# Package 'DensParcorr'

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Type Package
<b>Title</b> Dens-Based Method for Partial Correlation Estimation in Large Scale Brain Networks
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<b>Depends</b> R ( $>= 3.1.0$ ), clime, gplots
<b>Description</b> Provide a Dens-based method for estimating functional connection in large scale brain networks using partial correlation.
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DensParcorr Conduct the Dens-Based approach for partial correlation estimation

## Description

This function is to conduct the *Dens*-based approach for partial correlation estimation in large scale brain network study.

DensParcorr is the main function in this package. prec2dens and prec2part are sub-functions called by DensParcorr.

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#### Usage

#### **Arguments**

data Input data matrix with dimension of TxM where T is the number of observations

and M is the number of nodes. For example, in fMRI data the T is the number

of scans.

select Whether to conduct the *Dens*-based selection. If FALSE, output will only con-

tain the estimated partial correlation list and precision matrix list corresponding to the default tuning parameter series ranging from 1e-8 to 0.6. If TRUE, the ouput will include the previous results and the selected partial correlation matrix and percision matrix corresponding to the specified density level. Default is

FALSE.

dens.level Specify the density level in *Dens*-based tuning parameter selection method, in-

cluding the plateau based density selection (dens.level = "plateau") and p percentage density selection (dens.level = p, 0 ). This option is valid only

when select=TRUE. See Details. Default is "plateau".

plateau.thresh The criterion to select the plateau. This option is valid only when select=TRUE.

See Details. Default value is 0.01.

Parcorr.est Previous output from DensParcorr function.

directory The directory to output the figures and precision matrices and the partial correla-

tion matrices. The default (directory=NULL) is to output in the current working

directory.

1 The lambda value for estimating the precision matrix ranging from 0 to 1. The

default is NULL. If specified, no extra Dens-based step will be conducted.

#### **Details**

This function implements the statistical method proposed in Wang et al. (2016) to estimate partial correlation matrix for studying direct connectivity in large-scale brain network. The method derives partial correlation based on the precision matrix estimated via Constrained L1-minimization Approach (CLIME) (Cai et al., 2011). This function applies the *Dens*-based tuning parameter selection method in Wang et al. (2016) to help select an appropriate tuning parameter for sparsity control in the network estimation. Below is the breif step of *Dens*-based approach.

First, we specify a series of tuning parameters  $\{\lambda_n\}$ . Then, based on  $\{\lambda_n\}$  we esimate a list of precision matrices  $\Omega(\lambda_n)$  and and evaluate the density level of each precision matrix based on the Dens criterion function in equation (5) of Wang et al. (2016). This will provide the users the profile of the density level corresponding to the series of tuning parameters in  $\{\lambda_n\}$ . Users can use the dens.level option to specify the desired density level in the precision matrix estimation. If dens.level="plateau", the function will select the plateau point  $\lambda_{platu}$  in the density profile based on the plateau.thresh and output the precision matrix  $\Omega(\lambda_{platu})$ . If dens.level=p and 0<p<1, the function will select the tuning parameter  $\lambda_p$  to achieve p percentage density and output the precision matrix  $\Omega(\lambda_p)$ . Then, the partial correlation matrix will be derived from the precision matrix.

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Further details can be found in the Reference.

The density profile and the heatmaps of precision matrices and partial correlation matrices will be saved in directory, and the esimated list of precision matrices and partial correlation matrices will also be saved in directory.

When users would like to run the function multiple times on the same input data for different dens.level, it is computationally more efficient to read in the previous output from DensParcorr to Parcorr.est so that the function won't need to re-estimate the partial correlations based on the previous tuning parameters.

#### Value

An R list from DensParcorr containing the following terms:

selected.partial.corr

Selected Partial Correlation matrix corresponding to dens.level. Only when select=TRUE.

selected.precision

Selected Precision matrix corresponding to dens.level. Only when select=TRUE.

selected.lambda

Selected tuning parameter corresponding to dens.level. Only when select=TRUE.

lambda.list The series of tuning parameters used for esimation and density profile.

partial.corr.list

Estimated Partial Correlation matrix list corresponding to lambda.list.

precision.list Estimated Precision matrix list corresponding to lambda.list.

Dens Actual density levels for estimated precision matrix list.

Dens.Percentage

Actual percentage density levels for estimated precision matrix list.

selection.method

The method used for tuning parameter selection. For percentage *Dens* selection, this value will include the actual *Dens* precentage and the nominal *Dens* percentage. Only when select=TRUE.

## Author(s)

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### References

Wang, Y., Kang, J., Kemmer P. and Guo, Y. (2016). An efficient and reliable statistical method for estimating functional connectivity in large scale brain networks using partial correlation. Front. Neurosci. 10:123. doi: 10.3389/fnins.2016.00123

Cai, T.T., Liu, W., and Luo, X. (2011). A constrained  $\ell_1$  minimization approach for sparse precision matrix estimation. Journal of the American Statistical Association 106(494): 594-607.

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## **Examples**

```
# require(gplots)
# require(clime)
## Simulated the data to use.
# data = matrix(rnorm(200),ncol=20)
##### Example 1: Estimate the partial correlation matrices for the
##### default series of tuning parameters.
# t0 = proc.time()[3]
# dens.est = DensParcorr(data,select=FALSE)
# proc.time()[3]-t0
##### Example 2: Estimate the network that reaches 40% density level.
# partial.dens.est = DensParcorr(data,dens.level =.4,select=TRUE)
###### Example 3: Now, estimate the 60% density level network based
###### on the same data. To speed up computation, we read in the
###### previous output from Example 2 into Parcorr.est
# t0 = proc.time()[3]
# partial.dens.est2 = DensParcorr(data, Parcorr.est = partial.dens.est,
                                  dens.level=.6, select=TRUE)
# proc.time()[3]-t0
```

prec2dens

Calculate Dens value from Precision Matrix

#### **Description**

This function evaluates the density level of a precision matrix based on the Dens criterion function in equation (5) of Wang et al. (2016).

## Usage

```
prec2dens(precision)
```

#### **Arguments**

precision Input precision matrix (symmetric and positive definite).

#### Value

Density level from Precision matrix.

#### Author(s)

```
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```

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#### References

Wang, Y., Kang, J., Kemmer P. and Guo, Y. (2016). An efficient and reliable statistical method for estimating functional connectivity in large scale brain networks using partial correlation. Front. Neurosci. 10:123. doi: 10.3389/fnins.2016.00123

prec2part

Calculate Partial Correlation Matrix from Precision Matrix

## Description

This function is to derive the partial correlation matrix from the precision matrix.

## Usage

prec2part(Precision)

#### **Arguments**

Precision

Input precision matrix (symmetric and positive definite).

#### Value

Calculated partial correlation matrix.

## Author(s)

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#### References

Wang, Y., Kang, J., Kemmer P. and Guo, Y. (2016). An efficient and reliable statistical method for estimating functional connectivity in large scale brain networks using partial correlation. Front. Neurosci. 10:123. doi: 10.3389/fnins.2016.00123

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