# Package 'oncomsm'

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     The model can be used to sample from the predictive distribution to impute
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2 oncomsm-package

Author Kevin Kunzmann [aut, cre] (<a href="https://orcid.org/0000-0002-1140-7143">https://orcid.org/0000-0002-1140-7143</a>), Karthik Ananthakrishnan [ctb], Boehringer Ingelheim Ltd. [cph, fnd]

Maintainer Kevin Kunzmann < kevin.kunzmann@boehringer-ingelheim.com>

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## **R** topics documented:

	oncomsm-package	2
	check_data	
	compute_pfs	3
	impute	4
	parameter_sample_to_tibble	6
	plot.srpmodel	7
	plot_mstate	
	plot_pfs	9
	plot_response_probability	11
	plot_transition_times	12
	print.srpmodel	13
	sample_posterior	14
	simulate_decision_rule	15
	srpmodel	16
	visits_to_mstate	19
		•
Index		20

# Description

oncomsm-package

This package implements methods to dynamically predict response and progression of individuals in early oncology trials using parametric multi-state models and Bayesian inference. This allows the dynamic computation of Probability of Success for a wide The inference is implemented using 'rstan'.

The oncomsm package

#### References

Stan Development Team (2021). "RStan: the R interface to Stan". R package version 2.21.3. https://mc-stan.org

check\_data 3

check\_data

Check a visits data set for correct format

#### **Description**

Raises specific errors when encountering issues in the data.

#### Usage

```
check_data(data, model)
```

#### **Arguments**

data data.frame to check

model srpmodel object used to fit data

#### Value

data.frame, same as input but all censoring events after terminal states are removed.

#### **Examples**

```
tbl <- data.frame(group_id = "A", subject_id = "A1", t = 0, state = "stable")
mdl <- create_srpmodel(A = define_srp_prior())
check_data(tbl, mdl)</pre>
```

compute\_pfs

Compute progression-free-survival rate given sample

#### **Description**

compute\_pfs() computes the progression-free-survival rate at specified times given a paramter sample.

```
compute_pfs(
  model,
  t,
  parameter_sample = NULL,
  warmup = 500L,
  nsim = 1000L,
  seed = NULL,
  ...
)
```

impute impute

#### **Arguments**

#### Value

a data frame with samples of PFS rates at each of the time points in the vector t.

#### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
smpl <- sample_prior(mdl, nsim = 500, seed = 34L)
dplyr::filter(
  compute_pfs(mdl, t = seq(0, 12), parameter_sample = smpl),
  iter == 1
)</pre>
```

impute

Sample visits from predictive distribution

### Description

impute() samples visits for individuals in data and potentially missing individuals up to a maximum of n\_per\_group from the posterior predictive distribution of the given model.

sample\_predictive() draws samples from the predictive distribution of a model given a parameter sample.

```
impute(
  model,
  data,
  nsim,
  n_per_group = NULL,
  sample = NULL,
  p = NULL,
  shape = NULL,
```

impute 5

```
scale = NULL,
 now = NULL,
  seed = NULL.
  nsim_parameters = 1000L,
 warmup_parameters = 250L,
 nuts_control = list(),
  as_mstate = FALSE,
)
sample_predictive(
 model,
  nsim,
  n_per_group,
  sample = NULL,
  p = NULL,
  shape = NULL,
  scale = NULL,
  seed = NULL,
  nsim_parameters = 1000L,
 warmup_parameters = 250,
 nuts_control = list(),
  as_mstate = FALSE,
)
```

#### **Arguments**

	an object of class srpmodel containing prior information	
model		

data a data frame with variables subject\_id<chr> (subject identifier), group\_id<chr>

(group identifier), t<dbl> (time of visit, relative to first visit in study), state<chr> (state recorded at visit). Allowed states are "stable", "response", "progression" (or death), and "EOF" (end of follow-up). The EOF state marks the end of an

individual's follow-up before the absorbing state "progression".

nsim integer, number of samples to draw

n\_per\_group integer vector with number of individuals per group.sample a stanfit object with samples from the respective model.

p numeric, vector of optional fixed response probabilities to use for sampling

shape numeric, matrix of optional fixed Weibull shape parameters to use for sampling

must be a matrix of dim c(n\_groups, 3) where the second dimension corresponds

to the transitions between s->r, s->p, r->p

scale numeric, matrix of optional fixed Weibull scale parameters to use for sampling

must be a matrix of dim c(n\_groups, 3) where the second dimension corresponds

to the transitions between s->r, s->p, r->p

now numeric, time since first visit in data if not last recorded visit time

seed integer, fixed random seed; NULL for no fixed seed

```
nsim_parameters
integer, number of parameter samples
warmup_parameters
integer, number of warmup samples for the rstan sampler before retaining samples of the parameters.

nuts_control list, parameters for NUTS algorithm see control argument inrstan::stan()
as_mstate logical, return data in mstate format?
... further arguments passed to method implementations
```

#### Value

a data frame with variables subject\_id<chr> (subject identifier), group\_id<chr> (group identifier), t<dbl> (time of visit, relative to first visit in study), state<chr> (state recorded at visit) iter<int> (re-sample indicator). Allowed states are "stable", "response", "progression" (or death), and "EOF" (end of follow-up). The EOF state marks the end of an individual's follow-up before the absorbing state "progression".

#### See Also

```
sample_prior() sample_posterior()
```

#### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
tbl <- tibble::tibble(
    subject_id = c("A1", "A1"),
    group_id = c("A", "A"),
    t = c(0, 1.5),
    state = c("stable", "stable")
)
impute(mdl, tbl, 1L, seed = 38L)
sample_predictive(mdl, 1L, 20L, seed = 38L)</pre>
```

```
parameter_sample_to_tibble
```

Convert parameter sample to data table

#### Description

parameter\_sample\_to\_tibble() takes a rstan::stanfit parameter sample of a model, extracts the parameter values and returns them in a data frame.

```
parameter_sample_to_tibble(model, sample, ...)
```

plot.srpmodel 7

### **Arguments**

```
model an object of class srpmodel containing prior information sample a stanfit object with samples from the respective model.
... further arguments passed to method implementations
```

#### Value

a tibble with the sampled parameters, in long format

#### See Also

```
sample_prior() sample_posterior()
```

### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
smpl <- sample_prior(mdl, seed = 3647L)
parameter_sample_to_tibble(mdl, smpl)</pre>
```

plot.srpmodel

Summary plot of model prior

#### **Description**

Summary plot of model prior

```
## S3 method for class 'srpmodel'
plot(
    x,
    parameter_sample = NULL,
    seed = 42L,
    nsim = 500L,
    warmup = 250,
    nuts_control = list(),
    dt_interval = NULL,
    dt_n_grid = 25,
    dt_expand = 1.1,
    dt_grid = NULL,
    confidence = NULL,
    ...
)
```

8 plot\_mstate

#### **Arguments**

the model to plot parameter\_sample a stanfit object with samples from the respective model. integer, fixed random seed; NULL for no fixed seed seed nsim integer, number of samples to draw integer, number of warm-up samples for the MCMC sampler before retaining warmup samples; see warmup parameter in rstan::stan(). list, parameters for NUTS algorithm see control argument inrstan::stan() nuts\_control dt\_interval numeric vector of length two with minimal and maximal time (relative to individual first visit) to use for plotting dt\_n\_grid number of grid points to use when automatically choosing plotting interval expansion factor for upper plotting limit when using automatic interval detection dt\_expand dt\_grid numeric vector of time points to use for plotting confidence numeric in (0, 1) confidence level for point-wise confidence bands around mean; none plotted if NULL. further arguments passed to method implementations

#### Value

A patchwork object, see patchwork::patchwork

#### See Also

```
plot_pfs() plot_transition_times() plot_response_probability()
```

### Examples

```
## Not run:
mdl <- create_srpmodel(A = define_srp_prior())
plot(mdl)
## End(Not run)</pre>
```

plot\_mstate Swi

Swimmer plot of multi-state data

### Description

plot\_mstate() plots data in 'multi-state-format' as swimmer plot.

plot\_pfs 9

#### Usage

```
plot_mstate(
  data,
  model,
  now = max(tbl_mstate$t_max),
  relative_to_sot = TRUE,
  ...
)
```

#### **Arguments**

data a data frame with multi-state data; variables are subject\_id<chr>, group\_id<chr>,

subject\_id<chr>, from<chr>, to<chr>, t\_min<dbl>, t\_max<dbl>, t\_sot<dbl>, where to and from indicate the state from which and into which the transitions occurs (stable, response, progression), t\_max and t\_min specify the interval in

which the transition occurred relative to t\_sot (start of treatment).

model an object of class srpmodel containing prior information

now the current time relative to the start of the trial

relative\_to\_sot

logical, should the timeline be relative to the start of trial or the start of treatment

for each individual

... further arguments passed to method implementations

#### Value

```
a ggplot2::ggplot object
```

#### See Also

```
visits_to_mstate()
```

### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
tbl_visits <- sample_predictive(mdl, n_per_group = 5L, nsim = 1, seed = 468L)
tbl_mstate <- visits_to_mstate(tbl_visits, mdl)
plot_mstate(tbl_mstate, mdl)</pre>
```

plot\_pfs

Plot progression-free-survival function

### **Description**

plot\_pfs() plots the progression-free-survival function of a model.

plot\_pfs

### Usage

```
plot_pfs(
  model,
  parameter_sample = NULL,
  seed = 42L,
  nsim = 500L,
  warmup = 250,
  nuts_control = list(),
  dt_interval = NULL,
  dt_n_grid = 25,
  dt_expand = 1.1,
  dt_grid = NULL,
  confidence = NULL,
  ...
)
```

### Arguments

model	an object of class srpmodel containing prior information
parameter_samp	le
	a stanfit object with samples from the respective model.
seed	integer, fixed random seed; NULL for no fixed seed
nsim	integer, number of samples to draw
warmup	integer, number of warm-up samples for the MCMC sampler before retaining samples; see warmup parameter in rstan::stan().
nuts_control	list, parameters for NUTS algorithm see control argument inrstan::stan()
dt_interval	numeric vector of length two with minimal and maximal time (relative to individual first visit) to use for plotting
dt_n_grid	number of grid points to use when automatically choosing plotting interval
dt_expand	expansion factor for upper plotting limit when using automatic interval detection
dt_grid	numeric vector of time points to use for plotting
confidence	numeric in $(0,1)$ confidence level for point-wise confidence bands around mean; none plotted if NULL.
	further arguments passed to method implementations

### Value

```
a ggplot2::ggplot object
```

#### See Also

```
plot_transition_times() plot_response_probability()
```

#### **Examples**

```
## Not run:
mdl <- create_srpmodel(A = define_srp_prior())
plot_pfs(mdl)
## End(Not run)</pre>
```

plot\_response\_probability

Plot the response probability distributions

### Description

plot\_response\_probability() plots the distribution over the response probability parameter in the specified model.

### Usage

```
plot_response_probability(
  model,
  parameter_sample = NULL,
  seed = 42L,
  nsim = 500L,
  warmup = 250,
  nuts_control = list(),
  ...
)
```

#### **Arguments**

model an object of class srpmodel containing prior information

parameter\_sample

a stanfit object with samples from the respective model.

seed integer, fixed random seed; NULL for no fixed seed

nsim integer, number of samples to draw

warmup integer, number of warm-up samples for the MCMC sampler before retaining

samples; see warmup parameter in rstan::stan().

nuts\_control list, parameters for NUTS algorithm see control argument inrstan::stan()

... further arguments passed to method implementations

#### Value

```
a ggplot2::ggplot object
```

12 plot\_transition\_times

#### See Also

```
plot_transition_times() plot_pfs()
```

#### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
plot_response_probability(mdl)</pre>
```

 $plot\_transition\_times$  Plot the transition times of a model

#### **Description**

plot\_transition\_times() plots a the survival functions for the transition times in a multi-state model

#### Usage

```
plot_transition_times(
   model,
   parameter_sample = NULL,
   seed = 42L,
   nsim = 500L,
   warmup = 250,
   nuts_control = list(),
   dt_interval = NULL,
   dt_n_grid = 25,
   dt_expand = 1.1,
   dt_grid = NULL,
   confidence = NULL,
   ...
)
```

#### Arguments

model an object of class srpmodel containing prior information

parameter\_sample

a stanfit object with samples from the respective model.

seed integer, fixed random seed; NULL for no fixed seed

nsim integer, number of samples to draw

warmup integer, number of warm-up samples for the MCMC sampler before retaining

samples; see warmup parameter in rstan::stan().

nuts\_control list, parameters for NUTS algorithm see control argument inrstan::stan()

dt\_interval numeric vector of length two with minimal and maximal time (relative to indi-

vidual first visit) to use for plotting

print.srpmodel 13

dt_n	_grid	number of grid points to use when automatically choosing plotting interval
dt_e	xpand	expansion factor for upper plotting limit when using automatic interval detection
dt_g	rid	numeric vector of time points to use for plotting
conf	idence	numeric in $(0,1)$ confidence level for point-wise confidence bands around mean; none plotted if NULL.
		further arguments passed to method implementations

#### Value

```
a ggplot2::ggplot object
```

#### See Also

```
plot_pfs() plot_response_probability()
```

### **Examples**

```
## Not run:
mdl <- create_srpmodel(A = define_srp_prior())
plot_transition_times(mdl)
## End(Not run)</pre>
```

print.srpmodel

Print an srpmodel

### Description

Print an srpmodel

#### Usage

```
## $3 method for class 'srpmodel'
print(x, ...)
## $3 method for class 'srpmodel'
format(x, ...)
```

#### **Arguments**

x model to print

... further arguments passed to method implementations

#### Value

format() returns a character string representation of the object, print() prints to the console and returns the object itself invisibly.

sample\_posterior

#### **Examples**

```
print(create_srpmodel(A = define_srp_prior()))
format(create_srpmodel(A = define_srp_prior()))
```

sample\_posterior

Sample parameters from a model

### Description

sample\_posterior() draws samples from the posterior distribution of the specified model given a data set with visit data.

sample\_prior() draws samples from the prior distribution of the specified model object.

### Usage

```
sample_posterior(
 model,
 data,
 now = NULL,
 nsim = 2000L,
 seed = NULL,
 warmup = 500L,
 nuts_control = list(),
 acceptable_divergent_transition_fraction = 0.1,
)
sample_prior(
 model,
 nsim = 2000L,
 seed = NULL,
 warmup = 500L,
 nuts_control = list(),
)
```

#### **Arguments**

now	numeric, time from first visit in data if different form last recorded visit
	(group identifier), t <dbl> (time of visit, relative to first visit in study), state<chr> (state recorded at visit). Allowed states are "stable", "response", "progression" (or death), and "EOF" (end of follow-up). The EOF state marks the end of an individual's follow-up before the absorbing state "progression".</chr></dbl>
data	a data frame with variables subject_id <chr> (subject identifier), group_id<chr></chr></chr>
model	an object of class srpmodel containing prior information

nsim integer, number of samples to draw

simulate\_decision\_rule 15

#### Value

A rstan::stanfit object with posterior samples.

#### See Also

```
rstan::stan() parameter_sample_to_tibble() sample_predictive() impute()
```

#### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
tbl <- tibble::tibble(
    subject_id = c("A1", "A1"),
    group_id = c("A", "A"),
    t = c(0, 1.5),
    state = c("stable", "response")
)
sample_posterior(mdl, tbl, seed = 42L)
sample_prior(mdl, seed = 42L)</pre>
```

```
simulate_decision_rule
```

Simulate results under a custom decision rule

### Description

simulate\_decision\_rule() simulates from the prior or posterior predictive distribution of a model and applies a custom decision rule to each simulated data set.

```
simulate_decision_rule(
  model,
  n_per_group,
  decision_rule,
  data = NULL,
```

16 srpmodel

```
parameter_sample = NULL,
seed = NULL,
nsim = 1L
)
```

#### **Arguments**

model model to use for sampling

n\_per\_group group size

decision\_rule a function with signature rule(mdl, data, ...) returning a data frame with

results from a applying the decision rule to data setdata, typically contains a

column group\_id and a one column per decision/result.

data a data frame with visit data to condition on

parameter\_sample

an optional parameter sample to reuse

seed optional fixed seed

nsim the number of resamples to draw from the predictive distribution

#### **Details**

The sampling is implementing using furrr::future\_map() and thus supports parallel execution when specifying a future::plan().

#### Value

A data frame with columns iter (the resample index) and any columns returned by decision\_rule applied to each of the nsim datasets sampled from the predictive distribution.

### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
rule <- function(model, data) {
  tibble::tibble(decision = sample(c(0,1), 1))
}
simulate_decision_rule(mdl, 5, rule, nsim = 3)</pre>
```

srpmodel

A stable-response-progression model

#### **Description**

create\_model() takes one or more prior-specifications for an SRP multi-state model and combines them into a single model object. Groups are still treated as independent.

srpmodel 17

### Usage

```
define_srp_prior(
 p_mean = 0.5,
 p_n = 3,
 p_eta = 0,
 p_min = 0,
 p_max = 1,
 median_t_q05 = c(1, 1, 1),
 median_t_q95 = c(60, 60, 60),
 shape_q05 = rep(0.9, 3),
  shape_q95 = rep(2.5, 3),
 visit_spacing = 1,
  recruitment_rate = 1
)
create_srpmodel(
 maximal\_time = 10 * 12,
 states = c("stable", "response", "progression"),
 censored = "EOF"
)
```

#### **Arguments**

p_mean	numeric, mean of the beta prior for the response probability
p_n	numeric, beta prior equivalent sample size (a + b)
p_eta	numeric, robustification parameter for beta prior; actual prior is $(1 - eta)$ beta + eta; i.e., eta is the non-informative weight.
p_min	numeric, minimal response probability
p_max	numeric, maximal response probability
median_t_q05	numeric of length three, $5\%$ quantiles of the log-normal distributions for the median time-to-next-event for the three transitions s->r, s->p, r->p.
median_t_q95	numeric of length three, 95% quantiles of the log-normal distributions for the median time-to-next-event for the three transitions s->r, s->p, r->p.
shape_q05	numeric of length three, $5\%$ quantiles of the log-normal distributions for the shapes of the time-to-next-event distributions for the three transitions s->r, s->p, r->p.
shape_q95	numeric of length three, 95% quantiles of the log-normal distributions for the shapes of the time-to-next-event distributions for the three transitions s->r, s->p, r->p.
visit_spacing	numeric, fixed duration between visits
recruitment_rat	ce
	numeric, constant recruitment rate
	named srp_prior objects; the argument names serve as group labels

18 srpmodel

maximal\_time the maximal overall runtime of the trial as measured from the first visit of any

group. No visits past this point are sampled.

states character vector of three states (initial, intermediate, terminal)

censored string, indicator of premature censoring events; no data is imputed after this

point.

#### **Details**

define\_srp\_prior() specifies a prior distribution for a three state model (stable, response, progression) for a single group.

#### Value

define\_srp\_prior() returns an object of class srp\_prior, all inputs are accessible via \$x where x is the name of the input argument in the function call except for the two parameters visit\_spacing and recruitment\_rate. These two parameters are saved as attributes and can be retrieved directly using attr(mdl, "visit\_spacing") and attr(mdl, "recruitment\_rate").

create\_srpmodel() returns an object of class c("srpmodel", "list") that holds information about potentially multiple groups in a compact format and can be accessed using the list operator \$name. group\_id is a character vector with the group names, maximal\_time is the maximal follow-up time since the first visit in the study, visit\_spacing is the vector of per-group difference between visits (only relevant for forward sampling), recruitment\_rate is the vector of per-group recruitment rates, stan\_model is the pre-compiled 'stan' model used for inference, states is the vector of state names in the multi-state model, and prior is a list of hyperparamters for the model prior with elements p, vector, for the response probability per group, median\_t is an c(n\_groups, 3, 2) dimensional array where median\_t[i,j,1] holds the 5% quantile of the the lognormal prior on median transition time for group i and transition j and median\_t[i,j,2] the corresponding upper 95% quantile. The shape hyperparamter has the same format and specified the corresponding quantiles for the Weibull shape parameter.

#### **Examples**

```
# a model with prior 25% response rate and variance equivalent to
# 10 data points (i.e. a Beta(2.5, 7.5) distribution).
grp <- define_srp_prior(p_mean = 0.25, p_n = 10)
attr(grp, "recruitment_rate")

# a model with two groups and different priors on the respective response
# probabilities
mdl <- create_srpmodel(
    A = define_srp_prior(),
    B = define_srp_prior(p_mean = 0.33, p_n = 10)
)
mdl$median_t</pre>
```

visits\_to\_mstate 19

visits_to_mstate	Convert cross-sectional visit data to multi-state format
	*

#### Description

visits\_to\_mstate() converts visits to interval-censored multi-state data where each row corresponds to a transition between states. The conversion assumes that visit spacing is tight enough to not miss any transitions.

#### Usage

```
visits_to_mstate(tbl_visits, model, now = max(tbl_visits$t))
```

### **Arguments**

tbl\_visits data frame, visit data in long format

model an object of class srpmodel containing prior information

now time point since start of trial (might be later than last recorded visit)

#### Value

A data frame with multi-state data; variables are subject\_id<chr>, group\_id<chr>, subject\_id<chr>, from<chr>, to<chr>, t\_min<dbl>, t\_max<dbl>, t\_sot<dbl>, where to and from indicate the state from which and into which the transitions occurs, t\_max and t\_min specify the interval in which the transition occurred relative to t\_sot (start of treatment).

### **Examples**

```
mdl <- create_srpmodel(A = define_srp_prior())
tbl_visits <- sample_predictive(mdl, n_per_group = 5L, nsim = 1, seed = 468L)
visits_to_mstate(tbl_visits, mdl)</pre>
```

# **Index**

```
check_data, 3
                                                visits_to_mstate, 19
compute_pfs, 3
                                                visits_to_mstate(), 9
create_srpmodel (srpmodel), 16
define_srp_prior(srpmodel), 16
format.srpmodel(print.srpmodel), 13
ggplot2::ggplot, 9–11, 13
impute, 4
impute(), 15
oncomsm (oncomsm-package), 2
oncomsm-package, 2
parameter_sample_to_tibble, 6
parameter_sample_to_tibble(), 15
patchwork::patchwork, 8
plot.srpmodel, 7
plot_mstate, 8
plot_pfs, 9
plot_pfs(), 8, 12, 13
plot_response_probability, 11
plot_response_probability(), 8, 10, 13
plot_transition_times, 12
plot_transition_times(), 8, 10, 12
print.srpmodel, 13
rstan::stan(), 4, 6, 8, 10–12, 15
rstan::stanfit, 6, 15
sample_posterior, 14
sample_posterior(), 6, 7
sample_predictive (impute), 4
sample_predictive(), 15
sample_prior(sample_posterior), 14
sample_prior(), 6, 7
simulate_decision_rule, 15
srp-model (srpmodel), 16
srpmodel, 3-5, 7, 9-12, 14, 16, 19
```