# Package 'stochcorr'

# April 2, 2025

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Description Performs simulation and inference of diffusion processes on circle. Stochastic correla
tion models based on circular diffusion models are provided. For details see Majum-

dar, S. and Laha, A.K. (2024) ``Diffusion on the circle and a stochastic correlation model" <doi:10.48550/arXiv.2412.06343>.

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Author Sourav Majumdar [aut, cre] (<a href="https://orcid.org/0000-0002-7487-6449">https://orcid.org/0000-0002-7487-6449</a>)
Maintainer Sourav Majumdar <a href="mailto:souravm@iitk.ac.in">souravm@iitk.ac.in</a>>
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circ.bootstrap Bootstrap for circdiff

## **Description**

stoch.bootstrap returns the Bootstrap confidence interval for estimated parameters from circdiff.

## Usage

```
circ.bootstrap(est, theta, boot_iter=500, p=0.05, seed = NULL)
```

# **Arguments**

est object of class cbm or vmp

theta data of the discretely observed diffusion

boot\_iter number of bootstrap iteration (Default is 500)

p 1-p% confidence interval (Default is 0.05)

seed (optional) seed value

#### **Details**

This function returns a (1-p)% confidence interval for estimated parameters from circdiff using parametric bootstrap. See section 4 of Majumdar and Laha (2024) doi:10.48550/arXiv.2412.06343.

## Value

Returns a matrix of the bootstrap (1-p)% confidence interval for the parameters. The first row is the lower bound and the second row is the upper bound.

### See Also

circdiff()

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#### **Examples**

```
library(stochcorr)
data(wind)
if(requireNamespace("ggplot2")){
library(ggplot2)
ggplot2::ggplot(wind, aes(x = Date, y = Dir)) +
  geom_line() +
  labs(title = "Sotavento Wind Farm",
      x = "Date",
       y = "Wind Direction") +
  scale_x_datetime(date_labels = "%d-%b", date_breaks = "2 day") +
  theme_test() +
  theme(
   text = element_text(size = 15),
   axis.text.x = element_text(angle = 90, hjust = 1)
}
a<-circdiff(wind$Dir,10/1440,"vmp")
b<-circdiff(wind$Dir,10/1440,"cbm")
estimates_vmp<-circ.bootstrap(a,wind$Dir, seed = 100)</pre>
estimates_vmp
estimates_cbm<-circ.bootstrap(b,wind$Dir, seed = 100)</pre>
estimates_cbm
```

circdiff

Estimation of circular diffusion models

#### **Description**

circdiff returns the estimates of parameters of a discretely observed von-Mises process or Circular Brownian motion

## Usage

```
circdiff(theta, dt, corr_process, iter=2000, lambda=0, lambda_1=0, lambda_2=0)
```

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#### **Arguments**

theta data of the discretely observed diffusion

dt time step  $\Delta t$ 

corr\_process vmp for von-Mises process; cbm for circular brownian motion

iter number of iterations (Default is 2000)

lambda regularization parameter for cbm (Default is 0)
lambda\_1 regularization parameter for vmp (Default is 0)
lambda\_2 regularization parameter for vmp (Default is 0)

#### **Details**

Let  $\theta_0, \theta_{\Delta t}, \theta_{2\Delta t}, \dots, \theta_{n\Delta t}$  be a discretely observed circular diffusion at time step  $\Delta t$ . The circular diffusion could either be von-Mises process,

$$d\theta_t = -\lambda \sin(\theta_t - \mu)dt + \sigma dW_t$$

or the circular brownian motion,

$$d\theta_t = \sigma dW_t$$

under periodic boundary condition. The function returns the MLE of  $\lambda$ ,  $\sigma$ ,  $\mu$  for von-Mises process or  $\sigma$  for circular brownian motion.

We provide an option to perform penalised MLE using an iterative optimization procedure as following, we maximise for von Mises process, where n is the number of observations,

$$\operatorname{Log-lik} - n\lambda_1 \sum (1 - \cos(\theta_{i+1} - \theta_i)) - \lambda_2 \frac{2\lambda}{\sigma^2}$$

For Circular Brownian motion we maximise,

$$\operatorname{Log-lik} - n\lambda \sum (1 - \cos(\theta_{i+1} - \theta_i))$$

See section 3 of Majumdar and Laha (2024) doi:10.48550/arXiv.2412.06343.

## Value

A list containing the estimates of the model if corr\_process=vmp then it returns

- dt time step  $\Delta t$
- lambda\_vm the drift parameter of the von Mises process
- sigma\_vm the volatility parameter of the von Mises process
- mu\_vm the mean direction of the von Mises process
- lambda\_1, lambda\_2 value of the regularization parameters used for estimation

else if corr\_process=cbm then it returns

- dt time step  $\Delta t$
- sigma\_cbm the volatility parameter of the circular Brownian motion
- lambda value of the regularization parameter used for estimation

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#### See Also

```
circ.bootstrap()
```

## **Examples**

```
library(stochcorr)
data(wind)
if(requireNamespace("ggplot2")){
library(ggplot2)
ggplot2::ggplot(wind, aes(x = Date, y = Dir)) +
  geom_line() +
  labs(title = "Sotavento Wind Farm",
      x = "Date",
       y = "Wind Direction") +
  scale_x_datetime(date_labels = "%d-%b", date_breaks = "2 day") +
  theme_test() +
  theme(
   text = element_text(size = 15),
   axis.text.x = element_text(angle = 90, hjust = 1)
 }
a<-circdiff(wind$Dir,10/1440,"vmp")
b<-circdiff(wind$Dir,10/1440,"cbm")
```

dcbm

Probability transition density function for Circular Brownian Motion

# Description

dcbm evaluates the transition density for Circular Brownian Motion

# Usage

```
dcbm(theta, t, theta_0, sigma)
```

# Arguments

```
theta vector of data t time step \Delta t theta_0 initial value sigma
```

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## **Details**

See section 2 of Majumdar and Laha (2024) doi:10.48550/arXiv.2412.06343.

## Value

dcbm gives the transition density function of the circular Brownian motion

dvmp

Probability transition density function for von Mises process

# Description

dvmp evaluates the transition density for von Mises process

## Usage

```
dvmp(theta, t, theta_0, lambda, sigma, mu)
```

# Arguments

theta	vector of data
t	time step $\Delta t$
theta_0	initial value
lambda	lambda
sigma	sigma
mu	mu

## **Details**

See section 2 of Majumdar and Laha (2024) doi:10.48550/arXiv.2412.06343.

## Value

dvmp gives the transition density function of the von Mises process

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ftse2020

2020 USD/GBP and FTSE250 data

## **Description**

End of the day closing price for USD/GBP and FTSE250 in the year 2020.

# Usage

```
data("ftse2020")
```

#### **Format**

A data frame with 224 rows and 3 columns:

USD/GBP EOD USD/GBP rate FTSE250 EOD FTSE250 Date Date

#### Source

Yahoo Finance

nikkei2020

2020 USD/JPY and Nikkei data

## **Description**

End of the day closing price for USD/JPY and Nikkei in the year 2020.

#### Usage

```
data("nikkei2020")
```

#### **Format**

A data frame with 213 rows and 3 columns:

USD/JPY EOD USD/JPY rate Nikkei EOD Nikkei Date Date

#### Source

Yahoo Finance

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nse2020

2020 USD/INR and NIFTY data

# Description

End of the day closing price for USD/INR and NIFTY in the year 2020.

## Usage

```
data("nse2020")
```

#### **Format**

A data frame with 250 rows and 3 columns:

USD/INR EOD USD/INR rate

Nifty EOD Nifty

Date Date

#### **Source**

Yahoo Finance

rtraj.cbm

Simulate circular Brownian motion

# Description

rtraj.cbm returns a simulated path of a circular Brownian motion for given parameters

## Usage

```
rtraj.cbm(n, theta_0, dt, sigma, burnin=1000)
```

## **Arguments**

n number of steps in the simulated path

theta\_0 initial point dt Time step

sigma volatility parameter

burnin number of initial samples to be rejected (Default is 1000)

rtraj.vmp 9

## **Details**

Let  $\theta_t$  evolve according to a circular Brownian motion given by,

$$d\theta_t = \sigma dW_t$$

We simulate  $\theta_t$  by simulating from its transition density.

## Value

A vector of length n of the simulated path from circular Brownian motion

rtraj.vmp

Simulate von Mises process

## **Description**

rtraj.vmp returns a simulated path of a von Mises process for given parameters

#### Usage

```
rtraj.vmp(n, theta_0, dt, mu, lambda, sigma)
```

### **Arguments**

n number of steps in the simulated path

theta\_0 initial point dt Time step

mu mean parameter
lambda drift parameter
sigma volatility parameter

## **Details**

Let  $\theta_t$  evolve according to a von Mises process given by,

$$d\theta_t = -\lambda \sin(\theta_t - \mu)dt + \sigma dW_t$$

We simulate  $\theta_t$  by the Euler-Maruyama discretization of the above SDE.

## Value

A vector of length n of the simulated path from von Mises process

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stoch.bootstrap	Bootstrap for stochcorr	
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## Description

stoch.bootstrap returns the Bootstrap confidence interval for estimated rho from stochcorr.

# Usage

```
stoch.bootstrap(est, S_1, S_2, boot_iter=500, p=0.05, seed = NULL)
```

## **Arguments**

est	object of class cbm or vmp
S_1	historical price of the first asset
S_2	historical price of the second asset
boot_iter	number of bootstrap iteration (Default is 500)
p	1-p% confidence interval (Default is 0.05)
seed	(optional) seed value

#### **Details**

This function returns a p% confidence interval for estimated rho from stochcorr using parametric bootstrap. See section 4 of Majumdar and Laha (2024) doi:10.48550/arXiv.2412.06343.

#### Value

Returns a matrix for the bootstrap (1-p)% confidence interval for rho. The first row of the matrix is the lower bound and the second row is the upper bound.

#### See Also

```
stochcorr()
```

# **Examples**

```
library(stochcorr)

data("nse2020")

## using von Mises process as the correlation process

a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "vmp")
b <- stoch.bootstrap(a, nse2020$`USD/INR`, nse2020$Nifty, seed = 100)

rho_data <- as.data.frame(cbind(a$rho, nse2020$Date))
rho_data[, 2] <- as.Date(rho_data[, 2], origin = "1970-01-01")</pre>
```

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```
colnames(rho_data) <- c("Correlation", "Time")</pre>
if(requireNamespace("ggplot2")){
library(ggplot2)
ggplot2::ggplot(rho_data, aes(x = Time, y = Correlation)) +
 theme_test() +
 theme(
   text = element_text(size = 15),
   axis.text.x = element_text(angle = 90, hjust = 1)
 ) +
 geom_line() +
 geom_ribbon(aes(ymin = b[1, ], ymax = b[2, ]), fill = "blue", alpha = 0.15) +
 scale_y\_continuous(breaks = round(seq(-1, 1, by = 0.05), 1)) +
 scale_x_date(breaks = "1 month", date_labels = "%B %Y")
 }
## using Circular Brownian Motions as the correlation process
a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "cbm")
b <- stoch.bootstrap(a, nse2020$`USD/INR`, nse2020$Nifty, seed = 100)
rho_data <- as.data.frame(cbind(a$rho, nse2020$Date))</pre>
rho_data[, 2] <- as.Date(rho_data[, 2], origin = "1970-01-01")</pre>
colnames(rho_data) <- c("Correlation", "Time")</pre>
if(requireNamespace("ggplot2")){
library(ggplot2)
ggplot2::ggplot(rho_data, aes(x = Time, y = Correlation)) +
 theme_test() +
 theme(
   text = element_text(size = 15),
   axis.text.x = element_text(angle = 90, hjust = 1)
 ) +
 geom_line() +
 geom\_ribbon(aes(ymin = b[1, ], ymax = b[2, ]), fill = "blue", alpha = 0.15) +
 scale_y\_continuous(breaks = round(seq(-1, 1, by = 0.05), 1)) +
 scale_x_date(breaks = "1 month", date_labels = "%B %Y")}
```

stochcorr

Estimate a stochastic correlation model

### **Description**

stochcorr returns the estimates of the instantaneous correlation and other model parameters.

## Usage

```
stochcorr(S_1, S_2, dt, corr_process, iter=2000, lambda=4, lambda_1=10, lambda_2=0)
```

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#### **Arguments**

S_1	Historical price of the first asset
S_2	Historical price of the second asset
dt	Time step
corr_process	specify the correlation process, vmp for von Mises process or cbm for Circular Brownian Motion

iter Number of iteration (Default is 2000)

lambda regularization parameter for circular Brownian motion (Default is 4)

lambda\_1 (Default is 10)
lambda\_2 0 (Default)

#### **Details**

Let  $S^1_t$  and  $S^2_t$  be two discretely observed geometric Brownian motions observed at a time step of dt.

$$dS_t^1 = \mu_1 S_t^1 dt + \sigma_1 dW_t^1 dS_t^2 = \mu_2 S_t^2 dt + \sigma_2 (\rho_t dW_t^1 + \sqrt{1 - \rho_t^2} dW_t^2)$$

where  $\rho_t = \cos \theta_t$ , with  $\theta_t$  being specified by the von Mises Process  $(d\theta_t = \lambda \sin(\theta_t - \mu) + \sigma dW_t^3)$  or the Circular Brownian Motion,

$$d\theta = \sigma dW_t^3$$

with periodic boundary conditions. Here  $W_t^1, W_t^2, W_t^3$  are mutually independent Brownian Motions

We estimate the model by maximising penalized MLE, using an iterative optimization procedure. In case of the von Mises process as the correlation process we maximise,

Log-lik 
$$-\lambda_1 \sum_{i=1}^{\infty} (\rho_{i+1} - \rho_i)^2 - \lambda_2 \frac{2\lambda}{\sigma^2}$$

For Circular Brownian motion as the correlation process we maximise,

$$\text{Log-lik} - \lambda \sum (\rho_{i+1} - \rho_i)^2$$

See section 4 of Majumdar and Laha (2024) doi:10.48550/arXiv.2412.06343.

## Value

A list containing the estimates of the model including the asset price parameters, instantaneous correlations and estimates of the correlation process

- · rho Estimated instantaneous correlations
- mu\_1 Drift of the first asset
- mu\_2 Drift of the second asset
- sigma\_1 Volatility of the first asset
- sigma\_2 Volatility of the second asset

if corr\_process=vmp then it additionally returns

stochcorr.sim 13

- lambda\_vm the drift parameter of the von Mises process
- sigma\_vm the volatility parameter of the von Mises process
- mu\_vm the mean direction of the von Mises process
- lambda\_1, lambda\_2 value of the regularization parameters used for estimation

else if corr\_process=cbm then it returns

- sigma\_cbm the volatility parameter of the circular Brownian motion
- lambda value of the regularization parameter used for estimation

#### See Also

```
stoch.bootstrap()
```

### **Examples**

```
data("nse2020")
## using von Mises process as the correlation process
a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "vmp")
## using Circular Brownian Motions as the correlation process
a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "cbm")</pre>
```

stochcorr.sim

Simulate stochastic correlation model

# Description

stochcorr.sim returns the paths of stock price under a stochastic correlation model

#### Usage

```
stochcorr.sim(m=500, n, dt, S1_0, S2_0, mu1, sigma1, mu2, sigma2,
mu, lambda, sigma, corr_process)
```

## Arguments

m	number of paths (Default is 500)
n	number of steps in each simulated path
dt	time step
S1_0	initial price of the first asset
S2_0	initial price of the second asset
mu1	drift of the first asset

s&p2020

sigma1	volatility of the first asset
mu2	drift of the second asset
sigma2	volatility of the second asset
mu	mean direction of the correlation process (if corr_process=vmp)
lambda	drift of the correlation process (if corr_process=vmp)
sigma	$volatility\ of\ the\ correlation\ process\ (if\ corr\_process=vmp\ or\ corr\_process=cbm)$
corr_process	specify the correlation process, vmp for von Mises process or cbm for Circular

### **Details**

This function returns the simulated paths of two stock prices following a stochastic correlation model. See stochcorr() details of the stochastic correlation model

#### Value

Returns a list with prices of two assets S1 and S2 under the stochastic correlation model

**Brownian Motion** 

# **Examples**

```
library(stochcorr)
# Generate 500 paths of two geometric Brownian motions, S1 and S2, of length 100 each
# following the von Mises process with mu=pi/2, lambda=1 and sigma =1

a<-stochcorr.sim(m=500,100,0.01,100,100,0.05,0.05,0.06,0.1,pi/2,1,1,"vmp")
t<-seq(0,100*0.01-0.01,0.01)

# Plot the first realization of S1 and S2

plot(t,a$S1[1,], ylim=c(min(a$S1[1,],a$S2[1,]),max(a$S1[1,],a$S2[1,])),type="1")
lines(t,a$S2[1,], col="red",type="1")
legend(0.01,max(a$S1[1,],a$S2[1,]), legend = c("S1","S2"), col = c("black", "red"), lty=1)</pre>
```

s&p2020

2020 EUR/USD and S&P500 data

### **Description**

End of the day closing price for EUR/USD and S&P500 in the year 2020.

## Usage

```
data("s&p2020")
```

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## **Format**

A data frame with 224 rows and 3 columns:

EUR/USD EOD EUR/USD rate S&P500 EOD S&P500 Date Date

## Source

Yahoo Finance

wind

Wind direction data

# Description

Wind direction data from Sotavento Wind farm from 1 November 2024 to 30 November 2024 at a 10 minute frequency.

# Usage

```
data("wind")
```

### **Format**

A data frame with 4320 rows and 2 columns:

Dir Wind Direction data Date Date

#### Source

https://www.sotaventogalicia.com/en/technical-area/real-time-data/historical/

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