Package 'PWEXP'

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Type Package

Title Piecewise Exponential Distribution Prediction Model

Imports graphics, grDevices, stats, methods, utils, segmented,
foreach, doSNOW, parallel

Depends survival, fastmatch

Suggests knitr, RColorBrewer, rmarkdown

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Description Build piecewise exponential survival model for study design (planning) and event/timeline prediction.

URL <https://github.com/zjph602xtc/PWEXP>

BugReports <https://github.com/zjph602xtc/PWEXP/issues>

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boot.pwexp.fit   *Bootstrap a Piecewise Exponential Model*

Description

Bootstrap a existing piecewise exponential model or build a piecewise exponential model with bootstrapping.

Usage

```
## Default S3 method:
boot.pwexp.fit(time, event, nsim=100, breakpoint=NULL, nbreak=0,
               exclude_int=NULL, min_pt_tail=5, max_set=1000, seed=1818,
               optimizer='mle', tol=1e-4, parallel=FALSE, mc.core=4, ...)
## S3 method for class 'pwexp.fit'
boot.pwexp.fit(time, nsim=100, max_set=1000, seed=1818,
               optimizer='mle', tol=1e-4, parallel=FALSE, mc.core=4, ...)
```

Arguments

time	observed time from randomization or a pwexp.fit object.
event	the status indicator. See pwexp.fit.
nsim	the number of repeated bootstraping.
breakpoint	pre-specified breakpoints. See pwexp.fit.
nbreak	total number of breakpoints. See pwexp.fit.
exclude_int	an interval that excludes any estimated breakpoints. See pwexp.fit.
min_pt_tail	the minimum number of events used for estimating the tail (the hazard rate of the last piece). See pwexp.fit.
max_set	maximum estimated combination of breakpoints. See pwexp.fit.
seed	a random seed.
optimizer	one of the optimizers: mle, ols, or hybrid. See pwexp.fit.
tol	the minimum allowed gap between two breakpoints. The gap is calculated as (max(time)-min(time))*tol. Keep it as default in most cases.
parallel	logical. If TRUE, use **doSNOW** package to run in parallel.
mc.core	number of processes allowed to be run in parallel.
...	internal function reserved.

Details

Use bootstrap to repeatdly call `pwexp.fit` to estimate the uncertainty of parameters.

Value

A data frame (`res`) containing these columns:

`brk1, ..., brkx`	estimated breakpoints. The `attr(res,'brk')` can extract the result of break-point from each bootstrap sample (`res` is the returned model from `boot.pwexp.fit`).
`lam1, ..., lamx`	estimated piecewise hazard rates. The `attr(res,'lam')` can extract the result of hazard rates from bootstrap sample (`res` is the returned model from `boot.pwexp.fit`).
`likelihood`	the log-likelihood of the model.
`AIC`	the Akaike information criterion of the model.
`BIC`	the Bayesian information criterion of the model.

Author(s)

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See Also

`pwexp.fit`

Examples

```
event_dist <- function(n)rpwexp(n, rate = c(0.1, 0.01, 0.2), breakpoint =  c(5,14))
dat <- simdata(rand_rate = 20, drop_rate = 0.03,  total_sample = 1000,
               advanced_dist = list(event_dist=event_dist),
               add_column = c('censor_reason','event','followT','followT_abs'))

fit_res3 <- pwexp.fit(dat$followT, dat$event, nbreak = 2)
fit_res_boot <- boot.pwexp.fit(fit_res3, nsim = 10) # here nsim=10 is for demo purpose,
                                                    # pls increase it in practice
plot_survival(dat$followT, dat$event, xlim=c(0,40))
plot_survival(fit_res_boot, col='red', CI_par = list(col='red'))
brk_ci <- apply(attr(fit_res_boot, 'brk'), 2, function(x)quantile(x,c(0.025,0.975)))
abline(v=brk_ci, col='grey', lwd=2)
```

---

conditional piecewise exponential
The Conditional Piecewise Exponential Distribution

Description

Distribution function, quantile function and random generation for the piecewise exponential distribution t with piecewise rate `rate` given $t > qT$.

Usage

```
ppwexp_conditional(q, qT, rate=1, breakpoint=NULL, lower.tail=TRUE,
                    log.p=FALSE, one_piece, safety_check=TRUE)
qpwexp_conditional(p, qT, rate=1, breakpoint=NULL, lower.tail=TRUE,
                    log.p=FALSE, one_piece, safety_check=TRUE)
rpwexp_conditional(n, qT, rate, breakpoint=NULL)
```

Arguments

q	vector of quantiles.
p	vector of probabilities.
qT	the distribution is conditional on $t >$qT. qT can be a scalar or a vector with the same length of q or p.
n	number of observations. Must be a positive integer with length 1.
rate	a vector of rates in each piece.
breakpoint	a vector of breakpoints. The length is length(rate)-1. Can be NULL if rate is a single value.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
one_piece	(only required when safety_check=FALSE) whether the distribution only has one piece (i.e., rate is a single value and breakpoint=NULL).
safety_check	logical; whether check the input arguments; if FALSE, function has better computing performance by skipping all safety checks.

Details

See webpage https://zjph602xtc.github.io/PWEXP/ for more details for its survival function, cumulative density function, quantile function.

Value

ppwexp_conditional gives the conditional distribution function, qpwexp_conditional gives the conditional quantile function, and rpwexp_conditional generates conditional random variables.

The length of the result is determined by q, p or n for ppwexp_conditional, qpwexp_conditional or rpwexp_conditional. You can only specify a single piecewise exponential distribution every time you call these functions. This is different from the exponential distribution functions in package **stats**.

When the length of qT is 1, then all results are conditional on the same $t >$qT. In rpwexp_conditional, qT must be a scalar. When the length of qT equals to the length of q or p, then each value in the result is conditional on $t >$qT for each value in qT.

Arguments rate and breakpoint must match. The length of rate is the length of breakpoint + 1.

Author(s)

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See Also

[dpwexp](#), [ppwexp](#), [qpwexp](#), [rpwexp](#)

Examples

```
# CDF and qunatile function of conditional piecewise exp with rate 2, 1, 3 given t > 0.1
t <- seq(0.1, 1.2, 0.01)
F2_con <- ppwexp_conditional(t, qT=0.1, rate=c(2, 1, 3), breakpoint=c(0.3, 0.8))
plot(t, F2_con, type='l', col='red', lwd=2, main="CDF and Quantile Function of
    Conditional \nPiecewsie Exp Dist", xlim=c(0, 1.2), ylim=c(0, 1.2))
lines(F2_con, qpwexp_conditional(F2_con, qT=0.1, rate=c(2, 1, 3),
    breakpoint=c(0.3,0.8)), lty=2, lwd=2, col='red')

# compare with CDF and quantile function of unconditional piecewise exp with rate 2, 1, 3
t <- seq(0, 1.2, 0.01)
F2 <- ppwexp(t, rate=c(2, 1, 3), breakpoint=c(0.3,0.8))
lines(t, F2, lwd=2)
lines(F2, qpwexp(F2, rate=c(2, 1, 3), breakpoint=c(0.3,0.8)), lty=2, lwd=2)
abline(v=0.1, col='grey')
abline(h=0.1, col='grey')
legend('topleft', c('CDF of piecewise exp dist given t > 0.1', 'quantile
    function of piecewise exp dist given t > 0.1', 'CDF of piecewise exp dist',
  'quantile function of piecewise exp dist'), col=c('red', 'red', 'black', 'black'),
  lty=c(1, 2, 1, 2), lwd=2)

# use rpwexp_conditional function to generate piecewise exp samples with rate 2, 1, 3 given t > 0.1
r_sample_con <- rpwexp_conditional(3000, qT=0.1, rate=c(2, 1, 3), breakpoint=c(0.3,0.8))
plot(ecdf(r_sample_con), col='red', lwd=2,  main="Empirical CDF of Conditional
    Piecewsie Exp Dist", xlim=c(0, 1.2), ylim=c(0, 1))

# compare with its CDF
lines(seq(0.1, 1.2, 0.01), F2_con, lwd=2)
legend('topleft', c('empirial CDF of piecewise exp dist given t > 0.1',
  'true CDF of piecewise exp dist given t > 0.1'), col=c('red', 'black'), lty=c(1,2), lwd=2)
```

---

cut_dat	*Cut Data before a Specified Time*

Description

Take a subset of a dataset by constraining the randomization time <= cut time. Additionally, it updates the follow-up time, censor/event indicator, censor reason, accordingly.

Usage

```
cut_dat(cut, data, var_randT=NULL, var_followT=NULL, var_followT_abs=NULL,
     var_censor=NULL, var_event=NULL, var_censor_reason='status_at_end')
```

Arguments

`cut`	cut time (from the beginning of the trial); only rows with randomization time <= cut will be kept.
`data`	a data frame.
`var_randT`	character; the variable name of randomization time. If missing, then the randomization time will be treated as 0 and NO subjects will be filtered by `cut` time.
`var_followT`	character; the variable name of follow-up time (from randomization)
`var_followT_abs`	
	character; the variable name of follow-up time (from the beginning of the trial)
`var_censor`	character; the variable name of censoring (drop-out or death) indicator (1=censor, 0=event)
`var_event`	character; the variable name of event indicator (1=event, 0=censor)
`var_censor_reason`	
	character; the variable name of censoring reason (character variable). This variable will be created, if `data` does not contain it.

Details

We first filter rows that randomization time is equal to or less then `cut` time. Then we modify these columns (if provided):

- `var_followT`: change values to (cut - randomization time) if (follow-up time + randomization time) > cut

- `var_followT_abs`: change values to `cut` if (follow-up time from beginning) > cut

- `var_censor`: change values to 1 if (follow-up time from beginning) > cut

- `var_event`: change values to 0 if (follow-up time from beginning) > cut

- `var_censor_reason`: change values to 'cut' if (follow-up time from beginning) > cut

Value

A subset data frame with the same columns as `data`.

`var_censor_reason` is the only variable that is allowed to be absent in `data`. The function will create this variable in the returned data frame and set values 'cut' to the subjects whose (follow-up time from beginning) > cut.

Note

The original dataset `data` will NOT be modified.

Author(s)

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Examples

```
event_dist <- function(n)rpwexp(n, rate = c(0.1, 0.01, 0.2), breakpoint =  c(5,14))
dat <- simdata(rand_rate = 20, total_sample = 1000, drop_rate = 0.03,
                advanced_dist = list(event_dist=event_dist),
                add_column = c('censor_reason','event','followT','followT_abs'))
cut <- quantile(dat$randT, 0.8)
train <- cut_dat(var_randT = 'randT', cut = cut, data = dat,
                 var_followT = 'followT', var_followT_abs = 'followT_abs',
                 var_event = 'event', var_censor_reason = 'censor_reason')
```

---

cv.pwexp.fit   *Cross Validate a Piecewise Exponential Model*

Description

Cross Validate a existing piecewise exponential model.

Usage

```
## Default S3 method:
cv.pwexp.fit(time, event, nfold=5, nsim=100, breakpoint=NULL,
             nbreak=0, exclude_int=NULL, min_pt_tail=5, max_set=1000, seed=1818,
              optimizer='mle', tol=1e-4, parallel=FALSE, mc.core=4, ...)
## S3 method for class 'pwexp.fit'
cv.pwexp.fit(time, nfold=5, nsim=100, max_set=1000, seed=1818,
             optimizer='mle', tol=1e-4, parallel=FALSE, mc.core=4, ...)
```

Arguments

time	observed time from randomization or a `pwexp.fit` object.
event	the status indicator. See `pwexp.fit`.
nfold	the number of folds used in CV.
nsim	the number of simulations.
breakpoint	pre-specified breakpoints. See `pwexp.fit`.
nbreak	total number of breakpoints. See `pwexp.fit`.
exclude_int	an interval that excludes any estimated breakpoints. See `pwexp.fit`.
min_pt_tail	the minimum number of events used for estimating the tail (the hazard rate of the last piece). See `pwexp.fit`.
max_set	maximum estimated combination of breakpoints. See `pwexp.fit`.
seed	a random seed.
optimizer	one of the optimizers: mle, ols, or hybrid. See `pwexp.fit`.
tol	the minimum allowed gap between two breakpoints. The gap is calculated as (max(time)-min(time))*tol. Keep it as default in most cases.
parallel	logical. If TRUE, use **doSNOW** package to run in parallel.
mc.core	number of processes allowed to be run in parallel.
...	internal function reserved.

Details

Use cross validation obtain the prediction log likelihood.

Value

A vector of length `nsim` containing the CV log likelihood in each round of simulation.

Author(s)

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See Also

pwexp.fit

Examples

```
event_dist <- function(n)rpwexp(n, rate = c(0.1, 0.01, 0.2), breakpoint =  c(5,14))
dat <- simdata(rand_rate = 20, drop_rate = 0.03,  total_sample = 1000,
               advanced_dist = list(event_dist=event_dist),
               add_column = c('censor_reason','event','followT','followT_abs'))

# here nsim=10 is for demo purpose, pls increase it in practice!!

cv0 <- cv.pwexp.fit(dat$followT, dat$event, nsim = 10, nbreak = 0)
cv1 <- cv.pwexp.fit(dat$followT, dat$event, nsim = 10, nbreak = 1)
cv2 <- cv.pwexp.fit(dat$followT, dat$event, nsim = 10, nbreak = 2)
sapply(list(cv0,cv1,cv2), median)
```

---

piecewise exponential   *The Piecewise Exponential Distribution*

Description

Density, distribution function, quantile function and random generation for the piecewise exponential distribution with piecewise rate `rate`.

Usage

```
dpwexp(x, rate = 1, breakpoint = NULL, log = FALSE, one_piece, safety_check = TRUE)
ppwexp(q, rate = 1, breakpoint = NULL, lower.tail = TRUE, log.p = FALSE,
       one_piece, safety_check = TRUE)
qpwexp(p, rate = 1, breakpoint = NULL, lower.tail = TRUE, log.p = FALSE,
       one_piece, safety_check = TRUE)
rpwexp(n, rate = 1, breakpoint = NULL)
```

Arguments

`x, q`	vector of quantiles.
`p`	vector of probabilities.
`n`	number of observations. Must be a positive integer with length 1.
`rate`	a vector of rates in each piece.
`breakpoint`	a vector of breakpoints. The length is `length(rate)-1`. Can be NULL if rate is a single value.
`log, log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
`one_piece`	(only required when `safety_check=FALSE`) whether the distribution only has one piece (i.e., rate is a single value and breakpoint=NULL).
`safety_check`	logical; whether check the input arguments; if FALSE, function has better computing performance by skipping all safety checks.

Details

The piecewise distribution function with piecewise rate $\lambda_1, \ldots, \lambda_r$ is

$$f(t) = \lambda_{r+1} exp[\sum_{i=1}^{r}(\lambda_{i+1} - \lambda_i)d_i - \lambda_{r+1}t$$

for $d_r \leq t < d_{r+1}$.

See webpage <https://zjph602xtc.github.io/PWEXP/> for more details for its hazard function, cumulative hazard function, survival function, cumulative density function, quantile function.

Value

`dpwexp` gives the density, `ppwexp` gives the distribution function, `qpwexp` gives the quantile function, and `rpwexp` generates random deviates.

The length of the result is determined by x, q, p or n for `dpwexp`, `ppwexp`, `qpwexp` or `rpwexp`. You can only specify a single piecewise exponential distribution every time you call these functions. This is different from the exponential distribution functions in package **stats**.

Arguments `rate` and `breakpoint` must match. The length of rate is the length of breakpoint + 1.

Note

When `breakpoint=NULL`, the function calls exponential function in **stats**.

Author(s)

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See Also

[ppwexp_conditional](#), [qpwexp_conditional](#), [rpwexp_conditional](#)

Examples

```
# use rpwexp function to generate piecewise exp samples with rate 2, 1, 3
r_sample <- rpwexp(50000, rate=c(2, 1, 3), breakpoint=c(0.3, 0.8))
hist(r_sample, freq=FALSE, breaks=200, main="Density of Piecewsie Exp Dist",
    xlab='t', xlim=c(0, 1.2))

# piecewise exp density with rate 2, 1, 3
t <- seq(0, 1.5, 0.01)
f2 <- dpwexp(t, rate=c(2, 1, 3), breakpoint=c(0.3, 0.8))
points(t, f2, col='red', pch=16)

# exp distribution can be a special case of piecewise exp distribution
f1 <- dpwexp(t, rate=2)
lines(t, f1, lwd=2)
legend('topright', c('exp dist with rate 2','piecewise exp dist with rate 2, 1,
    3','histogram of piecewise exp dist with rate 2, 1, 3'),
    col=c('black','red'), fill=c(NA, NA, 'grey'), border=c('white', 'white',
    'black'), lty=c(1, NA, NA), pch=c(NA, 16, NA), lwd=2)

# CDF of piecewise exp with rate 2, 1, 3
F2 <- ppwexp(t, rate=c(2, 1, 3), breakpoint=c(0.3, 0.8), lower.tail=TRUE)
plot(t, F2, type='l', col='red', lwd=2, main="CDF and Quantile Function of
    Piecewsie Exp Dist", xlim=c(0, 1.5), ylim=c(0, 1.5))

# CDF of exp dist is compatible with our package
F1 <- ppwexp(t, rate=2, lower.tail=TRUE)
lines(t, F1, lwd=2)

# plot quantile functions of both distributions
lines(F1, qpwexp(F1, rate=2, lower.tail=TRUE), lty=2, lwd=2)
lines(F2, qpwexp(F2, rate=c(2, 1, 3), breakpoint=c(0.3,0.8), lower.tail=TRUE),
    col='red', lty=2, lwd=2)

abline(0, 1, col='grey')
legend('topleft', c('CDF of piecewise exp with rate 2, 1, 3', 'quantile
    function of piecewise exp with rate 2, 1, 3', 'CDF of exp with rate 2',
    'quantile function of exp with rate 2'), col=c('red', 'red', 'black',
    'black'), lty=c(1, 2, 1, 2), lwd=2)
```

---

plot_event   *Plot Cumulative Event Curve*

Description

Plot cumulative event curve with right censoring data.

Usage

```
## Default S3 method:
plot_event(time, event, abs_time=TRUE, additional_event=0,
```

```
          add=FALSE, plot=TRUE, xyswitch=FALSE, ...)
## S3 method for class 'predict.pwexp.fit'
plot_event(time, abs_time=TRUE, add=TRUE, plot=TRUE,
          xyswitch=FALSE, eval_at=NULL, ...)
## S3 method for class 'predict.boot.pwexp.fit'
plot_event(time, abs_time=TRUE, alpha=0.1, type='confidence',
          add=TRUE, plot=TRUE, xyswitch=FALSE, eval_at=NULL,
          show_CI=TRUE, CI_par=NULL, ...)
```

Arguments

`time`	observed/follow-up time from individual randomization time (`abs_time=FALSE`) or from the first subject randomization time (`abs_time=TRUE`); or a predicted object from [predict.pwexp.fit](), or a predicted object with bootstrapping from [predict.boot.pwexp.fit]().
`abs_time`	logical; if TRUE, `time` is the time from first randomization of the trial. if FALSE, `time` is the time from the randomization of each subject.
`event`	the status indicator, 0=censor, 1=event. Other choices are TRUE/FALSE (TRUE = event).
`additional_event`	
	adding the cumulative number of events by a constant number from the beginning.
`add`	logical; if TRUE add lines to current plot.
`plot`	logical; if FALSE, do not plot any lines, but return the line data
`xyswitch`	logical; if TRUE, x-axis will be cumulative number of events and y will be the time.
`eval_at`	a vector of the time (when `xyswitch=FALSE`) or the number of events (when `xyswitch=TRUE`) that you want to make prediction on.
`alpha`	the significance level of the confidence interval.
`type`	the type of prediction required. The default `confidence` returns the confidence interval without random error; the alternative `predictive` returns the predictive interval.
`show_CI`	logical; if TRUE add confidence interval of the estimated event curve.
`CI_par`	a list of parameters to control the apperance of lines of confidence intervals. The values pass to [lines]().
`...`	other arguments (e.g., `lwd`, etc.) are passed over to [plot]().

Details

A convenient function to calculate and plot the cumulative number of events.

Parameters in `...` are passed to [plot]() function to control the appearance of the event curve; parameters in `CI_par` are passed to [lines]() function to control the appearance of confidence intervals. See examples for usage.

By default, `plot_event` plots a data frame in a new figure; and plots a predicted model in existing figure.

Value

A data frame containing these columns:

`time`	sorted time
`n_event`	cumulative number of events

Author(s)

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See Also

[plot_survival](#)

Examples

```
set.seed(1818)
event_dist <- function(n)rpwexp(n, rate = c(0.1, 0.01, 0.2), breakpoint =  c(5,14))
dat <- simdata(rand_rate = 20, drop_rate = 0.03,  total_sample = 1000,
               advanced_dist = list(event_dist=event_dist),
               add_column = c('censor_reason','event','followT','followT_abs'))
cut <- quantile(dat$randT, 0.8)
train <- cut_dat(var_randT = 'randT', cut = cut, data = dat,
                 var_followT = 'followT', var_followT_abs = 'followT_abs',
                 var_event = 'event', var_censor_reason = 'censor_reason')

fit_res3 <- pwexp.fit(train$followT, train$event, nbreak = 2)
fit_res_boot <- boot.pwexp.fit(fit_res3, nsim = 8) # here nsim=8 is for demo purpose,
                                                   # pls increase it in practice

drop_indicator <- ifelse(train$censor_reason=='drop_out' & !is.na(train$censor_reason),1,0)
fit_res_censor <- pwexp.fit(train$followT, drop_indicator, nbreak = 0)
fit_res_censor_boot <- boot.pwexp.fit(fit_res_censor, nsim = 8)

cut_indicator <- train$censor_reason=='cut'
cut_indicator[is.na(cut_indicator)] <- 0

predicted_boot <- predict(fit_res_boot, cut_indicator = cut_indicator,
                     analysis_time = cut,  censor_model_boot=fit_res_censor_boot,
                     future_rand=list(rand_rate=20, total_sample=NROW(dat)-NROW(train)))

plot_event(dat$followT_abs, abs_time = TRUE, event=dat$event, ylim=c(0,800))
plot_event(predicted_boot, eval_at = seq(40,90,5), CI_par = list(lty=3, lwd=2))

plot_event(dat$followT_abs, xlim=c(0,800), event=dat$event, xyswitch = TRUE)
plot_event(predicted_boot, xyswitch = TRUE, eval_at = seq(600,900,50))
```

---

plot_survival   *Plot Survival Curve*

Description

Plot KM curve with right censoring data or the survival curve of a fitted piecewise exponential model.

Usage

```
## Default S3 method:
plot_survival(time, event, add=FALSE, conf.int=FALSE, mark.time=TRUE,
        lwd=2, xlab='Follow-up time', ylab='Survival function', ...)
## S3 method for class 'pwexp.fit'
plot_survival(time, add=TRUE, show_breakpoint=TRUE,
        breakpoint_par=NULL, ...)
## S3 method for class 'boot.pwexp.fit'
plot_survival(time, add=TRUE, alpha=0.1, show_breakpoint=TRUE,
        breakpoint_par=NULL, show_CI=TRUE, CI_par=NULL, ...)
```

Arguments

time	observed time from randomization or a `pwexp.fit`/ `boot.pwexp.fit` object.
event	the status indicator, normally 0=censor, 1=event. Other choices are TRUE/FALSE (TRUE = event).
add	logical; if TRUE add lines to current plot.
show_breakpoint	
	logical; if TRUE add vertial dashed lines to indicate breakpoints.
breakpoint_par	a list of parameters to control the apperance of vertical lines of breakpoionts. The values pass to `abline`.
alpha	the significance level of the confidence interval.
show_CI	logical; if TRUE add confidence interval of the estimated curve. For KM esitmator, use `conf.int=TRUE` to show CI band.
CI_par	a list of parameters to control the apperance of lines of confidence intervals. The values pass to `lines`.
conf.int	determines whether pointwise confidence intervals will be plotted. Passed over to `plot.survfit`.
mark.time	controls the labeling of the curves. Passed over to `plot.survfit`.
lwd	line width of the KM curve.
xlab	x label.
ylab	y label.
...	other arguments are passed over to `plot.survfit` (default method) or `plot` (for class pwexp.fit).

Details

For the default method, this a wrapper of `plot.survfit` function to plot right censoring data.

For class pwexp.fit, parameters in ... are passed to `plot` function to control the appearance of the survival curve; parameters in breakpoint_par are passed to `abline` function to control the appearance of vertical lines of breakpoints. See examples for usage.

For class boot.pwexp.fit, parameters in ... are passed to `plot` function to control the appearance of the survival curve; parameters in breakpoint_par are passed to `abline` function to control the appearance of vertical lines of breakpoints; parameters in CI_par are passed to `lines` function to control the appearance of confidence intervals. See examples for usage.

Value

No return value.

Author(s)

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See Also

`plot_event`

Examples

```
event_dist <- function(n)rpwexp(n, rate = c(0.1, 0.01, 0.2), breakpoint =  c(5,14))
dat <- simdata(rand_rate = 20, drop_rate = 0.03,  total_sample = 1000,
               advanced_dist = list(event_dist=event_dist),
               add_column = c('censor_reason','event','followT','followT_abs'))

plot_survival(dat$followT, dat$event, xlim=c(0,40))

fit_res <- pwexp.fit(dat$followT, dat$event, nbreak = 2)
plot_survival(fit_res, col='red', lwd=3, breakpoint_par = list(col='grey', lwd=2.5))
```

---

predict   *Predict Events for Piecewise Exponential Model*

Description

Obtians event prediction and (optionally) confidence interval from a piecewise exponential model.

Usage

```
## S3 method for class 'pwexp.fit'
predict(object, cut_indicator=NULL, analysis_time, censor_model=NULL,
      n_each=100, future_rand=NULL, seed=1818, ...)
## S3 method for class 'boot.pwexp.fit'
predict(object, cut_indicator=NULL, analysis_time,
      censor_model_boot=NULL, n_each=10, future_rand=NULL,
      seed=1818, ...)
```

Arguments

object	a [pwexp.fit](#) or [boot.pwexp.fit](#) object. It is the event model for the primary endpoint.
cut_indicator	(optional) A vector indicates which subject is censored due to the end of the trial. The length of the vector is the number of rows of the data used in event_model/event_model_boot. Value 0 means the subject had event or drop-out or death before the end of the trial; 1 means the subject didn't have any of these. See details.
analysis_time	the analysis time. This is the time length from the start of the trial to the time collecting data for the model.
censor_model	an object of class pwexp.fit returned by the [pwexp.fit](#) function. It is the censoring model for drop-out and death.
censor_model_boot	an object of class boot.pwexp.fit returned by the [boot.pwexp.fit](#) function. It is the censoring model with bootstrapping for drop-out and death.
n_each	the number of iterations for each bootstrapping sample to obtain predicitive CI. Typically, a value of 10 to 100 should be enough.
future_rand	the randomization curve in the following times. Can be NULL if all subjects have been randomized. You can specify **future** rand rate and **future** total number of samples to be randomized by list(rand_rate= ,total_sample=) or specify the **future** number of randomization each month by list(rand_n=). See details.
seed	a random seed.
...	internal function reserved.

Details

The prediction will have a confidence interval only if the event model and censor model are bootstrap models.

cut_indicator indicates the status of each subject in the event_model/event_model_boot model at the end of the trial. Value 1 means the subject didn't have events, drop-out or death at the end of the trial (or say, the subject was censored due to the end of the trial). When cut_indicator is NOT provided, we assign value 1 to the subject who didn't have event (or drop-out, or death) in both event_model/event_model_boot and censor_model/censor_model_boot models.

future_rand is a list determining the parameter of randomization curve in the following times. For example, you specify randomization rate=10pt/month and total sample size=1000 by list(rand_rate=10 ,total_sample=1000) or specify the number of randomization each month (e.g., 10,15,30,30 in four months) by list(n_rand=c(10,15,30,30)).

Value

A list containing:

- event_fun number of events vs. time curve function in each bootstrap.
- time_fun time vs. number of events curve function in each bootstrap.

This returned list should be used in [plot_event](#) function for summarizing its result.

Author(s)

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See Also

[plot_event](#)

Examples

```
set.seed(1818)
event_dist <- function(n)rpwexp(n, rate = c(0.1, 0.2), breakpoint = 14)
dat <- simdata(rand_rate = 20, drop_rate = 0.03,  total_sample = 500,
                advanced_dist = list(event_dist=event_dist),
                add_column = c('censor_reason','event','followT','followT_abs'))
cut <- quantile(dat$randT, 0.8)
train <- cut_dat(var_randT = 'randT', cut = cut, data = dat,
                 var_followT = 'followT', var_followT_abs = 'followT_abs',
                 var_event = 'event', var_censor_reason = 'censor_reason')

fit_res3 <- pwexp.fit(train$followT, train$event, nbreak = 1)
fit_res_boot <- boot.pwexp.fit(fit_res3, nsim = 8) # here nsim=8 is for demo purpose,
                                                   # pls increase it in practice

drop_indicator <- ifelse(train$censor_reason=='drop_out' & !is.na(train$censor_reason),1,0)
fit_res_censor <- pwexp.fit(train$followT, drop_indicator, nbreak = 0)
fit_res_censor_boot <- boot.pwexp.fit(fit_res_censor, nsim = 8)

cut_indicator <- train$censor_reason=='cut'
cut_indicator[is.na(cut_indicator)] <- 0

predicted_boot <- predict(fit_res_boot, cut_indicator = cut_indicator,
                       analysis_time = cut,  censor_model_boot=fit_res_censor_boot,
                       future_rand=list(rand_rate=20, total_sample=NROW(dat)-NROW(train)))
plot_event(train$followT_abs, train$event, xlim=c(0,69), ylim=c(0,800))
plot_event(predicted_boot, eval_at = 40:90)
plot_event(train$followT_abs, train$event, xyswitch = TRUE, ylim=c(0,69), xlim=c(0,800))
plot_event(predicted_boot, xyswitch = TRUE, eval_at = 600:900)
```

Description

Fit the piecewise exponential distribution with right censoring data. User can specifity all breakpoints, some of the breakpoints or let the function estimate the breakpoints.

Usage

```
pwexp.fit(time, event, breakpoint=NULL, nbreak=0, exclude_int=NULL, min_pt_tail=5,
        max_set=10000, seed=1818, trace=FALSE, optimizer='mle', tol=1e-4)
```

Arguments

time	observed time from randomization. For right censored data, this is the follow-up time.
event	the status indicator, normally 0=censor, 1=event. Other choices are TRUE/FALSE (TRUE = event).
breakpoint	fixed breakpoints. Pre-specifity some breakpionts. The maximum value must be earlier than the last event time.
nbreak	total number of breakpoints in the model. This number includes the points specified in breakpoint. If nbreak=NULL, then nbreak=ceiling(8*(# unique events)^0.2).
exclude_int	an interval that excludes any estimated breakpoints (e.g., exclude_int=c(10,Inf) will exclude any estimated breakpoints after t=10). See details.
min_pt_tail	the minimum number of events used for estimating the tail (the hazard rate of the last piece). See details.
max_set	maximum estimated combination of breakpoints.
seed	a random seed.
trace	(internal use) logical; if TRUE, the returned data frame contains the log-likelihood of all possible breakpoints instead of the one with maximum likelihood.
optimizer	one of the optimizers: mle, ols, or hybrid.
tol	the minimum allowed gap between two breakpoints. The gap is calculated as (max(time)-min(time))*tol. Keep it as default in most cases.

Details

See webpage <https://zjph602xtc.github.io/PWEXP/> for a detailed description of the model and optimizers.

If user specifies breakpoint, we will check the values to make the model identifiable. Any breakpoints after the last event time will be removed; Any breakpoints before the first event time will be removed; a mid-point will be used if there are NO events between any two concesutive breakpoints. A warning will be given.

If user sets nbreak=NULL, then the function will automatically apply nbreak=ceiling(8*(# unique events)^0.2). This empirical number of breakpoints is for the reference below, and it may be too large in many cases.

Argument exclude_int is a vector of two values such as exclude_int=c(a, b) (b can be Inf). It defines an interval that excludes any estimated breakpoints. It is helpful when excluding breakpoints that are too close to the tail.

In order to obtain a more robust hazard rate estimation of the tail, user can set min_pt_tail to the minimum number of events for estimating the tail (last piece of the piecewise exponential). It only works for optimizer='mle'.

Value

A data frame (res) containing these columns:

brk1, ..., brkx	estimated breakpoints. The attr(res,'brk') can extract the vector of breakpoint from the model (res is the returned model from pwexp.fit).
lam1, ..., lamx	estimated piecewise hazard rates. The attr(res,'lam') can extract the vector of hazard rates from the model (res is the returned model from pwexp.fit).
likelihood	the log-likelihood of the model.
AIC	the Akaike information criterion of the model.
BIC	the Bayesian information criterion of the model.

Author(s)

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References

Muller, H. G., & Wang, J. L. (1994). Hazard rate estimation under random censoring with varying kernels and bandwidths. Biometrics, 61-76.

See Also

boot.pwexp.fit, cv.pwexp.fit

Examples

```
event_dist <- function(n)rpwexp(n, rate=c(0.1, 0.01, 0.2), breakpoint=c(5,14))
dat <- simdata(rand_rate = 20, total_sample = 1000, drop_rate = 0.03,
               advanced_dist = list(event_dist=event_dist),
               add_column = c('censor_reason','event','followT','followT_abs'))
cut <- quantile(dat$randT, 0.8)
train <- cut_dat(var_randT = 'randT', cut = cut, data = dat,
                 var_followT = 'followT', var_followT_abs = 'followT_abs',
                 var_event = 'event', var_censor_reason = 'censor_reason')

fit_a0 <- pwexp.fit(train$followT, train$event, breakpoint = c(5,14))
fit_a1 <- pwexp.fit(train$followT, train$event, nbreak = 2, breakpoint = c(14))
fit_b0 <- pwexp.fit(train$followT, train$event, nbreak = 0)
```

```
fit_b1 <- pwexp.fit(train$followT, train$event, nbreak = 1)
fit_b2 <- pwexp.fit(train$followT, train$event, nbreak = 2)
```

---

simdata   *Simulate Survival Data*

Description

simdata is used to simulate a clinical trial data with time-to-event endpoints.

Usage

```
simdata(group="Group 1", strata="Strata 1", allocation=1,
    event_lambda=NA, drop_rate=NA, death_lambda=NA, n_rand=NULL,
    rand_rate=NULL, total_sample=NULL, add_column=c('followT'),
    simplify=TRUE, advanced_dist=NULL)
```

Arguments

group
: a character vector of the names of each group (e.g., c('treatment','control')).

strata
: a character vector of the names of strata in groups (e.g., c('young','old')).

allocation
: the relative ratio of sample size in each subgroup (group*strata). See details. The value will be recycled if the length is less than needed.

event_lambda
: the hazard rate of the primary endpoint (event). See details. The value will be recycled if the length is less than needed.

drop_rate
: (optional) the drop-out rate (patients/month). Not hazard rate. See details. The value will be recycled if the length is less than needed.

death_lambda
: (optional) the hazard rate of death. The value will be recycled if the length is less than needed.

n_rand
: (required when rand_rate=NULL) a vector of the number of randomization each month; can be non-integers.

rand_rate
: (required when n_rand=NULL) the randomization rate (patients/month; can be non-integer).

total_sample
: (required when n_rand=NULL) total scheduled sample size.

add_column
: request additional columns of the returned data frame.
  Valid options are:

  - 'eventT_abs': absolute event time from the beginning of the trial (=eventT+randT)
  - 'dropT_abs': absolute drop-out time from the beginning of the trial (=dropT+randT)
  - 'deathT_abs': absolute death time from the beginning of the trial (=deathT+randT)
  - 'censor': censoring (drop-out or death) indicator
  - 'event': event indicator
  - 'censor_reason': censoring reason ('drop_out','death','never_event'(eventT=inf))
  - 'followT': follow-up time (true observed time) from randT

- 'followT_abs': absolute follow-up time from the beginning of the trial (=followT+randT)

simplify   whether drop unused columns (e.g., the group variable when there is only one group). See details.

advanced_dist   use user-specified distributions for event, drop-out and death. A list containing random generation functions. See details and examples.

Details

See webpage <https://zjph602xtc.github.io/PWEXP/> for a diagram illustration of the relationship between returned variables.

The total number of subgroups will be '# treatment groups' * '# strata'. The `strata` variable will be distributed into each treatment group. For example, if group = c('trt','placebo'), strata=c('A','B','C'), then there will be 6 subgroups: trt+A, trt+B, trt+C, placebo+A, placebo+B, placebo+C. The lengths of `allocation`, `event_lambda`, `drop_rate`, `death_lambda` should be 6 as well. Note that the values will be recycled for these variables. For example, if allocation=c(1,2,3), then the proportion of 6 subgroups is actually 1:2:3:1:2:3, which means 1:1 ratio for groups, 1:2:3 ratio in each stratum.

The `event_lambda` (λ) is the hazard rate of the interested events. The density function of events is $f(t) = \lambda e^{-\lambda * t}$. Similarly, the `death_lambda` is the hazard rate of death.

The `drop_rate` is the probability of drop-out at $t = 1$, which means the hazard rate of drop-out is $-log(1 - drop_rate)$ (or say, `drop_rate`$= 1 - e^{-hazardrate}$.

When `simplify=TRUE`, these columns will NOT be included:

- group when only one group is specified
- strata when only one stratum is specified
- eventT when event_lambda=NA
- dropT when drop_rate=NA
- deathT when death_lambda=NA

advanced_dist is used to define non-exponential distributions for event, drop-out or death. It is a list containing at least one of the elements: `event_dist`, `drop_dist`, `death_dist`. Each element has random generation functions for each subgroups. For example, advanced_dist=list(event_dist=c(function1, function2), drop_dist=c(function3, function4)). Here function1, function3 are the event, drop-out generation function for the first subgroup; function2, function4 for the second. If there is a third subgroup, function1, function3 will be reused. Each data generation function (functionX) is a function with only one input argument n (sample size). If any of the event_dist, drop_dist, death_dist is missing, then we search for event_lambda, drop_rate, death_lambda to generate a exp distribution; if they are also missing, then corresponding variable will not be generated .

Value

A data frame containing the some of these columns:

ID   subject ID

group   group indicator

strata	stratum indicator
randT	randomization time (from the beginning of the trial)
eventT	event time (from randT)
eventT_abs	event time (from the beginning of the trial)
dropT	drop-out time (from randT)
dropT_abs	drop-out time (from the beginning of the trial)
deathT	death time (from randT)
deathT_abs	death time (from the beginning of the trial)
censor	censoring (drop-out or death) indicator
censor_reason	censoring reason ('drop_out','death','never_event'(followT=inf))
event	event indicator
followT	follow-up time / observed time (from randT)
followT_abs	follow-up time / observed time (from the beginning of the trial)

Note

event_lambda, drop_rate, death_lambda can be 0, which means the corresponding subgroup will have an Inf value for each variable.

Author(s)

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See Also

rpwexp, rpwexp_conditional

Examples

```
# Two groups with two strata. In the treatment group, there is a treatment
# sensitive stratum and a non-sensitive stratum. In the placebo group, all
# subjects are the same. Treatment:place=1:2. Drop rate=1% only in treatment group.
dat <- simdata(group=c('trt', 'place'), strata = c('sensitive','non-sensitive'),
               allocation = c(1,1,2,2), rand_rate = 20, total_sample = 1000,
               event_lambda = c(0.1, 0.2, 0.01, 0.01),
               drop_rate = c(0.01, 0.01, 0, 0))
# randomized subjects
table(dat$group,dat$strata)
# randomization curve
plot(sort(dat$randT), 1:1000, xlab='time', ylab='randomized subjects')
# event time in treatment group
plot(ecdf(dat$eventT[dat$group=='trt' & dat$strata=='sensitive']))
lines(ecdf(dat$eventT[dat$group=='trt' & dat$strata=='non-sensitive']), col='red')


# One group. Event follows a piecewise exponential distribution; drop-out follows
# a Weibull; death follows a exponential.
```

```
dist_trt <- function(n)rpwexp(n, rate=c(0.01, 0.05, 0.01), breakpoint = c(30,60))
dist_placebo <- function(n)rpwexp(n, rate=c(0.01, 0.005), breakpoint = c(50))
dat <- simdata(group = c('trt','placebo'), n_rand = c(rep(10,50),rep(20,10)),
               death_lambda = 0.01,
               advanced_dist = list(event_dist=c(dist_trt, dist_placebo),
                                    drop_dist=function(n)rweibull(n,3,40)))
# randomized subjects
table(dat$group)
# randomization curve
plot(sort(dat$randT), 1:700, xlab='time', ylab='randomized subjects')
# event time in both groups
plot(ecdf(dat$eventT[dat$group=='trt']), xlim=c(0,100))
lines(ecdf(dat$eventT[dat$group=='placebo']), col='red')
# drop-out time
plot(ecdf(dat$dropT), xlim=c(0,100))


# mixture cure distribution, 20% of the subject are cured and will not have events
dat <- simdata(strata=c('cure','non-cure'), allocation=c(20,80),
         event_lambda=c(0, 0.38), n_rand = rep(20,30),
         add_column = c('eventT_abs', 'censor', 'event',
                        'censor_reason', 'followT', 'followT_abs'))
```

---

sim_followup   *Estimate follow up time and number of events by simulation*

Description

sim_follwup is used to estimate follow-up time and number of events (given calander time, or number of randomized samples, or number of events).

Usage

```
sim_followup(at, type = 'calander', group="Group 1", strata='Strata 1',
            allocation=1, event_lambda=NA, drop_rate=NA, death_lambda=NA,
            n_rand=NULL, rand_rate=NULL, total_sample=NULL, extra_follow=0,
            by_group=FALSE, by_strata=FALSE, advanced_dist=NULL,
           stat=c(mean, median, sum), follow_up_endpoint=c('death', 'drop_out',
           'cut'), count_in_extra_follow=FALSE, count_insufficient_event=FALSE,
            start_date=NULL, rep=300, seed=1818)
```

Arguments

at	specify a vector of occasions. When type='calander', at is the time from fisrt randomization; when type='event', at is the number of accumulated events; when type='sample', at is the number of randomized samples.
type	specify the type of at. Must be 'calander', event or sample.
group	a character vector of the names of each group (e.g., c('treatment','control')). See [simdata](#).

strata	a character vector of the names of strata in groups (e.g., c('young','old')). See [simdata]().
allocation	the relative ratio of sample size in each subgroup (group*strata). The value will be recycled if the length is less than needed. See [simdata]().
event_lambda	the hazard rate of the primary endpoint (event). The value will be recycled if the length is less than needed. See [simdata]().
drop_rate	(optional) the drop-out rate (patients/month). Not hazard rate. The value will be recycled if the length is less than needed. See [simdata]().
death_lambda	(optional) the hazard rate of death. The value will be recycled if the length is less than needed. See [simdata]().
n_rand	(required when rand_rate=NULL) a vector of the number of randomization each month; can be non-integers. See [simdata]().
rand_rate	(required when n_rand=NULL) the randomization rate (patients/month; can be non-integer). See [simdata]().
total_sample	(required when n_rand=NULL) total scheduled sample size. See [simdata]().
extra_follow	delay the analysis time by extra time (extra_follow) after the time specified by at. See details.
by_group	logical; if TRUE, also return results by each group.
by_strata	logical; if TRUE, also return results by each stratum.
advanced_dist	use user-specified distributions for event, drop-out and death. A list containing random generation functions. See details and examples in [simdata]().
stat	a vector of functions to summarize the follow-up time. See example.
follow_up_endpoint	
	Which endpoints can be regarded as the end of follow-up. Choose from 'death', 'drop_out', 'cut' (censored at the end of the trial) or 'event'.'
count_in_extra_follow	
	logical; whether to count subjects who are randomized after the time spcified by at but before the time specified by at + extra_follow.
count_insufficient_event	
	logical; only affects the result when type='event'. If TRUE, for samples that cannot achieve required number of events, the last follow-up time is the analysis time. If FALSE, these samples will be dropped.
start_date	the start date of the first randomization; in the format: "2000-01-30"
rep	number simulated iterations.
seed	a random seed.

Details

See the help document of [simdata]() for most arguments details.

When type='calander', the function estimates the follow-up time and number of events at time at plus extra_follow; when type='event', the function estimates these at the time when total number of events is at plus time extra_follow; when type='sample', the function estimates these at the time when total number of randomized subjects is at plus time extra_follow.

The stat specifies a vector of user defined functions. Each of them must take a vector of individual follow-up time as input and return a single summary value. See example.

Value

A data frame containing the some of these columns:

ID	subject ID
group	group indicator
strata	stratum indicator
randT	randomization time (from the beginning of the trial)
eventT	event time (from randT)
eventT_abs	event time (from the beginning of the trial)
dropT	drop-out time (from randT)
dropT_abs	drop-out time (from the beginning of the trial)
deathT	death time (from randT)
deathT_abs	death time (from the beginning of the trial)
censor	censoring (drop-out or death) indicator
censor_reason	censoring reason ('drop_out','death','never_event'(followT=inf))
event	event indicator
followT	follow-up time / observed time (from randT)
followT_abs	follow-up time / observed time (from the beginning of the trial)

Note

event_lambda, drop_rate, death_lambda can be 0, which means the corresponding subgroup will have an Inf value for each variable.

Author(s)

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See Also

[simdata](#)

Examples

```
# Two groups. Treatment:place=1:2. Drop rate=3%/month. Hazard ratio=0.7.

# define the piecewiese exponential event generation function
myevent_dist_trt <- function(n)rpwexp(n, rate=c(0.1, 0.01, 0.2)*0.7, breakpoint=c(5,14))
myevent_dist_con <- function(n)rpwexp(n, rate=c(0.1, 0.01, 0.2), breakpoint=c(5,14))

# user defined summary function, the proportion of subjects that follow more than 12 month
prop_12 <- function(x)mean(x >= 12)

# estimate the event curve or timeline:
# (here rep=60 is for demo purpose only, please increase this value in practice!)
event_curve <- sim_followup(at=seq(20,90,10), type = 'calendar', group = c('trt','con'),
```

```
              rand_rate = 20, total_sample = 1000, drop_rate = 0.03, allocation = 1:2,
              advanced_dist = list(event_dist=c(myevent_dist_trt, myevent_dist_con)),
             by_group = TRUE, stat = c(median, mean, prop_12), start_date = "2020-01-01",
              rep=60)
time_curve <- sim_followup(at=seq(200,600,100), type = 'event', group = c('trt','con'),
              rand_rate = 20, total_sample = 1000, drop_rate = 0.03, allocation = 1:2,
              advanced_dist = list(event_dist=c(myevent_dist_trt, myevent_dist_con)),
              stat = c(median, mean, prop_12), start_date = "2020-01-01", rep=60)
# plot event curve or timeline
plot(event_curve$T_all$analysis_time_c, event_curve$T_all$event, xlab='Time',
    ylab='Number of events', type='b')
plot(time_curve$T_all$event, time_curve$T_all$analysis_time_c, xlab='Number of
    events', ylab='Time', type='b')
```

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