Package 'akima'

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Title Interpolation of Irregularly and Regularly Spaced Data

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Description Several cubic spline interpolation methods of H. Akima for irregular and
regular gridded data are available through this package, both for the bivariate case
(irregular data: ACM 761, regular data: ACM 760) and univariate case (ACM 433 and ACM 697).
Linear interpolation of irregular gridded data is also covered by reusing D. J. Renkas
triangulation code which is part of Akimas Fortran code. A bilinear interpolator
for regular grids was also added for comparison with the bicubic interpolator on
regular grids.

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Depends R (>= 2.0.0)

Imports sp

Enhances tripack

NeedsCompilation yes

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Albrecht Gebhardt [aut, cre, cph] (R port (interp*, bicubic*
functions), bilinear code),
Thomas Petzold [ctb, cph] (aspline function),
Martin Maechler [ctb, cph] (interp2xyz function + enhancements),
YYYY Association for Computing Machinery, Inc. [cph] (covers code from
TOMS 760, 761, 697 and 433)

License_restricts_use yes

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R topics documented:

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akima | *Waveform Distortion Data for Bivariate Interpolation*

Description

akima is a list with components x, y and z which represents a smooth surface of z values at selected points irregularly distributed in the x-y plane.

The data was taken from a study of waveform distortion in electronic circuits, described in: Hiroshi Akima, "A Method of Bivariate Interpolation and Smooth Surface Fitting Based on Local Procedures", CACM, Vol. 17, No. 1, January 1974, pp. 18-20.

References

Hiroshi Akima, "A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points", ACM Transactions on Mathematical Software, Vol. 4, No. 2, June 1978, pp. 148-159. Copyright 1978, Association for Computing Machinery, Inc., reprinted by permission.

Examples

```
## Not run:
library(rgl)
data(akima)
# data
rgl.spheres(akima$x,akima$z , akima$y,0.5,color="red")
rgl.bbox()
# bivariate linear interpolation
# interp:
akima.li <- interp(akima$x, akima$y, akima$z,
                   xo=seq(min(akima$x), max(akima$x), length = 100),
                   yo=seq(min(akima$y), max(akima$y), length = 100))
# interp surface:
rgl.surface(akima.li$x,akima.li$y,akima.li$z,color="green",alpha=c(0.5))
# interpp:
akima.p <- interpp(akima$x, akima$y, akima$z,
                    runif(200,min(akima$x),max(akima$x)),
```

```
                            runif(200,min(akima$y),max(akima$y)))
# interpp points:
rgl.points(akima.p$x,akima.p$z , akima.p$y,size=4,color="yellow")

# bivariate spline interpolation
# data
rgl.spheres(akima$x,akima$z , akima$y,0.5,color="red")
rgl.bbox()
# bivariate cubic spline interpolation
# interp:
akima.si <- interp(akima$x, akima$y, akima$z,
                   xo=seq(min(akima$x), max(akima$x), length = 100),
                   yo=seq(min(akima$y), max(akima$y), length = 100),
                   linear = FALSE, extrap = TRUE)
# interp surface:
rgl.surface(akima.si$x,akima.si$y,akima.si$z,color="green",alpha=c(0.5))
# interpp:
akima.sp <- interpp(akima$x, akima$y, akima$z,
                     runif(200,min(akima$x),max(akima$x)),
                     runif(200,min(akima$y),max(akima$y)),
                    linear = FALSE, extrap = TRUE)
# interpp points:
rgl.points(akima.sp$x,akima.sp$z , akima.sp$y,size=4,color="yellow")


## End(Not run)
```

---

akima760   *Sample data from Akima's Bicubic Spline Interpolation code (TOMS 760)*

Description

akima760 is a list with vector components x, y and a matrix z which represents a smooth surface of z values at the points of a regular grid spanned by the vectors x and y.

References

Hiroshi Akima, "

", ACM Transactions on Mathematical Software, Vol. 22, No. 3, September 1996, pp. 357-361.

Examples

```
## Not run:
library(rgl)
data(akima)
# data
rgl.spheres(akima760$x,akima760$z , akima760$y,0.5,color="red")
rgl.bbox()
```

```
# bivariate linear interpolation
# interp:
akima.li <- interp(akima$x, akima$y, akima$z,
                   xo=seq(min(akima$x), max(akima$x), length = 100),
                   yo=seq(min(akima$y), max(akima$y), length = 100))
# interp surface:
rgl.surface(akima.li$x,akima.li$y,akima.li$z,color="green",alpha=c(0.5))
# interpp:
akima.p <- interpp(akima$x, akima$y, akima$z,
                    runif(200,min(akima$x),max(akima$x)),
                    runif(200,min(akima$y),max(akima$y)))
# interpp points:
rgl.points(akima.p$x,akima.p$z , akima.p$y,size=4,color="yellow")

# bivariate spline interpolation
# data
rgl.spheres(akima$x,akima$z , akima$y,0.5,color="red")
rgl.bbox()
# bivariate cubic spline interpolation
# interp:
akima.si <- interp(akima$x, akima$y, akima$z,
                   xo=seq(min(akima$x), max(akima$x), length = 100),
                   yo=seq(min(akima$y), max(akima$y), length = 100),
                   linear = FALSE, extrap = TRUE)
# interp surface:
rgl.surface(akima.si$x,akima.si$y,akima.si$z,color="green",alpha=c(0.5))
# interpp:
akima.sp <- interpp(akima$x, akima$y, akima$z,
                     runif(200,min(akima$x),max(akima$x)),
                     runif(200,min(akima$y),max(akima$y)),
                    linear = FALSE, extrap = TRUE)
# interpp points:
rgl.points(akima.sp$x,akima.sp$z , akima.sp$y,size=4,color="yellow")


## End(Not run)
```

---

aspline   *Univariate Akima interpolation*

Description

The function returns a list of points which smoothly interpolate given data points, similar to a curve drawn by hand.

Usage

```
aspline(x, y=NULL, xout, n = 50, ties = mean, method="original", degree=3)
```

Arguments

x, y	vectors giving the coordinates of the points to be interpolated. Alternatively a single plotting structure can be specified: see `xy.coords`.
xout	an optional set of values specifying where interpolation is to take place.
n	If `xout` is not specified, interpolation takes place at `n` equally spaced points spanning the interval $[\min(x), \max(x)]$.
ties	Handling of tied `x` values. Either a function with a single vector argument returning a single number result or the string `"ordered"`.
method	either `"original"` method after Akima (1970) or `"improved"` method after Akima (1991)
degree	if improved algorithm is selected: degree of the polynomials for the interpolating function

Details

The original algorithm is based on a piecewise function composed of a set of polynomials, each of degree three, at most, and applicable to successive interval of the given points. In this method, the slope of the curve is determined at each given point locally, and each polynomial representing a portion of the curve between a pair of given points is determined by the coordinates of and the slopes at the points.

Value

A list with components `x` and `y`, containing `n` coordinates which interpolate the given data points.

References

Akima, H. (1970) A new method of interpolation and smooth curve fitting based on local procedures, J. ACM **17**(4), 589-602

Akima, H. (1991) A Method of Univariate Interpolation that Has the Accuracy of a Third-degree Polynomial. ACM Transactions on Mathematical Software, **17**(3), 341-366.

See Also

`approx`, `spline`

Examples

```
## regular spaced data
x <- 1:10
y <- c(rnorm(5), c(1,1,1,1,3))

xnew <- seq(-1, 11, 0.1)
plot(x, y, ylim=c(-3, 3), xlim=range(xnew))
lines(spline(x, y, xmin=min(xnew), xmax=max(xnew), n=200), col="blue")

lines(aspline(x, y, xnew), col="red")
lines(aspline(x, y, xnew, method="improved"), col="black", lty="dotted")
```

```
lines(aspline(x, y, xnew, method="improved", degree=10), col="green", lty="dashed")

## irregular spaced data
x <- sort(runif(10, max=10))
y <- c(rnorm(5), c(1,1,1,1,3))

xnew <- seq(-1, 11, 0.1)
plot(x, y, ylim=c(-3, 3), xlim=range(xnew))
lines(spline(x, y, xmin=min(xnew), xmax=max(xnew), n=200), col="blue")

lines(aspline(x, y, xnew), col="red")
lines(aspline(x, y, xnew, method="improved"), col="black", lty="dotted")
lines(aspline(x, y, xnew, method="improved", degree=10), col="green", lty="dashed")

## an example of Akima, 1991
x <- c(-3, -2, -1, 0,  1,  2, 2.5, 3)
y <- c( 0,  0,  0, 0, -1, -1, 0,   2)

plot(x, y, ylim=c(-3, 3))
lines(spline(x, y, n=200), col="blue")

lines(aspline(x, y, n=200), col="red")
lines(aspline(x, y, n=200, method="improved"), col="black", lty="dotted")
lines(aspline(x, y, n=200, method="improved", degree=10), col="green", lty="dashed")
```

---

bicubic   *Bivariate Interpolation for Data on a Rectangular grid*

Description

The description in the Fortran code says:

This subroutine performs interpolation of a bivariate function, $z(x,y)$, on a rectangular grid in the x-y plane. It is based on the revised Akima method.

In this subroutine, the interpolating function is a piecewise function composed of a set of bicubic (bivariate third-degree) polynomials, each applicable to a rectangle of the input grid in the x-y plane. Each polynomial is determined locally.

This subroutine has the accuracy of a bicubic polynomial, i.e., it interpolates accurately when all data points lie on a surface of a bicubic polynomial.

The grid lines can be unevenly spaced.

Usage

```
bicubic(x, y, z, x0, y0)
```

Arguments

x	a vector containing the x coordinates of the rectangular data grid.
y	a vector containing the y coordinates of the rectangular data grid.
z	a matrix containing the z[i,j] data values for the grid points (x[i],y[j]).
x0	vector of x coordinates used to interpolate at.
y0	vector of y coordinates used to interpolate at.

Details

This functiuon is a R interface to Akima's Rectangular-Grid-Data Fitting algorithm (TOMS 760). The algorithm has the accuracy of a bicubic (bivariate third-degree) polynomial.

Value

This function produces a list of interpolated points:

x	vector of x coordinates.
y	vector of y coordinates.
z	vector of interpolated data z.

If you need an output grid, see `bicubic.grid`.

Note

Use `interp` for the general case of irregular gridded data!

References

Akima, H. (1996) Rectangular-Grid-Data Surface Fitting that Has the Accuracy of a Bicubic Polynomial, J. ACM **22**(3), 357-361

See Also

`interp`, `bicubic.grid`

Examples

```
data(akima760)
# interpolate at the diagonal of the grid [0,8]x[0,10]
akima.bic <- bicubic(akima760$x,akima760$y,akima760$z,
                     seq(0,8,length=50), seq(0,10,length=50))
plot(sqrt(akima.bic$x^2+akima.bic$y^2), akima.bic$z, type="l")
```

| bicubic.grid | *Bicubic Interpolation for Data on a Rectangular grid* |

Description

The description in the Fortran code says:

This subroutine performs interpolation of a bivariate function, z(x,y), on a rectangular grid in the x-y plane. It is based on the revised Akima method.

In this subroutine, the interpolating function is a piecewise function composed of a set of bicubic (bivariate third-degree) polynomials, each applicable to a rectangle of the input grid in the x-y plane. Each polynomial is determined locally.

This subroutine has the accuracy of a bicubic polynomial, i.e., it interpolates accurately when all data points lie on a surface of a bicubic polynomial.

The grid lines can be unevenly spaced.

Usage

```
bicubic.grid(x,y,z,xlim=c(min(x),max(x)),ylim=c(min(y),max(y)),
            nx=40,ny=40,dx=NULL,dy=NULL)
```

Arguments

x	a vector containing the x coordinates of the rectangular data grid.
y	a vector containing the y coordinates of the rectangular data grid.
z	a matrix containing the z[i,j] data values for the grid points (x[i],y[j]).
xlim	vector of length 2 giving lower and upper limit for range x coordinates used for output grid.
ylim	vector of length 2 giving lower and upper limit for range of y coordinates used for output grid.
nx	output grid dimension in x direction.
ny	output grid dimension in y direction.
dx	output grid spacing in x direction, not used by default, overrides nx if specified.
dy	output grid spacing in y direction, not used by default, overrides ny if specified..

Details

This functiuon is a R interface to Akima's Rectangular-Grid-Data Fitting algorithm (TOMS 760). The algorithm has the accuracy of a bicubic (bivariate third-degree) polynomial.

Value

This function produces a grid of interpolated points, feasible to be used directly with [image](#) and [contour](#):

x	vector of x coordinates of the output grid.
y	vector of y coordinates of the output grid.
z	matrix of interpolated data for the output grid.

Note

Use [interp](#) for the general case of irregular gridded data!

References

Akima, H. (1996) Rectangular-Grid-Data Surface Fitting that Has the Accuracy of a Bicubic Polynomial, J. ACM **22**(3), 357-361

See Also

[interp](#), [bicubic](#)

Examples

```
data(akima760)
# interpolate at a grid [0,8]x[0,10]
akima.bic <- bicubic.grid(akima760$x,akima760$y,akima760$z)
zmin <- min(akima.bic$z, na.rm=TRUE)
zmax <- max(akima.bic$z, na.rm=TRUE)
breaks <- pretty(c(zmin,zmax),10)
colors <- heat.colors(length(breaks)-1)
image(akima.bic, breaks=breaks, col=colors)
contour(akima.bic, levels=breaks,  add=TRUE)
```

---

bilinear   *Bilinear Interpolation for Data on a Rectangular grid*

Description

This is an implementation of a bilinear interpolating function.

For a point (x0,y0) contained in a rectangle (x1,y1),(x2,y1), (x2,y2),(x1,y2) and x1<x2, y1<y2, the first step is to get z() at locations (x0,y1) and (x0,y2) as convex linear combinations z(x0,y*)=a*z(x1,y*)+(1-a)*z(x2,y*) where a=(x2-x1)/(x0-x1) for y*=y1,y2. In a second step z(x0,y0) is calculated as convex linear combination between z(x0,y1) and z(x0,y2) as z(x0,y1)=b*z(x0,y1)+(1-b)*z(x0,y2) where b=(y2-y1)/(y0-y1).

Finally, z(x0,y0) is a convex linear combination of the z values at the corners of the containing rectangle with weights according to the distance from (x0,y0) to these corners.

The grid lines can be unevenly spaced.

Usage

```
bilinear(x, y, z, x0, y0)
```

Arguments

x	a vector containing the x coordinates of the rectangular data grid.
y	a vector containing the y coordinates of the rectangular data grid.
z	a matrix containing the z[i,j] data values for the grid points (x[i],y[j]).
x0	vector of x coordinates used to interpolate at.
y0	vector of y coordinates used to interpolate at.

Value

This function produces a list of interpolated points:

x	vector of x coordinates.
y	vector of y coordinates.
z	vector of interpolated data z.

If you need an output grid, see `bilinear.grid`.

Note

Use `interpp` for the general case of irregular gridded data!

References

Pascal Getreuer, Linear Methods for Image Interpolation, Image Processing On Line, 2011, http://www.ipol.im/pub/art/2011/g

See Also

`interp`, `bilinear.grid`, `bicubic.grid`

Examples

```
data(akima760)
# interpolate at the diagonal of the grid [0,8]x[0,10]
akima.bil <- bilinear(akima760$x,akima760$y,akima760$z,
                      seq(0,8,length=50), seq(0,10,length=50))
plot(sqrt(akima.bil$x^2+akima.bil$y^2), akima.bil$z, type="l")
```

---

bilinear.grid   *Bilinear Interpolation for Data on a Rectangular grid*

Description

This is an implementation of a bilinear interpolating function.

For a point (x0,y0) contained in a rectangle (x1,y1),(x2,y1), (x2,y2),(x1,y2) and x1<x2, y1<y2, the first step is to get z() at locations (x0,y1) and (x0,y2) as convex linear combinations z(x0,y*)=a*z(x1,y*)+(1-a)*z(x2,y*) where a=(x2-x1)/(x0-x1) for y*=y1,y2. In a second step z(x0,y0) is calculated as convex linear combination between z(x0,y1) and z(x0,y2) as z(x0,y1)=b*z(x0,y1)+(1-b)*z(x0,y2) where b=(y2-y1)/(y0-y1).

Finally, z(x0,y0) is a convex linear combination of the z values at the corners of the containing rectangle with weights according to the distance from (x0,y0) to these corners.

The grid lines can be unevenly spaced.

Usage

```
bilinear.grid(x,y,z,xlim=c(min(x),max(x)),ylim=c(min(y),max(y)),
                      nx=40,ny=40,dx=NULL,dy=NULL)
```

Arguments

x	a vector containing the x coordinates of the rectangular data grid.
y	a vector containing the y coordinates of the rectangular data grid.
z	a matrix containing the z[i,j] data values for the grid points (x[i],y[j]).
xlim	vector of length 2 giving lower and upper limit for range x coordinates used for output grid.
ylim	vector of length 2 giving lower and upper limit for range of y coordinates used for output grid.
nx	output grid dimension in x direction.
ny	output grid dimension in y direction.
dx	output grid spacing in x direction, not used by default, overrides nx if specified.
dy	output grid spacing in y direction, not used by default, overrides ny if specified..

Value

This function produces a grid of interpolated points, feasible to be used directly with [image](#) and [contour](#):

x	vector of x coordinates of the output grid.
y	vector of y coordinates of the output grid.
z	matrix of interpolated data for the output grid.

Note

Use [interp](#) for the general case of irregular gridded data!

References

Pascal Getreuer, Linear Methods for Image Interpolation, Image Processing On Line, 2011, http://www.ipol.im/pub/art/2011/

See Also

[interp](#), [bicubic](#)

Examples

```
data(akima760)
# interpolate at a grid [0,8]x[0,10]
akima.bil <- bilinear.grid(akima760$x,akima760$y,akima760$z)
zmin <- min(akima.bil$z, na.rm=TRUE)
zmax <- max(akima.bil$z, na.rm=TRUE)
breaks <- pretty(c(zmin,zmax),10)
colors <- heat.colors(length(breaks)-1)
image(akima.bil, breaks=breaks, col=colors)
contour(akima.bil, levels=breaks, add=TRUE)
```

---

franke.data   *Test datasets from Franke for interpolation of scattered data*

Description

franke.data generates the test datasets from Franke, 1979, see references.

Usage

```
franke.data(fn = 1, ds = 1, data)
franke.fn(x, y, fn = 1)
```

Arguments

fn	function number, from 1 to 5.
x	'x' value
y	'y' value
ds	data set number, from 1 to 3. Dataset 1 consists of 100 points, dataset 2 of 33 points and dataset 3 of 25 points scattered in the square $[0, 1] \times [0, 1]$. (and partially slightly outside).
data	A list of dataframes with 'x' and 'y' to choose from, dataset franke should be used here.

Details

These datasets are mentioned in [Akima 1996] as testbed for the irregular scattered data interpolator.

Franke used the five functions:

$$0.75e^{-\frac{(9x-2)^2+(9y-2)^2}{4}} + 0.75e^{-\frac{(9x+1)^2}{49}-\frac{9y+1}{10}} + 0.5e^{-\frac{(9x-7)^2+(9y-3)^2}{4}} - 0.2e^{-((9x-4)^2-(9y-7)^2)}$$

$$\frac{\tanh(9y-9x)+1}{9}$$

$$\frac{1.25+\cos(5.4y)}{6(1+(3x-1)^2)}$$

$$e^{-\frac{81((x-0.5)^2+\frac{(y-0.5)^2}{16})}{3}}$$

$$e^{-\frac{81((x-0.5)^2+\frac{(y-0.5)^2}{4})}{3}}$$

$$\frac{\sqrt{64-81((x-0.5)^2+(y-0.5)^2)}}{9} - 0.5$$

and evaluated them on different more or less dense grids over $[0,1] \times [0,1]$.

Value

A data frame with components

x	'x' coordinate
y	'y' coordinate
z	'z' value

Note

The datasets have to be generated via `franke.data` before use, the dataset `franke` only contains a list of 3 dataframes of 'x' and 'y' coordinates for the above mentioned irregular grids. Do not forget to load the `franke` dataset first.

The 'x' and 'y' values have been taken out of [Akima 1996].

Author(s)

A. Gebhardt,

References

FRANKE, R., (1979). A critical comparison of some methods for interpolation of scattered data. Tech. Rep. NPS-53-79-003, Dept. of Mathematics, Naval Postgraduate School, Monterey, Calif.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic polynomial. ACM Transactions on Mathematical Software **22**, 362–371.

See Also

interp

Examples

```
## generate Frankes data set for function 2 and dataset 3:
data(franke)
F23 <- franke.data(2,3,franke)
str(F23)
```

---

interp   *Gridded Bivariate Interpolation for Irregular Data*

Description

These functions implement bivariate interpolation onto a grid for irregularly spaced input data. Bilinear or bicubic spline interpolation is applied using different versions of algorithms from Akima.

Usage

```
interp(x, y=NULL, z, xo=seq(min(x), max(x), length = nx),
       yo=seq(min(y), max(y), length = ny),
       linear = TRUE, extrap=FALSE, duplicate = "error", dupfun = NULL,
       nx = 40, ny = 40,
       jitter = 10^-12, jitter.iter = 6, jitter.random = FALSE,
       remove = !linear)
```

Arguments

x	vector of x-coordinates of data points or a `SpatialPointsDataFrame` object. Missing values are not accepted.
y	vector of y-coordinates of data points. Missing values are not accepted.
	If left as NULL indicates that x should be a `SpatialPointsDataFrame` and z names the variable of interest in this dataframe.
z	vector of z-coordinates of data points or a character variable naming the variable of interest in the `SpatialPointsDataFrame` x.
	Missing values are not accepted.
	x, y, and z must be the same length (execpt if x is a `SpatialPointsDataFrame`) and may contain no fewer than four points. The points of x and y should not be

collinear, i.e, they should not fall on the same line (two vectors x and y such that y = ax + b for some a, b will not produce menaningful results). Some heuristics is built in to avoid this case by adding small jitter to x and y when the number of NA values in the result exceeds 10%.

interp is meant for cases in which you have x, y values scattered over a plane and a z value for each. If, instead, you are trying to evaluate a mathematical function, or get a graphical interpretation of relationships that can be described by a polynomial, try outer().

xo
vector of x-coordinates of output grid. The default is 40 points evenly spaced over the range of x. If extrapolation is not being used (extrap=FALSE, the default), xo should have a range that is close to or inside of the range of x for the results to be meaningful.

yo
vector of y-coordinates of output grid; analogous to xo, see above.

linear
logical – indicating wether linear or spline interpolation should be used.

extrap
logical flag: should extrapolation be used outside of the convex hull determined by the data points?

duplicate
character string indicating how to handle duplicate data points. Possible values are

"error" produces an error message,

"strip" remove duplicate z values,

"mean","median","user" calculate mean , median or user defined function (dupfun) of duplicate z values.

dupfun
a function, applied to duplicate points if duplicate= "user".

nx
dimension of output grid in x direction

ny
dimension of output grid in y direction

jitter
Jitter of amount of diff(range(XX))*jitter (XX=x or y) will be added to coordinates if collinear points are detected. Afterwards interpolation will be tried once again.

Note that the jitter is not generated randomly unless jitter.random is set to TRUE. This ensures reproducable result. tri.mesh of package tripack uses the same jitter mechanism. That means you can plot the triangulation on top of the interpolation and see the same triangulation as used for interpolation, see examples below.

jitter.iter
number of iterations to retry with jitter, amount will be multiplied in each iteration by iter^1.5

jitter.random
logical, see jitter, defaults to FALSE

remove
logical, indicates whether Akimas removal of thin triangles along the border of the convex hull should be performed, experimental setting! defaults to !linear, so it will be left out for linear interpolation by default. For some point configurations it is the only available option to skip this removal step.

Details

If linear is TRUE (default), linear interpolation is used in the triangles bounded by data points. Cubic interpolation is done if linear is set to FALSE. If extrap is FALSE, z-values for points outside the convex hull are returned as NA. No extrapolation can be performed for the linear case.

The interp function handles duplicate (x,y) points in different ways. As default it will stop with an error message. But it can give duplicate points an unique z value according to the parameter duplicate (mean,median or any other user defined function).

The triangulation scheme used by interp works well if x and y have similar scales but will appear stretched if they have very different scales. The spreads of x and y must be within four orders of magnitude of each other for interp to work.

Value

list with 3 components:

x,y	vectors of x- and y- coordinates of output grid, the same as the input argument xo, or yo, if present. Otherwise, their default, a vector 40 points evenly spaced over the range of the input x.
z	matrix of fitted z-values. The value z[i,j] is computed at the x,y point xo[i], yo[j]. z has dimensions length(xo) times length(yo).

If input is a SpatialPointsDataFrame a SpatialPixelssDataFrame is returned.

Note

interp uses Akimas new Fortran code (ACM 761) from 1996 in the revised version by Renka from 1998 for spline interpolation, the triangulation (based on Renkas tripack) is reused for linear interpolation. In this newer version Akima switched from his own triangulation to Renkas tripack (ACM 751).

Note that earlier versions (up to version 0.5-12) as well as S-Plus used the old Fortran code from Akima 1978 (ACM 526).

The resulting structure is suitable for input to the functions contour and image. Check the requirements of these functions when choosing values for xo and yo.

References

Akima, H. (1978). A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points. ACM Transactions on Mathematical Software **4**, 148-164.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic polynomial. ACM Transactions on Mathematical Software **22**, 362–371.

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

R. J. Renka and Ron Brown (1998). Remark on algorithm 761. ACM Transactions on Mathematical Software. **24**, 383-385.

See Also

contour, image, approx, spline, aspline, outer, expand.grid, link{franke.data}.

Examples

```
data(akima)
plot(y ~ x, data = akima, main = "akima example data")
with(akima, text(x, y, formatC(z,dig=2), adj = -0.1))

## linear interpolation
akima.li <- interp(akima$x, akima$y, akima$z)
li.zmin <- min(akima.li$z,na.rm=TRUE)
li.zmax <- max(akima.li$z,na.rm=TRUE)
breaks <- pretty(c(li.zmin,li.zmax),10)
colors <- heat.colors(length(breaks)-1)
with(akima.li, image  (x,y,z, breaks=breaks, col=colors))
with(akima.li,contour(x,y,z, levels=breaks, add=TRUE))
points (akima, pch = 3)

## increase smoothness (using finer grid):
akima.smooth <-
    with(akima, interp(x, y, z, nx=100, ny=100))
si.zmin <- min(akima.smooth$z,na.rm=TRUE)
si.zmax <- max(akima.smooth$z,na.rm=TRUE)
breaks <- pretty(c(si.zmin,si.zmax),10)
colors <- heat.colors(length(breaks)-1)

image  (akima.smooth, main = "interp(<akima data>, *) on finer grid",
        breaks=breaks, col=colors)
contour(akima.smooth, add = TRUE, levels=breaks, col = "thistle")
points(akima, pch = 3, cex = 2, col = "blue")

## use triangulation package to show underlying triangulation:
## Not run:
if(library(tripack, logical.return=TRUE))
   plot(tri.mesh(akima), add=TRUE, lty="dashed")

## End(Not run)
## use only 15 points (interpolation only within convex hull!)
akima.part <- with(akima, interp(x[1:15], y[1:15], z[1:15]))
p.zmin <- min(akima.part$z,na.rm=TRUE)
p.zmax <- max(akima.part$z,na.rm=TRUE)
breaks <- pretty(c(p.zmin,p.zmax),10)
colors <- heat.colors(length(breaks)-1)

image(akima.part, breaks=breaks, col=colors)
title("interp() on subset of only 15 points")
contour(akima.part, levels=breaks, add=TRUE)
points(akima$x[1:15],akima$y[1:15], col = "blue")

## spline interpolation
akima.spl <- with(akima, interp(x, y, z, nx=100, ny=100, linear=FALSE))

contour(akima.spl, main = "smooth  interp(*, linear = FALSE)")
points(akima)
```

```
full.pal <- function(n) hcl(h = seq(340, 20, length = n))
cool.pal <- function(n) hcl(h = seq(120, 0, length = n) + 150)
warm.pal <- function(n) hcl(h = seq(120, 0, length = n) - 30)

filled.contour(akima.spl, color.palette = full.pal,
        plot.axes = { axis(1); axis(2);
                      title("smooth  interp(*, linear = FALSE)");
                      points(akima, pch = 3, col= hcl(c=100, l = 20))})
## no extrapolation!

## Not run:
    ## interp can handle spatial point dataframes created by the sp package:
    library(sp)
    data(meuse)
    coordinates(meuse) <- ~x+y
    ## argument z has to be named, y has to be omitted!
    z <- interp(meuse,z="zinc",nx=100,ny=150)
    spplot(z,"zinc")
    z <- interp(meuse,z="zinc",nx=100,ny=150,linear=FALSE)
    spplot(z,"zinc")

## End(Not run)

## Not run:
### An example demonstrating the problems that occur for rectangular
### gridded data.
###
require(tripack)
### Create irregularly spaced sample data on even values of x and y
### (the "14" makes it irregular spacing).
x    <- c(seq(2,10,2),14)
nx   <- length(x)
y    <- c(seq(2,10,2),14)
ny   <- length(y)
nxy <- nx*ny
xy   <- expand.grid(x,y)
colnames(xy) <- c("x","y")
### prepare a dataframe for interp
df   <- cbind(xy,z=rnorm(nxy))
### and a matrix for bicubic and bilinear
z    <- matrix(df$z,nx,ny)

old.par <- par(mfrow=c(2,2))
### First: bicubic spline interpolation:
### This is Akimas bicubic spline implementation for regular gridded
### data:
iRbic <- bicubic.grid(x,y,z,nx=250,ny=250)
### Note that this interpolation tends to extreme values in large cells.
### Therefore zmin and zmax are taken from here to generate the same
### color scheme for the next plots.
zmin <- min(iRbic$z, na.rm=TRUE)
zmax <- max(iRbic$z, na.rm=TRUE)
breaks <- pretty(c(zmin,zmax),10)
```

```
colors <- heat.colors(length(breaks)-1)
image(iRbic,breaks=breaks,col = colors)
contour(iRbic,col="black",levels=breaks,add=TRUE)
points(xy$x,xy$y)
title(main="bicubic interpolation",
      xlab="bcubic.grid(...)",
      sub="Akimas regular grid version, ACM 760")

### Now Akima splines with accurrary of bicubic polynomial
### for irregular gridded data:
iRspl <- with(df,interp(x,y,z,linear=FALSE,nx=250,ny=250))
### Note that the triangulation is created by adding small amounts
### of jitter to the coordinates, resulting in an unique triangulation.
### This jitter is not randomly choosen to get reproducable results.
### tri.mesh() from package tripack uses the same code and so produces the
### same triangulation.
image(iRspl,breaks=breaks,col = colors)
contour(iRspl,col="black",levels=breaks,add=TRUE)
plot(tri.mesh(xy$x,xy$y),col="white",add=TRUE)
title(main="bicubic* interpolation",
      xlab="interp(...,linear=FALSE)",
      ylab="*: accuracy of bicubic polynomial"
      sub="Akimas irregular grid version, ACM 761")

### Just for comparison an implementation of bilinear interpolation,
### only applicable to regular gridded data:
iRbil <- bilinear.grid(x,y,z,nx=250,ny=250)
### Note the lack of differentiability at grid cell borders.
image(iRbil,breaks=breaks,col = colors)
contour(iRbil,col="black",levels=breaks,add=TRUE)
points(xy$x,xy$y)
title(main="bilinear interpolation",
      xlab="bilinear.grid(...)",
      sub="only works for regular grid")

### Linear interpolation using the same triangulation as
### Akima bicubic splines for irregular gridded data.
iRlin <- with(df,interp(x,y,z,linear=TRUE,nx=250,ny=250))
### Note how the triangulation influences the interpolation.
### For this rectangular gridded dataset the triangulation
### in each rectangle is arbitraryly choosen from two possible
### solutions, hence the interpolation would change drastically
### when the triangulation changes. For this reason interp()
### is not meant for regular (rectangular) gridded data!
image(iRlin,breaks=breaks,col = colors)
contour(iRlin,col="black",levels=breaks,add=TRUE)
plot(tri.mesh(xy$x,xy$y),col="white",add=TRUE)
title(main="linear interpolation",
      xlab="interp(...,linear=TRUE)",
      sub="same triangulation as Akima irregular grid")

### And now four times Akima 761 with random jitter for
### triangulation correction, note that now interp() and tri.mesh()
```

```
### need the same random seed to produce identical triangulations!
for(i in 1:4){
    set.seed(42+i)
    iRspl <- with(df,interp(x,y,z,linear=FALSE,nx=250,ny=250,jitter.random=TRUE))
    image(iRspl,breaks=breaks,col = colors)
    contour(iRspl,col="black",levels=breaks,add=TRUE)
    set.seed(42+i)
    plot(tri.mesh(xy$x,xy$y,jitter.random=TRUE),col="white",add=TRUE)
    title(main="bicubic* interpolation",
          xlab="interp(...,linear=FALSE)",
          ylab="random jitter added",
          sub="Akimas irregular grid version, ACM 761")
}
par(old.par)


## End(Not run)
### Use all datasets from Franke, 1979:
data(franke)
for(i in 1:5)
    for(j in 1:3){
        FR <- franke.data(i,j,franke)
        IL <- with(FR, interp(x,y,z,linear=FALSE))
        image(IL)
        contour(IL,add=TRUE)
        with(FR,points(x,y))
    }
```

---

interp.old   *Gridded Bivariate Interpolation for Irregular Data*

Description

These functions implement bivariate interpolation onto a grid for irregularly spaced input data. These functions are only for backward compatibility, use interp instead.

Usage

```
interp.old(x, y, z, xo= seq(min(x), max(x), length = 40),
           yo=seq(min(y), max(y), length = 40), ncp = 0,
           extrap=FALSE, duplicate = "error", dupfun = NULL)
interp.new(x, y, z, xo = seq(min(x), max(x), length = 40),
           yo = seq(min(y), max(y), length = 40), linear = FALSE,
           ncp = NULL, extrap=FALSE, duplicate = "error", dupfun = NULL)
```

Arguments

x   vector of x-coordinates of data points or a SpatialPointsDataFrame object.
                  Missing values are not accepted.

y	vector of y-coordinates of data points. Missing values are not accepted.
	If left as NULL indicates that x should be a SpatialPointsDataFrame and z names the variable of interest in this dataframe.
z	vector of z-coordinates of data points or a character variable naming the variable of interest in the SpatialPointsDataFrame x.
	Missing values are not accepted.
	x, y, and z must be the same length (execpt if x is a SpatialPointsDataFrame) and may contain no fewer than four points. The points of x and y cannot be collinear, i.e, they cannot fall on the same line (two vectors x and y such that y = ax + b for some a, b will not be accepted). interp is meant for cases in which you have x, y values scattered over a plane and a z value for each. If, instead, you are trying to evaluate a mathematical function, or get a graphical interpretation of relationships that can be described by a polynomial, try outer().
xo	vector of x-coordinates of output grid. The default is 40 points evenly spaced over the range of x. If extrapolation is not being used (extrap=FALSE, the default), xo should have a range that is close to or inside of the range of x for the results to be meaningful.
yo	vector of y-coordinates of output grid; analogous to xo, see above.
linear	logical – indicating wether linear or spline interpolation should be used. supersedes old ncp parameter
ncp	deprecated, use parameter linear. Now only used by interp.old().
	old meaning was: number of additional points to be used in computing partial derivatives at each data point. ncp must be either 0 (partial derivatives are not used), or at least 2 but smaller than the number of data points (and smaller than 25).
extrap	logical flag: should extrapolation be used outside of the convex hull determined by the data points?
duplicate	character string indicating how to handle duplicate data points. Possible values are
	"error" produces an error message,
	"strip" remove duplicate z values,
	"mean","median","user" calculate mean , median or user defined function (dupfun) of duplicate z values.
dupfun	a function, applied to duplicate points if duplicate= "user".

Details

see [interp](#)

Value

list with 3 components:

x,y	vectors of x- and y- coordinates of output grid, the same as the input argument xo, or yo, if present. Otherwise, their default, a vector 40 points evenly spaced over the range of the input x.

z   matrix of fitted z-values. The value z[i,j] is computed at the x,y point xo[i],
                              yo[j]. z has dimensions length(xo) times length(yo).

If input is a SpatialPointsDataFrame a SpatialPixelssDataFrame is returned.

Note

interp.new is deprecated and interp.old will soon be deprecated.

References

Akima, H. (1978). A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly
Distributed Data Points. ACM Transactions on Mathematical Software **4**, 148-164.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic
polynomial. ACM Transactions on Mathematical Software **22**, 362–371.

See Also

contour, image, approx, spline, aspline, outer, expand.grid.

---

interp2xyz   *From interp() Result, Produce 3-column Matrix*

Description

From an interp() result, produce a 3-column matrix or data.frame cbind(x, y, z).

Usage

```
interp2xyz(al, data.frame = FALSE)
```

Arguments

al   a list as produced from interp().
data.frame   logical indicating if result should be data.frame or matrix (default).

Value

a matrix (or data.frame) with three columns, called "x", "y", "z".

Author(s)

Martin Maechler, Jan.18, 2013

See Also

expand.grid() is the "essential ingredient" of interp2xyz().
interp.

Examples

```
data(akima)
ak.spl <- with(akima, interp(x, y, z, linear = FALSE,
                             xo= seq(0,25, length=100),
                             yo= seq(0,20, length= 96)))
str(ak.spl)# list (x[i], y[j], z = <matrix>[i,j])

## Now transform to simple  (x,y,z)  matrix / data.frame :
str(am <- interp2xyz(ak.spl))
str(ad <- interp2xyz(ak.spl, data.frame=TRUE))
## and they are the same:
stopifnot( am == ad | (is.na(am) & is.na(ad)) )
```

---

interpp   *Pointwise Bivariate Interpolation for Irregular Data*

Description

These functions implement bivariate interpolation onto a set of points for irregularly spaced input data. These functions are only for backward compatibility, use interpp instead.

If linear is \codeTRUE, linear interpolation is used in the triangles bounded by data points, otherwise cubic interpolation is done.

If extrap is FALSE, z-values for points outside the convex hull are returned as NA. No extrapolation can be performed for linear interpolation.

The interpp function handles duplicate (x,y) points in different ways. As default it will stop with an error message. But it can give duplicate points an unique z value according to the parameter duplicate (mean,median or any other user defined function).

The triangulation scheme used by interp works well if x and y have similar scales but will appear stretched if they have very different scales. The spreads of x and y must be within four orders of magnitude of each other for interpp to work.

Usage

```
interpp(x, y=NULL, z, xo, yo=NULL, linear=TRUE, extrap=FALSE,
        duplicate = "error", dupfun = NULL,
        jitter = 10^-12, jitter.iter = 6, jitter.random = FALSE,
        remove = !linear)
```

Arguments

x	vector of x-coordinates of data points or a SpatialPointsDataFrame object. Missing values are not accepted.
y	vector of y-coordinates of data points. Missing values are not accepted.
	If left as NULL indicates that x should be a SpatialPointsDataFrame and z names the variable of interest in this dataframe.

z   vector of z-coordinates of data points or a character variable naming the variable
                           of interest in the `SpatialPointsDataFrame` x.

                           Missing values are not accepted.

                           x, y, and z must be the same length (execpt if x is a `SpatialPointsDataFrame`)
                           and may contain no fewer than four points. The points of x and y cannot be
                           collinear, i.e, they cannot fall on the same line (two vectors x and y such that y
                           = ax + b for some a, b will not be accepted).

xo   vector of x-coordinates of points at which to evaluate the interpolating function.
                           If x is a `SpatialPointsDataFrame` this has also to be a `SpatialPointsDataFrame`.

yo   vector of y-coordinates of points at which to evaluate the interpolating function.

                           If operating on `SpatialPointsDataFrames` this is left as `NULL`

linear   logical – indicating wether linear or spline interpolation should be used.

extrap   logical flag: should extrapolation be used outside of the convex hull determined
                           by the data points? Not possible for linear interpolation.

duplicate   indicates how to handle duplicate data points. Possible values are `"error"` - pro-
                           duces an error message, `"strip"` - remove duplicate z values, `"mean"`,`"median"`,`"user"`
                           - calculate mean , median or user defined function of duplicate z values.

dupfun   this function is applied to duplicate points if duplicate=`"user"`

jitter   Jitter of amount of `diff(range(XX))*jitter` (XX=x or y) will be added to
                           coordinates if collinear points are detected. Afterwards interpolation will be
                           tried once again.

                           Note that the jitter is not generated randomly unless `jitter.random` is set to
                           `TRUE`. This ensures reproducable result. [`tri.mesh`](#) of package `tripack` uses the
                           same jitter mechanism. That means you can plot the triangulation on top of
                           the interpolation and see the same triangulation as used for interpolation, see
                           examples below.

jitter.iter   number of iterations to retry with jitter, amount will be increased in each itera-
                           tion by `iter^1.5`

jitter.random   logical, see `jitter`, defaults to `FALSE`

remove   logical, indicates whether Akimas removal of thin triangles along the border of
                           the convex hull should be performed, experimental setting! defaults to `!linear`,
                           so it will be left out for linear interpolation by default. For some point configu-
                           rations it is the only available option to skip this removal step.

Value

list with 3 components:

x   vector of x-coordinates of output points, the same as the input argument xo.

y   vector of y-coordinates of output points, the same as the input argument yo.

z   fitted z-values. The value z[i] is computed at the x,y point x[i], y[i].

If input is `SpatialPointsDataFrame` than an according `SpatialPointsDataFrame` is returned.

NOTE

Use `interp` if interpolation on a regular grid is wanted.

See interp for more details.

References

Akima, H. (1978). A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points. ACM Transactions on Mathematical Software, **4**, 148-164.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic polynomial. ACM Transactions on Mathematical Software, **22**, 362-371.

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

R. J. Renka and Ron Brown (1998). Remark on algorithm 761. ACM Transactions on Mathematical Software. **24**, 383-385.

See Also

contour, image, approxfun, splinefun, outer, expand.grid, interp, aspline.

Examples

```
data(akima)
# linear interpolation at points (1,2), (5,6) and (10,12)
akima.lip<-interpp(akima$x, akima$y, akima$z,c(1,5,10),c(2,6,12))
akima.lip$z
# spline interpolation at the same locations
akima.sip<-interpp(akima$x, akima$y, akima$z,c(1,5,10),c(2,6,12),
  linear=FALSE)
akima.sip$z
## Not run:
    ## interaction with sp objects:
    library(sp)
    ## take 30 sample points out of meuse grid:
    data(meuse.grid)
    m0 <- meuse.grid[sample(1:3103,30),]
    coordinates(m0) <- ~x+y
    ## interpolate on this 30 points:
    ## note: both "meuse" and "m0" are sp objects
    ## (SpatialPointsDataFrame) !!
    ## arguments z and xo have to given, y has to be omitted!
    ipp <- interpp(meuse,z="zinc",xo=m0)
    spplot(ipp)

## End(Not run)
```

---

interpp.old   *Pointwise Bivariate Interpolation for Irregular Data*

Description

If ncp is zero, linear interpolation is used in the triangles bounded by data points. Cubic interpolation is done if partial derivatives are used. If extrap is FALSE, z-values for points outside the convex hull are returned as NA. No extrapolation can be performed if ncp is zero.

The interpp function handles duplicate (x,y) points in different ways. As default it will stop with an error message. But it can give duplicate points an unique z value according to the parameter duplicate (mean,median or any other user defined function).

The triangulation scheme used by interp works well if x and y have similar scales but will appear stretched if they have very different scales. The spreads of x and y must be within four orders of magnitude of each other for interpp to work.

Usage

```
interpp.old(x, y, z, xo, yo, ncp = 0, extrap = FALSE,
                  duplicate = "error", dupfun = NULL)
interpp.new(x, y, z, xo, yo, extrap = FALSE,
                  duplicate = "error", dupfun = NULL)
```

Arguments

x	vector of x-coordinates of data points or a SpatialPointsDataFrame object. Missing values are not accepted.
y	vector of y-coordinates of data points. Missing values are not accepted.
	If left as NULL indicates that x should be a SpatialPointsDataFrame and z names the variable of interest in this dataframe.
z	vector of z-coordinates of data points or a character variable naming the variable of interest in the SpatialPointsDataFrame x.
	Missing values are not accepted.
	x, y, and z must be the same length (execpt if x is a SpatialPointsDataFrame) and may contain no fewer than four points. The points of x and y cannot be collinear, i.e, they cannot fall on the same line (two vectors x and y such that y = ax + b for some a, b will not be accepted).
xo	vector of x-coordinates of points at which to evaluate the interpolating function. If x is a SpatialPointsDataFrame this has also to be a SpatialPointsDataFrame.
yo	vector of y-coordinates of points at which to evaluate the interpolating function.
	If operating on SpatialPointsDataFrames this is left as NULL
ncp	deprecated, use parameter linear. Now only used by interpp.old().
	meaning was: number of additional points to be used in computing partial derivatives at each data point. ncp must be either 0 (partial derivatives are not used, = linear interpolation), or at least 2 but smaller than the number of data points (and smaller than 25).

extrap	logical flag: should extrapolation be used outside of the convex hull determined by the data points?
duplicate	indicates how to handle duplicate data points. Possible values are `"error"` - produces an error message, `"strip"` - remove duplicate z values, `"mean"`,`"median"`,`"user"` - calculate mean , median or user defined function of duplicate z values.
dupfun	this function is applied to duplicate points if `duplicate="user"`

Value

list with 3 components:

x	vector of x-coordinates of output points, the same as the input argument xo.
y	vector of y-coordinates of output points, the same as the input argument yo.
z	fitted z-values. The value z[i] is computed at the x,y point x[i], y[i].

If input is `SpatialPointsDataFrame` than an according `SpatialPointsDataFrame` is returned.

NOTE

Use `interp` if interpolation on a regular grid is wanted.

The two versions `interpp.old` and `interpp.new` are now deprecated, use `interpp` instead, see details there.

Earlier versions (pre 0.5-1) of `interpp` used the parameter ncp to choose between linear and cubic interpolation, this is now done by setting the logical parameter `linear`. Use of ncp is still possible, but is deprecated.

References

Akima, H. (1978). A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points. ACM Transactions on Mathematical Software, **4**, 148-164.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic polynomial. ACM Transactions on Mathematical Software, **22**, 362-371.

See Also

contour, image, approxfun, splinefun, outer, expand.grid, interp, aspline.

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