Package 'hdme'

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Description Penalized regression for generalized linear models for measurement error problems (aka. errors-in-variables). The package contains a version of the lasso (L1-penalization) which corrects for measurement error (Sorensen et al. (2015) <doi:10.5705 ss.2013.180="">). It also contains an implementation of the Generalized Matrix Uncertainty Selector, which is a version the (Generalized) Dantzig Selector for the case of measurement error (Sorensen et al. (2018) <doi:10.1080 10618600.2018.1425626="">).</doi:10.1080></doi:10.5705>		
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 ${\tt coef.corrected_lasso}$ ${\tt \it Extract\ \it Coefficients\ of\ a\ \it Corrected\ \it \it Lasso\ object}$

Description

Default coef method for a corrected_lasso object.

Usage

```
## S3 method for class 'corrected_lasso'
coef(object, ...)
```

Arguments

object Fitted model object returned by corrected_lasso.
... Other arguments (not used).

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Extract Coefficients of a Generalized Dantzig Selector Object

Description

Default coef method for a gds object.

Usage

```
## S3 method for class 'gds'
coef(object, all = FALSE, ...)
```

Arguments

object	Fitted model object returned by gds.
all	Logical indicating whether to show all coefficient estimates, or only non-zeros.
	Other arguments (not used).

 $\verb|coef.gmus|$

Extract Coefficients of a GMUS object

Description

Default coef method for a gmus object.

Usage

```
## S3 method for class 'gmus'
coef(object, all = FALSE, ...)
```

Arguments

object	Fitted model object returned by gmus.
all	Logical indicating whether to show all coefficient estimates, or only non-zeros. Only used when delta is a single value.
	Other arguments (not used).

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coef.gmu_lasso

Extract Coefficients of a GMU Lasso object

Description

Default coef method for a gmu_lasso object.

Usage

```
## S3 method for class 'gmu_lasso'
coef(object, all = FALSE, ...)
```

Arguments

object Fitted model object returned by gmu_lasso.

all Logical indicating whether to show all coefficient estimates, or only non-zeros.
Only used when delta is a single value.

Other arguments (not used).

corrected_lasso

Corrected Lasso

Description

Lasso (L1-regularization) for generalized linear models with measurement error.

Usage

```
corrected_lasso(
    W,
    y,
    sigmaUU,
    family = c("gaussian", "binomial", "poisson"),
    radii = NULL,
    no_radii = NULL,
    alpha = 0.1,
    maxits = 5000,
    tol = 1e-12
)
```

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Arguments

W	Design matrix, measured with error. Must be a numeric matrix.
у	Vector of responses.
sigmaUU	Covariance matrix of the measurement error.
family	Response type. Character string of length 1. Possible values are "gaussian", "binomial" and "poisson".
radii	Vector containing the set of radii of the 11-ball onto which the solution is projected. If not provided, the algorithm will select an evenly spaced vector of 20 radii.
no_radii	Length of vector radii, i.e., the number of regularization parameters to fit the corrected lasso for.
alpha	Step size of the projected gradient descent algorithm. Default is 0.1.
maxits	Maximum number of iterations of the project gradient descent algorithm for each radius. Default is 5000.
tol	Iteration tolerance for change in sum of squares of beta. Defaults . to 1e-12.

Details

Corrected version of the lasso for generalized linear models. The method does require an estimate of the measurement error covariance matrix. The Poisson regression option might sensitive to numerical overflow, please file a GitHub issue in the source repository if you experience this.

Value

An object of class "corrected_lasso".

References

Loh P, Wainwright MJ (2012). "High-dimensional regression with noisy and missing data: Provable guarantees with nonconvexity." *Ann. Statist.*, **40**(3), 1637–1664.

Sorensen O, Frigessi A, Thoresen M (2015). "Measurement error in lasso: Impact and likelihood bias correction." *Statistica Sinica*, **25**(2), 809-829.

```
# Example with linear regression
# Number of samples
n <- 100
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
# (typically estimated by replicate measurements)
sigmaUU <- diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = sqrt(diag(sigmaUU)))</pre>
```

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```
# Coefficient
beta \leftarrow c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y \leftarrow X \% *\% beta + rnorm(n, sd = 1)
# Run the corrected lasso
fit <- corrected_lasso(W, y, sigmaUU, family = "gaussian")</pre>
coef(fit)
plot(fit)
plot(fit, type = "path")
# Binomial, logistic regression
# Number of samples
n <- 1000
# Number of covariates
p <- 50
# True (latent) variables
X \leftarrow matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
sigmaUU \leftarrow diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = sqrt(diag(sigmaUU)))
# Response
y \leftarrow rbinom(n, size = 1, prob = plogis(X %*% c(rep(5, 5), rep(0, p-5))))
fit <- corrected_lasso(W, y, sigmaUU, family = "binomial")</pre>
plot(fit)
coef(fit)
```

cv_corrected_lasso

Cross-validated Corrected lasso

Description

Cross-validated Corrected lasso

Usage

```
cv_corrected_lasso(
    W,
    y,
    sigmaUU,
    n_folds = 10,
    family = "gaussian",
    radii = NULL,
    no_radii = 100,
    alpha = 0.1,
    maxits = 5000,
    tol = 1e-12
)
```

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Arguments

W	Design matrix, measured with error.
У	Vector of the continuous response value.
sigmaUU	Covariance matrix of the measurement error.
n_folds	Number of folds to use in cross-validation. Default is 100.
family	Only "gaussian" is implemented at the moment.
radii	Optional vector containing the set of radii of the 11-ball onto which the solution is projected.
no_radii	Length of vector radii, i.e., the number of regularization parameters to fit the corrected lasso for.
alpha	Optional step size of the projected gradient descent algorithm. Default is 0.1.
maxits	Optional maximum number of iterations of the project gradient descent algorithm for each radius. Default is 5000.
tol	Iteration tolerance for change in sum of squares of beta. Defaults to 1e-12.

Details

Corrected version of the lasso for the case of linear regression, estimated using cross-validation. The method does require an estimate of the measurement error covariance matrix.

Value

An object of class "cv_corrected_lasso".

References

Loh P, Wainwright MJ (2012). "High-dimensional regression with noisy and missing data: Provable guarantees with nonconvexity." *Ann. Statist.*, **40**(3), 1637–1664.

Sorensen O, Frigessi A, Thoresen M (2015). "Measurement error in lasso: Impact and likelihood bias correction." *Statistica Sinica*, **25**(2), 809-829.

```
# Gaussian
set.seed(100)
n <- 100; p <- 50 # Problem dimensions
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
# (typically estimated by replicate measurements)
sigmaUU <- diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = sqrt(diag(sigmaUU)))
# Coefficient
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y <- X %*% beta + rnorm(n, sd = 1)</pre>
```

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```
# Run the corrected lasso
cvfit <- cv_corrected_lasso(W, y, sigmaUU, no_radii = 5, n_folds = 3)
plot(cvfit)
print(cvfit)
# Run the standard lasso using the radius found by cross-validation
fit <- corrected_lasso(W, y, sigmaUU, family = "gaussian",
radii = cvfit$radius_min)
coef(fit)
plot(fit)</pre>
```

cv_gds

Cross-Validated Generalized Dantzig Selector

Description

Generalized Dantzig Selector with cross-validation.

Usage

```
cv_gds(
    X,
    y,
    family = "gaussian",
    no_lambda = 10,
    lambda = NULL,
    n_folds = 5,
    weights = rep(1, length(y))
)
```

Arguments

Χ	Design matrix.
У	Vector of the continuous response value.
family	Use "gaussian" for linear regression, "binomial" for logistic regression and "poisson" for Poisson regression.
no_lambda	Length of the vector lambda of regularization parameters. Note that if lambda is not provided, the actual number of values might differ slightly, due to the algorithm used by glmnet::glmnet in finding a grid of lambda values.
lambda	Regularization parameter. If not supplied and if no_lambda > 1, a sequence of no_lambda regularization parameters is computed with glmnet::glmnet. If no_lambda = 1 then the cross-validated optimum for the lasso is computed using glmnet::cv.glmnet.
n_folds	Number of cross-validation folds to use.
weights	A vector of weights for each row of X. Defaults to 1 per observation.

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Details

Cross-validation loss is calculated as the deviance of the model divided by the number of observations. For the Gaussian case, this is the mean squared error. Weights supplied through the weights argument are used both in fitting the models and when evaluating the test set deviance.

Value

An object of class cv_gds.

References

Candes E, Tao T (2007). "The Dantzig selector: Statistical estimation when p is much larger than n." *Ann. Statist.*, **35**(6), 2313–2351.

James GM, Radchenko P (2009). "A generalized Dantzig selector with shrinkage tuning." *Biometrika*, **96**(2), 323-337.

```
## Not run:
# Example with logistic regression
n <- 1000 # Number of samples
p <- 10 # Number of covariates
X \leftarrow matrix(rnorm(n * p), nrow = n) # True (latent) variables # Design matrix
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5)) # True regression coefficients
y <- rbinom(n, 1, (1 + \exp(-X \% \% beta))^{-1}) # Binomially distributed response
cv_fit <- cv_gds(X, y, family = "binomial", no_lambda = 50, n_folds = 10)</pre>
print(cv_fit)
plot(cv_fit)
# Now fit a single GDS at the optimum lambda value determined by cross-validation
fit <- gds(X, y, lambda = cv_fit$lambda_min, family = "binomial")</pre>
plot(fit)
# Compare this to the fit for which lambda is selected by GDS
# This automatic selection is performed by glmnet::cv.glmnet, for
# the sake of speed
fit2 <- gds(X, y, family = "binomial")</pre>
The following plot compares the two fits.
library(ggplot2)
library(tidyr)
df <- data.frame(fit = fit$beta, fit2 = fit2$beta, index = seq(1, p, by = 1))</pre>
ggplot(gather(df, key = "Model", value = "Coefficient", -index),
       aes(x = index, y = Coefficient, color = Model)) +
       geom_point() +
       theme(legend.title = element_blank())
## End(Not run)
```

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gds

Generalized Dantzig Selector

Description

Generalized Dantzig Selector

Usage

```
gds(X, y, lambda = NULL, family = "gaussian", weights = NULL)
```

Arguments

X	Design matrix.
У	Vector of the continuous response value.
lambda	Regularization parameter. Only a single value is supported.
family	Use "gaussian" for linear regression, "binomial" for logistic regression and "poisson" for Poisson regression.
weights	A vector of weights for each row of X.

Value

Intercept and coefficients at the values of lambda specified.

References

Candes E, Tao T (2007). "The Dantzig selector: Statistical estimation when p is much larger than n." *Ann. Statist.*, **35**(6), 2313–2351.

James GM, Radchenko P (2009). "A generalized Dantzig selector with shrinkage tuning." *Biometrika*, **96**(2), 323-337.

```
# Example with logistic regression
n <- 1000  # Number of samples
p <- 10  # Number of covariates
X <- matrix(rnorm(n * p), nrow = n)  # True (latent) variables  # Design matrix
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))  # True regression coefficients
y <- rbinom(n, 1, (1 + exp(-X %*% beta))^(-1))  # Binomially distributed response
fit <- gds(X, y, family = "binomial")
print(fit)
plot(fit)
coef(fit)

# Try with more penalization
fit <- gds(X, y, family = "binomial", lambda = 0.1)
coef(fit)</pre>
```

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```
coef(fit, all = TRUE)
# Case weighting
# Assume we wish to put more emphasis on predicting the positive cases correctly
# In this case we give the 1s three times the weight of the zeros.
weights <- (y == 0) * 1 + (y == 1) * 3
fit_w \leftarrow gds(X, y, family = "binomial", weights = weights, lambda = 0.1)
# Next we test this on a new dataset, generated with the same parameters
X_new <- matrix(rnorm(n * p), nrow = n)</pre>
y_{new} \leftarrow rbinom(n, 1, (1 + exp(-X_{new } %*% beta))^{(-1)})
# We use a 50 % threshold as classification rule
# Unweighted classification
classification <- ((1 + exp(- fit\frac{1}{2} intercept - \frac{1}{2} new \frac{1}{2} fit\frac{1}{2} beta))^(-1) > 0.5) * 1
# Weighted classification
classification_w <- ((1 + exp(- fit_wsintercept - X_new %*% fit_w<math>sintercept - X_new %*% fit_w)^(-1) > 0.5) * 1
# As expected, the weighted classification predicts many more 1s than 0s, since
# these are heavily up-weighted
table(classification, classification_w)
# Here we compare the performance of the weighted and unweighted models.
# The weighted model gets most of the 1s right, while the unweighted model
# gets the highest overall performance.
table(classification, y_new)
table(classification_w, y_new)
```

gmus

Generalized Matrix Uncertainty Selector

Description

Generalized Matrix Uncertainty Selector

Usage

```
gmus(W, y, lambda = NULL, delta = NULL, family = "gaussian", weights = NULL)
```

Arguments

W	Design matrix, measured with error. Must be a numeric matrix.
у	Vector of responses.
lambda	Regularization parameter.
delta	Additional regularization parameter, bounding the measurement error.
family	"gaussian" for linear regression, "binomial" for logistic regression or "poisson' for Poisson regression. Defaults go "gaussian".
weights	A vector of weights for each row of X.

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Value

An object of class "gmus".

References

Rosenbaum M, Tsybakov AB (2010). "Sparse recovery under matrix uncertainty." *Ann. Statist.*, **38**(5), 2620–2651.

Sorensen O, Hellton KH, Frigessi A, Thoresen M (2018). "Covariate Selection in High-Dimensional Generalized Linear Models With Measurement Error." *Journal of Computational and Graphical Statistics*, **27**(4), 739-749. doi:10.1080/10618600.2018.1425626. https://doi.org/10.1080/10618600.2018.1425626.

Examples

```
# Example with linear regression
set.seed(1)
n <- 100 # Number of samples
p <- 50 # Number of covariates
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)</pre>
# Measurement matrix (this is the one we observe)
W \leftarrow X + matrix(rnorm(n*p, sd = 1), nrow = n, ncol = p)
# Coefficient vector
beta \leftarrow c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y \leftarrow X \% + mean \text{ beta + rnorm}(n, \text{ sd = 1})
# Run the MU Selector
fit1 <- gmus(W, y)</pre>
# Draw an elbow plot to select delta
plot(fit1)
coef(fit1)
# Now, according to the "elbow rule", choose
# the final delta where the curve has an "elbow".
# In this case, the elbow is at about delta = 0.08,
# so we use this to compute the final estimate:
fit2 <- gmus(W, y, delta = 0.08)
# Plot the coefficients
plot(fit2)
coef(fit2)
coef(fit2, all = TRUE)
```

gmu_lasso

Generalized Matrix Uncertainty Lasso

Description

Generalized Matrix Uncertainty Lasso

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Usage

```
gmu_lasso(
    W,
    y,
    lambda = NULL,
    delta = NULL,
    family = "binomial",
    active_set = TRUE,
    maxit = 1000
)
```

Arguments

Design matrix, measured with error. Must be a numeric matrix.

y Vector of responses.

lambda Regularization parameter. If not set, lambda.min from glmnet::cv.glmnet is

used

delta Additional regularization parameter, bounding the measurement error.

family Character string. Currently "binomial" and "poisson" are supported.

active_set Logical. Whether or not to use an active set strategy to speed up coordinate

descent algorithm.

maxit Maximum number of iterations of iterative reweighing algorithm.

Value

An object of class "gmu_lasso".

References

Rosenbaum M, Tsybakov AB (2010). "Sparse recovery under matrix uncertainty." *Ann. Statist.*, **38**(5), 2620–2651.

Sorensen O, Hellton KH, Frigessi A, Thoresen M (2018). "Covariate Selection in High-Dimensional Generalized Linear Models With Measurement Error." *Journal of Computational and Graphical Statistics*, **27**(4), 739-749. doi:10.1080/10618600.2018.1425626. https://doi.org/10.1080/10618600.2018.1425626.

```
set.seed(1)
# Number of samples
n <- 200
# Number of covariates
p <- 100
# Number of nonzero features
s <- 10
# True coefficient vector
beta <- c(rep(1,s),rep(0,p-s))
# Standard deviation of measurement error
sdU <- 0.2</pre>
```

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```
# True data, not observed
X <- matrix(rnorm(n*p),nrow = n,ncol = p)
# Measured data, with error
W <- X + sdU * matrix(rnorm(n * p), nrow = n, ncol = p)
# Binomial response
y <- rbinom(n, 1, (1 + exp(-X%*%beta))**(-1))
# Run the GMU Lasso
fit <- gmu_lasso(W, y, delta = NULL)
print(fit)
plot(fit)
coef(fit)
# Get an elbow plot, in order to choose delta.
plot(fit)</pre>
```

mus

Matrix Uncertainty Selector

Description

Matrix Uncertainty Selector for linear regression.

Usage

```
mus(W, y, lambda = NULL, delta = NULL)
```

Arguments

W Design matrix, measured with error. Must be a numeric matrix.

y Vector of responses.

lambda Regularization parameter.

delta Additional regularization parameter, bounding the measurement error.

Details

This function is just a wrapper for gmus(W, y, lambda, delta, family = "gaussian").

Value

An object of class "gmus".

References

Rosenbaum M, Tsybakov AB (2010). "Sparse recovery under matrix uncertainty." *Ann. Statist.*, **38**(5), 2620–2651.

Sorensen O, Hellton KH, Frigessi A, Thoresen M (2018). "Covariate Selection in High-Dimensional Generalized Linear Models With Measurement Error." *Journal of Computational and Graphical Statistics*, **27**(4), 739-749. doi:10.1080/10618600.2018.1425626. https://doi.org/10.1080/10618600.2018.1425626.

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Examples

```
# Example with Gaussian response
set.seed(1)
# Number of samples
n <- 100
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)</pre>
# Measurement matrix (this is the one we observe)
W \leftarrow X + matrix(rnorm(n*p, sd = 1), nrow = n, ncol = p)
# Coefficient vector
beta \leftarrow c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y \leftarrow X \% \% beta + rnorm(n, sd = 1)
# Run the MU Selector
fit1 \leftarrow mus(W, y)
# Draw an elbow plot to select delta
plot(fit1)
coef(fit1)
# Now, according to the "elbow rule", choose the final delta where the curve has an "elbow".
# In this case, the elbow is at about delta = 0.08, so we use this to compute the final estimate:
fit2 <- mus(W, y, delta = 0.08)
plot(fit2) # Plot the coefficients
coef(fit2)
coef(fit2, all = TRUE)
```

plot.corrected_lasso

Description

Plot the output of corrected_lasso

Usage

```
## S3 method for class 'corrected_lasso'
plot(x, type = "nonzero", label = FALSE, ...)
```

Arguments

X	Object of class corrected_lasso, returned from calling corrected_lasso()
type	Type of plot. Either "nonzero" or "path". Ignored if length(x\$radii) == 1, in case of which all coefficient estimates are plotted at the given regularization parameter.
label	Logical specifying whether to add labels to coefficient paths. Only used when type = "path".
	Other arguments to plot (not used)

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Examples

```
# Example with linear regression
n <- 100 # Number of samples
p <- 50 # Number of covariates
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)</pre>
# Measurement error covariance matrix
# (typically estimated by replicate measurements)
sigmaUU \leftarrow diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = sqrt(diag(sigmaUU)))
# Coefficient
beta \leftarrow c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y \leftarrow X \% \% beta + rnorm(n, sd = 1)
# Run the corrected lasso
fit <- corrected_lasso(W, y, sigmaUU, family = "gaussian")</pre>
plot(fit)
```

Description

Plot the output of cv_corrected_lasso.

Usage

```
## S3 method for class 'cv_corrected_lasso'
plot(x, ...)
```

Arguments

x The object to be plotted, returned from cv_corrected_lasso.

. . . Other arguments to plot (not used).

Description

Plot the output of cv_gds.

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Usage

```
## S3 method for class 'cv_gds'
plot(x, ...)
```

Arguments

x The object to be plotted, returned from cv_gds.

... Other arguments to plot (not used).

plot.gds

Plot the estimates returned by gds

Description

Plot the number of nonzero coefficients at the given lambda.

Usage

```
## S3 method for class 'gds'
plot(x, ...)
```

Arguments

x An object of class gds

... Other arguments to plot (not used).

```
set.seed(1)
# Example with logistic regression
# Number of samples
n <- 1000
# Number of covariates
p <- 10
# True (latent) variables (Design matrix)
X \leftarrow matrix(rnorm(n * p), nrow = n)
# True regression coefficients
beta \leftarrow c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Binomially distributed response
y <- rbinom(n, 1, (1 + exp(-X %*% beta))^(-1))
# Fit the generalized Dantzig Selector
gds <- gds(X, y, family = "binomial")</pre>
\# Plot the estimated coefficients at the chosen lambda
plot(gds)
```

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plot.gmus

Plot the estimates returned by gmus and mus

Description

Plot the number of nonzero coefficients along a range of delta values if delta has length larger than 1, or the estimated coefficients if delta has length 1.

Usage

```
## S3 method for class 'gmus'
plot(x, ...)
```

Arguments

x An object of class gmus

... Other arguments to plot (not used).

```
# Example with linear regression
set.seed(1)
# Number of samples
n <- 100
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)</pre>
# Measurement matrix (this is the one we observe)
W \leftarrow X + matrix(rnorm(n*p, sd = 0.4), nrow = n, ncol = p)
# Coefficient vector
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y \leftarrow X \% + mean + morm(n, sd = 1)
# Run the MU Selector
mus1 \leftarrow mus(W, y)
# Draw an elbow plot to select delta
plot(mus1)
# Now, according to the "elbow rule", choose the final
# delta where the curve has an "elbow".
# In this case, the elbow is at about delta = 0.08, so
# we use this to compute the final estimate:
mus2 \leftarrow mus(W, y, delta = 0.08)
# Plot the coefficients
plot(mus2)
```

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plot.gmu_lasso

Plot the estimates returned by gmu_lasso

Description

Plot the number of nonzero coefficients along a range of delta values if delta has length larger than 1, or the estimated coefficients of delta has length 1.

Usage

```
## S3 method for class 'gmu_lasso'
plot(x, ...)
```

Arguments

```
x An object of class gmu_lasso... Other arguments to plot (not used).
```

Examples

```
set.seed(1)
n <- 200
p <- 50
s <- 10
beta <- c(rep(1,s),rep(0,p-s))
sdU <- 0.2

X <- matrix(rnorm(n*p),nrow = n,ncol = p)
W <- X + sdU * matrix(rnorm(n * p), nrow = n, ncol = p)

y <- rbinom(n, 1, (1 + exp(-X%*%beta))**(-1))
gmu_lasso <- gmu_lasso(W, y)

plot(gmu_lasso)</pre>
```

print.corrected_lasso Print a Corrected Lasso object

Description

Default print method for a corrected_lasso object.

Usage

```
## S3 method for class 'corrected_lasso'
print(x, ...)
```

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Arguments

x Fitted model object returned by corrected_lasso.

... Other arguments (not used).

```
print.cv_corrected_lasso
```

Print a Cross-Validated Corrected Lasso object

Description

Default print method for a cv_corrected_lasso object.

Usage

```
## S3 method for class 'cv_corrected_lasso'
print(x, ...)
```

Arguments

x Fitted model object returned by cv_corrected_lasso.

... Other arguments (not used).

print.cv_gds

Print a Cross-Validated GDS Object

Description

Default print method for a cv_gds object.

Usage

```
## S3 method for class 'cv_gds'
print(x, ...)
```

Arguments

x Fitted model object returned by cv_gds.

... Other arguments (not used).

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print.gds

Print a Generalized Dantzig Selector Object

Description

Default print method for a gds object.

Usage

```
## S3 method for class 'gds'
print(x, ...)
```

Arguments

x Fitted model object returned by gds.

... Other arguments (not used).

print.gmus

Print a GMUS object

Description

Default print method for a gmus object.

Usage

```
## S3 method for class 'gmus'
print(x, ...)
```

Arguments

x Fitted model object returned by gmus.

... Other arguments (not used).

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print.gmu_lasso

Print a GMU Lasso object

Description

Default print method for a gmu_lasso object.

Usage

```
## S3 method for class 'gmu_lasso'
print(x, ...)
```

Arguments

x Fitted model object returned by gmu_lasso.

... Other arguments (not used).

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