# Package 'RTMBdist'

October 7, 2025

Type Package

**Title** Distributions Compatible with Automatic Differentiation by 'RTMB'

Version 0.1.0

#### **Description**

Extends the functionality of the 'RTMB' <a href="https://kaskr.r-universe.dev/RTMB">https://kaskr.r-universe.dev/RTMB</a> package by providing a collection of non-standard probability distributions compatible with automatic differentiation (AD). While 'RTMB' enables flexible and efficient modelling, including random effects, its built-in support is limited to standard distributions. The package adds additional AD-compatible distributions, broadening the range of models that can be implemented and estimated using 'RTMB'. Automatic differentiation and Laplace approximation are described in Kristensen et al. (2016) <a href="https://doi.org/10.18637/jss.v070.i05">doi:10.18637/jss.v070.i05</a>.

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**Encoding UTF-8** 

Imports stats, gamlss.dist, circular, sn, statmod, movMF

**Depends** R (>= 3.5.0), RTMB (>= 1.7.0)

RoxygenNote 7.3.2

**Suggests** knitr, rmarkdown, testthat (>= 3.0.0), LaMa (>= 2.0.6), Matrix, TMB, gamlss.data, mvtnorm

Config/testthat/edition 3

URL https://janoleko.github.io/RTMBdist/

VignetteBuilder knitr

NeedsCompilation no

**Author** Jan-Ole Koslik [aut, cre] (ORCID:

<https://orcid.org/0009-0004-1556-9053>)

Maintainer Jan-Ole Koslik < jan-ole.koslik@uni-bielefeld.de>

Repository CRAN

**Date/Publication** 2025-10-07 18:30:15 UTC

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bccg

Box-Cox Cole and Green distribution (BCCG)

# Description

Density, distribution function, quantile function, and random generation for the Box–Cox Cole and Green distribution.

# Usage

```
dbccg(x, mu = 1, sigma = 0.1, nu = 1, log = FALSE)
pbccg(q, mu = 1, sigma = 0.1, nu = 1, lower.tail = TRUE, log.p = FALSE)
qbccg(p, mu = 1, sigma = 0.1, nu = 1, lower.tail = TRUE, log.p = FALSE)
rbccg(n, mu = 1, sigma = 0.1, nu = 1)
```

# Arguments

x, q	vector of quantiles
mu	location parameter, must be positive.
sigma	scale parameter, must be positive.
nu	skewness parameter (real).
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x],$ otherwise $P[X > x].$
p	vector of probabilities
n	number of random values to return

#### **Details**

This implementation of dbccg and pbccg allows for automatic differentiation with RTMB while the other functions are imported from gamlss.dist package. See gamlss.dist::BCCG for more details.

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#### Value

dbccg gives the density, pbccg gives the distribution function, qbccg gives the quantile function, and rbccg generates random deviates.

#### References

Rigby, R. A., Stasinopoulos, D. M., Heller, G. Z., and De Bastiani, F. (2019) Distributions for modeling location, scale, and shape: Using GAMLSS in R, Chapman and Hall/CRC, doi:10.1201/9780429298547. An older version can be found in https://www.gamlss.com/.

# **Examples**

```
x <- rbccg(5, mu = 10, sigma = 0.2, nu = 0.5)
d <- dbccg(x, mu = 10, sigma = 0.2, nu = 0.5)
p <- pbccg(x, mu = 10, sigma = 0.2, nu = 0.5)
q <- qbccg(p, mu = 10, sigma = 0.2, nu = 0.5)</pre>
```

bcpe

Box-Cox Power Exponential distribution (BCPE)

# Description

Density, distribution function, quantile function, and random generation for the Box-Cox Power Exponential distribution.

### Usage

```
dbcpe(x, mu = 5, sigma = 0.1, nu = 1, tau = 2, log = FALSE)
pbcpe(q, mu = 5, sigma = 0.1, nu = 1, tau = 2, lower.tail = TRUE, log.p = FALSE)
qbcpe(p, mu = 5, sigma = 0.1, nu = 1, tau = 2, lower.tail = TRUE, log.p = FALSE)
rbcpe(n, mu = 5, sigma = 0.1, nu = 1, tau = 2)
```

# **Arguments**

x, q	vector of quantiles
mu	location parameter, must be positive.
sigma	scale parameter, must be positive.
nu	vector of nu parameter values.
tau	vector of tau parameter values, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x],$ otherwise $P[X > x].$
р	vector of probabilities
n	number of random values to return

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#### **Details**

This implementation of dbcpe and pbcpe allows for automatic differentiation with RTMB while the other functions are imported from gamlss.dist package. See gamlss.dist::BCPE for more details.

#### Value

dbcpe gives the density, pbcpe gives the distribution function, qbcpe gives the quantile function, and rbcpe generates random deviates.

#### References

Rigby, R. A., Stasinopoulos, D. M., Heller, G. Z., and De Bastiani, F. (2019) Distributions for modeling location, scale, and shape: Using GAMLSS in R, Chapman and Hall/CRC, doi:10.1201/9780429298547. An older version can be found in https://www.gamlss.com/.

### **Examples**

```
x <- rbcpe(1, mu = 5, sigma = 0.1, nu = 1, tau = 1)
d <- dbcpe(x, mu = 5, sigma = 0.1, nu = 1, tau = 1)
p <- pbcpe(x, mu = 5, sigma = 0.1, nu = 1, tau = 1)
q <- qbcpe(p, mu = 5, sigma = 0.1, nu = 1, tau = 1)</pre>
```

bct

Box-Cox t distribution (BCT)

### Description

Density, distribution function, quantile function, and random generation for the Box-Cox t distribution.

# Usage

```
dbct(x, mu = 5, sigma = 0.1, nu = 1, tau = 2, log = FALSE)

pbct(q, mu = 5, sigma = 0.1, nu = 1, tau = 2, lower.tail = TRUE, log.p = FALSE)

qbct(p, mu = 5, sigma = 0.1, nu = 1, tau = 2, lower.tail = TRUE, log.p = FALSE)

rbct(n, mu = 5, sigma = 0.1, nu = 1, tau = 2)
```

### Arguments

```
x, q vector of quantiles
mu location parameter, must be positive.
sigma scale parameter, must be positive.
nu skewness parameter (real).
```

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```
tau degrees of freedom, must be positive.  
\log \log p \qquad \log(x) \qquad \log(x)
```

#### **Details**

This implementation of dbct and pbct allows for automatic differentiation with RTMB while the other functions are imported from gamlss.dist package. See gamlss.dist::BCT for more details.

#### Value

dbct gives the density, pbct gives the distribution function, qbct gives the quantile function, and rbct generates random deviates.

#### References

Rigby, R. A., Stasinopoulos, D. M., Heller, G. Z., and De Bastiani, F. (2019) Distributions for modeling location, scale, and shape: Using GAMLSS in R, Chapman and Hall/CRC, doi:10.1201/9780429298547. An older version can be found in https://www.gamlss.com/.

# **Examples**

```
x <- rbct(1, mu = 10, sigma = 0.2, nu = 0.5, tau = 4)
d <- dbct(x, mu = 10, sigma = 0.2, nu = 0.5, tau = 4)
p <- pbct(x, mu = 10, sigma = 0.2, nu = 0.5, tau = 4)
q <- qbct(p, mu = 10, sigma = 0.2, nu = 0.5, tau = 4)</pre>
```

beta2

Reparameterised beta distribution

# Description

Density, distribution function, quantile function, and random generation for the beta distribution reparameterised in terms of mean and concentration.

```
dbeta(x, shape1, shape2, log = FALSE, eps = 0)
dbeta2(x, mu, phi, log = FALSE, eps = 0)
pbeta2(q, mu, phi, lower.tail = TRUE, log.p = FALSE)
qbeta2(p, mu, phi, lower.tail = TRUE, log.p = FALSE)
rbeta2(n, mu, phi)
```

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# **Arguments**

x, q	vector of quantiles
shape1, shape2	non-negative parameters
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
eps	for internal use only, don't change.
mu	mean parameter, must be in the interval from 0 to 1.
phi	concentration parameter, must be positive.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x],$ otherwise $P[X > x].$
p	vector of probabilities
n	number of random values to return.

# **Details**

This implementation allows for automatic differentiation with RTMB.

Currently, dbeta masks RTMB:: dbeta because the latter has a numerically unstable gradient.

# Value

dbeta2 gives the density, pbeta2 gives the distribution function, qbeta2 gives the quantile function, and rbeta2 generates random deviates.

# **Examples**

```
set.seed(123)
x <- rbeta2(1, 0.5, 1)
d <- dbeta2(x, 0.5, 1)
p <- pbeta2(x, 0.5, 1)
q <- qbeta2(p, 0.5, 1)</pre>
```

betabinom

Beta-binomial distribution

# **Description**

Density and random generation for the beta-binomial distribution.

```
dbetabinom(x, size, shape1, shape2, log = FALSE)
rbetabinom(n, size, shape1, shape2)
```

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### **Arguments**

X	vector of non-negative counts.
size	vector of total counts (number of trials). Needs to be $>= x$ .
shape1	positive shape parameter 1 of the Beta prior.
shape2	positive shape parameter 2 of the Beta prior.
log	logical; if TRUE, densities are returned on the log scale.
n	number of random values to return (for rbetabinom).

#### **Details**

This implementation of dbetabinom allows for automatic differentiation with RTMB.

#### Value

dbetabinom gives the density and rbetabinom generates random samples.

# **Examples**

```
set.seed(123)
x <- rbetabinom(1, 10, 2, 5)
d <- dbetabinom(x, 10, 2, 5)</pre>
```

cclayton

Clayton copula constructor

# **Description**

Returns a function that computes the log density of the bivariate Clayton copula, intended to be used with dcopula.

# Usage

```
cclayton(theta)
```

# Arguments

theta

Positive dependence parameter ( $\theta > 0$ ).

# **Details**

The Clayton copula density is

$$c(u, v; \theta) = (1 + \theta)(uv)^{-(1+\theta)} (u^{-\theta} + v^{-\theta} - 1)^{-(2\theta+1)/\theta}, \quad \theta > 0.$$

# Value

A function of two arguments (u,v) returning log copula density.

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#### See Also

```
cgaussian(), cgumbel(), cfrank()
```

#### **Examples**

```
x \leftarrow c(0.5, 1); y \leftarrow c(0.2, 0.8)

d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dbeta(y, 2, 1, log = TRUE)

p1 \leftarrow pnorm(x, 1); p2 \leftarrow pbeta(y, 2, 1)

dcopula(d1, d2, p1, p2, copula = cclayton(2), log = TRUE)
```

cfrank

Frank copula constructor

# **Description**

Returns a function computing the log density of the bivariate Frank copula, intended to be used with dcopula.

# Usage

```
cfrank(theta)
```

#### **Arguments**

theta

Dependence parameter ( $\theta = 0$ ).

### **Details**

The Frank copula density is

$$c(u, v; \theta) = \frac{\theta(1 - e^{-\theta})e^{-\theta(u+v)}}{\left[(e^{-\theta u} - 1)(e^{-\theta v} - 1) + (1 - e^{-\theta})\right]^2}, \quad \theta \neq 0.$$

# Value

Function of two arguments (u,v) returning log copula density.

#### See Also

```
cgaussian(), cclayton(), cgumbel()
```

```
x \leftarrow c(0.5, 1); y \leftarrow c(1, 2)

d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dexp(y, 2, log = TRUE)

p1 \leftarrow pnorm(x, 1); p2 \leftarrow pexp(y, 2)

dcopula(d1, d2, p1, p2, copula = cfrank(2), log = TRUE)
```

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cgaussian

Gaussian copula constructor

# Description

Returns a function computing the log density of the bivariate Gaussian copula, intended to be used with dcopula.

# Usage

```
cgaussian(rho = 0)
```

# **Arguments**

rho

Correlation parameter (-1 < rho < 1).

#### Value

Function of two arguments (u,v) returning log copula density.

The Gaussian copula density is

$$c(u, v; \rho) = \frac{1}{\sqrt{1 - \rho^2}} \exp\left\{-\frac{1}{2(1 - \rho^2)}(z_1^2 - 2\rho z_1 z_2 + z_2^2) + \frac{1}{2}(z_1^2 + z_2^2)\right\},\,$$

where  $z_1 = \Phi^{-1}(u)$ ,  $z_2 = \Phi^{-1}(v)$ , and  $-1 < \rho < 1$ .

### See Also

```
cclayton(), cgumbel(), cfrank()
```

```
x \leftarrow c(0.5, 1); y \leftarrow c(1, 2)

d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dexp(y, 2, log = TRUE)

p1 \leftarrow pnorm(x, 1); p2 \leftarrow pexp(y, 2)

dcopula(d1, d2, p1, p2, copula = cgaussian(0.5), log = TRUE)
```

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cgumbel

Gumbel copula constructor

# **Description**

Returns a function that computes the log density of the bivariate Gumbel copula, intended to be used with dcopula.

# Usage

```
cgumbel(theta)
```

# **Arguments**

theta

Dependence parameter ( $\theta >= 1$ ).

#### **Details**

The Gumbel copula density

$$c(u, v; \theta) = \exp\left[-\left((-\log u)^{\theta} + (-\log v)^{\theta}\right)^{1/\theta}\right] \cdot h(u, v; \theta),$$

where  $h(u, v; \theta)$  contains the derivative terms ensuring the function is a density.

#### Value

A function of two arguments (u,v) returning log copula density.

#### See Also

```
cgaussian(), cclayton(), cfrank()
```

```
x \leftarrow c(0.5, 1); y \leftarrow c(0.2, 0.4)

d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dbeta(y, 2, 1, log = TRUE)

p1 \leftarrow pnorm(x, 1); p2 \leftarrow pbeta(y, 2, 1)

dcopula(d1, d2, p1, p2, copula = cgumbel(1.5), log = TRUE)
```

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Joint density under a bivariate copula

# Description

Computes the joint density (or log-density) of a bivariate distribution constructed from two arbitrary margins combined with a specified copula.

#### Usage

```
dcopula(d1, d2, p1, p2, copula = cgaussian(0), log = FALSE)
```

# Arguments

d1, d2	Marginal density values. If log = TRUE, supply the log-density. If log = FALSE, supply the raw density.
p1, p2	Marginal CDF values. Need not be supplied on log scale.
copula	A function of two arguments (u, v) returning the log copula density $\log c(u,v)$ . You can either construct this yourself or use the copula constructors available (see details)
log	Logical; if TRUE, return the log joint density. In this case, d1 and d2 must be on the log scale.

# **Details**

The joint density is

$$f(x,y) = c(F_1(x), F_2(y)) f_1(x) f_2(y),$$

where  $F_i$  are the marginal CDFs,  $f_i$  are the marginal densities, and c is the copula density.

The marginal densities d1, d2 and CDFs p1, p2 must be differentiable for automatic differentiation (AD) to work.

Available copula constructors are:

- cgaussian (Gaussian copula)
- cclayton (Clayton copula)
- cgumbel (Gumbel copula)
- cfrank (Frank copula)

#### Value

Joint density (or log-density) under the bivariate copula.

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#### **Examples**

```
# Normal + Exponential margins with Gaussian copula
x \leftarrow c(0.5, 1); y \leftarrow c(1, 2)
d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dexp(y, 2, log = TRUE)
p1 <- pnorm(x, 1); p2 <- pexp(y, 2)
dcopula(d1, d2, p1, p2, copula = cgaussian(0.5), log = TRUE)
# Normal + Beta margins with Clayton copula
x \leftarrow c(0.5, 1); y \leftarrow c(0.2, 0.8)
d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dbeta(y, 2, 1, log = TRUE)
p1 \leftarrow pnorm(x, 1); p2 \leftarrow pbeta(y, 2, 1)
dcopula(d1, d2, p1, p2, copula = cclayton(2), log = TRUE)
# Normal + Beta margins with Gumbel copula
x \leftarrow c(0.5, 1); y \leftarrow c(0.2, 0.4)
d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dbeta(y, 2, 1, log = TRUE)
p1 \leftarrow pnorm(x, 1); p2 \leftarrow pbeta(y, 2, 1)
dcopula(d1, d2, p1, p2, copula = cgumbel(1.5), log = TRUE)
# Normal + Exponential margins with Frank copula
x \leftarrow c(0.5, 1); y \leftarrow c(1, 2)
d1 \leftarrow dnorm(x, 1, log = TRUE); d2 \leftarrow dexp(y, 2, log = TRUE)
p1 \leftarrow pnorm(x, 1); p2 \leftarrow pexp(y, 2)
dcopula(d1, d2, p1, p2, copula = cfrank(2), log = TRUE)
```

dirichlet

Dirichlet distribution

#### **Description**

Density and and random generation for the Dirichlet distribution.

### Usage

```
ddirichlet(x, alpha, log = FALSE)
rdirichlet(n, alpha)
```

#### **Arguments**

X	vector or matrix of quantiles. If $x$ is a vector, it needs to sum to one. If $x$ is a matrix, each row should sum to one.
alpha	vector or matrix of positive shape parameters
log	logical; if TRUE, densities $p$ are returned as $\log(p)$ .
n	number of random values to return.

# **Details**

This implementation of ddirichlet allows for automatic differentiation with RTMB.

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# Value

ddirichlet gives the density, rdirichlet generates random deviates.

# **Examples**

```
# single alpha
alpha <- c(1,2,3)
x <- rdirichlet(1, alpha)
d <- ddirichlet(x, alpha)
# vectorised over alpha
alpha <- rbind(alpha, 2*alpha)
x <- rdirichlet(2, alpha)</pre>
```

dirmult

Dirichlet-multinomial distribution

# Description

Density and and random generation for the Dirichlet-multinomial distribution.

### Usage

```
ddirmult(x, size, alpha, log = FALSE)
rdirmult(n, size, alpha)
```

# Arguments

X	vector or matrix of non-negative counts, where rows are observations and columns are categories.
size	vector of total counts for each observation. Needs to match the row sums of x.
alpha	vector or matrix of positive shape parameters
log	logical; if TRUE, densities $p$ are returned as $\log(p)$ .
n	number of random values to return.

# **Details**

This implementation of ddirmult allows for automatic differentiation with RTMB.

#### Value

ddirmult gives the density and rdirmult generates random samples.

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# **Examples**

```
# single alpha
alpha <- c(1,2,3)
size <- 10
x <- rdirmult(1, size, alpha)
d <- ddirmult(x, size, alpha)
# vectorised over alpha and size
alpha <- rbind(alpha, 2*alpha)
size <- c(size, 3*size)
x <- rdirmult(2, size, alpha)</pre>
```

erf

AD-compatible error function and complementary error function

# Description

AD-compatible error function and complementary error function

# Usage

```
erf(x)
```

erfc(x)

# Arguments

Х

vector of evaluation points

### Value

erf(x) returns the error function and erfc(x) returns the complementary error function.

```
erf(1)
erfc(1)
```

16 exgauss

exgauss

Exponentially modified Gaussian distribution

#### **Description**

Density, distribution function, quantile function, and random generation for the exponentially modified Gaussian distribution.

# Usage

```
dexgauss(x, mu = 0, sigma = 1, lambda = 1, log = FALSE)
pexgauss(q, mu = 0, sigma = 1, lambda = 1, lower.tail = TRUE, log.p = FALSE)
qexgauss(p, mu = 0, sigma = 1, lambda = 1, lower.tail = TRUE, log.p = FALSE)
rexgauss(n, mu = 0, sigma = 1, lambda = 1)
```

# **Arguments**

x, q	vector of quantiles
mu	mean parameter of the Gaussian part
sigma	standard deviation parameter of the Gaussian part, must be positive.
lambda	rate parameter of the exponential part, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
р	vector of probabilities
n	number of random values to return

#### **Details**

This implementation of dexgauss and pexgauss allows for automatic differentiation with RTMB. qexgauss and rexgauss are reparameterised imports from gamlss.dist::exGAUS.

If  $X \sim N(\mu, \sigma^2)$  and  $Y \sim \operatorname{Exp}(\lambda)$ , then Z = X + Y follows the exponentially modified Gaussian distribution with parameters  $\mu$ ,  $\sigma$ , and  $\lambda$ .

### Value

dexgauss gives the density, pexgauss gives the distribution function, qexgauss gives the quantile function, and rexgauss generates random deviates.

#### References

Rigby, R. A., Stasinopoulos, D. M., Heller, G. Z., and De Bastiani, F. (2019) Distributions for modeling location, scale, and shape: Using GAMLSS in R, Chapman and Hall/CRC, doi:10.1201/9780429298547. An older version can be found in https://www.gamlss.com/.

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#### **Examples**

```
x <- rexgauss(1, 1, 2, 2)
d <- dexgauss(x, 1, 2, 2)
p <- pexgauss(x, 1, 2, 2)
q <- qexgauss(p, 1, 2, 2)</pre>
```

foldnorm

Folded normal distribution

# Description

Density, distribution function, and random generation for the folded normal distribution.

# Usage

```
dfoldnorm(x, mu = 0, sigma = 1, log = FALSE)
pfoldnorm(q, mu = 0, sigma = 1, lower.tail = TRUE, log.p = FALSE)
rfoldnorm(n, mu = 0, sigma = 1)
```

# Arguments

x, q	vector of quantiles
mu	location parameter
sigma	scale parameter, must be positive.
log,log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x],$ otherwise, $P[X > x].$
n	number of random values to return
р	vector of probabilities

#### **Details**

This implementation of dfoldnorm allows for automatic differentiation with RTMB.

#### Value

dfoldnorm gives the density, pfoldnorm gives the distribution function, and rfoldnorm generates random deviates.

```
x <- rfoldnorm(1, 1, 2)
d <- dfoldnorm(x, 1, 2)
p <- pfoldnorm(x, 1, 2)</pre>
```

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gamma2

Reparameterised gamma distribution

# Description

Density, distribution function, quantile function, and random generation for the gamma distribution reparameterised in terms of mean and standard deviation.

### Usage

```
dgamma2(x, mean = 1, sd = 1, log = FALSE)
pgamma2(q, mean = 1, sd = 1, lower.tail = TRUE, log.p = FALSE)
qgamma2(p, mean = 1, sd = 1, lower.tail = TRUE, log.p = FALSE)
rgamma2(n, mean = 1, sd = 1)
```

# Arguments

x, q	vector of quantiles
mean	mean parameter, must be positive.
sd	standard deviation parameter, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
p	vector of probabilities
n	number of random values to return.

### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dgamma2 gives the density, pgamma2 gives the distribution function, qgamma2 gives the quantile function, and rgamma2 generates random deviates.

```
x <- rgamma2(1)
d <- dgamma2(x)
p <- pgamma2(x)
q <- qgamma2(p)</pre>
```

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Generalised Poisson distribution

# **Description**

Probability mass function, distribution function, and random generation for the generalised Poisson distribution.

# Usage

# **Arguments**

x, q	integer vector of counts
lambda	vector of positive means
phi	vector of non-negative dispersion parameters
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
p	vector of probabilities
max.value	a constant, set to the default value of $10000$ for how far the algorithm should look for ${\bf q}$ .
n	number of random values to return.

#### **Details**

This implementation of dgenpois allows for automatic differentiation with RTMB. The other functions are imported from gamlss.dist::GPO.

The distribution has mean  $\lambda$  and variance  $\lambda(1+\phi\lambda)^2$ . For  $\phi=0$  it reduces to the Poisson distribution, however  $\phi$  must be strictly positive here.

#### Value

dgenpois gives the probability mass function, pgenpois gives the distribution function, qgenpois gives the quantile function, and rgenpois generates random deviates.

20 gumbel

### **Examples**

```
set.seed(123)
x <- rgenpois(1, 2, 3)
d <- dgenpois(x, 2, 3)
p <- pgenpois(x, 2, 3)
q <- qgenpois(p, 2, 3)</pre>
```

gumbel

Gumbel distribution

# **Description**

Density, distribution function, quantile function, and random generation for the Gumbel distribution.

# Usage

```
dgumbel(x, location = 0, scale = 1, log = FALSE)
pgumbel(q, location = 0, scale = 1, lower.tail = TRUE, log.p = FALSE)
qgumbel(p, location = 0, scale = 1, lower.tail = TRUE, log.p = FALSE)
rgumbel(n, location = 0, scale = 1)
```

### **Arguments**

x, q	vector of quantiles
location	location parameter
scale	scale parameter, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
р	vector of probabilities
n	number of random values to return

#### **Details**

This implementation of dgumbel allows for automatic differentiation with RTMB.

### Value

dgumbel gives the density, pgumbel gives the distribution function, qgumbel gives the quantile function, and rgumbel generates random deviates.

invgauss 21

# **Examples**

```
x <- rgumbel(1, 0.5, 2)
d <- dgumbel(x, 0.5, 2)
p <- pgumbel(x, 0.5, 2)
q <- qgumbel(p, 0.5, 2)</pre>
```

invgauss

Inverse Gaussian distribution

# Description

Density, distribution function, and random generation for the inverse Gaussian distribution.

# Usage

```
dinvgauss(x, mean = 1, shape = 1, log = FALSE)
pinvgauss(q, mean = 1, shape = 1, lower.tail = TRUE, log.p = FALSE)
qinvgauss(p, mean = 1, shape = 1, lower.tail = TRUE, log.p = FALSE, ...)
rinvgauss(n, mean = 1, shape = 1)
```

#### **Arguments**

x, q	vector of quantiles, must be positive.
mean	location parameter
shape	shape parameter, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
p	vector of probabilities
•••	additional parameter passed to $\mathtt{statmod}: \mathtt{qinvgauss}$ for numerical evaluation of the quantile function.
n	number of random values to return

# **Details**

This implementation of dinvgauss allows for automatic differentiation with RTMB. qinvgauss and rinvgauss are imported from the statmod package.

### Value

dinvgauss gives the density, pinvgauss gives the distribution function, qinvgauss gives the quantile function, and rinvgauss generates random deviates.

22 laplace

### **Examples**

```
x <- rinvgauss(1, 1, 0.5)
d <- dinvgauss(x, 1, 0.5)
p <- pinvgauss(x, 1, 0.5)
q <- qinvgauss(p, 1, 0.5)</pre>
```

laplace

Laplace distribution

### **Description**

Density, distribution function, quantile function, and random generation for the Laplace distribution.

### Usage

```
dlaplace(x, mu = 0, b = 1, log = FALSE)
plaplace(q, mu = 0, b = 1, lower.tail = TRUE, log.p = FALSE)
qlaplace(p, mu = 0, b = 1, lower.tail = TRUE, log.p = FALSE)
rlaplace(n, mu = 0, b = 1)
```

### **Arguments**

```
x, q vector of quantiles mu location parameter b scale parameter, must be positive.  
log, log.p logical; if TRUE, probabilities p are returned as \log(p).  
lower.tail logical; if TRUE, probabilities are P[X \leq x], otherwise, P[X > x].  
p vector of probabilities  
n number of random values to return
```

#### **Details**

This implementation of dlaplace allows for automatic differentiation with RTMB.

### Value

dlaplace gives the density, plaplace gives the distribution function, qlaplace gives the quantile function, and rlaplace generates random deviates.

```
x <- rlaplace(1, 1, 1)
d <- dlaplace(x, 1, 1)
p <- plaplace(x, 1, 1)
q <- qlaplace(p, 1, 1)</pre>
```

mvt 23

mvt

Multivariate t distribution

# Description

Density and and random generation for the multivariate t distribution

# Usage

```
dmvt(x, mu, Sigma, df, log = FALSE)
rmvt(n, mu, Sigma, df)
```

# **Arguments**

X	vector or matrix of quantiles
mu	vector or matrix of location parameters (mean if $df > 1$ )
Sigma	positive definite scale matrix (proportional to the covariance matrix if $df > 2$ )
df	degrees of freedom; must be positive
log	logical; if TRUE, densities $p$ are returned as $\log(p)$ .
n	number of random values to return.

#### **Details**

This implementation of dmvt allows for automatic differentiation with RTMB.

Note: for df  $\leq 1$  the mean is undefined, and for df  $\leq 2$  the covariance is infinite. For df > 2, the covariance is df/(df-2) \* Sigma.

# Value

dmvt gives the density, rmvt generates random deviates.

```
# single mu
mu <- c(1,2,3)
Sigma <- diag(c(1,1,1))
df <- 5
x <- rmvt(2, mu, Sigma, df)
d <- dmvt(x, mu, Sigma, df)
# vectorised over mu
mu <- rbind(c(1,2,3), c(0, 0.5, 1))
x <- rmvt(2, mu, Sigma, df)
d <- dmvt(x, mu, Sigma, df)</pre>
```

24 nbinom2

nbinom2

Reparameterised negative binomial distribution

# Description

Probability mass function, distribution function, quantile function, and random generation for the negative binomial distribution reparameterised in terms of mean and size.

# Usage

```
dnbinom2(x, mu, size, log = FALSE)
pnbinom2(q, mu, size, lower.tail = TRUE, log.p = FALSE)
qnbinom2(p, mu, size, lower.tail = TRUE, log.p = FALSE)
rnbinom2(n, mu, size)
pnbinom(q, size, prob, lower.tail = TRUE, log.p = FALSE)
```

# Arguments

x, q	vector of quantiles
mu	mean parameter, must be positive.
size	size parameter, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x],$ otherwise, $P[X > x].$
p	vector of probabilities
n	number of random values to return.
prob	probability of success in each trial. $0 < \text{prob} \le 1$ .

#### **Details**

This implementation allows for automatic differentiation with RTMB.

pnbinom is an AD-compatible implementation of the standard parameterisation of the CDF, missing from RTMB.

#### Value

dnbinom2 gives the density, pnbinom2 gives the distribution function, qnbinom2 gives the quantile function, and rnbinom2 generates random deviates.

oibeta 25

### **Examples**

```
set.seed(123)
x <- rnbinom2(1, 1, 2)
d <- dnbinom2(x, 1, 2)
p <- pnbinom2(x, 1, 2)
q <- qnbinom2(p, 1, 2)</pre>
```

oibeta

One-inflated beta distribution

#### **Description**

Density, distribution function, and random generation for the one-inflated beta distribution.

#### Usage

```
doibeta(x, shape1, shape2, oneprob = 0, log = FALSE)
poibeta(q, shape1, shape2, oneprob = 0, lower.tail = TRUE, log.p = FALSE)
roibeta(n, shape1, shape2, oneprob = 0)
```

#### **Arguments**

```
x, q vector of quantiles shape 1, shape 2 non-negative shape parameters of the beta distribution one prob zero-inflation probability between 0 and 1.  
\log_{p} \log_
```

### **Details**

This implementation allows for automatic differentiation with RTMB.

#### Value

doibeta gives the density, poibeta gives the distribution function, and roibeta generates random deviates.

```
set.seed(123)
x <- roibeta(1, 2, 2, 0.5)
d <- doibeta(x, 2, 2, 0.5)
p <- poibeta(x, 2, 2, 0.5)</pre>
```

26 oibeta2

oibeta2

Reparameterised one-inflated beta distribution

# **Description**

Density, distribution function, and random generation for the one-inflated beta distribution reparameterised in terms of mean and concentration.

# Usage

```
doibeta2(x, mu, phi, oneprob = 0, log = FALSE)
poibeta2(q, mu, phi, oneprob = 0, lower.tail = TRUE, log.p = FALSE)
roibeta2(n, mu, phi, oneprob = 0)
```

# **Arguments**

x, q	vector of quantiles
mu	mean parameter, must be in the interval from 0 to 1.
phi	concentration parameter, must be positive.
oneprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x],$ otherwise, $P[X > x].$
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

doibeta2 gives the density, poibeta2 gives the distribution function, and roibeta2 generates random deviates.

```
set.seed(123)
x <- roibeta2(1, 0.6, 2, 0.5)
d <- doibeta2(x, 0.6, 2, 0.5)
p <- poibeta2(x, 0.6, 2, 0.5)</pre>
```

pareto 27

# Description

Density, distribution function, quantile function, and random generation for the pareto distribution.

#### Usage

```
dpareto(x, mu = 1, log = FALSE)

ppareto(q, mu = 1, lower.tail = TRUE, log.p = FALSE)

qpareto(p, mu = 1, lower.tail = TRUE, log.p = FALSE)

rpareto(n, mu = 1)
```

### Arguments

x, q	vector of quantiles
mu	location parameter, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise $P[X > x]$ .
р	vector of probabilities
n	number of random values to return

### **Details**

This implementation of dpareto and ppareto allows for automatic differentiation with RTMB while the other functions are imported from gamlss.dist package. See gamlss.dist::PARETO for more details.

#### Value

dpareto gives the density, ppareto gives the distribution function, apareto gives the quantile function, and rpareto generates random deviates.

#### References

Rigby, R. A., Stasinopoulos, D. M., Heller, G. Z., and De Bastiani, F. (2019) Distributions for modeling location, scale, and shape: Using GAMLSS in R, Chapman and Hall/CRC, doi:10.1201/9780429298547. An older version can be found in https://www.gamlss.com/.

28 powerexp

#### **Examples**

```
set.seed(123)
x <- rpareto(1, mu = 5)
d <- dpareto(x, mu = 5)
p <- ppareto(x, mu = 5)
q <- qpareto(p, mu = 5)</pre>
```

powerexp

*Power Exponential distribution (PE and PE2)* 

# **Description**

Density, distribution function, quantile function, and random generation for the Power Exponential distribution (two versions).

# Usage

```
dpowerexp(x, mu = 0, sigma = 1, nu = 2, log = FALSE)

ppowerexp(q, mu = 0, sigma = 1, nu = 2, lower.tail = TRUE, log.p = FALSE)

qpowerexp(p, mu = 0, sigma = 1, nu = 2, lower.tail = TRUE, log.p = FALSE)

rpowerexp(n, mu = 0, sigma = 1, nu = 2)

dpowerexp2(x, mu = 0, sigma = 1, nu = 2, log = FALSE)

ppowerexp2(q, mu = 0, sigma = 1, nu = 2, lower.tail = TRUE, log.p = FALSE)

qpowerexp2(p, mu = 0, sigma = 1, nu = 2, lower.tail = TRUE, log.p = FALSE)

rpowerexp2(n, mu = 0, sigma = 1, nu = 2, lower.tail = TRUE, log.p = FALSE)
```

#### **Arguments**

```
vector of quantiles
x, q
                   location parameter
mu
sigma
                   scale parameter, must be positive
nu
                   shape parameter (real)
                   logical; if TRUE, probabilities/ densities p are returned as log(p)
log, log.p
                   logical; if TRUE (default), probabilities are P[X \le x], otherwise P[X > x]
lower.tail
                   vector of probabilities
р
                   number of random values to return
n
```

skewnorm 29

#### **Details**

This implementation of the densities and distribution functions allow for automatic differentiation with RTMB while the other functions are imported from gamlss.dist package.

For powerexp, mu is the mean and sigma is the standard deviation while this does not hold for powerexp2.

See gamlss.dist::PE for more details.

#### Value

dpowerexp gives the density, ppowerexp gives the distribution function, qpowerexp gives the quantile function, and rpowerexp generates random deviates.

#### References

Rigby, R. A., Stasinopoulos, D. M., Heller, G. Z., and De Bastiani, F. (2019) Distributions for modeling location, scale, and shape: Using GAMLSS in R, Chapman and Hall/CRC, doi:10.1201/9780429298547. An older version can be found in https://www.gamlss.com/.

### **Examples**

```
# PE
x <- rpowerexp(1, mu = 0, sigma = 1, nu = 2)
d <- dpowerexp(x, mu = 0, sigma = 1, nu = 2)
p <- ppowerexp(x, mu = 0, sigma = 1, nu = 2)
q <- dpowerexp(p, mu = 0, sigma = 1, nu = 2)
# PE2
x <- rpowerexp2(1, mu = 0, sigma = 1, nu = 2)
d <- dpowerexp2(x, mu = 0, sigma = 1, nu = 2)
p <- ppowerexp2(x, mu = 0, sigma = 1, nu = 2)
q <- dpowerexp2(p, mu = 0, sigma = 1, nu = 2)</pre>
```

skewnorm

Skew normal distribution

#### **Description**

Density, distribution function, quantile function, and random generation for the skew normal distribution.

```
dskewnorm(x, xi = 0, omega = 1, alpha = 0, log = FALSE)
pskewnorm(q, xi = 0, omega = 1, alpha = 0, ...)
qskewnorm(p, xi = 0, omega = 1, alpha = 0, ...)
rskewnorm(n, xi = 0, omega = 1, alpha = 0)
```

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#### **Arguments**

x, q	vector of quantiles
xi	location parameter
omega	scale parameter, must be positive.
alpha	skewness parameter, +/- Inf is allowed.
log	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
•••	additional parameters to be passed to the sn package functions for pskewnorm and qskewnorm.
р	vector of probabilities
n	number of random values to return

# **Details**

This implementation of dskewnorm allows for automatic differentiation with RTMB while the other functions are imported from the sn package. See sn::dsn for more details.

#### Value

dskewnorm gives the density, pskewnorm gives the distribution function, qskewnorm gives the quantile function, and rskewnorm generates random deviates.

# Examples

```
# alpha is skew parameter
x <- rskewnorm(1, alpha = 1)
d <- dskewnorm(x, alpha = 1)
p <- pskewnorm(x, alpha = 1)
q <- qskewnorm(p, alpha = 1)</pre>
```

skewnorm2

Reparameterised skew normal distribution

# Description

Density, distribution function, quantile function and random generation for the skew normal distribution reparameterised in terms of mean, standard deviation and skew magnitude

```
dskewnorm2(x, mean = 0, sd = 1, alpha = 0, log = FALSE)

pskewnorm2(q, mean = 0, sd = 1, alpha = 0, ...)

qskewnorm2(p, mean = 0, sd = 1, alpha = 0, ...)

rskewnorm2(n, mean = 0, sd = 1, alpha = 0)
```

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### Arguments

x, q	vector of quantiles
mean	mean parameter
sd	standard deviation, must be positive.
alpha	skewness parameter, +/- Inf is allowed.
log	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
•••	additional parameters to be passed to the sn package functions for pskewnorm and qskewnorm.
р	vector of probabilities
n	number of random values to return

#### **Details**

This implementation of dskewnorm2 allows for automatic differentiation with RTMB while the other functions are imported from the sn package.

#### Value

dskewnorm2 gives the density, pskewnorm2 gives the distribution function, qskewnorm2 gives the quantile function, and rskewnorm2 generates random deviates.

# Examples

```
# alpha is skew parameter
x <- rskewnorm2(1, alpha = 1)
d <- dskewnorm2(x, alpha = 1)
p <- pskewnorm2(x, alpha = 1)
q <- qskewnorm2(p, alpha = 1)</pre>
```

skewt

Skewed students t distribution

# Description

Density, distribution function, quantile function, and random generation for the skew t distribution (type 2).

32 skewt

# **Arguments**

x, q	vector of quantiles
mu	location parameter
sigma	scale parameter, must be positive.
skew	skewness parameter, can be positive or negative.
df	degrees of freedom, must be positive.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
method	an integer value between 0 and 5 which selects the computing method; see 'Details' in the pst documentation below for the meaning of these values. If method=0 (default value), an automatic choice is made among the four actual computing methods, depending on the other arguments.
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
р	vector of probabilities
tol	a scalar value which regulates the accuracy of the result of qsn, measured on the probability scale.
n	number of random values to return.

#### **Details**

This corresponds to the skew t type 2 distribution in GAMLSS (ST2), see pp. 411-412 of Rigby et al. (2019) and the version implemented in the sn package. This implementation of dskewt allows for automatic differentiation with RTMB while the other functions are imported from the sn package. See sn::dst for more details.

**Caution:** In a numerial optimisation, the skew parameter should NEVER be initialised with exactly zero. This will cause the initial and all subsequent derivatives to be exactly zero and hence the parameter will remain at its initial value.

### Value

dskewt gives the density, pskewt gives the distribution function, qskewt gives the quantile function, and rskewt generates random deviates.

```
x <- rskewt(1, 1, 2, 5, 2)
d <- dskewt(x, 1, 2, 5, 2)
p <- pskewt(x, 1, 2, 5, 2)
q <- qskewt(p, 1, 2, 5, 2)
```

Student t distribution with location and scale

t2

# Description

Density, distribution function, quantile function, and random generation for the t distribution with location and scale parameters.

# Usage

```
dt2(x, mu, sigma, df, log = FALSE)
pt2(q, mu, sigma, df)
rt2(n, mu, sigma, df)
qt2(p, mu, sigma, df)
pt(q, df)
```

# Arguments

x, q	vector of quantiles
mu	location parameter
sigma	scale parameter, must be positive.
df	degrees of freedom, must be positive.
log	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
n	number of random values to return.
р	vector of probabilities

#### **Details**

This implementation of dt2 allows for automatic differentiation with RTMB.

# Value

dt2 gives the density, pt2 gives the distribution function, qt2 gives the quantile function, and rt2 generates random deviates.

```
x <- rt2(1, 1, 2, 5)
d <- dt2(x, 1, 2, 5)
p <- pt2(x, 1, 2, 5)
q <- qt2(p, 1, 2, 5)
```

34 truncnorm

truncnorm

Truncated normal distribution

### Description

Density, distribution function, quantile function, and random generation for the truncated normal distribution.

#### Usage

#### **Arguments**

x, q	vector of quantiles
mean	mean parameter, must be positive.
sd	standard deviation parameter, must be positive.
min, max	truncation bounds.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
p	vector of probabilities
n	number of random values to return.

#### **Details**

This implementation of dtruncnorm allows for automatic differentiation with RTMB.

# Value

dtruncnorm gives the density, ptruncnorm gives the distribution function, qtruncnorm gives the quantile function, and rtruncnorm generates random deviates.

```
x <- rtruncnorm(1, mean = 2, sd = 2, min = -1, max = 5)
d <- dtruncnorm(x, mean = 2, sd = 2, min = -1, max = 5)
p <- ptruncnorm(x, mean = 2, sd = 2, min = -1, max = 5)
q <- qtruncnorm(p, mean = 2, sd = 2, min = -1, max = 5)</pre>
```

trunct 35

trunct

Truncated t distribution

# Description

Density, distribution function, quantile function, and random generation for the truncated t distribution.

# Usage

```
dtrunct(x, df, min = -Inf, max = Inf, log = FALSE)
ptrunct(q, df, min = -Inf, max = Inf, lower.tail = TRUE, log.p = FALSE)
qtrunct(p, df, min = -Inf, max = Inf, lower.tail = TRUE, log.p = FALSE)
rtrunct(n, df, min = -Inf, max = Inf)
```

# **Arguments**

x, q	vector of quantiles
df	degrees of freedom parameter, must be positive.
min, max	truncation bounds.
log, log.p	logical; if TRUE, probabilities/densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise $P[X > x]$ .
р	vector of probabilities
n	number of random values to return.

#### **Details**

This implementation of dtrunct allows for automatic differentiation with RTMB.

#### Value

dtrunct gives the density, ptrunct gives the distribution function, qtrunct gives the quantile function, and rtrunct generates random deviates.

```
x <- rtrunct(1, df = 5, min = -1, max = 5)
d <- dtrunct(x, df = 5, min = -1, max = 5)
p <- ptrunct(x, df = 5, min = -1, max = 5)
q <- qtrunct(p, df = 5, min = -1, max = 5)</pre>
```

36 trunct2

trunct2

Truncated t distribution with location and scale

### Description

Density, distribution function, quantile function, and random generation for the truncated t distribution with location mu and scale sigma.

# Usage

#### **Arguments**

x, q	vector of quantiles
df	degrees of freedom parameter, must be positive.
mu	location parameter.
sigma	scale parameter, must be positive.
min, max	truncation bounds.
log, log.p	logical; if TRUE, probabilities/densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise $P[X > x]$ .
р	vector of probabilities
n	number of random values to return.

#### **Details**

This implementation of dtrunct2 allows for automatic differentiation with RTMB.

### Value

dtrunct2 gives the density, ptrunct2 gives the distribution function, qtrunct2 gives the quantile function, and rtrunct2 generates random deviates.

```
x <- rtrunct2(1, df = 5, mu = 2, sigma = 3, min = -1, max = 5)
d <- dtrunct2(x, df = 5, mu = 2, sigma = 3, min = -1, max = 5)
p <- ptrunct2(x, df = 5, mu = 2, sigma = 3, min = -1, max = 5)
q <- qtrunct2(p, df = 5, mu = 2, sigma = 3, min = -1, max = 5)</pre>
```

vm 37

vm ,	von Mises distribution
------	------------------------

# Description

Density, distribution function, and random generation for the von Mises distribution.

# Usage

```
dvm(x, mu = 0, kappa = 1, log = FALSE)
pvm(q, mu = 0, kappa = 1, from = NULL, tol = 1e-20)
rvm(n, mu = 0, kappa = 1, wrap = TRUE)
```

# Arguments

x, q	vector of angles measured in radians at which to evaluate the density function.
mu	mean direction of the distribution measured in radians.
kappa	non-negative numeric value for the concentration parameter of the distribution.
log	logical; if TRUE, densities are returned on the log scale.
from	value from which the integration for CDF starts. If NULL, is set to mu - pi.
tol	the precision in evaluating the distribution function
n	number of random values to return.
wrap	logical; if TRUE, generated angles are wrapped to the interval from -pi to pi.

#### **Details**

This implementation of dvm allows for automatic differentiation with RTMB. rvm and pvm are simply wrappers of the corresponding functions from circular.

#### Value

dvm gives the density, pvm gives the distribution function, and rvm generates random deviates.

```
set.seed(1)
x <- rvm(10, 0, 1)
d <- dvm(x, 0, 1)
p <- pvm(x, 0, 1)</pre>
```

38 vmf

vmf von Mises-Fisher distribution
-----------------------------------

# Description

Density, distribution function, and random generation for the von Mises-Fisher distribution.

# Usage

```
dvmf(x, mu, kappa, log = FALSE)
rvmf(n, mu, kappa)
```

# **Arguments**

X	unit vector or matrix (with each row being a unit vector) of evaluation points
mu	unit mean vector
kappa	non-negative numeric value for the concentration parameter of the distribution.
log	logical; if TRUE, densities are returned on the log scale.
n	number of random values to return.

#### **Details**

This implementation of dvmf allows for automatic differentiation with RTMB. rvmf is a reparameterised import from movMF::rmovMF.

#### Value

dvmf gives the density and rvm generates random deviates.

```
set.seed(123)
# single parameter set
mu <- rep(1, 3) / sqrt(3)
kappa <- 4
x <- rvmf(1, mu, kappa)
d <- dvmf(x, mu, kappa)

# vectorised over parameters
mu <- matrix(mu, nrow = 1)
mu <- mu[rep(1,10), ]
kappa <- rep(kappa, 10)
x <- rvmf(10, mu, kappa)
d <- dvmf(x, mu, kappa)</pre>
```

vmf2

vmf2
------

Reparameterised von Mises-Fisher distribution

# **Description**

Density, distribution function, and random generation for the von Mises-Fisher distribution.

### Usage

```
dvmf2(x, theta, log = FALSE)
rvmf2(n, theta)
```

#### **Arguments**

x	unit vector or matrix (with each row being a unit vector) of evaluation points
theta	direction and concentration vector. The direction of theta determines the mean direction on the sphere. The norm of theta is the concentration parameter of the distribution.
log	logical; if TRUE, densities are returned on the log scale.
n	number of random values to return.

# **Details**

In this parameterisation,  $\theta=\kappa\mu$ , where  $\mu$  is a unit vector and  $\kappa$  is the concentration parameter. dvmf2 allows for automatic differentiation with RTMB. rvmf2 is imported from movMF::rmovMF.

#### Value

dvmf gives the density and rvm generates random deviates.

```
set.seed(123)
# single parameter set
theta <- c(1,2,3)
x <- rvmf2(1, theta)
d <- dvmf2(x, theta)

# vectorised over parameters
theta <- matrix(theta, nrow = 1)
theta <- theta[rep(1,10), ]
x <- rvmf2(10, theta)
d <- dvmf2(x, theta)</pre>
```

40 wrpcauchy

wrpcauchy	wrapped Cauchy distribution	

# Description

Density and random generation for the wrapped Cauchy distribution.

# Usage

```
dwrpcauchy(x, mu = 0, rho, log = FALSE)
rwrpcauchy(n, mu = 0, rho, wrap = TRUE)
```

# Arguments

X	vector of angles measured in radians at which to evaluate the density function.
mu	mean direction of the distribution measured in radians.
rho	concentration parameter of the distribution, must be in the interval from $0\ \mathrm{to}\ 1.$
log	logical; if TRUE, densities are returned on the log scale.
n	number of random values to return.
wrap	logical; if TRUE, generated angles are wrapped to the interval from -pi to pi.

#### **Details**

This implementation of dwrpcauchy allows for automatic differentiation with RTMB. rwrpcauchy is simply a wrapper for rwrappedcauchyimported from circular.

### Value

dwrpcauchy gives the density and rwrpcauchy generates random deviates.

```
set.seed(1)

x \leftarrow \text{rwrpcauchy}(10, 0, 0.5)

d \leftarrow \text{dwrpcauchy}(x, 0, 0.5)
```

zero\_inflate 41

zero\_inflate

Zero-inflated density constructer

#### **Description**

Constructs a zero-inflated density function from a given probability density function

# Usage

```
zero_inflate(dist, discrete = NULL)
```

#### **Arguments**

dist either a probability density function or a probability mass function

discrete logical; if TRUE, the density for x = 0 will be zeroprob + (1-zeroprob) \* dist(0, x = 0) will be zeroprob + (1-zeroprob) \* d

 $\dots$ ). Otherwise it will just be zeroprob. In standard cases, this will be determined automatically. For non-standard cases, set this to TRUE or FALSE depend-

ing on the type of dist. See details.

#### **Details**

The definition of zero-inflation is different for discrete and continuous distributions. For discrete distributions with p.m.f. f and zero-inflation probability p, we have

$$Pr(X = 0) = p + (1 - p) \cdot f(0),$$

and

$$Pr(X = x) = (1 - p) \cdot f(x), \quad x > 0.$$

For continuous distributions with p.d.f. f, we have

$$f_{\text{zinfl}}(x) = p \cdot \delta_0(x) + (1-p) \cdot f(x),$$

where  $\delta_0$  is the Dirac delta function at zero.

#### Value

zero-inflated density function with first argument x, second argument zeroprob, and additional arguments . . . that will be passed to dist.

```
# Zero-inflated normal distribution
dzinorm <- zero_inflate(dnorm)
dzinorm(c(NA, 0, 2), 0.5, mean = 1, sd = 1)
# Zero-inflated Poisson distribution
zipois <- zero_inflate(dpois)
zipois(c(NA, 0, 1), 0.5, 1)</pre>
```

42 zibeta

```
# Non-standard case: Zero-inflated reparametrised beta distribution
dzibeta2 <- zero_inflate(dbeta2, discrete = FALSE)</pre>
```

zibeta

Zero-inflated beta distribution

# **Description**

Density, distribution function, and random generation for the zero-inflated beta distribution.

### Usage

```
dzibeta(x, shape1, shape2, zeroprob = 0, log = FALSE)
pzibeta(q, shape1, shape2, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzibeta(n, shape1, shape2, zeroprob = 0)
```

# Arguments

x, q	vector of quantiles
shape1, shape2	non-negative shape parameters of the beta distribution
zeroprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

### **Details**

This implementation allows for automatic differentiation with RTMB.

#### Value

dzibeta gives the density, pzibeta gives the distribution function, and rzibeta generates random deviates.

```
set.seed(123)
x <- rzibeta(1, 2, 2, 0.5)
d <- dzibeta(x, 2, 2, 0.5)
p <- pzibeta(x, 2, 2, 0.5)</pre>
```

zibeta2 43

he	

Reparameterised zero-inflated beta distribution

# Description

Density, distribution function, and random generation for the zero-inflated beta distribution reparameterised in terms of mean and concentration.

# Usage

```
dzibeta2(x, mu, phi, zeroprob = 0, log = FALSE)
pzibeta2(q, mu, phi, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzibeta2(n, mu, phi, zeroprob = 0)
```

#### **Arguments**

x, q	vector of quantiles
mu	mean parameter, must be in the interval from 0 to 1.
phi	concentration parameter, must be positive.
zeroprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise $P[X > x]$ .
n	number of random values to return.
p	vector of probabilities

#### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzibeta2 gives the density, pzibeta2 gives the distribution function, and rzibeta2 generates random deviates.

```
set.seed(123)
x <- rzibeta2(1, 0.5, 1, 0.5)
d <- dzibeta2(x, 0.5, 1, 0.5)
p <- pzibeta2(x, 0.5, 1, 0.5)</pre>
```

44 zibinom

71	hi	nom
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Zero-inflated binomial distribution

# **Description**

Probability mass function, distribution function, and random generation for the zero-inflated binomial distribution.

# Usage

```
dzibinom(x, size, prob, zeroprob = 0, log = FALSE)
pzibinom(q, size, prob, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzibinom(n, size, prob, zeroprob = 0)
```

# **Arguments**

x, q	vector of quantiles
size	number of trials (zero or more).
prob	probability of success on each trial.
zeroprob	zero-inflation probability between 0 and 1
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzibinom gives the probability mass function, pzibinom gives the distribution function, and rzibinom generates random deviates.

```
set.seed(123)
x <- rzibinom(1, size = 10, prob = 0.5, zeroprob = 0.5)
d <- dzibinom(x, size = 10, prob = 0.5, zeroprob = 0.5)
p <- pzibinom(x, size = 10, prob = 0.5, zeroprob = 0.5)</pre>
```

zigamma 45

71	gamma
~ -	Samma

Zero-inflated gamma distribution

# Description

Density, distribution function, and random generation for the zero-inflated gamma distribution.

# Usage

```
dzigamma(x, shape, scale, zeroprob = 0, log = FALSE)
pzigamma(q, shape, scale, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzigamma(n, shape, scale, zeroprob = 0)
```

# **Arguments**

x, q	vector of quantiles
shape	positive shape parameter
scale	positive scale parameter
zeroprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return

#### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzigamma gives the density, pzigamma gives the distribution function, and rzigamma generates random deviates.

```
x \leftarrow rzigamma(1, 1, 1, 0.5)

d \leftarrow dzigamma(x, 1, 1, 0.5)

p \leftarrow pzigamma(x, 1, 1, 0.5)
```

46 zigamma2

		_
71	gamı	maフ

Zero-inflated and reparameterised gamma distribution

# Description

Density, distribution function, and random generation for the zero-inflated gamma distribution reparameterised in terms of mean and standard deviation.

# Usage

```
dzigamma2(x, mean = 1, sd = 1, zeroprob = 0, log = FALSE)
pzigamma2(q, mean = 1, sd = 1, zeroprob = 0)
rzigamma2(n, mean = 1, sd = 1, zeroprob = 0)
```

#### **Arguments**

x, q	vector of quantiles
mean	mean parameter, must be positive.
sd	standard deviation parameter, must be positive.
zeroprob	zero-inflation probability between 0 and 1.
log	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
n	number of random values to return

# **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzigamma2 gives the density, pzigamma2 gives the distribution function, and rzigamma generates random deviates.

```
x \leftarrow rzigamma2(1, 2, 1, 0.5)

d \leftarrow dzigamma2(x, 2, 1, 0.5)

p \leftarrow pzigamma2(x, 2, 1, 0.5)
```

ziinvgauss 47

71	7	nvgauss
	_	IIV gauss

Zero-inflated inverse Gaussian distribution

# Description

Density, distribution function, and random generation for the zero-inflated inverse Gaussian distribution.

# Usage

```
dziinvgauss(x, mean = 1, shape = 1, zeroprob = 0, log = FALSE)
pziinvgauss(q, mean = 1, shape = 1, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rziinvgauss(n, mean = 1, shape = 1, zeroprob = 0)
```

# **Arguments**

x, q	vector of quantiles
mean	location parameter
shape	shape parameter, must be positive.
zeroprob	zero-probability, must be in $[0, 1]$ .
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \le x]$ , otherwise, $P[X > x]$ .
n	number of random values to return

#### **Details**

This implementation of zidinvgauss allows for automatic differentiation with RTMB.

# Value

dziinvgauss gives the density, pziinvgauss gives the distribution function, and rziinvgauss generates random deviates.

```
x <- rziinvgauss(1, 1, 2, 0.5)
d <- dziinvgauss(x, 1, 2, 0.5)
p <- pziinvgauss(x, 1, 2, 0.5)</pre>
```

48 zilnorm

zilnorm

Zero-inflated log normal distribution

# **Description**

Density, distribution function, and random generation for the zero-inflated log normal distribution.

# Usage

# Arguments

x, q	vector of quantiles
meanlog, sdlog	mean and standard deviation of the distribution on the $\log$ scale with default values of 0 and 1 respectively.
zeroprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return

#### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzilnorm gives the density, pzilnorm gives the distribution function, and rzilnorm generates random deviates.

```
x <- rzilnorm(1, 1, 1, 0.5)
d <- dzilnorm(x, 1, 1, 0.5)
p <- pzilnorm(x, 1, 1, 0.5)</pre>
```

zinbinom 49

zin	hп	nc	٦m

Zero-inflated negative binomial distribution

# Description

Probability mass function, distribution function, quantile function, and random generation for the zero-inflated negative binomial distribution.

# Usage

```
dzinbinom(x, size, prob, zeroprob = 0, log = FALSE)
pzinbinom(q, size, prob, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzinbinom(n, size, prob, zeroprob = 0)
```

#### Arguments

x, q	vector of (non-negative integer) quantiles
size	size parameter, must be positive.
prob	mean parameter, must be positive.
zeroprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.
р	vector of probabilities

# **Details**

This implementation allows for automatic differentiation with RTMB.

#### Value

dzinbinom gives the density, pzinbinom gives the distribution function, and rzinbinom generates random deviates.

```
set.seed(123) x \leftarrow rzinbinom(1, size = 2, prob = 0.5, zeroprob = 0.5) d \leftarrow dzinbinom(x, size = 2, prob = 0.5, zeroprob = 0.5) p \leftarrow pzinbinom(x, size = 2, prob = 0.5, zeroprob = 0.5)
```

50 zinbinom2

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Zero-inflated and reparameterised negative binomial distribution

# Description

Probability mass function, distribution function, quantile function and random generation for the zero-inflated negative binomial distribution reparameterised in terms of mean and size.

# Usage

```
dzinbinom2(x, mu, size, zeroprob = 0, log = FALSE)
pzinbinom2(q, mu, size, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzinbinom2(n, mu, size, zeroprob = 0)
```

#### **Arguments**

x, q	vector of (non-negative integer) quantiles
mu	mean parameter, must be positive.
size	size parameter, must be positive.
zeroprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x],$ otherwise, $P[X > x].$
n	number of random values to return.
p	vector of probabilities

#### **Details**

This implementation allows for automatic differentiation with RTMB.

#### Value

dzinbinom2 gives the density, pzinbinom2 gives the distribution function, and rzinbinom2 generates random deviates.

```
set.seed(123)
x <- rzinbinom2(1, 2, 1, zeroprob = 0.5)
d <- dzinbinom2(x, 2, 1, zeroprob = 0.5)
p <- pzinbinom2(x, 2, 1, zeroprob = 0.5)</pre>
```

zipois 51

Z1	poıs

Zero-inflated Poisson distribution

# Description

Probability mass function, distribution function, and random generation for the zero-inflated Poisson distribution.

# Usage

```
dzipois(x, lambda, zeroprob = 0, log = FALSE)
pzipois(q, lambda, zeroprob = 0, lower.tail = TRUE, log.p = FALSE)
rzipois(n, lambda, zeroprob = 0)
```

# Arguments

x, q	integer vector of counts
lambda	vector of (non-negative) means
zeroprob	zero-inflation probability between 0 and 1
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \leq x],$ otherwise, $P[X > x].$
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzipois gives the probability mass function, pzipois gives the distribution function, and rzipois generates random deviates.

```
set.seed(123)
x <- rzipois(1, 0.5, 1)
d <- dzipois(x, 0.5, 1)
p <- pzipois(x, 0.5, 1)</pre>
```

52 zoibeta

zoibeta

Zero- and one-inflated beta distribution

# **Description**

Density, distribution function, and random generation for the zero-one-inflated beta distribution.

# Usage

# **Arguments**

x, q	vector of quantiles
shape1, shape2	non-negative shape parameters of the beta distribution
zeroprob	zero-inflation probability between 0 and 1.
oneprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

# **Details**

This implementation allows for automatic differentiation with RTMB.

# Value

dzoibeta gives the density, pzoibeta gives the distribution function, and rzoibeta generates random deviates.

```
set.seed(123)
x <- rzoibeta(1, 2, 2, 0.2, 0.3)
d <- dzoibeta(x, 2, 2, 0.2, 0.3)
p <- pzoibeta(x, 2, 2, 0.2, 0.3)</pre>
```

zoibeta2 53

zoibeta2	Reparameterised zero- and one-inflated beta distribution	

# Description

Density, distribution function, and random generation for the zero-one-inflated beta distribution reparameterised in terms of mean and concentration.

# Usage

# **Arguments**

x, q	vector of quantiles
mu	mean parameter, must be in the interval from 0 to 1.
phi	concentration parameter, must be positive.
zeroprob	zero-inflation probability between 0 and 1.
oneprob	zero-inflation probability between 0 and 1.
log, log.p	logical; if TRUE, probabilities/ densities $p$ are returned as $\log(p)$ .
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

#### Value

dzoibeta2 gives the density, pzoibeta2 gives the distribution function, and rzoibeta2 generates random deviates.

```
set.seed(123)
x <- rzoibeta2(1, 0.6, 2, 0.2, 0.3)
d <- dzoibeta2(x, 0.6, 2, 0.2, 0.3)
p <- pzoibeta2(x, 0.6, 2, 0.2, 0.3)</pre>
```

54 ztbinom

ztbinom

Zero-truncated Binomial distribution

#### **Description**

Probability mass function, distribution function, and random generation for the zero-truncated Binomial distribution.

#### Usage

```
dztbinom(x, size, prob, log = FALSE)
pztbinom(q, size, prob, lower.tail = TRUE, log.p = FALSE)
rztbinom(n, size, prob)
```

#### **Arguments**

x, q	integer vector of counts
size	number of trials
prob	success probability in each trial
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \le x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

By definition, this distribution only has support on the positive integers (1, ..., size). Any zero-truncated distribution is defined as

$$P(X = x | X > 0) = P(X = x)/(1 - P(X = 0)),$$

where P(X = x) is the probability mass function of the corresponding untruncated distribution.

#### Value

dztbinom gives the probability mass function, pztbinom gives the distribution function, and rztbinom generates random deviates.

```
set.seed(123)
x <- rztbinom(1, size = 10, prob = 0.3)
d <- dztbinom(x, size = 10, prob = 0.3)
p <- pztbinom(x, size = 10, prob = 0.3)</pre>
```

ztnbinom 55

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Zero-truncated Negative Binomial distribution

# Description

Probability mass function, distribution function, and random generation for the zero-truncated Negative Binomial distribution.

### Usage

```
dztnbinom(x, size, prob, log = FALSE)
pztnbinom(q, size, prob, lower.tail = TRUE, log.p = FALSE)
rztnbinom(n, size, prob)
```

# Arguments

x, q	integer vector of counts
size	target for number of successful trials, or dispersion parameter (the shape parameter of the gamma mixing distribution). Must be strictly positive, need not be integer.
prob	probability of success in each trial. 0 < prob <= 1.
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \le x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

# Details

This implementation allows for automatic differentiation with RTMB.

By definition, this distribution only has support on the positive integers (1, 2, ...). Any zero-truncated distribution is defined as

$$P(X = x | X > 0) = P(X = x)/(1 - P(X = 0)),$$

where P(X = x) is the probability mass function of the corresponding untruncated distribution.

#### Value

dztnbinom gives the probability mass function, pztnbinom gives the distribution function, and rztnbinom generates random deviates.

```
set.seed(123)
x <- rztnbinom(1, size = 2, prob = 0.5)
d <- dztnbinom(x, size = 2, prob = 0.5)
p <- pztnbinom(x, size = 2, prob = 0.5)</pre>
```

56 ztnbinom2

ztnbinom2

Reparameterised zero-truncated negative binomial distribution

#### **Description**

Probability mass function, distribution function, quantile function, and random generation for the zero-truncated negative binomial distribution reparameterised in terms of mean and size.

#### Usage

```
dztnbinom2(x, mu, size, log = FALSE)
pztnbinom2(q, mu, size, lower.tail = TRUE, log.p = FALSE)
rztnbinom2(n, mu, size)
```

#### **Arguments**

x, q	integer vector of counts
mu	mean parameter, must be positive
size	size/dispersion parameter, must be positive
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

By definition, this distribution only has support on the positive integers (1, 2, ...). Any zero-truncated distribution is defined as

$$P(X = x | X > 0) = P(X = x)/(1 - P(X = 0)),$$

where P(X = x) is the probability mass function of the corresponding untruncated distribution.

#### Value

dztnbinom2 gives the probability mass function, pztnbinom2 gives the distribution function, and rztnbinom2 generates random deviates.

```
set.seed(123)
x <- rztnbinom2(1, mu = 2, size = 1)
d <- dztnbinom2(x, mu = 2, size = 1)
p <- pztnbinom2(x, mu = 2, size = 1)</pre>
```

ztpois 57

ztpois

Zero-truncated Poisson distribution

#### **Description**

Probability mass function, distribution function, and random generation for the zero-truncated Poisson distribution.

# Usage

```
dztpois(x, lambda, log = FALSE)
pztpois(q, lambda, lower.tail = TRUE, log.p = FALSE)
rztpois(n, lambda)
```

# Arguments

x, q	integer vector of counts
lambda	vector of (non-negative) means
log, log.p	logical; return log-density if TRUE
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
n	number of random values to return.

#### **Details**

This implementation allows for automatic differentiation with RTMB.

By definition, this distribution only has support on the positive integers (1, 2, ...). Any zero-truncated distribution is defined as

$$P(X = x | X > 0) = P(X = x)/(1 - P(X = 0)),$$

where P(X = x) is the probability mass function of the corresponding untruncated distribution.

### Value

dztpois gives the probability mass function, pztpois gives the distribution function, and rztpois generates random deviates.

```
set.seed(123)
x <- rztpois(1, 0.5)
d <- dztpois(x, 0.5)
p <- pztpois(x, 0.5)</pre>
```

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