

# Package ‘RSDC’

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**Title** Regime-Switching Dynamic Correlation Models

**Version** 1.1-2

**Description** Estimation, forecasting, simulation, and portfolio construction for regime-switching models with exogenous variables as in Pelletier (2006) <[doi:10.1016/j.jeconom.2005.01.013](https://doi.org/10.1016/j.jeconom.2005.01.013)>.

**License** GPL-3

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**BugReports** <https://github.com/ArdiaD/RSDC/issues>

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greenbrown	<i>Green vs Brown portfolio dataset</i>
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**Description**

Daily returns for a green and a brown portfolios constructed following the equal-weighted 10-90 percentile approach.

**Usage**

```
data(greenbrown)
```

**Format**

- A data frame with 2266 rows and three columns:
- DATE** Dates ranging from 2014-01-02 to 2024-12-30.
- return\_green** Numeric returns for the green portfolio.
- return\_brown** Numeric returns for the brown portfolio.

**Source**

Originally data in inst/extdata/green-brown-ptf.xlsx.

**Examples**

```
data("greenbrown")
str(greenbrown)
head(greenbrown)
```

## Description

The **RSDC** package provides a comprehensive framework for modeling, estimating, and forecasting correlation structures in multivariate time series under regime-switching dynamics. It supports both fixed transition probabilities and *time-varying transition probabilities* (TVTP) driven by exogenous variables.

The methodology is particularly suited to empirical asset pricing and portfolio management applications, enabling users to incorporate macroeconomic, financial, or climate-related predictors into the regime dynamics. The package integrates the full workflow — from model estimation to covariance matrix reconstruction and portfolio optimization — in a single, reproducible pipeline.

## Main Features

- **Model estimation and filtering:** `rsdc_hamilton` (Hamilton filter), `rsdc_likelihood` (likelihood computation), `rsdc_estimate` (parameter estimation).
- **Correlation and covariance forecasting:** `rsdc_forecast`.
- **Portfolio construction:** `rsdc_minvar` (minimum-variance portfolios), `rsdc_maxdiv` (maximum-diversification portfolios).
- **Simulation:** `rsdc_simulate` (simulate TVTP regime-switching series).

## Authors

David Ardia and Benjamin Seguin

## References

- Engle RF (2002). “Dynamic conditional correlation: A simple class of multivariate generalized autoregressive conditional heteroskedasticity models.” *Journal of Business & Economic Statistics*, **20**(3), 339–350. doi:10.1198/073500102288618487.
- Hamilton JD (1989). “A New Approach to the Economic Analysis of Nonstationary Time Series and the Business Cycle.” *Econometrica*, **57**(2), 357–384. doi:10.2307/1912559.
- Pelletier D (2006). “Regime switching for dynamic correlations.” *Journal of Econometrics*, **131**(1-2), 445–473. doi:10.1016/j.jeconom.2005.01.004.

rsdc\_estimate

*Estimate Regime-Switching or Constant Correlation Model (Wrapper)***Description**

Unified front-end that dispatches to one of three estimators:

- `f_optim()` — TVTP specification (`method = "tvtp"`).
- `f_optim_noX()` — fixed transition matrix (`method = "noX"`).
- `f_optim_const()` — constant correlation, single regime (`method = "const"`).

**Usage**

```
rsdc_estimate(
  method = c("tvtp", "noX", "const"),
  residuals,
  N = 2,
  X = NULL,
  out_of_sample = FALSE,
  control = list()
)
```

**Arguments**

<code>method</code>	Character. One of "tvtp", "noX", "const".
<code>residuals</code>	Numeric matrix $T \times K$ . Typically standardized residuals/returns.
<code>N</code>	Integer. Number of regimes. Ignored when <code>method = "const"</code> .
<code>X</code>	Numeric matrix $T \times p$ of exogenous covariates (required for "tvtp").
<code>out_of_sample</code>	Logical. If TRUE, a fixed 70/30 split is applied prior to estimation.
<code>control</code>	Optional list. Currently forwards <code>do_trace = FALSE</code> and <code>seed = 123</code> to the back-ends.

**Details**

- **Method selection:** `match.arg()` validates `method`.
- **Inputs:** "tvtp" requires non-NULL `X`; `N` is ignored for "const".
- **Split:** If `out_of_sample = TRUE`, the first 70\

**Value**

`transition_matrix` Estimated transition matrix ( $1 \times 1$  for "const").

`correlations` Regime lower-triangular correlations.

`covariances` Array of full correlation matrices.

`log_likelihood` Maximized log-likelihood.

`beta` TVTP coefficients (only for "tvtp").

## References

Mullen K, Ardia D, Gil D, Windover D, Ulrich J (2011). "DEoptim: An R Package for Global Optimization by Differential Evolution." *Journal of Statistical Software*, **40**(6), 1–26. doi:[10.18637/jss.v040.i06](https://doi.org/10.18637/jss.v040.i06).

Hamilton JD (1989). "A New Approach to the Economic Analysis of Nonstationary Time Series and the Business Cycle." *Econometrica*, **57**(2), 357–384. doi:[10.2307/1912559](https://doi.org/10.2307/1912559).

Pelletier D (2006). "Regime switching for dynamic correlations." *Journal of Econometrics*, **131**(1–2), 445–473. doi:[10.1016/j.jeconom.2005.01.004](https://doi.org/10.1016/j.jeconom.2005.01.004).

## See Also

[rsdc\\_hamilton](#) and [rsdc\\_likelihoood](#).

## Examples

```
y <- scale(matrix(rnorm(100 * 3), 100, 3))
rsdc_estimate("const", residuals = y)
rsdc_estimate("noX", residuals = y, N = 2)
X <- cbind(1, scale(seq_len(nrow(y))))
rsdc_estimate("tvtp", residuals = y, N = 2, X = X)
```

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rsdc\_forecast

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Forecast Covariance/Correlation Paths from an RSDC Model

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## Description

Generates per-period correlation and covariance matrices from a fitted model: "const" (constant correlation), "noX" (fixed transition matrix), or "tvtp" (time-varying transition probabilities).

## Usage

```
rsdc_forecast(
  method = c("tvtp", "noX", "const"),
  N,
  residuals,
  X = NULL,
  final_params,
  sigma_matrix,
  value_cols,
  out_of_sample = FALSE,
  control = list()
)
```

## Arguments

method	Character. One of "tvtp", "noX", "const".
N	Integer. Number of regimes (ignored for "const").
residuals	Numeric matrix $T \times K$ used to compute correlations or run the filter.
X	Optional numeric matrix $T \times p$ (required for "tvtp").
final_params	List with fitted parameters (e.g., from <a href="#">rsdc_estimate</a> ): must include correlations, and either transition_matrix ("noX") or beta ("tvtp"); include log_likelihood for BIC computation.
sigma_matrix	Numeric matrix $T \times K$ of forecasted standard deviations.
value_cols	Character/integer vector of columns in sigma_matrix that define asset order.
out_of_sample	Logical. If TRUE, use a fixed 70/30 split; otherwise use the whole sample.
control	Optional list; supports threshold (in (0,1), default 0.7).

## Details

- **Forecast horizon:** If out\_of\_sample = TRUE, filter on the first threshold fraction and forecast on the remainder.
- **Correlation paths:**
  - "const" — empirical correlation of residuals, repeated across time.
  - "noX"/"tvtp" — smoothed-probability weighted average of regime correlations.
- **Covariance build:** Reconstruct  $R_t$  from the pairwise vector (columns ordered by `combn(K, 2)`), set  $D_t = \text{diag}(\sigma_{t,1}, \dots, \sigma_{t,K})$ , and  $\Sigma_t = D_t R_t D_t$ .
- **BIC:** Parameter count  $k$  is  $N * \text{ncol}(X) + N * K * (K - 1) / 2$  for "tvtp",  $N * (N - 1) + N * K * (K - 1) / 2$  for "noX", and  $K * (K - 1) / 2$  for "const".

## Value

smoothed\_probs  $N \times T^*$  smoothed probabilities ("noX"/"tvtp" only).

sigma\_matrix  $T^* \times K$  slice aligned to the forecast horizon.

cov\_matrices List of  $K \times K$  covariance matrices  $\Sigma_t = D_t R_t D_t$ .

predicted\_correlations  $T^* \times \binom{K}{2}$  pairwise correlations in `combn(K, 2)` order.

BIC Bayesian Information Criterion  $\text{BIC} = \log(n) k - 2 \ell$ .

y  $T^* \times K$  residual matrix aligned to the forecast horizon.

## See Also

[rsdc\\_hamilton](#), [rsdc\\_estimate](#), [rsdc\\_minvar](#), [rsdc\\_maxdiv](#)

## Examples

```
set.seed(123)
T <- 60; K <- 3; N <- 2
y <- scale(matrix(rnorm(T*K), T, K))
vols <- matrix(0.2 + 0.05*abs(sin(seq_len(T)/7)), T, K)
rho <- rbind(c(0.10, 0.05, 0.00), c(0.60, 0.40, 0.30))
Pfix <- matrix(c(0.9, 0.1, 0.2, 0.8), 2, 2, byrow = TRUE)
rsdc_forecast("noX", N, y, NULL,
              list(correlations = rho, transition_matrix = Pfix, log_likelihood = -200),
              vols, 1:K)
```

rsdc\_hamilton

*Hamilton Filter (Fixed P or TVTP)*

## Description

Runs the Hamilton (1989) filter for a multivariate regime-switching *correlation* model. Supports either a fixed (time-invariant) transition matrix  $P$  or time-varying transition probabilities (TVTP) built from exogenous covariates  $X$  via a logistic link. Returns filtered/smoothed regime probabilities and the log-likelihood.

## Usage

```
rsdc_hamilton(y, X = NULL, beta = NULL, rho_matrix, K, N, P = NULL)
```

## Arguments

$y$	Numeric matrix $T \times K$ of observations (e.g., standardized residuals/returns). Columns are treated as mean-zero with unit variance; only the correlation structure is modeled.
$X$	Optional numeric matrix $T \times p$ of covariates for TVTP. Required if $\beta$ is supplied.
$\beta$	Optional numeric matrix $N \times p$ . TVTP coefficients; row $i$ governs persistence of regime $i$ via $\text{plogis}(X[t, ] \%*\% \beta[i, ])$ .
$\text{rho\_matrix}$	Numeric matrix $N \times C$ of regime correlation parameters, where $C = K(K - 1)/2$ . Each row is the lower-triangular part (by <code>lower.tri</code> ) of a regime's correlation matrix.
$K$	Integer. Number of observed series (columns of $y$ ).
$N$	Integer. Number of regimes.
$P$	Optional $N \times N$ fixed transition matrix. Used only when $X$ or $\beta$ is <code>NULL</code> .

## Details

- **Correlation rebuild:** For regime  $m$ , a correlation matrix  $R_m$  is reconstructed from `rho_matrix[m, ]` (lower-triangular fill + symmetrization). Non-PD proposals are penalized.
- **Transition dynamics:**
  - *Fixed P:* If  $X$  or  $\beta$  is missing, a constant  $P$  is used (user-provided via `P`; otherwise uniform  $1/N$  rows).
  - *TVTP:* With  $X$  and  $\beta$ , diagonal entries use `plogis(X[t, ] %*% beta[i, ])`. Off-diagonals are equal and sum to  $1 - p_{ii,t}$ . For  $N = 1$ ,  $P_t = [1]$ .
- **Numerical safeguards:** A small ridge is added before inversion; if filtering degenerates at a time step, `log_likelihood = -Inf` is returned.

## Value

A list with:

**filtered\_probs**  $N \times T$  matrix of filtered probabilities  $\Pr(S_t = j \mid \Omega_t)$ .

**smoothed\_probs**  $N \times T$  matrix of smoothed probabilities  $\Pr(S_t = j \mid \Omega_T)$ .

**log\_likelihood** Scalar log-likelihood of the model given  $y$ .

## Note

TVTP uses a logistic link on the diagonal; off-diagonals are equal by construction.

## References

Hamilton JD (1989). “A New Approach to the Economic Analysis of Nonstationary Time Series and the Business Cycle.” *Econometrica*, **57**(2), 357–384. doi:[10.2307/1912559](https://doi.org/10.2307/1912559).

## See Also

[rsdc\\_likelihood](#) and [rsdc\\_estimate](#).

## Examples

```
set.seed(1)
T <- 50; K <- 3; N <- 2
y <- scale(matrix(rnorm(T * K), T, K), center = TRUE, scale = TRUE)

# Example rho: two regimes with different average correlations
rho <- rbind(c(0.10, 0.05, 0.00),
             c(0.60, 0.40, 0.30)) # lower-tri order for K=3

# Fixed-P filtering
Pfix <- matrix(c(0.9, 0.1,
                 0.2, 0.8), nrow = 2, byrow = TRUE)
out_fix <- rsdc_hamilton(y = y, X = NULL, beta = NULL,
                       rho_matrix = rho, K = K, N = N, P = Pfix)
str(out_fix$filtered_probs)
```



```
# TVTP filtering (include an intercept yourself)
X <- cbind(1, scale(seq_len(T)))
beta <- rbind(c(1.2, 0.0),
              c(0.8, -0.1))
out_tvtp <- rsdc_hamilton(y = y, X = X, beta = beta,
                        rho_matrix = rho, K = K, N = N)
out_tvtp$log_likelihood
```

rsdc\_likelihood

*Negative Log-Likelihood for Regime-Switching Correlation Models*

## Description

Computes the negative log-likelihood for a multivariate *correlation-only* regime-switching model, with either a fixed (time-invariant) transition matrix or time-varying transition probabilities (TVTP) driven by exogenous covariates. Likelihood evaluation uses the Hamilton (1989) filter.

## Usage

```
rsdc_likelihood(params, y, exog = NULL, K, N)
```

## Arguments

params	Numeric vector of model parameters packed as: <ul style="list-style-type: none"> <li>• <b>No exogenous covariates</b> (exog = NULL): first <math>N(N - 1)</math> transition parameters (for the fixed transition matrix), followed by <math>N \times K(K - 1)/2</math> correlation parameters, stacked <i>row-wise by regime</i> in lower.tri order.</li> <li>• <b>With exogenous covariates</b> (exog provided): first <math>N \times p</math> TVTP coefficients (beta, row <math>i</math> corresponds to regime <math>i</math>), followed by <math>N \times K(K - 1)/2</math> correlation parameters, stacked <i>row-wise by regime</i> in lower.tri order.</li> </ul>
y	Numeric matrix $T \times K$ of observations (e.g., standardized residuals). Columns are treated as mean-zero, unit-variance; only correlation is modeled.
exog	Optional numeric matrix $T \times p$ of exogenous covariates. If supplied, a TVTP specification is used.
K	Integer. Number of observed series (columns of y).
N	Integer. Number of regimes.

## Details

### • Transition dynamics:

- *Fixed P* (no exog): params begins with transition parameters. For  $N = 2$ , the implementation maps them to  $P = \begin{pmatrix} p_{11} & 1 - p_{11} \\ 1 - p_{22} & p_{22} \end{pmatrix}$ .
- *TVTP*: with exog, diagonal persistence is  $p_{ii,t} = \text{logit}^{-1}(X_t^\top \beta_i)$ ; off-diagonals are equal and sum to  $1 - p_{ii,t}$ .

- **Correlation build:** per regime, the lower-triangular vector is filled into a symmetric correlation matrix. Non-positive-definite proposals or  $|\rho| \geq 1$  are penalized via a large objective value.
- **Evaluation:** delegates to `rsdc_hamilton`; if the filter returns `log_likelihood = -Inf`, a large penalty is returned.

## Value

Numeric scalar: the *negative* log-likelihood to be minimized by an optimizer.

## Note

The function is written for use inside optimizers; it performs inexpensive validation and returns large penalties for invalid parameterizations instead of stopping with errors.

## See Also

`rsdc_hamilton` (filter), `optim`, and `DEoptim`

## Examples

```
# Small toy example (N = 2, K = 3), fixed P (no exog)
set.seed(1)
T <- 40; K <- 3; N <- 2
y <- scale(matrix(rnorm(T * K), T, K), center = TRUE, scale = TRUE)

# Pack parameters: trans (p11, p22), then rho by regime (lower-tri order)
p11 <- 0.9; p22 <- 0.8
rho1 <- c(0.10, 0.05, 0.00) # (2,1), (3,1), (3,2)
rho2 <- c(0.60, 0.40, 0.30)
params <- c(p11, p22, rho1, rho2)

nll <- rsdc_likelihood(params, y = y, exog = NULL, K = K, N = N)
nll

# TVTP example: add X and beta (pack beta row-wise, then rho)
X <- cbind(1, scale(seq_len(T)))
beta <- rbind(c(1.2, 0.0),
              c(0.8, -0.1))
params_tvtp <- c(as.vector(t(beta)), rho1, rho2)
nll_tvtp <- rsdc_likelihood(params_tvtp, y = y, exog = X, K = K, N = N)
nll_tvtp
```

---

rsdc_maxdiv	<i>Maximum-Diversification Portfolio (Rolling Weights)</i>
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### Description

Computes rolling maximum-diversification (MaxDiv) portfolio weights from a sequence of per-period covariance matrices implied by forecasted volatilities and correlations. Falls back to equal weights if the nonlinear solver fails.

### Usage

```
rsdc_maxdiv(sigma_matrix, value_cols, predicted_corr, y, long_only = TRUE)
```

### Arguments

sigma_matrix	Numeric matrix $T \times K$ of forecasted standard deviations.
value_cols	Character/integer vector naming columns in sigma_matrix (asset order).
predicted_corr	Numeric matrix $T \times \binom{K}{2}$ of pairwise correlations in combn(K, 2) column order.
y	Numeric matrix $T \times K$ of asset returns (for realized stats).
long_only	Logical. If TRUE, impose $w \geq 0$ and $\sum_i w_i = 1$ ; otherwise bounds are $-1 \leq w_i \leq 1$ with $\sum_i w_i = 1$ .

### Details

- **Covariance build:** For each  $t$ , reconstruct  $R_t$  from the pairwise vector; set  $D_t = \text{diag}(\sigma_{t,1}, \dots, \sigma_{t,K})$  and  $\Sigma_t = D_t R_t D_t$ .
- **Objective (MaxDiv):** maximize  $\text{DR}(w) = \frac{\sum_i w_i \sigma_{t,i}}{\sqrt{w^\top \Sigma_t w}}$  subject to  $\sum_i w_i = 1$  and bounds on  $w$ . Implemented by minimizing the negative ratio.
- **Solver:** Rsolnp::solnp with equality  $\sum_i w_i = 1$  and bounds by long\_only; on error, weights default to  $1/K$ .

### Value

weights  $T \times K$  matrix of weights.  
 returns Vector of realized portfolio returns  $\text{sum}(y[t,] * \text{weights}[t,])$ .  
 diversification\_ratios Vector of realized diversification ratios.  
 mean\_diversification Average diversification ratio.  
 K Number of assets.  
 assets Asset names.  
 volatility Standard deviation of realized portfolio returns.

### See Also

[rsdc\\_minvar](#), [solnp](#)

## Examples

```
# Toy example with K = 3
if (requireNamespace("Rsolnp", quietly = TRUE)) {
  T <- 50; K <- 3
  set.seed(42)
  vols <- matrix(0.2 + 0.05*abs(sin(seq_len(T)/7)), T, K)
  colnames(vols) <- paste0("A", 1:K)
  # simple, stationary correlations (order: (2,1), (3,1), (3,2))
  pred_corr <- cbind(rep(0.20, T), rep(0.10, T), rep(0.05, T))
  rets <- matrix(rnorm(T*K, sd = 0.01), T, K); colnames(rets) <- colnames(vols)

  mx <- rsdc_maxdiv(sigma_matrix = vols,
                    value_cols   = colnames(vols),
                    predicted_corr = pred_corr,
                    y             = rets,
                    long_only     = TRUE)

  head(mx$weights)
  mx$mean_diversification
}
```

---

rsdc\_minvar

*Minimum-Variance Portfolio (Rolling Weights)*


---

## Description

Computes rolling minimum-variance (MV) portfolio weights from a sequence of per-period covariance matrices implied by forecasted volatilities and pairwise correlations. Supports long-only or unconstrained MV. If the QP solver fails at a time step, the routine falls back to equal weights.

## Usage

```
rsdc_minvar(sigma_matrix, value_cols, predicted_corr, y, long_only = TRUE)
```

## Arguments

sigma_matrix	Numeric matrix $T \times K$ of forecasted <i>volatilities</i> (standard deviations), one column per asset.
value_cols	Character or integer vector giving the columns in sigma_matrix to use as assets (order defines the asset order).
predicted_corr	Numeric matrix $T \times P$ of pairwise correlations, where $P = \binom{K}{2}$ and the columns correspond to <code>combn(K, 2)</code> order.
y	Numeric matrix $T \times K$ of asset returns aligned with sigma_matrix. Used only to compute the realized portfolio volatility.
long_only	Logical. If TRUE (default), imposes long-only MV with the full-investment constraint $\sum_i w_i = 1$ and $w_i \geq 0$ . If FALSE, solves unconstrained MV with only $\sum_i w_i = 1$ .

## Details

- **Covariance build:** For each  $t$ , a correlation matrix  $R_t$  is reconstructed ... Let  $D_t = \text{diag}(\sigma_{t,1}, \dots, \sigma_{t,K})$  and  $\Sigma_t = D_t R_t D_t$ .
- **Optimization:** Minimize  $\frac{1}{2} w^\top \Sigma_t w$  subject to  $\mathbf{1}^\top w = 1$  and, if `long_only`,  $w \geq 0$  (solved with `quadprog::solve.QP`).
- **Failure handling:** If the QP fails at time  $t$ , weights default to equal allocation ( $w_i = 1/K$ ).

## Value

An object of class "minvar\_portfolio":

**weights**  $T \times K$  matrix of MV weights (one row per time).

**cov\_matrices** List of length  $T$  with the per-period  $K \times K$  covariance matrices.

**volatility** Realized standard deviation of portfolio returns (see Note on units).

**y** The input y matrix (coerced to  $T \times K$ ).

**K** Number of assets.

## Note on units

The realized portfolio return at time  $t$  is computed as  $\text{sum}(y[t, ] * \text{weights}[t, ]) / 100$ . This assumes y is expressed in % remove the / 100 in the implementation or convert inputs accordingly.

## See Also

[rsdc\\_maxdiv](#) (maximum diversification), [solve.QP](#)

## Examples

```
# Toy example with K = 3
T <- 50; K <- 3
set.seed(42)
vols <- matrix(0.2 + 0.05*abs(sin(seq_len(T)/7)), T, K)
colnames(vols) <- paste0("A", 1:K)
# simple, stationary correlations
pred_corr <- cbind(rep(0.20, T), rep(0.10, T), rep(0.05, T)) # order: (2,1), (3,1), (3,2)
rets <- matrix(rnorm(T*K, sd = 0.01), T, K); colnames(rets) <- colnames(vols)

mv <- rsdc_minvar(sigma_matrix = vols,
                  value_cols   = colnames(vols),
                  predicted_corr= pred_corr,
                  y             = rets,
                  long_only     = TRUE)

head(mv$weights)
mv$volatility
```

rsdc\_simulate

Simulate Multivariate Regime-Switching Data (TVTP)

**Description**

Simulates a multivariate time series from a regime-switching model with *time-varying transition probabilities* (TVTP) driven by covariates  $X$ . Transition probabilities are generated via a multinomial logistic (softmax) link; observations are drawn from regime-specific Gaussian distributions.

**Usage**

```
rsdc_simulate(n, X, beta, mu, sigma, N, seed = NULL)
```

**Arguments**

<code>n</code>	Integer. Number of time steps to simulate.
<code>X</code>	Numeric matrix $n \times p$ of covariates used to form the transition probabilities. Row $X[t, ]$ corresponds to covariates available at time $t$ . Only rows 1:(n-1) are used to transition from $t-1$ to $t$ .
<code>beta</code>	Numeric array $N \times N \times p$ . Softmax coefficients for the multinomial transition model; $\text{beta}[i, j, ]$ parameterizes the transition from state $i$ to state $j$ .
<code>mu</code>	Numeric matrix $N \times K$ . Regime-specific mean vectors.
<code>sigma</code>	Numeric array $K \times K \times N$ . Regime-specific covariance (here, correlation/variance) matrices; each $K \times K$ slice must be symmetric positive definite.
<code>N</code>	Integer. Number of regimes.
<code>seed</code>	Optional integer. If supplied, sets the RNG seed for reproducibility.

**Details**

- **Initial state and first draw:** The initial regime  $S_1$  is sampled uniformly; the first observation  $y_1$  is drawn from  $\mathcal{N}(\mu_{S_1}, \Sigma_{S_1})$ .
- **TVTP via softmax:** For  $t \geq 2$ , the row  $i$  of  $P_t$  is

$$P_t(i, j) = \frac{\exp(X_{t-1}^\top \beta_{i,j})}{\sum_{h=1}^N \exp(X_{t-1}^\top \beta_{i,h})},$$

computed with log-sum-exp stabilization.

- **Sampling:** Given  $S_{t-1}$ , draw  $S_t$  from the categorical distribution with probabilities  $P_t(S_{t-1}, \cdot)$  and  $y_t \sim \mathcal{N}(\mu_{S_t}, \Sigma_{S_t})$ .

**Value**

A list with:

**states** Integer vector of length  $n$ ; the simulated regime index at each time.

**observations** Numeric matrix  $n \times K$ ; the simulated observations.

**transition\_matrices** Array  $N \times N \times n$ ; the transition matrix  $P_t$  used at each time step (with  $P_1$  undefined by construction; see Details).

**Note**

Requires **mvtnorm** for multivariate normal sampling (called as `mvtnorm::rmvnorm`).

**See Also**

[rsdc\\_hamilton](#) (filter/evaluation), [rsdc\\_estimate](#) (estimators), [rsdc\\_forecast](#) (forecasting)

**Examples**

```
set.seed(123)
n <- 200; K <- 3; N <- 2; p <- 2
X <- cbind(1, scale(seq_len(n)))

beta <- array(0, dim = c(N, N, p))
beta[1, 1, ] <- c(1.2, 0.0)
beta[2, 2, ] <- c(1.0, -0.1)

mu <- rbind(c(0, 0, 0),
            c(0, 0, 0))
rho <- rbind(c(0.10, 0.05, 0.00),
            c(0.60, 0.40, 0.30))
Sig <- array(0, dim = c(K, K, N))
for (m in 1:N) {
  R <- diag(K); R[lower.tri(R)] <- rho[m, ]; R[upper.tri(R)] <- t(R)[upper.tri(R)]
  Sig[, , m] <- R
}
sim <- rsdc_simulate(n = n, X = X, beta = beta, mu = mu, sigma = Sig, N = N, seed = 99)
```

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