Package 'm2r'

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```
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Description Persistent interface to 'Macaulay2' <a href="http://www.math.uiuc.edu/Macaulay2/">http://www.math.uiuc.edu/Macaulay2/</a>
      and front-end tools facilitating its use in the 'R' ecosystem. For details see
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```

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 $\verb"enter_m2"$

Enter a Macaulay2 session

Description

Enter a Macaulay2 session

Usage

```
enter_m2(port = 27436L, timeout = 10)
```

Arguments

port port for Macaulay2 socket

timeout number of seconds before aborting

Value

TRUE invisibly

factor_n 3

Examples

```
## Not run: requires Macaulay2 be installed and an interactive session
enter_m2()
# m2 code below
1 + 1
a = 1
R = QQ[t,x,y,z]
I = ideal(t^4 - x, t^3 - y, t^2 - z)
gens gb I
exit
# back in R, the variable persists using m2()
m2("I")
\# we can also define variables in R that persist in m2
m2("b = 5")
enter_m2()
exit
## End(Not run)
```

factor_n

Factor an integer into primes

Description

Factor an integer into primes

Usage

```
factor_n(n, code = FALSE, ...)
factor_n.(n, code = FALSE, ...)
```

Arguments

```
n an integer or a polynomial code return only the M2 code? (default: FALSE)
```

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Value

a data frame with integer columns prime and power or m2_pointer referencing the factorization in M2.

```
## Not run: requires Macaulay2
##### basic usage
2^2 * 3^7 * 5^2 # = 218700
factor_n(218700)
factor_n.(218700)
(df <- factor_n(218700))
df$prime
df$power
str(df)
factor_n(218700, code = TRUE)
##### other options
(integer_pointer <- m2.("218700"))</pre>
m2_name(integer_pointer)
factor_n(integer_pointer, code = TRUE)
factor_n(integer_pointer)
factor_n(3234432540)
factor_n(323443254223453)
factor_n(rpois(1, 1e4))
##### known issues
# R doesn't handle big ints well. note in the following
# the m2 code number is different than the supplied number
factor_n(32344325422364353453, code = TRUE)
# this can be circumvented by passing a string instead
factor_n("32344325422364353453", code = TRUE)
# but if the factors are large, R can't handle the parsing well
factor_n("32344325422364353453")
```

factor_poly 5

```
# here's a workaround:
factor_pointer <- factor_n.("32344325422364353453")</pre>
m2_meta(factor_pointer, "ext_str")
extract_factors <- function(pointer) {</pre>
  require(stringr)
  str <- m2_meta(pointer, "ext_str")</pre>
  str <- str_sub(str, 19, -2)
  str <- str_extract_all(str, "\\{[0-9]+,[0-9]+\\}")[[1]]</pre>
  str <- str_sub(str, 2, -2)
  str <- str_split(str, ",")</pre>
  df <- as.data.frame(t(simplify2array(str)))</pre>
  names(df) <- c("prime", "power")</pre>
}
(df <- extract_factors(factor_pointer))</pre>
# using gmp (currently broken)
# factor_n("32344325422364353453", gmp = TRUE)
m2("11 * 479 * 6138607975396537")
11 * 479 * 6138607975396537
## End(Not run)
```

factor_poly

Factor a polynomial

Description

Factor a polynomial

Usage

```
factor_poly(mpoly, code = FALSE)
factor_poly.(mpoly, code = FALSE, ...)
```

Arguments

```
mpoly a character parseable by mp(), an mpoly object, or a pointer to a polynomial in M2

code return only the M2 code? (default: FALSE)

...
```

Value

a named list with elements factor (an mpolyList object) and power, an integer vector

6 gb

Examples

```
## Not run: requires Macaulay2 be installed and an interactive session
##### basic usage
ring("x", "y", coefring = "QQ")
factor_poly("x^4 - y^4")
# reference function
factor_poly.("x^4 - y^4")
##### different inputs
# factor_poly accepts mpoly objects:
# remember you must create the ring first!
(p \leftarrow mp("x^4 - y^4"))
factor_poly.(p)
factor_poly(p)
mp("(x-y) (x+y) (x^2+y^2)")
##### other examples
ring("x", "y", "z", coefring = "QQ")
(p \leftarrow mp("(x^2 - y) (x^2 + y) (x + y)^2 (x - z)^2"))
factor_poly.(p)
factor_poly(p)
(p \leftarrow mp("(x-1)^3 (y-1)^3"))
factor_poly.(p)
factor_poly(p)
## End(Not run)
```

Compute a Grobner basis with Macaulay2

Description

gb

Compute a Grobner basis with Macaulay2

gb

Usage

```
gb(..., control = list(), raw_chars = FALSE, code = FALSE)
gb.(..., control = list(), raw_chars = FALSE, code = FALSE)
gb_(x, control = list(), raw_chars = FALSE, code = FALSE, ...)
gb_.(x, control = list(), raw_chars = FALSE, code = FALSE, ...)
```

Arguments

... ...

control a list of options, see examples

raw_chars if TRUE, the character vector will not be parsed by mp(), saving time (default:

FALSE). the down-side is that the strings must be formated for M2 use directly,

as opposed to for mp(). (e.g. "x*y+3" instead of "x y + 3")

code return only the M2 code? (default: FALSE)

x a character vector of polynomials to be parsed by mp(), a mpolyList object, an

ideal() or pointer to an ideal

Details

gb uses nonstandard evaluation; gb_ is the standard evaluation equivalent.

Value

an mpolyList object of class m2_grobner_basis or a m2_grobner_basis_pointer pointing to the same. See mpolyList().

See Also

```
mp(), use_ring()
```

gb

```
##### different versions of gb
# standard evaluation version
poly\_chars <- c("t^4 - x", "t^3 - y", "t^2 - z")
gb_(poly_chars)
# reference nonstandard evaluation version
gb.("t^4 - x", "t^3 - y", "t^2 - z")
# reference standard evaluation version
gb_.(poly_chars)
##### different inputs to gb
# ideals can be passed to gb
I \leftarrow ideal("t^4 - x", "t^3 - y", "t^2 - z")
gb_(I)
# note that gb() works here, too, since there is only one input
gb(I)
# ideal pointers can be passed to gb
I. \leftarrow ideal.("t^4 - x", "t^3 - y", "t^2 - z")
gb_(I.)
# setting raw_chars is a bit faster, because it doesn't use ideal()
gb("t^4 - x", "t^3 - y", "t^2 - z", raw_chars = TRUE, code = TRUE)
gb("t^4 - x", "t^3 - y", "t^2 - z", raw_chars = TRUE)
##### more advanced usage
# the control argument accepts a named list with additional
# options
gb_(
 c("t^4 - x", "t^3 - y", "t^2 - z"),
 control = list(StopWithMinimalGenerators = TRUE),
 code = TRUE
)
gb_(
 c("t^4 - x", "t^3 - y", "t^2 - z"),
 control = list(StopWithMinimalGenerators = TRUE)
```

End(Not run)

ideal

Create a new ideal in Macaulay2

Description

Create a new ideal in Macaulay2

Usage

```
ideal(..., raw_chars = FALSE, code = FALSE)
ideal.(..., raw_chars = FALSE, code = FALSE)
ideal_(x, raw_chars = FALSE, code = FALSE, ...)
ideal_.(x, raw_chars = FALSE, code = FALSE, ...)
## S3 method for class 'm2_ideal'
print(x, ...)
## S3 method for class 'm2_ideal_list'
print(x, ...)
radical(ideal, ring, code = FALSE, ...)
```

```
saturate(I, J, code = FALSE, ...)

saturate.(I, J, code = FALSE, ...)

quotient(I, J, code = FALSE, ...)

quotient.(I, J, code = FALSE, ...)

primary_decomposition(ideal, code = FALSE, ...)

primary_decomposition.(ideal, code = FALSE, ...)

dimension(ideal, code = FALSE, ...)

## S3 method for class 'm2_ideal'
e1 + e2

## S3 method for class 'm2_ideal'
e1 * e2

## S3 method for class 'm2_ideal'
e1 == e2

## S3 method for class 'm2_ideal'
e1 == e2
```

Arguments

raw_chars

if TRUE, the character vector will not be parsed by mp(), saving time (default: FALSE). the down-side is that the strings must be formated for M2 use directly, as opposed to for mp(). (e.g. "x*y+3" instead of "x y + 3")

code

return only the M2 code? (default: FALSE)

x

a listing of polynomials. several formats are accepted, see examples.

ideal

an ideal object of class m2_ideal or m2_ideal_pointer

ring

the referent ring in Macaulay2

I, J

ideals or objects parsable into ideals

e1, e2

ideals for arithmetic

Value

a reference to a Macaulay2 ideal

```
## Not run: requires Macaulay2
##### basic usage
ring("x", "y", coefring = "QQ")
ideal("x + y", "x^2 + y^2")
##### different versions of gb
# standard evaluation version
poly_chars <- c("x + y", "x^2 + y^2")
ideal_(poly_chars)
# reference nonstandard evaluation version
ideal.("x + y", "x^2 + y^2")
# reference standard evaluation version
ideal_.(poly_chars)
##### different inputs to gb
ideal_( c("x + y", "x^2 + y^2"))
ideal_(mp(c("x + y", "x^2 + y^2")))
ideal_(list("x + y", "x^2 + y^2"))
##### predicate functions
I <- ideal ("x + y", "x^2 + y^2")
I. <- ideal.("x + y", "x^2 + y^2")
is.m2_ideal(I)
is.m2_ideal(I.)
is.m2_ideal_pointer(I)
is.m2_ideal_pointer(I.)
##### ideal radical
I \leftarrow ideal("(x^2 + 1)^2 y", "y + 1")
radical(I)
radical.(I)
```

```
##### ideal dimension
I \leftarrow ideal_(c("(x^2 + 1)^2 y", "y + 1"))
dimension(I)
# dimension of a line
ring("x", "y", coefring = "QQ")
I <- ideal("y - (x+1)")
dimension(I)
# dimension of a plane
ring("x", "y", "z", coefring = "QQ")
I \leftarrow ideal("z - (x+y+1)")
dimension(I)
##### ideal quotients and saturation
ring("x", "y", "z", coefring = "QQ")
(I <- ideal("x^2", "y^4", "z + 1"))
(J \leftarrow ideal("x^6"))
quotient(I, J)
quotient.(I, J)
saturate(I)
saturate.(I)
saturate(I, J)
saturate(I, mp("x"))
saturate(I, "x")
ring("x", "y", coefring = "QQ")
saturate(ideal("x y"), "x^2")
# saturation removes parts of varieties
# solution over R is x = -1, 0, 1
ring("x", coefring = "QQ")
I \leftarrow ideal("(x-1) x (x+1)")
saturate(I, "x") # remove x = 0 from solution
ideal("(x-1) (x+1)")
##### primary decomposition
```

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```
ring("x", "y", "z", coefring = "QQ")
I \leftarrow ideal("(x^2 + 1) (x^2 + 2)", "y + 1")
primary_decomposition(I)
primary_decomposition.(I)
I \leftarrow ideal("x (x + 1)", "y")
primary_decomposition(I)
# variety = z axis union x-y plane
(I \leftarrow ideal("x z", "y z"))
dimension(I) # = max dimension of irreducible components
(Is <- primary_decomposition(I))</pre>
dimension(Is)
##### ideal arithmetic
ring("x", "y", "z", coefring = "RR")
# sums (cox et al., 184)
(I <- ideal("x^2 + y"))
(J <- ideal("z"))
I + J
# products (cox et al., 185)
(I \leftarrow ideal("x", "y"))
(J <- ideal("z"))
I * J
# equality
(I <- ideal("x", "y"))
(J \leftarrow ideal("z"))
I == J
I == I
# powers
(I <- ideal("x", "y"))
I^3
## End(Not run)
```

Macaulay2 object tests

Description

is

Predicate functions for Macaulay2 objects.

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```
Usage
```

```
is.m2(x)
   is.m2_pointer(x)
   is.ring(x)
   is.m2_polynomialring(x)
   is.m2_polynomialring_pointer(x)
   is.m2_grobner_basis(x)
   is.m2_ideal(x)
   is.m2_ideal_pointer(x)
   is.m2_ideal_list(x)
   is.m2_ideal_list_pointer(x)
   is.m2_module(x)
   is.m2_option(x)
   is.m2_matrix(x)
   is.m2_matrix_pointer(x)
   is.m2_list(x)
   is.m2_array(x)
   is.m2_sequence(x)
Arguments
                   an object
Value
   logical(1)
Examples
   ## Not run: requires Macaulay2
```

R <- ring(c("x1", "x2", "x3"))

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```
is.m2(R)
is.ring(R)
is.ring(10)
is.ring(mp("x+1"))
## End(Not run)
```

LLL

LLL algorithm

Description

Macaulay2's implementation of the LLL algorithm. This implementation is still under development and is currently untested.

Usage

```
LLL(mat, control = list(), code = FALSE)
LLL.(mat, control = list(), code = FALSE)
```

Arguments

mat a matrix (integer entries)

control additional arguments to pass to LLL; see examples

code return only the M2 code? (default: FALSE)

Value

```
an object of class m2_matrix
```

See Also

```
m2_matrix()
```

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```
0, 1, 0, 0,
  0, 0, 1, 0,
 0, 0, 0, 1
), nrow = 6, byrow = TRUE)
LLL(M)
# example 2 (wikipedia)
M <- matrix(c(</pre>
 1, -1, 3,
 1, 0, 5,
 1, 2, 6
), nrow = 3, byrow = TRUE)
LLL(M)
##### control
M <- matrix(c(
 1, 1, 1, 1,
  2, 0, 3, 4,
  1, 0, 0, 0,
  0, 1, 0, 0,
  0, 0, 1, 0,
  0, 0, 0, 1
), nrow = 6, byrow = TRUE)
LLL(M, code = TRUE)
LLL(M, control = list(Strategy = "NTL"), code = TRUE)
LLL(M, control = list(Strategy = c("BKZ", "RealFP")), code = TRUE)
LLL(M)
LLL(M, control = list(Strategy = "NTL"))
LLL(M, control = list(Strategy = c("BKZ", "RealFP")))
LLL(M, control = list(Strategy = c("BKZ", "RealQP")))
# method timings with microbenchmark. note they are roughly the same
# for this example matrix
microbenchmark::microbenchmark(
  "NTL" = LLL(M, control = list(Strategy = "NTL")),
  "BKZ_RealFP" = LLL(M, control = list(Strategy = c("BKZ", "RealFP"))),
  "BKZ_RealQP" = LLL(M, control = list(Strategy = c("BKZ", "RealQP"))),
  "BKZ_RealRR" = LLL(M, control = list(Strategy = c("BKZ", "RealRR")))
)
```

m2r

m2r

Macaulay2 in R

Description

m2r provides a persistent interface to Macaulay2 (http://www.math.uiuc.edu/Macaulay2/) and front-end tools facilitating its use in the R ecosystem. For details, see vignette("m2r").

References

D. Kahle, C. O'Neill, and J. Sommars (2020). "A Computer Algebra System for R: Macaulay2 and the m2r Package." Journal of Statistical Software, 93(9):1-31.

m2_call

Call and reset a Macaulay2 process

Description

Call and reset a Macaulay2 process

Usage

```
m2r_version_number()
m2r_cloud_url()
has_m2_connection()
start_m2(
  port = 27436L,
  timeout = 10,
  attempts = 10,
  cloud = FALSE,
```

m2_call

```
hostname = m2r_cloud_url()
)
stop_m2()
reset_m2(
  port = 27436L,
  timeout = 10,
  attempts = 10,
  hostname = "ec2-52-10-66-241.us-west-2.compute.amazonaws.com"
)
m2(code, timeout = -1)
m2.(code, timeout = -1)
## S3 method for class 'm2_pointer'
print(x, ...)
```

Arguments

port port for Macaulay2 socket

timeout number of seconds before aborting

attempts numer of times to try to make connection

cloud use a cloud?

hostname the remote host to connect to; defaults to the Amazon EC2 instance

code Macaulay2 code

x formal argument for print method

Value

m2 return value

```
## Not run: requires Macaulay2

m2("1 + 1")
m2.("1 + 1")

m2("factor 32004")

# run a chunk of m2 code, only pulling the end value back into R
m2("
    R = QQ[a..d]
    I = ideal(a^3-b^2*c, b*c^2-c*d^2, c^3)
```

m2_matrix

```
G = gens gb I
# illustrate the persistent connection
m2("a = 1 + 1")
m2("a")
reset_m2()
m2("a")
# forcing a cloud start
if(has_m2_connection()) stop_m2()
start_m2(cloud = TRUE)
m2("1 + 1")
stop_m2()
m2.("peek(QQ[x,y,z])")
m2("peek(QQ[x,y,z])")
# m2 returns in its ext_str position the result of running
\# toExternalString on the return value of the chunk of code
\mbox{\#} you run. in principle, to
ExternalString provides the code
# needed to recreate the m2 object of interest. however,
# does not work for all objects representable in the m2 language.
# in particular, mutable objects are not supported.
# this is what happens when you look at those:
m2.("new MutableList from {1,2,3}")
m2("new MutableList from {1,2,3}")
## End(Not run)
```

m2_matrix

Create a new matrix in Macaulay2

Description

Create a new matrix in Macaulay2

Usage

```
m2_matrix(mat, ring, name, code = FALSE)
m2_matrix.(mat, ring, name, code = FALSE)
m2_numrows(x, code = FALSE, ...)
m2_numcols(x, code = FALSE, ...)
```

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```
m2_length(x, code = FALSE, ...)
## S3 method for class 'm2_matrix'
print(x, ...)
## S3 method for class 'm2_image'
print(x, ...)

m2_kernel(mat, name, code = FALSE)

m2_kernel.(mat, name, code = FALSE)
```

Arguments

mat a matrix

ring a ring containing the matrix entries

name the m2_name of the object, which is it's name on the M2 side

code return only the M2 code? (default: FALSE)

x formal argument for print method

...

Value

an object of class m2_matrix

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```
# the above is an mpoly problem, not a m2r problem
# mpoly does not have a data structure for matrices (as of 12/2016)
mat_chars <- sapply(m2_matrix(mat), print, silent = TRUE)
dim(mat_chars) <- c(2, 3)
mat_chars

m2_numrows(mat)
m2_numcols(mat)
m2_parse(mat)

(mat <- m2_matrix(matrix(c(1,2),nrow=1)))
m2_kernel(mat)

## End(Not run)</pre>
```

m2_parser

Convert a M2 object into an R object

Description

Convert a M2 object into an R object

Usage

```
m2_parse(s)
## S3 method for class 'm2_integer'
print(x, ...)
## S3 method for class 'm2_float'
print(x, ...)
## S3 method for class 'm2_complex'
print(x, ...)
## S3 method for class 'm2_string'
print(x, ...)
## S3 method for class 'm2_boolean'
print(x, ...)
## S3 method for class 'm2_list'
print(x, ...)
## S3 method for class 'm2_list'
print(x, ...)
```

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```
print(x, ...)
## S3 method for class 'm2_sequence'
print(x, ...)
## S3 method for class 'm2_symbol'
print(x, ...)
## S3 method for class 'm2_option'
print(x, ...)
## S3 method for class 'm2_hashtable'
print(x, ...)
## S3 method for class 'm2_module'
print(x, ...)
## S3 method for class 'm2_module'
print(x, ...)
```

Arguments

s a character(1), typically the result of running toExternalString on an M2 object
x an object to be printed

Value

an R object

References

D. Kahle, C. O'Neill, and J. Sommars (2020). "A Computer Algebra System for R: Macaulay2 and the m2r Package." Journal of Statistical Software, 93(9):1-31.

```
## Not run: requires Macaulay2

m2("1+1")
m2.("1+1")
m2_parse(m2.("1+1"))

m2("QQ[x,y]")
m2.("QQ[x,y]")
m2_parse(m2.("QQ[x,y]"))
get_m2_gmp()
```

m2_path

```
m2("3/2") %>% m2_parse()
m2_toggle_gmp() # gmp on
m2("3/2") %>% m2_parse()
m2("6/4") %>% m2_parse()
m2("3345234524352435432/223454325235432524352433245") %>% m2_parse()
m2_toggle_gmp() # gmp off

m2("50!") %>% m2_parse()
m2_toggle_gmp() # gmp on
m2("50!") %>% m2_parse()
m2_toggle_gmp() # gmp off

## End(Not run)
```

m2_path

Set path to Macaulay2 (M2)

Description

These are helper functions that deal with pathing to Macaulay2 and asking if it is present. When the Macaulay2 package is loaded it attempts to find the Macaulay2 executable by looking for an environment variable indicating where it is, i.e. its path as specified in your .Renviron file.

Usage

```
set_m2_path(path = NULL)
get_m2_path()
get_m2_connection()
get_m2_con()
get_m2_procid()
get_m2_port()
```

Arguments

path

A character string, the path to M2

Details

For easiest use, you'll want to specify the path the Macaulay2 executable in your ~/.Renviron file. It should look something like

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```
M2=/Applications/Macaulay2-1.10/bin
```

You can set this permanently with edit_r_environ(). Note that absolute paths should be specified, not relative paths, e.g. don't use ~/path/to/exe.

You can change this for the current session using set_m2_path(), which accepts a character string or, if missing, uses file.choose() to let you interactively; you just select an arbitrary executable.

On Windows, m2r just defaults to the cloud implementation. Local M2 instances are not currently supported on Windows.

Value

An invisible character string, the path found. More importantly, the function has the side effect of setting the global m2r option "m2 path"

Author(s)

David Kahle <david@kahle.com>

```
## Not run: requires Macaulay2
getOption("m2r")
get_m2_path()
set_m2_path()
## each of these functions can be used statically as well
(m2_path <- get_m2_path())</pre>
set_m2_path("/path/to/m2/directory")
get_m2_path()
set_m2_path(m2_path) # undoes example
# if you'd like to use the cloud, after you library(m2r)
# and before you use m2() type
set_m2_path(NULL)
# alternatively, if you have already been using m2, do:
stop_m2()
set_m2_path(NULL)
m2("1+1")
## End(Not run)
```

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m2_utility

Utility tools for M2

Description

Utility tools for M2

Usage

```
m2_name(x)
m2_name(x) <- value
m2_meta(x, m2_attr)
m2_meta(x, m2_attr) <- value
m2_structure(x = NA, m2_name, m2_class, m2_meta, base_class)
m2_exists(name)
m2_ls(all.names = FALSE)
m2_rm(name)
m2_getwd()</pre>
```

Arguments

х	an object of class m2
value	the value to assign
m2_attr	the name of an M2 attribute
m2_name	m2_name M2 attribute
m2_class	m2_class M2 attribute
m2_meta	m2_meta M2 attribute
base_class	a base class; an R class to use for dispatching if there is no relevant method for the other classes (e.g. $m2$)
name	a string; the name of a M2 object
all.names	if TRUE, all registered Macaulay2 variables, including ones internally used by m2r, will be returned

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Examples

```
## Not run: requires Macaulay2
m2("a = 5")
m2_ls()
m2_exists("a")
m2("b = 1")
m2_exists(c("a","b","c"))
m2_getwd()
x <- 1
class(x) <- "m2"</pre>
attr(x, "m2\_meta") \leftarrow list(a = 1, b = 2)
m2_meta(x)
m2_meta(x, "b")
m2_meta(x, "b") <- 5
m2_meta(x, "b")
# R <- ring(c("x1", "x2", "x3"))
# m2_name(R)
# m2(sprintf("class %s", m2_name(R)))
# m2_ls()
# m2_rm(m2_name(R))
# m2_ls()
# m2(paste("class", m2_name(R)))
m2_ls()
m2_ls(all.names = TRUE)
## End(Not run)
```

phc

PHCpack

Description

Call PHCpack to solve a zero-dimensional system

Usage

```
solve_system(mpolyList)
solve_system.(mpolyList)
mixed_volume(mpolyList)
```

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Arguments

```
mpolyList An mpolyList object
```

Details

Note that solve_system() doesn't take in an input ring because the solver only works over the complex numbers.

Value

```
(currently) the output of an m2() call (string?)
```

Examples

```
## Not run: requires Macaulay2

# for this to work, you need to have modified your
# init-PHCpack.m2 file instead of changing your .bashrc
# file to establish the path of phc
# (**clarify**, maybe checkout algstat::polySolve)

(mpolyList <- mp(c("t^4 - x", "t^3 - y", "t^2 - z", "x+y+z")))
solve_system(mpolyList)
mixed_volume(mpolyList)

## End(Not run)</pre>
```

ring

Create a new ring in Macaulay2

Description

Create a new ring in Macaulay2

Usage

```
ring(..., coefring = m2_coefrings(), order = m2_termorders(), code = FALSE)
ring.(..., coefring = m2_coefrings(), order = m2_termorders(), code = FALSE)
ring_(
  vars,
  coefring = m2_coefrings(),
  order = m2_termorders(),
  code = FALSE,
```

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```
ring_.(
  vars,
  coefring = m2_coefrings(),
  order = m2_termorders(),
  code = FALSE,
  ...
)

m2_coefrings()

m2_termorders()

## S3 method for class 'm2_polynomialring'
print(x, ...)
```

Arguments

... ...

coefring coefficient ring (default: "CC")
order a term order (default: "grevlex")

 $code \qquad \qquad return \ only \ the \ M2 \ code? \ (default: \ FALSE)$

vars vector of variable names

x formal argument for print method

Value

a reference to a Macaulay2 ring

snf 29

snf

Smith normal form

Description

For an integer matrix M, this computes the matrices D, P, and Q such that D = PMQ, which can be seen as an analogue of the singular value decomposition. All are integer matrices, and P and Q are unimodular (have determinants +- 1).

Usage

```
snf(mat, code = FALSE)
snf.(mat, code = FALSE)
```

Arguments

```
mat a matrix (integer entries)

code return only the M2 code? (default: FALSE)
```

Value

```
a list of m2_matrix objects with names D, P, and Q
```

See Also

```
m2_matrix()
```

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```
## Not run: requires Macaulay2
##### basic usage
M <- matrix(c(</pre>
 2, 4, 4,
-6, 6, 12,
 10, -4, -16
), nrow = 3, byrow = TRUE)
snf(M)
(mats <- snf(M))</pre>
P \leftarrow mats\P; D \leftarrow mats\D; Q \leftarrow mats\Q
P %*% M %*% Q
                            # = D
solve(P) %*% D %*% solve(Q) # = M
det(P)
det(Q)
M <- matrix(c(</pre>
   1, 2, 3,
   1, 34, 45,
  2213, 1123, 6543,
    0, 0, 0
), nrow = 4, byrow = TRUE)
(mats <- snf(M))</pre>
P \leftarrow mats\P; D \leftarrow mats\D; Q \leftarrow mats\Q
P %*% M %*% Q
                            \# = D
##### understanding lattices
\# cols of m generate the lattice L
M \leftarrow matrix(c(2,-1,1,3), nrow = 2)
row.names(M) \leftarrow c("x", "y")
# plot lattice
df <- expand.grid(x = -20:20, y = -20:20)
pts <- t(apply(df, 1, function(v) M %*% v))</pre>
w <- c(-15, 15)
```

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str_m2

Give the structure of a Macaulay2 ring

Description

Give the structure of a Macaulay2 ring

Usage

```
str_m2(object, ...)
```

Arguments

```
object An m2 object
```

Value

Invisible the object passed in.

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Examples

```
## Not run: requires Macaulay2
a <- m2("1")
R <- ring(c("x1", "x2", "x3"))
str_m2(R)
str_m2.default(R)
## End(Not run)</pre>
```

use_ring

Set Macaulay2 ring

Description

use_ring() sets the default referent ring on the Macaulay2 side using the use function.

Usage

```
use_ring(ring)
```

Arguments

ring

a m2_ring (see ring()), m2_ring_pointer (see ring.()), or a character string containing the name of a ring in Macaulay2

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End(Not run)

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