## Package 'mmcif'

October 13, 2022

```
Title Mixed Multivariate Cumulative Incidence Functions
Version 0.1.1
Description Fits the mixed cumulative incidence functions model suggested by
     <doi:10.1093/biostatistics/kxx072> which decomposes within cluster
     dependence of risk and timing. The estimation method supports computation in
     parallel using a shared memory C++ implementation. A sandwich estimator of the
     covariance matrix is available. Natural cubic splines are used to provide a
     flexible model for the cumulative incidence functions.
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```

Type Package

log\_chol

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log\_chol

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Computes the Log Cholesky Decomposition and the Inverse

## Description

Computes the log Cholesky decomposition and the inverse of it. The functions are provided as the log Cholesky decomposition is used in the parameterization of the covariance matrix.

## Usage

```
log_chol(x)
log_chol_inv(x)
```

### **Arguments**

Х

A positive definite matrix or a vector with a log Cholesky decomposition.

#### Value

A numeric vector with the log Cholesky decomposition or a matrix with the inverse.

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 ${\tt mmcif\_data}$ 

Sets up an Object to Compute the Log Composite Likelihood

## Description

Sets up the R and C++ objects that are needed to evaluate the log composite likelihood. This reduces to a log likelihood when only clusters of size one or two are used.

## Usage

```
mmcif_data(
  formula,
  data,
  cause,
  time,
  cluster_id,
  max_time,
  spline_df = 3L,
  left_trunc = NULL,
  ghq_data = NULL,
  knots = NULL,
  boundary_quantiles = c(0.025, 0.975)
)
```

### **Arguments**

formula	formula for covariates in the risk and trajectories.
data	data.frame with the covariate and outcome information.
cause	an integer vector with the cause of each outcome. If there are $n_causes$ of outcome, then the vector should have values in 1: $(n_causes + 1)$ with $n_causes + 1$ indicating censoring.
time	a numeric vector with the observed times.
cluster_id	an integer vector with the cluster id of each individual.
max_time	the maximum time after which there are no observed events. It is denoted by $\tau$ in the original article (Cederkvist et al., 2019).
spline_df	degrees of freedom to use for each spline in the cumulative incidence functions.
left_trunc	numeric vector with left-truncation times. NULL implies that there are not any individuals with left-truncation.
ghq_data	the default Gauss-Hermite quadrature nodes and weights to use. It should be a list with two elements called "node" and "weight". A default is provided if NULL is passed.
strata	an integer vector or a factor vector with the strata of each individual. NULL implies that there are no strata.

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knots

A list of lists with knots for the splines. The inner lists needs to have elements called "knots" and "boundary\_knots" which are passed to a function like ns. NULL yields defaults based on the quantiles of the observed event times. Note that the knots needs to be on the atanh((time - max\_time / 2) / (max\_time / 2)) scale.

boundary\_quantiles

two dimensional numerical vector with boundary quantile probabilities after which the natural cubic splines for the time transformations are restricted to be linear. Only relevant if knots is not NULL.

#### Value

An object of class mmcif which is needed for the other functions in the package.

#### References

Cederkvist, L., Holst, K. K., Andersen, K. K., & Scheike, T. H. (2019). *Modeling the cumulative incidence function of multivariate competing risks data allowing for within-cluster dependence of risk and timing*. Biostatistics, Apr 1, 20(2), 199-217.

#### See Also

```
mmcif_fit, mmcif_start_values and mmcif_sandwich.
```

```
if(require(mets)){
  # prepare the data
 data(prt)
 # truncate the time
 max_time <- 90
 prt <- within(prt, {</pre>
   status[time >= max_time] <- 0</pre>
    time <- pmin(time, max_time)</pre>
 })
 # select the DZ twins and re-code the status
 prt_use <- subset(prt, zyg == "DZ") |>
    transform(status = ifelse(status == 0, 3L, status))
 # randomly sub-sample
 set.seed(1)
 prt_use <- subset(</pre>
   prt_use, id %in% sample(unique(id), length(unique(id)) %/% 10L))
 mmcif_obj <- mmcif_data(</pre>
    ~ country - 1, prt_use, status, time, id, max_time,
    2L, strata = country)
}
```

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mmcif\_fit

Fits a Mixed Competing Risk Model

### **Description**

Fits mixed cumulative incidence functions model by maximizing the log composite likelihood function.

#### Usage

```
mmcif_fit(
  par,
  object,
  n_threads = 1L,
  control.outer = list(itmax = 100L, method = "nlminb", kkt2.check = FALSE, trace =
    FALSE),
  control.optim = list(eval.max = 10000L, iter.max = 10000L),
  ghq_data = object$ghq_data,
  ...
)
```

#### **Arguments**

par numeric vector with parameters. This is using a log Cholesky decomposition for

the covariance matrix.

object an object from mmcif\_data.

n\_threads the number of threads to use.

control.outer, control.optim, ...

arguments passed to auglag.

ghq\_data the Gauss-Hermite quadrature nodes and weights to use. It should be a list

with two elements called "node" and "weight". The argument can also be a list with lists with different sets of quadrature nodes. In this case, fits are successively made using the previous fit as the starting value. This may reduce

the computation time by starting with fewer quadrature nodes.

#### Value

The output from auglag.

### References

Cederkvist, L., Holst, K. K., Andersen, K. K., & Scheike, T. H. (2019). *Modeling the cumulative incidence function of multivariate competing risks data allowing for within-cluster dependence of risk and timing*. Biostatistics, Apr 1, 20(2), 199-217.

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#### See Also

mmcif\_data, mmcif\_start\_values and mmcif\_sandwich.

```
if(require(mets)){
 # prepare the data
 data(prt)
 # truncate the time
 max_time <- 90
 prt <- within(prt, {</pre>
   status[time >= max_time] <- 0</pre>
    time <- pmin(time, max_time)</pre>
 })
 # select the DZ twins and re-code the status
 prt_use <- subset(prt, zyg == "DZ") |>
    transform(status = ifelse(status == 0, 3L, status))
 # randomly sub-sample
 set.seed(1)
 prt_use <- subset(</pre>
   prt_use, id %in% sample(unique(id), length(unique(id)) %/% 10L))
 n_threads <- 2L
 mmcif_obj <- mmcif_data(</pre>
   ~ country - 1, prt_use, status, time, id, max_time,
   2L, strata = country)
 # get the staring values
 start_vals <- mmcif_start_values(mmcif_obj, n_threads = n_threads)</pre>
 # estimate the parameters
 ests <- mmcif_fit(start_vals$upper, mmcif_obj, n_threads = n_threads)</pre>
 # show the estimated covariance matrix of the random effects
 tail(ests$par, 10L) |> log_chol_inv() |> print()
 # gradient is ~ zero
 mmcif_logLik_grad(
   mmcif_obj, ests$par, is_log_chol = TRUE, n_threads = n_threads) |>
   print()
}
```

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### **Description**

Evaluates the log composite likelihood and its gradient using adaptive Gauss-Hermite quadrature.

## Usage

```
mmcif_logLik(
  object,
  par,
  ghq_data = object$ghq_data,
  n_threads = 1L,
  is_log_chol = FALSE
)

mmcif_logLik_grad(
  object,
  par,
  ghq_data = object$ghq_data,
  n_threads = 1L,
  is_log_chol = FALSE
)
```

### **Arguments**

object	an object from mmcif_data.
par	numeric vector with parameters. This is either using a log Cholesky decomposition for the covariance matrix or the covariance matrix.
ghq_data	the Gauss-Hermite quadrature nodes and weights to use. It should be a list with two elements called "node" and "weight". A default is provided if NULL is passed.
n_threads	the number of threads to use.
is_log_chol	logical for whether a log Cholesky decomposition is used for the covariance matrix or the full covariance matrix.

#### Value

A numeric vector with either the log composite likelihood or the gradient of it.

```
if(require(mets)){
    # prepare the data
    data(prt)

# truncate the time
max_time <- 90
prt <- within(prt, {
    status[time >= max_time] <- 0
    time <- pmin(time, max_time)</pre>
```

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```
})
 # select the DZ twins and re-code the status
 prt_use <- subset(prt, zyg == "DZ") |>
   transform(status = ifelse(status == 0, 3L, status))
 # randomly sub-sample
 set.seed(1)
 prt_use <- subset(</pre>
   prt_use, id %in% sample(unique(id), length(unique(id)) %/% 10L))
 n_threads <- 2L
 mmcif_obj <- mmcif_data(</pre>
   ~ country - 1, prt_use, status, time, id, max_time,
   2L, strata = country)
 # get the staring values
 start_vals <- mmcif_start_values(mmcif_obj, n_threads = n_threads)</pre>
 # compute the log composite likelihood and the gradient at the starting
 # values
 mmcif_logLik(
   mmcif_obj, start_vals$upper, is_log_chol = TRUE, n_threads = n_threads) |>
   print()
 mmcif_logLik_grad(
   mmcif_obj, start_vals$upper, is_log_chol = TRUE, n_threads = n_threads) |>
}
```

mmcif\_pd\_cond

Computes Marginal Measures Using Two Observations

#### **Description**

Computes bivariate figures such as conditional CIFs, survival probabilities, and hazards or bivariate CIFs, densities, and survival probabilities.

### Usage

```
mmcif_pd_cond(
  par,
  object,
  newdata,
  cause,
  time,
  left_trunc = NULL,
  ghq_data = object$ghq_data,
  strata = NULL,
```

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```
which_cond,
  type_cond = "derivative",
  type_obs = "cumulative"
)
mmcif_pd_bivariate(
  par,
  object,
  newdata,
  cause,
  time,
  left_trunc = NULL,
  ghq_data = object$ghq_data,
  strata = NULL,
  use_log = FALSE,
  type = c("cumulative", "cumulative")
)
```

#### **Arguments**

par numeric vector with the model parameters.

object an object from mmcif\_data.

newdata a data. frame with data for the observations. It needs to have two rows.

cause an integer vector with the cause of each outcome. If there are n\_causes of out-

come, then the vector should have values in 1: (n\_causes + 1) with n\_causes

+ 1 indicating censoring.

time a numeric vector with the observed times.

left\_trunc numeric vector with left-truncation times. NULL implies that there are not any

individuals with left-truncation.

ghq\_data the Gauss-Hermite quadrature nodes and weights to use. It should be a list with

two elements called "node" and "weight". A default is provided if NULL is

passed.

strata an integer vector or a factor vector with the strata of each individual. NULL

implies that there are no strata.

which\_cond an integer with value one or two for the index of the individual that is being

conditioned on.

type\_cond a character for the type of outcome that is being conditioned on. "derivative"

for the derivative of a CIF or "cumulative" for a CIF or the survival probability.

type\_obs a character the type of conditional measure. It can be "derivative" for the

derivative of a CIF, "cumulative" for a CIF or the survival probability, and

"hazard" for the hazard.

use\_log a logical for whether the returned output should be on the log scale.

type a 2D character vector for the type of measures for each observation. The ele-

ments can be "derivative" for the derivative of a CIF or "cumulative" for a

CIF or the survival probability.

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#### Value

A numeric scalar with the requested quantity.

#### See Also

```
mmcif_pd_univariate and mmcif_fit.
```

```
if(require(mets)){
 data(prt)
 # truncate the time
 max_time <- 90
 prt <- within(prt, {</pre>
   status[time >= max_time] <- 0</pre>
   time <- pmin(time, max_time)</pre>
 # select the DZ twins and re-code the status
 prt_use <- subset(prt, zyg == "DZ") |>
    transform(status = ifelse(status == 0, 3L, status))
 # Gauss Hermite quadrature nodes and weights from fastGHQuad::gaussHermiteData
 ghq_data <- list(</pre>
   node = c(-3.43615911883774, -2.53273167423279, -1.75668364929988, -1.03661082978951,
             -0.342901327223705, 0.342901327223705, 1.03661082978951, 1.75668364929988,
             2.53273167423279, 3.43615911883774),
  weight = c(7.6404328552326e-06,\ 0.00134364574678124,\ 0.0338743944554811,\ 0.240138611082314.
              0.610862633735326, 0.610862633735326, 0.240138611082315, 0.033874394455481,
               0.00134364574678124, 7.64043285523265e-06))
 # setup the object for the computation
 mmcif_obj <- mmcif_data(</pre>
   ~ country - 1, prt_use, status, time, id, max_time,
   2L, strata = country, ghq_data = ghq_data)
 # previous estimates
 par < -c(0.727279974859164, 0.640534073288067, 0.429437766165371, 0.434367104339573,
           -2.4737847536253, -1.49576564624673, -1.89966050143904, -1.58881346649412,
           -5.5431198001029, -3.5328359024178, -5.82305147022587, -3.4531896212114,
           -5.29132887832377, -3.36106297109548, -6.03690322125729, -3.49516746825624,
           2.55000711185704, 2.71995985605891, 2.61971498736444, 3.05976391058032,
           -5.97173564860957, -3.37912051983482, -5.14324860374941, -3.36396780694965,
           -6.02337246348561, -3.03754644968859, -5.51267338700737, -3.01148582224673,
           2.69665543753264, 2.59359057553995, 2.7938341786374, 2.70689750644755,
           -0.362056555418564, 0.24088005091276, 0.124070380635372, -0.246152029808377,
         -0.0445628476462479, -0.911485513197845, -0.27911988106887, -0.359648419277058,
           -0.242711959678559, -6.84897302527358)
  # the test data we will use
 test_dat <- data.frame(</pre>
```

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```
country = factor(c("Norway", "Norway"), levels(prt_use$country)),
    status = c(1L, 2L), time = c(60, 75))
 # probability that both experience the event prior to the two times
 mmcif_pd_bivariate(
   par = par, object = mmcif_obj, newdata = test_dat, cause = status,
   strata = country, ghq_data = ghq_data, time = time, type =
     c("cumulative", "cumulative")) |>
   print()
 # density that one experiences an event at the point and the other
 # experiences an event prior to the point
 mmcif_pd_bivariate(
   par = par, object = mmcif_obj, newdata = test_dat, cause = status,
   strata = country, ghq_data = ghq_data, time = time, type =
     c("derivative", "cumulative")) |>
   print()
 # probability that both survive up to the passed points
 mmcif_pd_bivariate(
   par = par, object = mmcif_obj, newdata = test_dat, cause = c(3L, 3L),
   strata = country, ghq_data = ghq_data, time = time, type =
     c("cumulative", "cumulative")) |>
   print()
 # conditional hazard given that the other experiences an event prior to time
 mmcif_pd_cond(
   par = par, object = mmcif_obj, newdata = test_dat, cause = status,
    strata = country, ghq_data = ghq_data, time = time, which_cond = 1L,
    type_cond = "cumulative", type_obs = "hazard") |>
   print()
 # conditional CIF given that the other experiences an event prior to the
 # time
 mmcif_pd_cond(
   par = par, object = mmcif_obj, newdata = test_dat, cause = c(2L, 2L),
   strata = country, ghq_data = ghq_data, time = time, which_cond = 1L,
    type_cond = "cumulative", type_obs = "cumulative") |>
   print()
 # same but given that the other experiences the event at the point
 mmcif_pd_cond(
   par = par, object = mmcif_obj, newdata = test_dat, cause = c(2L, 2L),
   strata = country, ghq_data = ghq_data, time = time, which_cond = 1L,
   type_cond = "derivative", type_obs = "cumulative") |>
   print()
}
```

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#### **Description**

Computes the marginal cumulative incidence functions (CIF), marginal survival function or the derivative of the CIF.

#### Usage

```
mmcif_pd_univariate(
  par,
  object,
  newdata,
  cause,
  time,
  left_trunc = NULL,
  ghq_data = object$ghq_data,
  strata = NULL,
  use_log = FALSE,
  type = "cumulative"
)
```

#### **Arguments**

par numeric vector with the model parameters.

object an object from mmcif\_data.

newdata a data. frame with data for the observation. It needs to have one row.

cause an integer vector with the cause of each outcome. If there are n\_causes of out-

come, then the vector should have values in 1: (n\_causes + 1) with n\_causes

+ 1 indicating censoring.

time a numeric vector with the observed times.

left\_trunc numeric vector with left-truncation times. NULL implies that there are not any

individuals with left-truncation.

ghq\_data the Gauss-Hermite quadrature nodes and weights to use. It should be a list with

two elements called "node" and "weight". A default is provided if NULL is

passed.

strata an integer vector or a factor vector with the strata of each individual. NULL

implies that there are no strata.

use\_log a logical for whether the returned output should be on the log scale.

type a character for the type of measures for the observation. It can have value

"derivative" for the derivative of a CIF or "cumulative" for a CIF or the

survival probability.

#### Value

A numeric scalar with the requested quantity.

#### See Also

```
mmcif_pd_bivariate and mmcif_pd_cond.
```

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```
if(require(mets)){
   data(prt)
   # truncate the time
   max_time <- 90
   prt <- within(prt, {</pre>
       status[time >= max_time] <- 0</pre>
       time <- pmin(time, max_time)</pre>
   })
   # select the DZ twins and re-code the status
   prt_use <- subset(prt, zyg == "DZ") |>
       transform(status = ifelse(status == 0, 3L, status))
   # Gauss Hermite quadrature nodes and weights from fastGHQuad::gaussHermiteData
   ghq_data <- list(</pre>
       node = c(-3.43615911883774, -2.53273167423279, -1.75668364929988, -1.03661082978951,
                         -0.342901327223705, 0.342901327223705, 1.03661082978951, 1.75668364929988,
                         2.53273167423279, 3.43615911883774),
     weight = c(7.6404328552326e-06, 0.00134364574678124, 0.0338743944554811, 0.240138611082314,
                           0.610862633735326, 0.610862633735326, 0.240138611082315, 0.033874394455481,
                             0.00134364574678124, 7.64043285523265e-06))
   # setup the object for the computation
   mmcif_obj <- mmcif_data(</pre>
       ~ country - 1, prt_use, status, time, id, max_time,
       2L, strata = country, ghq_data = ghq_data)
   # previous estimates
   par <- \ c (0.727279974859164, \ 0.640534073288067, \ 0.429437766165371, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339573, \ 0.434367104339574, \ 0.434367104339574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671043574, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.4343671044, \ 0.434671044, \ 0.434671044, \ 0.43
                     -2.4737847536253, -1.49576564624673, -1.89966050143904, -1.58881346649412,
                     -5.5431198001029, -3.5328359024178, -5.82305147022587, -3.4531896212114,
                     -5.29132887832377, -3.36106297109548, -6.03690322125729, -3.49516746825624,
                     2.55000711185704, 2.71995985605891, 2.61971498736444, 3.05976391058032,
                     -5.97173564860957, -3.37912051983482, -5.14324860374941, -3.36396780694965,
                     -6.02337246348561, -3.03754644968859, -5.51267338700737, -3.01148582224673,
                     2.69665543753264, 2.59359057553995, 2.7938341786374, 2.70689750644755,
                     -0.362056555418564, 0.24088005091276, 0.124070380635372, -0.246152029808377,
                  -0.0445628476462479, -0.911485513197845, -0.27911988106887, -0.359648419277058,
                     -0.242711959678559, -6.84897302527358)
   # the test data we will use
   test_dat <- data.frame(country = factor("Norway", levels(prt_use$country)),</pre>
                                                 status = 2L)
   # compute the CIF
   mmcif_pd_univariate(
       par = par, object = mmcif_obj, newdata = test_dat, cause = status,
       strata = country, ghq_data = ghq_data, time = 75, type = "cumulative") |>
       print()
```

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```
# compute the derivative of the CIF
mmcif_pd_univariate(
   par = par, object = mmcif_obj, newdata = test_dat, cause = status,
   strata = country, ghq_data = ghq_data, time = 75, type = "derivative") |>
   print()

# compute the survival probability
mmcif_pd_univariate(
   par = par, object = mmcif_obj, newdata = test_dat, cause = 3L,
   strata = country, ghq_data = ghq_data, time = 75, type = "cumulative") |>
   print()
}
```

mmcif sandwich

Computes the Sandwich Estimator

#### **Description**

Computes the sandwich estimator of the covariance matrix. The parameter that is passed is using the log Cholesky decomposition. The Hessian is computed using numerical differentiation with Richardson extrapolation to refine the estimate.

#### Usage

```
mmcif_sandwich(
  object,
  par,
  ghq_data = object$ghq_data,
  n_threads = 1L,
  eps = 0.01,
  scale = 2,
  tol = 1e-08,
  order = 3L
)
```

#### **Arguments**

object an object from mmcif\_data.

par numeric vector with the parameters to compute the sandwich estimator at.

ghq\_data the Gauss-Hermite quadrature nodes and weights to use. It should be a list with

two elements called "node" and "weight". A default is provided if NULL is

passed.

n\_threads the number of threads to use.

eps determines the step size in the numerical differentiation using max(sqrt(.Machine\$double.eps),

|par[i]| \* eps) for each parameter i.

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scale	scaling factor in the Richardson extrapolation. Each step is smaller by a factor scale.
tol	relative convergence criteria in the extrapolation given by $\max(tol,  g[i]  * tol)$ with g being the gradient and for each parameter i.
order	maximum number of iteration of the Richardson extrapolation.

#### Value

The sandwich estimator along attributes called

- "meat" for the "meat" of the sandwich estimator.
- "hessian" for the Hessian of the log composite likelihood.
- "res vcov" which is the sandwich estimator where the last elements are the upper triangle of the covariance matrix of the random effects rather than the log Cholesky decomposition of the matrix.

#### References

Cederkvist, L., Holst, K. K., Andersen, K. K., & Scheike, T. H. (2019). *Modeling the cumulative incidence function of multivariate competing risks data allowing for within-cluster dependence of risk and timing*. Biostatistics, Apr 1, 20(2), 199-217.

#### See Also

```
mmcif_fit and mmcif_data.
```

```
if(require(mets)){
 # prepare the data
 data(prt)
 # truncate the time
 max_time <- 90
 prt <- within(prt, {</pre>
   status[time >= max_time] <- 0</pre>
    time <- pmin(time, max_time)</pre>
 })
 # select the DZ twins and re-code the status
 prt\_use <- subset(prt, zyg == "DZ") |>
    transform(status = ifelse(status == 0, 3L, status))
 # randomly sub-sample
 set.seed(1)
 prt_use <- subset(</pre>
   prt_use, id %in% sample(unique(id), length(unique(id)) %/% 10L))
 n_threads <- 2L
 mmcif_obj <- mmcif_data(</pre>
```

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```
~ country - 1, prt_use, status, time, id, max_time,
   2L, strata = country)
 # get the staring values
 start_vals <- mmcif_start_values(mmcif_obj, n_threads = n_threads)</pre>
 # estimate the parameters
 ests <- mmcif_fit(start_vals$upper, mmcif_obj, n_threads = n_threads)</pre>
 # get the sandwich estimator
 vcov_est <- mmcif_sandwich(</pre>
   mmcif_obj, ests$par, n_threads = n_threads, order = 2L)
 # show the parameter estimates along with the standard errors
 rbind(Estimate = ests$par,
        SE = sqrt(diag(vcov_est))) |>
   print()
 # show the upper triangle of the covariance matrix and the SEs
 rbind(`Estimate (vcov)` = tail(ests$par, 10) |> log_chol_inv() |>
          (\x) x[upper.tri(x, TRUE)])(),
        SE = attr(vcov_est, "res vcov") |> diag() |> sqrt() |> tail(10)) |>
   print()
}
```

mmcif\_start\_values

Finds Staring Values

#### Description

Fast heuristic for finding starting values for the mixed cumulative incidence functions model.

### Usage

```
mmcif_start_values(object, n_threads = 1L, vcov_start = NULL)
```

#### Arguments

object an object from mmcif\_data. n\_threads the number of threads to use.

vcov\_start starting value for the covariance matrix of the random effects. NULL yields the

identity matrix.

#### Value

A list with

 an element called "full" with the starting value where the last components are the covariance matrix. mmcif\_start\_values 17

• an element called "upper" the staring values where the covariance matrix is stored as a log Cholesky decomposition. This is used e.g. for optimization with mmcif\_fit.

```
if(require(mets)){
 # prepare the data
 data(prt)
 # truncate the time
 max_time <- 90
 prt <- within(prt, {</pre>
   status[time >= max_time] <- 0</pre>
   time <- pmin(time, max_time)</pre>
 })
 # select the DZ twins and re-code the status
 prt_use <- subset(prt, zyg == "DZ") |>
   transform(status = ifelse(status == 0, 3L, status))
 # randomly sub-sample
 set.seed(1)
 prt_use <- subset(</pre>
   prt_use, id %in% sample(unique(id), length(unique(id)) %/% 10L))
 n_threads <- 2L
 mmcif_obj <- mmcif_data(</pre>
   ~ country - 1, prt_use, status, time, id, max_time,
   2L, strata = country)
 # get the staring values
 start_vals <- mmcif_start_values(mmcif_obj, n_threads = n_threads)</pre>
 # the starting values
 print(start_vals)
}
```

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