# Package 'JoF'

October 12, 2022

Type Package

Version 0.1.0

Title Modelling and Simulating Judgments of Frequency

Maintainer Markus Burkhardt <markus.burkhardt@psychologie.tu-chemnitz.de></markus.burkhardt@psychologie.tu-chemnitz.de>
<b>Description</b> In a typical experiment for the intuitive judgment of frequencies (JoF) different stimuli with different frequencies are presented. The participants consider these stimuli with a constant duration and give a judgment of frequency. These judgments can be simulated by formal models: PASS 1 and PASS 2 based on Sedlmeier (2002, ISBN:978-0198508632), MIN-ERVA 2 based on Hintzman (1984) <doi:10.3758 bf03202365=""> and TODAM 2 based on Murdock, Smith &amp; Bai (2001) <doi:10.1006 jmps.2000.1339="">. The package provides an assessment of the frequency by determining the core aspects of these four models (attention, decay, and presented frequency) that can be compared to empirical results.</doi:10.1006></doi:10.3758>
<b>Depends</b> R (>= $3.1.0$ )
License GPL-3
Encoding UTF-8
LazyData true
RoxygenNote 7.0.2
Suggests testthat, knitr, rmarkdown
VignetteBuilder knitr
NeedsCompilation no
Author Markus Burkhardt [aut, cre]
Repository CRAN
<b>Date/Publication</b> 2020-04-03 14:10:36 UTC
R topics documented:
MINERVA2       2         PASS1       3         PASS2       5         plot.JoF       6         print.JoF       7         TODAM2       7

2 MINERVA2

Index 9

MINERVA2

Modeling Judgments of Frequency with MINERVA 2

#### **Description**

Modeling Judgments of Frequency with MINERVA 2

#### Usage

```
MINERVA2(x, y, ..., sqc, L, dec = NULL)
```

## **Arguments**

sqc

L

dec

x input handled by MINERVA 2. Values -1, 0 and 1 are allowed. -1 represents the absence of a feature, 0 the irrelevance of a feature and 1 the presence of a feature.

y another input handled by MINERVA 2. At least two inputs are needed for the simulation.

... other inputs for modeling.

sequence of the different objects. Each input gets an ascending number. x gets the value 1, y gets the value 2, ... gets the value 3 and so on. The argument sqc = c(1, 2, 3, 2) means: first input x is processed, second input y is processed followed by processing input number three and fourth, th input y is used again. So sqc contains the frequency information too. In c(1, 2, 3, 2), x and the third input are presented once. The input y is presented twice.

learning parameter. This is the proportion of a correctly stored vector. L = 1 means 100 % of the input is processed correctly. If L is a vector, each input could be handled differently. So L = c(.5, .6, .9) means, input x is correctly stored to 50 %, input y is stored to 60 % and the third input (inserted in . . .) is stored with 90 % probability.

decay is not part of the original version of MINERVA 2. This is just implemented for a better comparison with the other models of JoF. In dec = NULL, decay has no effect. For dec = 'curve' decay uses a forgetting curve. If dec is a numeric Vector e. g. dec = c(.8, .9, 1) the memory traces are weighted. The first represented trace is weighted by .8 the second by .9 and the youngest trace by 1. The value dec = 1 corresponds with the original model.

## **Details**

Calculations of MINERVA 2 contain four steps.

$$S_i = \frac{\sum_{j=1}^{N} P_j T_{ij}}{N_i}$$
$$A_i = S_i^3$$

PASS1 3

$$I = \sum_{i=1}^{M} A_i$$
 
$$relative JoF = \frac{I_j}{\sum_{i}^{K} I_j}$$

#### Value

MINERVA2 returns the relative judgment of frequency

#### References

Dougherty, M. R., Gettys, C. F., & Ogden, E. E. (1999). MINERVA-DM: A memory processes model for judgments of likelihood. Psychological Review, 106(1), 180.

Hintzman, D. L. (1984). MINERVA 2: A simulation model of human memory. Behavior Research Methods, Instruments, and Computers, 16, 96-101.

#### **Examples**

```
#This example is presented in Dougherty,
#Gettys, & Ogden, 1999 (p. 185)
H1 \leftarrow c(-1, 1, 0, 1, 0, -1, 1, -1, 0)
H2 \leftarrow c(-1, 0, 0, 1, 0, 0, 1, 0, 0)
x \leftarrow MINERVA2(H1, H2, sqc = c(2, 1), L = 1)
```

PASS1

Modeling Judgments of Frequency with PASS 1

## **Description**

Modeling Judgments of Frequency with PASS 1

## Usage

```
PASS1(x, y, ..., sqc, att, dec, ifc, rdm_weights = TRUE, noise = 0)
```

#### **Arguments**

X	input handled by	v PASS 1. Onl	v binarv i	nput is allowed.

a second binary input handled by PASS 1. At least two inputs are needed for the у simulation.

other binary inputs for modeling.

sequence of the different objects. Each input gets an ascending number. x gets sqc

the value 1, y gets the value 2, ... gets the value 3 and so on. The argument sqc = c(1, 2, 3, 2) means: first input x is processed, second input y is processed followed by processing input number three and fourth, th input y is used again. So sqc contains the frequency information too. In c(1, 2, 3, 2), x and the third

input are presented once. The input y is presented twice.

4 PASS1

att	attention is a vector with numeric values between 0 and 1. att has the same
	length like sqc, so each input processing have its own value and PASS 1 can
	modulate attention by time or input. If att is exact one numeric value (e.g. att
	= .1), all inputs get the same parameter of attention.

decay is a vector with numeric values between -1 and 0. dec has the same length as sqc, so each input processing have its own value and PASS 1 can modulate decay by time. If dec is exact one numeric value (e.g. dec = -.1), all inputs get the same parameter of decay.

interference is a vector with numeric values between -1 and 0. ifc must have

the same length as sqc. So each input processing have its own value and PASS 1 can modulate inference by time. If ifc is exact one numeric value (e.g. ifc =

-. 1), all inputs get the same parameter of inference.

rdm\_weights a logical value indicating whether random weights in the neural network are

used or not. If rdm\_weights = FALSE all network connections are zero at the

beginning.

noise a proportion between 0 and 1 which determine the number of randome activiated

inputunits (hihger numbers indicate higher noise).

#### **Details**

dec

ifc

PASS 1 is a simple neural pattern associator learning by delta rule.

Learning:

$$ifU_i andU_j are activated, then \Delta w_{ij} = \Theta_1(1 - w_{ij})$$

Interference:

$$ifeither U_i or U_j is activated, then \Delta w_{ij} = \Theta_2 * w_{ij}$$

Decay:

$$ifneither U_i nor U_i is activated, then \Delta w_{ij} = \Theta_3 * w_{ij}$$

## Value

PASS1 returns the relative judgment of frequency for each input.

#### References

Sedlmeier, P. (2002). Associative learning and frequency judgements: The PASS model. In P. Sedlmeier, T. Betsch (Eds.), *Etc.: Frequency processing and cognition* (pp. 137-152). New York: Oxford University Press.

## **Examples**

```
o1 <- c(1, 0, 0, 0)

o2 <- c(0, 1, 0, 0)

o3 <- c(0, 0, 1, 0)

o4 <- c(0, 0, 0, 1)

PASS1(o1, o2, o3, o4,

sqc = rep(1:4, 4:1), att = .1, dec = -.05,

ifc = -.025, rdm_weights = FALSE, noise = 0)
```

PASS2 5

PASS2

 $Modelling\ \textit{Judgments}\ of\ \textit{Frequency}\ with\ \textit{PASS}\ 2$ 

## **Description**

Modelling Judgments of Frequency with PASS 2

## Usage

```
PASS2(x, y, ..., sqc, att, n_output_units = "half", rdm_weights = F, noise = 0)
```

## **Arguments**

 ,	
x	input handled by PASS 2. Only binary input is allowed.
У	a second binary input handled by PASS 1. At least two inputs are needed for the simulation.
	other binary inputs for modeling.
sqc	sequence of the different objects. Each input gets an ascending number. $x$ gets the value 1, $y$ gets the value 2, gets the value 3 and so on. The argument sqc = $c(1, 2, 3, 2)$ means: first input $x$ is processed, second input $y$ is processed followed by processing input number three and fourth, th input $y$ is used again. So sqc contains the frequency information too. In $c(1, 2, 3, 2)$ , $x$ and the third input are presented once. The input $y$ is presented twice.
att	attention is a vector with numeric values between 0 and 1. att has the same length like sqc, so each input processing have its own value and PASS 1 can modulate attention by time or input. If att is exact one numeric value (e.g. att = .1), all inputs get the same parameter of attention.
n_output_units	number of output units as numeric value. This must be between 1 and the maximum number of input units. n_output_units = 'half' determines the half of the input units.
rdm_weights	a logical value indicating whether random weights in the neural network are used or not. If rdm_weights = FALSE all network connections are zero at the beginning.
noise	a proportion between $0$ and $1$ which determines the number of random activated

## **Details**

PASS 2 uses a competitive learning algorithm, which usually clusters the input as side effect. If weights are equal, the winning unit is chosen randomly, because of this, each simulation is slightly different.

input units (higher numbers indicate higher noise).

$$if an output un i O_i losses: \Delta w_{ij} = 0$$
 
$$if an output un i O_i wins: \Delta w_{ij} = g_w \frac{a_i}{\sum_i^n a_i} - g_w w_{ij}$$

plot.JoF

## Value

PASS2 returns the relative judgment of frequency for each input.

#### References

Sedlmeier, P. (2002). Associative learning and frequency judgements: The PASS model. In P. Sedlmeier, T. Betsch (Eds.), *Etc.: Frequency processing and cognition* (pp. 137-152). New York: Oxford University Press.

## **Examples**

```
o1 <- c(1, 0, 0, 0)

o2 <- c(0, 1, 0, 0)

o3 <- c(0, 0, 1, 0)

o4 <- c(0, 0, 0, 1)

PASS2(o1, o2, o3, o4,

    sqc = rep(1:4, 4:1), att = .1, n_output_units = 2,

    rdm_weights = FALSE, noise = 0)
```

plot.JoF

plot progress of judgment of frequency simulation

## **Description**

plot progress of judgment of frequency simulation

## Usage

```
## S3 method for class 'JoF'
plot(x, type = "1", ...)
```

## **Arguments**

```
x output of JoF simulation

type "1" for lines, "p" for points, "b" for both

further arguments
```

#### Value

Displays the judgment of frequency as proportion of all inputs

print.JoF 7

print.JoF

Output of judgment of frequecny simulation

## **Description**

Output of judgment of frequecny simulation

## Usage

```
## S3 method for class 'JoF'
print(x, ...)
```

## **Arguments**

x output of JoF simulation
... further arguments

## Value

Displays the judgment of frequency as proportion of all inputs

TODAM2

Modeling Judgments of Frequency with TODAM 2

## **Description**

Modeling Judgments of Frequency with TODAM 2

## Usage

```
TODAM2(x, y, ..., sqc, gamma = 1, alpha = 1)
```

## **Arguments**

sqc

Х	input handled by TODAM 2. Normal distributed inputs with mean $= 0$ and sd
	= 1 / n are allowed. This representation enables discrimination and similarity
	between different items. See vignette for details.

y another input handled by TODAM 2. At least two inputs are needed for the simulation.

... other inputs handled by TODAM 2.

sequence of the different objects. Each input gets an ascending number. x gets the value 1, y gets the value 2, ... gets the value 3 and so on. The argument sqc = c(1, 2, 3, 2) means: first input x is processed, second input y is processed followed by processing input number three and fourth, th input y is used again. So sqc contains the frequency information too. In c(1, 2, 3, 2), x and the third input are presented once. The input y is presented twice.

8 TODAM2

gamma is the attention- or learning parameter. Values between 0 and 1 are allowed. 1

represents perfect learning. If gamma its a vector, each input could be handled differently. So gamma = c(.5, .6, 1) means, the third input is stored correctly

and betther than the y better than first input x).

alpha represents the decay. If alpha = 1, the complete memory vector is used (and no

forgetting takes place). If alpha is an numeric Vector e. g. alpha = c(.8, .9, 1), the memory vector is weighted. The memory for the first input is weaker

than the second than the third.

#### **Details**

In the original publication TODAM 2 is more complex and has more parameters. Especially the design for the input is a concatenation between item and context. The normal distributed input has a mean = 0 and sd = 1/n. A pragmatic solution to make the models input comparable is to use a binary input like in PASS. There is no explicit argument for noise.

Convolution:

$$F_i^2 = \sum_{i=1}^{n} f_i * f_{m-i+1} and m = 2n - 1$$

Memory:

$$M_t = \alpha M_{t-1} + \gamma F_t^2$$

Correlation

$$R_m = \sum_{(i;j) \in S(m)} F_t^2 thereS(m)(i;j) |-(n-1)/2 \le i, j \le (n-1)/2 and i - j = m$$

## References

Murdock, B. B., Smith, D., & Bai, J. (2001). Judgments of frequency and recency in a distributed memory model. *Journal of Mathematical Psychology*, 45, 564–602. https://doi.org/10.1006/jmps.2000.1339

## **Examples**

```
o1 <- c(-0.27, -0.24, -0.24, 0.75)

o2 <- c(-0.06, -0.55, 0.66, -0.06)

o3 <- c(0.04, 0.57, -0.65, 0.04)

o4 <- c(0.73, -0.39, -0.20, -0.14)

TODAM2(o1, o2, o3, o4, gamma = rep(c(0.7, 0.8), 5), alpha = 0.95, sqc = rep(1:4, 4:1))
```

# **Index**

```
MINERVA2, 2

PASS1, 3

PASS2, 5

plot.JoF, 6

print.JoF, 7

TODAM2, 7
```