

# Package ‘spCF’

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**Type** Package

**Title** Coarse-to-Fine Spatial Modeling

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**Imports** FNN, fields, nloptr, dbscan, ranger, withr

**Suggests** sp, sf, knitr, rmarkdown

**Description** Provides functions for coarse-to-fine spatial modeling (CFSM), enabling fast spatial prediction, regression, and uncertainty quantification. For further details, see Murakami et al. (2025) <[doi:10.48550/arXiv.2510.00968](https://doi.org/10.48550/arXiv.2510.00968)>.

**License** GPL (>= 2)

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**cf\_lm***Coarse-to-fine spatial linear modeling*

## Description

Prediction and regression via coarse-to-fine spatial linear modeling.

## Usage

```
cf_lm(y, x, coords, x0 = NULL, coords0 = NULL, mod_hv)
```

## Arguments

<b>y</b>	Vector of response variables (N x 1).
<b>x</b>	Matrix of covariates (N x K).
<b>coords</b>	Matrix of 2-dimensional point coordinates (N x 2).
<b>x0</b>	Optional. Matrix of covariates at prediction sites (N0 x K).
<b>coords0</b>	Optional. Matrix of 2-dimensional point coordinates at prediction sites (N0 x 2).
<b>mod_hv</b>	Output object of the <a href="#">cf_lm_hv</a> function.

## Value

A list with the following elements:

**beta** Regression coefficients, their standard errors, and the lower and upper limits of the 95 percent confidence intervals.

**sd\_summary** Standard deviation of the regression term (xb), spatial process (spatial\_scale1, spatial\_scale2,...), additional learning, and residuals.

**e\_summary** R-squared and RMSE for validation samples, and residual standard deviation (residual\_SD), and root mean squared error for the validation samples (validation\_RMSE)

**pred** Predictive means and standard deviations (sample sites).

**pred0** Predictive means and standard deviations (prediction sites).

**bands** Bandwidth values for each scale. The i-th bandwidth is used for the spatial process corresponding to the i-th column of the Z matrix.

**Z** Predictive mean of the spatial process in each scale (sample sites; list).

**Z\_sd** Predictive standard deviation of the spatial process in each scale (sample sites; list).

**Z0** Predictive mean of the spatial process in each scale (prediction sites; list).

**Z0\_sd** Predictive standard deviation of the spatial process in each scale (prediction sites; list).

**Other** Other internal output objects.

## Author(s)

Daisuke Murakami

## References

Murakami, D., Comber, A., Yoshida, T., Tsutsumida, N., Brunsdon, C., & Nakaya, T. (2025). Coarse-to-fine spatial modeling: A scalable, machine-learning-compatible spatial model. \*arXiv:2510.00968\*.

## See Also

[cf\\_lm\\_hv](#), [sp\\_scalewise](#)

## Examples

```
set.seed(123)
require(sp); require(sf)
data(meuse)
data(meuse.grid)

### Data
y      <- log(meuse[, "zinc"])
coords <- meuse[, c("x", "y")]
x      <- data.frame(dist = meuse[, "dist"],
                      ffreq2 = as.integer(meuse$ffreq == 2),
                      ffreq3 = as.integer(meuse$ffreq == 3))

### Data at prediction sites
coords0 <- meuse.grid[, c("x", "y")]
x0       <- data.frame(dist = meuse.grid[, "dist"],
                        ffreq2 = as.integer(meuse.grid$ffreq == 2),
                        ffreq3 = as.integer(meuse.grid$ffreq == 3))

### Holdout validation optimizing the number of spatial scales
mod_hv   <- cf_lm_hv(y = y, x = x, coords = coords, add_learn = "none")

### Spatial modeling and prediction
mod      <- cf_lm(y = y, x = x, x0 = x0, coords = coords, coords0 = coords0,
                  mod_hv = mod_hv)
mod

### Mapping predictive mean and standard deviations (SD)
meuse.grid$pred  <- mod$pred$pred
meuse.grid$pred_sd<- mod$pred$pred_sd
meuse.grid_sf    <- st_as_sf(meuse.grid, coords = c("x", "y"))
plot(meuse.grid_sf[, "pred"], pch = 15, cex = 0.5, nbreaks = 20) # Predictive mean
plot(meuse.grid_sf[, "pred_sd"], pch = 15, cex = 0.5, nbbreaks = 20) # Predictive SD

### Multiscale spatial pattern/feature extraction
mod_s1<- sp_scalewise(mod, bw_range=c(1000,Inf)) # Large scale (1000 <= bandwidth)
mod_s2<- sp_scalewise(mod, bw_range=c(500,1000)) # Middle scale (500 <= bandwidth <= 1000)
mod_s3<- sp_scalewise(mod, bw_range=c(0,500))     # Small scale (bandwidth <= 500)
z1      <- mod_s1$pred$pred                      # Predictive mean
z2      <- mod_s2$pred$pred
z3      <- mod_s3$pred$pred
z1_sd  <- mod_s1$pred$pred_sd                   # Predictive SD
z2_sd  <- mod_s2$pred$pred_sd
```

```

z3_sd <- mod_s3$pred0$pred_sd
meuse.grid_sf3 <- cbind(meuse.grid_sf, z1, z2, z3, z1_sd, z2_sd, z3_sd)
plot(meuse.grid_sf3[,c("z1","z2","z3")], pch = 15,
     cex = 0.5, nbreaks = 20, key.pos=4, axes=TRUE) # Predictive means
plot(meuse.grid_sf3[,c("z1_sd","z2_sd","z3_sd")], pch = 15,
     cex = 0.5, nbreaks = 20, key.pos=4, axes=TRUE) # Predictive SD

```

**cf\_lm\_hv***Holdout validation for coarse-to-fine training of spatial linear models***Description**

Trains a coarse-to-fine spatial linear model and optimizes the spatial scale (resolution) through progressive holdout validation.

**Usage**

```

cf_lm_hv(
  y,
  x = NULL,
  coords,
  train_rat = 0.75,
  id_train = NULL,
  alpha = 0.9,
  kernel = "exp",
  add_learn = "none"
)

```

**Arguments**

<b>y</b>	Vector of response variables (N x 1).
<b>x</b>	Matrix of covariates (N x K).
<b>coords</b>	Matrix of 2-dimensional point coordinates (N x 2).
<b>train_rat</b>	Training sample ratio (default: 0.75). When N >= 1000, training samples are randomly selected. Otherwise, samples closest to the k-mean centers are used to stabilize the training.
<b>id_train</b>	Optional. If specified, the corresponding samples are used as training samples. Otherwise, training samples are selected at random (default).
<b>alpha</b>	Decay ratio of the kernel bandwidth in the coarse-to-fine training (default: 0.9).
<b>kernel</b>	Kernel type for modeling spatial dependence. "exp" for the exponential kernel (default) and "gau" for the Gaussian kernel.
<b>add_learn</b>	If "rf", random forest is additionally trained to capture non-linear patterns and/or higher-order interactions. Default is "none", meaning no additional training.

## Value

A list with the following elements:

**sse\_hv** Sum-of-squared error (SSE) for validation samples.

**sse\_hv\_all** All the SSEs obtained in each learning step.

**id\_train** ID of training samples.

**other** List of other outcomes, which are internally used.

## Author(s)

Daisuke Murakami

## References

Murakami, D., Comber, A., Yoshida, T., Tsutsumida, N., Brunsdon, C., & Nakaya, T. (2025). Coarse-to-fine spatial modeling: A scalable, machine-learning-compatible spatial model. \*arXiv:2510.00968\*.

## See Also

[cf\\_lm](#)

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sp\_scalewise

*Extract scale-wise spatial processes*

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## Description

Evaluate mean and variance of the spatial process with bandwidth values within a pre-specified range

## Usage

```
sp_scalewise(mod, bw_range = c(0, Inf))
```

## Arguments

**mod** Output object from the `cf_lm` function.

**bw\_range** Range of bandwidth values of the simulated spatial processes. For example, if `bw_range = c(10, 20)`, spatial processes with bandwidths between 10 and 20 are synthesized and simulated. The default is `c(0, Inf)`, which synthesizes all scales.

## Value

A list with the following elements:

**pred** Means and standard deviations of the spatial process (sample sites).

**pred0** Means and standard deviations of the spatial process (prediction sites).

**Author(s)**

Daisuke Murakami

**See Also**

[cf\\_1m](#)

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