Package 'vstdct'

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Title Nonparametric Estimation of Toeplitz Covariance Matrices

Version 0.2

Description A nonparametric method to estimate Toeplitz covariance matrices from a sample of n independently and identically distributed p-dimensional vectors with mean zero. The data is preprocessed with the discrete cosine matrix and a variance stabilization transformation to obtain an approximate Gaussian regression setting for the log-spectral density function. Estimates of the spectral density function and the inverse of the covariance matrix are provided as well. Functions for simulating data and a protein data example are included. For details see (Klockmann, Krivobokova; 2023), <arXiv:2303.10018>.

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Author Karolina Klockmann [aut, cre], Tatyana Krivobokova [aut]
Maintainer Karolina Klockmann <karolina.klockmann@gmx.de></karolina.klockmann@gmx.de>
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aquaporin

Aquaporin Dataset

Description

Dataset with molecular dynamics simulations for the yeast aquaporin (Aqy1) - the gated water channel of the yeast Pichi pastoris. The dataset contains only the diameter Y of the channel which is used in the data analysis in (Klockmann and Krivobokova, 2023). The diameter Y is measured by the distance between two centers of mass of certain residues of the protein. The dataset includes a 100 nanosecond time frame, split into 20000 equidistant observations. The full dataset, including the Euclidean coordinates of all 783 atoms, is available from the authors. For more details see (Klockmann, Krivobokova; 2023).

Usage

aquaporin

Format

A data frame with 20000 rows and 1 variable:

• Y: the diameter of the channel

Source

see (Klockmann, Krivobokova; 2023).

Examples

data(aquaporin)

Data Examples

Data Examples

Description

example1, example2 and example3 generate i.i.d. vectors from a given distribution with different Toeplitz covariance matrices. The covariance function σ of the Toeplitz covariance matrix of

- example1: has a polynomial decay, $\sigma(\tau) = sd^2(1+|\tau|)^{-gamma}$,
- example2: follows an ARMA(2,2) model with coefficients (0.7, -0.4, -0.2, 0.2) and innovations variance sd^2 ,
- example3: yields a Lipschitz continuous spectral density f that is not differentiable, i.e. $f(x) = sd^2(|\sin(x+0.5\pi)|^{gamma} + 0.45)$

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Usage

```
example1(p, n, sd, gamma, family = "Gaussian")
example2(p, n, sd, family = "Gaussian")
example3(p, n, sd, gamma, family = "Gaussian")
```

Arguments

p vector length n sample size

sd standard deviation

gamma polynomial decay of covariance function for example1 resp. exponent for example3 family distribution of the simulated data. Available distributions are "Gaussian", "Gamma",

"Uniform". The default is "Gaussian".

Value

A list containing the following elements:

• Y: pxn dimensional data matrix

• sdf: true spectral density function

• acf: true covariance function

Examples

```
example1(p=10, n=1, sd=1, gamma=1.2, family="Gaussian")
example2(p=10,n=1,sd=1,family="Gaussian")
example3(p=10, n=1, sd=1, gamma=2,family="Gaussian")
```

Data.trafo

Data Transformation

Description

Applies the Discrete Cosine I transform, data binning and the variance stabilizing transform function to the data.

Usage

```
Data.trafo(y, Te, dct.out = FALSE)
```

Arguments

y nxp dimensional data matrix

Te number of bins for data binning. Te should be smaller than the vector length p.

dct.out logical. If TRUE, the p-dim. DCT-I matrix is returned. The default is FALSE.

DR.basis

Value

A list containing the following elements:

• m: number of data points per bin, that is m=n*round(p/Te). If p/Te is not an integer, the first/last bin may contain more than m data points.

- y.star: 2Te-2 dimensional vector with binned, variance stabilized and mirrowed data. The bin number Te may be modified to guarantee at least two data points per bin. If p/Te is not an integer, the vector dimension is 2*floor(p/round(p/Te))-2.
- dct.matrix: p-dim. DCT-I matrix (if dct.out=TRUE)

DR.basis

Periodic Demmler-Reinsch Basis

Description

Calculates the periodic Demmler-Reinsch basisfor a given smoothness and a given vector of grid points. For details see (Schwarz, Krivobokova; 2016).

Usage

```
DR.basis(x, n, q)
```

Arguments

x m-dim. vector with grid values in [0,1]

n dimension of the basis

q penalization order, q=1,2,3,4 are available

Value

mxn dimensional matrix with the n DR basis functions evaluated at grid points x

Examples

```
DR.basis(seq(1,10)/10,5,2)
```

Toep.estimator 5

•	Toep.estimator	Toeplitz Covariance and Precision Matrix Estimator

Description

Estimates the Toeplitz covariance matrix, the inverse matrix and the spectral density from a sample of n i.i.d. p-dimensional vectors with mean zero.

Usage

```
Toep.estimator(y, Te, q, method, f.true = NULL)
```

Arguments

У	nxp dimensional data matrix
Te	number of bins for data binning.
q	penalization order, q=1,2,3,4 are available
method	to select the smoothing parameter of the smoothing spline. Available methods are restricted maxmimum likelihodd "ML", generalized cross-validation "GCV" and the oracle versions "ML-oracle", "GCV-oracle".
f.true	Te-dimensional vector with the true spectral density function evaluated at equisapced points in [0,pi]. Only required, if an oracle method ("ML-oracle", "GCV-oracle") is chosen for method.

Value

A list containing the following elements:

- toep: p-dim. Toeplitz covariance matrix
- toep.inv: p-dim. precision matrix
- acf: p-dim. vector with the covariance function
- sdf: p-dim. vector with the spectral density in the interval [0,1]

Examples

```
#EXAMPLE 1: Simulate Gaussian ARMA(2,2)
library(nlme)
library(MASS)
p=100
n=1
Sigma=1.44*corMatrix(Initialize(corARMA(c(0.7, -0.4,-0.2, 0.2),p=2,q=2),data=diag(1:p)))
Y=matrix(mvrnorm(n, mu=numeric(p), Sigma=Sigma),n,p)
fit.toep=Toep.estimator(y=Y,Te=10,q=2,method="GCV")$toep

#EXAMPLE 2: AQUAPORIN DATA
```

Toep.estimator

```
data(aquaporin)
n=length(aquaporin$Y)
y.train=aquaporin$Y[1:(0.01*n)]
y.train=y.train-mean(y.train)
fit.toep=Toep.estimator(y=y.train,Te=10,q=1,method="ML")$toep
```

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