

# Package ‘EstemPMM’

November 7, 2025

**Type** Package

**Title** Polynomial Maximization Method for Non-Gaussian Regression

**Version** 0.1.1

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**Description** Implements the Polynomial Maximization Method ('PMM') for parameter estimation in linear and time series models when error distributions deviate from normality.

The 'PMM2' variant achieves lower variance parameter estimates compared to ordinary least squares ('OLS') when errors exhibit significant skewness. Includes methods for linear regression, 'AR'/'MA'/'ARMA'/'ARIMA' models, and bootstrap inference.

Methodology described in Zabolotnii, Warsza, and Tkachenko (2018) <[doi:10.1007/978-3-319-77179-3\\_75](https://doi.org/10.1007/978-3-319-77179-3_75)>,

Zabolotnii, Tkachenko, and Warsza (2022) <[doi:10.1007/978-3-031-03502-9\\_37](https://doi.org/10.1007/978-3-031-03502-9_37)>, and Zabolotnii, Tkachenko, and Warsza (2023) <[doi:10.1007/978-3-031-25844-2\\_21](https://doi.org/10.1007/978-3-031-25844-2_21)>.

**License** GPL-3

**Encoding** UTF-8

**Depends** R (>= 3.5.0)

**Imports** methods, stats, graphics, utils

**Suggests** dplyr, ggplot2, gridExtra, testthat (>= 3.0.0), rmarkdown, knitr, MASS

**LazyData** true

**RoxygenNote** 7.3.3

**Config/testthat/edition** 3

**URL** <https://github.com/SZabolotnii/EstemPMM>

**BugReports** <https://github.com/SZabolotnii/EstemPMM/issues>

**VignetteBuilder** knitr

**NeedsCompilation** no

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---

AIC,PMM2fit-method      *Calculate AIC for PMM2fit object*

---

**Description**

Calculate AIC for PMM2fit object

**Usage**

```
## S4 method for signature 'PMM2fit'  
AIC(object, ..., k = 2)
```

**Arguments**

|        |  |
|--------|--|
| object | PMM2fit object                                 |
| ...    | Additional arguments (not used)                |
| k      | Penalty per parameter to be used; default is 2 |

**Value**

AIC value

---

ARIMAPMM2-class      *S4 class for storing PMM2 ARIMA model results*

---

**Description**

S4 class for storing PMM2 ARIMA model results

---

arima\_pmm2      *Fit an ARIMA model using PMM2 (wrapper)*

---

**Description**

Fit an ARIMA model using PMM2 (wrapper)

## Usage

```
arima_pmm2(
  x,
  order = c(1, 1, 1),
  method = "pmm2",
  max_iter = 50,
  tol = 1e-06,
  include.mean = TRUE,
  initial = NULL,
  na.action = na.fail,
  regularize = TRUE,
  reg_lambda = 1e-08,
  verbose = FALSE
)
```

## Arguments

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data  |
| <code>order</code>        | Model order specification: - For AR models: a single integer (AR order) - For MA models: a single integer (MA order) - For ARMA models: vector $c(p, q)$ (AR and MA orders) - For ARIMA models: vector $c(p, d, q)$ (AR, differencing, and MA orders) |
| <code>method</code>       | String: estimation method, one of "pmm2" (default), "css", "ml", "yw", "ols"  |
| <code>max_iter</code>     | Integer: maximum number of iterations for the algorithm   |
| <code>tol</code>          | Numeric: tolerance for convergence  |
| <code>include.mean</code> | Logical: whether to include a mean (intercept) term   |
| <code>initial</code>      | List or vector of initial parameter estimates (optional)  |
| <code>na.action</code>    | Function for handling missing values, default is <code>na.fail</code>   |
| <code>regularize</code>   | Logical, add small values to diagonal for numerical stability   |
| <code>reg_lambda</code>   | Regularization parameter (if <code>regularize=TRUE</code> )   |
| <code>verbose</code>      | Logical: whether to print progress information  |

## Value

An S4 object of class ARIMAPMM2 containing fitted AR and MA coefficients, residual series, central moments, differencing order, intercept, original series, and convergence diagnostics.

## Description

S4 class for storing PMM2 ARMA model results

---

|                        |   |
|------------------------|---|
| <code>arma_pmm2</code> | <i>Fit an ARMA model using PMM2 (wrapper)</i> |
|------------------------|---|

---

## Description

Fit an ARMA model using PMM2 (wrapper)

## Usage

```
arma_pmm2(
  x,
  order = c(1, 1),
  method = "pmm2",
  max_iter = 50,
  tol = 1e-06,
  include.mean = TRUE,
  initial = NULL,
  na.action = na.fail,
  regularize = TRUE,
  reg_lambda = 1e-08,
  verbose = FALSE
)
```

## Arguments

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data  |
| <code>order</code>        | Model order specification: - For AR models: a single integer (AR order) - For MA models: a single integer (MA order) - For ARMA models: vector c(p, q) (AR and MA orders) - For ARIMA models: vector c(p, d, q) (AR, differencing, and MA orders) |
| <code>method</code>       | String: estimation method, one of "pmm2" (default), "css", "ml", "yw", "ols"  |
| <code>max_iter</code>     | Integer: maximum number of iterations for the algorithm   |
| <code>tol</code>          | Numeric: tolerance for convergence  |
| <code>include.mean</code> | Logical: whether to include a mean (intercept) term   |
| <code>initial</code>      | List or vector of initial parameter estimates (optional)  |
| <code>na.action</code>    | Function for handling missing values, default is <code>na.fail</code>   |
| <code>regularize</code>   | Logical, add small values to diagonal for numerical stability   |
| <code>reg_lambda</code>   | Regularization parameter (if <code>regularize=TRUE</code> )   |
| <code>verbose</code>      | Logical: whether to print progress information  |

## Value

An S4 object of class ARMAPMM2 containing fitted AR and MA coefficients, residuals, central moments, model specification, intercept, original series, and convergence diagnostics.

---

|              |   |
|--------------|---|
| ARPMM2-class | <i>S4 class for storing PMM2 AR model results</i> |
|--------------|---|

---

**Description**

S4 class for storing PMM2 AR model results

---

|         |   |
|---------|---|
| ar_pmm2 | <i>Fit an AR model using PMM2 (wrapper)</i> |
|---------|---|

---

**Description**

Fit an AR model using PMM2 (wrapper)

**Usage**

```
ar_pmm2(
  x,
  order = 1,
  method = "pmm2",
  max_iter = 50,
  tol = 1e-06,
  include.mean = TRUE,
  initial = NULL,
  na.action = na.fail,
  regularize = TRUE,
  reg_lambda = 1e-08,
  verbose = FALSE
)
```

**Arguments**

|              |   |
|--------------|---|
| x            | Numeric vector of time series data  |
| order        | Model order specification: - For AR models: a single integer (AR order) - For MA models: a single integer (MA order) - For ARMA models: vector c(p, q) (AR and MA orders) - For ARIMA models: vector c(p, d, q) (AR, differencing, and MA orders) |
| method       | String: estimation method, one of "pmm2" (default), "css", "ml", "yw", "ols"  |
| max_iter     | Integer: maximum number of iterations for the algorithm   |
| tol          | Numeric: tolerance for convergence  |
| include.mean | Logical: whether to include a mean (intercept) term   |
| initial      | List or vector of initial parameter estimates (optional)  |
| na.action    | Function for handling missing values, default is na.fail  |

|            |   |
|------------|---|
| regularize | Logical, add small values to diagonal for numerical stability |
| reg_lambda | Regularization parameter (if regularize=TRUE)                 |
| verbose    | Logical: whether to print progress information                |

**Value**

An S4 object of class ARPMM2 containing fitted autoregressive coefficients, residuals, central moment estimates (m2-m4), model order, intercept, original series, and convergence diagnostics.

BasePMM2-class

*Base S4 class for storing PMM2 model results***Description**

Base S4 class for storing PMM2 model results

**Slots**

|              |  |
|--------------|--|
| coefficients | numeric vector of estimated parameters                         |
| residuals    | numeric vector of final residuals                              |
| m2           | numeric second central moment of initial residuals             |
| m3           | numeric third central moment of initial residuals              |
| m4           | numeric fourth central moment of initial residuals             |
| convergence  | logical or integer code indicating whether algorithm converged |
| iterations   | numeric number of iterations performed                         |
| call         | original function call   |

coef,PM2fit-method

*Extract coefficients from PMM2fit object***Description**

Extract coefficients from PMM2fit object

**Usage**

```
## S4 method for signature 'PMM2fit'
coef(object, ...)
```

**Arguments**

|        |                                 |
|--------|---------------------------------|
| object | PMM2fit object                  |
| ...    | Additional arguments (not used) |

**Value**

Vector of coefficients

`coef,TS2fit-method`      *Extract coefficients from TS2fit object*

### Description

Extract coefficients from TS2fit object

### Usage

```
## S4 method for signature 'TS2fit'
coef(object, ...)
```

### Arguments

|                     |                                 |
|---------------------|---------------------------------|
| <code>object</code> | TS2fit object                   |
| <code>...</code>    | Additional arguments (not used) |

### Value

Named vector of coefficients

`compare_arima_methods` *Compare ARIMA methods*

### Description

Compare ARIMA methods

### Usage

```
compare_arima_methods(
  x,
  order = c(1, 1, 1),
  include.mean = TRUE,
  pmm2_args = list()
)
```

### Arguments

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data                              |
| <code>order</code>        | Model order specification (see <code>ts_pmm2</code> for format) |
| <code>include.mean</code> | Logical, whether to include intercept term                      |
| <code>pmm2_args</code>    | List of additional arguments to pass to <code>ts_pmm2()</code>  |

**Value**

A named list containing the fitted objects for each estimation approach (e.g., YW/OLS/MLE or CSS/ML alongside PMM2) plus two data frames: `coefficients` (side-by-side parameter estimates) and `residual_stats` (residual RSS, MAE, skewness, and kurtosis).

---

compare\_arma\_methods    *Compare ARMA methods*

---

**Description**

Compare ARMA methods

**Usage**

```
compare_arma_methods(  
  x,  
  order = c(1, 1),  
  include.mean = TRUE,  
  pmm2_args = list()  
)
```

**Arguments**

|              |   |
|--------------|---|
| x            | Numeric vector of time series data                              |
| order        | Model order specification (see <code>ts_pmm2</code> for format) |
| include.mean | Logical, whether to include intercept term                      |
| pmm2_args    | List of additional arguments to pass to <code>ts_pmm2()</code>  |

**Value**

A named list containing the fitted objects for each estimation approach (e.g., YW/OLS/MLE or CSS/ML alongside PMM2) plus two data frames: `coefficients` (side-by-side parameter estimates) and `residual_stats` (residual RSS, MAE, skewness, and kurtosis).

---

compare\_ar\_methods    *Compare AR methods*

---

**Description**

Compare AR methods

**Usage**

```
compare_ar_methods(x, order = 1, include.mean = TRUE, pmm2_args = list())
```

**Arguments**

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data                              |
| <code>order</code>        | Model order specification (see <code>ts_pmm2</code> for format) |
| <code>include.mean</code> | Logical, whether to include intercept term                      |
| <code>pmm2_args</code>    | List of additional arguments to pass to <code>ts_pmm2()</code>  |

**Value**

A named list containing the fitted objects for each estimation approach (e.g., YW/OLS/MLE or CSS/ML alongside PMM2) plus two data frames: `coefficients` (side-by-side parameter estimates) and `residual_stats` (residual RSS, MAE, skewness, and kurtosis).

---

|                                 |                           |
|---------------------------------|---------------------------|
| <code>compare_ma_methods</code> | <i>Compare MA methods</i> |
|---------------------------------|---------------------------|

---

**Description**

Compare MA methods

**Usage**

```
compare_ma_methods(x, order = 1, include.mean = TRUE, pmm2_args = list())
```

**Arguments**

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data                              |
| <code>order</code>        | Model order specification (see <code>ts_pmm2</code> for format) |
| <code>include.mean</code> | Logical, whether to include intercept term                      |
| <code>pmm2_args</code>    | List of additional arguments to pass to <code>ts_pmm2()</code>  |

**Value**

A named list containing the fitted objects for each estimation approach (e.g., YW/OLS/MLE or CSS/ML alongside PMM2) plus two data frames: `coefficients` (side-by-side parameter estimates) and `residual_stats` (residual RSS, MAE, skewness, and kurtosis).

---

|                                 |   |
|---------------------------------|---|
| <code>compare_ts_methods</code> | <i>Compare PMM2 with classical time series estimation methods</i> |
|---------------------------------|---|

---

### Description

Compare PMM2 with classical time series estimation methods

### Usage

```
compare_ts_methods(
  x,
  order,
  model_type = c("ar", "ma", "arma", "arima"),
  include.mean = TRUE,
  pmm2_args = list()
)
```

### Arguments

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data                              |
| <code>order</code>        | Model order specification (see <code>ts_pmm2</code> for format) |
| <code>model_type</code>   | Model type: "ar", "ma", "arma", or "arima"                      |
| <code>include.mean</code> | Logical, whether to include intercept term                      |
| <code>pmm2_args</code>    | List of additional arguments to pass to <code>ts_pmm2()</code>  |

### Value

A named list containing the fitted objects for each estimation approach (e.g., YW/OLS/MLE or CSS/ML alongside PMM2) plus two data frames: `coefficients` (side-by-side parameter estimates) and `residual_stats` (residual RSS, MAE, skewness, and kurtosis).

---

|                               |                              |
|-------------------------------|------------------------------|
| <code>compare_with_ols</code> | <i>Compare PMM2 with OLS</i> |
|-------------------------------|------------------------------|

---

### Description

Compare PMM2 with OLS

### Usage

```
compare_with_ols(formula, data, pmm2_args = list())
```

**Arguments**

|           |  |
|-----------|--|
| formula   | Model formula                          |
| data      | Data frame                             |
| pmm2_args | List of arguments to pass to lm_pmm2() |

**Value**

List with OLS and PMM2 fit objects

|                 |  |
|-----------------|--|
| compute_moments | <i>Calculate moments and cumulants of error distribution</i> |
|-----------------|--|

**Description**

Calculate moments and cumulants of error distribution

**Usage**

```
compute_moments(errors)
```

**Arguments**

|        |                          |
|--------|--------------------------|
| errors | numeric vector of errors |
|--------|--------------------------|

**Value**

list with moments, cumulants and theoretical variance reduction coefficient

|            |                             |
|------------|-----------------------------|
| DCOILWTICO | <i>WTI Crude Oil Prices</i> |
|------------|-----------------------------|

**Description**

Daily spot prices for West Texas Intermediate (WTI) crude oil in U.S. dollars per barrel.

**Usage**

```
DCOILWTICO
```

**Format**

A data frame with observations for each trading day:

**observation\_date** Date of observation in YYYY-MM-DD format

**DCOILWTICO** Crude Oil Price: West Texas Intermediate (WTI) in USD per barrel

**Source**

Federal Reserve Economic Data (FRED), Federal Reserve Bank of St. Louis <https://fred.stlouisfed.org/series/DCOILWTICO>

**Examples**

```
data(DCOILWTICO)
head(DCOILWTICO)
summary(DCOILWTICO$DCOILWTICO)
```

**fitted,PMM2fit-method** *Extract fitted values from PMM2fit object*

**Description**

Extract fitted values from PMM2fit object

**Usage**

```
## S4 method for signature 'PMM2fit'
fitted(object, data = NULL, ...)
```

**Arguments**

|        |  |
|--------|--|
| object | PMM2fit object   |
| data   | Optional data source for model reconstruction, if object does not contain saved data |
| ...    | Additional arguments (not used)  |

**Value**

Vector of fitted values

**fitted,TS2fit-method** *Extract fitted values from TS2fit object*

**Description**

Extract fitted values from TS2fit object

**Usage**

```
## S4 method for signature 'TS2fit'
fitted(object, ...)
```

**Arguments**

|        |                                 |
|--------|---------------------------------|
| object | TS2fit object                   |
| ...    | Additional arguments (not used) |

**Value**

Vector of fitted values

**lm\_pmm2**

*PMM2: Main function for PMM2 (S=2)*

**Description**

Fits a linear model using the Polynomial Maximization Method (order 2), which is robust to non-Gaussian errors.

**Usage**

```
lm_pmm2(
  formula,
  data,
  max_iter = 50,
  tol = 1e-06,
  regularize = TRUE,
  reg_lambda = 1e-08,
  na.action = na.fail,
  weights = NULL,
  verbose = FALSE
)
```

**Arguments**

|            |  |
|------------|--|
| formula    | R formula for the model                                      |
| data       | data.frame containing variables in the formula               |
| max_iter   | integer: maximum number of iterations for the algorithm      |
| tol        | numeric: tolerance for convergence                           |
| regularize | logical: add small value to diagonal for numerical stability |
| reg_lambda | numeric: regularization parameter (if regularize=TRUE)       |
| na.action  | function for handling missing values, default is na.fail     |
| weights    | optional weight vector (not yet implemented)                 |
| verbose    | logical: whether to print progress information               |

## Details

The PMM2 algorithm works as follows:

1. Fits ordinary least squares (OLS) regression to obtain initial estimates
2. Computes central moments ( $m_2$ ,  $m_3$ ,  $m_4$ ) from OLS residuals
3. Iteratively improves parameter estimates using a gradient-based approach

PMM2 is especially useful when error terms are not Gaussian.

## Value

S4 object of class PMM2fit

## Examples

```
set.seed(123)
n <- 80
x <- rnorm(n)
y <- 2 + 3 * x + rt(n, df = 3)
dat <- data.frame(y = y, x = x)

fit <- lm_pmm2(y ~ x, data = dat)
summary(fit, formula = y ~ x, data = dat)
```

MAPMM2-class

*S4 class for storing PMM2 MA model results*

## Description

S4 class for storing PMM2 MA model results

ma\_pmm2

*Fit an MA model using PMM2 (wrapper)*

## Description

Fit an MA model using PMM2 (wrapper)

**Usage**

```
ma_pmm2(
  x,
  order = 1,
  method = "pmm2",
  max_iter = 50,
  tol = 1e-06,
  include.mean = TRUE,
  initial = NULL,
  na.action = na.fail,
  regularize = TRUE,
  reg_lambda = 1e-08,
  verbose = FALSE
)
```

**Arguments**

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data  |
| <code>order</code>        | Model order specification: - For AR models: a single integer (AR order) - For MA models: a single integer (MA order) - For ARMA models: vector c(p, q) (AR and MA orders) - For ARIMA models: vector c(p, d, q) (AR, differencing, and MA orders) |
| <code>method</code>       | String: estimation method, one of "pmm2" (default), "css", "ml", "yw", "ols"  |
| <code>max_iter</code>     | Integer: maximum number of iterations for the algorithm   |
| <code>tol</code>          | Numeric: tolerance for convergence  |
| <code>include.mean</code> | Logical: whether to include a mean (intercept) term   |
| <code>initial</code>      | List or vector of initial parameter estimates (optional)  |
| <code>na.action</code>    | Function for handling missing values, default is <code>na.fail</code>   |
| <code>regularize</code>   | Logical, add small values to diagonal for numerical stability   |
| <code>reg_lambda</code>   | Regularization parameter (if <code>regularize=TRUE</code> )   |
| <code>verbose</code>      | Logical: whether to print progress information  |

**Value**

An S4 object of class MAPMM2 containing moving-average coefficients, residual innovations, central moments, model order, intercept, original series, and convergence diagnostics.

**plot,PMM2fit,missing-method**

*Plot diagnostic plots for PMM2fit object*

**Description**

Plot diagnostic plots for PMM2fit object

**Usage**

```
## S4 method for signature 'PMM2fit,missing'
plot(x, y, which = 1:4, ...)
```

**Arguments**

|       |   |
|-------|---|
| x     | PMM2fit object                                    |
| y     | Not used (compatibility with generic)             |
| which | Set of plots to display (values 1-4)              |
| ...   | Additional arguments passed to plotting functions |

**Value**

Invisibly returns the input object

**plot,TS2fit,missing-method**

*Build diagnostic plots for TS2fit objects*

**Description**

Build diagnostic plots for TS2fit objects

**Usage**

```
## S4 method for signature 'TS2fit,missing'
plot(x, y, which = c(1:4), ...)
```

**Arguments**

|       |  |
|-------|--|
| x     | TS2fit object                                    |
| y     | Not used (for S4 method compatibility)           |
| which | Integer vector indicating which plots to produce |
| ...   | additional arguments passed to plot functions    |

**Value**

Invisibly returns x

`plot_pmm2_bootstrap`     *Plot bootstrap distributions for PMM2 fit*

### Description

Plot bootstrap distributions for PMM2 fit

### Usage

```
plot_pmm2_bootstrap(object, coefficients = NULL)
```

### Arguments

|                           |   |
|---------------------------|---|
| <code>object</code>       | Result from <code>pmm2_inference</code>     |
| <code>coefficients</code> | Which coefficients to plot, defaults to all |

### Value

Invisibly returns histogram information

PMM2fit-class     *S4 class for storing PMM2 regression model results*

### Description

Class for storing results of linear model estimation using PMM2

### Slots

|                           |  |
|---------------------------|--|
| <code>coefficients</code> | numeric vector of estimated parameters                         |
| <code>residuals</code>    | numeric vector of final residuals                              |
| <code>m2</code>           | numeric second central moment of initial residuals             |
| <code>m3</code>           | numeric third central moment of initial residuals              |
| <code>m4</code>           | numeric fourth central moment of initial residuals             |
| <code>convergence</code>  | logical or integer code indicating whether algorithm converged |
| <code>iterations</code>   | numeric number of iterations performed                         |
| <code>call</code>         | original function call   |

**Slots**

- coefficients** Estimated coefficients
- residuals** Final residuals
- m2** Second central moment
- m3** Third central moment
- m4** Fourth central moment
- convergence** Convergence status
- iterations** Number of iterations performed
- call** Original call

pmm2\_inference      *Bootstrap inference for PMM2 fit*

**Description**

Bootstrap inference for PMM2 fit

**Usage**

```
pmm2_inference(
  object,
  formula,
  data,
  B = 200,
  seed = NULL,
  parallel = FALSE,
  cores = NULL
)
```

**Arguments**

|                 |  |
|-----------------|--|
| <b>object</b>   | object of class PMM2fit  |
| <b>formula</b>  | the same formula that was used initially                               |
| <b>data</b>     | data frame that was used initially                                     |
| <b>B</b>        | number of bootstrap replications                                       |
| <b>seed</b>     | (optional) for reproducibility   |
| <b>parallel</b> | logical, whether to use parallel computing                             |
| <b>cores</b>    | number of cores to use for parallel computing, defaults to auto-detect |

**Value**

data.frame with columns: Estimate, Std.Error, t.value, p.value

---

pmm2\_monte\_carlo\_compare

*Monte Carlo comparison of PMM2 estimation methods*

---

## Description

Function generates time series for given models, repeatedly estimates parameters using different methods and compares their accuracy by MSE criterion. Additionally outputs theoretical and empirical characteristics of the innovation distribution (skewness, excess kurtosis, theoretical gain of PMM2).

## Usage

```
pmm2_monte_carlo_compare(
  model_specs,
  methods = c("css", "pmm2"),
  n,
  n_sim,
  innovations = list(type = "gaussian"),
  seed = NULL,
  include.mean = TRUE,
  progress = interactive(),
  verbose = FALSE
)
```

## Arguments

|              |   |
|--------------|---|
| model_specs  | List of model specifications. Each element must contain:<br><b>model</b> "ar", "ma" or "arma"<br><b>order</b> order (for AR/MA) or vector c(p, q) for ARMA<br><b>theta</b> numeric vector of true parameters; for ARMA a list list(ar = . . . , ma = . . . )<br><b>label</b> (optional) model name in report<br><b>innovations</b> (optional) description of innovation distribution: list(type = "gamma", shape = 2), list(type = "student_t", df = 5), etc. Can also pass an arbitrary generation function via generator. |
| methods      | Vector of estimation methods (e.g., c("css", "pmm2")). The first method is considered baseline for relative MSE calculation.  |
| n            | Sample size for simulation.   |
| n_sim        | Number of Monte Carlo experiments.  |
| innovations  | Function or distribution description, used by default for all models (if not specified in spec).  |
| seed         | Initial seed for random number generator (optional).  |
| include.mean | Logical flag: whether to include intercept during estimation.   |
| progress     | Logical flag: print Monte Carlo progress.   |
| verbose      | Whether to print diagnostic messages on failures.   |

**Value**

List with three components:

**parameter\_results** MSE and relative MSE for each parameter

**summary** Averaged MSE over parameters for each model/method

**gain** Comparison of theoretical and empirical PMM2 gain

**pmm2\_variance\_factor** *Calculate theoretical skewness, kurtosis coefficients and variance reduction factor*

**Description**

Calculate theoretical skewness, kurtosis coefficients and variance reduction factor

**Usage**

```
pmm2_variance_factor(m2, m3, m4)
```

**Arguments**

|            |  |
|------------|--|
| m2, m3, m4 | central moments of second, third and fourth orders |
|------------|--|

**Value**

List with fields c3, c4 and g

**pmm2\_variance\_matrices**

*Calculate theoretical variance matrices for OLS and PMM2*

**Description**

Calculate theoretical variance matrices for OLS and PMM2

**Usage**

```
pmm2_variance_matrices(X, m2, m3, m4)
```

**Arguments**

|   |                                   |
|---|-----------------------------------|
| X | Design matrix with column of ones |
|---|-----------------------------------|

|            |                                  |
|------------|----------------------------------|
| m2, m3, m4 | central moments of OLS residuals |
|------------|----------------------------------|

**Value**

List with fields ols, pmm2, c3, c4, g

---

**pmm\_kurtosis**      *Calculate kurtosis from data*

---

**Description**

Calculate kurtosis from data

**Usage**

```
pmm_kurtosis(x, excess = TRUE)
```

**Arguments**

|        |   |
|--------|---|
| x      | numeric vector  |
| excess | logical, whether to return excess kurtosis (kurtosis - 3) |

**Value**

Kurtosis value

---

**pmm\_skewness**      *Calculate skewness from data*

---

**Description**

Calculate skewness from data

**Usage**

```
pmm_skewness(x)
```

**Arguments**

|   |                |
|---|----------------|
| x | numeric vector |
|---|----------------|

**Value**

Skewness value

---

**predict,PMM2fit-method**

*Prediction method for PMM2fit objects*

---

**Description**

Prediction method for PMM2fit objects

**Usage**

```
## S4 method for signature 'PMM2fit'  
predict(object, newdata = NULL, debug = FALSE, ...)
```

**Arguments**

|         |  |
|---------|--|
| object  | PMM2fit object                                     |
| newdata | New data frame for prediction                      |
| debug   | Logical value, whether to output debug information |
| ...     | additional arguments (not used)                    |

**Value**

Vector of predictions

---

---

**predict,TS2fit-method** *Prediction method for TS2fit objects*

---

**Description**

Prediction method for TS2fit objects

**Usage**

```
## S4 method for signature 'TS2fit'  
predict(object, n.ahead = 1, ...)
```

**Arguments**

|         |                                      |
|---------|--------------------------------------|
| object  | TS2fit object                        |
| n.ahead | Number of steps ahead for prediction |
| ...     | additional arguments (not used)      |

**Value**

Vector or list of predictions, depending on model type

**residuals,PMM2fit-method**

*Extract residuals from PMM2fit object*

### Description

Extract residuals from PMM2fit object

### Usage

```
## S4 method for signature 'PMM2fit'
residuals(object, ...)
```

### Arguments

|        |                                 |
|--------|---------------------------------|
| object | PMM2fit object                  |
| ...    | Additional arguments (not used) |

### Value

Vector of residuals

**residuals,TS2fit-method**

*Extract residuals from TS2fit object*

### Description

Extract residuals from TS2fit object

### Usage

```
## S4 method for signature 'TS2fit'
residuals(object, ...)
```

### Arguments

|        |                                 |
|--------|---------------------------------|
| object | TS2fit object                   |
| ...    | Additional arguments (not used) |

### Value

Vector of residuals (innovations)

---

**summary , PMM2fit-method**

*Generic summary method for PMM2fit objects*

---

**Description**

Generic summary method for PMM2fit objects

**Usage**

```
## S4 method for signature 'PMM2fit'  
summary(object, formula = NULL, data = NULL, B = 100, ...)
```

**Arguments**

|         |  |
|---------|--|
| object  | object of class "PMM2fit"                                  |
| formula | (optional) formula used for the model                      |
| data    | (optional) data used                                       |
| B       | number of bootstrap replications for statistical inference |
| ...     | additional arguments (not used)                            |

**Value**

Prints summary to console; returns object (invisibly).

---

**summary , TS2fit-method** *Generic summary method for TS2fit objects*

---

**Description**

Generic summary method for TS2fit objects

**Usage**

```
## S4 method for signature 'TS2fit'  
summary(object, ...)
```

**Arguments**

|        |                                      |
|--------|--------------------------------------|
| object | object of class "TS2fit" or subclass |
| ...    | additional arguments (not used)      |

**Value**

Prints summary to console; returns object (invisibly).

---

**TS2fit-class***Base S4 class for storing PMM2 time series model results*

---

## Description

Base class for storing results of time series model estimation using PMM2

### Slots

**coefficients** numeric vector of estimated parameters  
**residuals** numeric vector of final residuals  
**m2** numeric second central moment of initial residuals  
**m3** numeric third central moment of initial residuals  
**m4** numeric fourth central moment of initial residuals  
**convergence** logical or integer code indicating whether algorithm converged  
**iterations** numeric number of iterations performed  
**call** original function call  
**model\_type** character string indicating model type  
**intercept** numeric value of intercept  
**original\_series** numeric vector of original time series  
**order** list of order parameters

### Slots

**coefficients** Estimated coefficients  
**residuals** Final residuals  
**m2** Second central moment  
**m3** Third central moment  
**m4** Fourth central moment  
**convergence** Convergence status  
**iterations** Number of iterations performed  
**call** Original call  
**model\_type** Model type  
**intercept** Intercept  
**original\_series** Original time series  
**order** Model orders

---

|                      |  |
|----------------------|--|
| <code>ts_pmm2</code> | <i>Fit a time series model using the PMM2 method</i> |
|----------------------|--|

---

## Description

Fit a time series model using the PMM2 method

## Usage

```
ts_pmm2(
  x,
  order,
  model_type = c("ar", "ma", "arma", "arima"),
  method = "pmm2",
  max_iter = 50,
  tol = 1e-06,
  include.mean = TRUE,
  initial = NULL,
  na.action = na.fail,
  regularize = TRUE,
  reg_lambda = 1e-08,
  verbose = FALSE
)
```

## Arguments

|                           |   |
|---------------------------|---|
| <code>x</code>            | Numeric vector of time series data  |
| <code>order</code>        | Model order specification: - For AR models: a single integer (AR order) - For MA models: a single integer (MA order) - For ARMA models: vector c(p, q) (AR and MA orders) - For ARIMA models: vector c(p, d, q) (AR, differencing, and MA orders) |
| <code>model_type</code>   | String specifying the model type: "ar", "ma", "arma", or "arima"  |
| <code>method</code>       | String: estimation method, one of "pmm2" (default), "css", "ml", "yw", "ols"  |
| <code>max_iter</code>     | Integer: maximum number of iterations for the algorithm   |
| <code>tol</code>          | Numeric: tolerance for convergence  |
| <code>include.mean</code> | Logical: whether to include a mean (intercept) term   |
| <code>initial</code>      | List or vector of initial parameter estimates (optional)  |
| <code>na.action</code>    | Function for handling missing values, default is <code>na.fail</code>   |
| <code>regularize</code>   | Logical, add small values to diagonal for numerical stability   |
| <code>reg_lambda</code>   | Regularization parameter (if <code>regularize=TRUE</code> )   |
| <code>verbose</code>      | Logical: whether to print progress information  |

## Details

The PMM2 algorithm works as follows:

1. Fits an initial model using a standard method (OLS, Yule-Walker, CSS or ML)
2. Computes central moments ( $m_2$ ,  $m_3$ ,  $m_4$ ) from initial residuals/innovations
3. Uses these moments with a specialized solver (pmm2\_algorithm) to find robust parameter estimates

## Value

An S4 object TS2fit of the corresponding subclass

**ts\_pmm2\_inference**

*Bootstrap inference for PMM2 time series models*

## Description

Bootstrap inference for PMM2 time series models

## Usage

```
ts_pmm2_inference(
  object,
  x = NULL,
  B = 200,
  seed = NULL,
  block_length = NULL,
  method = c("residual", "block"),
  parallel = FALSE,
  cores = NULL,
  debug = FALSE
)
```

## Arguments

|                     |  |
|---------------------|--|
| <b>object</b>       | object of class TS2fit   |
| <b>x</b>            | (optional) original time series; if NULL, uses <code>object@original_series</code> |
| <b>B</b>            | number of bootstrap replications   |
| <b>seed</b>         | (optional) for reproducibility   |
| <b>block_length</b> | block length for block bootstrap; if NULL, uses heuristic value                    |
| <b>method</b>       | bootstrap type: "residual" or "block"  |
| <b>parallel</b>     | logical, whether to use parallel computing   |
| <b>cores</b>        | number of cores for parallel computing   |
| <b>debug</b>        | logical, whether to output additional diagnostic information                       |

**Value**

data.frame with columns: Estimate, Std.Error, t.value, p.value

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