# Package 'LATERmodel'

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Title Linear Approach to Threshold with Ergodic Rate for Reaction
Times

Version 0.2.0

**Description** Implements the Linear Approach to Threshold with Ergodic Rate (LATER) model, which predicts distributions of reaction times and summarises them with as little as two free parameters. Allows for easy visualisation and comparison of datasets, along with fitting of datasets using the LATER model.

```
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carpenter\_williams\_1995

Digitised data corresponding to Figure 2 of Carpenter and Williams (1995)

# **Description**

Digitised data corresponding to Figure 2 of Carpenter and Williams (1995)

# Usage

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```
carpenter_williams_1995
```

# **Format**

```
carpenter_williams_1995:
```

A dataframe of 20014 reaction times for participant a and 22518 reaction times for participant b **participant** Participant "name", either "a" or "b"

**condition** Prior percentage probability of the target being in the location of the eye movement (p05, p10, p25, p50, p75, p90, or p95)

time Saccadic latency in ms

#### Source

Carpenter, R. H., & Williams, M. L. L. (1995). Neural computation of log likelihood in control of saccadic eye movements. Nature, 377(6544), 59-62.

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compare\_fits

Compares the goodness-of-fit of a set of fit outcomes.

#### Description

Compares the goodness-of-fit of a set of fit outcomes.

# Usage

```
compare_fits(fits)
```

# Arguments

fits

A list where each item has a name that identifies the fit and a value given by the output of LATERmodel::fit\_data.

#### **Details**

The 'evidence ratio' is calculated as per Motulsky & Christopolous (2004), p. 146.

#### Value

A list of fit comparison results, ordered such that the fit with the lowest AIC value is in the first row.

- aic contains the fit AIC values.
- preferred\_rel\_fit\_delta\_aic is the AIC value for the fit relative to the AIC of the fit with the lowest AIC (preferred AIC current AIC).
- preferred\_rel\_fit\_evidence\_ratio is the evidence ratio for the fit with the lowest AIC relative to the current fit.
- preferred is a boolean that indicates whether the fit has the lowest AIC value among the fits (is 'preferred').

```
data <- rbind(
  data.frame(name = "test", time = 1000/rnorm(100, 3, 1)),
  data.frame(name = "test_2", time = 1000/rnorm(100, 1, 1))
) |> dplyr::filter(time > 0)
data <- prepare_data(data)
fit_a <- fit_data(data = data, share_a = TRUE)
fit_b <- fit_data(data = data, share_sigma = TRUE)
comparison <- compare_fits(fits = list(a = fit_a, b = fit_b))</pre>
```

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fit\_data

Fit a LATER model to a single dataset or a pair of datasets.

# **Description**

Fit a LATER model to a single dataset or a pair of datasets.

#### Usage

```
fit_data(
  data,
  share_a = FALSE,
  share_sigma = FALSE,
  share_sigma_e = FALSE,
  with_early_component = FALSE,
  intercept_form = FALSE,
  use_minmax = FALSE,
  fit_criterion = "likelihood",
  jitter_settings = list(n = 7, prop = 0.5, seed = NA, processes = 2)
```

#### **Arguments**

data

A data frame with columns name and promptness.

share\_a, share\_sigma, share\_sigma\_e

If FALSE (the default), each dataset has its own parameter. If TRUE, the datasets share the relevant parameter.

with\_early\_component

If TRUE, the model contains a second 'early' component that is absent when FALSE (the default).

intercept\_form If FALSE (the default), the a parameter describes the mu parameter in the model; if TRUE, the a parameter describes the k parameter in the model (the intercept).

use\_minmax

If FALSE (the default), the optimiser targets the sum of the goodness-of-fit values across datasets; if TRUE, it instead targets the maximum of the goodness-of-fit values across datasets.

fit\_criterion

String indicating the criterion used to optimise the fit by seeking its minimum.

- ks: Kolmogorov-Smirnov statistic.
- likelihood: Negative log-likelihood.

jitter\_settings

Settings for running the fitting multiple times with randomly-generated offsets ('jitter') applied to the starting estimates.

- n: How many jitter iterations to run (default of 7); the total number of fits is n + 1 (because the un-jittered start points are also fit).
- prop: The maximum jitter offset, as a proportion of the start value (default of 0.5).

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- seed: Seed for the random jitter generator (default is unseeded).
- processes: Maximum number of CPU processes that can be used (default is 2).

#### Value

A list of fitting arguments and outcomes.

- fitted\_params is a named list of fitted parameter values.
- named\_fit\_params is a data frame with rows given by the dataset names and columns given by the parameter names.
- loglike is the overall log-likelihood of the fit.
- aic is the "Akaike's 'An Information Criterion'" value for the model.
- optim\_result is the raw output from stats::optim for the best fit.
- jitter\_optim\_results contains the raw output from each call to stats::optim for the different start points.

#### **Examples**

```
data <- data.frame(name = "test", promptness = rnorm(100, 3, 1))
data_other <- data.frame(name = "test_2", promptness = rnorm(100, 1, 1))
fit_shared_sigma <- fit_data(
    data = rbind(data, data_other), share_sigma = TRUE
)</pre>
```

individual\_later\_fit Fit individual LATER model to each dataset in a dataframe of datasets

# Description

Fit individual LATER model to each dataset in a dataframe of datasets

# Usage

```
individual_later_fit(
   df,
   with_early_component = FALSE,
   fit_criterion = "likelihood",
   jitter_settings = list(n = 7, prop = 0.5, seed = NA, processes = 2)
)
```

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# **Arguments**

 $\label{eq:component} A \ data frame \ with \ columns: \ time, \ name, \ promptness, \ and \ e\_cdf$  with\_early\_component

If TRUE, the model contains a second 'early' component that is absent when FALSE (the default).

fit\_criterion String indicating the criterion used to optimise the fit by seeking its minimum.

- ks: Kolmogorov-Smirnov statistic.
- neg\_loglike: Negative log-likelihood.

jitter\_settings

Settings for running the fitting multiple times with randomly-generated offsets ('jitter') applied to the starting estimates.

- n: How many jitter iterations to run (default of 7).
- prop: The maximum jitter offset, as a proportion of the start value (default of 0.5).
- seed: Seed for the random jitter generator (default is unseeded).
- processes: Maximum number of CPU processes that can be used (default is 2).

#### Value

A dataframe with one row for each named dataset in df and columns equal to the LATER model parameters returned by fit\_data\$named\_fit\_params

# **Examples**

```
data <- rbind(
  data.frame(name = "test", promptness = rnorm(100, 3, 1)),
  data.frame(name = "test_2", promptness = rnorm(100, 1, 1))
)
fit_params <- individual_later_fit(data)</pre>
```

ks\_compare

Apply two-sample KS test to all pairs of datasets contained within a dataframe

# **Description**

Apply two-sample KS test to all pairs of datasets contained within a dataframe

# Usage

```
ks_compare(df, correct_multiple_comparisons = TRUE)
```

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# Arguments

df A dataframe of datasets with columns: name and time, one unique name per dataset correct\_multiple\_comparisons

If TRUE, an adjustment will be made to the p-values based on Holm, 1979, A simple sequentially rejective multiple test procedure

#### Value

A dataframe with columns name1, name2, D, and p\_value

### **Examples**

```
data <- prepare_data(dplyr::filter(
  carpenter_williams_1995,
  participant == "b"
))
ks_compare(data)</pre>
```

ks\_heatmap

Create a heatmap to visualise if there is not enough evidence to reject the null hypothesis that two datasets come from the same underlying distribution

# Description

Create a heatmap to visualise if there is not enough evidence to reject the null hypothesis that two datasets come from the same underlying distribution

# Usage

```
ks_heatmap(ks_results)
```

# Arguments

ks\_results

A dataframe with columns name1, name2, D, and p-value, obtained using the function ks\_compare

# Value

A heatmap plot with all paired comparisons

```
data <- prepare_data(dplyr::filter(
   carpenter_williams_1995,
   participant == "b"
))
ks_results <- ks_compare(data)
ks_heatmap(ks_results)</pre>
```

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model_cdf	Evalulate the cumulative distribution function under the model.	

# Description

Evalulate the cumulative distribution function under the model.

# Usage

```
model_cdf(q, later_mu, later_sd, early_sd = NULL)
```

# Arguments

q	Vector of quantiles
later_mu	Vector of the mean of the later component.
later_sd	Vector of the standard deviation of the later component.
early_sd	Vector of the standard deviation of the early component, or NULL if there is no
	early component (the default).

# Value

Vector of cumulative distribution values

# **Examples**

```
model_cdf(q = 1, later_mu = 1, later_sd = 1)
model_cdf(q = 1, later_mu = 1, later_sd = 1, early_sd = 3)
```

model\_pdf

Evalulate the probability density function under the model.

# Description

Evalulate the probability density function under the model.

# Usage

```
model_pdf(x, later_mu, later_sd, early_sd = NULL, log = FALSE)
```

# Arguments

Х	Vector of quantiles
later_mu	Vector of the mean of the later component.
later_sd	Vector of the standard deviation of the later component.
early_sd	Vector of the standard deviation of the early component, or NULL if there is no early component (the default).
log	If TRUE, probabilities are given as log(p).

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#### Value

Vector of probabilities

### **Examples**

```
model_pdf(x = 1, later_mu = 1, later_sd = 1)
model_pdf(x = 1, later_mu = 1, later_sd = 1, early_sd = 3)
```

prepare\_data

Prepares data for reciprobit plot

# **Description**

Prepares data for reciprobit plot

# Usage

```
prepare_data(raw_data, time_unit = "ms", name_separator = "_")
```

# **Arguments**

raw\_data

Vector of reaction times for a single participant, or a dataframe containing a column called time with the reaction times and optional other columns:

- a column called name with a unique label for each dataset
- a column called participant with a unique id per participant and another called condition with a unique label for each condition. In this case the name for each dataset will be constructed as participant+name\_separator+condition.
- a column called color that contains one hexadecimal color code for each dataset. In this case the name for each dataset will be set to be the name of the color.

time\_unit

Units of the reaction times in rt\_vector, must be one of "ms", "ds", or "s".

name\_separator If the raw\_data dataframe does not contain a name column, but does have participant and condition columns, the name for each dataset will be constructed as participant+name\_separator+condition.

#### Value

A dataframe with columns: time, color, name, promptness, and e\_cdf.

```
df <- prepare_data(carpenter_williams_1995)</pre>
```

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promptness_ecdf	Compute the empirical cumulative distribution function for promptness

# Description

Compute the empirical cumulative distribution function for promptness

# Usage

```
promptness_ecdf(promptness, adjust_for_times = TRUE, eval_unique = FALSE)
```

# **Arguments**

```
promptness A vector of promptness values (1 / times)

adjust_for_times

If TRUE (the default), the returned y value is such that 1 - y = P(1/promptness <= 1/x). If FALSE, the eval_unique

If FALSE (the default), the ECDF is evaluated at all values in promptness. If TRUE, the ECDF is evaluated at the unique values in promptness.
```

#### Value

A data frame with attributes:

- x is the values at which the ECDF was evaluated.
- y is the evaluated value of the ECDF.

#### **Examples**

```
p <- promptness_ecdf(promptness = rnorm(100, 3, 1))</pre>
```

# Description

Plot reaction times and LATER model fit in reciprobit axes

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# Usage

```
reciprobit_plot(
  plot_data,
  fit_params = NULL,
  time_breaks = c(0.1, 0.2, 0.3, 0.5, 1),
  probit_breaks = c(0.1, 1, 5, 10, 20, 50, 80, 90, 95, 99, 99.9),
  z_breaks = c(-2, -1, 0, 1, 2),
  xrange = NULL,
  yrange = NULL
)
```

# **Arguments**

plot_data	A dataframe with columns: time, name, promptness, and e_cdf. Optionally, there may be a color column, which contains hex values, one unique hex value per named dataset
fit_params	A dataframe with one row for each named dataset and columns equal to the LATER model parameters returned by $fit_data$named_fit_params$
time_breaks	Desired tick marks on the x axis, expressed in promptness (1/s)
probit_breaks	Desired tick marks on the y axis in probit space
z_breaks	Desired tick marks on secondary y axis, in z values
xrange	Desired range for the x axis, in promptness (1/s)
yrange	Desired range for the y axis, in cumulative probability space

# Value

A reciprobit plot with the cumulative probability distribution of the reaction times

```
data <- rbind(
  data.frame(name = "test", time = 1000/rnorm(100, 3, 1)),
  data.frame(name = "test_2", time = 1000/rnorm(100, 4, 1))
) |> dplyr::filter(time > 0)
data <- prepare_data(data)
fit_params <- individual_later_fit(data)
reciprobit_plot(data, fit_params)</pre>
```

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```
reddi_asrress_carpenter_2003
```

Digitised data corresponding to Figure 2 of Reddi, Asrress, and Carpenter, 2003.

# **Description**

Digitised data corresponding to Figure 2 of Reddi, Asrress, and Carpenter, 2003.

# Usage

```
reddi_asrress_carpenter_2003
```

#### **Format**

```
reddi_asrress_carpenter_2003:

A dataframe of 1600 reaction times for participant J

participant Participant "name", equal to "J"

condition Different degrees of coherence of the kinematograms shown as stimuli, (64%, 32%, 16%, 8%: S, low-urgency-slow and accurate-conditions)

time Saccadic latency in ms
```

#### **Source**

Reddi, B. A., Asrress, K. N., & Carpenter, R. H. (2003). Accuracy, information, and response time in a saccadic decision task. Journal of Neurophysiology, 90(5), 3538-3546.

simulate\_dataset

Simulate a dataset given model parameters.

# Description

Generates samples from a set of provided LATER model parameters, with the option to iteratively replace invalid samples (reaction times  $\leq$  0).

# Usage

```
simulate_dataset(
    n,
    later_mu,
    later_sd,
    early_sd = NULL,
    seed = NA,
    allow_negative_times = FALSE
)
```

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# Arguments

n	Number of samples (trials)
later_mu	Mean of the later component.
later_sd	Standard deviation of the later component.
early_sd	Standard deviation of the early component, or NULL if there is no early component (the default).
seed	Seed for the random number generator
allow_negative_	times

If FALSE (the default), any random samples that have negative response times are iteratively replaced such that all returned samples are positive. If TRUE, no such replacement is performed.

### •

# Value

Vector of response times (in seconds)

```
simulate_dataset(n = 100, later_mu = 5, later_sd = 1)
simulate_dataset(n = 100, later_mu = 5, later_sd = 1, early_sd = 5)
```

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