Package 'hdcate'

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Type Package

Title Estimation of Conditional Average Treatment Effects with High-Dimensional Data

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Imports KernSmooth, R6, hdm, locpol, caret

Description A two-step double-robust method to estimate the conditional average treatment effects (CATE) with potentially high-dimensional covariate(s). In the first stage, the nuisance functions necessary for identifying CATE are estimated by machine learning methods, allowing the number of covariates to be comparable to or larger than the sample size. The second stage consists of a low-dimensional local linear regression, reducing CATE to a function of the covariate(s) of interest. The CATE estimator implemented in this package not only allows for high-dimensional data, but also has the "double robustness" property: either the model for the propensity score or the models for the conditional means of the potential outcomes are allowed to be misspecified (but not both). This package is based on the paper by Fan et al., "Estimation of Conditional Average Treatment Effects With High-Dimensional Data" (2022), Journal of Business & Economic Statistics <doi:10.1080/07350015.2020.1811102>.

License GPL (>= 3)

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2 HDCATE

R topics documented:

	HDCATE	- 2
	HDCATE.fit	3
	HDCATE.get_sim_data	4
	HDCATE.inference	
	HDCATE.plot	6
	HDCATE.set_bw	7
	HDCATE.set_condition_var	
	HDCATE.set_first_stage	9
	HDCATE.unset_first_stage	11
	HDCATE.use_cross_fitting	12
	HDCATE.use_full_sample	13
Index		14

Description

HDCATE

Use a two-step procedure to estimate the conditional average treatment effects (CATE) with potentially high-dimensional covariate(s). Run browseVignettes('hdcate') to browse the user manual of this package.

High-Dimensional Conditional Average Treatment Effects (HDCATE)

Usage

```
HDCATE(data, y_name, d_name, x_formula)
```

Arguments

data	data frame of the observed data
y_name	variable name of the observed outcomes
d_name	variable name of the treatment indicators
x_formula	formula of the covariates

Estimator

Value

An initialized HDCATE model (object), ready for estimation.

HDCATE.fit 3

Examples

```
# get simulation data
n_obs <- 500 # Num of observations
n_var <- 100 # Num of observed variables
n rel var <- 4 # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)</pre>
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')</pre>
# for example, and alternatively, the propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')</pre>
# Example 1: full-sample estimator
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)</pre>
# estimate HDCATE function, inference, and plot
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)
HDCATE.inference(model)
HDCATE.plot(model)
# Example 2: cross-fitting estimator
# change above estimator to cross-fitting mode, 5 folds, for example.
HDCATE.use_cross_fitting(model, k_fold=5)
# estimate HDCATE function, inference, and plot
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)
HDCATE.inference(model)
HDCATE.plot(model)
```

HDCATE.fit

Fit the HDCATE function

Description

Fit the HDCATE function

Usage

```
HDCATE.fit(HDCATE_model, verbose = TRUE)
```

Arguments

```
HDCATE_model an object created via HDCATE

verbose whether the verbose message is displayed, the default is TRUE
```

Value

None. The HDCATE_model is fitted.

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)</pre>
```

HDCATE.get_sim_data

Get simulation data

Description

Get simulation data

Usage

```
HDCATE.get_sim_data(
    n_obs = 500,
    n_var = 100,
    n_rel_var = 4,
    sig_strength_propensity = 0.5,
    sig_strength_outcome = 1,
    intercept = 10
)
```

Arguments

n_obsNum of observationsn_varNum of covariates

HDCATE.inference 5

n_rel_var Num of relevant variables, only the first n_rel_var covariates are actually present

in the expectation function of potential outcome, and only the last n_rel_var

covariates are present in the propensity score function.

sig_strength_propensity

signal strength in propensity score functions

sig_strength_outcome

signal strength in outcome functions

intercept value of intercept in outcome functions

Value

a data.frame, which is the simulated observed data.

Examples

```
HDCATE.get_sim_data()
HDCATE.get_sim_data(n_obs=50, n_var=4, n_rel_var=2)
```

HDCATE.inference

Construct uniform confidence bands

Description

Construct uniform confidence bands

Usage

```
HDCATE.inference(
  HDCATE_model,
  sig_level = 0.01,
  n_rep_boot = 1000,
  verbose = FALSE
)
```

Arguments

HDCATE_model an object created via HDCATE

sig_level a (vector of) significant level, such as 0.01, or c(0.01, 0.05, 0.10)

n_rep_boot repeat n times for bootstrap, the default is 1000

verbose whether the verbose message is displayed, the default is FALSE

Value

None. The HDCATE confidence bands are constructed.

6 HDCATE.plot

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)

HDCATE.fit(model)
HDCATE.inference(model)</pre>
```

HDCATE.plot

Plot HDCATE function and the uniform confidence bands

Description

Plot HDCATE function and the uniform confidence bands

Usage

```
HDCATE.plot(
  HDCATE_model,
  output_pdf = FALSE,
  pdf_name = "hdcate_plot.pdf",
  include_band = TRUE,
  test_side = "both",
  y_axis_min = "auto",
  y_axis_max = "auto",
  display.hdcate = "HDCATEF",
  display.ate = "ATE",
  display.siglevel = "sig_level"
)
```

Arguments

```
HDCATE_model an object created via HDCATE

output_pdf if TRUE, the plot will be saved as a PDF file, the default is FALSE

pdf_name file name when output_pdf=TRUE
```

HDCATE.set_bw 7

include_band	if TRUE, plot the uniform confidence bands (need: HDCATE.inference was called before)			
test_side	'both', 'left' or 'right', i.e. 2-side test or one-side test			
y_axis_min	minimum value of the Y axis to plot in the graph, the default is auto			
y_axis_max	maximum value of the Y axis to plot in the graph, the default is auto			
${\tt display.hdcate}$	the name of HDCATE function in the legend, the default is 'HDCATEF'			
display.ate	the name of average treatment effect in the legend, the default is 'ATE'			
display.siglevel				
	the name of the significant level for confidence bands in the legend, the default			

is 'sig_level'

Value

None. A plot will be shown or saved as PDF.

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)
HDCATE.inference(model)
HDCATE.plot(model)</pre>
```

HDCATE.set_bw

Set bandwidth

Description

Set user-defined bandwidth.

Usage

```
HDCATE.set_bw(model, bandwidth = "default")
```

Arguments

model an object created via HDCATE bandwidth the value of bandwidth

Value

None.

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
# Set user-defined bandwidth, e.g., 0.15.
HDCATE.set_bw(model, 0.15)</pre>
```

HDCATE.set_condition_var

Set the conditional variable in CATE

Description

Set the conditional variable in CATE

Usage

```
HDCATE.set_condition_var(
  HDCATE_model,
  name = NA,
  min = NA,
  max = NA,
  step = NA
)
```

Arguments

```
HDCATE_model an object created via HDCATE

name name of the conditional variable

min minimum value of the conditional variable for evaluation

max maximum value of the conditional variable for evaluation

step minimum distance between two evaluation points
```

Value

None. The HDCATE_model is ready to fit.

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)</pre>
```

```
HDCATE.set_first_stage
```

Set user-defined first-stage estimating methods

Description

Set user-defined ML methods (such as random forests, elastic-net, boosting) to run the first-stage estimation.

Usage

```
HDCATE.set_first_stage(
  model,
  fit.treated,
  fit.untreated,
  fit.propensity,
  predict.treated,
  predict.untreated,
  predict.propensity
)
```

Arguments

fit.treated function that accepts a data.frame as the only argument, fits the treated expectation function, and returns a fitted object

fit.untreated function that accepts a data.frame as the only argument, fits the untreated expectation function, and returns a fitted object

fit prepared to function that accepts a data frame as the only argument, fits the prepared fits the prepared function.

fit.propensity function that accepts a data.frame as the only argument, fits the propensity function, and return a fitted object

predict.treated

function that accepts the returned object of fit.treated and a data.frame as arguments, and returns the predicted vector of that data.frame

predict.untreated

function that accepts the returned object of fit.untreated and a data.frame as arguments, and returns the predicted vector that data.frame

predict.propensity

function that accepts the returned object of fit.propensity and a data.frame as arguments, and returns the predicted vector that data.frame

Value

None.

```
# get simulation data
n_obs <- 500 # Num of observations
n_var <- 100 # Num of observed variables
n_rel_var <- 4 # Num of relevant variables</pre>
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)</pre>
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')</pre>
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')</pre>
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)</pre>
# manually define a lasso method
my_lasso_fit_exp <- function(df) {</pre>
  hdm::rlasso(as.formula(paste0('Y', "~", x_formula)), df)
my_lasso_predict_exp <- function(fitted_model, df) {</pre>
  predict(fitted_model, df)
my_lasso_fit_ps <- function(df) {</pre>
  hdm::rlassologit(as.formula(paste0('D', "~", x_formula)), df)
}
my_lasso_predict_ps <- function(fitted_model, df) {</pre>
  predict(fitted_model, df, type="response")
```

```
HDCATE.unset_first_stage
```

```
# Apply the "my-lasso" apporach to the first stage
HDCATE.set_first_stage(
  model,
  my_lasso_fit_exp,
  my_lasso_fit_exp,
  my_lasso_fit_exp,
  my_lasso_predict_exp,
  my_lasso_predict_exp,
  my_lasso_predict_exp,
  my_lasso_predict_ps
)
```

HDCATE.unset_first_stage

Clear the user-defined first-stage estimating methods

Description

Inverse operation of HDCATE.set_first_stage

Usage

```
HDCATE.unset_first_stage(model)
```

Arguments

model

an object created via HDCATE

Value

None.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
# ... manually set user-defined first-stage estimating methods via `HDCATE.set_first_stage`</pre>
```

Clear those user-defined methods and use the built-in method HDCATE.unset_first_stage(model)

```
HDCATE.use_cross_fitting
```

Use k-fold cross-fitting estimator

Description

Use k-fold cross-fitting estimator

Usage

```
HDCATE.use_cross_fitting(model, k_fold = 5, folds = NULL)
```

Arguments

model an object created via HDCATE

k_fold number of folds

folds you can manually set the folds, should be a list of index vector

Value

None.

```
# get simulation data
n_obs <- 500 # Num of observations
n_var <- 100 # Num of observed variables
n_rel_var <- 4 # Num of relevant variables</pre>
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)</pre>
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')</pre>
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')</pre>
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)</pre>
# for example, use 5-fold cross-fitting estimator
\label{eq:hdcate} \mbox{\sc HDCATE.use\_cross\_fitting(model, k\_fold=5)}
# alternatively, pass a list of index vector to the third argument to set the folds manually,
# in this case, the second argument k_fold is auto detected, you can pass any value to it.
HDCATE.use_cross_fitting(model, k_fold=2, folds=list(c(1:250), c(251:500)))
```

```
HDCATE.use_full_sample
```

Use full-sample estimator

Description

This is the default mode when creating a model via HDCATE

Usage

```
HDCATE.use_full_sample(model)
```

Arguments

model

an object created via HDCATE

Value

None.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.use_full_sample(model)</pre>
```

Index

```
HDCATE, 2, 3, 5, 6, 8–13
HDCATE.fit, 3
HDCATE.get_sim_data, 4
HDCATE.inference, 5, 7
HDCATE.plot, 6
HDCATE.set_bw, 7
HDCATE.set_condition_var, 8
HDCATE.set_first_stage, 9, 11
HDCATE.unset_first_stage, 11
HDCATE.use_cross_fitting, 12
HDCATE.use_full_sample, 13
```