Package 'Silhouette'

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Title Proximity Measure Based Diagnostics for Standard, Soft, and

Type Package

```
Multi-Way Clustering
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Maintainer Shrikrishna Bhat K < skbhat.in@gmail.com>
Description Quantifies clustering quality by measuring both cohesion within clusters and separa-
      tion between clusters. Implements advanced silhouette width computations for diverse cluster-
      ing structures, including: simplified silhou-
      ette (Van der Laan et al., 2003) <doi:10.1080/0094965031000136012>, Probability of Alterna-
      tive Cluster normalization methods (Raymaek-
      ers & Rousseeuw, 2022) <doi:10.1080/10618600.2022.2050249>, fuzzy clustering and silhou-
      ette diagnostics using membership probabilities (Campello & Hr-
      uschka, 2006; Bhat & Kiruthika, 2024) <doi:10.1016/j.fss.2006.07.006>, <doi:10.1080/23737484.2024.2408534>, and mul
      way clustering extensions such as block and tensor clustering (Schep-
      ers et al., 2008; Bhat & Kiruthika, 2025) <doi:10.1007/s00357-008-9005-
      9>, <doi:10.21203/rs.3.rs-6973596/v1>. Provides tools for computation and visualiza-
      tion (Rousseeuw, 1987) <doi:10.1016/0377-0427(87)90125-7> to support robust and repro-
      ducible cluster diagnostics across standard, soft, and multi-way clustering settings.
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```

2 extSilhouette

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Contents

Index	Silhouette softSilhouette																																	. 1	0
extSilhouette			 - Cal	си	la	te .	<u> </u>	xte	ne	dec	l S	Sill	- ho	ие	ette	e V	Via	lth	ı fe	or	M	ul	ti-	W	ay	<i>c</i>	lu	ste	er.	in	g			-	

Description

Computes an extended silhouette width for multi-way clustering (e.g., biclustering, triclustering, or n-mode tensor clustering) by combining silhouette widths from a list of Silhouette objects, each representing one mode of clustering. The extended silhouette width is the weighted average of the average silhouette widths from each mode, weighted by the number of observations in each mode's silhouette analysis. The output is an object of class extSilhouette.

Usage

```
extSilhouette(sil_list, dim_names = NULL, print.summary = FALSE)
```

Arguments

sil_list	A list of objects of class "Silhouette", typically the output of Silhouette or softSilhouette, where each object represents the silhouette analysis for one mode of multi-way clustering (e.g., rows, columns, or other dimensions in biclustering or tensor clustering).
dim_names	An optional character vector of dimension names (e.g., $c("Rows", "Columns")$). If NULL, defaults to "Mode 1", "Mode 2", etc.
print.summary	Logical; if TRUE, prints a summary of the extended silhouette width and dimension table. Default is FALSE.

Details

The extended silhouette width is computed as:

$$ExS = \frac{\sum (n_i \cdot w_i)}{\sum n_i}$$

where n_i is the number of observations in mode i (derived from nrow(x\$widths)), and w_i is the average silhouette width for that mode (from x\$avg.width). Each Silhouette object in sil_list

extSilhouette 3

must contain a non-empty widths data frame and a numeric avg.width value. Modes with zero observations ($n_i = 0$) are not allowed, as they would result in an undefined weighted average. For consistency make sure all Silhouette objects derived from same method and arguments.

Value

A list of class "extSilhouette" with the following components:

ext sil width A numeric scalar representing the extended silhouette width.

dim_table A data frame with columns dimension (e.g., "Mode 1", "Mode 2"), n_obs (number of observations), and avg_sil_width (average silhouette width for each mode).

References

Schepers, J., Ceulemans, E., & Van Mechelen, I. (2008). Selecting among multi-mode partitioning models of different complexities: A comparison of four model selection criteria. *Journal of Classification*, 25(1), 67–85. doi:10.1007/s0035700890059

Bhat Kapu, S., & Kiruthika, C. (2025). Block Probabilistic Distance Clustering: A Unified Framework and Evaluation. PREPRINT (Version 1) available at Research Square. doi:10.21203/rs.3.rs-6973596/v1

See Also

```
Silhouette, softSilhouette
```

```
# Example using iris dataset with two modes
data(iris)
if (requireNamespace("blockcluster", quietly = TRUE)) {
 library(blockcluster)
 result <- coclusterContinuous(</pre>
    as.matrix(iris[, -5]),
    nbcocluster = c(3, 2)
 )
} else {
 message("Install 'blockcluster': install.packages('blockcluster')")
if (requireNamespace("blockcluster", quietly = TRUE)) {
 sil_mode1 <- softSilhouette(</pre>
   prob_matrix = result@rowposteriorprob,
   method = "pac")
 sil_mode2 <- softSilhouette(</pre>
    prob_matrix = result@colposteriorprob,
   method = "pac"
 # Extended silhouette
 ext_sil <- extSilhouette(list(sil_mode1, sil_mode2),print.summary = TRUE)</pre>
```

4 plotSilhouette

}

plotSilhouette

Plot Silhouette Analysis Results

Description

Creates a silhouette plot for visualizing the silhouette widths of clustering results, with bars colored by cluster and an optional summary of cluster statistics in legend.

Usage

```
plotSilhouette(x, label = FALSE, summary.legend = TRUE, grayscale = FALSE, ...)
```

Arguments

х	An object of class "Silhouette", typically the output of the Silhouette and softSilhouette function. Also supports objects classes eclust, hcut, pam, clara, fanny, or silhouette from cluster, factoextra packages. For these classes, explicitly call plotSilhouette() to generate the plot.
label	Logical; if TRUE, the x-axis is labeled with observation row indices from the input data and titled "Row Index". Defaults to FALSE.
summary.legend	Logical; if TRUE, prints a summary of average silhouette widths and sizes for each cluster in legend ("Cluster (Size): Width"). If FALSE, the legend shows only cluster numbers. Defaults to TRUE.
grayscale	Logical; if TRUE, the plot uses a grayscale color palette for clusters. If FALSE, uses the default or specified color palette. Defaults to FALSE.
• • •	Additional arguments passed to ggpar for customizing the plot (e.g., palette, legend).

Details

The Silhouette plot displays the silhouette width (sil_width) for each observation, grouped by cluster, with bars sorted by cluster and descending silhouette width. The summary.legend option adds cluster sizes and average silhouette widths to the legend.

This function replica of S3 method for objects of class "Silhouette", typically produced by the Silhouette or softSilhouette functions in this package. It also supports objects of the following classes, with silhouette information extracted from their respective component:

- "eclust": Produced by eclust from the factoextra package.
- "hcut": Produced by hcut from the factoextra package.
- "pam": Produced by pam from the **cluster** package.
- "clara": Produced by clara from the cluster package.

plotSilhouette 5

- "fanny": Produced by fanny from the **cluster** package.
- "silhouette": Produced by silhouette from the cluster package.

For these classes ("eclust", "hcut", "pam", "clara", "fanny", "silhouette"), users should explicitly call plotSilhouette() (e.g., plotSilhouette(pam_result)) to ensure the correct method is used, as the generic plot() may not dispatch to this function for these objects.

Value

A ggplot2 object representing the Silhouette plot.

References

Rousseeuw, P. J. (1987). Silhouettes: A graphical aid to the interpretation and validation of cluster analysis. *Journal of Computational and Applied Mathematics*, 20, 53–65. doi:10.1016/0377-0427(87)901257

See Also

Silhouette, softSilhouette, eclust, hcut, pam, clara, fanny, silhouette

```
data(iris)
# Crisp Silhouette with k-means
out <- kmeans(iris[, -5], 3)</pre>
if (requireNamespace("proxy", quietly = TRUE)) {
  library(proxy)
  dist <- dist(iris[, -5], out$centers)</pre>
  plot(Silhouette(dist))
#' # Fuzzy Silhouette with ppclust::fcm
if (requireNamespace("ppclust", quietly = TRUE)) {
  library(ppclust)
  out_fuzzy <- Silhouette(</pre>
    prox_matrix = "d",
    proximity_type = "dissimilarity",
    prob_matrix = "u",
    clust_fun = ppclust::fcm,
    x = iris[, 1:4],
    centers = 3,
    sort = TRUE
  plot(out_fuzzy, summary.legend = FALSE, grayscale = TRUE)
  message("Install 'ppclust': install.packages('ppclust')")
# Silhouette plot for pam clustering
if (requireNamespace("cluster", quietly = TRUE)) {
```

```
library(cluster)
 pam_result \leftarrow pam(iris[, 1:4], k = 3)
 plotSilhouette(pam_result)
}
# Silhouette plot for clara clustering
if (requireNamespace("cluster", quietly = TRUE)) {
 clara_result <- clara(iris[, 1:4], k = 3)</pre>
 plotSilhouette(clara_result)
}
# Silhouette plot for fanny clustering
if (requireNamespace("cluster", quietly = TRUE)) {
 fanny_result <- fanny(iris[, 1:4], k = 3)</pre>
 plotSilhouette(fanny_result)
}
# Example using base silhouette() object
if (requireNamespace("cluster", quietly = TRUE)) {
 sil <- silhouette(pam_result)</pre>
 plotSilhouette(sil)
}
# Silhouette plot for eclust clustering
if (requireNamespace("factoextra", quietly = TRUE)) {
 library(factoextra)
 eclust_result <- eclust(iris[, 1:4], "kmeans", k = 3, graph = FALSE)</pre>
 plotSilhouette(eclust_result)
}
# Silhouette plot for hcut clustering
if (requireNamespace("factoextra", quietly = TRUE)) {
 hcut_result <- hcut(iris[, 1:4], k = 3)</pre>
 plotSilhouette(hcut_result)
}
```

Silhouette

Calculate Silhouette Widths, Summary, and Plot for Clustering Results

Description

Computes the silhouette width for each observation based on clustering results, measuring how similar an observation is to its own cluster compared to nearest neighbor cluster. The silhouette width ranges from -1 to 1, where higher values indicate better cluster cohesion and separation.

Usage

```
Silhouette(
  prox_matrix,
```

```
proximity_type = c("dissimilarity", "similarity"),
 method = c("medoid", "pac"),
 prob_matrix = NULL,
  a = 2,
  sort = FALSE,
  print.summary = FALSE,
  clust_fun = NULL,
)
## S3 method for class 'Silhouette'
plot(x, label = FALSE, summary.legend = TRUE, grayscale = FALSE, ...)
## S3 method for class 'Silhouette'
summary(object, print.summary = TRUE, ...)
```

Arguments

prox_matrix

A numeric matrix where rows represent observations and columns represent proximity measures (e.g., distances or similarities) to clusters. Typically, this is a membership or dissimilarity matrix from clustering results. If clust_fun is provided, prox_matrix should be the name of the matrix component as a string (e.g., if clust_fun = fcm from **ppclust** package the prox_matrix = "d").

proximity_type Character string specifying the type of proximity measure in prox_matrix. Options are "similarity" (higher values indicate closer proximity) or "dissimilarity" (lower values indicate closer proximity). Defaults to "dissimilarity".

method

Character string specifying the silhouette calculation method. Options are "pac" (Probability of Alternative Cluster) or "medoid". Defaults to "medoid".

prob_matrix

A numeric matrix where rows represent observations and columns represent cluster membership probabilities, depending on prob_type). If clust_fun is provided, prob_matrix should be the name of the matrix component as a string (e.g., "u" for fcm). When not NULL, fuzzy silhouette width is calculated. Defaults to NULL for crisp silhouette.

а

Numeric value controlling the fuzzifier or weight scaling in fuzzy silhouette averaging. Higher values increase the emphasis on strong membership differences. Must be positive. Defaults to 2.

sort

Logical; if TRUE, sorts the output widths data frame by cluster and descending silhouette width. Defaults to FALSE.

print.summary

Logical; if TRUE, prints a summary table of average silhouette widths and sizes for each cluster. Defaults to TRUE.

clust_fun

Optional S3 or S4 function object or function as character string specifying a clustering function that produces the proximity measure matrix. For example, fcm or "fcm". If provided, prox_matrix must be the name of the matrix component in the clustering output (e.g., "d" for fcm when proximity_type = "dissimilarity"). Defaults to NULL.

Additional arguments passed to clust_fun, such as x, centers for fcm.

An object of class "Silhouette", typically the output of the Silhouette and Х softSilhouette function. Also supports objects classes eclust, hcut, pam, clara, fanny, or silhouette from cluster, factoextra packages. For these classes, explicitly call plotSilhouette() to generate the plot. label Logical; if TRUE, the x-axis is labeled with observation row indices from the input data and titled "Row Index". Defaults to FALSE. summary.legend Logical; if TRUE, prints a summary of average silhouette widths and sizes for each cluster in legend ("Cluster (Size): Width"). If FALSE, the legend shows only cluster numbers. Defaults to TRUE. Logical; if TRUE, the plot uses a grayscale color palette for clusters. If FALSE, grayscale uses the default or specified color palette. Defaults to FALSE. object An object of class "Silhouette", typically the output of the Silhouette and softSilhouette function.

Details

The Silhouette function implements the Simplified Silhouette method introduced by Van der Laan, Pollard, & Bryan (2003), which adapts and generalizes the classic silhouette method of Rousseeuw (1987).

Clustering quality is evaluated using a proximity matrix, denoted as $\Delta = [\delta_{ik}]_{n \times K}$ for dissimilarity measures or $\Delta' = [\delta'_{ik}]_{n \times K}$ for similarity measures. Here, $i = 1, \ldots, n$ indexes observations, and $k = 1, \ldots, K$ indexes clusters. δ_{ik} represents the dissimilarity (e.g., distance) between observation i and cluster k, while δ'_{ik} represents similarity values.

The silhouette width $S(x_i)$ for observation i depends on the proximity type:

For dissimilarity measures:

$$S(x_i) = \frac{\min_{k' \neq k} \delta_{ik'} - \delta_{ik}}{N(x_i)}$$

For **similarity** measures:

$$S(x_i) = \frac{\delta'_{ik} - \max_{k' \neq k} \delta'_{ik'}}{N(x_i)}$$

where $N(x_i)$ is a normalizing factor defined by the method.

Choice of method: The normalizer $N(x_i)$ is selected according to the method argument. The method names reference their origins but may be used with any proximity matrix, not exclusively certain clustering algorithms:

- For medoid (Van der Laan et al., 2003):
 - Dissimilarity: $\max(\delta_{ik}, \min_{k' \neq k} \delta_{ik'})$
 - Similarity: $\max(\delta'_{ik}, \max_{k'\neq k} \delta'_{ik'})$
- For pac (Raymaekers & Rousseeuw, 2022):
 - Dissimilarity: $\delta_{ik} + \min_{k' \neq k} \delta_{ik'}$
 - Similarity: $\delta'_{ik} + \max_{k' \neq k} \delta'_{ik'}$

Note: The "medoid" and "pac" options reflect the normalization formula—not a requirement to use the PAM algorithm or posterior/ensemble methods—and are general scoring approaches. These

methods can be applied to any suitable proximity matrix, including proximity, similarity, or dissimilarity matrices derived from **classification algorithms**. This flexibility means silhouette indices may be computed to assess group separation when clusters or groups are formed from classification-derived proximities, not only from unsupervised clustering.

If prob_matrix is NULL, the **crisp silhouette index** (CS) is:

$$CS = \frac{1}{n} \sum_{i=1}^{n} S(x_i)$$

summarizing overall clustering quality.

If prob_matrix is provided, denoted as $\Gamma = [\gamma_{ik}]_{n \times K}$, with γ_{ik} representing the probability of observation i belonging to cluster k, the **fuzzy silhouette index** (FS) is used:

$$FS = \frac{\sum_{i=1}^{n} (\gamma_{ik} - \max_{k' \neq k} \gamma_{ik'})^{\alpha} S(x_i)}{\sum_{i=1}^{n} (\gamma_{ik} - \max_{k' \neq k} \gamma_{ik'})^{\alpha}}$$

where α (the a argument) controls the emphasis on confident assignments.

Value

A data frame of class "Silhouette" containing cluster assignments, nearest neighbor clusters, silhouette widths for each observation, and weights (for fuzzy clustering). The object includes the following attributes:

proximity_type The proximity type used ("similarity" or "dissimilarity").
method The silhouette calculation method used ("medoid" or "pac").

Further, summary returns a list containing:

- clus.avg.widths: A named numeric vector of average silhouette widths per cluster.
- avg.width: The overall average silhouette width.
- sil.sum: A data frame with columns cluster, size, and avg.sil.width summarizing cluster sizes and average silhouette widths.

References

Rousseeuw, P. J. (1987). Silhouettes: A graphical aid to the interpretation and validation of cluster analysis. *Journal of Computational and Applied Mathematics*, 20, 53–65. doi:10.1016/0377-0427(87)901257

Van der Laan, M., Pollard, K., & Bryan, J. (2003). A new partitioning around medoids algorithm. Journal of Statistical Computation and Simulation, 73(8), 575–584. doi:10.1080/0094965031000136012

Campello, R. J., & Hruschka, E. R. (2006). A fuzzy extension of the silhouette width criterion for cluster analysis. *Fuzzy Sets and Systems*, 157(21), 2858–2875. doi:10.1016/j.fss.2006.07.006

Raymaekers, J., & Rousseeuw, P. J. (2022). Silhouettes and quasi residual plots for neural nets and tree-based classifiers. *Journal of Computational and Graphical Statistics*, 31(4), 1332–1343. doi:10.1080/10618600.2022.2050249

Bhat Kapu, S., & Kiruthika. (2024). Some density-based silhouette diagnostics for soft clustering algorithms. Communications in Statistics: Case Studies, Data Analysis and Applications, 10(3-4), 221-238. doi:10.1080/23737484.2024.2408534

See Also

softSilhouette, plotSilhouette

```
# Standard silhouette with k-means on iris dataset
data(iris)
# Crisp Silhouette with k-means
out <- kmeans(iris[, -5], 3)</pre>
if (requireNamespace("ppclust", quietly = TRUE)) {
  library(proxy)
  dist <- proxy::dist(iris[, -5], out$centers)</pre>
  silh_out <- Silhouette(dist,print.summary = TRUE)</pre>
  plot(silh_out)
} else {
  message("Install 'ppclust': install.packages('ppclust')")
# Scree plot for optimal clusters (2 to 7)
if (requireNamespace("ppclust", quietly = TRUE)) {
  library(ppclust)
  avg_sil_width <- numeric(6)</pre>
  for (k in 2:7) {
    out <- Silhouette(</pre>
      prox_matrix = "d",
      proximity_type = "dissimilarity",
      prob_matrix = "u",
      clust_fun = ppclust::fcm,
      x = iris[, 1:4],
      centers = k,
      sort = TRUE
    # Compute average silhouette width from widths
    avg_sil_width[k - 1] <- summary(out, print.summary = FALSE)$avg.width</pre>
  plot(avg_sil_width,
    type = "o",
    ylab = "Overall Silhouette Width",
    xlab = "Number of Clusters",
    main = "Scree Plot"
  )
} else {
  message("Install 'ppclust': install.packages('ppclust')")
```

Description

Computes silhouette widths for soft clustering results by interpreting cluster membership probabilities (or their transformations) as proximity measures. Although originally designed for evaluating clustering quality within a method, this adaptation allows heuristic comparison across soft clustering algorithms using average silhouette widths.

Usage

```
softSilhouette(
  prob_matrix,
  prob_type = c("pp", "nlpp", "pd"),
  method = c("pac", "medoid"),
  average = c("crisp", "fuzzy"),
  a = 2,
  print.summary = FALSE,
  clust_fun = NULL,
  ...
)
```

Arguments

prob_matrix

A numeric matrix where rows represent observations and columns represent cluster membership probabilities (or transformed probabilities, depending on prob_type). If clust_fun is provided, prob_matrix should be the name of the matrix component as a string (e.g., "u" for fcm).

prob_type

Character string specifying the type transformation of membership matrix considered as proximity matrix in prob_matrix. Options are:

"pp" Posterior probabilities $[\gamma_{ik}]_{n \times K}$ (non-negative, typically summing to 1 per row), treated as similarities

"nlpp" Negative log of posterior probabilities $[-\ln \gamma_{ik}]_{n\times K}$ (non-positive), treated as dissimilarities.

"pd" Probability distribution $[\gamma_{ik}/\pi_k]_{n\times K}$ (normalized posterior probabilities relative to cluster proportions π_k), treated as similarities.

Defaults to "pp".

method

Character string specifying the silhouette calculation method. Options are "pac" (Probability of Alternative Cluster) or "medoid". Defaults to "pac".

average

Character string specifying the type of average silhouette width calculation. Options are "crisp" (simple average) or "fuzzy" (weighted average based on membership differences). Defaults to "crisp".

а

Numeric value controlling the fuzzifier or weight scaling in fuzzy silhouette averaging. Higher values increase the emphasis on strong membership differences. Must be positive. Defaults to 2.

print.summary

Logical; if TRUE, prints a summary table of average silhouette widths and sizes for each cluster. Defaults to FALSE.

clust_fun

Optional S3 or S4 function object or function as character string specifying a clustering function that produces the proximity measure matrix. For example, fcm or "fcm". If provided, prox_matrix must be the name of the matrix component in the clustering output (e.g., "d" for fcm when proximity_type = "dissimilarity"). Defaults to NULL.

.. Additional arguments passed to clust_fun, such as x, centers for fcm.

Details

Although the silhouette method was originally developed for evaluating clustering structure within a single result, this implementation allows leveraging cluster membership probabilities from soft clustering methods to construct proximity-based silhouettes. These silhouette widths can be compared heuristically across different algorithms to assess clustering quality.

See doi:10.1080/23737484.2024.2408534 for more details.

Value

A data frame of class "Silhouette" containing cluster assignments, nearest neighbor clusters, silhouette widths for each observation, and weights (for fuzzy clustering). The object includes the following attributes:

```
proximity_type The proximity type used ("similarity" or "dissimilarity").
method The silhouette calculation method used ("medoid" or "pac").
```

References

Raymaekers, J., & Rousseeuw, P. J. (2022). Silhouettes and quasi residual plots for neural nets and tree-based classifiers. *Journal of Computational and Graphical Statistics*, 31(4), 1332–1343. doi:10.1080/10618600.2022.2050249

Bhat Kapu, S., & Kiruthika. (2024). Some density-based silhouette diagnostics for soft clustering algorithms. Communications in Statistics: Case Studies, Data Analysis and Applications, 10(3-4), 221-238. doi:10.1080/23737484.2024.2408534

See Also

Silhouette,plotSilhouette

```
# Compare two soft clustering algorithms using softSilhouett
# Example: FCM vs. FCM2 on iris data, using average silhouette width as a criterion
data(iris)
if (requireNamespace("ppclust", quietly = TRUE)) {
  fcm_result <- ppclust::fcm(iris[, 1:4], 3)
  out_fcm <- softSilhouette(prob_matrix = fcm_result$u,print.summary = TRUE)
  plot(out_fcm)
  sfcm <- summary(out_fcm, print.summary = FALSE)
} else {
  message("Install 'ppclust' to run this example: install.packages('ppclust')")
}</pre>
```

```
if (requireNamespace("ppclust", quietly = TRUE)) {
   fcm2_result <- ppclust::fcm2(iris[, 1:4], 3)
   out_fcm2 <- softSilhouette(prob_matrix = fcm2_result$u,print.summary = TRUE)
   plot(out_fcm2)
   sfcm2 <- summary(out_fcm2, print.summary = FALSE)
} else {
   message("Install 'ppclust' to run this example: install.packages('ppclust')")
}
# Compare average silhouette widths of fcm and fcm2
if (requireNamespace("ppclust", quietly = TRUE)) {
   cat("FCM average silhouette width:", sfcm$avg.width, "\n")
   cat("FCM2 average silhouette width:", sfcm2$avg.width, "\n")
}</pre>
```

Index

```
clara, 4, 5, 8
eclust, 4, 5, 8
extSilhouette, 2

fanny, 4, 5, 8
fcm, 7, 11, 12

ggpar, 4

hcut, 4, 5, 8
pam, 4, 5, 8
plot.Silhouette (Silhouette), 6
plotSilhouette, 4, 10, 12

Silhouette, 2-5, 6, 8, 12
silhouette, 4, 5, 8
softSilhouette, 2-5, 8, 10, 10
summary.Silhouette (Silhouette), 6
```