# Package 'SBCK'

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Author Yoann Robin [aut, cre], Mathieu Vrac [cph]
Maintainer Yoann Robin <yoann.robin.k@gmail.com></yoann.robin.k@gmail.com>
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AR2D2		AR2D2 (Analogues dences) method	Rank Resampling for Distributions and Depen-

## **Description**

Perform a multivariate (non stationary) bias correction.

#### **Details**

Use Quantiles shuffle in calibration and projection period with CDFt

## **Public fields**

```
mvq [MVQuantilesShuffle] Class to transform dependance structure bc_method [SBCK::] Bias correction method bckwargs [list] List of arguments of bias correction bcm_ [SBCK::] Instancied bias correction method reverse [bool] If we apply bc_method first and then shuffle, or reverse
```

#### Methods

#### **Public methods:**

```
• AR2D2$new()
```

- AR2D2\$fit()
- AR2D2\$predict()
- AR2D2\$clone()

Method new(): Create a new AR2D2 object.

```
Usage:
AR2D2$new(
  col_cond = base::c(1),
  lag_search = 1,
  lag_keep = 1,
  bc_method = SBCK::CDFt,
  shuffle = "quantile",
  reverse = FALSE,
  ...
)
Arguments:
```

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```
col_cond Conditionning colum
 lag_search Number of lags to transform the dependence structure
 lag_keep Number of lags to keep
 bc_method Bias correction method
 shuffle Shuffle method used, can be quantile or rank
 reverse If we apply bc_method first and then shuffle, or reverse
 ... Others named arguments passed to bc_method$new
 Returns: A new 'AR2D2' object.
Method fit(): Fit the bias correction method. If X1 is NULL, the method is considered as
stationary
 Usage:
 AR2D2\$fit(Y0, X0, X1 = NULL)
 Arguments:
 Y0 [matrix: n_samples * n_features] Observations in calibration
 X0 [matrix: n_samples * n_features] Model in calibration
 X1 [matrix: n_samples * n_features] Model in projection
 Returns: NULL
Method predict(): Predict the correction
 Usage:
 AR2D2\$predict(X1 = NULL, X0 = NULL)
 Arguments:
 X1 [matrix: n_samples * n_features or NULL] Model in projection
 X0 [matrix: n_samples * n_features or NULL] Model in calibration
 Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL (and vice-versa),
 else return a list containing Z1 and Z0, the corrections of X1 and X0
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 AR2D2$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

# References

Vrac, M. et S. Thao (2020). "R2 D2 v2.0: accounting for temporal dependences in multivariate bias correction via analogue rank resampling". In: Geosci. Model Dev. 13.11, p. 5367-5387. doi:10.5194/gmd-13-5367-2020.

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#### **Examples**

```
## Three 4-variate random variables
Y0 = matrix( stats::rnorm( n = 1000 ) , ncol = 4 ) ## Biased in calibration period
X0 = matrix( stats::rnorm( n = 1000 ) , ncol = 4 ) / 2 + 3 ## Reference in calibration period
X1 = matrix( stats::rnorm( n = 1000 ) , ncol = 4 ) * 2 + 6 ## Biased in projection period
## Bias correction
cond_col = base::c(2,4)
lag_search = 6
lag_keep = 3
## Step 1 : construction of the class AR2D2
ar2d2 = SBCK::AR2D2$new( cond_col , lag_search , lag_keep )
## Step 2 : Fit the bias correction model
ar2d2$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction
Z = ar2d2$predict(X1,X0)
```

bin\_width\_estimator

bin\_width\_estimator method

#### **Description**

Lenght of cell to compute an histogram

#### Usage

```
bin_width_estimator(X, method = "auto")
```

#### **Arguments**

X method

[matrix] A matrix containing data, nrow = n\_samples, ncol = n\_features [string] Method to estimate bin\_width, values are "auto", "FD" (Friedman Dra-

conis, robust over outliners) or "Sturges". If "auto" is used and if nrow(X) < 0

1000, "Sturges" is used, else "FD" is used.

# Value

[vector] Lenght of bins

```
X = base::cbind( stats::rnorm( n = 2000 ) , stats::rexp(2000) )
## Friedman Draconis is used
binw_width = SBCK::bin_width_estimator( X , method = "auto" )
X = stats::rnorm( n = 500 )
## Sturges is used
binw_width = SBCK::bin_width_estimator( X , method = "auto" )
```

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CDFt

CDFt method (Cumulative Distribution Function transfer)

#### **Description**

Perform an univariate bias correction of X with respect to Y.

#### **Details**

Correction is applied margins by margins.

#### **Public fields**

```
n_features [integer] Number of features
```

tol [double] Floatting point tolerance

- distY0 [ROOPSD distribution or a list of them] Describe the law of each margins. A list permit to use different laws for each margins. Default is ROOPSD::rv\_histogram.
- distY1 [ROOPSD distribution or a list of them] Describe the law of each margins. A list permit to use different laws for each margins. Default is ROOPSD::rv\_histogram.
- distX0 [ROOPSD distribution or a list of them] Describe the law of each margins. A list permit to use different laws for each margins. Default is ROOPSD::rv\_histogram.
- distX1 [ROOPSD distribution or a list of them] Describe the law of each margins. A list permit to use different laws for each margins. Default is ROOPSD::rv\_histogram.

#### Methods

#### **Public methods:**

- CDFt\$new()
- CDFt\$fit()
- CDFt\$predict()
- CDFt\$clone()

**Method** new(): Create a new CDFt object.

```
Usage:
CDFt$new(...)
```

Arguments:

... Optional arguments are: - distX0, distX1, models in calibration and projection period, see ROOPSD - distY0, distY1, observations in calibration and projection period, see ROOPSD - kwargsX0, kwargsX1, list of arguments for each respective distribution - kwargsY0, kwargsY1, list of arguments for each respective distribution - scale\_left\_tail [float] Scale applied on the left support (min to median) between calibration and projection period. If NULL (default), it is determined during the fit. If == 1, equivalent to the original algorithm of CDFt. - scale\_right\_tail [float] Scale applied on the right support (median to max) between calibration and projection period. If NULL (default), it is determined during the fit.

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If == 1, equivalent to the original algorithm of CDFt. - normalize\_cdf [bool or vector of bool] If a normalization is applied to the data to maximize the overlap of the support. Can be a bool (True or False, applied for all colums), or a list of bool of size 'n\_features' to distinguished each columns.

```
Returns: A new 'CDFt' object.
```

```
Method fit(): Fit the bias correction method
 Usage:
 CDFt$fit(Y0, X0, X1)
 Arguments:
 Y0 [matrix: n_samples * n_features] Observations in calibration
 X0 [matrix: n_samples * n_features] Model in calibration
 X1 [matrix: n_samples * n_features] Model in projection
 Returns: NULL
Method predict(): Predict the correction
 Usage:
 CDFt$predict(X1, X0 = NULL)
 Arguments:
 X1 [matrix: n_samples * n_features] Model in projection
 X0 [matrix: n_samples * n_features or NULL] Model in calibration
 Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list
 containing Z1 and Z0, the corrections of X1 and X0
```

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
CDFt$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Michelangeli, P.-A., Vrac, M., and Loukos, H.: Probabilistic downscaling approaches: Application to wind cumulative distribution functions, Geophys. Res. Lett., 36, L11708, https://doi.org/10.1029/2009GL038401, 2009.

```
## Three bivariate random variables (rnorm and rexp are inverted between ref and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period
## Bias correction
```

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```
## Step 1 : construction of the class CDFt
cdft = SBCK::CDFt$new()
## Step 2 : Fit the bias correction model
cdft$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction, Z is a list containing
## corrections
Z = cdft$predict(X1,X0)
Z$Z0 ## Correction in calibration period
Z$Z1 ## Correction in projection period
```

chebyshev

Chebyshev distance

## **Description**

Compute Chebyshev distance between two dataset or SparseHist X and Y

## Usage

```
chebyshev(X, Y)
```

# Arguments

```
X [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
Y [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
```

#### Value

[float] value of distance

```
X = base::cbind( stats::rnorm(2000) , stats::rnorm(2000) )
Y = base::cbind( stats::rnorm(2000,mean=2) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four are equals
d = SBCK::chebyshev( X , Y )
d = SBCK::chebyshev(muX , Y )
d = SBCK::chebyshev(muX , muY )
d = SBCK::chebyshev(muX , muY )
```

```
\label{local_continuous_continuous} cpp\_pairwise\_distances\_XCall \\ cpp\_pairwise\_distances\_XCall
```

# Description

Pairwise distances between X and themselves with a R function (metric). DO NOT USE, use SBCK::pairwise\_distances

# Usage

```
cpp_pairwise_distances_XCall(X,metric)
```

## **Arguments**

X [Rcpp::NumericMatrix] Matrix metric [Rcpp::Function] R function

```
cpp\_pairwise\_distances\_Xstr \\ cpp\_pairwise\_distances\_Xstr
```

# Description

Pairwise distances between X and themselves with a compiled str\_metric. DO NOT USE, use SBCK::pairwise\_distances

# Usage

```
cpp_pairwise_distances_Xstr(X,str_metric)
```

# Arguments

X [Rcpp::NumericMatrix] Matrix str\_metric [std::string] c++ string

```
\label{local_continuous_continuous} cpp\_pairwise\_distances\_XYCall \\ cpp\_pairwise\_distances\_XYCall
```

## **Description**

Pairwise distances between X and Y with a R function (metric). DO NOT USE, use SBCK::pairwise\_distances

## Usage

```
cpp_pairwise_distances_XYCall(X,Y,metric)
```

# Arguments

X [Rcpp::NumericMatrix] Matrix
Y [Rcpp::NumericMatrix] Matrix
metric [Rcpp::Function] R function

# Description

Pairwise distances between two differents matrix X and Y with a compiled str\_metric. DO NOT USE, use SBCK::pairwise\_distances

## Usage

```
cpp_pairwise_distances_XYstr(X,Y,str_metric)
```

# **Arguments**

X [Rcpp::NumericMatrix] Matrix
Y [Rcpp::NumericMatrix] Matrix

str\_metric [std::string] c++ string

#### **Description**

Generate a testing dataset from bimodale random bivariate Gaussian distribution

## Usage

```
dataset_bimodal_reverse_2d(n_samples)
```

#### **Arguments**

n\_samples [integer] numbers of samples drawn

#### Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

# **Examples**

```
XY = SBCK::dataset_bimodal_reverse_2d(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

```
dataset_gaussian_2d dataset_gaussian_2d
```

# Description

Generate a testing dataset from random bivariate Gaussian distribution

#### Usage

```
dataset_gaussian_2d(n_samples)
```

#### **Arguments**

```
n_samples [integer] numbers of samples drawn
```

#### Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

#### **Examples**

```
XY = SBCK::dataset_gaussian_2d(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

# Description

Generate a testing dataset such that the biased dataset is a distribution of the the form Normal x Exp and the reference of the the form Exp x Normal.

#### Usage

```
dataset_gaussian_exp_2d(n_samples)
```

#### **Arguments**

```
n_samples [integer] numbers of samples drawn
```

#### Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

#### **Examples**

```
XY = SBCK::dataset_gaussian_exp_2d(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

## **Description**

Generate a univariate testing dataset from a mixture of gaussian and exponential distribution

## Usage

```
dataset_gaussian_exp_mixture_1d(n_samples)
```

dataset\_gaussian\_L\_2d

#### **Arguments**

```
n_samples [integer] numbers of samples drawn
```

#### Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

#### **Examples**

```
XY = SBCK::dataset_gaussian_exp_mixture_1d(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

```
dataset_gaussian_L_2d dataset_gaussian_L_2d
```

## **Description**

Generate a testing dataset such that the biased dataset is a normal distribution and reference a mixture a normal with a form in "L"

## Usage

```
dataset_gaussian_L_2d(n_samples)
```

# **Arguments**

```
n_samples [integer] numbers of samples drawn
```

## Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

```
XY = SBCK::dataset_gaussian_L_2d(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

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#### **Description**

Generate a univariate testing dataset such that biased data follow an exponential law whereas reference follow a normal distribution

#### Usage

```
dataset_gaussian_VS_exp_1d(n_samples)
```

#### **Arguments**

n\_samples [integer] numbers of samples drawn

#### Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

## **Examples**

```
XY = SBCK::dataset_gaussian_VS_exp_1d(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

```
dataset_like_tas_pr
dataset_like_tas_pr
```

#### **Description**

Generate a testing dataset similar to temperature and precipitation. The method is the following: - Data from a multivariate normal law ( $\dim = 2$ ) are drawn - The quantile mapping is used to map the last column into the exponential law - Values lower than a fixed quantile are replaced by 0

# Usage

```
dataset_like_tas_pr(n_samples)
```

# **Arguments**

n\_samples [integer] numbers of samples drawn

data\_to\_hist

## Value

[list] a list containing X0, X1 (biased in calibration/projection) and Y0 (reference in calibration)

#### **Examples**

```
XY = SBCK::dataset_like_tas_pr(2000)
XY$X0 ## Biased in calibration period
XY$Y0 ## Reference in calibration period
XY$X1 ## Biased in projection period
```

data\_to\_hist

data\_to\_hist

## **Description**

Just a function to transform two datasets into SparseHist, if X or Y (or the both) are already a SparseHist, update just the second

#### Usage

```
data_to_hist(X, Y)
```

## **Arguments**

```
X [matrix or SparseHist]
Y [matrix or SparseHist]
```

# Value

[list(muX,muY)] a list with the two SparseHist

```
X = base::cbind( stats::rnorm(2000) , stats::rexp(2000) )
Y = base::cbind( stats::rexp(2000) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four give the same result
SBCK::data_to_hist( X , Y )
SBCK::data_to_hist( muX , Y )
SBCK::data_to_hist( X , muY )
SBCK::data_to_hist( muX , muY )
```

DistHelper

DistHelper

Dist Helper

## **Description**

Class used by CDFt and QM to facilitate fit, do not use

#### **Details**

Used to parallel work for margins

#### **Public fields**

```
dist [ROOPSD distribution] name of class
law [ROOPSD distribution] class set
kwargs [list] arguments of dist
```

#### Methods

#### **Public methods:**

- DistHelper\$new()
- DistHelper\$set\_features()
- DistHelper\$fit()
- DistHelper\$is\_frozen()
- DistHelper\$is\_parametric()
- DistHelper\$clone()

**Method** new(): Create a new DistHelper object.

```
DistHelper$new(dist, kwargs)

Arguments:
```

Usage:

dist [ROOPSD distribution or list] statistical law

kwargs [list] arguments passed to dist

Returns: A new 'DistHelper' object.

**Method** set\_features(): set the number of features

Usage:

DistHelper\$set\_features(n\_features)

Arguments:

n\_features [integer] numbers of features

Returns: NULL

Method fit(): fit the laws

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```
Usage:
       DistHelper$fit(X, i)
       Arguments:
       X [matrix] dataset to fit
       i [integer] margins to fit
       Returns: NULL
     Method is_frozen(): Test if margins i is frozen
       Usage:
       DistHelper$is_frozen(i)
       Arguments:
       i [integer] margins to fit
       Returns: [bool]
     Method is_parametric(): Test if margins i is parametric
       Usage:
       DistHelper$is_parametric(i)
       Arguments:
       i [integer] margins to fit
       Returns: [bool]
     Method clone(): The objects of this class are cloneable with this method.
       Usage:
       DistHelper$clone(deep = FALSE)
       Arguments:
       deep Whether to make a deep clone.
Examples
    ##
```

## **Description**

d0TC

Perform a multivariate (non stationary) bias correction.

## **Details**

Three random variables are needed, Y0, X0 and X1. The dynamic between X0 and X1 is estimated, and applied to Y0 to estimate Y1. Finally, OTC is used between X1 and the Y1 estimated.

dOTC (dynamical Optimal Transport Correction) method

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#### Super class

```
SBCK::OTC -> dOTC
```

#### Methods

#### **Public methods:**

```
dOTC$new()
```

- dOTC\$fit()
- dOTC\$predict()
- dOTC\$clone()

## Method new(): Create a new dOTC object.

```
Usage:
dOTC$new(
   bin_width = NULL,
   bin_origin = NULL,
   cov_factor = "std",
   ot = SBCK::OTNetworkSimplex$new()
)
```

#### Arguments:

bin\_width [vector or NULL] A vector of lengths of the cells discretizing R^numbers of variables. If NULL, it is estimating during the fit

bin\_origin [vector or NULL] Coordinate of lower corner of one cell. If NULL, c(0,...,0) is used

cov\_factor [string or matrix] Covariance factor to correct the dynamic transferred between X0 and Y0. For string, available values are "std" and "cholesky"

ot [OTSolver] Optimal Transport solver, default is the network simplex

Returns: A new 'dOTC' object.

# Method fit(): Fit the bias correction method

```
Usage:
dOTC$fit(Y0, X0, X1)

Arguments:
Y0 [matrix: n_samples * n_features] Observations in calibration
X0 [matrix: n_samples * n_features] Model in calibration
X1 [matrix: n_samples * n_features] Model in projection

Returns: NULL
```

#### Method predict(): Predict the correction

Usage:

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```
dOTC$predict(X1, X0 = NULL)

Arguments:

X1 [matrix: n_samples * n_features] Model in projection

X0 [matrix: n_samples * n_features or NULL] Model in calibration

Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list containing Z1 and Z0, the corrections of X1 and X0
```

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
dOTC$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Robin, Y., Vrac, M., Naveau, P., Yiou, P.: Multivariate stochastic bias corrections with optimal transport, Hydrol. Earth Syst. Sci., 23, 773–786, 2019, https://doi.org/10.5194/hess-23-773-2019

### **Examples**

```
## Three bivariate random variables (rnorm and rexp are inverted between ref and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period
## Bin length
bin_width = c(0.2, 0.2)
## Bias correction
## Step 1 : construction of the class dOTC
dotc = SBCK::dOTC$new( bin_width )
## Step 2 : Fit the bias correction model
dotc$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction, Z is a list containing
## corrections
Z = dotc\predict(X1,X0)
Z$Z0 ## Correction in calibration period
Z$Z1 ## Correction in projection period
```

dTSMBC

dTSMBC (dynamical Time Shifted Multivariate Bias Correction)

## Description

Perform a bias correction of auto-correlation

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#### **Details**

Correct auto-correlation with a shift approach, taking into account of non stationarity.

#### **Public fields**

```
shift [Shift class] Shift class to shift data.
bc_method [SBCK::BC_method] Underlying bias correction method.
```

#### **Active bindings**

```
method [character] If inverse is by row or column, see class Shift ref [integer] reference column/row to inverse shift, see class Shift. Default is 0.5 * (lag+1)
```

#### Methods

#### **Public methods:**

```
dTSMBC$new()
```

- dTSMBC\$fit()
- dTSMBC\$predict()
- dTSMBC\$clone()

**Method** new(): Create a new dTSMBC object.

```
Usage:

dTSMBC$new(lag, bc_method = dOTC, method = "row", ref = "middle", ...)

Arguments:

lag [integer] max lag of autocorrelation

bc_method [SBCK::BC_METHOD] bias correction method to use after shift of data, default is

OTC

method [character] If inverse is by row or column, see class Shift

ref [integer] reference column/row to inverse shift, see class Shift. Default is 0.5 * (lag+1)

... [] All others arguments are passed to bc_method
```

Returns: A new 'dTSMBC' object.

```
Method fit(): Fit the bias correction method
```

```
Usage:
dTSMBC$fit(Y0, X0, X1)

Arguments:
Y0 [matrix: n_samples * n_features] Observations in calibration
X0 [matrix: n_samples * n_features] Model in calibration
X1 [matrix: n_samples * n_features] Model in projection

Returns: NULL
```

Method predict(): Predict the correction

Usage:

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```
dTSMBC$predict(X1, X0 = NULL)
Arguments:
X1 [matrix: n_samples * n_features] Model in projection
X0 [matrix: n_samples * n_features or NULL] Model in calibration
```

*Returns:* [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list containing Z1 and Z0, the corrections of X1 and X0

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
dTSMBC$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Robin, Y. and Vrac, M.: Is time a variable like the others in multivariate statistical downscaling and bias correction?, Earth Syst. Dynam. Discuss. [preprint], https://doi.org/10.5194/esd-2021-12, in review, 2021.

```
## arima model parameters
modelX0 = list( ar = base::c( 0.6 , 0.2 , -0.1 ) )
modelX1 = list( ar = base::c( 0.4 , 0.1 , -0.3 ) )
modelY0 = list( ar = base::c( -0.3 , 0.4 , -0.2 ) )
## arima random generator
rand.genX0 = function(n){ return(stats::rnorm( n , mean = 0.2 , sd = 1 )) }
rand.genX1 = function(n){ return(stats::rnorm( n , mean = 0.8 , sd = 1 )) }
rand.genY0 = function(n){ return(stats::rnorm( n , mean = 0 , sd = 0.7 )) }
## Generate two AR processes
X0 = stats::arima.sim( n = 1000 , model = modelX0 , rand.gen = rand.genX0 )
X1 = stats::arima.sim( n = 1000 , model = modelX1 , rand.gen = rand.genX1 )
Y0 = stats::arima.sim( n = 1000 , model = modelY0 , rand.gen = rand.genY0 )
X0 = as.vector(X0)
X1 = as.vector(X1)
Y0 = as.vector(Y0 + 5)
## And correct it with 30 lags
dtsbc = SBCK::dTSMBC$new( 30 )
dtsbc$fit( Y0 , X0 , X1 )
Z = dtsbc\predict(X1,X0)
```

ECBC ECBC

**ECBC** 

ECBC (Empirical Copula Bias Correction) method

### **Description**

Perform a multivariate (non stationary) bias correction.

#### **Details**

use Schaake shuffle

## Super class

```
SBCK::CDFt -> ECBC
```

#### Methods

#### **Public methods:**

```
• ECBC$new()
```

- ECBC\$fit()
- ECBC\$predict()
- ECBC\$clone()

• ECBC2CTOLIG()

```
Method new(): Create a new ECBC object.
```

```
Usage:
```

```
ECBC$new(...)
```

Arguments:

... This class is based to CDFt, and takes the same arguments.

Returns: A new 'ECBC' object.

#### **Method** fit(): Fit the bias correction method

```
Usage:
```

```
ECBC$fit(Y0, X0, X1)
```

Arguments:

Y0 [matrix: n\_samples \* n\_features] Observations in calibration

X0 [matrix: n\_samples \* n\_features] Model in calibration

X1 [matrix: n\_samples \* n\_features] Model in projection

Returns: NULL

## Method predict(): Predict the correction

Usage:

```
ECBC$predict(X1, X0 = NULL)
```

Arguments:

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```
X1 [matrix: n_samples * n_features] Model in projectionX0 [matrix: n_samples * n_features or NULL] Model in calibration
```

*Returns:* [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list containing Z1 and Z0, the corrections of X1 and X0

Method clone(): The objects of this class are cloneable with this method.

```
Usage:
ECBC$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Vrac, M. and P. Friederichs, 2015: Multivariate—Intervariable, Spatial, and Temporal—Bias Correction. J. Climate, 28, 218–237, https://doi.org/10.1175/JCLI-D-14-00059.1

#### **Examples**

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)

XY = SBCK::dataset_gaussian_exp_2d(2000)

X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period

## Step 1 : construction of the class ECBC
ecbc = SBCK::ECBC$new()

## Step 2 : Fit the bias correction model
ecbc$fit( Y0 , X0 , X1 )

## Step 3 : perform the bias correction
Z = ecbc$predict(X1,X0)
```

energy

Energy distance

#### **Description**

Compute Energy distance between two dataset or SparseHist X and Y

# Usage

```
energy(X, Y, p = 2, metric = "euclidean")
```

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# Arguments

```
X [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)

Y [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)

p [float] power of energy distance, default is 2.

metric [str or function] metric for pairwise distance, default is "euclidean", see SBCK::pairwise_distances
```

#### Value

[float] value of distance

## **Examples**

```
X = base::cbind( stats::rnorm(2000) , stats::rnorm(2000) )
Y = base::cbind( stats::rnorm(2000,mean=10) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four are equals
w2 = SBCK::energy(X,Y)
w2 = SBCK::energy(muX,Y)
w2 = SBCK::energy(x,muY)
w2 = SBCK::energy(muX,muY)
```

euclidean

Euclidean distance

# Description

Compute Euclidean distance between two dataset or SparseHist X and Y

#### Usage

```
euclidean(X, Y)
```

#### **Arguments**

```
X [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
Y [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
```

#### Value

[float] value of distance

IdBC 25

#### **Examples**

```
X = base::cbind( stats::rnorm(2000) , stats::rnorm(2000) )
Y = base::cbind( stats::rnorm(2000,mean=2) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four are equals
d = SBCK::euclidean( X , Y )
d = SBCK::euclidean(muX , Y )
d = SBCK::euclidean(muX , muY )
d = SBCK::euclidean(muX , muY )
```

IdBC

IdBC (Identity Bias Correction) method

# **Description**

Always return X1 / X0 as correction.

#### **Details**

Only for comparison.

# Methods

#### **Public methods:**

```
• IdBC$new()
```

- IdBC\$fit()
- IdBC\$predict()
- IdBC\$clone()

**Method** new(): Create a new IdBC object.

```
Usage:
IdBC$new()
```

Returns: A new 'IdBC' object.

Method fit(): Fit the bias correction method

```
Usage:
```

```
IdBC\$fit(Y0, X0, X1 = NULL)
```

Arguments:

```
Y0 [matrix: n_samples * n_features] Observations in calibration
```

X0 [matrix: n\_samples \* n\_features] Model in calibration

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```
X1 [matrix: n_samples * n_features] Model in projection, can be NULL for stationary BC
     method
 Returns: NULL
Method predict(): Predict the correction. Use named keywords to use stationary or non-
stationary method.
 Usage:
 IdBC$predict(X1 = NULL, X0 = NULL)
 Arguments:
 X1 [matrix: n_samples * n_features or NULL] Model in projection
 X0 [matrix: n_samples * n_features or NULL] Model in calibration
 Returns: [matrix or list] Return X1 and / or X0
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 IdBC$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

#### **Examples**

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period

## Step 1 : construction of the class IdBC
idbc = SBCK::IdBC$new()
## Step 2 : Fit the bias correction model
idbc$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction
Z = idbc$predict(X1,X0)
## Z$Z0 # == X0
## Z$Z1 # == X1
```

manhattan

Manhattan distance

#### **Description**

Compute Manhattan distance between two dataset or SparseHist X and Y

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#### Usage

```
manhattan(X, Y)
```

#### **Arguments**

```
X [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
Y [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
```

#### Value

[float] value of distance

## **Examples**

```
X = base::cbind( stats::rnorm(2000) , stats::rnorm(2000) )
Y = base::cbind( stats::rnorm(2000,mean=2) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four are equals
d = SBCK::manhattan( X , Y )
d = SBCK::manhattan(muX , Y )
d = SBCK::manhattan(muX , muY )
d = SBCK::manhattan(muX , muY )
```

MBCn

MBCn (Multivariate Bias Correction)

## **Description**

Perform a multivariate bias correction.

#### **Details**

BC is performed with an alternance of rotation and univariate BC.

## **Public fields**

```
n_features [integer] Numbers of features
bc [BC class] Univariate BC method
metric [function] distance between two datasets
iter_slope [Stopping class criteria] class used to test when stop
bc_params [list] Parameters of bc
ortho_mat [array] Array of orthogonal matrix
tips [array] Array which contains the product of ortho and inverse of next
lbc [list] list of BC method used.
```

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#### Methods

```
Public methods:
  • MBCn$new()
  • MBCn$fit()
  • MBCn$predict()
  • MBCn$clone()
Method new(): Create a new MBCn object.
 Usage:
 MBCn$new(
   bc = QDM,
   metric = wasserstein,
    stopping_criteria = SlopeStoppingCriteria,
    stopping_criteria_params = list(minit = 20, maxit = 100, tol = 0.001),
 )
 Arguments:
 bc [BC class] Univariate bias correction method
 metric [function] distance between two datasets
 stopping_criteria [Stopping class criteria] class use to test when to stop the iterations
 stopping_criteria_params [list] parameters passed to stopping_criteria class
 ... [] Others arguments passed to bc.
 Returns: A new 'MBCn' object.
Method fit(): Fit the bias correction method
 Usage:
 MBCn$fit(Y0, X0, X1)
 Arguments:
 Y0 [matrix: n_samples * n_features] Observations in calibration
 X0 [matrix: n_samples * n_features] Model in calibration
 X1 [matrix: n_samples * n_features] Model in projection
 Returns: NULL
Method predict(): Predict the correction
 Usage:
 MBCn$predict(X1, X0 = NULL)
 Arguments:
 X1 [matrix: n_samples * n_features] Model in projection
 X0 [matrix: n_samples * n_features or NULL] Model in calibration
 Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list
 containing Z1 and Z0, the corrections of X1 and X0
```

Method clone(): The objects of this class are cloneable with this method.

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```
Usage:
MBCn$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Cannon, A. J., Sobie, S. R., and Murdock, T. Q.: Bias correction of simulated precipitation by quantile mapping: how well do methods preserve relative changes in quantiles and extremes?, J. Climate, 28, 6938–6959, https://doi.org/10.1175/JCLI-D-14-00754.1, 2015.

#### **Examples**

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)
XY = SBCK::dataset_gaussian_exp_2d(200)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period
## Bias correction
## Step 1 : construction of the class MBCn
mbcn = SBCK::MBCn$new()
## Step 2 : Fit the bias correction model
mbcn$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction, Z is a list containing
## corrections
Z = mbcnpredict(X1.X0)
Z$Z0 ## Correction in calibration period
Z$Z1 ## Correction in projection period
```

minkowski

Minkowski distance

## **Description**

Compute Minkowski distance between two dataset or SparseHist X and Y. If p = 2, it is the Euclidean distance, for p = 1, it is the manhattan distance, if p = Inf, chebyshev distance is called.

# Usage

```
minkowski(X, Y, p = 2)
```

#### **Arguments**

```
X [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
Y [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
p [float] power of distance
```

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#### Value

[float] value of distance

#### **Examples**

```
X = base::cbind( stats::rnorm(2000) , stats::rnorm(2000) )
Y = base::cbind( stats::rnorm(2000,mean=2) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four are equals
d = SBCK::minkowski( X , Y , p = 3 )
d = SBCK::minkowski(muX , Y , p = 3 )
d = SBCK::minkowski( X , muY , p = 3 )
d = SBCK::minkowski(muX , muY , p = 3 )
```

MRec

MRec (Matrix Recorrelation) method

# **Description**

Perform a multivariate bias correction with Gaussian assumption.

#### **Details**

Only pearson correlations are corrected.

#### **Public fields**

n\_features [integer] Numbers of features

#### Methods

#### **Public methods:**

- MRec\$new()
- MRec\$fit()
- MRec\$predict()
- MRec\$clone()

Method new(): Create a new MRec object.

```
Usage:
```

```
MRec$new(distY = NULL, distX = NULL)
```

Arguments:

distY [A list of ROOPSD distribution or NULL] Describe the law of each margins. A list permit to use different laws for each margins. Default is empirical.

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distX [A list of ROOPSD distribution or NULL] Describe the law of each margins. A list permit to use different laws for each margins. Default is empirical. Returns: A new 'MRec' object. Method fit(): Fit the bias correction method Usage: MRec\$fit(Y0, X0, X1) Arguments: Y0 [matrix: n\_samples \* n\_features] Observations in calibration X0 [matrix: n\_samples \* n\_features] Model in calibration X1 [matrix: n\_samples \* n\_features] Model in projection Returns: NULL Method predict(): Predict the correction Usage: MRec\$predict(X1, X0 = NULL) Arguments: X1 [matrix: n\_samples \* n\_features] Model in projection X0 [matrix: n\_samples \* n\_features or NULL] Model in calibration Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list

**Method** clone(): The objects of this class are cloneable with this method.

containing Z1 and Z0, the corrections of X1 and X0

```
Usage:
MRec$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Bárdossy, A. and Pegram, G.: Multiscale spatial recorrelation of RCM precipitation to produce unbiased climate change scenarios over large areas and small, Water Resources Research, 48, 9502–, https://doi.org/10.1029/2011WR011524, 2012.

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)

XY = SBCK::dataset_gaussian_exp_2d(2000)

X0 = XY$X0 ## Biased in calibration period

Y0 = XY$Y0 ## Reference in calibration period

X1 = XY$X1 ## Biased in projection period

## Bias correction

## Step 1 : construction of the class MRec

mrec = SBCK::MRec$new()
```

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```
## Step 2 : Fit the bias correction model
mrec$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction, Z is a list containing corrections.
Z = mrec$predict(X1,X0) ## X0 is optional, in this case Z0 is NULL
Z$Z0 ## Correction in calibration period
Z$Z1 ## Correction in projection period
```

MVQuantilesShuffle

MVQuantilesShuffle

## **Description**

Multivariate Schaake shuffle using the quantiles.

#### **Details**

Used to reproduce the dependence structure of a dataset to another dataset

#### **Public fields**

```
col_cond [vector] Conditionning columns

col_ucond [vector] Un-conditionning columns

lag_search [integer] Number of lags to transform the dependence structure

lag_keep [integer] Number of lags to keep

n_features [integer] Number of features (dimensions), internal

qY [matrix] Quantile structure fitted, internal

bsyc [matrix] Block search fitted, internal
```

#### Methods

#### **Public methods:**

- MVQuantilesShuffle\$new()
- MVQuantilesShuffle\$fit()
- MVQuantilesShuffle\$transform()
- MVQuantilesShuffle\$clone()

**Method** new(): Create a new MVQuantilesShuffle object.

```
Usage:
MVQuantilesShuffle$new(col_cond = base::c(1), lag_search = 1, lag_keep = 1)
Arguments:
col_cond Conditionning colum
lag_search Number of lags to transform the dependence structure
lag_keep Number of lags to keep
```

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```
Method fit(): Fit method
 Usage:
 MVQuantilesShuffle$fit(Y)
 Arguments:
 Y [vector] Dataset to infer the dependance structure
 Returns: NULL
Method transform(): Transform method
 Usage:
 MVQuantilesShuffle$transform(X)
 Arguments:
 X [vector] Dataset to match the dependance structure with the Y fitted
 Returns: Z The X with the quantiles structure of Y
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 MVQuantilesShuffle$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

Returns: A new 'MVQuantilesShuffle' object.

#### References

Vrac, M. et S. Thao (2020). "R2 D2 v2.0 : accounting for temporal dependences in multivariate bias correction via analogue rank resampling". In : Geosci. Model Dev. 13.11, p. 5367-5387. doi :10.5194/gmd-13-5367-2020.

```
## Generate sample
X = matrix( stats::rnorm( n = 100 ) , ncol = 4 )
Y = matrix( stats::rnorm( n = 100 ) , ncol = 4 )

## Fit dependence structure
## Assume that the link beween column 2 and 4 is correct, and change also
## the auto-correlation structure until lag 3 = lag_keep - 1
mvq = MVQuantilesShuffle$new( base::c(2,4) , lag_search = 6 , lag_keep = 4 )
mvq$fit(Y)
Z = mvq$transform(X)
```

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MVRanksShuffle

MVRanksShuffle

#### **Description**

Multivariate Schaake shuffle using the ranks.

#### **Details**

Used to reproduce the dependence structure of a dataset to another dataset

#### **Public fields**

```
col_cond [vector] Conditionning columns
col_ucond [vector] Un-conditionning columns
lag_search [integer] Number of lags to transform the dependence structure
lag_keep [integer] Number of lags to keep
n_features [integer] Number of features (dimensions), internal
qY [matrix] Ranks structure fitted, internal
bsYc [matrix] Block search fitted, internal
```

#### Methods

#### **Public methods:**

```
• MVRanksShuffle$new()
```

- MVRanksShuffle\$fit()
- MVRanksShuffle\$transform()
- MVRanksShuffle\$clone()

```
Method new(): Create a new MVRanksShuffle object.
```

```
Usage:
 MVRanksShuffle$new(col_cond = base::c(1), lag_search = 1, lag_keep = 1)
 Arguments:
 col_cond Conditionning colum
 lag_search Number of lags to transform the dependence structure
 lag_keep Number of lags to keep
 Returns: A new 'MVRanksShuffle' object.
Method fit(): Fit method
```

MVRanksShuffle\$fit(Y)

Arguments:

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Y [vector] Dataset to infer the dependance structure

Returns: NULL

Method transform(): Transform method

Usage:

MVRanksShuffle\$transform(X)

Arguments:

X [vector] Dataset to match the dependance structure with the Y fitted

Returns: Z The X with the quantiles structure of Y

**Method** clone(): The objects of this class are cloneable with this method.

Usage:

MVRanksShuffle\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

#### References

Vrac, M. et S. Thao (2020). "R2 D2 v2.0: accounting for temporal dependences in multivariate bias correction via analogue rank resampling". In: Geosci. Model Dev. 13.11, p. 5367-5387. doi:10.5194/gmd-13-5367-2020.

#### **Examples**

```
## Generate sample
X = matrix( stats::rnorm( n = 100 ) , ncol = 4 )
Y = matrix( stats::rnorm( n = 100 ) , ncol = 4 )

## Fit dependence structure
## Assume that the link beween column 2 and 4 is correct, and change also
## the auto-correlation structure until lag 3 = lag_keep - 1
mvr = MVRanksShuffle$new( base::c(2,4) , lag_search = 6 , lag_keep = 4 )
mvr$fit(Y)
Z = mvr$transform(X)
```

OTC

OTC (Optimal Transport Correction) method

## **Description**

Perform a multivariate bias correction of X0 with respect to Y0.

#### Details

Joint distribution, i.e. all dependence are corrected.

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#### **Public fields**

bin\_width [vector or NULL] A vector of lengths of the cells discretizing R^numbers of variables.
 If NULL, it is estimating during the fit
 bin\_origin [vector or NULL] Coordinate of lower corner of one cell. If NULL, c(0,...,0) is used
 muX [SparseHist] Histogram of the data from the model
 muY [SparseHist] Histogram of the data from the observations
 ot [OTSolver] Optimal Transport solver, default is the network simplex
 plan [matrix] The plan computed by the ot solver.
 n\_features [integer] Numbers of features

#### Methods

#### **Public methods:**

- OTC\$new()
- OTC\$fit()
- OTC\$predict()
- OTC\$clone()

**Method** new(): Create a new OTC object.

```
Usage:
```

OTC\$new(bin\_width = NULL, bin\_origin = NULL, ot = SBCK::OTNetworkSimplex\$new())

Arguments:

bin\_width [vector or NULL] A vector of lengths of the cells discretizing R^numbers of variables. If NULL, it is estimating during the fit

bin\_origin [vector or NULL] Coordinate of lower corner of one cell. If NULL, c(0,...,0) is used

ot [OTSolver] Optimal Transport solver, default is the network simplex

Returns: A new 'OTC' object.

# Method fit(): Fit the bias correction method

Usage:

OTC\$fit(Y0, X0)

Arguments:

Y0 [matrix: n\_samples \* n\_features] Observations in calibration

X0 [matrix: n\_samples \* n\_features] Model in calibration

Returns: NULL

## Method predict(): Predict the correction

Note: Only the center of the bins associated to the corrected points are returned, but all corrections of the form:  $bw = otc bin_width / 2 = base::prod(base::dim(X0)) = Z0 = otc predict(X0) = Z0 + t(matrix(stats::runif(n = n min = -bw, max = bw), ncol = dim(X0)[1]) ) are equivalent for OTC.$  OTHist 37

```
Usage:

OTC$predict(X0)

Arguments:

X0 [matrix: n_samples * n_features or NULL] Model in calibration

Returns: [matrix] Return the corrections of X0

Method clone(): The objects of this class are cloneable with this method.

Usage:

OTC$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.
```

## References

Robin, Y., Vrac, M., Naveau, P., Yiou, P.: Multivariate stochastic bias corrections with optimal transport, Hydrol. Earth Syst. Sci., 23, 773–786, 2019, https://doi.org/10.5194/hess-23-773-2019

## **Examples**

```
## Two bivariate random variables (rnorm and rexp are inverted between ref
## and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
## Bin length
bin_width = SBCK::bin_width_estimator( list(X0,Y0) )
## Step 1 : construction of the class OTC
otc = SBCK::OTC$new( bin_width )
## Step 2 : Fit the bias correction model
otc$fit( Y0 , X0 )
## Step 3 : perform the bias correction, Z0 is the correction of
## X0 with respect to the estimation of Y0
Z0 = otc$predict(X0)
```

OTHist

Optimal Transport Histogram

# Description

Histogram

# **Details**

Just a generic class which contains two arguments, p (probability) and c (center of bins)

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## **Public fields**

```
    p [vector] Vector of probability
    c [matrix] Vector of center of bins, with nrow = n_samples and ncol = n_features
    bin_width [vector or NULL] A vector of lengths of the cells discretizing R^numbers of variables.
        If NULL, it is estimating during the fit
    bin_origin [vector or NULL] Coordinate of lower corner of one cell. If NULL, c(0,...,0) is used
```

## Methods

## **Public methods:**

```
• OTHist$new()
```

• OTHist\$clone()

```
Method new(): Create a new OTHist object.
```

```
Usage:
OTHist$new(p, c)
Arguments:
p [vector] Vector of probability
c [matrix] Vector of center of bins, with nrow = n_samples and ncol = n_features
Returns: A new 'OTHist' object.
```

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
OTHist$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

```
## Build a random discrete probability distribution
p = stats::rnorm(100)
p = p / base::sum(p)
c = base::seq( -1 , 1 , length = 100 )
mu = OTHist$new( p , c )
```

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OTNetworkSimplex

Optimal Transport Network Simplex solver

#### **Description**

Solve the optimal transport problem with the package 'transport'

#### **Details**

use the network simplex algorithm

#### **Public fields**

```
p [double] Power of the planplan [matrix] transport plansuccess [bool] If the fit is a success or notC [matrix] Cost matrix
```

#### Methods

#### **Public methods:**

```
• OTNetworkSimplex$new()
```

- OTNetworkSimplex\$fit()
- OTNetworkSimplex\$clone()

**Method** new(): Create a new OTNetworkSimplex object.

```
Usage:
OTNetworkSimplex$new(p = 2)
Arguments:
```

Returns: A new 'OTNetworkSimplex' object.

```
Method fit(): Fit the OT plan
```

p [double] Power of the plan

Usage:

OTNetworkSimplex\$fit(muX0, muX1, C = NULL)

Arguments:

muX0 [SparseHist or OTHist] Source histogram to move

muX1 [SparseHist or OTHist] Target histogram

C [matrix or NULL] Cost matrix (without power p) between muX0 and muX1, if NULL pairwise\_distances is called with Euclidean distance.

Returns: NULL

Method clone(): The objects of this class are cloneable with this method.

40 pairwise\_distances

```
Usage:
OTNetworkSimplex$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Bazaraa, M. S., Jarvis, J. J., and Sherali, H. D.: Linear Programming and Network Flows, 4th edn., John Wiley & Sons, 2009.

# Examples

```
## Define two dataset
X = stats::rnorm(2000)
Y = stats::rnorm(2000 , mean = 5 )
bw = base::c(0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## Find solution
ot = OTNetworkSimplex$new()
ot$fit( muX , muY )

print( sum(ot$plan) ) ## Must be equal to 1
print( ot$success ) ## If solve is success
print( sqrt(sum(ot$plan * ot$C)) ) ## Cost of plan
```

pairwise\_distances

Pairwise distances

## **Description**

Compute the matrix of pairwise distances between a matrix X and a matrix Y

## Usage

```
pairwise_distances(X,Y,metric)
```

## **Arguments**

	r	1 4 6	, <b>1</b> .	C
<b>V</b>	Imotriv	I A tiret matrix i	complet in row	tanturas in columns)
Λ	HHIALITAT	i A ilist matrix t	isannuics in tuw.	features in columns).

Y [matrix] A second matrix (samples in row, features in columns). If Y = NULL,

then pairwise distances is computed between X and X

metric [string or callable] The metric used. If metric is a string, then metric is com-

piled (so faster). Available string are: "euclidean", "sqeuclidean" (Square of Euclidean distance), "logeulidean" (log of the Euclidean distance) and "chebyshev" (max). Callable must be a function taking two vectors and returning a

double.

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# Value

distXY [matrix] Pairwise distances. distXY[i,j] is the distance between X[i,] and Y[j,]

## **Examples**

```
X = matrix( stats::rnorm(200) , ncol = 100 , nrow = 2 )
Y = matrix( stats::rexp(300) , ncol = 150 , nrow = 2 )
distXY = SBCK::pairwise_distances( X , Y )
```

**PPPDiffRef** 

**PPPDiffRef** 

## **Description**

Apply the diff w.r.t. a ref transformation.

#### **Details**

Transform a dataset such that all 'lower' dimensions are replaced by the 'ref' dimension minus the 'lower'; and all 'upper' dimensions are replaced by 'upper' minus 'ref'.

# Super class

```
SBCK::PrePostProcessing -> PPPDiffRef
```

## **Public fields**

```
ref [integer] The reference column
lower [vector integer] Dimensions lower than ref
upper [vector integer] Dimensions upper than ref
```

#### Methods

#### **Public methods:**

- PPPDiffRef\$new()
- PPPDiffRef\$transform()
- PPPDiffRef\$itransform()
- PPPDiffRef\$clone()

Method new(): Create a new PPPDiffRef object.

```
Usage:
PPPDiffRef$new(ref, lower = NULL, upper = NULL, ...)
Arguments:
```

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```
ref The reference column
 lower Dimensions lower than ref
 upper Dimensions upper than ref
 ... Others arguments are passed to PrePostProcessing
 Returns: A new 'PPPDiffRef' object.
Method transform(): Apply the DiffRef transform.
 PPPDiffRef$transform(X)
 Arguments:
 X Data to transform
 Returns: Xt a transformed matrix
Method itransform(): Apply the DiffRef inverse transform.
 Usage:
 PPPDiffRef$itransform(Xt)
 Arguments:
 Xt Data to transform
 Returns: X a transformed matrix
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 PPPDiffRef$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

```
## Parameters
size = 2000
nfeat = 5
sign = base::sample( base::c(-1,1) , nfeat - 1 , replace = TRUE )
## Build data
     = matrix( stats::rnorm( n = size ) , ncol = 1 )
for( s in sign )
X = base::cbind(X, X[,1] + s * base::abs(matrix(stats::rnorm(n = size), ncol = 1)))
}
## PPP
lower = which( sign == 1 ) + 1
upper = which( sign == -1 ) + 1
ppp = SBCK::PPPDiffRef$new( ref = 1 , lower = lower , upper = upper )
     = ppp$transform(X)
     = ppp$itransform(Xt)
print( base::max( base::abs( X - Xti ) ) )
```

PPPFunctionLink 43

PPPFunctionLink

**PPPFunctionLink** 

## Description

Base class to build link function pre-post processing class. See also the PrePostProcessing documentation

## **Details**

This class is used to define pre/post processing class with a link function and its inverse. See example.

## Super class

```
SBCK::PrePostProcessing -> PPPFunctionLink
```

#### Methods

#### **Public methods:**

- PPPFunctionLink\$new()
- PPPFunctionLink\$transform()
- PPPFunctionLink\$itransform()
- PPPFunctionLink\$clone()

```
Method new(): Create a new PPPFunctionLink object.
```

```
Usage:
```

```
PPPFunctionLink$new(transform_, itransform_, cols = NULL, ...)
```

## Arguments:

transform\_ The transform function

itransform\_ The inverse transform function

cols Columns to apply the link function

... Others arguments are passed to PrePostProcessing

Returns: A new 'PPPFunctionLink' object.

**Method** transform(): Apply the transform.

Usage:

PPPFunctionLink\$transform(X)

Arguments:

X Data to transform

Returns: Xt a transformed matrix

**Method** itransform(): Apply the inverse transform.

PPPLogLinLink

```
Usage:
PPPFunctionLink$itransform(Xt)
Arguments:
Xt Data to transform
Returns: X a transformed matrix

Method clone(): The objects of this class are cloneable with this method.
Usage:
PPPFunctionLink$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

# **Examples**

PPPLogLinLink

**PPPLogLinLink** 

# Description

Log linear link function. See also the PrePostProcessing documentation.

## **Details**

Log linear link function. The transform is log(x) if 0 < x < 1, else x - 1, and the inverse transform exp(x) if x < 0, else x + 1.

PPPLogLinLink 45

## Super classes

```
SBCK::PrePostProcessing -> SBCK::PPPFunctionLink -> PPPLogLinLink
```

#### Methods

```
Public methods:
```

```
• PPPLogLinLink$new()
```

```
• PPPLogLinLink$clone()
```

```
Method new(): Create a new PPPLogLinLink object.
```

```
Usage:

PPPLogLinLink$new(s = 1e-05, cols = NULL, ...)

Arguments:

s The value where the function jump from exp to linear cols Columns to apply the link function
... Others arguments are passed to PrePostProcessing

Returns: A new 'PPPLogLinLink' object.
```

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
PPPLogLinLink$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

46 PPPPreserveOrder

PPPPreserveOrder

**PPPPreserveOrder** 

## **Description**

Set an order between cols, and preserve it by swapping values after the correction

## **Details**

Set an order between cols, and preserve it by swapping values after the correction

# Super class

```
SBCK::PrePostProcessing -> PPPPreserveOrder
```

#### Methods

#### **Public methods:**

```
• PPPPreserveOrder$new()
```

- PPPPreserveOrder\$transform()
- PPPPreserveOrder\$itransform()
- PPPPreserveOrder\$clone()

```
Method new(): Create a new PPPPreserveOrder object.
```

```
Usage:
 PPPPreserveOrder$new(cols = NULL, ...)
 Arguments:
 cols The columns to keep the order
 ... Others arguments are passed to PrePostProcessing
 Returns: A new 'PPPPreserveOrder' object.
Method transform(): nothing occur here
```

Usage:

PPPPreserveOrder\$transform(X)

Arguments:

X Data to transform

Returns: Xt a transformed matrix

Method itransform(): sort along cols

Usage:

PPPPreserveOrder\$itransform(Xt)

Arguments:

Xt Data to transform

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Returns: X a transformed matrix

**Method** clone(): The objects of this class are cloneable with this method.

```
Usage:
PPPPreserveOrder$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

# **Examples**

```
## Build data
X = matrix( stats::rnorm( n = 20 ) , ncol = 2 )
## PPP
ppp = SBCK::PPPPreserveOrder$new( cols = base::c(1,2) )
Xt = ppp$transform(X) ## Nothing
Xti = ppp$itransform(Xt) ## Order
```

PPPSquareLink

**PPPSquareLink** 

## **Description**

Square link function. See also the PrePostProcessing documentation.

## **Details**

Square link function. The transform is  $x^2$ , and the sign(x) \* sqrt(abs(x)) its inverse.

# Super classes

```
SBCK::PrePostProcessing -> SBCK::PPPFunctionLink -> PPPSquareLink
```

# Methods

## **Public methods:**

- PPPSquareLink\$new()
- PPPSquareLink\$clone()

Method new(): Create a new PPPSquareLink object.

```
Usage:
PPPSquareLink$new(cols = NULL, ...)
Arguments:
cols Columns to apply the link function
... Others arguments are passed to PrePostProcessing
```

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```
Returns: A new 'PPPSquareLink' object.
```

Method clone(): The objects of this class are cloneable with this method.

```
Usage:
PPPSquareLink$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

## **Examples**

```
## Start with data
XY = SBCK::dataset_like_tas_pr(2000)
X0 = XY$X0
X1 = XY$X1
Y0 = XY$Y0

## Define the PPP method
ppp = PPPSquareLink$new( bc_method = CDFt , cols = 2 )

## And now the correction
## Bias correction
ppp$fit(Y0,X0,X1)
Z = ppp$predict(X1,X0)
```

**PPPSSR** 

**PPPSSR** 

## **Description**

Apply the SSR transformation.

## **Details**

Apply the SSR transformation. The SSR transformation replace the 0 by a random values between 0 and the minimal non zero value (the threshold). The inverse transform replace all values lower than the threshold by 0. The threshold used for inverse transform is given by the keyword 'isaved', which takes the value 'Y0' (reference in calibration period), or 'X0' (biased in calibration period), or 'X1' (biased in projection period)

# Super class

```
SBCK::PrePostProcessing -> PPPSSR
```

## **Public fields**

```
Xn [vector] Threshold
```

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## Methods

```
Public methods:
```

```
• PPPSSR$new()
```

- PPPSSR\$transform()
- PPPSSR\$itransform()
- PPPSSR\$clone()

Method new(): Create a new PPPSSR object.

```
Usage:

PPPSSR$new(cols = NULL, isaved = "Y0", ...)

Arguments:

cols Columns to apply the SSR

isaved Choose the threshold used for the inverse transform. Can be "Y0", "X0" and "X1".

... Others arguments are passed to PrePostProcessing
```

Returns: A new 'PPPSSR' object.

**Method** transform(): Apply the SSR transform, i.e. all 0 are replaced by random values between 0 (excluded) and the minimal non zero value.

Usage:
PPPSSR\$transform(X)

Arguments:
X Data to transform

Returns: Xt a transformed matrix

**Method** itransform(): Apply the inverse SSR transform, i.e. all values lower than the threshold found in the transform function are replaced by 0.

```
Usage:
PPPSSR$itransform(Xt)

Arguments:
Xt Data to transform

Returns: X a transformed matrix
```

Method clone(): The objects of this class are cloneable with this method.

```
Usage:
PPPSSR$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

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## **Examples**

```
## Start with data
XY = SBCK::dataset_like_tas_pr(2000)
X0 = XY$X0
X1 = XY$X1
Y0 = XY$Y0

## Define the PPP method
ppp = PPPSSR$new( bc_method = CDFt , cols = 2 )

## And now the correction
## Bias correction
ppp$fit(Y0,X0,X1)
Z = ppp$predict(X1,X0)
```

PrePostProcessing

PrePostProcessing base class

# **Description**

Base class to pre/post process data before/after a bias correction

#### **Details**

This base class can be considered as the identity pre-post processing, and is used to be herited by others pre/post processing class. The key ideas are:

- A PrePostProcessing based class contains a bias correction method, initalized by the 'bc\_method' argument, always available for all herited class
- The 'pipe' keyword is a list of pre/post processing class, applied one after the other.

Try with an example, start with a dataset similar to tas/pr:

```
>> XY = SBCK::dataset_like_tas_pr(2000)
>> X0 = XY$X0
>> X1 = XY$X1
>> Y0 = XY$Y0
```

The first column is Gaussian, but the second is an exponential law with a Dirac mass at 0, represented the 0 of precipitations. For a quantile mapping correction in the calibration period, we just apply

```
»> qm = SBCK::QM$new()
»> qm$fit(Y0,X0)
»> Z0 = qm$predict(X0)
```

Now, if we want to pre-post process with the SSR method (0 are replaced by random values between 0 (excluded) and the minimal non zero value), we write:

```
»> ppp = SBCK::PPPSSR$new( bc_method = QM , cols = 2 )
```

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```
»> ppp$fit(Y0,X0)
»> Z0 = ppp$predict(X0)
```

The SSR approach is applied only on the second column (the precipitation), and the syntax is the same than for a simple bias correction method.

Imagine now that we want to apply the SSR, and to ensure the positivity of CDFt for precipitation, we also want to use the LogLinLink pre-post processing method. This can be done with the following syntax:

```
»> ppp = PPPLogLinLink$new( bc_method = CDFt , cols = 2 ,
»> pipe = list(PPPSSR) ,
»> pipe_kwargs = list( list(cols = 2) ) )
»> ppp$fit(Y0,X0,X1)
»> Z = ppp$predict(X1,X0)
```

With this syntax, the pre processing operation is PPPLogLinLink\$transform(PPPSSR\$transform(data)) and post processing operation PPPSSR\$itransform(PPPLogLinLink\$itransform(bc\_data)). So the formula can read from right to left (as the mathematical composition). Note it is equivalent to define:

```
»> ppp = PrePostProcessing$new( bc_method = CDFt,
»> pipe = list(PPPLogLinLink,PPPSSR),
»> pipe_kwargs = list( list(cols=2) , list(cols=2) )
```

#### Methods

#### **Public methods:**

- PrePostProcessing\$new()
- PrePostProcessing\$transform()
- PrePostProcessing\$itransform()
- PrePostProcessing\$fit()
- PrePostProcessing\$predict()
- PrePostProcessing\$clone()

**Method** new(): Create a new PrePostProcessing object.

```
Usage:
PrePostProcessing$new(
    bc_method = NULL,
    bc_method_kwargs = list(),
    pipe = list(),
    pipe_kwargs = list()
)
Arguments:
bc_method The bias correction method
bc_method_kwargs Dict of keyword arguments passed to bc_method
pipe list of others PrePostProcessing class to pipe
```

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pipe\_kwargs list of list of keyword arguments passed to each elements of pipe Returns: A new 'PrePostProcessing' object. Method transform(): Transformation applied to data before the bias correction. Just the identity for this class Usage: PrePostProcessing\$transform(X) Arguments: X [matrix: n\_samples \* n\_features] Returns: Xt [matrix: n samples \* n features] **Method** itransform(): Transformation applied to data after the bias correction. Just the identity for this class Usage: PrePostProcessing\$itransform(Xt) Arguments: Xt [matrix: n\_samples \* n\_features] Returns: X [matrix: n\_samples \* n\_features] Method fit(): Apply the pre processing and fit the bias correction method. If X1 is NULL, the method is considered as stationary Usage: PrePostProcessing\$fit(Y0, X0, X1 = NULL) Arguments: Y0 [matrix: n\_samples \* n\_features] Observations in calibration X0 [matrix: n\_samples \* n\_features] Model in calibration X1 [matrix: n\_samples \* n\_features] Model in projection Returns: NULL **Method** predict(): Predict the correction, apply pre-processing before, and post-processing after Usage: PrePostProcessing\$predict(X1 = NULL, X0 = NULL) Arguments: X1 [matrix: n\_samples \* n\_features or NULL] Model in projection X0 [matrix: n\_samples \* n\_features or NULL] Model in calibration Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL (and vice-versa), else return a list containing Z1 and Z0, the corrections of X1 and X0 **Method** clone(): The objects of this class are cloneable with this method. Usage: PrePostProcessing\$clone(deep = FALSE) Arguments: deep Whether to make a deep clone.

QDM 53

## **Examples**

QDM

QDM (Quantile delta mapping method)

## **Description**

Perform a bias correction.

#### **Details**

Mix of delta and quantile method

## Methods

## **Public methods:**

- QDM\$new()
- QDM\$fit()
- QDM\$predict()
- QDM\$clone()

Method new(): Create a new QDM object.

```
Usage:
QDM$new(delta = "additive", ...)
Arguments:
delta [character or list] If character : "additive" or "multiplicative". If a list is given, delta[[1]]
    is the delta transform operator, and delta[[2]] its inverse.
... [] Named arguments passed to quantile mapping
Returns: A new 'QDM' object.
```

Method fit(): Fit the bias correction method

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```
Usage:
 QDM$fit(Y0, X0, X1)
 Arguments:
 Y0 [matrix: n_samples * n_features] Observations in calibration
 X0 [matrix: n_samples * n_features] Model in calibration
 X1 [matrix: n_samples * n_features] Model in projection
 Returns: NULL
Method predict(): Predict the correction
 Usage:
 QDM\$predict(X1, X0 = NULL)
 Arguments:
 X1 [matrix: n_samples * n_features] Model in projection
 X0 [matrix: n_samples * n_features or NULL] Model in calibration
 Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list
 containing Z1 and Z0, the corrections of X1 and X0
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 QDM$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

#### References

Cannon, A. J., Sobie, S. R., and Murdock, T. Q.: Bias correction of simulated precipitation by quantile mapping: how well do methods preserve relative changes in quantiles and extremes?, J. Climate, 28, 6938–6959, https://doi.org/10.1175/JCLI-D-14-00754.1, 2015.

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period
## Bias correction
## Step 1 : construction of the class QDM
qdm = SBCK::QDM$new()
## Step 2 : Fit the bias correction model
qdm$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction, Z is a list containing
## corrections
Z = qdm predict(X1, X0)
Z$Z0 ## Correction in calibration period
Z$Z1 ## Correction in projection period
```

QM 55

QM

Quantile Mapping method

## Description

Perform an univariate bias correction of X0 with respect to Y0

#### **Details**

Correction is applied margins by margins.

#### **Public fields**

distX0 [ROOPSD distribution or a list of them] Describe the law of each margins. A list permit to use different laws for each margins. Default is ROOPSD::rv\_histogram.

distY0 [ROOPSD distribution or a list of them] Describe the law of each margins. A list permit to use different laws for each margins. Default is ROOPSD::rv\_histogram.

n\_features [integer] Numbers of features

tol [double] Floatting point tolerance

#### Methods

## **Public methods:**

- QM\$new()
- QM\$fit()
- QM\$predict()
- QM\$clone()

Method new(): Create a new QM object.

```
Usage:
```

```
\label{eq:QMsnew} $$ QM$ new(distX0 = ROOPSD::rv\_histogram, distY0 = ROOPSD::rv\_histogram, \ldots)$
```

Arguments:

distX0 [ROOPSD distribution or a list of them] Describe the law of model

distY0 [ROOPSD distribution or a list of them] Describe the law of observations

... [] kwargsX0 or kwargsY0, arguments passed to distX0 and distY0

Returns: A new 'QM' object.

Method fit(): Fit the bias correction method

```
Usage:
```

```
QM\$fit(Y0 = NULL, X0 = NULL)
```

Arguments:

Y0 [matrix: n\_samples \* n\_features] Observations in calibration

X0 [matrix: n\_samples \* n\_features] Model in calibration

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```
Returns: NULL

Method predict(): Predict the correction
    Usage:
    QM$predict(X0)
    Arguments:
    X0 [matrix: n_samples * n_features or NULL] Model in calibration
    Returns: [matrix] Return the corrections of X0

Method clone(): The objects of this class are cloneable with this method.
    Usage:
    QM$clone(deep = FALSE)
    Arguments:
    deep Whether to make a deep clone.
```

#### References

Panofsky, H. A. and Brier, G. W.: Some applications of statistics to meteorology, Mineral Industries Extension Services, College of Mineral Industries, Pennsylvania State University, 103 pp., 1958.

Wood, A. W., Leung, L. R., Sridhar, V., and Lettenmaier, D. P.: Hydrologic Implications of Dynamical and Statistical Approaches to Downscaling Climate Model Outputs, Clim. Change, 62, 189–216, https://doi.org/10.1023/B:CLIM.0000013685.99609.9e, 2004.

Déqué, M.: Frequency of precipitation and temperature extremes over France in an anthropogenic scenario: Model results and statistical correction according to observed values, Global Planet. Change, 57, 16–26, https://doi.org/10.1016/j.gloplacha.2006.11.030, 2007.

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
## Bias correction
## Step 1 : construction of the class QM
qm = SBCK::QM$new()
## Step 2 : Fit the bias correction model
qm$fit( Y0 , X0 )
## Step 3 : perform the bias correction, Z0 is the correction of
## X0 with respect to the estimation of Y0
Z0 = qm$predict(X0)
# ## But in fact the laws are known, we can fit parameters:
distY0 = list( ROOPSD::Exponential , ROOPSD::Normal )
distX0 = list( ROOPSD::Normal , ROOPSD::Exponential )
qm_fix = SBCK::QM$new( distY0 = distY0 , distX0 = distX0 )
qm_fix$fit( Y0 , X0 )
Z0 = qm_fix predict(X0)
```

QMrs 57

QMrs

Quantile Mapping RankShuffle method

## **Description**

Perform a multivariate bias correction of X with respect to Y

#### **Details**

Dependence is corrected with multi\_schaake\_shuffle.

# Super class

```
SBCK::QM->QMrs
```

#### **Public fields**

irefs [vector of int] Indexes for shuffle. Defaults is base::c(1)

## Methods

## **Public methods:**

- QMrs\$new()
- QMrs\$fit()
- QMrs\$predict()
- QMrs\$clone()

Returns: NULL

Method new(): Create a new QMrs object.

```
Usage:
QMrs$new(irefs = base::c(1), ...)
Arguments:
irefs [vector of int] Indexes for shuffle. Def
```

irefs [vector of int] Indexes for shuffle. Defaults is base::c(1) model ... [] all others arguments are passed to QM class.

Returns: A new 'QMrs' object.

Method fit(): Fit the bias correction method

```
Usage:
QMrs$fit(Y0, X0)
Arguments:
Y0 [matrix: n_samples * n_features] Observations in calibration
X0 [matrix: n_samples * n_features] Model in calibration
```

Method predict(): Predict the correction

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```
Usage:
QMrs$predict(X0)
Arguments:
X0 [matrix: n_samples * n_features or NULL] Model in calibration
Returns: [matrix] Return the corrections of X0

Method clone(): The objects of this class are cloneable with this method.
Usage:
QMrs$clone(deep = FALSE)
Arguments:
deep Whether to make a deep clone.
```

#### References

Vrac, M.: Multivariate bias adjustment of high-dimensional climate simulations: the Rank Resampling for Distributions and Dependences (R2 D2) bias correction, Hydrol. Earth Syst. Sci., 22, 3175–3196, https://doi.org/10.5194/hess-22-3175-2018, 2018.

## **Examples**

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)
XY = SBCK::dataset_gaussian_exp_2d(2000)
X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period

## Bias correction
## Step 1 : construction of the class QMrs
qmrs = SBCK::QMrs$new()
## Step 2 : Fit the bias correction model
qmrs$fit( Y0 , X0 )
## Step 3 : perform the bias correction
Z0 = qmrs$predict(X0)
```

R2D2

R2D2 (Rank Resampling for Distributions and Dependences) method

# Description

Perform a multivariate (non stationary) bias correction.

# **Details**

Use rankshuffle in calibration and projection period with CDFt

R2D2 59

## Super class

```
SBCK::CDFt -> R2D2
```

## **Public fields**

irefs [vector of int] Indexes for shuffle. Defaults is base::c(1)

## Methods

```
Public methods:
```

```
• R2D2$new()
```

- R2D2\$fit()
- R2D2\$predict()
- R2D2\$clone()

```
Method new(): Create a new R2D2 object.
```

```
Usage:
```

```
R2D2$new(irefs = base::c(1), ...)
```

Arguments:

 $irefs \ \ [vector\ of\ int]\ Indexes\ for\ shuffle.\ Defaults\ is\ base::c(1)\ model$ 

... [] all others arguments are passed to CDFt class.

Returns: A new 'R2D2' object.

## **Method** fit(): Fit the bias correction method

Usage:

```
R2D2$fit(Y0, X0, X1)
```

Arguments:

Y0 [matrix: n\_samples \* n\_features] Observations in calibration

X0 [matrix: n\_samples \* n\_features] Model in calibration

X1 [matrix: n\_samples \* n\_features] Model in projection

Returns: NULL

# Method predict(): Predict the correction

Usage:

```
R2D2\$predict(X1, X0 = NULL)
```

Arguments:

X1 [matrix: n\_samples \* n\_features] Model in projection

X0 [matrix: n\_samples \* n\_features or NULL] Model in calibration

*Returns:* [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list containing Z1 and Z0, the corrections of X1 and X0

**Method** clone(): The objects of this class are cloneable with this method.

Usage:

```
R2D2$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

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## References

Vrac, M.: Multivariate bias adjustment of high-dimensional climate simulations: the Rank Resampling for Distributions and Dependences (R2 D2) bias correction, Hydrol. Earth Syst. Sci., 22, 3175–3196, https://doi.org/10.5194/hess-22-3175-2018, 2018.

# **Examples**

```
## Three bivariate random variables (rnorm and rexp are inverted between ref
## and bias)

XY = SBCK::dataset_gaussian_exp_2d(2000)

X0 = XY$X0 ## Biased in calibration period
Y0 = XY$Y0 ## Reference in calibration period
X1 = XY$X1 ## Biased in projection period

## Bias correction
## Step 1 : construction of the class R2D2
r2d2 = SBCK::R2D2$new()
## Step 2 : Fit the bias correction model
r2d2$fit( Y0 , X0 , X1 )
## Step 3 : perform the bias correction
Z = r2d2$predict(X1,X0)
```

RBC

RBC (Random Bias Correction) method

# Description

Perform a multivariate bias correction of X with respect to Y randomly.

## **Details**

Only for comparison.

#### Methods

#### **Public methods:**

- RBC\$new()
- RBC\$fit()
- RBC\$predict()
- RBC\$clone()

Method new(): Create a new RBC object.

Usage:
RBC\$new()

Returns: A new 'RBC' object.

```
Method fit(): Fit the bias correction method
       RBC\$fit(Y0, X0, X1 = NULL)
       Arguments:
       Y0 [matrix: n samples * n features] Observations in calibration
       X0 [matrix: n_samples * n_features] Model in calibration
       X1 [matrix: n samples * n features] Model in projection, can be NULL for stationary BC
           method
       Returns: NULL
     Method predict(): Predict the correction. Use named keywords to use stationary or non-
     stationary method.
       Usage:
       RBC$predict(X1 = NULL, X0 = NULL)
       Arguments:
       X1 [matrix: n_samples * n_features or NULL] Model in projection
       X0 [matrix: n_samples * n_features or NULL] Model in calibration
       Returns: [matrix or list] Return the matrix of correction of X1 if X0 is NULL, else return a list
       containing Z1 and Z0, the corrections of X1 and X0
     Method clone(): The objects of this class are cloneable with this method.
       Usage:
       RBC$clone(deep = FALSE)
       Arguments:
       deep Whether to make a deep clone.
Examples
    ## Three bivariate random variables (rnorm and rexp are inverted between ref
    ## and bias)
   XY = SBCK::dataset_gaussian_exp_2d(2000)
   X0 = XY$X0 ## Biased in calibration period
    Y0 = XY$Y0 ## Reference in calibration period
   X1 = XY$X1 ## Biased in projection period
    ## Bias correction
    ## Step 1 : construction of the class RBC
    rbc = SBCK::RBC$new()
    ## Step 2 : Fit the bias correction model
    rbc$fit( Y0 , X0 , X1 )
    ## Step 3 : perform the bias correction
    Z = rbc predict(X1, X0)
```

## Z\$Z0 # BC of X0 ## Z\$Z1 # BC of X1 62 SchaakeShuffle

**SBCK** 

SBCK

# Description

Statistical Bias Correction Kit

# Author(s)

Yoann Robin Maintainer: Yoann Robin <yoann.robin.k@gmail.com>

SchaakeShuffle

ShaakeShuffle class

# Description

Perform the Schaake Shuffle

## **Details**

as fit/predict mode

#### Methods

# **Public methods:**

- SchaakeShuffle\$new()
- SchaakeShuffle\$fit()
- SchaakeShuffle\$predict()
- SchaakeShuffle\$clone()

Method new(): Create a new ShaakeShuffle object.

Usage:

SchaakeShuffle\$new(Y0 = NULL)

Arguments:

Y0 [vector] The reference vector

Returns: A new 'ShaaleShuffle' object.

Method fit(): Fit the model

Usage:

SchaakeShuffle\$fit(Y0)

Arguments:

Y0 [vector] The reference vector

SchaakeShuffleMultiRef 63

```
Returns: NULL
```

```
Method predict(): Fit the model
```

Usage:

SchaakeShuffle\$predict(X0)

Arguments:

X0 [vector] The vector to apply shuffle

Returns: Z0 [vector] data shuffled

**Method** clone(): The objects of this class are cloneable with this method.

Usage:

SchaakeShuffle\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

## **Examples**

```
X0 = matrix( stats::runif(20) , ncol = 2 )
Y0 = matrix( stats::runif(20) , ncol = 2 )
ss = SchaakeShuffle$new()
ss$fit(Y0)
Z0 = ss$predict(X0)
```

SchaakeShuffleMultiRef

ShaakeShuffleMultiRef class

# Description

Match the rank structure of X with them of Y by reordering X.

# **Details**

Can keep multiple features to keep the structure of X.

## **Public fields**

```
cond_cols [vector of integer] The conditioning columns
lag_search [integer] Number of lag to take into account
lag_keep [integer] Number of lag to keep
Y0 [matrix] Reference data
```

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#### Methods

```
Public methods:
```

```
• SchaakeShuffleMultiRef$new()
       • SchaakeShuffleMultiRef$fit()
       • SchaakeShuffleMultiRef$predict()
       • SchaakeShuffleMultiRef$clone()
     Method new(): Create a new ShaakeShuffleMultiRef object.
       Usage:
       SchaakeShuffleMultiRef$new(lag_search, lag_keep, cond_cols = base::c(1))
       Arguments:
       lag_search [integer] Number of lag to take into account
       lag_keep [integer] Number of lag to keep
       cond_cols [vector of integer] The conditioning columns
       Returns: A new 'ShaaleShuffleMultiRef' object.
     Method fit(): Fit the model
       Usage:
       SchaakeShuffleMultiRef$fit(Y0)
       Arguments:
       Y0 [vector] The reference vector
       Returns: NULL
     Method predict(): Fit the model
       Usage:
       SchaakeShuffleMultiRef$predict(X0)
       Arguments:
       X0 [vector] The vector to apply shuffle
       Returns: Z0 [vector] data shuffled
     Method clone(): The objects of this class are cloneable with this method.
       Usage:
       SchaakeShuffleMultiRef$clone(deep = FALSE)
       Arguments:
       deep Whether to make a deep clone.
Examples
   X0 = matrix( stats::runif(50) , ncol = 2 )
   Y0 = matrix( stats::runif(50) , ncol = 2 )
    ssmr = SchaakeShuffleMultiRef$new( lag_search = 3 , lag_keep = 1 , cond_cols = 1 )
    ssmr$fit(Y0)
    Z0 = ssmr$predict(X0)
```

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SchaakeShuffleRef

ShaakeShuffleRef class

## **Description**

Match the rank structure of X with them of Y by reordering X.

## **Details**

Fix one features to keep the structure of X.

## Super class

```
SBCK::SchaakeShuffle -> SchaakeShuffleRef
```

#### **Public fields**

```
ref [integer] Reference
```

#### Methods

#### **Public methods:**

- SchaakeShuffleRef\$new()
- SchaakeShuffleRef\$fit()
- SchaakeShuffleRef\$predict()
- SchaakeShuffleRef\$clone()

```
Method new(): Create a new ShaakeShuffleRef object.
```

```
Usage:
```

```
SchaakeShuffleRef$new(ref, Y0 = NULL)
```

Arguments:

ref [integer] Reference

Y0 [vector] The reference vector

Returns: A new 'ShaaleShuffleRef' object.

# Method fit(): Fit the model

Usage:

SchaakeShuffleRef\$fit(Y0)

Arguments:

Y0 [vector] The reference vector

Returns: NULL

Method predict(): Fit the model

Usage:

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```
SchaakeShuffleRef$predict(X0)
 Arguments:
 X0 [vector] The vector to apply shuffle
 Returns: Z0 [vector] data shuffled
Method clone(): The objects of this class are cloneable with this method.
 Usage:
```

SchaakeShuffleRef\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

# **Examples**

```
X0 = matrix( stats::runif(20) , ncol = 2 )
Y0 = matrix( stats::runif(20) , ncol = 2 )
ss = SchaakeShuffleRef$new( ref = 1 )
ss$fit(Y0)
Z0 = ss$predict(X0)
```

schaake\_shuffle

schaake\_shuffle function

## **Description**

Apply the Schaake shuffle to transform the rank of X0 such that its correspond to the rank of Y0

## Usage

```
schaake_shuffle(Y0,X0)
```

## **Arguments**

```
Y0
                   [vector] The reference vector
Χ0
                   [vector] The vector to transform the rank
```

# Value

Z0 [vector] X shuffled.

```
X0 = stats::runif(10)
Y0 = stats::runif(10)
Z0 = SBCK::schaake_shuffle( Y0 , X0 )
```

Shift 67

Shift

Shift

## **Description**

Class to shift a dataset.

#### **Format**

R6Class object.

#### **Details**

Transform autocorrelations to intervariables correlations

## Value

```
Object of R6Class
```

## Methods

```
new(lag,method,ref,) This method is used to create object of this class with Shift transform(X) Method to shift a dataset inverse(Xs) Method to inverse the shift of a dataset
```

#### **Public fields**

lag [integer] max lag for autocorrelations

# **Active bindings**

```
method [character] If inverse is by row or column.
ref [integer] reference column/row to inverse shift.
```

## Methods

#### **Public methods:**

- Shift\$new()
- Shift\$transform()
- Shift\$inverse()
- Shift\$clone()

Method new(): Create a new Shift object.

```
Usage:
Shift$new(lag, method = "row", ref = 1)
Arguments:
```

```
lag [integer] max lag for autocorrelations
 method [character] If "row" inverse by row, else by column
 ref [integer] starting point for inverse transform
 Returns: A new 'Shift' object.
Method transform(): Shift the data
 Usage:
 Shift$transform(X)
 Arguments:
 X [matrix: n_samples * n_features] Data to shift
 Returns: [matrix] Matrix shifted
Method inverse(): Inverse the shift of the data
 Usage:
 Shift$inverse(Xs)
 Arguments:
 Xs [matrix] Data Shifted
 Returns: [matrix] Matrix un shifted
Method clone(): The objects of this class are cloneable with this method.
 Usage:
 Shift$clone(deep = FALSE)
 Arguments:
 deep Whether to make a deep clone.
```

# Examples

```
X = base::t(matrix( 1:20 , nrow = 2 , ncol = 10 ))
sh = Shift$new(1)
Xs = sh$transform(X)
Xi = sh$inverse(Xs)
```

SlopeStoppingCriteria Slope stopping criteria

## **Description**

Class which send a stop signal when a time series stay constant.

## **Details**

Test the slope.

## **Public fields**

```
minit [integer] Minimal number of iterations. At least 3.

maxit [integer] Maximal number of iterations.

nit [integer] Number of iterations.

tol [float] Tolerance to control if slope is close to zero stop [bool] If we stop

criteria [vector] State of criteria

slope [vector] Values of slope
```

#### Methods

## **Public methods:**

- SlopeStoppingCriteria\$new()
- SlopeStoppingCriteria\$reset()
- SlopeStoppingCriteria\$append()
- SlopeStoppingCriteria\$clone()

```
Method new(): Create a new SlopeStoppingCriteria object.

Usage:
SlopeStoppingCriteria$new(minit, maxit, tol)

Arguments:
minit [integer] Minimal number of iterations. At least 3.
maxit [integer] Maximal number of iterations.
tol [float] Tolerance to control if slope is close to zero

Returns: A new 'SlopeStoppingCriteria' object.
```

```
Method reset(): Reset the class
```

Usage:

SlopeStoppingCriteria\$reset()

Returns: NULL

Method append(): Add a new value

Usage:

SlopeStoppingCriteria\$append(value)

Arguments:

value [double] New metrics

Returns: NULL

**Method** clone(): The objects of this class are cloneable with this method.

Usage:

SlopeStoppingCriteria\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

70 SparseHist

## **Examples**

```
stop_slope = SlopeStoppingCriteria$new( 20 , 500 , 1e-3 )
x = 0
while(!stop_slope$stop)
{
stop_slope$append(base::exp(-x))
x = x + 0.1
}
print(stop_slope$nit)
```

SparseHist

SparseHist

## **Description**

Return the Rcpp Class SparseHistBase initialized

## Usage

```
SparseHist(X, bin_width = NULL, bin_origin = NULL)
```

# Arguments

```
X [matrix] Dataset to find the SparseHist
bin_width [vector] Width of a bin for each dimension
bin_origin [vector] Coordinate of the "0" bin
```

## Value

[SparseHist] SparseHist class

```
## Data
X = base::matrix( stats::rnorm( n = 10000 ) , nrow = 5000 , ncol = 2 )
muX = SparseHist(X)

print(muX$p) ## Vector of probabilities
print(muX$c) ## Matrix of coordinates of each bins
print(muX$argwhere(X)) ## Index of bins of dataset X
```

TSMBC 71

**TSMBC** 

TSMBC (Time Shifted Multivariate Bias Correction)

## **Description**

Perform a bias correction of auto-correlation

#### **Details**

Correct auto-correlation with a shift approach.

#### **Public fields**

```
shift [Shift class] Shift class to shift data.
bc_method [SBCK::BC_method] Underlying bias correction method.
```

# **Active bindings**

```
method [character] If inverse is by row or column, see class Shift ref [integer] reference column/row to inverse shift, see class
```

#### Methods

## **Public methods:**

```
• TSMBC$new()
```

- TSMBC\$fit()
- TSMBC\$predict()
- TSMBC\$clone()

Method new(): Create a new TSMBC object.

```
Usage:
```

```
TSMBC$new(lag, bc_method = OTC, method = "row", ref = "middle", ...)
```

Arguments:

lag [integer] max lag of autocorrelation

bc\_method [SBCK::BC\_METHOD] bias correction method to use after shift of data, default is OTC

method [character] If inverse is by row or column, see class Shift

ref [integer] reference column/row to inverse shift, see class Shift. Default is 0.5 \* (lag+1)

... [] All others arguments are passed to bc\_method

Returns: A new 'TSMBC' object.

Method fit(): Fit the bias correction method

Usage:

TSMBC\$fit(Y0, X0)

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```
Arguments:

Y0 [matrix: n_samples * n_features] Observations in calibration

X0 [matrix: n_samples * n_features] Model in calibration

Returns: NULL

Method predict(): Predict the correction

Usage:

TSMBC$predict(X0)

Arguments:

X0 [matrix: n_samples * n_features or NULL] Model in calibration

Returns: [matrix] Return the corrections of X0

Method clone(): The objects of this class are cloneable with this method.

Usage:

TSMBC$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.
```

#### References

Robin, Y. and Vrac, M.: Is time a variable like the others in multivariate statistical downscaling and bias correction?, Earth Syst. Dynam. Discuss. [preprint], https://doi.org/10.5194/esd-2021-12, in review, 2021.

wasserstein 73

wasserst	- A 1 N

wasserstein distance

## **Description**

Compute wasserstein distance between two dataset or SparseHist X and Y

## Usage

```
wasserstein(X, Y, p = 2, ot = SBCK::OTNetworkSimplex$new())
```

## **Arguments**

```
X [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
Y [matrix or SparseHist] If matrix, dim = (nrow = n_samples, ncol = n_features)
p [float] Power of the metric (default = 2)
ot [Optimal transport solver]
```

#### Value

[float] value of distance

## References

Wasserstein, L. N. (1969). Markov processes over denumerable products of spaces describing large systems of automata. Problems of Information Transmission, 5(3), 47-52.

```
X = base::cbind( stats::rnorm(2000) , stats::rnorm(2000) )
Y = base::cbind( stats::rnorm(2000,mean=10) , stats::rnorm(2000) )
bw = base::c(0.1,0.1)
muX = SBCK::SparseHist( X , bw )
muY = SBCK::SparseHist( Y , bw )

## The four are equals
w2 = SBCK::wasserstein(X,Y)
w2 = SBCK::wasserstein(muX,Y)
w2 = SBCK::wasserstein(X,muY)
w2 = SBCK::wasserstein(muX,muY)
```

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where

where function

# Description

This function return a vector / matrix / array of the same shape than cond / x / y such that if(cond) values are x, and else y.

## Usage

```
where(cond,x,y)
```

# Arguments

```
cond [vector/matrix/array] Boolean values

x [vector/matrix/array] Values if cond is TRUE

y [vector/matrix/array] Values if cond is FALSE
```

# Value

```
z [vector/matrix/array].
```

```
x = base::seq(-2, 2, length = 100)

y = where(x < 1, x, exp(x)) ## y = x if x < 1, else exp(x)
```

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