSums(mat) == 6] <- 1
closedpCI.t(hare, mX = cbind(mat, col), mname = "Mt without 111111")
    # This gives N = 76.8 (s.e. = 3.9) with an AIC of 146.</pre>
```

histpos

Possible Capture Histories

#### **Description**

 $\label{limits} \mbox{histpos.t builds the matrix of observable capture histories in terms of captures and misses for a capture-recapture experiment with t capture occasions.}$ 

histpos.0 builds the matrix of observable capture histories in terms of number of captures for each primary period of a robust design with vt capture occasions. For closed populations, vt=t and histpos.0 simply returns t:1.

38 histpos

# Usage

```
histpos.t(t)
histpos.0(vt)
```

# **Arguments**

t The number of capture occasions.

vt A vector containing the numbers of capture occasions for each primary sampling period of a robust design. The length of this vector equals the number of primary

sampling periods (noted I).

# Value

histpos.t gives a  $2^t - 1$  by t matrix with rows representing capture histories. This matrix contains only zeros and ones.

histpos.0 gives a  $(t_1+1)\times(t_2+1)\times\ldots\times(t_I+1)-1$  by I matrix with rows representing possible capture histories in terms of number of captures. This matrix elements are integers between 0 and  $t_i$  inclusively.

### Note

The histpos.t function is called by descriptive, closedp.bc, closedp.Mtb, openp, robustd.t.

The histpos.0 function is called by robustd.0.

# Author(s)

Louis-Paul Rivest <Louis-Paul.Rivest@mat.ulaval.ca> and Sophie Baillargeon

### References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

### See Also

```
periodhist, descriptive
```

```
histpos.t(5)
histpos.0(5)
histpos.0(rep(5, 3))
```

HIV 39

HIV

Epidemiological capture-recapture Data on HIV

# **Description**

Epidemiological capture-recapture data on HIV from four reporting centers in Rome, Italy.

# Usage

HIV

#### **Format**

```
15 by 5 numeric matrix, with the following columns:
c1, c2, c3, c4 Capture histories from the four capture occasions
freq Observed frequencies for each capture history
```

### **Details**

The capture histories were obtained by linking the records of the four reporting centers. Each row of this data set represents an observed capture history followed by its frequency.

### Source

Abeni, D.A., Brancato, G. and Perucci, C. A. (1994) Capture-recapture to estimate the size of the population with human immunodeficiency virus type 1 infection. *Epidemiology*, **5**, 410–414.

# References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

40 ill

```
# Eliminating the non significant interactions stepwise shows that only
# the [1,2] interaction is important.
closedpCI.t(HIV, dfreq = TRUE, mX = ~ . + c1:c2, mname = "Mt interaction 1,2")
```

ill

Illegal immigrants in the Netherlands

# **Description**

This data set contains the frequency  $f_i$  that an illegal immigrant who is not effectively expelled is apprehended exactly i times.

# Usage

i11

#### **Format**

6 by 2 numeric matrix, with the following columns:

nbcap Numbers of captures, i.e. number of times an illegal immigrant is apprehended by the police freq Observed frequencies for each number of captures

### **Details**

Bohning and Schon (2005) presented this data set as follows:

The illegal immigrant data are from van der Heijden et al. (2003) and refer to count data on illegal immigrants in four large cities in the Netherlands who could not be effectively expelled from the country. Illegal immigrants who are apprehended by the police often cannot be effectively expelled because either they refuse to disclose their nationality or their home country does not cooperate in receiving them back. In such cases they will be asked by the police to leave the country, but it is unlikely that they will abide by this request. The data were collected by the police and date back to the year 1995.

# Source

van der Heijden, P.G.M., Cruyff, M. and van Houwelingen, H.C. (2003) Estimating the size of a criminal population from police records using the truncated Poisson regression model. *Statistica Neerlandica*, **57**(3), 289-304.

# References

Bohning, D. and Schon, D. (2005) Nonparametric Maximum Likelihood Estimation of Population Size Based on the Counting Distribution. *Journal of the Royal Statistical Society: Series C (Applied Statistics)*, **54**(4), 721-737.

lesbian 41

### **Examples**

```
sdesc <- descriptive(ill, dtype = "nbcap", dfreq = TRUE, t = Inf)
plot(sdesc)
    # A mixture model looks appropriate

closedp.0(ill, dtype = "nbcap", dfreq = TRUE, t = Inf)

# We can try to fit a normal mixture model:
closedpCI.0(ill, dtype = "nbcap", dfreq = TRUE, t = Inf, m = "Mh", h = "Normal")
    # We get an estimate similar to the Mh Gamma3.5 estimate.

# Estimates are highly variable and it seems difficult to come up with a
    # definitive answer. The lower bound estimate is useful in this context.
closedpCI.0(ill, dtype = "nbcap", dfreq = TRUE, t = Inf, m = "Mh", h = "LB")
    # Considering the lower limit of a 95% confidence estimate for the lower bound,
    # there should be at least 8 000 illegal immigrants in the Netherlands.
    # Less than 25% have been caught.</pre>
```

lesbian

Epidemiological capture-recapture Data on the lesbian population

# Description

Epidemiological capture-recapture data on the lesbian population from four organisations that serve the lesbian and gay population of Allegheny County, Pennsylvania, United States and maintain large mailing lists.

### Usage

lesbian

#### **Format**

15 by 5 numeric matrix, with the following columns:

A, B, C, D Capture histories from the four organisations mailling lists freq Observed frequencies for each capture history

### **Details**

The capture histories were obtained by matching the names on the four mailling lists.

Each row of this data set represents an observed capture history followed by its frequency.

### Source

Aaron, D.J., Chang, Y.-F., Markovic, N., LaPorte, R. E. (2003) Estimating the lesbian population: a capture-recapture approach. *Journal of Epidemiology and Community Health*, **57**(3), 207–209.

42 mvole

# **Examples**

```
closedp(lesbian, dfreq = TRUE)

# According to the BIC, the best model is Mth Darroch.
# Let's see if adding interactions between capture
# histories to the model could improve the model's fit.

closedpMS.t(lesbian, dfreq = TRUE, h = "Darroch")

# According to the BIC, the best heterogeneous Darroch model
# contains the double interactions 12, 13, 14.
```

mvole

Robust Design Data for Adult Male Meadow Voles

# **Description**

This data set contains robust design capture history data for adult male meadow voles.

# Usage

mvole

# **Format**

171 by 30 numeric matrix, with the following columns:

c11, c12, c13, c14, c15 Capture histories from the 5 capture occasions within primary period 1 c21, c22, c23, c24, c25 Capture histories from the 5 capture occasions within primary period 2 c31, c32, c33, c34, c35 Capture histories from the 5 capture occasions within primary period 3 c41, c42, c43, c44, c45 Capture histories from the 5 capture occasions within primary period 4 c51, c52, c53, c54, c55 Capture histories from the 5 capture occasions within primary period 5 c61, c62, c63, c64, c65 Capture histories from the 5 capture occasions within primary period 6

### Details

The data set is extracted from Table 19.1 of Williams, Nichols and Conroy (2002). The capture occasions represent five consecutive days of trapping each month from June to December 1981 at Patuxent Wildlife Research Center, Laurel, Maryland.

Each row of this data set represents the capture history of one animal.

### Note

In this data set, ten animals are in fact not released after capture. These trap deaths are not identified.

mvole 43

#### **Source**

Williams, B.K., Nichols, J.D., and Conroy, M.J. (2002) *Analysis and Management of Animal Populations*, San Diego: Academic Press.

#### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

```
# This example deals only with the first four primary periods of the data set.
mvole4 <- mvole[, 1:20]</pre>
 # First, a between primary period Jolly-Seber analysis is obtained.
mvole4.pp <- periodhist(mvole4, vt = rep(5,4))</pre>
op.m1 <- openp(mvole4.pp, dfreq = TRUE)
plot(op.m1)
 # There is one large residual, removing the corresponding capture history
 # from the analysis does not change the results. The model fits well.
keep2 <- residuals(op.m1$glm, type = "pearson") < 4</pre>
op.m2 <- openp(mvole4.pp, dfreg = TRUE, keep = keep2)
op.m2$model.fit
 # To find a suitable model within each primary period, the function closedp.t
 # can be used repeatedly. Heterogeneity is detected in all periods except
 # the second one where the data collection was perturbed (the last capture
 # occasion doesn't have any new capture and is taken out of the analysis).
 # In a robust design, we use Mh models for all primary periods bearing in
 # mind the questionable fit in the second one. Since there is no time effect
 # within primary periods, we use the function robustd.0 to fit the model.
 ### The following command might take a few minutes to run.
rd.m1 <- robustd.0(mvole4[, -10], vt = c(5, 4, 5, 5), vm = "Mh", vh = "Chao")
rd.m1$model.fit
rd.m1$emig.fit
 # The test for temporary immigration is not significant meaning that capture
 # probabilities estimated with the Jolly-Seber model are not different from
 # those estimated with the individual closed population models. The
 # differences, on the logit scale, of the Jolly-Seber minus the closed
 # population models capture probabilities are
rd.m1$emig.param
 # Even in period 2, where the closed population model does not fit well, the
 # difference on the logit scale is non significant (estimate=.56, s.e.=1.13).
 # The following command allows to fit a robust design that does not specify
 # any model for the second period.
  ### The following command might take a few minutes to run.
rd.m3 \leftarrow robustd.0(mvole4[, -10], vt = c(5, 4, 5, 5),
                   vm = c("Mh", "none", "Mh", "Mh"), vh = "Chao")
 # With Darroch's model, the closed population estimates of the capture
```

44 openp

openp

Loglinear Models for Open Population Capture-Recapture Experiments

# Description

This function computes various demographic parameters using a loglinear model for open populations in capture-recapture experiments.

# Usage

```
openp(X, dfreq=FALSE, m=c("up","ep"), neg=TRUE, keep=rep(TRUE,2^I-1))
## S3 method for class 'openp'
print(x, ...)
## S3 method for class 'openp'
plot(x, main="Scatterplot of Pearson Residuals", ...)
```

### Arguments

Χ

The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).

dfreq

A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.

 ${\sf m}$ 

This argument is a character string taking the value "up" (up = unconstrained probabilities) or "ep" (ep = equal probabilities). If m is set to "up" (the default), no constraint is set on the loglinear parameters. Therefore some loglinear and demographic parameters are not estimable. On the other hand, when m takes the value "ep", the capture probabilities are set to a common value; this enables the estimation of all the parameters.

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keep	This option is useful to fit the model on a subset of the possible capture histories. keep is a logical vector of length $2^I-1$ taking the value TRUE for a history kept and FALSE for a history put aside. In this vector, the order of the capture histories is as defined in the histpos.t function. By default, every capture history is kept.
neg	If this option is set to TRUE, relevant negative gamma parameters are set to zero. This insures that the estimated survival probabilities belong to [0, 1] and that the births are positive.
х	An object, produced by the openp function, to print or to plot.
main	A main title for the plot
	Further arguments to be passed to methods (see print, default and plot, default).

# **Details**

The function openp generates statistics to test the presence of a trap effect.

The plot.openp function produces a scatterplot of the Pearson residuals of the model versus the frequencies of capture.

If the data matrix X was obtained through the periodhist function, the dfreq argument must be set to TRUE.

Standard errors are calculated by linearization.

# Value

n	The number of captured units
model.fit	A table containing the deviance, degrees of freedom and AIC of the fitted model.
trap.fit	A table containing, for the models with an added trap effect, the deviance, degrees of freedom and AIC.
trap.param	The estimated trap effect parameters and their standard errors. For m="up", the $I-3$ first rows of trap.param are estimations of the differences $logit$ (capture probability after a capture)- $logit$ (capture probability after a miss) for periods 3 to $I-1$ . The last row gives a pooled estimate of these differences calculated under the assumption that they are homogeneous.
capture.prob	The estimated capture probabilities per period and their standard errors.
survivals	The estimated survival probabilities between periods and their standard errors.
N	The estimated population sizes per period and their standard errors.
birth	The estimated number of new arrivals in the population between periods and their standard errors.
Ntot	The estimated total number of units who ever inhabited the survey area and its standard error.
glm	The 'glm' object obtained from fitting the loglinear model
loglin.param	The loglinear model parameters estimations and their standard errors, calculated by the glm function.
u.vector	The Ui statistics, useful for the survival probabilities calculation, and their standard errors

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v.vector	The Vi statistics, useful for the population sizes estimation, and their standard errors
cov	The covariance matrix of all the demographic parameters estimates.
neg	The position of the gamma parameters set to zero in the loglinear parameter vector.

#### Note

If your data contains more than one capture occasion within primary periods, use the periodhist function to create the input data matrix X needed by the openp function.

This function uses the glm function of the stats package.

### Author(s)

Louis-Paul Rivest < Louis - Paul . Rivest@mat.ulaval.ca> and Sophie Baillargeon

# References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Rivest, L.P. and Daigle, G. (2004) Loglinear models for the robust design in mark-recapture experiments. *Biometrics*, **60**, 100–107.

### See Also

```
closedp, periodhist, robustd
```

```
# duck data set
op.m1 <- openp(duck, dfreq = TRUE)
plot(op.m1)

# To remove the capture history 111111.
keep2 <- apply(histpos.t(6), 1, sum) != 6
op.m2 <- openp(duck, dfreq = TRUE, keep = keep2)
op.m2

# To remove the capture histories with 5 captures or more keep3 <- apply(histpos.t(6), 1, sum) < 5
op.m3 <- openp(duck, dfreq = TRUE, keep = keep3)
op.m3

# mvole data set aggregated per primary period mvole.op <- periodhist(mvole, vt = rep(5, 6))
openp(mvole.op, dfreq = TRUE)</pre>
```

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periodhist	Merge capture occasions	

# Description

This function produces a reduced matrix of capture histories from a complete one by merging together some capture occasions.

It can also be used to change the format of a capture-recapture data set with complete capture histories: it transforms a data set with one row per captured unit to a data set with one row per capture history followed by its frequency.

# Usage

```
periodhist(X, dfreq=FALSE, vt, drop=TRUE)
```

# **Arguments**

X	The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).
dfreq	A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.
vt	A vector containing the numbers of capture occasions for each pooled capture occasions. The length of this vector equals the number of capture occasions in the reduced matrix (noted $I$ ).
drop	A logical, by default TRUE, meaning that in the output matrix the unobserved capture histories (frequency of 0) are omitted. To keep them, drop must be set to FALSE.

### **Details**

This function is useful when using an open population model to analyze a robust design data set. It can be used to reduce the data set to one observation per primary period. A one represents a unit caught at least once during the period and a zero a unit never caught.

It is also useful for experiments with a large number of capture occasions but a limited number of catches, especially when there is no capture on some occasions. In such cases, one can pool together some capture occasions with the periodhist function.

If a data matrix produced by the periodhist function is given as an argument to a **Reapture** function, the dfreq argument must be set to TRUE.

# Value

A  $2^I - 1$  by I + 1 matrix of all the pooled capture histories, with their observed frequencies. If drop=TRUE (the default), the number of rows of this matrix is in fact  $2^I - 1$  minus the number of unobserved capture histories.

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### Author(s)

Louis-Paul Rivest < Louis - Paul . Rivest@mat.ulaval.ca> and Sophie Baillargeon

### References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

### See Also

openp

# **Examples**

```
# mvole data set aggregated per primary period
mvole.op <- periodhist(mvole, vt = rep(5, 6))
openp(mvole.op, dfreq = TRUE)</pre>
```

profileCI

Profile Likelihood Confidence Interval for Abundance Estimation in Closed Populations Capture-Recapture Experiments

# **Description**

As of version 1.2-0 of **Reapture**, this function is deprecated, but kept for back compatibility. Please use closedpCI.t instead.

The profileCI function computes the multinomial profile likelihood for the abundance of some closed population capture-recapture models.

# Usage

# **Arguments**

Χ

The table of the observed capture histories in one of the two accepted formats. In the default format, it has one row per unit captured in the experiment. In this case, the number of columns in the table represents the number of capture occasions in the experiment (noted t). In the alternative format, it contains one row per capture history followed by its frequency. In that case, X has t+1 columns. The first t columns of X, identifying the capture histories, must contain only zeros and ones. The number one indicates a capture.

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dfreq	This argument specifies the format of the data matrix X. By default, it is set to "FALSE", which means that X has one row per unit. If it is set to TRUE, then the matrix X contains frequencies in its last column.
m	A character string identifying the model, either "M0"=M0 model, "Mt"=Mt model, "Mh"=Mh model or "Mth"=Mth model.
h	A character string ("Chao" = Chao model, "Poisson" = $2^k - 1$ ), "Darroch" = $(k^2)/2$ or a numerical function taking only one argument specifying the form of the column for heterogeneity in the design matrix.
a	The value of the exponent's base for a Poisson model.
mX	The design matrix of the loglinear model. In this matrix, the order of the capture histories is as defined in the histpos.t function.
mname	A character string specifying the name of the customized model.
neg	If this option is set to TRUE, negative eta parameters in Chao models are set to zero.
alpha	A confidence interval with confidence level 1-alpha is constructed. The value of alpha must be between 0 and 1; the default is 0.05.
х	An object, produced by the profileCI function, to print.
	Further arguments passed to or from other methods.

# **Details**

This function does not work for closed population models featuring a behavioral effect, such as Mb and Mbh.

# Value

This function produces a plot of the multinomial profile likelihood for N. The value of N maximizing the profile likelihood and the bounds of the confidence interval are identified. It also produces the following objects:

n The number of captured units

results A table containing the abundance estimation and its confidence interval.

alpha 1-the confidence level of the interval.

# Author(s)

Louis-Paul Rivest < Louis-Paul . Rivest@mat.ulaval.ca> and Sophie Baillargeon

# References

Baillargeon, S. and Rivest, L.P. (2007) Reapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Cormack, R. M. (1992) Interval estimation for mark-recapture studies of closed populations. *Biometrics*, **48**, 567–576.

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# See Also

```
closedp, closedp.mX, closedp.h
```

### **Examples**

```
# hare data set
profileCI(hare, m = "Mth", h = "Poisson", a = 2)
# HIV data set
mat <- histpos.t(4)
mX2 <- cbind(mat, mat[, 1] * mat[, 2])
profileCI(hare, m = "Mh", h = "Chao")</pre>
```

rbvole

Robust Design Data for Red-Back Voles

# **Description**

This data set contains robust design capture history data for red-back voles.

# Usage

rbvole

# **Format**

66 by 19 numeric matrix, with the following columns:

c11, c12, c13 Capture histories from the three capture occasions within primary period 1

c21, c22, c23 Capture histories from the three capture occasions within primary period 2

c31, c32, c33 Capture histories from the three capture occasions within primary period 3

c41, c42, c43 Capture histories from the three capture occasions within primary period 4

c51, c52, c53 Capture histories from the three capture occasions within primary period 5

c61, c62, c63 Capture histories from the three capture occasions within primary period 6

freq Observed frequencies for each capture history

# **Details**

Data collection was carried out by Etcheverry and al.. The capture occasions represent three consecutive days of trapping in May 1999, July 1999, August 1999, May 2000, July 2000 and August 2000 in the Duchenier conservation area in southeastern Quebec. This data set is analyzed in Rivest and Daigle (2004).

Each row of this data set represents an observed capture history followed by its frequency.

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#### References

Rivest, L.P. and Daigle, G. (2004) Loglinear models for the robust design in mark-recapture experiments. *Biometrics*, **60**, 100–107.

# **Examples**

```
# According to Rivest and Daigle (2004), a good robust design model
# for this data set is formed of an Mth Chao model for each period.
# This model can be fitted as follows.

### memory.limit(size = 2000)
### rd <- robustd.t(rbvole, dfreq = TRUE, vt = rep(3, 6), vm = "Mth", vh = "Chao")

# WARNING : Because the data has 18 capture occasions, fitting this
# model uses a lot of memory. Its runtime is several minutes long.</pre>
```

robustd

Loglinear Models for Capture-Recapture Experiments Carried Out According to a Robust Design

# **Description**

These functions compute various demographic parameters and capture probabilities per period using loglinear robust design models in capture-recapture experiments.

robustd.t and robustd.0 fit the model using different response variable. robustd.t uses the frequencies of the observable capture histories in terms of capture success or failure for each capture occasions of each primary period. robustd.0 uses the frequencies of the observable capture histories in terms of number of captures per primary period.

# Usage

# Arguments

X The matrix of the observed capture histories (see Rcapture-package for a description of the accepted formats).

dfreq A logical. By default FALSE, which means that X has one row per unit. If TRUE, it indicates that the matrix X contains frequencies in its last column.

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νt A vector containing the numbers of capture occasions for each primary sampling period. The length of this vector equals the number of primary sampling periods (noted I).

A vector indicating the closed population model for each primary period. The νm elements of vm can be "none"=no model, "M0"=M0 model, "Mt"=Mt model,

"Mh"=Mh model or "Mth"=Mth model for robustd.t. For robustd.0, models with time effect are not allowed. So vm can than be "none"=no model, "M0"=M0 model, or "Mh"=Mh model. The 'no model' cannot be selected for the first or the last period. If a single character string is given for vm, the corresponding model is used for all periods. The default value for vm is "M0" for all period.

A list indicating, for each primary period with a heterogeneity model, the form of the columns for heterogeneity in the design matrix. The elements of vh can be "Chao", "Poisson", "Darroch" or any numerical R function created beforehand by the user. "Chao" represents Chao's model, "Poisson" represents the function  $f(k) = theta^k - 1$ , where k is the number of captures, "Darroch" represents the function  $f(k) = k^2/2$ , and "Gamma" represents the function  $f(k) = -\log(theta + k) + \log(theta)$ . If an R function is given, it is the implementation of any convex mathematical function f(k). It has only one argument. For the Poisson or Gamma model, the parameter theta is specified in

the argument vtheta.

A vector indicating, for each primary period with a Poisson or Gamma heterogeneity model, the value of the parameter. If vtheta consists of a single number, this number is used for all the periods with a Poisson or Gamma model. The default value for vtheta is 2 for all the periods with a Poisson or Gamma model.

If this option is set to TRUE, negative gamma parameters and negative eta parameters in Chao's models are set to zero. This insures that the estimated survival probabilities belong to [0, 1] and that the births are positive.

An object, produced by the robustd.t or the robustd.0 function, to print.

Further arguments to be passed to print.default.

### **Details**

These functions also generate statistics to test the presence of temporary emigration.

The Poisson regression used to fit a robust design model has one entry for each possible capture history, including those that are unobserved. The size of the dependent vector is therefore  $2^{\text{sum}(\text{vt})} - 1$ for robustd.t. Models with a large sum(vt) are hard to fit with robustd.t. robustd.0 uses a more parsimonious coding for the capture histories and can fit larger models.

Standard errors are calculated by linearization.

### Value

The number of captured units n

models A vector of length I identifying the closed population models chosen for each

period.

model.fit A table containing the deviance, degrees of freedom and AIC of the fitted model.

νh

vtheta

neg

х

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emig.fit	A table containing, for the model with an added temporary emigration effect, the deviance, the degrees of freedom and the Akaike's information criterion.
emig.param	The estimated temporary emigration parameters and their standards errors. The $I-1$ first rows are estimations of the differences $logit(p^b)-logit(p^w)$ for periods 2 to $I-1$ ( $p^b$ represents a between primary period and $p^w$ a within primary period estimate of the capture probability). The last row gives a pooled estimate of these differences calculated under the assumption that they are homogeneous. Negative estimates are associated with a temporary emigration.
capture.prob	The estimated capture probabilities per period and their standard errors.
survivals	The estimated survival probabilities between periods and their standard errors.
N	The estimated population sizes per period and their standard errors.
birth	The estimated number of new arrivals in the population between periods and their standard errors.
Ntot	The estimated total number of units who ever inhabited the survey area and its standard error.
loglin.param	The loglinear model parameters estimations and their standard errors, calculated by the ${\tt glm}$ function.
u.vector	The Ui statistics, useful for the survival probabilities calculation, and their standard errors
v.vector	The Vi statistics, useful for the population sizes estimation, and their standard errors
cov	The covariance matrix of all the demographic parameters estimates.
neg	The position of the gamma and eta parameters set to zero in the loglinear parameter vector.

# Note

This function uses the glm function of the **stats** package.

# Author(s)

Louis-Paul Rivest <Louis-Paul.Rivest@mat.ulaval.ca> and Sophie Baillargeon

# References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

Rivest, L.P. and Daigle, G. (2004) Loglinear models for the robust design in mark-recapture experiments. *Biometrics*, **60**, 100–107.

### See Also

closedp, openp

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# **Examples**

```
# The mvole data set contains a total of 30 capture occasions (the
# tenth capture occasion doesn't have any new capture and is taken
# out of the analysis). This number being large, we can only use
# the robustd.0 function to fit a robust design model.

# Not run :
# robustd.0(mvole[, -10], vt = c(5, 4, rep(5, 4)), vm = "Mh", vh = "Poisson", vtheta = 1.5)
# Should take a few seconds to run.

# Not run:
# robustd.t(mvole[, -10], vt = c(5, 4, rep(5, 4)), vm = 'Mh', vh = 'Poisson', vtheta = 1.5)
# Should fail.

# Considering only the first 3 periods of the data set, we can use the
# robustd.t function to fit a model with a temporal effect.
robustd.t(mvole[, c(1:9, 11:15)], vt = c(5, 4, 5), vm = "Mth", vh = "Poisson", vtheta = 1.5)
```

uifit

Closed Population Models Fit Statistics Concerning the ui

# Description

This function produces fit statistics concerning the  $u_i$ , i.e. the numbers of first captures on each capture occasion, for closed population models. It also forecasts, for some models, the number of additional units that would be captured if the experiment was continued for five more occasions.

# Usage

```
uifit(x.closedp)
```

### **Arguments**

x.closedp

An object produced by the closedp.t function.

### Value

predicted

The observed and predicted values of the ui frequencies,  $i=1,\ldots,t$ , for each model in closedp. For models M0, Mh Poisson2, Mh Darroch and Mb, predicted values are also extrapolated for  $i=t+1,\ldots,t+5$ .

fit.stat

 $\text{Chi-square fit statistics for each model in closedp} \ \big( \sum_{i=1}^t \frac{(\mathsf{observed}_i - \mathsf{predicted}_i)^2}{\mathsf{predicted}_i} \big).$ 

day.first.capt

The mean and variance of the day of first capture, calculated with the observed and predicted  $u_i$ , for each model in closedp.t.

# Author(s)

Louis-Paul Rivest < Louis - Paul . Rivest@mat.ulaval.ca> and Sophie Baillargeon

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# References

Baillargeon, S. and Rivest, L.P. (2007) Rcapture: Loglinear models for capture-recapture in R. *Journal of Statistical Software*, **19**(5), doi:10.18637/jss.v019.i05.

# See Also

closedp

```
# Third primary period of mvole data set
period3 <- mvole[, 11:15]
cp <- closedp(period3)
uifit(cp)</pre>
```

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