Package 'HistDAWass'

January 24, 2024

Type Package

Title Histogram-Valued Data Analysis

Version 1.0.8 **Date** 2024-01-24

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Description In the framework of Symbolic Data Analysis, a relatively new approach to the statistical analysis of multi-valued data, we consider histogram-valued data, i.e., data described by univariate histograms. The methods and the basic statistics for histogram-valued data are mainly based on the L2 Wasserstein metric between distributions, i.e., the Euclidean metric between quantile functions. The package contains unsupervised classification techniques, least square regression and tools for histogram-valued data and for histogram time series. An introducing paper is Irpino A. Verde R. (2015) <doi:10.1007/s11634-014-0176-4>.

License GPL (>= 2)

Imports graphics, class, FactoMineR, ggplot2, ggridges, grid, histogram, grDevices, stats, utils, Rcpp

Depends R(>=3.1), methods

LazyData true

Collate 'For_Rccp_int.R' 'All_classes.R' 'RcppExports.R' 'Utility.R'
'Met_HTS.R' 'Met_MatH.R' 'Met_distributionH.R' 'Fuzzy_cmeans.R'
'H_time_series.R' 'HistDAWass-package.R' 'Kohonen_maps.R'
'principal_components.R' 'regression.R'
'unsuperv_classification.R' 'Plotting_with_ggplot.R'

Encoding UTF-8

RoxygenNote 7.3.1

NeedsCompilation yes

LinkingTo Rcpp,RcppArmadillo

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Repository CRAN

Date/Publication 2024-01-24 17:42:31 UTC

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HistDAWass-package

Histogram-Valued Data Analysis

Description

We consider histogram-valued data, i.e., data described by univariate histograms. The methods and the basic statistics for histogram-valued data are mainly based on the L2 Wasserstein metric between distributions, i.e., a Euclidean metric between quantile functions. The package contains unsupervised classification techniques, least square regression and tools for histogram-valued data and for histogram time series.

Details

Package: HistDAWass
Type: Package
Version: 0.1.1
Date: 2014-09-17
License: GPL (>=2)
Depends: methods

An overview of how to use the package, including the most important functions

Author(s)

Antonio Irpino <antonio.irpino@unicampania.it>

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach*, Advances in Data Analysis and Classification, Volume 9, Issue 2, pp 143–175. DOI doi:10.1007/s1163401401764

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```
a[[3]] <- distributionH(
    x = c(95, 110, 125, 140, 155, 170, 185, 200, 215, 230, 245),
    p = c(0, 0.012, 0.041, 0.154, 0.36, 0.595, 0.781, 0.929, 0.972, 0.992, 1)
)
a[[4]] <- distributionH(
    x = c(105, 120, 135, 150, 165, 180, 195, 210, 225, 240, 260),
    p = c(0, 0.009, 0.035, 0.081, 0.186, 0.385, 0.633, 0.832, 0.932, 0.977, 1)
)
# Generating a list of names of observations
namerows <- list("u1", "u2")
# Generating a list of names of variables
namevars <- list("Var_1", "Var_2")
# creating the MatH
Mat_of_distributions <- MatH(
    x = a, nrows = 2, ncols = 2,
    rownames = namerows, varnames = namevars, by.row = FALSE
)</pre>
```

*-methods

Method *

Description

the product of a number and a distribution according to the L2 Wasssertein the product of a number and a distribution according to the L2 Wasssertein the product of a number and a distribution according to the L2 Wasssertein

Usage

```
## S4 method for signature 'distributionH, distributionH'
e1 * e2

## S4 method for signature 'numeric, distributionH'
e1 * e2

## S4 method for signature 'distributionH, numeric'
e1 * e2
```

Arguments

```
e1 a distributionH object or a number
```

e2 a distributionH object or a number

Age_Pyramids_2014

+ Method +

Description

the sum of two distribution according to the L2 Wasssertein the sum of a number and a distribution according to the L2 Wasssertein the sum of adistribution and a number according to the L2 Wasssertein

Usage

```
## S4 method for signature 'distributionH,distributionH'
e1 + e2

## S4 method for signature 'numeric,distributionH'
e1 + e2

## S4 method for signature 'distributionH,numeric'
e1 + e2
```

Arguments

e1 a distributionH object or a number e2 a distributionH object or a number

Value

a distributionH object

Age_Pyramids_2014

Age pyramids of all the countries of the World in 2014

Description

The dataset contains a MatH (matrix of histogram-valued data) object, with three hisogram-valued variables, the 5-years age (relative frequencies) distribution of all the population, of the male and of the female population of 228 countries of the World. The first row is the World data. Thus it contains 229 rows(228 countries plus the World) and 3 variables: "Both.Sexes.Population", "Male.Population", "Female.Population"

Format

a MatH object, a matrix of distributions.

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Author(s)

Antonio Irpino, 2014-10-05

Source

United States Census Bureau https://www.census.gov/data.html

Agronomique

Agronomique data

Description

A dataset with the distributions of marginal costs of farms in 22 France regions. It contains four histogram variables: "Y_TSC" (Total costs of a farm), "X_Wheat" (Costs for Wheat), "X_Pig" (Costs for Pigs) "X_Cmilk" (Costs for Cow Milk)

Format

a MatH object, a matrix of distributions.

Author(s)

Antonio Irpino, 2014-10-05

Source

Rosanna Verde, Antonio Irpino, Second University of Naples; Dominique Desbois, UMR Economie publique, INRA-AgroParisTech, How to cope with modelling and privacy concerns? A regression model and a visualization tool for aggregated data, Conference of European Statistics Stakeholders, Rome, November, 24-25,2014

BLOOD

Blood dataset for Histogram data analysis

Description

The dataset contains a MatH (matrix of histogram-valued data) object This data set list 14 groups of patients described by 3 variables.

Format

a MatH istance, 1 row per group.

Author(s)

Antonio Irpino, 2014-10-05

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Source

Billard L. and Diday E. (2006). Symbolic Data Analysis: Conceptual Statistics and Data Mining, Wiley.

BloodBRIT0

Blood dataset from Brito P. for Histogram data analysis

Description

The dataset contains a MatH (matrix of histogram-valued data) object This data set list 10 patients described by 2 variables.

Format

a MatH istance, 1 row per patient.

Author(s)

Antonio Irpino, 2014-10-05

Source

Dias, S. and Brito P. Distribution and Symmetric Distribution Regression Model for Histogram-Valued Variables, ArXiv, arXiv:1303.6199 [stat.ME]

Center.cell.MatH

Method Center.cell.MatH Centers all the cells of a matrix of distributions

Description

The function transform a MatH object (i.e. a matrix of distributions), such that each distribution is shifted and has a mean equal to zero

Usage

```
Center.cell.MatH(object)
## S4 method for signature 'MatH'
Center.cell.MatH(object)
```

Arguments

object

a MatH object, a matrix of distributions.

checkEmptyBins 9

Value

A MatH object, having each distribution with a zero mean.

Examples

```
CEN_BLOOD <- Center.cell.MatH(BLOOD)
get.MatH.stats(BLOOD, stat = "mean")</pre>
```

checkEmptyBins

Method checkEmptyBins

Description

The method checking for empty bins in a distribution, i.e. if two cdf consecutive values are equal. In that case a probability value of 1e-7 is assigned to the empty bin and the cdf is recomputed. This methods is useful for numerical reasons.

Usage

```
checkEmptyBins(object)
## S4 method for signature 'distributionH'
checkEmptyBins(object)
```

Arguments

object

a distributionH object

Value

A distributionH object without empty bins

Author(s)

Antonio Irpino

```
## ---- A mydist distribution with an empty bin i.e. two consecutive values of p are equal---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.5, 0.5, 1)) ## ---- Checks for empty byns and returns the newdist object without empty bins ---- newdist <- checkEmptyBins(mydist)
```

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China_Month

A monthly climatic dataset of China

Description

A dataset with the distributions of some climatic variables collected for each month in 60 stations of China. The collected variables are 168 i.e. 14 climatic variables observed for 12 months. The 14 variables are the following: mean station pressure (mb), mean temperature, mean maximum temperature, mean minimum temperature, total precipitation (mm), sunshine duration (h), mean cloud amount (percentage of sky cover), mean relative humidity (mean wind speed (m/s), dominant wind frequency (extreme minimum temperature. Use the command get.Math.main.info(China_Month) for rapid info.

Format

a MatH object, a matrix of distributions.

Author(s)

Antonio Irpino, 2014-10-05

Source

raw data are available here: https://data.ess-dive.lbl.gov/view/doi:10.3334/CDIAC/CLI.TR055

China_Seas

A seasonal climatic dataset of China

Description

A dataset with the distributions of some climatic variables collected for each season in 60 stations of China. The collected variables are 56 i.e. 14 climatic variables observed for 4 seasons. The 14 variables are the following: mean station pressure (mb), mean temperature, mean maximum temperature, mean minimum temperature, total precipitation (mm), sunshine duration (h), mean cloud amount (percentage of sky cover), mean relative humidity (mean wind speed (m/s), dominant wind frequency (extreme minimum temperature. Use the command get.Math.main.info(China_Seas) for rapid info.

Format

a MatH object, a matrix of distributions.

Author(s)

Antonio Irpino, 2014-10-05

compP 11

Source

raw data are available here: https://data.ess-dive.lbl.gov/view/doi:10.3334/CDIAC/CLI. TR055. Climate Data Bases of the People's Republic of China 1841-1988 (TR055) DOI: 10.3334/CDIAC/cli.tr055

compP

Method compP

Description

Compute the cdf probability at a given value for a histogram

Usage

```
compP(object, q)
## S4 method for signature 'distributionH,numeric'
compP(object, q)
```

Arguments

object is an object of distributionH class q is a numeric value

Value

Returns a value between 0 and 1.

Examples

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the cfd value for q=5 (not observed) ---- p <- compP(mydist, 5)
```

compQ

Method compQ

Description

Compute the quantile value of a histogram for a given probability.

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Usage

```
compQ(object, p)
## S4 method for signature 'distributionH,numeric'
compQ(object, p)
```

Arguments

object an object of distributionH class
p a number between 0 and 1

Value

$$y = F^{-1}(p) = Q(p)$$

A number that is the quantile of the passed histogram object at level p.

Author(s)

Antonio Irpino

Examples

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the quantile of mydist for different values of p ---- y <- compQ(mydist, 0.5) # the median y <- compQ(mydist, 0) # the minimum y <- compQ(mydist, 1) # the maximum y <- compQ(mydist, 0.25) # the first quartile y <- compQ(mydist, 0.9) # the ninth decile
```

crwtransform

Method crwtransform: *returns the centers and the radii of bins of a distribution*

Description

Centers and ranges calculation for bins of a histogram. It is useful for a very fast computation of statistics and methods based on the L2 Wassertein distance between histograms.

Usage

```
crwtransform(object)
## S4 method for signature 'distributionH'
crwtransform(object)
```

data2hist 13

Arguments

object a distributionH object

Value

A list containing

\$Centers The midpoints of the bins of the histogram
\$Radii The half-lenghts of the bins of the histogram

\$Weights The relative frequencies or the probailities associated with each bin (the sum is

equal to 1)

Author(s)

Antonio Irpino

References

Irpino, A., Verde, R., Lechevallier, Y. (2006) *Dynamic clustering of histograms using Wasserstein metric*, In: Proceedings of COMPSTAT 2006, Physica-Verlag, 869-876

Examples

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the cfd value for q=5 (not observed) ---- crwtransform(mydist)
```

data2hist

From real data to distributionH.

Description

From real data to distributionH.

Usage

```
data2hist(
  data,
  algo = "histogram",
  type = "combined",
  qua = 10,
  breaks = numeric(0),
  epsilon = 0.01
)
```

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Arguments

data a set of numeric values.

algo (optional) a string. Default is "histogram", i.e. the function "histogram" defined

in the histogram package.

If "base" the hist function is used.

"FixedQuantiles" computes the histogram using as breaks a fixed number of

quantiles.

"ManualBreaks" computes a histogram where braks are provided as a vector of

values.

"PolyLine" computes a histogram using a piecewise linear approximation of the empirical cumulative distribution function using the "Ramer-Douglas-Peucker

algorithm", https://en.wikipedia.org/wiki/Ramer-Douglas-Peucker_algorithm.

An epsilon parameter is required. The data are scaled in order to have a stan-

dard deviation equal to one.

type (optional) a string. Default is "combined" and generates a histogram having

regularly spaced breaks (i.e., equi-width bins) and irregularly spaced ones. The choice is done accordingly with the penalization method described in histogram. "regular" returns equi-width binned histograms, "irregular" returns a histogram

without equi-width histograms.

qua a positive integer to provide if algo="FixedQuantiles" is chosen. Default=10.

breaks a vector of values to provide if algo="ManualBreaks" is chosen.

epsilon a number between 0 and 1 to provide if algo="PolyLine" is chosen. De-

fault=0.01.

Value

A distributionH object, i.e. a distribution.

See Also

histogram function

Examples

```
data <- rnorm(n = 1000, mean = 2, sd = 3)
mydist <- data2hist(data)
plot(mydist)</pre>
```

distributionH-class

Class distributionH.

Description

Class "distributionH" desfines an histogram object The class describes a histogram by means of its cumulative distribution function. The methods are developed accordingly to the L2 Wasserstein distance between distributions.

A histogram object can be created also with the function distributionH(...), the costructor function for creating an object containing the description of a histogram.

distributionH-class 15

Usage

```
## S4 method for signature 'distributionH'
initialize(
   .Object,
   x = numeric(0),
   p = numeric(0),
   m = numeric(0),
   s = numeric(0)
)

distributionH(x = numeric(0), p = numeric(0))
```

Arguments

.Object	the type ("distributionH")
x	a numeric vector. it is the domain of the distribution (i.e. the extremes of bins).
p	a numeric vector (of the same lenght of \mathbf{x}). It is the cumulative distribution function CDF.
m	(optional) a numeric value. Is the mean of the histogram.
S	(optional) a numeric positive value. It is the standard deviation of a histogram.

Details

Class distributionH defines a histogram object

Value

A distributionH object

Objects from the Class

Objects can be created by calls of the form new("distributionH", x, p, m, s).

Author(s)

Antonio Irpino

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

See Also

meanH computes the mean. stdH computes the standard deviation.

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Examples

```
#---- initialize a distributionH object mydist
# from a simple histogram
# -----
# | Bins | Prob | cdf |
# | [1,2) | 0.4 | 0.4 |
# | [2,3] | 0.6 | 1.0 |
# | Tot. | 1.0 | - |
mydist <- new("distributionH", c(1, 2, 3), c(0, 0.4, 1))
str(mydist)
# OUTPUT
# Formal class 'distributionH' [package "HistDAWass"] with 4 slots
   ..@ x: num [1:3] 1 2 3 the quantiles
  ..@ p: num [1:3] 0 0.4 1 the cdf
  ..@ m: num 2.1 the mean
  ..@ s: num 0.569 the standard deviation
# or using
mydist <- distributionH(x = c(1, 2, 3), p = c(0, 0.4, 1))
```

dotpW

Method dotpW

Description

The dot product of two distributions inducing the L2 Wasserstein metric

The dot product of a number (considered as an impulse distribution function) and a distribution

The dot product of a distribution and a number (considered as an impulse distribution function).

Usage

```
dotpW(e1, e2)
## S4 method for signature 'distributionH,distributionH'
dotpW(e1, e2)
## S4 method for signature 'numeric,distributionH'
dotpW(e1, e2)
## S4 method for signature 'distributionH,numeric'
dotpW(e1, e2)
```

Arguments

```
e1 a distributionH object or a number
e2 a distributionH object or a number
```

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Value

A numeric value

Author(s)

Antonio Irpino

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

Examples

```
## let's define two distributionH objects mydist1 <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) mydist2 <- distributionH(x = c(5, 7, 15), p = c(0, 0.7, 1))  
## the dot product between the distributions dotpW(mydist1, mydist2) #---> 39.51429  
## the dot product between a distribution and a numeric dotpW(mydist1, 3) #---> 13.2 dotpW(3, mydist1) #---> 13.2
```

DouglasPeucker

Ramer-Douglas-Peucker algorithm for curve fitting with a PolyLine

Description

Ramer-Douglas-Peucker algorithm for curve fitting with a PolyLine

Usage

```
DouglasPeucker(points, epsilon)
```

Arguments

```
points a 2D matrix with the coordinates of 2D points epsilon an number between 0 and 1. Recomended 0.01.
```

Value

A matrix with the points of segments of a Poly Line.

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See Also

data2hist function

get.cell.Math Method get.cell.Math Returns the histogram in a cell of a matrix of distributions	- -	hod get.cell.MatH Returns the histogram in a cell of a matrix of ributions
---	----------------	--

Description

Returns the histogram data in the r-th row and the c-th column.

Usage

```
get.cell.MatH(object, r, c)
## S4 method for signature 'MatH,numeric,numeric'
get.cell.MatH(object, r, c)
```

Arguments

object a MatH object, a matrix of distributions.

r an integer, the row index.c an integer, the column index

Value

A distributionH object.

Examples

```
get.cell.MatH(BLOOD, r = 1, c = 1)
```

get.distr

Method get.distr: show the distribution

Description

This function return the cumulative distribution function of a distributionH object.

Usage

```
get.distr(object)
## S4 method for signature 'distributionH'
get.distr(object)
```

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Arguments

object

a distributionH object.

Value

A data frame: the first column contains the domain the second the CDF values.

Examples

```
D <- distributionH(x = c(1, 2, 3, 4), p = c(0, 0.2, 0.6, 1)) get.distr(D) # a data.frame describing the CDF of D
```

get.histo

Method get.histo: show the distribution with bins

Description

This functon return a data.frame describing the histogram of a distributionH object.

Usage

```
get.histo(object)
## S4 method for signature 'distributionH'
get.histo(object)
```

Arguments

object

a distributionH object.

Value

A matrix: the two columns contains the bounds of the histogram the third contains the probablity (or the relative frequency) of the bin.

```
D <- distributionH(x = c(1, 2, 3, 4), p = c(0, 0.2, 0.6, 1)) get.histo(D) # returns the histogram representation of D by a data.frame
```

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get.m

Method get.m: the mean of a distribution

Description

This functon return the mean of a distributionH object.

Usage

```
get.m(object)
## S4 method for signature 'distributionH'
get.m(object)
```

Arguments

object

a distributionH object

Value

A numeric value

Examples

```
D <- distributionH(x = c(1, 2, 3, 4), p = c(0, 0.2, 0.6, 1)) get.m(D) # returns the mean of D
```

get.MatH.main.info

Method get.MatH.main.info

Description

It returns the number of rows, of columns the labels of rows and columns of a MatH object.

Usage

```
get.MatH.main.info(object)
## S4 method for signature 'MatH'
get.MatH.main.info(object)
```

Arguments

object

a MatH object

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Value

A list of char, the labels of the columns, or the names of the variables.

Slots

```
nrows - the number of rows

ncols - the number of columns

rownames - a vector of char, the names of rows

varnames - a vector of char, the names of columns
```

get.MatH.ncols

Method get.MatH.ncols

Description

It returns the number of columns of a MatH object

Usage

```
get.MatH.ncols(object)
## S4 method for signature 'MatH'
get.MatH.ncols(object)
```

Arguments

object

a MatH object

Value

An integer, the number of columns.

get.MatH.nrows

Method get.MatH.nrows

Description

It returns the number of rows of a MatH object

Usage

```
## S4 method for signature 'MatH'
get.MatH.nrows(object)
```

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Arguments

object a MatH object

Value

An integer, the number of rows.

get.MatH.rownames

Method get.MatH.rownames

Description

It returns the labels of the rows of a MatH object

Usage

```
get.MatH.rownames(object)
## S4 method for signature 'MatH'
get.MatH.rownames(object)
```

Arguments

object

a MatH object

Value

A vector of char, the label of the rows.

get.MatH.stats

Method get.MatH.stats

Description

It returns statistics for each distribution contained in a MatH object.

Usage

```
get.MatH.stats(object, ...)
## S4 method for signature 'MatH'
get.MatH.stats(object, stat = "mean", prob = 0.5)
```

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Arguments

```
object
                  a MatH object
                  a set of other parameters
. . .
stat
                  (optional) a string containing the required statistic. Default='mean'
                  - stat='mean' - for computing the mean of each histogram
                  - stat='median' - for computing the median of each histogram
                  - stat='min' - for computing the minimum of each histogram
                  - stat='max' - for computing the maximum of each histogram
                  - stat='std' - for computing the standard deviatio of each histogram
                  - stat='skewness' - for computing the skewness of each histogram
                  - stat='kurtosis' - for computing the kurtosis of each histogram
                  - stat='quantile' - for computing the quantile ot level prob of each histogram
                  (optional)a number between 0 and 1 for computing the value once choosen the
prob
                   'quantile' option for stat.
```

Value

A list

Slots

```
stat - the chosen statisticprob - level of probability if stat='quantile'MAT - a matrix of values
```

```
get.MatH.stats(BLOOD) # the means of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "median") # the medians of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "quantile", prob = 0.5) # the same as median get.MatH.stats(BLOOD, stat = "min") # minima of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "quantile", prob = 0) # the same as min get.MatH.stats(BLOOD, stat = "max") # maxima of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "quantile", prob = 1) # the same as max get.MatH.stats(BLOOD, stat = "std") # standard deviations of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "skewness") # skewness indices of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "kurtosis") # kurtosis indices of the distributions in BLOOD dataset get.MatH.stats(BLOOD, stat = "quantile", prob = 0.05) # the fifth percentiles of distributions in BLOOD dataset
```

24 get.s

get.MatH.varnames

Method get.MatH.varnames

Description

It returns the labels of the columns, or the names of the variables, of a MatH object

Usage

```
get.MatH.varnames(object)
## S4 method for signature 'MatH'
get.MatH.varnames(object)
```

Arguments

object

a MatH object

Value

A vector of char, the labels of the columns, or the names of the variables.

get.s

Method get.s: the standard deviation of a distribution

Description

This functon return the standard deviation of a distributionH object.

Usage

```
get.s(object)
## S4 method for signature 'distributionH'
get.s(object)
```

Arguments

object

a distributionH object.

Value

A numeric positive value, the standard deviation.

```
D <- distributionH(x = c(1, 2, 3, 4), p = c(0, 0.2, 0.6, 1)) get.s(D) # returns the standard deviation of D
```

HTS-class 25

HTS-class

Class HTS

Description

Class HTS defines a histogram time series, i.e. a set of histograms observed along time

Usage

```
## S4 method for signature 'HTS'
initialize(.Object, epocs = 1, ListOfTimedElements = c(new("TdistributionH")))
```

Arguments

. Object type ("HTS") a histogram time series

epocs the number of histograms (one for each timepoint or period)

ListOfTimedElements

a vector of TdistributionH objects

HTS.exponential.smoothing

Smoothing with exponential smoothing of a histogram time series

Description

(Beta verson of) Extends the exponential smoothing of a time series to a histogram time series, using L2 Wasserstein distance.

Usage

```
HTS.exponential.smoothing(HTS, alpha = 0.9)
```

Arguments

HTS A HTS object (a histogram time series).

alpha a number between 0 and 1 for exponential smoothing

Value

a list with the results of the smoothing procedure.

Slots

```
smoothing.alpha the alpha parameter AveragedHTS The smoothed HTS
```

Examples

```
mov.expo.smooth <- HTS.exponential.smoothing(HTS = RetHTS, alpha = 0.8)
# a show method for HTS must be implemented you can see it using
# str(mov.expo.smooth$AveragedHTS)</pre>
```

HTS.moving.averages

Smoothing with moving averages of a histogram time series

Description

(Beta verson of) Extends the moving average smoothing of a time series to a histogram time series, using L2 Wasserstein distance.

Usage

```
HTS.moving.averages(HTS, k = 3, weights = rep(1, k))
```

Arguments

HTS A HTS object (a histogram time series).

k an integer value, the number of elements for moving averagesweights a vector of positive weights for a weighted moving average

Value

a list with the results of the smoothing procedure.

Slots

```
k the number of elements for the average
weights the vector of weights for smoothing
AveragedHTS The smoothed HTS
```

```
mov.av.smoothed <- HTS.moving.averages(HTS = RetHTS, k = 5)
# a show method for HTS must be implemented you can see it using
# str(mov.av.smoothed$AveragedHTS)</pre>
```

HTS.predict.knn 27

HTS.predict.knn	K-NN predictions of a histogram time series	

Description

(Beta verson of) Extends the K-NN algorithm for predicting a time series to a histogram time series, using L2 Wasserstein distance.

Usage

```
HTS.predict.knn(HTS, position = length(HTS@data), k = 3)
```

Arguments

HTS A HTS object (a histogram time series).

position an integer, the data histogram to predict the number of neighbours (default=3)

Details

Histogram time series (HTS) describe situations where a distribution of values is available for each instant of time. These situations usually arise when contemporaneous or temporal aggregation is required. In these cases, histograms provide a summary of the data that is more informative than those provided by other aggregates such as the mean. Some fields where HTS are useful include economy, official statistics and environmental science. The function adapts the k-Nearest Neighbours (k-NN) algorithm to forecast HTS and, more generally, to deal with histogram data. The proposed k-NN relies on the L2 Wasserstein distance that is used to measure dissimilarities between sequences of histograms and to compute the forecasts.

Value

a distributionH object predicted from data.

References

Javier Arroyo, Carlos Mate, Forecasting histogram time series with k-nearest neighbours methods, International Journal of Forecasting, Volume 25, Issue 1, January-March 2009, Pages 192-207, ISSN 0169-2070, http://dx.doi.org/10.1016/j.ijforecast.2008.07.003.

```
prediction <- HTS.predict.knn(HTS = RetHTS, position = 108, k = 3)</pre>
```

28 is.registeredMH

is.registeredMH

Method is.registeredMH

Description

Checks if a MatH contains histograms described by the same number of bins and the same cdf.

Usage

```
is.registeredMH(object)
## S4 method for signature 'MatH'
is.registeredMH(object)
```

Arguments

object

A Math object

Value

a logical value TRUE if the distributions share the same cdf, FALSE otherwise.

Author(s)

Antonio Irpino

References

Irpino, A., Lechevallier, Y. and Verde, R. (2006): *Dynamic clustering of histograms using Wasser-stein metric* In: Rizzi, A., Vichi, M. (eds.) COMPSTAT 2006. Physica-Verlag, Berlin, 869-876. Irpino, A., Verde, R. (2006): *A new Wasserstein based distance for the hierarchical clustering of histogram symbolic data* In: Batanjeli, V., Bock, H.H., Ferligoj, A., Ziberna, A. (eds.) Data Science and Classification, IFCS 2006. Springer, Berlin, 185-192.

```
## ---- initialize three distributionH objects mydist1 and mydist2
mydist1 <- new("distributionH", c(1, 2, 3), c(0, 0.4, 1))
mydist2 <- new("distributionH", c(7, 8, 10, 15), c(0, 0.2, 0.7, 1))
mydist3 <- new("distributionH", c(9, 11, 20), c(0, 0.8, 1))
## create a MatH object
MyMAT <- new("MatH", nrows = 1, ncols = 3, ListOfDist = c(mydist1, mydist2, mydist3), 1, 3)
is.registeredMH(MyMAT)
## [1] FALSE #the distributions do not share the same cdf
## Hint: check with str(MyMAT)
## register the two distributions
MATregistered <- registerMH(MyMAT)</pre>
```

kurtH 29

```
is.registeredMH(MATregistered)
## TRUE #the distributions share the same cdf
## Hint: check with str(MATregistered)
```

kurtH

Method kurtH: computes the kurthosis of a distribution

Description

Kurtosis of a histogram (using the fourth standardized moment)

Usage

```
kurtH(object)
## S4 method for signature 'distributionH'
kurtH(object)
```

Arguments

object

a distributionH object

Value

A value for the kurtosis index, 3 is the kurtosis of a Gaussian distribution

Author(s)

Antonio Irpino

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the kurtosis of mydist ---- kurtH(mydist) #---> 1.473242
```

30 MatH-class

MatH-class

Class MatH.

Description

Class MatH defines a matrix of distributionH objects

This function create a matrix of histogram data, i.e. a MatH object

Usage

```
## S4 method for signature 'MatH'
initialize(
  .Object,
  nrows = 1,
  ncols = 1,
  ListOfDist = NULL,
  names.rows = NULL,
  names.cols = NULL,
  by.row = FALSE
)
MatH(
  x = NULL,
  nrows = 1,
  ncols = 1,
  rownames = NULL,
  varnames = NULL,
  by.row = FALSE
)
```

Arguments

.Object	the object type "MatH"
nrows	(optional, default=1)an integer, the number of rows.
ncols	(optional, default=1) an integer, the number of columns (aka variables).
ListOfDist	a vector or a list of distributionH objects
names.rows	a vector or list of strings with thenames of the rows
names.cols	a vector or list of strings with thenames of the columns (variables)
by.row	(optional, default=FALSE) a logical value, TRUE the matrix is row wise filled, FALSE the matrix is filled column wise.
X	(optional, default= an empty distributionH object) a list of distributionH objects
rownames	(optional, default=NULL) a list of strings containing the names of the rows.
varnames	(optional, default=NULL) a list of strings containing the names of the columns (aka variables).

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Value

A matH object

Author(s)

Antonio Irpino

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

Examples

```
## ---- create a list of six distributionH objects
ListOfDist <- vector("list", 6)</pre>
ListOfDist[[1]] <- distributionH(c(1, 2, 3), c(0, 0.4, 1))
ListOfDist[[2]] <- distributionH(c(7, 8, 10, 15), c(0, 0.2, 0.7, 1))
ListOfDist[[3]] <- distributionH(c(9, 11, 20), c(0, 0.5, 1))
ListOfDist[[4]] <- distributionH(c(2, 5, 8), c(0, 0.3, 1))
ListOfDist[[5]] <- distributionH(c(8, 10, 15), c(0, 0.75, 1))
ListOfDist[[6]] <- distributionH(c(20, 22, 24), c(0, 0.12, 1))
## create a MatH object filling it by columns
MyMAT <- new("MatH",
  nrows = 3, ncols = 2, ListOfDist = ListOfDist,
  names.rows = c("I1", "I2", "I3"), names.cols = c("Var1", "Var2"), by.row = FALSE
)
showClass("MatH")
# bulding an empty 10 by 4 matrix of histograms
MAT <- MatH(nrows = 10, ncols = 4)
```

meanH

Method meanH: computes the mean of a distribution

Description

Mean of a histogram (First moment of the distribution)

Usage

```
meanH(object)
## S4 method for signature 'distributionH'
meanH(object)
```

32 minus

Arguments

object a distributionH object

Value

the mean of the distribution

Author(s)

Antonio Irpino

Examples

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the mean of mydist ---- meanH(mydist) #---> 4.4
```

minus

Method -

Description

the difference of two distribution according to the L2 Wasssertein the difference of a number and a distribution according to the L2 Wasssertein the difference of a distribution and a number according to the L2 Wasssertein

Usage

```
## S4 method for signature 'distributionH, distributionH'
e1 - e2

## S4 method for signature 'numeric, distributionH'
e1 - e2

## S4 method for signature 'distributionH, numeric'
e1 - e2
```

Arguments

```
e1 a distributionH object or a number
e2 a distributionH object or a number
```

Note

it may not works properly if the difference is not a distribution

OzoneFull 33

OzoneFull

Full Ozone dataset for Histogram data analysis

Description

The dataset contains MatH (matrix of histogram-valued data) object This data set list 78 stations located in the USA recording four variables, without missing data.

Format

a MatH istance, 1 row per station.

Author(s)

Antonio Irpino, 2014-10-05

Source

http://java.epa.gov/castnet/epa_jsp/prepackageddata.jsp ftp://ftp.epa.gov/castnet/data/metdata.zip

0zoneH

Complete Ozone dataset for Histogram data analysis

Description

The dataset contains MatH (matrix of histogram-valued data) object This data set list 84 stations located in the USA recording four variables. Some stations contains missing data.

Format

a MatH istance, 1 row per station.

Author(s)

Antonio Irpino, 2014-10-05

Source

http://java.epa.gov/castnet/epa_jsp/prepackageddata.jsp ftp://ftp.epa.gov/castnet/data/metdata.zip

34 plot-HTS

plot-distributionH

plot for a distributionH object

Description

A plot function for a distributionH object. The function returns a representation of the histogram.

Usage

```
## S4 method for signature 'distributionH'
plot(x, type = "HISTO", col = "green", border = "black")
```

Arguments

x a distributionH object

type (optional) a string describing the type of plot, default="HISTO".

Other allowed types are

"CDF"=Cumulative distribution function,

"QF"= quantile function,

"DENS"=a density approximation, "HBOXPLOT"=horizontal boxplot, "VBOXPLOT"= vertical boxplot,

col (optional) a string the color of the plot, default="green".

border (optional) a string the color of the border of the plot, default="black".

Examples

```
## ---- initialize a distributionH
mydist <- distributionH(x = c(7, 8, 10, 15), p = c(0, 0.2, 0.7, 1))
# show the histogram
plot(mydist) # plots mydist
plot(mydist, type = "HISTO", col = "red", border = "blue") # plots mydist
plot(mydist, type = "DENS", col = "red", border = "blue") # plots a density approximation for mydist
plot(mydist, type = "HBOXPLOT") # plots a horizontal boxplot for mydist
plot(mydist, type = "VBOXPLOT") # plots a vertical boxplot for mydist
plot(mydist, type = "CDF") # plots the cumulative distribution function of mydist
plot(mydist, type = "QF") # plots the quantile function of mydist</pre>
```

plot-HTS

Method plot for a histogram time series

Description

An overloading plot function for a HTS object. The method returns a graphical representation of a histogram time series.

plot-MatH 35

Usage

```
## S4 method for signature 'HTS'
plot(x, y = "missing", type = "VIOLIN", border = "black", maxno.perplot = 30)
```

Arguments

x a distributionH object y not used in this implementation

type (optional) a string describing the type of plot, default="BOXPLOT".

Other allowed types are

"VIOLIN"=a violin-plot representation,

border (optional) a string the color of the border of the plot, default="black".

maxno.perplot An integer (DEFAULT=30). Maximum number of timestamps per row. It allows

a plot organized by rows, each row of the plot contains a max number of time

stamps indicated by maxno.perplot.

Examples

```
plot(subsetHTS(RetHTS, from = 1, to = 10)) # plots RetHTS dataset
## Not run:
plot(RetHTS, type = "BOXPLOT", border = "blue", maxno.perplot = 20)
plot(RetHTS, type = "VIOLIN", border = "blue", maxno.perplot = 20)
plot(RetHTS, type = "VIOLIN", border = "blue", maxno.perplot = 10)
## End(Not run)
```

plot-MatH

Method plot for a matrix of histograms

Description

An overloading plot function for a MatH object. The method returns a graphical representation of the matrix of histograms.

Usage

```
## S4 method for signature 'MatH'
plot(x, y = "missing", type = "HISTO", border = "black", angL = 330)
```

Arguments

x a distributionH object

y not used in this implementation

type (optional) a string describing the type of plot, default="HISTO".

Other allowed types are

"DENS"=a density approximation,

"BOXPLOT"=1 boxplot

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```
border (optional) a string the color of the border of the plot, default="black".

angL (optional) angle of labels of rows (DEFAULT=330).
```

Examples

```
plot(BLOOD) # plots BLOOD dataset
## Not run:
plot(BLOOD, type = "HISTO", border = "blue") # plots a matrix of histograms
plot(BLOOD, type = "DENS", border = "blue") # plots a matrix of densities
plot(BLOOD, type = "BOXPLOT") # plots a boxplots
## End(Not run)
```

plot-TdistributionH plot for a TdistributionH object

Description

A plot function for a TdistributionH object. The function returns a representation of the histogram.

Usage

```
## S4 method for signature 'TdistributionH'
plot(x, type = "HISTO", col = "green", border = "black")
```

Arguments

x a TdistributionH object

type (optional) a string describing the type of plot, default="HISTO".

Other allowed types are

"CDF"=Cumulative distribution function,

"QF"= quantile function,

"DENS"=a density approximation, "HBOXPLOT"=horizontal boxplot, "VBOXPLOT"= vertical boxplot,

col (optional) a string the color of the plot, default="green".

border (optional) a string the color of the border of the plot, default="black".

plotPredVsObs 37

plotPredVsObs	A function for comparing observed vs predicted histograms

Description

This function allows the representation of observed vs predicted histograms. It can be used as a tool for interpreting preditive methods (for exampe, the regression of histogram data)

Usage

```
plotPredVsObs(PRED, OBS, type = "HISTO", ncolu = 2)
```

Arguments

PRED	a MatH object with one column, the predicted data
OBS	a MatH object with one column, the observed data
type	a string. "HISTO" (default), if ones want to compare histograms "CDF", if ones want to compare cumulative distribution functions; "DENS" if ones want to compare approximated densities (using KDE);
ncolu	number of columns in which is arranged the plot, default is 2. If you have a lot of data consider to choose higher values.

Value

A plot with compared histogram-valued data.

```
## do a regression
pars <- WH.regression.two.components(BLOOD, Yvar = 1, Xvars = c(2:3))
## predict data
PRED <- WH.regression.two.components.predict(data = BLOOD[, 2:3], parameters = pars)
## define observed data
## Not run:
OBS <- BLOOD[, 1]
plotPredVsObs(PRED, OBS, "HISTO")
plotPredVsObs(PRED, OBS, "CDF")
plotPredVsObs(PRED, OBS, "DENS")
## End(Not run)</pre>
```

38 plot_errors

plot_error	^S
------------	----

A function for plotting functions of errors

Description

This function allows the representation of the difference between observed histograms and the respective predicted ones. It can be used as a tool for interpreting preditive methods (for exampe, the regression of histogram data)

Usage

```
plot_errors(PRED, OBS, type = "HISTO_QUA", np = 200)
```

Arguments

PRED

a MatH object with one column, the predicted data

a MatH object with one column, the observed data

type

a string. "HISTO_QUA" (default), if ones want to compare histograms quantile differences

"HISTO_DEN", if ones want to show the histogram densities differences;

"DENS_KDE" if ones want to show the differences between approximated densities (using KDE);

np number of points considered for density or quantile computation (default=200).

Value

A plot with functions of differences between observed and predicted histograms, and a Root Mean Squared value computing by using the L2 Wasserstein distance.

```
## do a regression
pars <- WH.regression.two.components(BLOOD, Yvar = 1, Xvars = c(2:3))
## predict data
PRED <- WH.regression.two.components.predict(data = BLOOD[, 2:3], parameters = pars)
## define observed data
OBS <- BLOOD[, 1]
plot_errors(PRED, OBS, "HISTO_QUA")
plot_errors(PRED, OBS, "HISTO_DEN")
plot_errors(PRED, OBS, "DENS_KDE")</pre>
```

register 39

Description

Given two distributionH objects, it returns two equivalent distributions such that they share the same cdf values. This function is useful for computing basic statistics.

Usage

```
register(object1, object2)
## S4 method for signature 'distributionH, distributionH'
register(object1, object2)
```

Arguments

object1 A distributionH object object2 A distributionH object

Value

The two distributionH objects in input sharing the same cdf (the p slot)

Author(s)

Antonio Irpino

References

Irpino, A., Lechevallier, Y. and Verde, R. (2006): *Dynamic clustering of histograms using Wasser-stein metric* In: Rizzi, A., Vichi, M. (eds.) COMPSTAT 2006. Physica-Verlag, Berlin, 869-876. Irpino, A., Verde, R. (2006): *A new Wasserstein based distance for the hierarchical clustering of histogram symbolic data* In: Batanjeli, V., Bock, H.H., Ferligoj, A., Ziberna, A. (eds.) Data Science and Classification, IFCS 2006. Springer, Berlin, 185-192.

```
## ---- initialize two distributionH objects mydist1 and mydist2
mydist1 <- distributionH(c(1, 2, 3), c(0, 0.4, 1))
mydist2 <- distributionH(c(7, 8, 10, 15), c(0, 0.2, 0.7, 1))
## register the two distributions
regDist <- register(mydist1, mydist2)

## OUTPUT:
## regDist$[[1]]
## An object of class "distributionH"</pre>
```

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```
## Slot "x": [1] 1.0 1.5 2.0 2.5 3.0
## Slot "p": [1] 0.0 0.2 0.4 0.7 1.0
## ...
## regDist$[[2]]
## An object of class "distributionH"
## Slot "x": [1] 7.0 8.0 8.8 10.0 15.0
## Slot "p": [1] 0.0 0.2 0.4 0.7 1.0
## ...
# The REGISTER function ----
```

registerMH

Method registerMH

Description

registerMH method registers a set of distributions of a MatH object All the distribution are recomputed to obtain distributions sharing the same p slot. This methods is useful for using fast computation of all methods based on L2 Wasserstein metric. The distributions will have the same number of element in the x slot without modifing their density function.

Usage

```
registerMH(object)
## S4 method for signature 'MatH'
registerMH(object)
```

Arguments

object

A MatH object (a matrix of distributions)

Value

A MatH object, a matrix of distributions sharing the same p slot (i.e. the same cdf).

Author(s)

Antonio Irpino

References

Irpino, A., Lechevallier, Y. and Verde, R. (2006): *Dynamic clustering of histograms using Wasser-stein metric* In: Rizzi, A., Vichi, M. (eds.) COMPSTAT 2006. Physica-Verlag, Berlin, 869-876. Irpino, A., Verde, R. (2006): *A new Wasserstein based distance for the hierarchical clustering of histogram symbolic data* In: Batanjeli, V., Bock, H.H., Ferligoj, A., Ziberna, A. (eds.) Data Science and Classification, IFCS 2006. Springer, Berlin, 185-192.

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Examples

```
# initialize three distributionH objects mydist1 and mydist2
mydist1 \leftarrow new("distributionH", c(1, 2, 3), c(0, 0.4, 1))
mydist2 \leftarrow new("distributionH", c(7, 8, 10, 15), c(0, 0.2, 0.7, 1))
mydist3 <- new("distributionH", c(9, 11, 20), c(0, 0.8, 1))
# create a MatH object
MyMAT <- new("MatH", nrows = 1, ncols = 3, ListOfDist = c(mydist1, mydist2, mydist3), 1, 3)
# register the two distributions
MATregistered <- registerMH(MyMAT)</pre>
# OUTPUT the structure of MATregstered
str(MATregistered)
   Formal class 'MatH' [package "HistDAWass"] with 1 slots
   .. @ M:List of 3
   ....$:Formal class 'distributionH' [package "HistDAWass"] with 4 slots
   .. .. ..@ x: num [1:6] 1 1.5 2 2.5 2.67 ...
   .. .. .. ..@ p: num [1:6] 0 0.2 0.4 0.7 0.8 1
    ....$ :Formal class 'distributionH' [package "HistDAWass"] with 4 slots
    .. .. .. ..@ x: num [1:6] 7 8 8.8 10 11.7 ...
    .. .. .. ..@ p: num [1:6] 0 0.2 0.4 0.7 0.8 1
   ....$:Formal class 'distributionH' [package "HistDAWass"] with 4 slots
   .. .. .. ..@ x: num [1:6] 9 9.5 10 10.8 11 ...
   .. .. .. ..@ p: num [1:6] 0 0.2 0.4 0.7 0.8 1
   .. ..- attr(*, "dim")= int [1:2] 1 3
   ...- attr(*, "dimnames")=List of 2
   .. .. ..$ : chr "I1"
   .. .. ..$ : chr [1:3] "X1" "X2" "X3"
```

RetHTS

A histogram-valued dataset of returns

Description

A histogram-valued dataset of returns of dollar vs yen change rates

Format

a MatH object, a matrix of distributions.

Author(s)

Antonio Irpino, 2014-10-05

rQQ

rQQ Method rQQ

Description

Quantile-Quantile correlation between two distributions

Usage

```
rQQ(e1, e2)
## S4 method for signature 'distributionH, distributionH'
rQQ(e1, e2)
```

Arguments

e1 A distributionH object e2 A distributionH object

Value

Pearson correlation index between quantiles

Author(s)

Antonio Irpino

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

```
## ---- initialize two distributionH object mydist1 and mydist2 mydist1 <- distributionH(x = c(1, 2, 3), p = c(0, 0.4, 1)) mydist2 <- distributionH(x = c(7, 8, 10, 15), p = c(0, 0.2, 0.7, 1)) ## computes the rQQ rQQ(mydist1, mydist2) ## OUTPUT 0.916894
```

set.cell.MatH 43

set.cell.MatH	Method set.cell.MatH assign a histogram to a cell of a matrix of histograms

Description

Assign a histogram data to the r-th row and the c-th column of a matrix of histograms.

Usage

```
set.cell.MatH(object, mat, r, c)
## S4 method for signature 'distributionH,MatH,numeric,numeric'
set.cell.MatH(object, mat, r, c)
```

Arguments

object a distributionH object, a matrix of distributions.

mat a MatH object, a matrix of distributions.

r an integer, the row index.
c an integer, the column index

Value

A MatH object.

Examples

```
\label{eq:mydist} $$ \leftarrow distributionH(x = c(0, 1, 2, 3, 4), p = c(0, 0.1, 0.6, 0.9, 1))$$ $$ MAT \leftarrow set.cell.MatH(mydist, BLOOD, r = 1, c = 1)$
```

ShortestDistance

Shortes distance from a point o a 2d segment

Description

Shortes distance from a point o a 2d segment

Usage

```
ShortestDistance(p, line)
```

Arguments

coordinates of a point

line a 2x2 matrix with the coordinates of two points defining a line

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Value

A numeric value, the Euclidean distance of point p to the line.

See Also

data2hist function and DouglasPeucker function

show

Method show for distributionH

Description

An overriding show function for a distributionH object. The function returns a representation of the histogram, if the number of bins is high the central part of the histogram is truncated.

Usage

```
## S4 method for signature 'distributionH'
show(object)
```

Arguments

object

a distributionH object

Examples

```
## ---- initialize a distributionH mydist <- distributionH(x = c(7, 8, 10, 15), p = c(0, 0.2, 0.7, 1)) # show the histogram mydist
```

show-MatH

Method show for MatH

Description

An overriding show method for a MatH object. The method returns a representation of the matrix using the mean and the standard deviation for each histogram.

Usage

```
## S4 method for signature 'MatH'
show(object)
```

Arguments

object

a MatH object

skewH 45

Examples

```
show(BL00D)
print(BL00D)
BL00D
```

skewH

Method skewH: computes the skewness of a distribution

Description

Skewness of a histogram (using the third standardized moment)

Usage

```
skewH(object)
## S4 method for signature 'distributionH'
skewH(object)
```

Arguments

object

a distributionH object

Value

A value for the skewness index

Author(s)

Antonio Irpino

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the skewness of mydist ---- skewH(mydist) #---> -1.186017
```

46 stdH

Description

A dataset containing the geographical coordinates of stations described in China_Month and China_Seas datasets

Format

a data.frame

Author(s)

Antonio Irpino, 2014-10-05

Source

raw data are available here: https://data.ess-dive.lbl.gov/view/doi:10.3334/CDIAC/CLI.
TR055. Climate Data Bases of the People's Republic of China 1841-1988 (TR055) DOI: 10.3334/CDIAC/cli.tr055

stdH

Method stdH: computes the standard deviation of a distribution

Description

Standard deviation of a histogram (i.e., the square root of the centered second moment)

Usage

```
stdH(object)
## S4 method for signature 'distributionH'
stdH(object)
```

Arguments

object a distributionH object

Value

A value for the standard deviation

Author(s)

Antonio Irpino

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Examples

```
## ---- A mydist distribution ---- mydist <- distributionH(x = c(1, 2, 3, 10), p = c(0, 0.1, 0.5, 1)) ## ---- Compute the standard deviation of mydist ---- stdH(mydist) #---> 2.563851
```

subsetHTS

Method subsetHTS: extract a subset of a histogram time series

Description

This functon return the mean of a distributionH object.

Usage

```
subsetHTS(object, from, to)
## S4 method for signature 'HTS,numeric,numeric'
subsetHTS(object, from, to)
```

Arguments

object a HTS object. A histogram 1d time series
from an integer, the initioal timepont
to an integer, a final timepoint

Value

```
a HTS object. A histogram 1d time series
```

```
SUB_RetHTS <- subsetHTS(RetHTS, from = 1, to = 20) # the first 20 elements
```

48 TdistributionH-class

summaryHTS

A function for summarize HTS

Description

A summarizer for HTS

Usage

```
summaryHTS(x)
```

Arguments

Χ

a HTS

Value

A matrix with basic statistics.

Examples

```
summaryHTS(subsetHTS(RetHTS, from = 1, to = 10))
```

TdistributionH-class Class TdistributionH

Description

Class TdistributionH defines a histogram with a time (point or period)

Usage

```
## S4 method for signature 'TdistributionH'
initialize(
   .Object,
   tstamp = numeric(0),
   period = list(start = -Inf, end = -Inf),
   x = numeric(0),
   p = numeric(0),
   m = numeric(0),
   s = numeric(0)
)
```

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Arguments

.Object	the type of object ("TdistributionH") a "distributionH" object with a time reference
tstamp	a numeric value related to a timestamp
period	a list of two values, the starting time and the ending time (alternative to tstamp if the distribution is observed along a period and not on a timestamp)
X	a vector of increasing values, the domain of the distribution (the same of $\mbox{distributionH}$ object)
p	a vector of increasing values from 0 to 1, the CDF of the distribution (the same of distributionH object)
m	a number, the mean of the distribution (the same of distributionH object)
S	a positive number, the standard deviation of the distribution (the same of distributionH object)

Description

Class TMatH defines a matrix of histograms, a TMatH object, with a time (a timepoint or a time window).

Usage

```
## S4 method for signature 'TMatH'
initialize(
   .Object,
   tstamp = numeric(0),
   period = list(start = -Inf, end = -Inf),
   mat = new("MatH")
)
```

Arguments

.Object the type of object ("TMatH")

tstamp a vector of time stamps, numeric.

period a list of pairs with a vectorof starting time and a vector ofending time. This parameter is used alternatively to tstamp if the distributions are related to time periods instead of timestamps

mat a MatH object

50 WassSqDistH

Description

Computes the squared L2 Wasserstein distance between two distributionH objects.

Usage

```
WassSqDistH(object1, object2, ...)
## S4 method for signature 'distributionH, distributionH'
WassSqDistH(object1 = object1, object2 = object2, details = FALSE)
```

Arguments

object1	is an object of distributionH class
object2	is an object of distributionH class
	optional parameters
details	(optional, default=FALSE) is a logical value, if TRUE returns the decomposition of the distance

Value

If details=FALSE, the function returns the squared L2 Wasserstein distance.

If details=TRUE, the function returns list containing the squared distance, its decomposition in three parts (position, size and shape) and the correlation coefficient between the quantile functions.

References

Irpino, A. and Romano, E. (2007): *Optimal histogram representation of large data sets: Fisher vs piecewise linear approximations*. RNTI E-9, 99-110.

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

```
## ---- create two distributionH objects ---- mydist1 <- distributionH(x = c(1, 2, 3), p = c(0, 0.4, 1)) mydist2 <- distributionH(x = c(7, 8, 10, 15), p = c(0, 0.2, 0.7, 1)) # -- compute the squared L2 Waaserstein distance WassSqDistH(mydist1, mydist2) # -- compute the squared L2 Waaserstein distance with details WassSqDistH(mydist1, mydist2, details = TRUE)
```

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WH.1d.PCA	Principal	components	analysis	of	histogram	variable	based	on
	Wasserste	in distance						

Description

The function implements a Principal components analysis of histogram variable based on Wasserstein distance. It performs a centered (not standardized) PCA on a set of quantiles of a variable. Being a distribution a multivalued description, the analysis performs a dimensional reduction and a visualization of distributions. It is a 1d (one dimension) because it is considered just one histogram variable.

Usage

```
WH.1d.PCA(
   data,
   var,
   quantiles = 10,
   plots = TRUE,
   listaxes = c(1:4),
   axisequal = FALSE,
   qcut = 1,
   outl = 0
)
```

Arguments

data	A MatH object (a matrix of distributionH).
var	An integer, the variable number.
quantiles	An integer, it is the number of quantiles used in the analysis.
plots	a logical value. Default=TRUE plots are drawn.
listaxes	A vector of integers listing the axis for the 2d factorial reperesntations.
axisequal	A logical value. Default TRUE, the plot have the same scale for the \boldsymbol{x} and the \boldsymbol{y} axes.
qcut	a number between 0.5 and 1, it is used for the plot of densities, and avoids very peaked densities. Default=1, all the densities are considered.
outl	a number between 0 (default) and 0.5 . For each distribution, is the amount of mass removed from the tails of the distribution. For example, if 0.1 , from each distribution is cut away a left tail and a right one each containing the 0.1 of mass.

Details

In the framework of symbolic data analysis (SDA), distribution-valued data are defined as multivalued data, where each unit is described by a distribution (e.g., a histogram, a density, or a quantile function) of a quantitative variable. SDA provides different methods for analyzing multivalued

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data. Among them, the most relevant techniques proposed for a dimensional reduction of multivalued quantitative variables is principal component analysis (PCA). This paper gives a contribution in this context of analysis. Starting from new association measures for distributional variables based on a peculiar metric for distributions, the squared Wasserstein distance, a PCA approach is proposed for distribution-valued data, represented by quantile-variables.

Value

a list with the results of the PCA in the MFA format of package FactoMineR for function MFA

References

Verde, R.; Irpino, A.; Balzanella, A., "Dimension Reduction Techniques for Distributional Symbolic Data," Cybernetics, IEEE Transactions on , vol.PP, no.99, pp.1,1 doi: 10.1109/TCYB.2015.2389653 keywords: Correlation; Covariance matrices; Distribution functions; Histograms; Measurement; Principal component analysis; Shape; Distributional data; Wasserstein distance; principal components analysis; quantiles, https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=7024099&isnumber=6352949

Examples

```
results <- WH.1d.PCA(data = BLOOD, var = 1, listaxes = c(1:2))
```

WH.bind

Method WH.bind

Description

It attaches two MatH objects with the same columns by row, or the same rows by colum.

Usage

```
WH.bind(object1, object2, byrow)
## S4 method for signature 'MatH,MatH'
WH.bind(object1, object2, byrow = TRUE)
```

Arguments

object1 a MatH object object2 a MatH object

byrow a logical value (default=TRUE) attaches the objects by row

Value

```
a MatH object,
```

WH.bind.col 53

See Also

```
WH.bind.row for binding by row, WH.bind.col for binding by column
```

Examples

```
# binding by row
M1 <- BLOOD[1:10, 1]
M2 <- BLOOD[1:10, 3]
MAT <- WH.bind(M1, M2, byrow = TRUE)
# binding by col
M1 <- BLOOD[1:10, 1]
M2 <- BLOOD[1:10, 3]
MAT <- WH.bind(M1, M2, byrow = FALSE)</pre>
```

WH.bind.col

Method WH.bind.col

Description

It attaches two MatH objects with the same rows by colums.

Usage

```
WH.bind.col(object1, object2)
## S4 method for signature 'MatH,MatH'
WH.bind.col(object1, object2)
```

Arguments

```
object1 a MatH object
object2 a MatH object
```

Value

```
a MatH object,
```

```
M1 <- BLOOD[1:10, 1]
M2 <- BLOOD[1:10, 3]
MAT <- WH.bind.col(M1, M2)
```

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WH.bind.row

Method WH.bind.row

Description

It attaches two MatH objects with the same columns by row.

Usage

```
WH.bind.row(object1, object2)
## S4 method for signature 'MatH,MatH'
WH.bind.row(object1, object2)
```

Arguments

```
object1 a MatH object
object2 a MatH object
```

Value

```
a MatH object,
```

Examples

```
M1 <- BLOOD[1:3, ]
M2 <- BLOOD[5:8, ]
MAT <- WH.bind.row(M1, M2)
```

WH.correlation

Method WH.correlation

Description

Compute the correlation matrix of a MatH object, i.e. a matrix of values consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.correlation(object, ...)
## S4 method for signature 'MatH'
WH.correlation(object, w = numeric(0))
```

WH.correlation2 55

Arguments

```
object a MatH object
... some optional parameters

w it is possible to add a vector of weights (positive numbers) having the same size of the rows of the MatH object, default = equal weight for each row
```

Value

a squared matrix with the (weighted) correlations indices

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

Examples

```
WH.correlation(BLOOD)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD))
WH.correlation(BLOOD, w = RN)</pre>
```

WH.correlation2

Method WH.correlation2

Description

Compute the correlation matrix using two MatH objects having the same number of rows, It returns a rectangular a matrix of numbers, consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.correlation2(object1, object2, ...)
## S4 method for signature 'MatH,MatH'
WH.correlation2(object1, object2, w = numeric(0))
```

Arguments

```
object1 a MatH object
object2 a MatH object
```

... some optional parameters

w it is possible to add a vector of weights (positive numbers) having the same size

of the rows of the MatH object, default = equal weight for each row

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Value

a rectangular matrix with the weighted sum of squares

Examples

```
M1 <- BLOOD[, 1]
M2 <- BLOOD[, 2:3]
WH.correlation2(M1, M2)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD))
WH.correlation2(M1, M2, w = RN)
```

WH.mat.prod

Method WH.mat.prod

Description

It is the matrix product of two MatH objects, i.e. two matrices of distributions, by using the dot product of two histograms that is consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.mat.prod(object1, object2, ...)
## S4 method for signature 'MatH,MatH'
WH.mat.prod(object1, object2, traspose1 = FALSE, traspose2 = FALSE)
```

Arguments

```
object1 a MatH object
object2 a MatH object
... other optional parameters
traspose1 a logical value, default=FALSE. If TRUE trasposes object1
traspose2 a logical value, default=FALSE. If TRUE trasposes object2
```

Value

a matrix of numbers

```
M1 <- BLOOD[1:5, ]
M2 <- BLOOD[6:10, ]
MAT <- WH.mat.prod(M1, M2, traspose1 = TRUE, traspose2 = FALSE)
```

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WH.mat.sum

Method WH.mat.sum

Description

It sums two MatH objects, i.e. two matrices of distributions, by summing the quantile functions of histograms. This sum is consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.mat.sum(object1, object2)
## S4 method for signature 'MatH,MatH'
WH.mat.sum(object1, object2)
```

Arguments

object1 a MatH object object2 a MatH object

Value

a MatH object,

Examples

```
# binding by row
M1 <- BLOOD[1:5, ]
M2 <- BLOOD[6:10, ]
MAT <- WH.mat.sum(M1, M2)</pre>
```

WH.MultiplePCA

Principal components analysis of a set of histogram variable based on Wasserstein distance

Description

(Beta version) The function implements a Principal components analysis of a set of histogram variables based on Wasserstein distance. It performs a centered (not standardized) PCA on a set of quantiles of a variable. Being a distribution a multivalued description, the analysis performs a dimensional reduction and a visualization of distributions. It is a 1d (one dimension) becase it is considered just one histogram variable.

Usage

```
WH.MultiplePCA(data, list.of.vars, quantiles = 10, outl = 0)
```

Arguments

data A MatH object (a matrix of distributionH).

list.of.vars A list of integers, the active variables.

quantiles An integer, it is the number of quantiles used in the analysis. Default=10.

outl a number between 0 (default) and 0.5. For each distribution, is the amount of mass removed from the tails of the distribution. For example, if 0.1, from each distribution is cut away a left tail and a right one each containing the 0.1 of mass.

Details

It is an extension of WH.1d.PCA to the multiple case.

Value

a list with the results of the PCA in the MFA format of package FactoMineR for function MFA

```
WH.plot_multiple_indivs
```

Plot histograms of individuals after a Multiple factor analysis of Histogram Variables

Description

(Beta version) The function plots histogram data of the individuals for a particular variable on a factorial palne after a Multiple factor analysis.

Usage

```
WH.plot_multiple_indivs(
  data,
  res,
  axes = c(1, 2),
  indiv = 0,
  var = 1,
  strx = 0.1,
  stry = 0.1,
  HISTO = TRUE,
  coor = 0,
  stat = "mean"
)
```

Arguments

data	a MatH object
res	Results from WH.MultiplePCA.
axes	A list of integers, the new factorial axes $c(1,2)$ are the default.
indiv	A list of objects (rows) of data to plot. Default=0 all the objects of data.
var	An integer indicating an original histogrma variable to plot.
strx	a resizing factor for the domain of histograms (default=0.1 means that each distribution has a support that is one tenth of the spread of the x axis)
stry	a resizing factor for the density of histograms (default=0.1 means that each distribution has a density that is one tenth of the spread of the y axis)
HISTO	a logical value. Default=TRUE plots histograms, FALSE plot smooth densities.
coor	(optional) if 0 (Default) takes the coordinates in res, if a a matrix is passed the coordinates are those passed $$
stat	(optional) if 'mean' (Default) a plot of individuals labeled by the means is produced. Otherwise if 'std', 'skewness' or 'kurtosis', data are labeled with this statistic.

Value

a plot of class ggplot

```
# Do a MultiplePCA on the BLOOD dataset
## Not run:
#' results=WH.MultiplePCA(BLOOD,list.of.vars = c(1:3))
# Plot histograms of variable 1 of BLOOD dataset on the first
# factorial plane showing histograms
WH.plot_multiple_indivs(BLOOD, results,
    axes = c(1, 2), var = 1, strx = 0.1,
    stry = 0.1, HISTO = TRUE
)
# Plot histograms of variable 1 of BLOOD dataset on the first
# factorial plane showing densities

WH.plot_multiple_indivs(BLOOD, results,
    axes = c(1, 2), var = 1, strx = 0.1,
    stry = 0.1, HISTO = FALSE
)

## End(Not run)
```

```
WH.plot_multiple_Spanish.funs
```

Plotting Spanish fun plots for Multiple factor analysis of Histogram Variables

Description

The function plots the circle of correlation of the quantiles of the histogrma variables after a Multiple factor analysis.

Usage

```
WH.plot_multiple_Spanish.funs(
  res,
  axes = c(1, 2),
  var = 1,
  LABS = TRUE,
  multi = TRUE,
  corplot = TRUE
)
```

Arguments

res	Results from WH.MultiplePCA, or WH.1D.PCA.
axes	A list of integers, the new factorial axes $c(1,2)$ are the default.
var	A list of integers are the variables to plot.
LABS	Logical, if TRUE graph is labeled, otherwise it does not.
multi	Logical, if TRUE (default) results come from a WH.MultiplePCA, if FALSE results come from WH.1D.PCA.
corplot	Logical, if TRUE (default) the plot reports correlations, if FALSE the coordinates of quantiles on the factorial plane

Value

a plot of class ggplot

```
# Do a MultiplePCA on the BLOOD dataset
## Not run:
res <- WH.MultiplePCA(BLOOD, list.of.vars = c(1:3))

## End(Not run)
# Plot results
## Not run:
WH.plot_multiple_Spanish.funs(res, axes = c(1, 2), var = c(1:3))
## End(Not run)</pre>
```

WH.regression.GOF 61

_	edness of Fit indices for Multiple regression of histogram variables ed on a two component model and L2 Wasserstein distance
---	--

Description

It computes three goodness of fit indices using the results and the predictions of a regression done with WH.regression.two.components function.

Usage

```
WH.regression.GOF(observed, predicted)
```

Arguments

observed A one column MatH object, the observed histogram variable predicted A one column MatH object, the predicted histogram variable.

Value

a list with the GOF indices

References

Irpino A, Verde R (in press 2015). Linear regression for numeric symbolic variables: a least squares approach based on Wasserstein Distance. ADVANCES IN DATA ANALYSIS AND CLASSIFICATION, ISSN: 1862-5347, DOI:10.1007/s11634-015-0197-7

An extended version is available on arXiv repository arXiv:1202.1436v2 https://arxiv.org/abs/1202.1436v2

WH.regression.two.components

Multiple regression analysis for histogram variables based on a two component model and L2 Wasserstein distance

Description

The function implements Multiple regression analysis for histogram variables based on a two component model and L2 Wasserstein distance. Taking as imput dependent histogram variable and a set of explanatory histogram variables the methods return a least squares estimation of a two component regression model based on the decomposition of L2 Wasserstein metric for distributional data.

Usage

```
WH.regression.two.components(data, Yvar, Xvars, simplify = FALSE, qua = 20)
```

Arguments

data A MatH object (a matrix of distributionH).

Yvar An integer, the dependent variable number in data.

Xvars A set of integers the explanantory variables in data.

simplify a logical argument (default=FALSE). If TRUE only few equally spaced quan-

tiles are considered (for speeding up the algorithm)

qua If simplify=TRUE is the number of quantiles to consider.

Details

A two component regression model is implemented. The observed variables are histogram variables according to the definition given in the framework of Symbolic Data Analysis and the parameters of the model are estimated using the classic Least Squares method. An appropriate metric is introduced in order to measure the error between the observed and the predicted distributions. In particular, the Wasserstein distance is proposed. Such a metric permits to predict the response variable as direct linear combination of other independent histogram variables.

Value

a named vector with the model estimated parameters

References

Irpino A, Verde R (in press 2015). Linear regression for numeric symbolic variables: a least squares approach based on Wasserstein Distance. ADVANCES IN DATA ANALYSIS AND CLASSIFICATION, ISSN: 1862-5347, DOI:10.1007/s11634-015-0197-7

An extended version is available on arXiv repository arXiv:1202.1436v2 https://arxiv.org/abs/1202.1436v2

Examples

```
model.parameters <- WH.regression.two.components(data = BLOOD, Yvar = 1, Xvars = c(2:3))
```

WH.regression.two.components.predict

Multiple regression analysis for histogram variables based on a two component model and L2 Wasserstein distance

Description

Predict distributions using the results of a regression done with WH.regression.two.components function

Usage

```
WH.regression.two.components.predict(data, parameters)
```

Arguments

data A MatH object (a matrix of distributionH) explantory part.

parameters A named vector with the parameter from a WH.regression.two.components

model

Value

a MatH object, the predicted histograms

References

Irpino A, Verde R (in press 2015). Linear regression for numeric symbolic variables: a least squares approach based on Wasserstein Distance. ADVANCES IN DATA ANALYSIS AND CLASSIFICATION, ISSN: 1862-5347, DOI:10.1007/s11634-015-0197-7

An extended version is available on arXiv repository arXiv:1202.1436v2 https://arxiv.org/abs/1202.1436v2

WH.SSQ2

WH.SSQ

Method WH.SSQ

Description

Compute the sum-of-squares-deviations (from the mean) matrix of a MatH object, i.e. a matrix of numbers, consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.SSQ(object, ...)
## S4 method for signature 'MatH'
WH.SSQ(object, w = numeric(0))
```

Arguments

object a MatH object
... some optional parameters

w it is possible to add a vector of weights (positive numbers) having the same size of the rows of the MatH object, default = equal weight for each row

Value

a squared matrix with the weighted sum of squares

Examples

```
WH.SSQ(BLOOD)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD))
WH.SSQ(BLOOD, w = RN)</pre>
```

WH.SSQ2

Method WH.SSQ2

Description

Compute the sum-of-squares-deviations (from the mean) matrix using two MatH objects having the same number of rows, It returns a rectangular a matrix of numbers, consistent with a set of distributions equipped with a L2 wasserstein metric.

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Usage

```
WH.SSQ2(object1, object2, ...)
## S4 method for signature 'MatH,MatH'
WH.SSQ2(object1, object2, w = numeric(0))
```

Arguments

object1 a MatH object object2 a MatH object

... some optional parameters

w it is possible to add a vector of weights (positive numbers) having the same size

of the rows of the MatH object, default = equal weight for each row

Value

a rectangular matrix with the weighted sum of squares

Examples

```
M1 <- BLOOD[, 1]
M2 <- BLOOD[, 2:3]
WH.SSQ2(M1, M2)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD))
WH.SSQ2(M1, M2, w = RN)
```

WH.var.covar

Method WH.var.covar

Description

Compute the variance-covariance matrix of a MatH object, i.e. a matrix of values consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.var.covar(object, ...)
## S4 method for signature 'MatH'
WH.var.covar(object, w = numeric(0))
```

Arguments

object a MatH object

... some optional parameters

w it is possible to add a vector of weights (positive numbers) having the same size

of the rows of the MatH object, default = equal weight for each row

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Value

a squared matrix with the (weighted) variance-covariance values

References

Irpino, A., Verde, R. (2015) *Basic statistics for distributional symbolic variables: a new metric-based approach* Advances in Data Analysis and Classification, DOI 10.1007/s11634-014-0176-4

Examples

```
WH.var.covar(BLOOD)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD))
WH.var.covar(BLOOD, w = RN)</pre>
```

WH.var.covar2

Method WH.var.covar2

Description

Compute the covariance matrix using two MatH objects having the same number of rows, It returns a rectangular a matrix of numbers, consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.var.covar2(object1, object2, ...)
## S4 method for signature 'MatH,MatH'
WH.var.covar2(object1, object2, w = numeric(0))
```

Arguments

```
object1 a MatH object
object2 a MatH object
```

... some optional parameters

w it is possible to add a vector of weights (positive numbers) having the same size

of the rows of the MatH object, default = equal weight for each row

Value

a rectangular matrix with the weighted sum of squares

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Examples

```
M1 <- BLOOD[, 1]
M2 <- BLOOD[, 2:3]
WH.var.covar2(M1, M2)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD))
WH.var.covar2(M1, M2, w = RN)
```

WH.vec.mean

Method WH.vec.mean

Description

Compute a histogram that is the weighted mean of the set of histograms contained in a MatH object, i.e. a matrix of histograms, consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.vec.mean(object, ...)
## S4 method for signature 'MatH'
WH.vec.mean(object, w = numeric(0))
```

Arguments

```
object a MatH object
... optional arguments

w it is possible to add a vector of weights (positive numbers) having the same size of the MatH object, default = equal weights for all
```

Value

```
a distributionH object, i.e. a histogram
```

```
hmean <- WH.vec.mean(BLOOD)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD) * get.MatH.ncols(BLOOD))
hmean <- WH.vec.mean(BLOOD, w = RN)</pre>
```

WH.vec.sum

Method WH.vec.sum

Description

Compute a histogram that is the weighted sum of the set of histograms contained in a MatH object, i.e. a matrix of histograms, consistent with a set of distributions equipped with a L2 wasserstein metric.

Usage

```
WH.vec.sum(object, ...)
## S4 method for signature 'MatH'
WH.vec.sum(object, w = numeric(0))
```

Arguments

object a MatH object optional arguments

w it is possible to add a vector of weights (positive numbers) having the same size

of the MatH object, default = equal weights for all cells

Value

a distributionH object, i.e. a histogram

Examples

```
hsum <- WH.vec.sum(BLOOD)
# generate a set of random weights
RN <- runif(get.MatH.nrows(BLOOD) * get.MatH.ncols(BLOOD))
hsum <- WH.vec.sum(BLOOD, w = RN)
### SUM of distributions ----</pre>
```

```
WH_2d_Adaptive_Kohonen_maps
```

Batch Kohonen self-organizing 2d maps using adaptive distances for histogram-valued data

Description

The function implements a Batch Kohonen self-organizing 2d maps algorithm for histogram-valued data.

Usage

```
WH_2d_Adaptive_Kohonen_maps(
  net = list(xdim = 4, ydim = 3, topo = c("rectangular")),
  kern.param = 2,
 TMAX = -9999,
 Tmin = -9999,
 niter = 30,
  repetitions,
  simplify = FALSE,
  qua = 10,
  standardize = FALSE,
  schema = 6,
  init.weights = "EQUAL",
 weight.sys = "PROD",
  theta = 2,
 Wfix = FALSE,
 verbose = FALSE,
  atleast = 2
)
```

Arguments

X	A MatH object (a matrix of distributionH).
net	a list describing the topology of the net list(xdim=number of rows,ydim=numbers of columns,topo=c('rectangular' or 'hexagonal')), see somgrid sintax in packageclass default net=list(xdim=4,ydim=3,topo=c('rectangular'))
kern.param	(default =2) the kernel parameter for the RBF kernel used in the algorithm
TMAX	a parameter useful for the iterations (default=2)
Tmin	a parameter useful for the iterations (default=0.2)
niter	maximum number of iterations (default=30)
repetitions	number of repetion of the algorithm (default=5), beacuase each launch may generate a local optimum
simplify	a logical parameter for speeding up computations (default=FALSE). If true data are recoded in order to have fast computations
qua	if simplify=TRUE number of equally spaced quantiles for recodify the histograms (default=10)
standardize	A logic value (default is FALSE). If TRUE, histogram-valued data are standardized, variable by variable, using the Wassertein based standard deviation. Use if one wants to have variables with std equal to one.
schema	a number from 1 to 4 1=A weight for each variable (default) 2=A weight for the average and the dispersion component of each variable 3=Same as 1 but a different set of weights for each cluster

4=Same as 2 but a different set of weights for each cluster

init.weights a string how to initialize weights: 'EQUAL' (default), all weights are the same, weight.sys a string. Weights may add to one ('SUM') or their product is equal to 1 ('PROD',

default).

theta a number. A parameter if weight.sys='SUM', default is 2.

Wfix a logical parameter (default=FALSE). If TRUE the algorithm does not use adap-

tive distances.

verbose a logical parameter (default=FALSE). If TRUE details of computation are shown

during the execution. #'

atleast integer. Check for degeneration of the map into a very low number of voronoi

sets. (default 2) 2 means that the map will have at least 2 neurons attracting data

instances in their voronoi sets.

Details

An extension of Batch Self Organised Map (BSOM) is here proposed for histogram data. These kind of data have been defined in the context of symbolic data analysis. The BSOM cost function is then based on a distance function: the L2 Wasserstein distance. This distance has been widely proposed in several techniques of analysis (clustering, regression) when input data are expressed by distributions (empirical by histograms or theoretical by probability distributions). The peculiarity of such distance is to be an Euclidean distance between quantile functions so that all the properties proved for L2 distances are verified again. An adaptative versions of BSOM is also introduced considering an automatic system of weights in the cost function in order to take into account the different effect of the several variables in the Self-Organised Map grid.

Value

a list with the results of the Batch Kohonen map

Slots

solution A list.Returns the best solution among the repetitionsetitions, i.e. the one having the minimum sum of squares criterion.

solution\$MAP The map topology.

solution\$IDX A vector. The clusters at which the objects are assigned.

solution\$cardinality A vector. The cardinality of each final cluster.

solution\$proto A MatH object with the description of centers.

solution\$Crit A number. The criterion (Sum od square deviation from the centers) value at the end of the run.

solution\$Weights.comp the final weights assigned to each component of the histogram variables solution\$Weight.sys a string the type of weighting system ('SUM' or 'PRODUCT')

quality A number. The percentage of Sum of square deviation explained by the model. (The higher the better)

References

Irpino A, Verde R, De Carvalho FAT (2012). Batch self organizing maps for interval and histogram data. In: Proceedings of COMPSTAT 2012. p. 143-154, ISI/IASC, ISBN: 978-90-73592-32-2

Examples

```
## Not run:
results <- WH_2d_Adaptive_Kohonen_maps(
    x = BLOOD,
    net = list(xdim = 2, ydim = 3, topo = c("rectangular")),
    repetitions = 2, simplify = TRUE,
    qua = 10, standardize = TRUE
)
## End(Not run)</pre>
```

WH_2d_Kohonen_maps

Batch Kohonen self-organizing 2d maps for histogram-valued data

Description

The function implements a Batch Kohonen self-organizing 2d maps algorithm for histogram-valued data.

Usage

```
WH_2d_Kohonen_maps(
    x,
    net = list(xdim = 4, ydim = 3, topo = c("rectangular")),
    kern.param = 2,
    TMAX = 2,
    Tmin = 0.2,
    niter = 30,
    repetitions = 5,
    simplify = FALSE,
    qua = 10,
    standardize = FALSE,
    verbose = FALSE
)
```

Arguments

X	A MatH object (a matrix of distributionH).
net	a list describing the topology of the net list(xdim=number of rows,ydim=numbers of columns,topo=c('rectangular' or 'hexagonal')), see somgrid sintax in packageclass default net=list(xdim=4,ydim=3,topo=c('rectangular'))
kern.param	(default =2) the kernel parameter for the RBF kernel used in the algorithm
TMAX	a parameter useful for the iterations (default=2)
Tmin	a parameter useful for the iterations (default=0.2)
niter	maximum number of iterations (default=30)

repetitions number of repetion of the algorithm (default=5), beacuase each launch may gen-

erate a local optimum

simplify a logical parameter for speeding up computations (default=FALSE). If true data

are recoded in order to have fast computations

qua if simplify=TRUE number of equally spaced quantiles for recodify the his-

tograms (default=10)

standardize A logic value (default is FALSE). If TRUE, histogram-valued data are standard-

ized, variable by variable, using the Wassertein based standard deviation. Use if

one wants to have variables with std equal to one.

verbose a logical parameter (default=FALSE). If TRUE details of computation are shown

during the execution.

Details

An extension of Batch Self Organised Map (BSOM) is here proposed for histogram data. These kind of data have been defined in the context of symbolic data analysis. The BSOM cost function is then based on a distance function: the L2 Wasserstein distance. This distance has been widely proposed in several techniques of analysis (clustering, regression) when input data are expressed by distributions (empirical by histograms or theoretical by probability distributions). The peculiarity of such distance is to be an Euclidean distance between quantile functions so that all the properties proved for L2 distances are verified again. An adaptative versions of BSOM is also introduced considering an automatic system of weights in the cost function in order to take into account the different effect of the several variables in the Self-Organised Map grid.

Value

a list with the results of the Batch Kohonen map

Slots

solution A list.Returns the best solution among the repetitionsetitions, i.e. the one having the minimum sum of squares criterion.

solution\$MAP The map topology.

solution\$IDX A vector. The clusters at which the objects are assigned.

solution\$cardinality A vector. The cardinality of each final cluster.

solution\$proto A MatH object with the description of centers.

solution\$Crit A number. The criterion (Sum od square deviation from the centers) value at the end of the run.

quality A number. The percentage of Sum of square deviation explained by the model. (The higher the better)

References

Irpino A, Verde R, De Carvalho FAT (2012). Batch self organizing maps for interval and histogram data. In: Proceedings of COMPSTAT 2012. p. 143-154, ISI/IASC, ISBN: 978-90-73592-32-2

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Examples

```
## Not run:
results <- WH_2d_Kohonen_maps(
    x = BL00D,
    net = list(xdim = 2, ydim = 3, topo = c("rectangular")),
    repetitions = 2, simplify = TRUE,
    qua = 10, standardize = TRUE
)
## End(Not run)</pre>
```

WH_adaptive.kmeans

K-means of a dataset of histogram-valued data using adaptive Wasserstein distances

Description

The function implements the k-means using adaptive distance for a set of histogram-valued data.

Usage

```
WH_adaptive.kmeans(
    x,
    k,
    schema = 1,
    init,
    rep,
    simplify = FALSE,
    qua = 10,
    standardize = FALSE,
    weight.sys = "PROD",
    theta = 2,
    init.weights = "EQUAL",
    verbose = FALSE
)
```

Arguments

A MatH object (a matrix of distributionH).

An integer, the number of groups.

schema

a number from 1 to 4

1=A weight for each variable (default)

2=A weight for the average and the dispersion component of each variable

3=Same as 1 but a different set of weights for each cluster

4=Same as 2 but a different set of weights for each cluster

init

(optional, do not use) initialization for partitioning the data default is 'RPART',

other strategies shoul be implemented.

rep	An integer, maximum number of repetitions of the algorithm (default rep=5).
simplify	A logic value (default is FALSE), if TRUE histograms are recomputed in order to speed-up the algorithm.
qua	An integer, if simplify=TRUE is the number of quantiles used for recodify the histograms.
standardize	A logic value (default is FALSE). If TRUE, histogram-valued data are standardized, variable by variable, using the Wassertein based standard deviation. Use if one wants to have variables with std equal to one.
weight.sys	a string. Weights may add to one ('SUM') or their product is equal to 1 ('PROD', default).
theta	a number. A parameter if weight.sys='SUM', default is 2.
init.weights	a string how to initialize weights: 'EQUAL' (default), all weights are the same, 'RANDOM', weights are initalised at random.
verbose	A logic value (default is FALSE). If TRUE, details on computations are shown.

Value

a list with the results of the k-means of the set of Histogram-valued data x into k cluster.

Slots

solution A list.Returns the best solution among the repetitions, i.e. the one having the minimum sum of squares criterion.

solution\$IDX A vector. The clusters at which the objects are assigned.

solution\$cardinality A vector. The cardinality of each final cluster.

solution\$centers A MatH object with the description of centers.

solution\$Crit A number. The criterion (Sum od square deviation from the centers) value at the end of the run.

quality A number. The percentage of Sum of square deviation explained by the model. (The higher the better)

References

Irpino A., Rosanna V., De Carvalho F.A.T. (2014). Dynamic clustering of histogram data based on adaptive squared Wasserstein distances. EXPERT SYSTEMS WITH APPLICATIONS, vol. 41, p. 3351-3366, ISSN: 0957-4174, doi: http://dx.doi.org/10.1016/j.eswa.2013.12.001

Examples

```
results <- WH_adaptive.kmeans(x = BLOOD, k = 2, rep = 10, simplify = TRUE, qua = 10, standardize = TRUE)
```

WH_adaptive_fcmeans

Fuzzy c-means with adaptive distances for histogram-valued data

Description

Fuzzy c-means of a dataset of histogram-valued data using different adaptive distances based on the L2 Wasserstein metric.

Usage

```
WH_adaptive_fcmeans(
    x,
    k = 5,
    schema,
    m = 1.6,
    rep,
    simplify = FALSE,
    qua = 10,
    standardize = FALSE,
    init.weights = "EQUAL",
    weight.sys = "PROD",
    theta = 2,
    verbose = FALSE
)
```

Arguments

x	A MatH object (a matrix of distributionH).
k	An integer, the number of groups.
schema	An integer. 1=one weight per variable, 2=two weights per variables (one for each component: the mean and the variability component), 3=one weight per variable and per cluster, 4= two weights per variable and per cluster.
m	A number grater than 0, a fuzziness coefficient (default m=1.6).
rep	An integer, maximum number of repetitions of the algorithm (default rep=5).
simplify	A logic value (default is FALSE), if TRUE histograms are recomputed in order to speed-up the algorithm.
qua	An integer, if simplify=TRUE is the number of quantiles used for recodify the histograms.
standardize	A logic value (default is FALSE). If TRUE, histogram-valued data are standardized, variable by variable, using the Wassertein based standard deviation. Use if one wants to have variables with std equal to one.
init.weights	A string. (default='EQUAL'). EQUAL, all variables or components have the same weight; 'RANDOM', a random assignment is done.
weight.sys	A string. (default='PROD') PROD, Weights product is equal to one. SUM, the weights sum up to one.

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theta A number. (default=2) A parameter for the system of weights summing up to

one.

verbose A logic value (default is FALSE). If TRUE some details are provided.

Value

The results of the fuzzy c-means of the set of Histogram-valued data x into k cluster.

solution A list.Returns the best solution among the repetitions, i.e. the ona having the

minimum sum of squares deviation.

solution\$membership

A matrix. The membership degree of each unit to each cluster.

solution\$IDX A vector. The crisp assignement to a cluster.

solution\$cardinality

A vector. The cardinality of each final cluster (after the crisp assignement).

solution\$Crit A number. The criterion (Sum od square deviation from the prototypes) value at

the end of the run.

quality A number. The percentage of Sum of square deviation explained by the model.

(The higher the better)

Examples

```
results <- WH_adaptive_fcmeans(
  x = BLOOD, k = 2, schema = 4, m = 1.5, rep = 3, simplify = TRUE,
  qua = 10, standardize = TRUE, init.weights = "EQUAL", weight.sys = "PROD"
)</pre>
```

WH_fcmeans

Fuzzy c-means of a dataset of histogram-valued data

Description

The function implements the fuzzy c-means for a set of histogram-valued data.

Usage

```
WH_fcmeans(x, k, m = 1.6, rep, simplify = FALSE, qua = 10, standardize = FALSE)
```

Arguments

x A MatH object (a matrix of distributionH).

k An integer, the number of groups.

m A number grater than 0, a fuzziness coefficient (default m=1.6).

rep An integer, maximum number of repetitions of the algorithm (default rep=5).

simplify A logic value (default is FALSE), if TRUE histograms are recomputed in order

to speed-up the algorithm.

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qua An integer, if simplify=TRUE is the number of quantiles used for recodify the

histograms.

standardize A logic value (default is FALSE). If TRUE, histogram-valued data are standard-

ized, variable by variable, using the Wassertein based standard deviation. Use if

one wants to have variables with std equal to one.

Value

a list with the results of the fuzzy c-means of the set of Histogram-valued data x into k cluster.

Slots

solution A list.Returns the best solution among the repetitions, i.e. the one having the minimum sum of squares deviation.

solution\$membership A matrix. The membership degree of each unit to each cluster.

solution\$IDX A vector. The crisp assignement to a cluster.

solution\$cardinality A vector. The cardinality of each final cluster (after the crisp assignement).

solution\$Crit A number. The criterion (Sum of square deviation from the prototypes) value at the end of the run.

quality A number. The percentage of Sum of square deviation explained by the model. (The higher the better)

Examples

```
results <- WH_fcmeans(x = BLOOD, k = 2, m = 1.5, rep = 10, simplify = TRUE, qua = 10, standardize = TRUE)
```

WH_hclust

Hierarchical clustering of histogram data

Description

The function implements a Hierarchical clustering for a set of histogram-valued data, based on the L2 Wassertein distance. Extends the hclust function of the **stat** package.

Usage

```
WH_hclust(
    x,
    simplify = FALSE,
    qua = 10,
    standardize = FALSE,
    distance = "WDIST",
    method = "complete"
)
```

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Arguments

X	A MatH object (a matrix of distributionH).
simplify	A logic value (default is FALSE), if TRUE histograms are recomputed in order to speed-up the algorithm.
qua	An integer, if simplify=TRUE is the number of quantiles used for recodify the histograms.
standardize	A logic value (default is FALSE). If TRUE, histogram-valued data are standardized, variable by variable, using the Wassertein based standard deviation. Use if one wants to have variables with std equal to one.
distance	A string default "WDIST" the L2 Wasserstein distance (other distances will be implemented)
method	A string, default="complete", is the the agglomeration method to be used. This should be (an unambiguous abbreviation of) one of "ward.D", "ward.D2", "single", "complete", "average" (= UPGMA), "mcquitty" (= WPGMA), "median" (= WPGMC) or "centroid" (= UPGMC).

Value

An object of class helust which describes the tree produced by the clustering process.

References

Irpino A., Verde R. (2006). A new Wasserstein based distance for the hierarchical clustering of histogram symbolic data. In: Batanjeli et al. Data Science and Classification, IFCS 2006. p. 185-192, BERLIN:Springer, ISBN: 3-540-34415-2

See Also

hclust of stat package for further details.

Examples

```
results <- WH_hclust(x = BLOOD, simplify = TRUE, method = "complete") plot(results) # it plots the dendrogram cutree(results, k = 5) # it returns the labels for 5 clusters
```

WH_kmeans K-means of a dataset of histogram-valued data

Description

The function implements the k-means for a set of histogram-valued data.

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Usage

```
WH_kmeans(
    x,
    k,
    rep = 5,
    simplify = FALSE,
    qua = 10,
    standardize = FALSE,
    verbose = FALSE
)
```

Arguments

x A MatH object (a matrix of distributionH).

k An integer, the number of groups.

rep An integer, maximum number of repetitions of the algorithm (default rep=5).

simplify A logic value (default is FALSE), if TRUE histograms are recomputed in order

to speed-up the algorithm.

qua An integer, if simplify=TRUE is the number of quantiles used for recodify the

histograms.

standardize A logic value (default is FALSE). If TRUE, histogram-valued data are standard-

ized, variable by variable, using the Wassertein based standard deviation. Use if

one wants to have variables with std equal to one.

verbose A logic value (default is FALSE). If TRUE, details on computations are shown.

Value

a list with the results of the k-means of the set of Histogram-valued data x into k cluster.

Slots

solution A list.Returns the best solution among the repetitions, i.e. the one having the minimum sum of squares criterion.

solution\$IDX A vector. The clusters at which the objects are assigned.

solution\$cardinality A vector. The cardinality of each final cluster.

solution\$centers A MatH object with the description of centers.

solution\$Crit A number. The criterion (Sum od square deviation from the centers) value at the end of the run.

quality A number. The percentage of Sum of square deviation explained by the model. (The higher the better)

References

Irpino A., Verde R., Lechevallier Y. (2006). Dynamic clustering of histograms using Wasserstein metric. In: Rizzi A., Vichi M.. COMPSTAT 2006 - Advances in computational statistics. p. 869-876, Heidelberg:Physica-Verlag

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Examples

```
results <- WH_kmeans(
  x = BLOOD, k = 2, rep = 10, simplify = TRUE,
  qua = 10, standardize = TRUE, verbose = TRUE)</pre>
```

WH_MAT_DIST

L2 Wasserstein distance matrix

Description

The function extracts the L2 Wasserstein distance matrix from a MatH object.

Usage

```
WH_MAT_DIST(x, simplify = FALSE, qua = 10, standardize = FALSE)
```

Arguments

x A MatH object (a matrix of distributionH).

simplify A logic value (default is FALSE), if TRUE histograms are recomputed in order

to speed-up the algorithm.

qua An integer, if simplify=TRUE is the number of quantiles used for recodify the

histograms.

standardize A logic value (default is FALSE). If TRUE, histogram-valued data are standard-

ized, variable by variable, using the Wasserstein based standard deviation. Use

if one wants to have variables with std equal to one.

Value

A matrix of squared L2 distances.

References

Irpino A., Verde R. (2006). A new Wasserstein based distance for the hierarchical clustering of histogram symbolic data. In: Batanjeli et al. Data Science and Classification, IFCS 2006. p. 185-192, BERLIN:Springer, ISBN: 3-540-34415-2

Examples

```
DMAT <- WH_MAT_DIST(x = BLOOD, simplify = TRUE)
```

[

extract from a MatH Method [

Description

This method overrides the "[" operator for a matH object.

Usage

```
## S4 method for signature 'MatH' x[i, j, ..., drop = TRUE]
```

Arguments

```
    x a matH object
    i a set of integer values identifying the rows
    j a set of integer values identifying the columns
    ... not useful
    drop a logical value inherited from the basic method "[" but not used (default=TRUE)
```

Value

A matH object

Examples

```
D <- BLOOD # the BLOOD dataset SUB_D <- BLOOD[c(1, 2, 5), c(1, 2)]
```

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