Package 'CMTFtoolbox'

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      ing 'ACMTF_modelSelection()' and 'ACMTFR_modelSelection()'. The CMTF and ACMTF meth-
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```

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 ${\tt acmtfr_fg}$

Calculate function value of ACMTF

Description

Calculate function value of ACMTF

Usage

```
acmtfr_fg(
    x,
    Z,
    Y,
    alpha = 1,
    beta = rep(0.001, length(Z$object)),
    epsilon = 1e-08,
    pi = 0.5,
    mu = 1e-06
)
```

Arguments

X	Vectorized parameters of the CMTF model.
Z	Z object as generated by setupCMTFdata().
Υ	Dependent variable (regression part).
alpha	Alpha value of the loss function as specified by Acar et al., 2014
beta	Beta value of the loss function as specified by Acar et al., 2014
epsilon	Epsilon value of the loss function as specified by Acar et al., 2014
pi	Pi value of the loss function as specified by Van der Ploeg et al., 2025.
mu	Ridge term parameter for calculation of the regression coefficients rho (default = 1e-6).

Value

Scalar of the loss function value (when manual=FALSE), otherwise a list containing all loss terms.

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
```

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```
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
Y = A[,1]

init = initializeACMTF(Z, 2, output="vect")
outcome = acmtfr_fg(init, Z, Y)
f = outcome$fn
g = outcome$gr
```

 $acmtfr_fun$

Calculate function value of ACMTF

Description

Calculate function value of ACMTF

Usage

```
acmtfr_fun(
    x,
    Z,
    Y,
    alpha = 1,
    beta = rep(0.001, length(Z$object)),
    epsilon = 1e-08,
    pi = 0.5,
    mu = 1e-06,
    manual = FALSE
)
```

Arguments

X	Vectorized parameters of the CMTF model.
Z	Z object as generated by setupCMTFdata().
Υ	Dependent variable (regression part).
alpha	Alpha value of the loss function as specified by Acar et al., 2014
beta	Beta value of the loss function as specified by Acar et al., 2014
epsilon	Epsilon value of the loss function as specified by Acar et al., 2014
pi	Pi value of the loss function as specified by Van der Ploeg et al., 2025.
mu	Ridge term parameter for calculation of the regression coefficients rho (default = $1e$ -6).
manual	Manual calculation of each loss term (default FALSE).

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Value

Scalar of the loss function value (when manual=FALSE), otherwise a list containing all loss terms.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(100,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
Y = A[,1]

init = initializeACMTF(Z, 2, output="vect")
f = acmtfr_fun(init, Z, Y)
```

acmtfr_gradient

Calculate gradient of ACMTF model.

Description

Calculate gradient of ACMTF model.

Usage

```
acmtfr_gradient(
    x,
    Z,
    Y,
    alpha = 1,
    beta = rep(0.001, length(Z$object)),
    epsilon = 1e-08,
    pi = 0.5,
    mu = 1e-06
)
```

Arguments

```
    Vectorized parameters of the CMTF model.
    Z object as generated by setupCMTFdata().
    Y Dependent variable (regression part).
    alpha Alpha value of the loss function as specified by Acar et al., 2014
```

beta	Beta value of the loss function as specified by Acar et al., 2014
epsilon	Epsilon value of the loss function as specified by Acar et al., 2014
pi	Pi value of the loss function as specified by Van der Ploeg et al., 2025.
mu	Ridge term parameter for calculation of the regression coefficients rho (default = 1e-6).

Value

Vectorized gradient of the ACMTF regression model.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
Y = A[,1]

init = initializeACMTF(Z, 2, output="vect")
g = acmtfr_gradient(init, Z, Y)
```

 ${\tt ACMTFR_modelSelection} \ \ \textit{Model selection for ACMTFR}$

Description

Model selection for ACMTFR

```
ACMTFR_modelSelection(
  datasets,
  modes,
  Y,
  sharedMode = 1,
  maxNumComponents = 5,
  alpha = 1,
  beta = rep(0.001, length(Z$object)),
  epsilon = 1e-08,
  pi = 0.5,
  normalize = TRUE,
```

```
normY = 1,
method = "CG",
cg_update = "HS",
line_search = "MT",
max_iter = 10000,
max_fn = 10000,
abs_tol = 1e-10,
rel_tol = 1e-10,
grad_tol = 1e-10,
nstart = 5,
numCores = 1,
cvFolds = 2
```

Arguments

datasets List of arrays of datasets. Multi-way and two-way may be combined.

Mumbered modes per dataset in a list. Example element 1: 1 2 3 and element 2:

1 4 for the X tensor and Y matrix case with a shared subject mode.

Y Dependent variable (regression part).

sharedMode Mode that is shared between all blocks, used to remove fibers for numFolds

randomly initialized models.

maxNumComponents

Maximum number of components to check (default 3).

alpha Scalar penalizing the components to be norm 1 (default 1).

beta Vector of penalty values for each dataset, penalizing the lambda terms (default

1e-3).

epsilon Scalar value to make it possible to compute the partial derivatives of lambda

(default 1e-8).

pi Pi value of the loss function as specified by Van der Ploeg et al., 2025.

normalize Normalize the X blocks to frobenius norm 1 (default TRUE).

normY Normalize Y to a specific value, (default: 1).

method Optimization method to use (default = "CG", the conjugate gradient). See

mize::mize() for other options.

cg_update Update method for the conjugate gradient algorithm, see mize::mize() for the

options (default="HS", Hestenes-Steifel).

line_search Line search algorithm to use, see mize::mize() for the options (default="MT",

More-Thuente).

max_iter Maximum number of iterations.

max_fn Maximum number of function evaluations.

abs_tol Function tolerance criterion for convergence.

rel_tol Relative function tolerance criterion for convergence.

grad_tol Absolute tolerence for the 12-norm of the gradient vector.

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Number of models to produce (default 1). If set higher than one, the package will return the best fitted model.

NumCores

Number of cores to use (default 1). If set higher than one, the package will attempt to run in parallel.

cvFolds

Number of CV folds to create (default 10).

Value

List object containing plots of all metrics and dataframes containing the data used to create them.

Examples

```
set.seed(123)
I = 10
J = 5
K = 3
df = array(rnorm(I*J*K), c(I,J,K))
df2 = array(rnorm(I*J*K), c(I,J,K))
datasets = list(df, df2)
modes = list(c(1,2,3), c(1,4,5))
Y = as.matrix(rnorm(I))
# A very small procedure is run to limit computational requirements
result = ACMTFR_modelSelection(datasets,
                              modes,
                              Υ,
                              pi=1.0,
                              maxNumComponents=2,
                              nstart=2,
                              cvFolds=2,
                              rel_tol=0.5,
                              abs_tol=0.5)
result$plots$overview
```

acmtfr_opt

Advanced coupled matrix and tensor factorizations

Description

Advanced coupled matrix and tensor factorizations

```
acmtfr_opt(
  Z,
  Y,
  numComponents,
```

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```
initialization = "random",
  alpha = 1,
  beta = rep(0.001, length(Z$object)),
  epsilon = 1e-08,
  pi = 0.5,
 mu = 1e-06,
 method = "CG",
  cg_update = "HS",
  line_search = "MT",
 max_iter = 10000,
 max_fn = 10000,
  abs_tol = 1e-10,
  rel_tol = 1e-10,
  grad_tol = 1e-10,
  nstart = 1,
  numCores = 1,
  sortComponents = TRUE,
  allOutput = FALSE
)
```

Arguments

Z Combined dataset and mode object as produced by setupCMTFdata().

Y Dependent variable (regression part).

numComponents Number of components

initialization Initialization, either "random" (default) or "nvec" for numComponents compo-

nents of the concatenated data using svd. Ignored and uses NPLS based initial-

ization if pi=0.

alpha Scalar penalizing the components to be norm 1 (default 1).

beta Vector of penalty values for each dataset, penalizing the lambda terms (default

1e-3).

epsilon Scalar value to make it possible to compute the partial derivatives of lambda

(default 1e-8).

pi Pi value of the loss function as specified by Van der Ploeg et al., 2025.

mu Ridge term parameter for calculation of the regression coefficients rho (default

= 1e-6).

method Optimization method to use (default = "CG", the conjugate gradient). See

mize::mize() for other options.

cg_update Update method for the conjugate gradient algorithm, see mize::mize() for the

options (default="HS", Hestenes-Steifel).

line_search Line search algorithm to use, see mize::mize() for the options (default="MT",

More-Thuente).

max_iter Maximum number of iterations.

max_fn Maximum number of function evaluations.
abs_tol Function tolerance criterion for convergence.

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rel_tol	Relative function tolerance criterion for convergence.	
grad_tol	Absolute tolerence for the 12-norm of the gradient vector. Number of models to produce (default 1). If set higher than one, the packag will return the best fitted model.	
nstart		
numCores	Number of cores to use (default 1). If set higher than one, the package will attempt to run in parallel.	
sortComponents	Sort the components in the output by descending order of variation explained.	
allOutput	Return all created models. Ignored if nstart=1.	

Value

List object, similar to mize::mize() output. Includes a Fac object of the model, which is a list of components per mode. Also includes an init object giving the initialized input vectors.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
Y = A[,1]
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

# specific setting to reduce runtime for CRAN
model = acmtfr_opt(Z, Y, 2, rel_tol=1e-5, abs_tol=1e-5)
```

acmtf_fg

Function value and gradient calculation for ACMTF

Description

Function value and gradient calculation for ACMTF

```
acmtf_fg(x, Z, alpha = 1, beta = rep(0.001, length(Z$object)), epsilon = 1e-08)
```

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Arguments

X	Vectorized parameters of the CMTF model.
Z	Z object as generated by setupCMTFdata().
alpha	Alpha value of the loss function as specified by Acar et al., 2014
beta	Beta value of the loss function as specified by Acar et al., 2014
epsilon	Epsilon value of the loss function as specified by Acar et al., 2014

Value

A list containing the function ("fn") and the gradient ("gr").

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

init = initializeACMTF(Z, 2, output="vect")
outcome = acmtf_fg(init, Z)
f = outcome$fn
g = outcome$gr
```

acmtf_fun

Calculate function value of ACMTF

Description

Calculate function value of ACMTF

```
acmtf_fun(
    x,
    Z,
    alpha = 1,
    beta = rep(0.001, length(Z$object)),
    epsilon = 1e-08,
    manual = FALSE
)
```

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Arguments

X	Vectorized parameters of the CMTF model.
Z	Z object as generated by setupCMTFdata().
alpha	Alpha value of the loss function as specified by Acar et al., 2014
beta	Beta value of the loss function as specified by Acar et al., 2014
epsilon	Epsilon value of the loss function as specified by Acar et al., 2014
manual	Manual calculation of each loss term (default FALSE)

Value

Scalar of the loss function value (when manual=FALSE), otherwise a list containing all loss terms

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
init = initializeACMTF(Z, 2, output="vect")
f = acmtf_fun(init, Z)
```

 $acmtf_gradient$

Calculate gradient of ACMTF model.

Description

Calculate gradient of ACMTF model.

```
acmtf_gradient(
   x,
   Z,
   alpha = 1,
   beta = rep(0.001, length(Z$object)),
   epsilon = 1e-08
)
```

Arguments

X	Vectorized parameters of the CMTF model.
Z	Z object as generated by setupCMTFdata().
alpha	Alpha value of the loss function as specified by Acar et al., 2014
beta	Beta value of the loss function as specified by Acar et al., 2014
epsilon	Epsilon value of the loss function as specified by Acar et al., 2014

Value

Vectorized gradient of the ACMTF model.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

init = initializeACMTF(Z, 2, output="vect")
g = acmtf_gradient(init, Z)
```

Description

Model selection for ACMTF

```
ACMTF_modelSelection(
  datasets,
  modes,
  maxNumComponents = 3,
  sharedMode = 1,
  alpha = 1,
  beta = rep(0.001, length(datasets)),
  epsilon = 1e-08,
  nstart = 10,
  cvFolds = 10,
```

```
numCores = 1,
method = "CG",
cg_update = "HS",
line_search = "MT",
max_iter = 10000,
max_fn = 1e+05,
rel_tol = 1e-08,
abs_tol = 1e-08,
grad_tol = 1e-08,
plots = TRUE
)
```

Arguments

datasets List of arrays of datasets. Multi-way and two-way may be combined.

modes Numbered modes per dataset in a list. Example element 1: 1 2 3 and element 2:

1 4 for the X tensor and Y matrix case with a shared subject mode.

maxNumComponents

Maximum number of components to check (default 3).

sharedMode Mode that is shared between all blocks, used to remove fibers for numFolds

randomly initialized models.

alpha Scalar penalizing the components to be norm 1 (default 1).

beta Vector of penalty values for each dataset, penalizing the lambda terms (default

1e-3).

epsilon Scalar value to make it possible to compute the partial derivatives of lambda

(default 1e-8).

nstart Number of randomly initialized models to create (default 10).

cvFolds Number of CV folds to create (default 10).

numCores Number of cores to use (default 1). A number higher than 1 will run the process

in parallel.

method Optimization method to use (default = "CG", the conjugate gradient). See

mize::mize() for other options.

cg_update Update method for the conjugate gradient algorithm, see mize::mize() for the

options (default="HS", Hestenes-Steifel).

line_search Line search algorithm to use, see mize::mize() for the options (default="MT",

More-Thuente).

max_iter Maximum number of iterations.

max_fn Maximum number of function evaluations.

rel_tol Relative function tolerance criterion for convergence.

abs_tol Function tolerance criterion for convergence.

grad_tol Absolute tolerence for the 12-norm of the gradient vector.

plots Boolean to state if plots should be made of the outcome.

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Value

List object containing variation explained, FMS, and degeneracy score metrics. If plots=TRUE, plots will be attached to the list.

Examples

```
set.seed(123)
I = 10
J = 5
K = 3
df = array(rnorm(I*J*K), c(I,J,K))
df2 = array(rnorm(I*J*K), c(I,J,K))
datasets = list(df, df2)
modes = list(c(1,2,3), c(1,4,5))
# A very small procedure is run to limit computational requirements
# Plots are not made to reduce CRAN runtime.
result = ACMTF_modelSelection(datasets,
                              maxNumComponents=1,
                              nstart=2,
                              cvFolds=2,
                              rel_tol=1e-1,
                              abs_tol=1e-1,
                              max_iter=2,
                              plots=FALSE)
```

acmtf_opt

Advanced coupled matrix and tensor factorizations

Description

Advanced coupled matrix and tensor factorizations

```
acmtf_opt(
  Z,
  numComponents,
  initialization = "random",
  alpha = 1,
  beta = rep(0.001, length(Z$object)),
  epsilon = 1e-08,
  method = "CG",
  cg_update = "HS",
  line_search = "MT",
  max_iter = 10000,
```

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```
max_fn = 10000,
abs_tol = 1e-10,
rel_tol = 1e-10,
grad_tol = 1e-10,
nstart = 1,
numCores = 1,
sortComponents = TRUE,
allOutput = FALSE
)
```

Arguments

Z	Combined dataset and mode object as produced by setupCMTFdata().
numComponents	Number of components
initialization	Initialization, either "random" (default) or "nvec" for numComponents components of the concatenated data using svd.
alpha	Scalar penalizing the components to be norm 1 (default 1).
beta	Vector of penalty values for each dataset, penalizing the lambda terms (default 1e-3).
epsilon	Scalar value to make it possible to compute the partial derivatives of lambda (default 1e-8).
method	Optimization method to use (default = "CG", the conjugate gradient). See $mize::mize()$ for other options.
cg_update	Update method for the conjugate gradient algorithm, see mize::mize() for the options (default="HS", Hestenes-Steifel).
line_search	Line search algorithm to use, see $mize::mize()$ for the options (default="MT", More-Thuente).
max_iter	Maximum number of iterations.
max_fn	Maximum number of function evaluations.
abs_tol	Function tolerance criterion for convergence.
rel_tol	Relative function tolerance criterion for convergence.
grad_tol	Absolute tolerence for the 12-norm of the gradient vector.
nstart	Number of models to produce (default 1). If set higher than one, the package will return the best fitted model.
numCores	Number of cores to use (default 1). If set higher than one, the package will attempt to run in parallel.
sortComponents	Sort the components in the output by descending order of variation explained.
allOutput	Return all created models. Ignored if nstart=1.

Value

List object, similar to mize::mize() output. Includes a Fac object of the model, which is a list of components per mode. Also includes an init object giving the initialized input vectors.

cmtf_fg

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

# specific setting to reduce runtime for CRAN
model = acmtf_opt(Z, 1, rel_tol=1e-5, abs_tol=1e-5)
```

cmtf_fg

Function value and gradient calculation for CMTF

Description

Function value and gradient calculation for CMTF

Usage

```
cmtf_fg(x, Z)
```

Arguments

- x Vectorized parameters of the CMTF model.
- Z dobject as generated by setupCMTFdata().

Value

A list containing the function ("fn") and the gradient ("gr").

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
```

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```
init = initializeCMTF(Z, 2, output="vect")
outcome = cmtf_fg(init, Z)
f = outcome$fn
g = outcome$gr
```

cmtf_fun

Calculate function value of CMTF

Description

Calculate function value of CMTF

Usage

```
cmtf_fun(x, Z, manual = FALSE)
```

Arguments

x Vectorized parameters of the CMTF model.

Z object as generated by setupCMTFdata().

manual Manual calculation of each loss term (default FALSE)

Value

Function value of the CMTF loss value if manual=FALSE, otherwise a vector of the loss values per term.

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

init = initializeCMTF(Z, 2, output="vect")
f = cmtf_fun(init, Z)
```

cmtf_gradient 19

cmtf_gradient

Calculate gradient of CMTF model.

Description

Calculate gradient of CMTF model.

Usage

```
cmtf_gradient(x, Z)
```

Arguments

- x Vectorized parameters of the CMTF model.
- Z doject as generated by setupCMTFdata().

Value

Vectorized gradient of the CMTF model.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
init = initializeCMTF(Z, 2, output="vect")
g = cmtf_gradient(init, Z)
```

cmtf_opt

Coupled matrix and tensor factorizations

Description

Coupled matrix and tensor factorizations

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Usage

```
cmtf_opt(
 Ζ,
  numComponents,
  initialization = "random",
 method = "CG",
  cg\_update = "HS",
  line_search = "MT",
 max_iter = 10000,
 max_fn = 10000,
  abs_tol = 1e-08,
  rel_tol = 1e-08,
 grad_tol = 1e-08,
  nstart = 1,
 numCores = 1,
  sortComponents = TRUE,
 allOutput = FALSE
)
```

Arguments

Z	Combined dataset and mode object as produced by setupCMTFdata().
numComponents	Number of components
initialization	Initialization, either "random" (default) or "nvec" for numComponents components of the concatenated data using svd.
method	Optimization method to use (default = "CG", the conjugate gradient). See $mize::mize()$ for other options.
cg_update	Update method for the conjugate gradient algorithm, see mize::mize() for the options (default="HS", Hestenes-Steifel).
line_search	Line search algorithm to use, see $\mbox{mize::mize()}$ for the options (default="MT", More-Thuente).
max_iter	Maximum number of iterations.
max_fn	Maximum number of function evaluations.
abs_tol	Function tolerance criterion for convergence.
rel_tol	Relative function tolerance criterion for convergence.
grad_tol	Absolute tolerence for the l2-norm of the gradient vector.
nstart	Number of models to produce (default 1). If set higher than one, the package will return the best fitted model.
numCores	Number of cores to use (default 1). If set higher than one, the package will attempt to run in parallel.
sortComponents	Sort the components in the output by descending order of variation explained.
allOutput	Return all created models. Ignored if nstart=1.

computeFMS 21

Value

List object, similar to mize::mize() output. Includes a Fac object of the model, which is a list of components per mode. Also includes an init object giving the initialized input vectors.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

model = cmtf_opt(Z, 1, rel_tol=1e-4) # quick convergence for example only
```

computeFMS

Compute Factor Match Score for two models.

Description

Compute Factor Match Score for two models.

Usage

```
computeFMS(Fac1, Fac2, modes)
```

Arguments

Fac1 A list of matrices corresponding to found components per mode in model 1.

Fac2 A list of matrices corresponding to found components per mode in model 2.

modes List of modes per dataset.

Value

Vector of FMS scores, one per dataset.

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100, 2))
E = array(rnorm(10*2), c(10, 2))
```

22 degenScore

```
Fac1 = list(A,B,C,D,E)

Fac2 = Fac1 # identical models for the purposes of demonstration

modes = list(c(1,2,3), c(1,4,5))

FMS_result = computeFMS(Fac1, Fac2, modes) # FMS_result = c(1,1)
```

degenScore

degenScore

Description

Computes the maximum absolute off-diagonal Tucker congruence coefficient between subject-mode components in an ACMTF model. This metric serves as a diagnostic tool to detect potential degeneracy in the subject-mode loadings.

Usage

```
degenScore(A)
```

Arguments

Α

A numeric matrix of subject-mode loadings (dimensions: subjects x components).

Details

A high degenScore (e.g., > 0.85) indicates that two or more components in the subject mode are highly similar, suggesting a possible degeneracy or lack of uniqueness. A low value (e.g., < 0.3) indicates well-separated components.

Value

A numeric scalar representing the maximum absolute off-diagonal Tucker congruence between components.

```
# Example: Compute degenScore for a random loading matrix
A <- matrix(rnorm(100), nrow = 10, ncol = 10)
degenScore(A)</pre>
```

fac_to_vect 23

fac_to_vect

Vectorize Fac object

Description

Vectorize Fac object

Usage

```
fac_to_vect(Fac)
```

Arguments

Fac

Fac object from CMTF and ACMTF

Value

Vectorized Fac object

Examples

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))
Fac = list(A, B, C, D, E)
v = fac_to_vect(Fac)
```

FMS_cv

Compute Factor Match Score for two models.

Description

Compute Factor Match Score for two models.

Usage

```
FMS_cv(Fac1, Fac2, sharedMode = 1)
```

Arguments

Fac1 A list of matrices corresponding to found components per mode in model 1.

Fac2 A list of matrices corresponding to found components per mode in model 2.

sharedMode The shared mode that is excluded from FMS calculation.

24 FMS_random

Value

Scalar of FMS value

Examples

```
set.seed(123)

I = 10
J = 5
K = 3
df = array(rnorm(I*J*K), c(I,J,K))
datasets = list(df, df)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes)

model1 = acmtf_opt(Z, 1)

Fac1 = model1$Fac[1:3]
Fac2 = Fac1 # identical models for the purposes of demonstration
result = FMS_cv(Fac1, Fac2) # [1] 1
```

FMS_random

Compute Factor Match Score for two models.

Description

Compute Factor Match Score for two models.

Usage

```
FMS_random(Fac1, Fac2)
```

Arguments

Fac1 A list of matrices corresponding to found components per mode in model 1.

Fac2 A list of matrices corresponding to found components per mode in model 2.

Value

Scalar of FMS value

```
set.seed(123)

I = 10
J = 5
K = 3
df = array(rnorm(I*J*K), c(I,J,K))
```

Georgiou2025

```
datasets = list(df, df)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes)

model1 = acmtf_opt(Z, 1)

Fac1 = model1$Fac[1:3]
Fac2 = Fac1 # identical models for the purposes of demonstration
result = FMS_random(Fac1, Fac2) # [1] 1
```

Georgiou2025

Georgiou2025 Apical Periodontitis data

Description

The Georgiou longitudinal dataset as a three-dimensional array and a matrix, with subjects in mode 1, features in mode 2, and time in mode3.

Usage

Georgiou2025

Format

Georgiou2025:

A list object with two elements

Inflammatory_mediators Longitudinally measured inflammatory mediator data. **Tooth_microbiome** Single-timepoint tooth microbiome data of the extracted tooth

Source

TBD

initializeACMTF

Initialize input vectors for the ACMTF algorithm

Description

Initialize input vectors for the ACMTF algorithm

```
initializeACMTF(
   Z,
   numComponents,
   initialization = "random",
   output = "Fac",
   Y = NULL
)
```

26 initializeCMTF

Arguments

Z List object as generated by setupCMTFdata().

numComponents Integer stating the number of desired components for the CMTF model.

initialization Initialization method, either "random" or "nvec" (default "random"). Random will initialize random input vectors. Nvec will initialize vectors according to an singular value decomposition of the (matricized, if needed) concatenated datasets per mode.

output How to return output: as a "Fac" object (default) or vectorized ("vect").

Y Used as dependent variable when initialization is set to "npls". Not used by default.

Value

List or vector of initialized input vectors per mode.

Examples

```
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
init = initializeACMTF(Z, 2)
```

initializeCMTF

Initialize input vectors for the CMTF algorithm

Description

Initialize input vectors for the CMTF algorithm

```
initializeCMTF(
   Z,
   numComponents,
   initialization = "random",
   output = "Fac",
   Y = NULL
)
```

normalizeFac 27

Arguments

Z List object as generated by setupCMTFdata().

numComponents Integer stating the number of desired components for the CMTF model.

initialization Initialization method, either "random" or "nvec" (default "random"). Random will initialize random input vectors. Nvec will initialize vectors according to an singular value decomposition of the (matricized, if needed) concatenated datasets per mode.

output How to return output: as a "Fac" object (default) or vectorized ("vect").

Y Used as dependent variable when initialization is set to "npls". Not used by

default.

Value

List or vector of initialized input vectors per mode.

Examples

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
init = initializeCMTF(Z, 1)
```

normalizeFac

Normalize all vectors in model output Fac object to norm 1.

Description

Normalize all vectors in model output Fac object to norm 1.

Usage

```
normalizeFac(Fac, modes)
```

Arguments

Fac List object with all components per mode per item.

modes List object with modes per dataset (see also setupCMTFdata())

28 npred

Value

List object of normalized Fac object, the extracted norms per loading vector per component, and the norms per dataset per component.

Examples

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100, 2))
E = array(rnorm(10*2), c(10, 2))
modes = list(c(1,2,3), c(1,4,5))
Fac = list(A, B, C, D, E)
output = normalizeFac(Fac, modes)
```

npred

Predict Y for new data by projecting the data onto the latent space defined by an ACMTF-R model.

Description

Predict Y for new data by projecting the data onto the latent space defined by an ACMTF-R model.

Usage

```
npred(model, newX, Z, sharedMode = 1)
```

Arguments

model ACMTF-R model

newX List object of new data, where each element corresponds to a block

Z Original input data used for the model

sharedMode Shared mode between the blocks (default 1).

Value

Ypred: the predicted value of Y for the new data

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100, 2))
E = array(rnorm(10*2), c(10, 2))
```

reinflateFac 29

```
df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes)
Y = matrix(A[,1])
# Remove a sample and define
i = 1
Xtest = lapply(Z$object, function(x){x@data[i,,]})
Ytest = Y[i]
Xtrain = lapply(Z$object, function(x){x@data[-i,,]})
Ytrain = Y[-i]
Ztrain = setupCMTFdata(Xtrain, Z$modes)
model = acmtfr_opt(Ztrain,Ytrain,1,initialization="random",pi=1, nstart=1, max_iter=10)
Ypred = npred(model, Xtest, Ztrain, sharedMode=1)
```

reinflateFac

Reinflate all datablocks from a model Fac object.

Description

Basically a wrapper function for reinflateTensor() and reinflateMatrix().

Usage

```
reinflateFac(Fac, Z, returnAsTensor = FALSE)
```

Arguments

Fac object output from CMTF and ACMTF

Z object as generated by setupCMTFdata().

returnAsTensor Boolean to return data blocks as rTensor tensor objects (default FALSE)

Value

List of data blocks

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100, 2))
E = array(rnorm(10*2), c(100, 2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
```

30 reinflateTensor

```
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
result = cmtf_opt(Z, 1, max_iter=2)
Xhats = reinflateFac(result$Fac, Z)
```

reinflateMatrix

Create a matrix from a matrix of scores and loadings similar to a component model.

Description

Create a matrix from a matrix of scores and loadings similar to a component model.

Usage

```
reinflateMatrix(A, B)
```

Arguments

A I x N matrix corresponding to scores for N components.

B J x N matrix corresponding to loadings for N components.

Value

M, an I x J matrix.

Examples

```
A = rnorm(108)
B = rnorm(100)
M = reinflateMatrix(A,B)
```

reinflateTensor

Create a tensor out of a set of matrices similar to a component model.

Description

Create a tensor out of a set of matrices similar to a component model.

```
reinflateTensor(A, B, C)
```

removeTwoNormCol 31

Arguments

Α	x N matrix corresponding to loadings in the first mode for N components.	

B J x N matrix corresponding to loadings in the second mode for N components.

C K x N matrix corresponding to loadings in the third mode for N components.

Value

```
M, an I x J x K tensor.
```

Examples

```
A = rnorm(108)
B = rnorm(100)
C = rnorm(10)
M = reinflateTensor(A,B,C)
```

removeTwoNormCol

Remove two-norms column-wise from a matrix

Description

Remove two-norms column-wise from a matrix

Usage

```
removeTwoNormCol(df)
```

Arguments

df

Matrix of loadings

Value

Matrix of loadings where the column-wise 2-norm is 1.

```
A = array(rnorm(108*4), c(108,4))
Anorm = removeTwoNormCol(A)
```

32 setupCMTFdata

setu	nCMT	Fdata
3C Cu	PCIII	i data

Set up datasets for (A)CMTF input

Description

Set up datasets for (A)CMTF input

Usage

```
setupCMTFdata(datasets, modes, normalize = TRUE)
```

Arguments

List of arrays of datasets. Multi-way and two-way may be combined.

Numbered modes per dataset in a list. Example element 1: 1 2 3 and element 2: 1 4 for the X tensor and Y matrix case with a shared subject mode.

Boolean specifying if the datasets should be normalized to Frobenium norm 1.

Note: this function puts zeroes in positions with missing values. The indices of missing data are conserved in the output.

Value

Z, a list with "object" listing the datasets, "sizes" with their size, "norms" with their norms and "missing" stating the missing data.

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)
```

vect_to_fac 33

vect_to_fac	Convert vectorized output of (a)cmtf to a Fac list object with all loadings per mode.

Description

Convert vectorized output of (a)cmtf to a Fac list object with all loadings per mode.

Usage

```
vect_to_fac(vect, Z, sortComponents = FALSE)
```

Arguments

```
vect Vectorized output of (a)cmtf

Z Original Z input object (see setupCMTFdata).

sortComponents Sort the order of the components by variation explained (default FALSE).
```

Value

Fac: list object with all loadings in all components per mode, ordered the same way as Z\$modes.

```
set.seed(123)
A = array(rnorm(108*2), c(108, 2))
B = array(rnorm(100*2), c(100, 2))
C = array(rnorm(10*2), c(10, 2))
D = array(rnorm(100*2), c(100,2))
E = array(rnorm(10*2), c(10,2))

df1 = reinflateTensor(A, B, C)
df2 = reinflateTensor(A, D, E)
datasets = list(df1, df2)
modes = list(c(1,2,3), c(1,4,5))
Z = setupCMTFdata(datasets, modes, normalize=FALSE)

result = cmtf_opt(Z, 2, initialization="random", max_iter = 2)
Fac = vect_to_fac(result$par, Z)
```

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