# Package 'HydroPortailStats'

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```
Type Package
Title 'HydroPortail' Statistical Functions
Version 1.1.0
Description
               Statistical functions used in the French 'HydroPortail' <a href="https://hydro.eaufrance.fr/">https://hydro.eaufrance.fr/</a>.
               This includes functions to estimate distributions, quantile curves and uncertain-
               ties, along with various other utilities.
               Technical details are available (in French) in Renard (2016) <a href="https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.com/https://example.
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# Description

A named list containing information (parameters, contraints, notes, warnings, etc.) for all available univariate distributions.

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### Usage

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#### **Format**

A named list where each element is itself a list containing:

parName parameters short names

parLongName parameters long names

parSymbol parameters typical symbols

constraints constraints on parameters

**url** link to more information

note notes

**warning** warnings: read carefully since this highlights in particular differences with "standard" parameterizations found in e.g. Wikipedia or R.

Generate

Random numbers generator

### **Description**

Generate random realizations from a distribution

#### Usage

```
Generate(dist, par, n = 1)
```

# Arguments

dist character, distribution name

par numeric vector, parameter vector

n integer, number of values to generate

#### Value

The generated values as a numeric vector.

```
Generate('Normal',c(0,1),10)
Generate('GEV',c(100,25,-0.2),10)
Generate('GEV',c(100,25,0.2),10)
Generate('Poisson',0.75,10)
```

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GenerateWithinBounds Constrained random numbers generator

# Description

Generate random realizations from a distribution, constraining these realizations to stay within bounds.

### Usage

```
GenerateWithinBounds(dist, par, n = 1, lowerBound = -Inf, higherBound = Inf)
```

### **Arguments**

dist character, distribution name

par numeric vector, parameter vector

n integer, number of values to generate

lowerBound Numeric, lower bound

higherBound Numeric, higher bound, should be strictly larger than the lower bound

## Value

The generated values as a numeric vector.

### **Examples**

```
set.seed(123456)\\ y0=GenerateWithinBounds(dist='GEV',par=c(0,1,-0.2),n=1000)\\ y1=GenerateWithinBounds(dist='GEV',par=c(0,1,-0.2),n=1000,lowerBound=0,higherBound=5)\\ plot(y0);points(y1,col='red')
```

GetCdf

Cumulative Distribution Function (cdf)

## **Description**

Evaluates the cdf of a distribution

## Usage

```
GetCdf(y, dist, par)
```

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# Arguments

y numeric, value at which the cdf is evaluated

dist character, distribution name

par numeric vector, parameter vector

#### Value

The cdf as a numeric.

# **Examples**

```
GetCdf(0,'Normal',c(0,1))

GetCdf(200,'GEV',c(100,25,-0.2))

GetCdf(200,'GEV',c(100,25,0.2))

GetCdf(3,'Poisson',0.75)
```

GetEmpFreq

Empirical nonexceedance frequency

# **Description**

Computes the empirical nonexceedance frequency of the ith sorted value amongst n

# Usage

```
GetEmpFreq(i, n, formula = "Hazen")
```

#### **Arguments**

i integer or integer vector, observation rank(s)

n integer, number of observations

formula character, formula, available: 'Hazen', 'Standard', 'MinusOne', 'Weibull', 'Be-

nard', 'Cunnane', 'Beard', 'Blom', 'Gringorten', 'Landwehr', 'Tukey'.

### Value

The nonexceedance frequency.

```
GetEmpFreq(i=1:10,n=10)
GetEmpFreq(i=1:10,n=10,formula='Standard')
GetEmpFreq(i=1:10,n=10,formula='MinusOne')
GetEmpFreq(i=1:10,n=10,formula='Cunnane')
```

6 GetEstimate\_BAY

GetEstimate\_BAY

Bayesian estimation of a distribution

# Description

Returns MCMC samples from the posterior distribution.

# Usage

```
GetEstimate_BAY(
   y,
   dist,
   prior,
   par0,
   mult = 0.1,
   eps = 0.1,
   batch.length = 100,
   batch.n = 100,
   moverate.min = 0.1,
   moverate.max = 0.5,
   mult.down = 0.9,
   mult.up = 1.1
)
```

# Arguments

У	numeric vector, data
dist	character, distribution name
prior	list of lists, prior distributions. For each parameter to be estimated, the prior is a list of the form pr=list(dist=, par=). See example below.
par0	numeric vector, initial parameter guess. You may use GetEstimate_ROUGH().
mult	numeric, initial jump standard deviations are set to mult * abs(par0)
eps	numeric, where par0 is zero, initial jump standard deviations are set to eps (to avoid jumps of size zero)
batch.length	integer, MCMC parameter: length of each non-adaptive batch
batch.n	integer, MCMC parameter: number of batches (= adaptation period). Total number of simulations is nsim=batch.n*batch.length
moverate.min	numeric in (0;1), MCMC parameter: lower bound for the desired move rate interval
moverate.max	numeric in $(0;1)$ , MCMC parameter: upper bound for the desired move rate interval
mult.down	numeric in (0;1), MCMC parameter: multiplication factor used to decrease jump size when move rate is too low.
mult.up	numeric (>1, avoid 1/mult.down), MCMC parameter: multiplication factor used to increase jump size when move rate is too high.

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#### Value

A list with the following components:

```
x numeric matrix nsim*length(par0), MCMC simulations
fx numeric vector, corresponding values f(x)
```

#### **Examples**

```
 y = c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4) \\ prior1 = list(dist='FlatPrior',par=NULL) \\ prior2 = list(dist='LogNormal',par=c(1,1)) \\ prior3 = list(dist='Normal',par=c(0,0.25)) \\ prior=list(prior1,prior2,prior3) \\ par0 = GetEstimate_ROUGH(y,'GEV') \\ par \\ mcmc = GetEstimate_BAY(y,'GEV',prior,par0,batch.length=50,batch.n=50) \\ graphicalpar=par(mfrow=c(2,3)) \\ plot(mcmc$x[,1],type='l'); plot(mcmc$x[,2],type='l'); plot(mcmc$x[,3],type='l') \\ hist(mcmc$x[,1]); hist(mcmc$x[,2]); hist(mcmc$x[,3]) \\ par(graphicalpar) \\ \end{cases}
```

GetEstimate\_HBay

Bayesian estimation using historical data

### Description

Bayesian estimation of a GEV or Gumbel distribution based on a mixed sample containing point (i.e. perfectly known) or interval (i.e. known to be within bounds) data. Systematic errors induced by rating curve errors can also be accounted for. Returns MCMC samples from the posterior distribution.

#### Usage

```
GetEstimate_HBay(
  у,
  dist,
  prior,
  SystErrorIndex = rep(0, NROW(y)),
  SystErrorPrior = list(),
 par0 = GetEstimate_ROUGH(0.5 * (y[, 1] + y[, 2])[is.finite(y[, 1] + y[, 2])], dist) *par,
  SystError0 = rep(1, length(SystErrorPrior)),
 mult = 0.1,
  eps = 0.1,
  batch.length = 100,
  batch.n = 100,
 moverate.min = 0.1,
 moverate.max = 0.5,
 mult.down = 0.9,
  mult.up = 1.1
)
```

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#### **Arguments**

numeric 2-column matrix, data. The first column gives the lower bound, the sec-У ond column gives the upper bound. Where y[i,1]==y[i,2], the value is assumed perfectly known (up to systematic errors, see below). Where y[i,1]<y[i,2], the value is assumed to be in the interval [y[i,1];y[i,2]] -Inf and +Inf are allowed for data being only right- or left-censored (i.e. values known to be smaller than or larger than some threshold). character, distribution name. Only distributions 'GEV' and 'Gumbel' are supdist ported. prior list of lists, prior distributions. For each parameter to be estimated, the prior is a list of the form pr=list(dist=..., par=...). See example below. SystErrorIndex integer vector, length NROW(y). Index of systematic errors. Rows where SystErrorIndex==k are all affected by the same multiplicative error gamma\_k, typically induced by the kth rating curve. SystErrorIndex==0 means no systematic error. Should only contain integer values between 0 and N\_{systematic errors}. list of lists, prior distribution for each systematic error. For instance for a sys-SystErrorPrior tematic error in the range +/- 20%, you may use a Uniform between 0.8 and 1.2, or a triangular distribution with the same bounds and peak at 1. numeric vector, initial parameter guess. par0 SystError0 numeric vector, initial guess for systematic errors. Typically a vector of 1. mult numeric, initial jump standard deviations are set to mult \* abs(par0) numeric, where par0 is zero, initial jump standard deviations are set to eps (to eps avoid jumps of size zero) batch.length integer, MCMC parameter: length of each non-adaptive batch integer, MCMC parameter: number of batches (= adaptation period). Total numbatch.n ber of simulations is nsim=batch.n\*batch.length numeric in (0;1), MCMC parameter: lower bound for the desired move rate moverate.min interval numeric in (0;1), MCMC parameter: upper bound for the desired move rate moverate.max interval mult.down numeric in (0;1), MCMC parameter: multiplication factor used to decrease jump size when move rate is too low. mult.up numeric (>1, avoid 1/mult.down), MCMC parameter: multiplication factor used to increase jump size when move rate is too high.

#### Value

A list with the following components:

x numeric matrix nsim \* (length(par0)+length(SystError0)), MCMC simulations fx numeric vector, corresponding values f(x)

#### **Examples**

```
set.seed(98765)
n=50;n_censored=30
y0=Generate('GEV',c(100,50,-0.2),n)
y=cbind(y0,y0)
# Mimics censoring between 0 and 300 for first n_censored years
y[1:n_censored,1][y0[1:n_censored]<300]=0
y[1:n_censored, 2][y0[1:n_censored]<300]=300</pre>
plot(y[,1]); points(y[,2])
# Systematic errors
SystErrorIndex=c(rep(1,n_censored),rep(2,n-n_censored))
SystErrorPrior=list(list(dist="Triangle",par=c(1,0.7,1.3)),
                    list(dist="Triangle",par=c(1,0.95,1.05)))
# Priors on GEV parameters
prior=list(list(dist="FlatPrior",par=NULL),
           list(dist="FlatPrior",par=NULL),
           list(dist="Normal",par=c(0,0.25)))
# Go!
mcmc=GetEstimate_HBay(y=y,dist='GEV',prior=prior,
                      SystErrorIndex=SystErrorIndex,
                      SystErrorPrior=SystErrorPrior,
                      # The values below aim at making this example fast to run.
                      # In practice, it is recommended to use the default values
                      # (batch.length=100,batch.n=100) or larger.
                      batch.length=25,batch.n=20)
graphicalpar=par(mfrow=c(2,3))
for(i in 1:5){hist(mcmc$x[,i])}
par(graphicalpar)
```

GetEstimate\_HYDR02

Hydro2 estimate of a distribution

## **Description**

Returns an estimate of a distribution as it was computed in the old HYDRO2 software. Only available for distributions 'Normal', 'LogNormal', and 'Gumbel'.

## Usage

```
GetEstimate_HYDRO2(y, dist)
```

# Arguments

```
y numeric vector, data
dist character, distribution name
```

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#### Value

A list with the following components:

par numeric vector, estimated parameter vector.

obj numeric, objective fonction (NA for this estimate)

ok logical, did computation succeed?

err integer, error code (0 if ok)

message error message

#### **Examples**

```
y=c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4)
GetEstimate_HYDRO2(y,'Normal')
GetEstimate_HYDRO2(y,'LogNormal')
GetEstimate_HYDRO2(y,'Gumbel')
GetEstimate_HYDRO2(y,'GEV')
GetEstimate_HYDRO2(y,'Poisson')
```

GetEstimate\_LMOM

L-Moment estimate of a distribution

# Description

Returns an estimate of a distribution using the method of L-moments. Note that for some distributions, this is not strictly speaking the L-moment estimate: For LogNormal and LogPearsonIII, the L-moment estimate of log(data) is used.

#### Usage

```
GetEstimate_LMOM(y, dist)
```

# **Arguments**

y numeric vector, data

dist character, distribution name

#### Value

A list with the following components:

par numeric vector, estimated parameter vector.

obj numeric, objective fonction (NA for this estimate)

ok logical, did computation succeed?

err integer, error code (0 if ok)

message error message

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#### **Examples**

```
y=c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4)
GetEstimate_LMOM(y,'Normal')
GetEstimate_LMOM(y,'LogNormal')
GetEstimate_LMOM(y,'Gumbel')
GetEstimate_LMOM(y,'GEV')
GetEstimate_LMOM(y,'Poisson')
```

GetEstimate\_ML

Maximum-likelihood estimate of a distribution

### **Description**

Returns an estimate of a distribution using the method of maximum likelihood.

#### Usage

```
GetEstimate_ML(
   y,
   dist,
   par0 = NULL,
   method = optim_method_def,
   lower = -Inf,
   upper = Inf
)
```

#### **Arguments**

y numeric vector, data
dist character, distribution name
par0 numeric vector, initial parameter guess. You may use GetEstimate\_ROUGH().
method character, method used to maximize likelihood, see ?optim
lower numeric vector, lower bounds, see ?optim
upper numeric vector, upper bounds, see ?optim

#### Value

A list with the following components:

par numeric vector, estimated parameter vector.

obj numeric, objective fonction (maximum log-likelihood)

ok logical, did computation succeed?

err integer, error code (0 if ok)

message error message

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# **Examples**

```
\label{eq:condition} $$ y = c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4)$$ GetEstimate_ML(y,'Normal')$$ GetEstimate_ML(y,'LogNormal')$$ GetEstimate_ML(y,'Gumbel')$$ GetEstimate_ML(y,'Gumbel',par0=GetEstimate_ROUGH(y,'Gumbel')$$ par)$$ GetEstimate_ML(y,'GEV',par0=GetEstimate_ROUGH(y,'GEV')$$ par)$$ GetEstimate_ML(y,'Poisson')$$
```

GetEstimate\_MOM

Moment estimate of a distribution

# **Description**

Returns an estimate of a distribution using the method of moments. Note that for some distributions, this is not strictly speaking the moment estimate. For LogPearsonIII for instance, the moment estimate of log(data) is used. Also for GPD3, the threshold is estimated as min(data).

#### Usage

```
GetEstimate_MOM(y, dist)
```

# Arguments

y numeric vector, data
dist character, distribution name

#### Value

A list with the following components:

par numeric vector, estimated parameter vector.

obj numeric, objective fonction (NA for this estimate)

ok logical, did computation succeed?

err integer, error code (0 if ok)

message error message

```
y=c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4)
GetEstimate_MOM(y,'Normal')
GetEstimate_MOM(y,'LogNormal')
GetEstimate_MOM(y,'Gumbel')
GetEstimate_MOM(y,'GEV')
GetEstimate_MOM(y,'Poisson')
```

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#### **Description**

Returns a rough first-guess estimate of a distribution. This estimate may be poor but it solely aims at being used as a starting point for more advanced estimation approaches (e.g. max-likelihood or Bayesian). It is therefore chosen as an easy-to-compute explicit formula, robust and error-proof.

#### **Usage**

```
GetEstimate_ROUGH(y, dist)
```

# Arguments

У numeric vector, data

dist character, distribution name

## Value

A list with the following components:

numeric vector, estimated parameter vector. par numeric, objective fonction (NA for this estimate)

ok logical, did computation succeed?

integer, error code (0 if ok) err

error message message

# **Examples**

obj

```
y=c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4)
GetEstimate_ROUGH(y,'Normal')
GetEstimate_ROUGH(y,'LogNormal')
GetEstimate_ROUGH(y,'Gumbel')
GetEstimate_ROUGH(y,'GEV')
GetEstimate_ROUGH(y, 'Poisson')
```

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GetParFeas

Parameter feasibility

## **Description**

Evaluates whether a parameter vector is feasible (for instance, are scale parameters >0 ?)

# Usage

```
GetParFeas(dist, par)
```

## **Arguments**

dist character, distribution name
par numeric vector, parameter vector

#### Value

A logical.

# **Examples**

```
# Feasible  \begin{tabular}{ll} $\tt GetParFeas('Normal',c(0,1))$ \\ # Not feasible because second parameter (standard deviation) is negative $\tt GetParFeas('Normal',c(0,-1))$ \\ \hline \end{tabular}
```

 ${\tt GetParName}$ 

Parameter names.

# **Description**

Returns the names of the parameters of a distribution, in French (default) or English.

### Usage

```
GetParName(dist, lang = "fr")
```

### **Arguments**

dist character, distribution name
lang character, language ('en' or 'fr')

## Value

A character vector.

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# **Examples**

```
GetParName('Normal')
GetParName('GEV')
GetParName('GEV',lang='en')
```

GetParNumber

Number of parameters.

# Description

Returns the number of parameters of a distribution.

### Usage

```
GetParNumber(dist)
```

### **Arguments**

dist

character, distribution name

### Value

An integer.

# **Examples**

```
GetParNumber('Normal')
GetParNumber('GEV')
```

GetPdf

Probability Density Function (pdf)

# Description

Evaluates the pdf of a distribution

#### Usage

```
GetPdf(y, dist, par, log = FALSE)
```

### **Arguments**

y numeric, value at which the pdf is evaluated

dist character, distribution name

par numeric vector, parameter vector

log logical, returns log-pdf if TRUE

GetQfromT

### Value

The pdf or the log-pdf as a numeric.

# **Examples**

```
GetPdf(0,'Normal',c(0,1))
GetPdf(200,'GEV',c(100,25,-0.2))
GetPdf(200,'GEV',c(100,25,0.2))
GetPdf(3,'Poisson',0.75)
```

 ${\tt GetQfromT}$ 

Get quantile from return period

# Description

Compute the T-quantile from the results of Hydro3\_Estimation()

# Usage

```
GetQfromT(RP, H3, options = options_def)
```

### **Arguments**

RP numeric, return period

H3 list, resulting from a call to Hydro3\_Estimation()

options list, see ?Hydro3\_Estimation

# Value

A list with the following components:

q numeric, quantile

IC numeric vector, uncertainty interval

```
y=stats::rnorm(50)
H3=Hydro3_Estimation(y,'Normal')
GetQfromT(100,H3)
```

GetQuantile 17

GetQuantile

Quantile Function

### **Description**

Evaluates the quantiles of a distribution

### Usage

```
GetQuantile(p, dist, par)
```

### **Arguments**

p numeric in (0;1), nonexceedance probability

dist character, distribution name

par numeric vector, parameter vector

#### Value

The p-quantile as a numeric.

#### **Examples**

```
GetQuantile(0.99, 'Normal',c(0,1))
GetQuantile(0.99, 'GEV',c(100,25,-0.2))
GetQuantile(0.99, 'GEV',c(100,25,0.2))
GetQuantile(0.99, 'Poisson',0.75)
```

GetReducedVariate

Reduced variate

# Description

Returns the 'reduced variate' that is used in some quantile plots (see e.g. quantile curve on Gumbel paper)

# Usage

```
GetReducedVariate(p, dist)
```

# Arguments

p numeric in (0;1), nonexceedance probability

dist character, distribution name

GetTfromQ

### Value

The reduced variate with nonexceedance probability p.

### **Examples**

```
GetReducedVariate(0.99,'Normal')
GetReducedVariate(0.99,'Gumbel')
GetReducedVariate(0.99,'GEV')
GetReducedVariate(0.99,'Poisson')
```

 ${\tt GetTfromQ}$ 

Get return period from value

# Description

Compute the return period associated with a value from the results of Hydro3\_Estimation()

# Usage

```
GetTfromQ(q, H3, options = options_def)
```

### **Arguments**

q numeric, value

H3 list, resulting from a call to Hydro3\_Estimation()

options list, see ?Hydro3\_Estimation

# Value

A list with the following components:

RP numeric, return period

IC numeric vector, uncertainty interval

```
y=stats::rnorm(50)
H3=Hydro3_Estimation(y,'Normal')
GetTfromQ(3,H3)
```

GetUncertainty\_ML 19

GetUncertainty_ML	Maximum-likelihood	estimation of	of uncertainty

### **Description**

Returns an estimate of the uncertainty around the maximum-likelihood estimate, in the form of a covariance matrix and some simulations from the corresponding Gaussian distribution.

### Usage

```
GetUncertainty_ML(y, dist, par, nsim = nsim_def)
```

# Arguments

у	numeric vector, data
dist	character, distribution name
par	$numeric\ vector,\ estimated\ parameter\ (using\ GetEstimate\_ML()).$
nsim	integer, number of simulated parameter replicates.

### Value

A list with the following components:

```
cov numeric matrix npar*npar, covariance matrix.

sim numeric matrix nsim*npar, simulated parameter replicates.

ok logical, did computation succeed?

err integer, error code (0 if ok)

message error message
```

```
\label{eq:condition} $$y=c(9.2,9.5,11.4,9.5,9.4,9.6,10.5,11.1,10.5,10.4)$$ estim=GetEstimate_ML(y,'Gumbel',par0=GetEstimate_ROUGH(y,'Gumbel')$par)$$ GetUncertainty_ML(y,'Gumbel',par=estim$par)
```

20 HBay\_Plot

HBay\_Plot

HBay plot

#### **Description**

Plot summarizing the results of Hydro3\_HBay()

## Usage

```
HBay_Plot(H3, curve_color = "black")
```

#### **Arguments**

```
H3 list, resulting from a call to Hydro3_HBay()
curve_color color, color used for quantile curve
```

#### Value

nothing (just creates a plot)

```
set.seed(98765)
n=50; n_censored=30
y0=Generate('GEV',c(100,50,-0.2),n)
y=cbind(y0,y0)
\# Mimics censoring between 0 and 300 for first n_censored years
y[1:n_censored,1][y0[1:n_censored]<300]=0</pre>
y[1:n_censored,2][y0[1:n_censored]<300]=300
plot(y[,1]); points(y[,2])
# Systematic errors
SystErrorIndex=c(rep(1,n_censored),rep(2,n-n_censored))
SystErrorPrior=list(list(dist="Triangle",par=c(1,0.7,1.3)),
                    list(dist="Triangle",par=c(1,0.95,1.05)))
# Priors on GEV parameters
prior=list(list(dist="FlatPrior",par=NULL),
           list(dist="FlatPrior",par=NULL),
           list(dist="Normal",par=c(0,0.25)))
# Handle MCMC options
# The values below aim at making this example fast to run.
# In practice, it is recommended to use the default values
# (batch.length=100,batch.n=100) or larger.
mcmcoptions=mcmcoptions_def
mcmcoptions$batch.length=25
mcmcoptions$batch.n=20
# Go!
H3=Hydro3_HBay(y=y,dist='GEV',prior=prior,
               SystErrorIndex=SystErrorIndex,
               SystErrorPrior=SystErrorPrior,
```

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```
mcmcoptions=mcmcoptions)
# HBay plot
HBay_Plot(H3)
```

Hydro3\_Estimation

Hydro3 estimation

#### **Description**

Main estimation function used in the HydroPortail. In short, this function estimates a distribution and the associated uncertainty, and returns all needed information to display and plot the results (parameter estimates, quantile curves, etc.)

#### Usage

```
Hydro3_Estimation(
   y,
   dist,
   Emeth = Emeth_def,
   Umeth = Umeth_def,
   options = options_def,
   mcmcoptions = mcmcoptions_def,
   prior = GetDefaultPrior(GetParNumber(dist)),
   do.KS = TRUE,
   do.MK = TRUE,
   do.Pettitt = TRUE
)
```

#### **Arguments**

y numeric vector, data.

dist character, distribution name. See dataset distInfo for a description of available

distributions. In particular, type names(distInfo) for the list of available distributions, and distInfo[['GEV']] for more information on a particular distribution

(here, GEV).

Emeth character, estimation method. Default is 'LMOM' (L-Moments), available:

'MOM' (Moments), 'ML' (Maximum Likelihood), 'BAY' (Bayesian).

Umeth character, uncertainty quantification method. Default is 'PBOOT' (Parametric

bootstrap), available: 'BOOT' (Bootstrap, not recommended), 'NONE', 'ML' (only usable when Emeth='ML' as well), and 'BAY' (the only usable method

when Emeth='BAY').

options list, options, see details below.

mcmcoptions list, MCMC options, see details below.

prior list, prior distributions, only used when Emeth='BAY'. See ?GetEstimate\_BAY

for details.

do.KS, do.MK, do.Pettitt

logical, perform KS/MK/Pettitt tests?

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#### **Details**

The argument 'options' allows controlling various properties of the analysis and results. It is a list with the following components:

- FreqFormula, character, formula for computing nonexceedance frequency, see ?GetEmpFreq.
- pgrid, numeric vector, probabilities defining the x values where pdf f(x) and cdf F(x) are computed. These x values are quantiles from the estimated distribution with probabilities pgrid.
- Tgrid, numeric vector, return periods where quantile function q(T) is computed.
- IClevel, numeric, level of uncertainty interval.
- p2T, numeric, conversion factor between nonexceedance probability p and return period T. p=1-1/(p2T\*T). In general p2T=1 but for a peak-over-threshold approach leading to say 3 events per year on average, p2T=3.
- invertT, logical, when invertT=TRUE, LARGE return periods correspond to SMALL data values. This is typically used for low-flow statistics.
- splitZeros, logical, when splitZeros=TRUE zero and negative values are removed from the data y before estimating the distribution, and are used to estimate the probability of zeros p0. This is typically used for low-flow statistics to estimate the probability of zero streamflow.
- lang, chanracter, language ('fr' or 'en').
- · nsim, integer, number of replicated parameters representing uncertainty.

The argument 'mcmcoptions' is only used when Emeth='BAY' and is a list controlling MCMC properties:

- mult, numeric, see ?Metropolis\_OAAT\_adaptive
- eps, numeric, see ?Metropolis\_OAAT\_adaptive
- batch.length, integer, see ?Metropolis\_OAAT\_adaptive
- batch.n, integer, see ?Metropolis\_OAAT\_adaptive
- moverate.min, numeric, see ?Metropolis\_OAAT\_adaptive
- moverate.max, numeric, see ?Metropolis\_OAAT\_adaptive
- mult.down, numeric, see ?Metropolis\_OAAT\_adaptive
- mult.up, numeric, see ?Metropolis\_OAAT\_adaptive
- burn, numeric, burn-in factor, e.g. if burn=0.2 the first 20 percents of MCMC samples are discarded
- slim, integer, sliming factor, e.g. if slim=5 only one MCMC sample every 5 is kept (after burn-in)

#### Value

A list with the following components:

dist character, estimated distribution.
ok logical, did estimation succeed?
err integer, error code (0 if ok).

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empirical data frame, sorted data and empirical estimates (nonexceedance frequency, return period and reduced variate)

pcdf data frame, estimated pdf and cdf

quantile data frame, estimated quantiles and uncertainty intervals

par data frame, estimated quantiles and uncertainty intervals

ks list, result of the Kolmogorov-Smirnov test, see ?KS

MK list, result of the Mann-Kendall test, see ?MK

Pettitt list, result of the Pettitt test, see ?Pettitt

u list, parameter uncertainty in the form of a covariance matrix (\$cov) and simu-

lated parameter replicates (\$sim). Also contains error-handling flags \$ok, \$err

and \$message.

error message.

# Examples

message

```
y=stats::rnorm(50)
H3=Hydro3_Estimation(y,'Normal')
H3=Hydro3_Estimation(y,'GEV',Emeth='ML',Umeth='ML')
```

Hydro3\_HBay

Bayesian estimation using historical data

#### **Description**

Bayesian estimation of a GEV or Gumbel distribution based on a mixed sample containing point (i.e. perfectly known) or interval (i.e. known to be within bounds) data. Systematic errors induced by rating curve errors can also be accounted for. Returns an Hydro3 object

#### Usage

```
Hydro3_HBay(
   y,
   dist,
   prior = GetDefaultPrior(GetParNumber(dist)),
   SystErrorIndex = rep(0, NROW(y)),
   SystErrorPrior = list(),
   options = options_def,
   mcmcoptions = mcmcoptions_def,
   do.KS = TRUE,
   do.Pettitt = TRUE
)
```

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#### **Arguments**

y numeric 2-column matrix, data. The first column gives the lower bound, the sec-

ond column gives the upper bound. Where y[i,1]==y[i,2], the value is assumed perfectly known (up to systematic errors, see below). Where y[i,1]< y[i,2], the value is assumed to be in the interval [y[i,1];y[i,2]]-Inf and +Inf are allowed for data being only right- or left-censored (i.e. values known to be smaller than or

larger than some threshold).

dist character, distribution name. Only distributions 'GEV' and 'Gumbel' are sup-

ported.

prior list of lists, prior distributions. For each parameter to be estimated, the prior is a

list of the form pr=list(dist=..., par=...). See example below.

SystErrorIndex integer vector, length NROW(y). Index of systematic errors. Rows where Sys-

tErrorIndex==k are all affected by the same multiplicative error gamma\_k, typically induced by the kth rating curve. SystErrorIndex==0 means no systematic error. Should only contain integer values between 0 and N\_{systematic errors}.

SystErrorPrior list of lists, prior distribution for each systematic error. For instance for a sys-

tematic error in the range +/- 20%, you may use a Uniform between 0.8 and 1.2,

or a triangular distribution with the same bounds and peak at 1.

options list, options, see details below.

mcmcoptions list, MCMC options, see details below.

do.KS, do.MK, do.Pettitt

logical, perform KS/MK/Pettitt tests?

#### **Details**

The argument 'options' allows controlling various properties of the analysis and results. It is a list with the following components:

- FreqFormula, character, formula for computing nonexceedance frequency, see ?GetEmpFreq.
- pgrid, numeric vector, probabilities defining the x values where pdf f(x) and cdf F(x) are computed. These x values are quantiles from the estimated distribution with probabilities pgrid.
- Tgrid, numeric vector, return periods where quantile function q(T) is computed.
- IClevel, numeric, level of uncertainty interval.
- p2T, numeric, conversion factor between nonexceedance probability p and return period T. p=1-1/(p2T\*T). Here p2T=1 in general since GEV/Gumbel are applied to annual maxima in general.
- invertT, logical, when invertT=TRUE, LARGE return periods correspond to SMALL data values. This is typically used for low-flow statistics. Unused here.
- splitZeros, logical, when splitZeros=TRUE zero and negative values are removed from the data y before estimating the distribution, and are used to estimate the probability of zeros p0. This is typically used for low-flow statistics to estimate the probability of zero streamflow. Unused here.
- lang, chanracter, language ('fr' or 'en').

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• nsim, integer, number of replicated parameters representing uncertainty. Unused here (derives from mcmc options)

The argument 'mcmcoptions' is a list controlling MCMC properties:

- mult, numeric, see ?Metropolis\_OAAT\_adaptive
- eps, numeric, see ?Metropolis\_OAAT\_adaptive
- batch.length, integer, see ?Metropolis\_OAAT\_adaptive
- batch.n, integer, see ?Metropolis\_OAAT\_adaptive
- moverate.min, numeric, see ?Metropolis\_OAAT\_adaptive
- moverate.max, numeric, see ?Metropolis\_OAAT\_adaptive
- mult.down, numeric, see ?Metropolis\_OAAT\_adaptive
- mult.up, numeric, see ?Metropolis\_OAAT\_adaptive
- burn, numeric, burn-in factor, e.g. if burn=0.2 the first 20 percents of MCMC samples are discarded
- slim, integer, sliming factor, e.g. if slim=5 only one MCMC sample every 5 is kept (after burn-in)

#### Value

A list with the following components:

character, estimated distribution.

ok logical, did estimation succeed?

err integer, error code (0 if ok).

message error message.

empirical data frame, sorted data and empirical estimates (nonexceedance frequency, re-

turn period and reduced variate). NOTE: interval data are replaced by a value randomly sampled from a GEV constrained in this interval. See ?GenerateWith-

inBounds.

pcdf data frame, estimated pdf and cdf

quantile data frame, estimated quantiles and uncertainty intervals data frame, estimated parameters and uncertainty intervals

KS list, result of the Kolmogorov-Smirnov test, see ?KS. NOTE: interval data are

replaced by a value randomly sampled from a GEV constrained in this interval.

See ?HBay\_simGEV.

MK list, result of the Mann-Kendall test, see ?MK. Same note as KS test.

Pettitt list, result of the Pettitt test, see ?Pettitt. Same note as KS test.

u list, parameter uncertainty in the form of a covariance matrix (\$cov) and simu-

lated parameter replicates (\$sim). Also contains error-handling flags \$ok, \$err

and \$message.

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#### **Examples**

```
set.seed(98765)
n=50; n_censored=30
y0=Generate('GEV',c(100,50,-0.2),n)
y=cbind(y0,y0)
\# Mimics censoring between 0 and 300 for first n_censored years
y[1:n_censored,1][y0[1:n_censored]<300]=0</pre>
y[1:n_censored,2][y0[1:n_censored]<300]=300
plot(y[,1]); points(y[,2])
# Systematic errors
SystErrorIndex=c(rep(1,n_censored),rep(2,n-n_censored))
SystErrorPrior=list(list(dist="Triangle",par=c(1,0.7,1.3)),
                    list(dist="Triangle",par=c(1,0.95,1.05)))
# Priors on GEV parameters
prior=list(list(dist="FlatPrior",par=NULL),
           list(dist="FlatPrior",par=NULL),
           list(dist="Normal",par=c(0,0.25)))
# Handle MCMC options
# The values below aim at making this example fast to run.
# In practice, it is recommended to use the default values
# (batch.length=100,batch.n=100) or larger.
mcmcoptions=mcmcoptions_def
mcmcoptions$batch.length=25
mcmcoptions$batch.n=20
H3=Hydro3_HBay(y=y,dist='GEV',prior=prior,
               SystErrorIndex=SystErrorIndex,
               SystErrorPrior=SystErrorPrior,
               mcmcoptions=mcmcoptions)
Hydro3_Plot(H3)
```

Hydro3\_Plot

Hydro3 plot

#### **Description**

Plot summarizing the results of Hydro3\_Estimation()

#### Usage

```
Hydro3_Plot(
    H3,
    useU = FALSE,
    lwd = 2,
    cex.lab = 2,
    cex.axis = 1.3,
    pch = 19,
    col = "red"
)
```

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#### Arguments

H3 list, resulting from a call to Hydro3\_Estimation()

useU logical, use reduced variate u rather than return period T in plots?

lwd, cex.lab, cex.axis, pch

numeric, graphical parameters, see ?graphics::par

col character, graphical parameter (points color)

#### Value

```
nothing (just creates a plot)
```

#### **Examples**

```
y=stats::rnorm(50)
H3=Hydro3_Estimation(y,'Normal')
Hydro3_Plot(H3)
```

Import\_HBayConfig

Import HBay Configuration folder

## **Description**

Imports configuration data as specified with HBay executable. Returns NULL if configuration folder is not found

#### Usage

```
Import_HBayConfig(path)
```

#### **Arguments**

path character, path to configuration folder.

#### Value

A list with the following components (see ?Hydro3\_HBay for details):

y numeric matrix, data.

dist character, distribution name.
prior list of lists, prior distributions.

SystErrorIndex integer vector, index of systematic errors.

SystErrorPrior list of lists, prior distribution for each systematic error.

options list, inference options.

mcmcoptions list, MCMC options.

year numeric vector, years.

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#### **Examples**

KS

Kolmogorov-Smirnov Test

# Description

Applies a one-sample Kolmogorov-Smirnov test (see ?stats::ks.test)

#### Usage

```
KS(y, dist, par)
```

# Arguments

y numeric vector, data
dist character, distribution name
par numeric vector, parameter vector

#### Value

A list with the following components:

pval numeric, p-value of the test
stat numeric, test statistics
xtra numeric, xtra information: empty for this test

```
y=stats::rnorm(20)
KS(y,'Normal',c(0,1))
KS(y,'Normal',c(1,1))
KS(y,'Gumbel',c(0,1))
```

mcmcoptions\_def 29

mcmcoptions	def

Default MCMC options

#### **Description**

A named list containing the default MCMC options. See ?Hydro3\_Estimation for more details.

# Usage

```
mcmcoptions_def
```

#### **Format**

An object of class list of length 10.

Metropolis\_OAAT

One-At-A-Time Metropolis sampler

# Description

Performs nsim iterations of the OAAT Metropolis sampler (simulated vector is updated one component at a time). a.k.a block Metropolis sampler with blocks of length one. Sometimes also called 'Metropolis-within-Gibbs'.

#### Usage

```
Metropolis_OAAT(f, x0, nsim, sdjump, ...)
```

# **Arguments**

f function, log-pdf of the target distribution

x0 numeric vector, starting point nsim integer, number of simulations

sdjump numeric vector, standard deviation of the Gaussian jump for each component

... other arguments passed to f

#### Value

A list with the following components:

x numeric matrix nsim\*length(x0), MCMC simulations

fx numeric vector, corresponding values f(x)

moverate numeric vector, move rate associated with each component

#### **Examples**

```
# Bivariate target distribution: beta(0.8,0.4) X exp(1) f=function(x){stats::dbeta(x[1],0.8,0.4,log=TRUE)+stats::dexp(x[2],log=TRUE)} x0=c(0.5,2) sdjump=c(0.5,1) mcmc=Metropolis_OAAT(f,x0,1000,sdjump) graphicalpar=par(mfrow=c(1,3)) plot(mcmc$x);hist(mcmc$x[,1]); hist(mcmc$x[,2]) par(graphicalpar)
```

Metropolis\_OAAT\_adaptive

Adaptive One-At-A-Time Metropolis sampler

# Description

Performs nsim iterations of the Adaptive version of the OAAT Metropolis sampler (see ?Metropolis\_OAAT). Adaptation is performed by monitoring move rates every batch.length iterations, and increasing / decreasing the jump standard deviation if the move rate is not within specified bounds.

#### Usage

```
Metropolis_OAAT_adaptive(
   f,
   x0,
   sdjump,
   ...,
   batch.length = 100,
   batch.n = 100,
   moverate.min = 0.1,
   moverate.max = 0.5,
   mult.down = 0.9,
   mult.up = 1.1
)
```

#### **Arguments**

f	function, log-pdf of the target distribution
x0	numeric vector, starting point
sdjump	numeric vector, initial standard deviation of the Gaussian jump for each component
	other arguments passed to f
batch.length	integer, length of each non-adaptive batch
batch.n	integer, number of batches (= adaptation period). Total number of simulations is nsim=batch.n*batch.length

moverate.min numeric in (0;1), lower bound for the desired move rate interval numeric in (0;1), upper bound for the desired move rate interval

mult.down numeric in (0;1), multiplication factor used to decrease jump size when move

rate is too low.

mult.up numeric (>1, avoid 1/mult.down) multiplication factor used to increase jump

size when move rate is too high.

#### Value

A list with the following components:

x numeric matrix nsim\*length(x0), MCMC simulations

fx numeric vector, corresponding values f(x)

## **Examples**

```
# Bivariate target distribution: beta(0.8,0.4) X exp(1) f=function(x)\{stats::dbeta(x[1],0.8,0.4,log=TRUE)+stats::dexp(x[2],log=TRUE)\}\\ x0=c(0.5,2)\\ sdjump=c(0.5,1)\\ mcmc=Metropolis_OAAT_adaptive(f,x0,sdjump)\\ graphicalpar=par(mfrow=c(1,3))\\ plot(mcmc$x);hist(mcmc$x[,1]); hist(mcmc$x[,2])\\ par(graphicalpar)
```

#### **Description**

Performs a single iteration of the OAAT Metropolis sampler (simulated vector is updated one component at a time). a.k.a block Metropolis sampler with blocks of length one. Sometimes also called 'Metropolis-within-Gibbs'.

#### Usage

```
Metropolis_OAAT_jump(f, x0, fx0, sdjump, ...)
```

# **Arguments**

f	function, log-pdf of the target distribution
x0	numeric vector, starting point
fx0	numeric, $f(x0)$
sdjump	numeric vector, standard deviation of the Gaussian jump for each component
	other arguments passed to f

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### Value

A list with the following components:

x numeric vector, updated point after the iteration

fx numeric, updated value f(x)

move logical vector, TRUE for components of the vector x that changed

# **Examples**

```
# Bivariate target distribution: beta(2,10) X exp(1) f=function(x){stats::dbeta(x[1],2,10,log=TRUE)+stats::dexp(x[2],log=TRUE)} x0=c(0.5,0.5) fx0=f(x0) sdjump=c(0.1,0.1) Metropolis_OAAT_jump(f,x0,fx0,sdjump)
```

MK

Mann-Kemdall Test

### **Description**

Applies the Mann-Kendall trend test

### Usage

MK(y)

### **Arguments**

y numeric vector, data

#### Value

A list with the following components:

pval numeric, p-value of the test stat numeric, test statistics

xtra numeric, xtra information: empty for this test

```
y=stats::rnorm(50)
MK(y)
y=y+0.1*(1:length(y))
MK(y)
```

options\_def 33

options\_def

Default estimation options

# Description

A named list containing the default estimation options. See ?Hydro3\_Estimation for more details.

# Usage

```
options_def
```

#### **Format**

An object of class list of length 9.

Pettitt

Pettitt Test

# **Description**

Applies the Pettitt step-change test

## Usage

```
Pettitt(y)
```

#### **Arguments**

у

numeric vector, data

# Value

A list with the following components:

pval numeric, p-value of the test stat numeric, test statistics

xtra numeric, xtra information: position of the step change

```
y=stats::rnorm(50)
Pettitt(y)
y[26:50]=y[26:50]+2
Pettitt(y)
```

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