

# Package ‘eco’

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**Title** Ecological Inference in 2x2 Tables

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**Depends** R (>= 2.0), MASS, utils

**Suggests** testthat

**Description** Implements the Bayesian and likelihood methods proposed in Imai, Lu, and Strauss (2008 <[doi:10.1093/pan/mpm017](https://doi.org/10.1093/pan/mpm017)>) and (2011 <[doi:10.18637/jss.v042.i05](https://doi.org/10.18637/jss.v042.i05)>) for ecological inference in 2 by 2 tables as well as the method of bounds introduced by Duncan and Davis (1953). The package fits both parametric and nonparametric models using either the Expectation-Maximization algorithms (for likelihood models) or the Markov chain Monte Carlo algorithms (for Bayesian models). For all models, the individual-level data can be directly incorporated into the estimation whenever such data are available. Along with in-sample and out-of-sample predictions, the package also provides a functionality which allows one to quantify the effect of data aggregation on parameter estimation and hypothesis testing under the parametric likelihood models.

**LazyLoad** yes

**LazyData** yes

**License** GPL (>= 2)

**URL** <https://github.com/kosukeimai/eco>

**BugReports** <https://github.com/kosukeimai/eco/issues>

**RoxygenNote** 7.3.3

**NeedsCompilation** yes

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**Repository** CRAN

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census	<i>Black Illiteracy Rates in 1910 US Census</i>
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### Description

This data set contains the proportion of the residents who are black, the proportion of those who can read, the total population as well as the actual black literacy rate and white literacy rate for 1040 counties in the US. The dataset was originally analyzed by Robinson (1950) at the state level. King (1997) recoded the 1910 census at county level. The data set only includes those who are older than 10 years of age.

### Format

A data frame containing 5 variables and 1040 observations

X	numeric	the proportion of Black residents in each county
Y	numeric	the overall literacy rates in each county
N	numeric	the total number of residents in each county
W1	numeric	the actual Black literacy rate
W2	numeric	the actual White literacy rate

## References

- Robinson, W.S. (1950). "Ecological Correlations and the Behavior of Individuals." *American Sociological Review*, vol. 15, pp.351-357.
- King, G. (1997). "A Solution to the Ecological Inference Problem: Reconstructing Individual Behavior from Aggregate Data". Princeton University Press, Princeton, NJ.

eco

*Fitting the Parametric Bayesian Model of Ecological Inference in 2x2 Tables*

## Description

eco is used to fit the parametric Bayesian model (based on a Normal/Inverse-Wishart prior) for ecological inference in  $2 \times 2$  tables via Markov chain Monte Carlo. It gives the in-sample predictions as well as the estimates of the model parameters. The model and algorithm are described in Imai, Lu and Strauss (2008, 2011).

## Usage

```
eco(
  formula,
  data = parent.frame(),
  N = NULL,
  supplement = NULL,
  context = FALSE,
  mu0 = 0,
  tau0 = 2,
  nu0 = 4,
  S0 = 10,
  mu.start = 0,
  Sigma.start = 10,
  parameter = TRUE,
  grid = FALSE,
  n.draws = 5000,
  burnin = 0,
  thin = 0,
  verbose = FALSE
)
```

## Arguments

formula	A symbolic description of the model to be fit, specifying the column and row margins of $2 \times 2$ ecological tables. $Y \sim X$ specifies $Y$ as the column margin (e.g., turnout) and $X$ as the row margin (e.g., percent African-American). Details and specific examples are given below.
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<b>data</b>	An optional data frame in which to interpret the variables in <b>formula</b> . The default is the environment in which <b>eco</b> is called.
<b>N</b>	An optional variable representing the size of the unit; e.g., the total number of voters. <b>N</b> needs to be a vector of same length as <b>Y</b> and <b>X</b> or a scalar.
<b>supplement</b>	An optional matrix of supplemental data. The matrix has two columns, which contain additional individual-level data such as survey data for $W_1$ and $W_2$ , respectively. If <b>NULL</b> , no additional individual-level data are included in the model. The default is <b>NULL</b> .
<b>context</b>	Logical. If <b>TRUE</b> , the contextual effect is also modeled, that is to assume the row margin <b>X</b> and the unknown $W_1$ and $W_2$ are correlated. See Imai, Lu and Strauss (2008, 2011) for details. The default is <b>FALSE</b> .
<b>mu0</b>	A scalar or a numeric vector that specifies the prior mean for the mean parameter $\mu$ for $(W_1, W_2)$ (or for $(W_1, W_2, X)$ if <b>context=TRUE</b> ). When the input of <b>mu0</b> is a scalar, its value will be repeated to yield a vector of the length of $\mu$ , otherwise, it needs to be a vector of same length as $\mu$ . When <b>context=TRUE</b> , the length of $\mu$ is 3, otherwise it is 2. The default is 0.
<b>tau0</b>	A positive integer representing the scale parameter of the Normal-Inverse Wishart prior for the mean and variance parameter $(\mu, \Sigma)$ . The default is 2.
<b>nu0</b>	A positive integer representing the prior degrees of freedom of the Normal-Inverse Wishart prior for the mean and variance parameter $(\mu, \Sigma)$ . The default is 4.
<b>S0</b>	A positive scalar or a positive definite matrix that specifies the prior scale matrix of the Normal-Inverse Wishart prior for the mean and variance parameter $(\mu, \Sigma)$ . If it is a scalar, then the prior scale matrix will be a diagonal matrix with the same dimensions as $\Sigma$ and the diagonal elements all take value of <b>S0</b> , otherwise <b>S0</b> needs to have same dimensions as $\Sigma$ . When <b>context=TRUE</b> , $\Sigma$ is a $3 \times 3$ matrix, otherwise, it is $2 \times 2$ . The default is 10.
<b>mu.start</b>	A scalar or a numeric vector that specifies the starting values of the mean parameter $\mu$ . If it is a scalar, then its value will be repeated to yield a vector of the length of $\mu$ , otherwise, it needs to be a vector of same length as $\mu$ . When <b>context=FALSE</b> , the length of $\mu$ is 2, otherwise it is 3. The default is 0.
<b>Sigma.start</b>	A scalar or a positive definite matrix that specified the starting value of the variance matrix $\Sigma$ . If it is a scalar, then the prior scale matrix will be a diagonal matrix with the same dimensions as $\Sigma$ and the diagonal elements all take value of <b>S0</b> , otherwise <b>S0</b> needs to have same dimensions as $\Sigma$ . When <b>context=TRUE</b> , $\Sigma$ is a $3 \times 3$ matrix, otherwise, it is $2 \times 2$ . The default is 10.
<b>parameter</b>	Logical. If <b>TRUE</b> , the Gibbs draws of the population parameters, $\mu$ and $\Sigma$ , are returned in addition to the in-sample predictions of the missing internal cells, $W$ . The default is <b>TRUE</b> .
<b>grid</b>	Logical. If <b>TRUE</b> , the grid method is used to sample $W$ in the Gibbs sampler. If <b>FALSE</b> , the Metropolis algorithm is used where candidate draws are sampled from the uniform distribution on the tomography line for each unit. Note that the grid method is significantly slower than the Metropolis algorithm. The default is <b>FALSE</b> .
<b>n.draws</b>	A positive integer. The number of MCMC draws. The default is 5000.

burnin	A positive integer. The burnin interval for the Markov chain; i.e. the number of initial draws that should not be stored. The default is 0.
thin	A positive integer. The thinning interval for the Markov chain; i.e. the number of Gibbs draws between the recorded values that are skipped. The default is 0.
verbose	Logical. If TRUE, the progress of the Gibbs sampler is printed to the screen. The default is FALSE.

## Details

An example of  $2 \times 2$  ecological table for racial voting is given below:

$$\begin{array}{ccccc}
 & & \text{black voters} & \text{white voters} & \\
 & \text{vote} & W_{1i} & W_{2i} & Y_i \\
 & \text{not vote} & 1 - W_{1i} & 1 - W_{2i} & 1 - Y_i \\
 & & X_i & 1 - X_i &
 \end{array}$$

where  $Y_i$  and  $X_i$  represent the observed margins, and  $W_1$  and  $W_2$  are unknown variables. In this example,  $Y_i$  is the turnout rate in the  $i$ th precinct,  $X_i$  is the proportion of African American in the  $i$ th precinct. The unknowns  $W_{1i}$  and  $W_{2i}$  are the black and white turnout, respectively. All variables are proportions and hence bounded between 0 and 1. For each  $i$ , the following deterministic relationship holds,  $Y_i = X_i W_{1i} + (1 - X_i) W_{2i}$ .

## Value

An object of class eco containing the following elements:

call	The matched call.
X	The row margin, $X$ .
Y	The column margin, $Y$ .
N	The size of each table, $N$ .
burnin	The number of initial burnin draws.
thin	The thinning interval.
nu0	The prior degrees of freedom.
tau0	The prior scale parameter.
mu0	The prior mean.
S0	The prior scale matrix.
W	A three dimensional array storing the posterior in-sample predictions of $W$ . The first dimension indexes the Monte Carlo draws, the second dimension indexes the columns of the table, and the third dimension represents the observations.
Wmin	A numeric matrix storing the lower bounds of $W$ .
Wmax	A numeric matrix storing the upper bounds of $W$ .

The following additional elements are included in the output when parameter = TRUE.

mu	The posterior draws of the population mean parameter, $\mu$ .
Sigma	The posterior draws of the population variance matrix, $\Sigma$ .

## References

- Imai, Kosuke, Ying Lu and Aaron Strauss. (2011). “eco: R Package for Ecological Inference in 2x2 Tables” Journal of Statistical Software, Vol. 42, No. 5, pp. 1-23.
- Imai, Kosuke, Ying Lu and Aaron Strauss. (2008). “Bayesian and Likelihood Inference for 2 x 2 Ecological Tables: An Incomplete Data Approach” Political Analysis, Vol. 16, No. 1 (Winter), pp. 41-69.

## See Also

`ecoML`, `ecoNP`, `predict.eco`, `summary.eco`

## Examples

```
## load the registration data
data(reg)

## NOTE: convergence has not been properly assessed for the following
## examples. See Imai, Lu and Strauss (2008, 2011) for more
## complete analyses.

## fit the parametric model with the default prior specification
res <- eco(Y ~ X, data = reg, verbose = TRUE)
## summarize the results
summary(res)

## obtain out-of-sample prediction
out <- predict(res, verbose = TRUE)
## summarize the results
summary(out)

## load the Robinson's census data
data(census)

## fit the parametric model with contextual effects and N
## using the default prior specification
res1 <- eco(Y ~ X, N = N, context = TRUE, data = census, verbose = TRUE)
## summarize the results
summary(res1)

## obtain out-of-sample prediction
out1 <- predict(res1, verbose = TRUE)
## summarize the results
summary(out1)
```

## Description

ecoBD is used to calculate the bounds for missing internal cells of  $R \times C$  ecological table. The data can be entered either in the form of counts or proportions.

## Usage

```
ecoBD(formula, data = parent.frame(), N = NULL)
```

## Arguments

<code>formula</code>	A symbolic description of ecological table to be used, specifying the column and row margins of $R \times C$ ecological tables. Details and specific examples are given below.
<code>data</code>	An optional data frame in which to interpret the variables in <code>formula</code> . The default is the environment in which ecoBD is called.
<code>N</code>	An optional variable representing the size of the unit; e.g., the total number of voters. If <code>formula</code> is entered as counts and the last row and/or column is omitted, this input is necessary.

## Details

The data may be entered either in the form of counts or proportions. If proportions are used, `formula` may omit the last row and/or column of tables, which can be calculated from the remaining margins. For example,  $Y \sim X$  specifies  $Y$  as the first column margin and  $X$  as the first row margin in  $2 \times 2$  tables. If counts are used, `formula` may omit the last row and/or column margin of the table only if `N` is supplied. In this example, the columns will be labeled as  $X$  and not  $X$ , and the rows will be labeled as  $Y$  and not  $Y$ .

For larger tables, one can use `cbind()` and `+`. For example,  $\text{cbind}(Y_1, Y_2, Y_3) \sim X_1 + X_2 + X_3 + X_4$  specifies  $3 \times 4$  tables.

An  $R \times C$  ecological table in the form of counts:

$$\begin{array}{ccccc} n_{i11} & n_{i12} & \dots & n_{i1C} & n_{i1.} \\ n_{i21} & n_{i22} & \dots & n_{i2C} & n_{i2.} \\ \dots & \dots & \dots & \dots & \dots \\ n_{iR1} & n_{iR2} & \dots & n_{iRC} & n_{iR.} \\ n_{i.1} & n_{i.2} & \dots & n_{i.C} & N_i \end{array}$$

where  $n_{nr.}$  and  $n_{i.c}$  represent the observed margins,  $N_i$  represents the size of the table, and  $n_{irc}$  are unknown variables. Note that for each  $i$ , the following deterministic relationships hold;  $n_{ir.} = \sum_{c=1}^C n_{irc}$  for  $r = 1, \dots, R$ , and  $n_{i.c} = \sum_{r=1}^R n_{irc}$  for  $c = 1, \dots, C$ . Then, each of the unknown inner cells can be bounded in the following manner,

$$\max(0, n_{ir.} + n_{i.c} - N_i) \leq n_{irc} \leq \min(n_{ir.}, n_{i.c}).$$

If the size of tables,  $N$ , is provided,

An  $R \times C$  ecological table in the form of proportions:

$$\begin{array}{ccccc} W_{i11} & W_{i12} & \dots & W_{i1C} & Y_{i1} \\ W_{i21} & W_{i22} & \dots & W_{i2C} & Y_{i2} \\ \dots & \dots & \dots & \dots & \dots \\ W_{iR1} & W_{iR2} & \dots & W_{iRC} & Y_{iR} \\ X_{i1} & X_{i2} & \dots & X_{iC} & \end{array}$$

where  $Y_{ir}$  and  $X_{ic}$  represent the observed margins, and  $W_{irc}$  are unknown variables. Note that for each  $i$ , the following deterministic relationships hold;  $Y_{ir} = \sum_{c=1}^C X_{ic} W_{irc}$  for  $r = 1, \dots, R$ , and  $\sum_{r=1}^R W_{irc} = 1$  for  $c = 1, \dots, C$ . Then, each of the inner cells of the table can be bounded in the following manner,

$$\max(0, (X_{ic} + Y_{ir} - 1)/X_{ic}) \leq W_{irc} \leq \min(1, Y_{ir}/X_{ir}).$$

### Value

An object of class `ecoBD` containing the following elements (When three dimensional arrays are used, the first dimension indexes the observations, the second dimension indexes the row numbers, and the third dimension indexes the column numbers):

<code>call</code>	The matched call.
<code>X</code>	A matrix of the observed row margin, $X$ .
<code>Y</code>	A matrix of the observed column margin, $Y$ .
<code>N</code>	A vector of the size of ecological tables, $N$ .
<code>aggWmin</code>	A three dimensional array of aggregate lower bounds for proportions.
<code>aggWmax</code>	A three dimensional array of aggregate upper bounds for proportions.
<code>Wmin</code>	A three dimensional array of lower bounds for proportions.
<code>Wmax</code>	A three dimensional array of upper bounds for proportions.
<code>Nmin</code>	A three dimensional array of lower bounds for counts.
<code>Nmax</code>	A three dimensional array of upper bounds for counts.

The object can be printed through `print.ecoBD`.

### References

Imai, Kosuke, Ying Lu and Aaron Strauss. (2011) “eco: R Package for Ecological Inference in 2x2 Tables” Journal of Statistical Software, Vol. 42, No. 5, pp. 1-23.

Imai, Kosuke, Ying Lu and Aaron Strauss. (2008) “Bayesian and Likelihood Inference for 2 x 2 Ecological Tables: An Incomplete Data Approach” Political Analysis, Vol. 16, No. 1, (Winter), pp. 41-69.

### See Also

`eco`, `ecoNP`

## Examples

```
## load the registration data
data(reg)

## calculate the bounds
res <- ecoBD(Y ~ X, N = N, data = reg)
## print the results
print(res)
```

ecoML

*Fitting Parametric Models and Quantifying Missing Information for Ecological Inference in 2x2 Tables*

## Description

ecoML is used to fit parametric models for ecological inference in  $2 \times 2$  tables via Expectation Maximization (EM) algorithms. The data is specified in proportions. At its most basic setting, the algorithm assumes that the individual-level proportions (i.e.,  $W_1$  and  $W_2$ ) are distributed bivariate normally (after logit transformations). The function calculates point estimates of the parameters for models based on different assumptions. The standard errors of the point estimates are also computed via Supplemented EM algorithms. Moreover, ecoML quantifies the amount of missing information associated with each parameter and allows researcher to examine the impact of missing information on parameter estimation in ecological inference. The models and algorithms are described in Imai, Lu and Strauss (2008, 2011).

## Usage

```
ecoML(
  formula,
  data = parent.frame(),
  N = NULL,
  supplement = NULL,
  theta.start = c(0, 0, 1, 1, 0),
  fix.rho = FALSE,
  context = FALSE,
  sem = TRUE,
  epsilon = 10^(-6),
  maxit = 1000,
  loglik = TRUE,
  hyptest = FALSE,
  verbose = FALSE
)
```

## Arguments

<code>formula</code>	A symbolic description of the model to be fit, specifying the column and row margins of $2 \times 2$ ecological tables. $Y \sim X$ specifies $Y$ as the column margin (e.g., turnout) and $X$ (e.g., percent African-American) as the row margin. Details and specific examples are given below.
<code>data</code>	An optional data frame in which to interpret the variables in <code>formula</code> . The default is the environment in which <code>ecoML</code> is called.
<code>N</code>	An optional variable representing the size of the unit; e.g., the total number of voters. <code>N</code> needs to be a vector of same length as $Y$ and $X$ or a scalar.
<code>supplement</code>	An optional matrix of supplemental data. The matrix has two columns, which contain additional individual-level data such as survey data for $W_1$ and $W_2$ , respectively. If <code>NULL</code> , no additional individual-level data are included in the model. The default is <code>NULL</code> .
<code>theta.start</code>	A numeric vector that specifies the starting values for the mean, variance, and covariance. When <code>context = FALSE</code> , the elements of <code>theta.start</code> correspond to $(E(W_1), E(W_2), var(W_1), var(W_2), cor(W_1, W_2))$ . When <code>context = TRUE</code> , the elements of <code>theta.start</code> correspond to $(E(W_1), E(W_2), var(W_1), var(W_2), corr(W_1, X), corr(W_2, X), corr(W_1, W_2))$ . Moreover, when <code>fix.rho=TRUE</code> , <code>corr(W_1, W_2)</code> is set to be the correlation between $W_1$ and $W_2$ when <code>context = FALSE</code> , and the partial correlation between $W_1$ and $W_2$ given $X$ when <code>context = TRUE</code> . The default is <code>c(0, 0, 1, 1, 0)</code> .
<code>fix.rho</code>	Logical. If <code>TRUE</code> , the correlation (when <code>context=TRUE</code> ) or the partial correlation (when <code>context=FALSE</code> ) between $W_1$ and $W_2$ is fixed through the estimation. For details, see Imai, Lu and Strauss(2006). The default is <code>FALSE</code> .
<code>context</code>	Logical. If <code>TRUE</code> , the contextual effect is also modeled. In this case, the row margin (i.e., $X$ ) and the individual-level rates (i.e., $W_1$ and $W_2$ ) are assumed to be distributed tri-variate normally (after logit transformations). See Imai, Lu and Strauss (2006) for details. The default is <code>FALSE</code> .
<code>sem</code>	Logical. If <code>TRUE</code> , the standard errors of parameter estimates are estimated via SEM algorithm, as well as the fraction of missing data. The default is <code>TRUE</code> .
<code>epsilon</code>	A positive number that specifies the convergence criterion for EM algorithm. The square root of <code>epsilon</code> is the convergence criterion for SEM algorithm. The default is $10^{-6}$ .
<code>maxit</code>	A positive integer specifies the maximum number of iterations before the convergence criterion is met. The default is <code>1000</code> .
<code>loglik</code>	Logical. If <code>TRUE</code> , the value of the log-likelihood function at each iteration of EM is saved. The default is <code>TRUE</code> .
<code>hyptest</code>	Logical. If <code>TRUE</code> , model is estimated under the null hypothesis that means of $W_1$ and $W_2$ are the same. The default is <code>FALSE</code> .
<code>verbose</code>	Logical. If <code>TRUE</code> , the progress of the EM and SEM algorithms is printed to the screen. The default is <code>FALSE</code> .

## Details

When `SEM` is `TRUE`, `ecoML` computes the observed-data information matrix for the parameters of interest based on Supplemented-EM algorithm. The inverse of the observed-data information matrix

can be used to estimate the variance-covariance matrix for the parameters estimated from EM algorithms. In addition, it also computes the expected complete-data information matrix. Based on these two measures, one can further calculate the fraction of missing information associated with each parameter. See Imai, Lu and Strauss (2006) for more details about fraction of missing information.

Moreover, when `hytest=TRUE`, ecoML allows to estimate the parametric model under the null hypothesis that  $\mu_1=\mu_2$ . One can then construct the likelihood ratio test to assess the hypothesis of equal means. The associated fraction of missing information for the test statistic can be also calculated. For details, see Imai, Lu and Strauss (2006) for details.

### Value

An object of class `ecoML` containing the following elements:

<code>call</code>	The matched call.
<code>X</code>	The row margin, $X$ .
<code>Y</code>	The column margin, $Y$ .
<code>N</code>	The size of each table, $N$ .
<code>context</code>	The assumption under which model is estimated. If <code>context = FALSE</code> , CAR assumption is adopted and no contextual effect is modeled. If <code>context = TRUE</code> , NCAR assumption is adopted, and contextual effect is modeled.
<code>sem</code>	Whether SEM algorithm is used to estimate the standard errors and observed information matrix for the parameter estimates.
<code>fix.rho</code>	Whether the correlation or the partial correlation between $W_1$ and $W_2$ is fixed in the estimation.
<code>r12</code>	If <code>fix.rho = TRUE</code> , the value that $\text{corr}(W_1, W_2)$ is fixed to.
<code>epsilon</code>	The precision criterion for EM convergence. $\sqrt{\epsilon}$ is the precision criterion for SEM convergence.
<code>theta.sem</code>	The ML estimates of $E(W_1), E(W_2), \text{var}(W_1), \text{var}(W_2)$ , and $\text{cov}(W_1, W_2)$ . If <code>context = TRUE</code> , $E(X), \text{cov}(W_1, X), \text{cov}(W_2, X)$ are also reported.
<code>W</code>	In-sample estimation of $W_1$ and $W_2$ .
<code>suff.stat</code>	The sufficient statistics for <code>theta.em</code> .
<code>iters.em</code>	Number of EM iterations before convergence is achieved.
<code>iters.sem</code>	Number of SEM iterations before convergence is achieved.
<code>loglik</code>	The log-likelihood of the model when convergence is achieved.
<code>loglik.log.em</code>	A vector saving the value of the log-likelihood function at each iteration of the EM algorithm.
<code>mu.log.em</code>	A matrix saving the unweighted mean estimation of the logit-transformed individual-level proportions (i.e., $W_1$ and $W_2$ ) at each iteration of the EM process.
<code>Sigma.log.em</code>	A matrix saving the log of the variance estimation of the logit-transformed individual-level proportions (i.e., $W_1$ and $W_2$ ) at each iteration of EM process. Note, non-transformed variances are displayed on the screen (when <code>verbose = TRUE</code> ).

**rho.fisher.em** A matrix saving the fisher transformation of the estimation of the correlations between the logit-transformed individual-level proportions (i.e.,  $W_1$  and  $W_2$ ) at each iteration of EM process. Note, non-transformed correlations are displayed on the screen (when verbose = TRUE).

Moreover, when sem=TRUE, ecoML also output the following values:

<b>DM</b>	The matrix characterizing the rates of convergence of the EM algorithms. Such information is also used to calculate the observed-data information matrix
<b>Icom</b>	The (expected) complete data information matrix estimated via SEM algorithm. When context=FALSE, fix.rho=TRUE, Icom is 4 by 4. When context=FALSE, fix.rho=FALSE, Icom is 5 by 5. When context=TRUE, Icom is 9 by 9.
<b>Iobs</b>	The observed information matrix. The dimension of Iobs is same as Icom.
<b>Imiss</b>	The difference between Icom and Iobs. The dimension of Imiss is same as miss.
<b>Vobs</b>	The (symmetrized) variance-covariance matrix of the ML parameter estimates. The dimension of Vobs is same as Icom.
<b>Iobs</b>	The (expected) complete-data variance-covariance matrix. The dimension of Iobs is same as Icom.
<b>Vobs.original</b>	The estimated variance-covariance matrix of the ML parameter estimates. The dimension of Vobs is same as Icom.
<b>Fmis</b>	The fraction of missing information associated with each parameter estimation.
<b>VFmis</b>	The proportion of increased variance associated with each parameter estimation due to observed data.
<b>Ieigen</b>	The largest eigen value of Imiss.
<b>Icom.trans</b>	The complete data information matrix for the fisher transformed parameters.
<b>Iobs.trans</b>	The observed data information matrix for the fisher transformed parameters.
<b>Fmis.trans</b>	The fractions of missing information associated with the fisher transformed parameters.

## References

Imai, Kosuke, Ying Lu and Aaron Strauss. (2011). “eco: R Package for Ecological Inference in 2x2 Tables” Journal of Statistical Software, Vol. 42, No. 5, pp. 1-23.

Imai, Kosuke, Ying Lu and Aaron Strauss. (2008). “Bayesian and Likelihood Inference for 2 x 2 Ecological Tables: An Incomplete Data Approach” Political Analysis, Vol. 16, No. 1 (Winter), pp. 41-69.

## See Also

`eco`, `ecoNP`, `summary.ecoML`

## Examples

```

## load the census data
data(census)

## NOTE: convergence has not been properly assessed for the following
## examples. See Imai, Lu and Strauss (2006) for more complete analyses.
## In the first example below, in the interest of time, only part of the
## data set is analyzed and the convergence requirement is less stringent
## than the default setting.

## In the second example, the program is arbitrarily halted 100 iterations
## into the simulation, before convergence.

## load the Robinson's census data
data(census)

## fit the parametric model with the default model specifications
res <- ecoML(Y ~ X, data = census[1:100,], N=census[1:100,3],
               epsilon=10^(-6), verbose = TRUE)
## summarize the results
summary(res)

## fit the parametric model with some individual
## level data using the default prior specification
surv <- 1:600
res1 <- ecoML(Y ~ X, context = TRUE, data = census[-surv,],
                supplement = census[surv,c(4:5,1)], maxit=100, verbose = TRUE)
## summarize the results
summary(res1)

```

## Description

ecoNP is used to fit the nonparametric Bayesian model (based on a Dirichlet process prior) for ecological inference in  $2 \times 2$  tables via Markov chain Monte Carlo. It gives the in-sample predictions as well as out-of-sample predictions for population inference. The models and algorithms are described in Imai, Lu and Strauss (2008, 2011).

## Usage

```

ecoNP(
  formula,
  data = parent.frame(),
  N = NULL,

```

```

supplement = NULL,
context = FALSE,
mu0 = 0,
tau0 = 2,
nu0 = 4,
S0 = 10,
alpha = NULL,
a0 = 1,
b0 = 0.1,
parameter = FALSE,
grid = FALSE,
n.draws = 5000,
burnin = 0,
thin = 0,
verbose = FALSE
)

```

## Arguments

formula	A symbolic description of the model to be fit, specifying the column and row margins of $2 \times 2$ ecological tables. $Y \sim X$ specifies $Y$ as the column margin (e.g., turnout) and $X$ as the row margin (e.g., percent African-American). Details and specific examples are given below.
data	An optional data frame in which to interpret the variables in formula. The default is the environment in which ecoNP is called.
N	An optional variable representing the size of the unit; e.g., the total number of voters. N needs to be a vector of same length as Y and X or a scalar.
supplement	An optional matrix of supplemental data. The matrix has two columns, which contain additional individual-level data such as survey data for $W_1$ and $W_2$ , respectively. If NULL, no additional individual-level data are included in the model. The default is NULL.
context	Logical. If TRUE, the contextual effect is also modeled, that is to assume the row margin $X$ and the unknown $W_1$ and $W_2$ are correlated. See Imai, Lu and Strauss (2008, 2011) for details. The default is FALSE.
mu0	A scalar or a numeric vector that specifies the prior mean for the mean parameter $\mu$ of the base prior distribution $G_0$ (see Imai, Lu and Strauss (2008, 2011) for detailed descriptions of Dirichlet prior and the normal base prior distribution). If it is a scalar, then its value will be repeated to yield a vector of the length of $\mu$ , otherwise, it needs to be a vector of same length as $\mu$ . When context=TRUE, the length of $\mu$ is 3, otherwise it is 2. The default is 0.
tau0	A positive integer representing the scale parameter of the Normal-Inverse Wishart prior for the mean and variance parameter $(\mu_i, \Sigma_i)$ of each observation. The default is 2.
nu0	A positive integer representing the prior degrees of freedom of the variance matrix $\Sigma_i$ . the default is 4.
S0	A positive scalar or a positive definite matrix that specifies the prior scale matrix for the variance matrix $\Sigma_i$ . If it is a scalar, then the prior scale matrix will be

	a diagonal matrix with the same dimensions as $\Sigma_i$ and the diagonal elements all take value of $S0$ , otherwise $S0$ needs to have same dimensions as $\Sigma_i$ . When context=TRUE, $\Sigma$ is a $3 \times 3$ matrix, otherwise, it is $2 \times 2$ . The default is 10.
alpha	A positive scalar representing a user-specified fixed value of the concentration parameter, $\alpha$ . If NULL, $\alpha$ will be updated at each Gibbs draw, and its prior parameters $a0$ and $b0$ need to be specified. The default is NULL.
a0	A positive integer representing the value of shape parameter of the gamma prior distribution for $\alpha$ . The default is 1.
b0	A positive integer representing the value of the scale parameter of the gamma prior distribution for $\alpha$ . The default is 0.1.
parameter	Logical. If TRUE, the Gibbs draws of the population parameters, $\mu$ and $\Sigma$ , are returned in addition to the in-sample predictions of the missing internal cells, $W$ . The default is FALSE. This needs to be set to TRUE if one wishes to make population inferences through predict.eco. See an example below.
grid	Logical. If TRUE, the grid method is used to sample $W$ in the Gibbs sampler. If FALSE, the Metropolis algorithm is used where candidate draws are sampled from the uniform distribution on the tomography line for each unit. Note that the grid method is significantly slower than the Metropolis algorithm.
n.draws	A positive integer. The number of MCMC draws. The default is 5000.
burnin	A positive integer. The burnin interval for the Markov chain; i.e. the number of initial draws that should not be stored. The default is 0.
thin	A positive integer. The thinning interval for the Markov chain; i.e. the number of Gibbs draws between the recorded values that are skipped. The default is 0.
verbose	Logical. If TRUE, the progress of the Gibbs sampler is printed to the screen. The default is FALSE.

## Value

An object of class ecoNP containing the following elements:

call	The matched call.
X	The row margin, $X$ .
Y	The column margin, $Y$ .
burnin	The number of initial burnin draws.
thin	The thinning interval.
nu0	The prior degrees of freedom.
tau0	The prior scale parameter.
mu0	The prior mean.
S0	The prior scale matrix.
a0	The prior shape parameter.
b0	The prior scale parameter.
W	A three dimensional array storing the posterior in-sample predictions of $W$ . The first dimension indexes the Monte Carlo draws, the second dimension indexes the columns of the table, and the third dimension represents the observations.

Wmin	A numeric matrix storing the lower bounds of $W$ .
Wmax	A numeric matrix storing the upper bounds of $W$ .

The following additional elements are included in the output when `parameter = TRUE`.

mu	A three dimensional array storing the posterior draws of the population mean parameter, $\mu$ . The first dimension indexes the Monte Carlo draws, the second dimension indexes the columns of the table, and the third dimension represents the observations.
Sigma	A three dimensional array storing the posterior draws of the population variance matrix, $\Sigma$ . The first dimension indexes the Monte Carlo draws, the second dimension indexes the parameters, and the third dimension represents the observations.
alpha	The posterior draws of $\alpha$ .
nstar	The number of clusters at each Gibbs draw.

## References

- Imai, Kosuke, Ying Lu and Aaron Strauss. (2011). “eco: R Package for Ecological Inference in 2x2 Tables” Journal of Statistical Software, Vol. 42, No. 5, pp. 1-23.
- Imai, Kosuke, Ying Lu and Aaron Strauss. (2008). “Bayesian and Likelihood Inference for 2 x 2 Ecological Tables: An Incomplete Data Approach” Political Analysis, Vol. 16, No. 1 (Winter), pp. 41-69.

## See Also

`eco`, `ecoML`, `predict.eco`, `summary.ecoNP`

## Examples

```
## load the registration data
data(reg)

## NOTE: We set the number of MCMC draws to be a very small number in
## the following examples; i.e., convergence has not been properly
## assessed. See Imai, Lu and Strauss (2006) for more complete examples.

## fit the nonparametric model to give in-sample predictions
## store the parameters to make population inference later
res <- ecoNP(Y ~ X, data = reg, n.draws = 50, param = TRUE, verbose = TRUE)

##summarize the results
summary(res)

## obtain out-of-sample prediction
out <- predict(res, verbose = TRUE)

## summarize the results
summary(out)
```

```

## density plots of the out-of-sample predictions
oldpar <- par(mfrow=c(2,1))
plot(density(out[,1]), main = "W1")
plot(density(out[,2]), main = "W2")

## load the Robinson's census data
data(census)

## fit the parametric model with contextual effects and N
## using the default prior specification

res1 <- ecoNP(Y ~ X, N = N, context = TRUE, param = TRUE, data = census,
n.draws = 25, verbose = TRUE)

## summarize the results
summary(res1)

## out-of sample prediction
pres1 <- predict(res1)
summary(pres1)
par(oldpar)

```

## Description

This data set contains, on a state level, the proportion of white residents ten years and older who are foreign born, and the proportion of those residents who are literate. Data come from the 1930 census and were first analyzed by Robinson (1950).

## Format

A data frame containing 5 variables and 48 observations

X	numeric	proportion of the white population at least 10 years of age that is foreign born
Y	numeric	proportion of the white population at least 10 years of age that is illiterate
W1	numeric	proportion of the foreign-born white population at least 10 years of age that is illiterate
W2	numeric	proportion of the native-born white population at least 10 years of age that is illiterate
ICPSR	numeric	the ICPSR state code

## References

Robinson, W.S. (1950). “Ecological Correlations and the Behavior of Individuals.” *American Sociological Review*, vol. 15, pp.351-357.

forgnlit30c

*Foreign-born literacy in 1930, County Level*

### Description

This data set contains, on a county level, the proportion of white residents ten years and older who are foreign born, and the proportion of those residents who are literate. Data come from the 1930 census and were first analyzed by Robinson (1950). Counties with fewer than 100 foreign born residents are dropped.

### Format

A data frame containing 6 variables and 1976 observations

X	numeric	proportion of the white population at least 10 years of age that is foreign born
Y	numeric	proportion of the white population at least 10 years of age that is illiterate
W1	numeric	proportion of the foreign-born white population at least 10 years of age that is illiterate
W2	numeric	proportion of the native-born white population at least 10 years of age that is illiterate
state	numeric	the ICPSR state code
county	numeric	the ICPSR (within state) county code

### References

Robinson, W.S. (1950). "Ecological Correlations and the Behavior of Individuals." *American Sociological Review*, vol. 15, pp.351-357.

housep88

*Electoral Results for the House and Presidential Races in 1988*

### Description

This data set contains, on a House district level, the percentage of the vote for the Democratic House candidate, the percentage of the vote for the Democratic presidential candidate (Dukakis), the number of voters who voted for a major party candidate in the presidential race, and the ratio of voters in the House race versus the number who cast a ballot for President. Eleven (11) uncontested races are not included. Dataset compiled and analyzed by Burden and Kimball (1988). Complete dataset and documentation available at ICSPR study number 1140.

### Format

A data frame containing 5 variables and 424 observations

X	numeric	proportion voting for the Democrat in the presidential race
Y	numeric	proportion voting for the Democrat in the House race
N	numeric	number of major party voters in the presidential contest

HPCT	numeric	House election turnout divided by presidential election turnout (set to 1 if House turnout exceeds presidential turnout)
DIST	numeric	4-digit ICPSR state and district code: first 2 digits for the state code, last two digits for the district number

## References

Burden, Barry C. and David C. Kimball (1988). "A New Approach To Ticket-Splitting." *The American Political Science Review*. vol 92., no. 3, pp. 553-544.

predict.eco

*Out-of-Sample Posterior Prediction under the Parametric Bayesian Model for Ecological Inference in 2x2 Tables*

## Description

Obtains out-of-sample posterior predictions under the fitted parametric Bayesian model for ecological inference. predict method for class eco and ecoX.

## Usage

```
## S3 method for class 'eco'
predict(object, newdraw = NULL, subset = NULL, verbose = FALSE, ...)
```

## Arguments

object	An output object from eco or ecoNP.
newdraw	An optional list containing two matrices (or three dimensional arrays for the nonparametric model) of MCMC draws of $\mu$ and $\Sigma$ . Those elements should be named as mu and Sigma, respectively. The default is the original MCMC draws stored in object.
subset	A scalar or numerical vector specifying the row number(s) of mu and Sigma in the output object from eco. If specified, the posterior draws of parameters for those rows are used for posterior prediction. The default is NULL where all the posterior draws are used.
verbose	logical. If TRUE, helpful messages along with a progress report on the Monte Carlo sampling from the posterior predictive distributions are printed on the screen. The default is FALSE.
...	further arguments passed to or from other methods.

## Details

The posterior predictive values are computed using the Monte Carlo sample stored in the eco output (or other sample if newdraw is specified). Given each Monte Carlo sample of the parameters, we sample the vector-valued latent variable from the appropriate multivariate Normal distribution. Then, we apply the inverse logit transformation to obtain the predictive values of proportions,  $W$ . The computation may be slow (especially for the nonparametric model) if a large Monte Carlo sample of the model parameters is used. In either case, setting verbose = TRUE may be helpful in monitoring the progress of the code.

**Value**

*predict.eco* yields a matrix of class *predict.eco* containing the Monte Carlo sample from the posterior predictive distribution of inner cells of ecological tables. *summary.predict.eco* will summarize the output, and *print.summary.predict.eco* will print the summary.

**See Also**

*eco*, *predict.ecoNP*

*predict.ecoNP*

*Out-of-Sample Posterior Prediction under the Nonparametric Bayesian Model for Ecological Inference in 2x2 Tables*

**Description**

Obtains out-of-sample posterior predictions under the fitted nonparametric Bayesian model for ecological inference. *predict* method for class *ecoNP* and *ecoNPX*.

**Usage**

```
## S3 method for class 'ecoNP'
predict(
  object,
  newdraw = NULL,
  subset = NULL,
  obs = NULL,
  verbose = FALSE,
  ...
)
```

**Arguments**

<i>object</i>	An output object from <i>ecoNP</i> .
<i>newdraw</i>	An optional list containing two matrices (or three dimensional arrays for the nonparametric model) of MCMC draws of $\mu$ and $\Sigma$ . Those elements should be named as <i>mu</i> and <i>Sigma</i> , respectively. The default is the original MCMC draws stored in <i>object</i> .
<i>subset</i>	A scalar or numerical vector specifying the row number(s) of <i>mu</i> and <i>Sigma</i> in the output object from <i>eco</i> . If specified, the posterior draws of parameters for those rows are used for posterior prediction. The default is <i>NULL</i> where all the posterior draws are used.
<i>obs</i>	An integer or vector of integers specifying the observation number(s) whose posterior draws will be used for predictions. The default is <i>NULL</i> where all the observations in the data set are selected.

verbose	logical. If TRUE, helpful messages along with a progress report on the Monte Carlo sampling from the posterior predictive distributions are printed on the screen. The default is FALSE.
...	further arguments passed to or from other methods.

## Details

The posterior predictive values are computed using the Monte Carlo sample stored in the eco or ecoNP output (or other sample if newdraw is specified). Given each Monte Carlo sample of the parameters, we sample the vector-valued latent variable from the appropriate multivariate Normal distribution. Then, we apply the inverse logit transformation to obtain the predictive values of proportions,  $W$ . The computation may be slow (especially for the nonparametric model) if a large Monte Carlo sample of the model parameters is used. In either case, setting verbose = TRUE may be helpful in monitoring the progress of the code.

## Value

`predict.eco` yields a matrix of class `predict.eco` containing the Monte Carlo sample from the posterior predictive distribution of inner cells of ecological tables. `summary.predict.eco` will summarize the output, and `print.summary.predict.eco` will print the summary.

## See Also

`eco`, `ecoNP`, `summary.eco`, `summary.ecoNP`

<code>predict.ecoNPX</code>	<i>Out-of-Sample Posterior Prediction under the Nonparametric Bayesian Model for Ecological Inference in 2x2 Tables</i>
-----------------------------	---

## Description

Obtains out-of-sample posterior predictions under the fitted nonparametric Bayesian model for ecological inference. `predict` method for class `ecoNP` and `ecoNPX`.

## Usage

```
## S3 method for class 'ecoNPX'
predict(
  object,
  newdraw = NULL,
  subset = NULL,
  obs = NULL,
  cond = FALSE,
  verbose = FALSE,
  ...
)
```

## Arguments

<code>object</code>	An output object from <code>ecoNP</code> .
<code>newdraw</code>	An optional list containing two matrices (or three dimensional arrays for the nonparametric model) of MCMC draws of $\mu$ and $\Sigma$ . Those elements should be named as <code>mu</code> and <code>Sigma</code> , respectively. The default is the original MCMC draws stored in <code>object</code> .
<code>subset</code>	A scalar or numerical vector specifying the row number(s) of <code>mu</code> and <code>Sigma</code> in the output object from <code>eco</code> . If specified, the posterior draws of parameters for those rows are used for posterior prediction. The default is <code>NULL</code> where all the posterior draws are used.
<code>obs</code>	An integer or vector of integers specifying the observation number(s) whose posterior draws will be used for predictions. The default is <code>NULL</code> where all the observations in the data set are selected.
<code>cond</code>	logical. If <code>TRUE</code> , then the conditional prediction will made for the parametric model with contextual effects. The default is <code>FALSE</code> .
<code>verbose</code>	logical. If <code>TRUE</code> , helpful messages along with a progress report on the Monte Carlo sampling from the posterior predictive distributions are printed on the screen. The default is <code>FALSE</code> .
<code>...</code>	further arguments passed to or from other methods.

## Details

The posterior predictive values are computed using the Monte Carlo sample stored in the `eco` or `ecoNP` output (or other sample if `newdraw` is specified). Given each Monte Carlo sample of the parameters, we sample the vector-valued latent variable from the appropriate multivariate Normal distribution. Then, we apply the inverse logit transformation to obtain the predictive values of proportions,  $W$ . The computation may be slow (especially for the nonparametric model) if a large Monte Carlo sample of the model parameters is used. In either case, setting `verbose = TRUE` may be helpful in monitoring the progress of the code.

## Value

`predict.eco` yields a matrix of class `predict.eco` containing the Monte Carlo sample from the posterior predictive distribution of inner cells of ecological tables. `summary.predict.eco` will summarize the output, and `print.summary.predict.eco` will print the summary.

## See Also

`eco`, `ecoNP`, `summary.eco`, `summary.ecoNP`

predict.ecoX

*Out-of-Sample Posterior Prediction under the Parametric Bayesian Model for Ecological Inference in 2x2 Tables*

## Description

Obtains out-of-sample posterior predictions under the fitted parametric Bayesian model for ecological inference. predict method for class eco and ecoX.

## Usage

```
## S3 method for class 'ecoX'
predict(
  object,
  newdraw = NULL,
  subset = NULL,
  newdata = NULL,
  cond = FALSE,
  verbose = FALSE,
  ...
)
```

## Arguments

object	An output object from eco or ecoNP.
newdraw	An optional list containing two matrices (or three dimensional arrays for the nonparametric model) of MCMC draws of $\mu$ and $\Sigma$ . Those elements should be named as mu and Sigma, respectively. The default is the original MCMC draws stored in object.
subset	A scalar or numerical vector specifying the row number(s) of mu and Sigma in the output object from eco. If specified, the posterior draws of parameters for those rows are used for posterior prediction. The default is NULL where all the posterior draws are used.
newdata	An optional data frame containing a new data set for which posterior predictions will be made. The new data set must have the same variable names as those in the original data.
cond	logical. If TRUE, then the conditional prediction will be made for the parametric model with contextual effects. The default is FALSE.
verbose	logical. If TRUE, helpful messages along with a progress report on the Monte Carlo sampling from the posterior predictive distributions are printed on the screen. The default is FALSE.
...	further arguments passed to or from other methods.

## Details

The posterior predictive values are computed using the Monte Carlo sample stored in the eco output (or other sample if newdraw is specified). Given each Monte Carlo sample of the parameters, we sample the vector-valued latent variable from the appropriate multivariate Normal distribution. Then, we apply the inverse logit transformation to obtain the predictive values of proportions,  $W$ . The computation may be slow (especially for the nonparametric model) if a large Monte Carlo sample of the model parameters is used. In either case, setting verbose = TRUE may be helpful in monitoring the progress of the code.

## Value

`predict.eco` yields a matrix of class `predict.eco` containing the Monte Carlo sample from the posterior predictive distribution of inner cells of ecological tables. `summary.predict.eco` will summarize the output, and `print.summary.predict.eco` will print the summary.

## See Also

`eco`, `predict.ecoNP`

<code>print.summary.eco</code>	<i>Print the Summary of the Results for the Bayesian Parametric Model for Ecological Inference in 2x2 Tables</i>
--------------------------------	--

## Description

summary method for class `eco`.

## Usage

```
## S3 method for class 'summary.eco'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

## Arguments

- x An object of class `summary.eco`.
- digits the number of significant digits to use when printing.
- ... further arguments passed to or from other methods.

## Value

`summary.eco` yields an object of class `summary.eco` containing the following elements:

- call The call from `eco`.
- n.obs The number of units.
- n.draws The number of Monte Carlo samples.

`agg.table` Aggregate posterior estimates of the marginal means of  $W_1$  and  $W_2$  using  $X$  and  $N$  as weights.

If `param = TRUE`, the following elements are also included:

`param.table` Posterior estimates of model parameters: population mean estimates of  $W_1$  and  $W_2$  and their logit transformations.

If `units = TRUE`, the following elements are also included:

`W1.table` Unit-level posterior estimates for  $W_1$ .

`W2.table` Unit-level posterior estimates for  $W_2$ .

This object can be printed by `print.summary.eco`

## See Also

`eco, predict.eco`

`print.summary.ecoML` *Print the Summary of the Results for the Maximum Likelihood Parametric Model for Ecological Inference in 2x2 Tables*

## Description

summary method for class `eco`.

## Usage

```
## S3 method for class 'summary.ecoML'
print(x, digits = max(3,getOption("digits") - 3), ...)
```

## Arguments

<code>x</code>	An object of class <code>summary.ecoML</code> .
<code>digits</code>	the number of significant digits to use when printing.
<code>...</code>	further arguments passed to or from other methods.

## Value

`summary.eco` yields an object of class `summary.eco` containing the following elements:

<code>call</code>	The call from <code>eco</code> .
<code>sem</code>	Whether the SEM algorithm was executed, as specified by the user upon calling <code>ecoML</code> .
<code>fix.rho</code>	Whether the correlation parameter was fixed or allowed to vary, as specified by the user upon calling <code>ecoML</code> .
<code>epsilon</code>	The convergence threshold specified by the user upon calling <code>ecoML</code> .

<code>n.obs</code>	The number of units.
<code>iters.em</code>	The number iterations the EM algorithm cycled through before convergence or reaching the maximum number of iterations allowed.
<code>iters.sem</code>	The number iterations the SEM algorithm cycled through before convergence or reaching the maximum number of iterations allowed.
<code>loglik</code>	The final observed log-likelihood.
<code>rho</code>	A matrix of <code>iters.em</code> rows specifying the correlation parameters at each iteration of the EM algorithm. The number of columns depends on how many correlation parameters exist in the model. Column order is the same as the order of the parameters in <code>param.table</code> .
<code>param.table</code>	Final estimates of the parameter values for the model. Excludes parameters fixed by the user upon calling <code>ecoML</code> . See <code>ecoML</code> documentation for order of parameters.
<code>agg.table</code>	Aggregate estimates of the marginal means of $W_1$ and $W_2$
<code>agg.wtable</code>	Aggregate estimates of the marginal means of $W_1$ and $W_2$ using $X$ and $N$ as weights.

If `units = TRUE`, the following elements are also included:

<code>W.table</code>	Unit-level estimates for $W_1$ and $W_2$ .
----------------------	--

This object can be printed by `print.summary.eco`

## See Also

`ecoML`

`print.summary.ecoNP` *Print the Summary of the Results for the Bayesian Nonparametric Model for Ecological Inference in 2x2 Tables*

## Description

summary method for class `ecoNP`.

## Usage

```
## S3 method for class 'summary.ecoNP'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

## Arguments

<code>x</code>	An object of class <code>summary.ecoNP</code> .
<code>digits</code>	the number of significant digits to use when printing.
<code>...</code>	further arguments passed to or from other methods.

**Value**

`summary.ecoNP` yields an object of class `summary.ecoNP` containing the following elements:

<code>call</code>	The call from <code>ecoNP</code> .
<code>n.obs</code>	The number of units.
<code>n.draws</code>	The number of Monte Carlo samples.
<code>agg.table</code>	Aggregate posterior estimates of the marginal means of $W_1$ and $W_2$ using $X$ and $N$ as weights.

If `param = TRUE`, the following elements are also included:

<code>param.table</code>	Posterior estimates of model parameters: population mean estimates of $W_1$ and $W_2$ . If <code>subset</code> is specified, only a subset of the population parameters are included.
--------------------------	---

If `unit = TRUE`, the following elements are also included:

<code>W1.table</code>	Unit-level posterior estimates for $W_1$ .
<code>W2.table</code>	Unit-level posterior estimates for $W_2$ .

This object can be printed by `print.summary.ecoNP`

**See Also**

`ecoNP`, `predict.eco`

Qfun

*Fitting the Parametric Bayesian Model of Ecological Inference in 2x2 Tables*

**Description**

`Qfun` returns the complete log-likelihood that is used to calculate the fraction of missing information.

**Usage**

```
Qfun(theta, suff.stat, n)
```

**Arguments**

<code>theta</code>	A vector that contains the MLE $E(W_1), E(W_2), var(W_1), var(W_2)$ , and $cov(W_1, W_2)$ . Typically it is the element <code>theta.em</code> of an object of class <code>ecoML</code> .
<code>suff.stat</code>	A vector of sufficient statistics of $E(W_1), E(W_2), var(W_1), var(W_2)$ , and $cov(W_1, W_2)$ .
<code>n</code>	A integer representing the sample size.

**Value**

A single numeric value: the complete-data log-likelihood.

**References**

Imai, Kosuke, Ying Lu and Aaron Strauss. (2011). “eco: R Package for Ecological Inference in 2x2 Tables” Journal of Statistical Software, Vol. 42, No. 5, pp. 1-23.

Imai, Kosuke, Ying Lu and Aaron Strauss. (2008). “Bayesian and Likelihood Inference for 2 x 2 Ecological Tables: An Incomplete Data Approach” Political Analysis, Vol. 16, No. 1 (Winter), pp. 41-69.

**See Also**

[ecoML](#)

reg

*Voter Registration in US Southern States*

**Description**

This data set contains the racial composition, the registration rate, the number of eligible voters as well as the actual observed racial registration rates for every county in four US southern states: Florida, Louisiana, North Carolina, and South Carolina.

**Format**

A data frame containing 5 variables and 275 observations

X	numeric	the fraction of Black voters
Y	numeric	the fraction of voters who registered themselves
N	numeric	the total number of voters in each county
W1	numeric	the actual fraction of Black voters who registered themselves
W2	numeric	the actual fraction of White voters who registered themselves

**References**

King, G. (1997). “A Solution to the Ecological Inference Problem: Reconstructing Individual Behavior from Aggregate Data”. Princeton University Press, Princeton, NJ.

---

summary.eco

*Summarizing the Results for the Bayesian Parametric Model for Eco-logical Inference in 2x2 Tables*

---

## Description

summary method for class eco.

## Usage

```
## S3 method for class 'eco'
summary(
  object,
  CI = c(2.5, 97.5),
  param = TRUE,
  units = FALSE,
  subset = NULL,
  ...
)
```

## Arguments

object	An output object from eco.
CI	A vector of lower and upper bounds for the Bayesian credible intervals used to summarize the results. The default is the equal tail 95 percent credible interval.
param	Logical. If TRUE, the posterior estimates of the population parameters will be provided. The default value is TRUE.
units	Logical. If TRUE, the in-sample predictions for each unit or for a subset of units will be provided. The default value is FALSE.
subset	A numeric vector indicating the subset of the units whose in-sample predictions to be provided when units is TRUE. The default value is NULL where the in-sample predictions for each unit will be provided.
...	further arguments passed to or from other methods.

## Value

summary.eco yields an object of class summary.eco containing the following elements:

call	The call from eco.
n.obs	The number of units.
n.draws	The number of Monte Carlo samples.
agg.table	Aggregate posterior estimates of the marginal means of $W_1$ and $W_2$ using $X$ and $N$ as weights.

If param = TRUE, the following elements are also included:

**param.table** Posterior estimates of model parameters: population mean estimates of  $W_1$  and  $W_2$  and their logit transformations.

If **units** = TRUE, the following elements are also included:

**W1.table** Unit-level posterior estimates for  $W_1$ .

**W2.table** Unit-level posterior estimates for  $W_2$ .

This object can be printed by `print.summary.eco`

## See Also

`eco`, `predict.eco`

**summary.ecoML** *Summarizing the Results for the Maximum Likelihood Parametric Model for Ecological Inference in 2x2 Tables*

## Description

summary method for class `eco`.

## Usage

```
## S3 method for class 'ecoML'
summary(
  object,
  CI = c(2.5, 97.5),
  param = TRUE,
  units = FALSE,
  subset = NULL,
  ...
)
```

## Arguments

<b>object</b>	An output object from <code>eco</code> .
<b>CI</b>	A vector of lower and upper bounds for the Bayesian credible intervals used to summarize the results. The default is the equal tail 95 percent credible interval.
<b>param</b>	Ignored.
<b>units</b>	Logical. If TRUE, the in-sample predictions for each unit or for a subset of units will be provided. The default value is FALSE.
<b>subset</b>	A numeric vector indicating the subset of the units whose in-sample predictions to be provided when <b>units</b> is TRUE. The default value is NULL where the in-sample predictions for each unit will be provided.
<b>...</b>	further arguments passed to or from other methods.

**Value**

`summary.eco` yields an object of class `summary.eco` containing the following elements:

<code>call</code>	The call from <code>eco</code> .
<code>sem</code>	Whether the SEM algorithm was executed, as specified by the user upon calling <code>ecoML</code> .
<code>fix.rho</code>	Whether the correlation parameter was fixed or allowed to vary, as specified by the user upon calling <code>ecoML</code> .
<code>epsilon</code>	The convergence threshold specified by the user upon calling <code>ecoML</code> .
<code>n.obs</code>	The number of units.
<code>iters.em</code>	The number iterations the EM algorithm cycled through before convergence or reaching the maximum number of iterations allowed.
<code>iters.sem</code>	The number iterations the SEM algorithm cycled through before convergence or reaching the maximum number of iterations allowed.
<code>loglik</code>	The final observed log-likelihood.
<code>rho</code>	A matrix of <code>iters.em</code> rows specifying the correlation parameters at each iteration of the EM algorithm. The number of columns depends on how many correlation parameters exist in the model. Column order is the same as the order of the parameters in <code>param.table</code> .
<code>param.table</code>	Final estimates of the parameter values for the model. Excludes parameters fixed by the user upon calling <code>ecoML</code> . See <code>ecoML</code> documentation for order of parameters.
<code>agg.table</code>	Aggregate estimates of the marginal means of $W_1$ and $W_2$
<code>agg.wtable</code>	Aggregate estimates of the marginal means of $W_1$ and $W_2$ using $X$ and $N$ as weights.

If `units = TRUE`, the following elements are also included:

<code>W.table</code>	Unit-level estimates for $W_1$ and $W_2$ .
----------------------	--

This object can be printed by `print.summary.eco`

**See Also**

`ecoML`

`summary.ecoNP`

*Summarizing the Results for the Bayesian Nonparametric Model for Ecological Inference in 2x2 Tables*

**Description**

summary method for class `ecoNP`.

## Usage

```
## S3 method for class 'ecoNP'
summary(
  object,
  CI = c(2.5, 97.5),
  param = FALSE,
  units = FALSE,
  subset = NULL,
  ...
)
```

## Arguments

object	An output object from ecoNP.
CI	A vector of lower and upper bounds for the Bayesian credible intervals used to summarize the results. The default is the equal tail 95 percent credible interval.
param	Logical. If TRUE, the posterior estimates of the population parameters will be provided. The default value is FALSE.
units	Logical. If TRUE, the in-sample predictions for each unit or for a subset of units will be provided. The default value is FALSE.
subset	A numeric vector indicating the subset of the units whose in-sample predictions to be provided when units is TRUE. The default value is NULL where the in-sample predictions for each unit will be provided.
...	further arguments passed to or from other methods.

## Value

summary.ecoNP yields an object of class summary.ecoNP containing the following elements:

call	The call from ecoNP.
n.obs	The number of units.
n.draws	The number of Monte Carlo samples.
agg.table	Aggregate posterior estimates of the marginal means of $W_1$ and $W_2$ using $X$ and $N$ as weights.

If param = TRUE, the following elements are also included:

param.table	Posterior estimates of model parameters: population mean estimates of $W_1$ and $W_2$ . If subset is specified, only a subset of the population parameters are included.
-------------	--

If unit = TRUE, the following elements are also included:

W1.table	Unit-level posterior estimates for $W_1$ .
W2.table	Unit-level posterior estimates for $W_2$ .

This object can be printed by print.summary.ecoNP

**See Also**

`ecoNP`, `predict.eco`

`varcov`

*Calculate the variance or covariance of the object*

**Description**

`varcov` returns the variance or covariance of the object.

**Usage**

`varcov(object, ...)`

**Arguments**

<code>object</code>	An object
<code>...</code>	The rest of the input parameters if any

**Value**

a variance-covariance matrix

`wallace`

*Black voting rates for Wallace for President, 1968*

**Description**

This data set contains, on a county level, the proportion of county residents who are Black and the proportion of presidential votes cast for Wallace. Demographic data is based on the 1960 census. Presidential returns are from ICPSR study 13. County data from 10 southern states (Alabama, Arkansas, Georgia, Florida, Louisiana, Mississippi, North Carolina, South Carolina, Tennessee, Texas) are included. (Virginia is excluded due to the difficulty of matching counties between the datasets.) This data is analyzed in Wallace and Segal (1973).

**Format**

A data frame containing 3 variables and 1009 observations

<code>X</code>	numeric	proportion of the population that is Black
<code>Y</code>	numeric	proportion presidential votes cast for Wallace
<code>FIPS</code>	numeric	the FIPS county code

**References**

Wasserman, Ira M. and David R. Segal (1973). "Aggregation Effects in the Ecological Study of Presidential Voting." *American Journal of Political Science*. vol. 17, pp. 177-81.

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