Package 'ICSsmoothing'

January 10, 2024

tridiag_inv_general	Type Package					
Author Juraj Hudak, Viliam Kacala, Csaba Torok, Lubomir Antoni Maintainer Lubomir Antoni 1 Description We construct the explicit form of clamped cubic interpolating spline (both uniform-knots are equidistant and non-uniform - knots are arbitrary). Using this form, we propose a linear regression model suitable for real data smoothing. Depends R (>= 3.5.0), polynom, ggplot2 License GPL-2 Encoding UTF-8 LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit cics_explicit cics_explicit cics_explicit cics_explicit cics_unif_explicit sics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Title Data Smoothing by Interpolating Cubic Splines					
Maintainer Lubomir Antoni <lubomir.antoni@upjs.sk> Description We construct the explicit form of clamped cubic interpolating spline (both uniform-knots are equidistant and non-uniform-knots are arbitrary). Using this form, we propose a linear regression model suitable for real data smoothing. Depends R (>= 3.5.0), polynom, ggplot2 License GPL-2 Encoding UTF-8 LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit cics_explicit cics_unif_explicit cics_unif_explicit forecast_demo hermite_bf_matrix [16]</lubomir.antoni@upjs.sk>	Version 1.2.8					
Description We construct the explicit form of clamped cubic interpolating spline (both uniform-knots are equidistant and non-uniform - knots are arbitrary). Using this form, we propose a linear regression model suitable for real data smoothing. Depends R (>= 3.5.0), polynom, ggplot2 License GPL-2 Encoding UTF-8 LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit cics_explicit smooth cics_unif_explicit smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Author Juraj Hudak, Viliam Kacala, Csaba Torok, Lubomir Antoni					
knots are equidistant and non-uniform - knots are arbitrary). Using this form, we propose a linear regression model suitable for real data smoothing. Depends R (>= 3.5.0), polynom, ggplot2 License GPL-2 Encoding UTF-8 LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit cics_unif_explicit cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Maintainer Lubomir Antoni < lubomir antoni@upjs.sk>					
License GPL-2 Encoding UTF-8 LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general LazyData RoxygenNote RoyygenNote RoxygenNote RoxygenNote RoxygenNote RoxygenNote RoxygenNote RoxygenNote RoxygenNote RoyygenNote R	knots are equidistant and non-uniform - knots are arbitrary). Using this form, we propose a lin-					
Encoding UTF-8 LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Depends R (>= 3.5.0), polynom, ggplot2					
LazyData true RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit cics_explicit cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	License GPL-2					
RoxygenNote 7.2.3 Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit	Encoding UTF-8					
Suggests knitr, rmarkdown, testthat VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	LazyData true					
VignetteBuilder knitr NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	RoxygenNote 7.2.3					
NeedsCompilation no Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Suggests knitr, rmarkdown, testthat					
Repository CRAN Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	VignetteBuilder knitr					
Date/Publication 2024-01-10 10:33:21 UTC R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	NeedsCompilation no					
R topics documented: CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Repository CRAN					
CERN cics_explicit cics_explicit_smooth cics_unif_explicit cics_unif_explicit_smooth explicit_spline forecast_demo hermite_bf_matrix tridiag_inv_general	Date/Publication 2024-01-10 10:33:21 UTC					
cics_explicit	R topics documented:					
tridiag_inv_unit_by_sums	cics_explicit					

2 cics_explicit

Index 12

CERN

277 measurements of the cross sections for π^-p collision (nuclear physics).

Description

277 measurements of the cross sections for $\pi^- p$ collision (nuclear physics).

Usage

CERN

Format

A data frame with 277 elements.

Source

```
https://link.springer.com/article/10.1007/BF02683433
```

cics_explicit

Construct the explicit form of non-uniform clamped interpolating cubic spline (NcICS).

Description

cics_explicit constructs the explicit form of non-uniform clamped interpolating cubic spline (via Hermite cubic spline) for nodes uu, function values yy and exterior-node derivatives d.

Usage

```
cics_explicit(
   uu,
   yy,
   d,
   clrs = c("blue", "red"),
   xlab = NULL,
   ylab = NULL,
   title = NULL
)
```

cics_explicit 3

Arguments

ι	uu	a vector of arbitrary nodes (ordered ascendingly), with magnitude n+2, $n \ge 1$.
,	уу	a vector of function values pertaining to nodes in uu.
(b	a vector of two values of derivative, in the first and the last node of uu.
(clrs	a vector of colours that are used alternately to plot the graph of spline's components.
)	klab	a title (optional parameter) for the x axis.
,	ylab	a title (optional parameter) for the y axis.
1	title	a title (optional parameter) for the plot.

Value

a list with components

spline_coeffs matrix, whose i-th row contains coefficients of non-uniform ICS's i-th component.
spline_polynomials

list of NcICS's components string representations.

B 4-element array of (n+1)x(n+4) matrices, whereas element in i-th row and j-th column of 1-th matrix contains coefficient by x^{1-1} of cubic polynomial that is in i-th row and j-th column of matrix B from spline's explicit form

$$S = B.\gamma$$
.

gamma $\gamma=$ vector of spline coefficients - function values and exterior-node derivatives that takes part in the explicit form $S=B.\gamma.$

 $\begin{array}{ll} \mbox{aux_BF} & \mbox{A basis function of the spline} \\ \mbox{aux_tridiag_inverse} \end{array}$

An inverse of the tridiagonal matrix used for spline derivatives construction

Examples

```
cics_explicit(
    uu = c(1, 2.2, 3, 3.8, 7),
    CERN$y[1:5],
    d=c(0,-2),
    xlab="X axis",
    ylab="Y axis"
)

uu <- c(0, 1, 4, 6);
yy <- c(4, 5, 2, 1.8);
sp <- cics_explicit(uu, yy, c(1,0))
sp$spline_polynomials
### <~~>
### Spline components' coefficients
explicit_spline(sp$B, sp$gamma)
sp$spline_coeffs == .Last.value
```

4 cics_explicit_smooth

cics_explicit_smooth Smooth given data set by k-component non-uniform clamped interpolating spline (NcICS).

Description

cics_explicit_smooth constructs the non-uniform clamped interpolating spline with k components that smoothes given data set $\{(xx[i],yy[i]), i=1...length(xx)\}.$

Usage

```
cics_explicit_smooth(
    xx,
    yy,
    uu,
    clrs = c("blue", "red"),
    d,
    xlab = NULL,
    ylab = NULL,
    title = NULL
)
```

Arguments

xx	a vector of data set's x-coordinates (that are in increasing order).
уу	a vector of data set's y-coordinates.
uu	a vector of arbitrary nodes, based on which we construct the smoothing spline. $uu[1]$ and $uu[length(uu)]$ must be equal to $xx[1]$ and $xx[length(xx)]$, respectively.
clrs	a vector of colours that are used alternately to plot the graph of spline's components.
d	a vector (optional parameter) that contains two values of derivative, in the first and the last node from uu. If missing, values of derivative are estimated by given linear regression model. If present, their contribution is removed from linear model and only function values are estimated.
xlab	a title (optional parameter) for the x axis.
ylab	a title (optional parameter) for the y axis.
title	a title (optional parameter) for the plot.

Value

a list with components

cics_unif_explicit 5

```
est_spline_coeffs
```

4-element array of (k)x(k+3) matrices, whereas element in i-th row and j-th of 1-th matrix contains coefficient by x^{1-1} of cubic polynomial, which is in i-th row and j-th column of matrix B from smoothing spline's explicit form

$$S = B.\gamma$$
.

est_spline_polynomials

list of string representations of smoothing NcICS.

est_gamma vector of estimated smoothing spline's coefficients (function values and exterior-

node derivatives).

aux_BF A basis function of the spline

aux_tridiag_inverse

An inverse of the tridiagonal matrix used for spline derivatives construction

aux_M An estimation matrix used to compute est_gamma

Examples

```
cics_explicit_smooth(
xx = CERN$x,
yy = CERN$y,
d = c(0, 1),
uu = c(1, sort(runif(20,1,277)), 277),
xlab = "X axis",
ylab = "Y axis"
yy \leftarrow c(1, 2, 3, 4, 3, 2, 2, 3, 5, 6, 7, 6, 5, 5, 4, 3, 2, 1, 0)
xx <- c(1:length(yy))</pre>
uu < -c(1,7,10,19)
sp <- cics_explicit_smooth(xx,yy,uu)</pre>
### We can change the derivatives at the end nodes:
sp \leftarrow cics_explicit_smooth(xx,yy, uu, d=c(3,-7/10))
### CERN:
uu <- c(1, 15, 26, 63, 73, 88, 103, 117, 132, 200, 203, 219, 258, 277)
sp <- cics_explicit_smooth(</pre>
  xx = CERN$x,
  yy = CERN$y,
  d = c(1, 0),
  uu
)
```

cics_unif_explicit Construct the explicit form of uniform clamped interpolating cubic spline (UcICS).

6 cics_unif_explicit

Description

cics_unif_explicit constructs the explicit form of uniform clamped interpolating cubic spline (via Hermite cubic spline) for nodes uu, function values yy and exterior-node derivatives d.

Usage

```
cics_unif_explicit(
  uumin,
  uumax,
  yy,
  d,
  clrs = c("blue", "red"),
  xlab = NULL,
  ylab = NULL,
  title = NULL
)
```

Arguments

uumin	a starting node.
uumax	an ending node.
уу	a vector of function values pertaining to nodes in uu.
d	a vector of two values of derivative, in the first and the last node of uu.
clrs	a vector (optional parameter) of colours that are used alternately to plot the graph of spline's components.
xlab	a title (optional parameter) for the x axis.
ylab	a title (optional parameter) for the y axis.
title	a title (optional parameter) for the plot.

Value

A list of spline components

spline_coeffs matrix, whose i-th row contains coefficients of uniform ICS's i-th component. spline_polynomials

list of UcICS's components string representations.

B 4-element array of (n+1)x(n+4) matrices, whereas element in i-th row and j-th column of 1-th matrix contains coefficient by x^{1-1} of cubic polynomial that

is in i-th row and j-th column of matrix B from spline's explicit form

$$S = B.\gamma.$$

gamma $\gamma=$ vector of spline coefficients - function values and exterior-node derivatives

that takes part in the explicit form $S = B.\gamma$.

aux_BF A basis function of the spline

aux_tridiag_inverse

An inverse of the tridiagonal matrix used for spline derivatives construction

Examples

```
yy <- c(4, 5, 2, 1.8);
sp <- cics_unif_explicit(0, 6, yy, c(2, 0.9))
sp$spline_polynomials
### <~~>
### Spline components' coefficients
explicit_spline(sp$B, sp$gamma)
sp$spline_coeffs == .Last.value
```

 $cics_unif_explicit_smooth$

Smooth given data set by k-component uniform clamped interpolating spline (UcICS).

Description

cics_unif_explicit_smooth constructs the uniform clamped interpolating spline with k components that smoothes given data set $\{(xx[i],yy[i]), i=1..length(xx)\}$.

Usage

```
cics_unif_explicit_smooth(
    xx,
    yy,
    k,
    clrs = c("blue", "red"),
    d,
    xlab = NULL,
    ylab = NULL,
    title = NULL,
    plotTF = TRUE
)
```

Arguments

XX	a vector of data set's x-coordinates (that are in increasing order).
уу	a vector of datanvidi set's y-coordinates.
k	a chosen number of components of smoothing UcICS (integer ≥ 2).
clrs	a vector of colours that are used alternately to plot the graph of spline's components.
d	a vector (optional parameter) that contains two values of derivative, in the first and the last computed node. If missing, values of derivative are estimated by given linear regression model. If present, their contribution is removed from linear model and only function values are estimated.
xlab	a title (optional parameter) for the x axis.

8 explicit_spline

ylab a title (optional parameter) for the y axis.

title a title (optional parameter) for the plot.

plotTF a boolean value (optional parameter), if TRUE then plot.

Value

a list with components

nodes vector of equidistant nodes, based on which we construct the smoothing spline. est_spline_coeffs

4-element array of (k)x(k+3) matrices, whereas element in i-th row and j-th of l-th matrix contains coefficient by x^{1-1} of cubic polynomial, which is in i-th row and j-th column of matrix B from smoothing spline's explicit form

$$S = B.\gamma$$
.

est_spline_polynomials

list of string representations of smoothing UcICS.

est_gamma vector of estimated smoothing spline's coefficients (function values and exterior-

node derivatives).

aux_BF A basis function of the spline

aux_tridiag_inverse

An inverse of the tridiagonal matrix used for spline derivatives construction

aux_M An estimation matrix used to compute est_gamma

Examples

```
cp <- cics_unif_explicit_smooth(
xx = CERN$x,
    yy = CERN$y,
    k = 19, #23,
    d = c(1, 0),
    xlab = "X axis",
    ylab = "Y axis"
)</pre>
```

explicit_spline

The function computes the coefficients of the cubic polynomials as spline components of the clamped interpolating cubic spline of class C^2 in its explicit form S=B * gamma.

Description

The function computes the coefficients of the cubic polynomials as spline components of the clamped interpolating cubic spline of class C^2 in its explicit form S=B * gamma.

forecast_demo 9

Usage

```
explicit_spline(B, gamma)
```

Arguments

B a 4-element array of (n+1)x(n+4) matrices, whereas element in i-th row and

j-th column of 1-th matrix contains coefficient by x^{1-1} of cubic polynomial that is in i-th row and j-th column of matrix B from spline's explicit form

S=B.gamma.

gamma a vector of spline coefficients - function values and exterior-node derivatives that

takes part in the explicit form $S = B.\gamma$.

Value

a matrix with four columns, whose i-th row contains the coefficients of the splines's i-th component

Examples

See functions cics_explicit, cics_unif_explicit and the vignette.

forecast_demo

Forecasting demo using cics_unif_explicit_smooth.

Description

Forecasting demo using cics_unif_explicit_smooth.

Usage

```
forecast_demo()
```

Value

a forecast result

Examples

Plots as well as the process of computation of future derivatives and values using extrapolation. ud <- forecast_demo()

10 tridiag_inv_general

hermite_bf_matrix

Construct 4 Hermite basis functions.

Description

hermite_bf_matrix constructs matrix of Hermite basis functions' coefficients on [u,v], that is the matrix of 4 cubic polynomials' coefficients of one-component Hermite cubic spline.

Usage

```
hermite_bf_matrix(u, v)
```

Arguments

u a left border of interval [u,v].

v a right border of interval [u,v], $u \le v$.

Value

The matrix of 4 Hermite basis functions' coefficients.

Examples

```
hermite_bf_matrix(0,1)
hermite_bf_matrix(-2,3)
```

tridiag_inv_general

Construct inverse of a general tridiagonal matrix.

Description

tridiag_inv_general constructs inverse of a general tridiagonal matrix T of order n, using Usmani's theorem.

Usage

```
tridiag_inv_general(T, n)
```

Arguments

T a tridiagonal matrix.

n an order of given tridiagonal matrix.

Value

The inverse of matrix T.

Examples

```
tridiag_inv_general(matrix(c(1, 4, 0, -9), 2, 2), 2)
tridiag_inv_general(matrix(c(1, 3, 5, -2, 0, 8, 7, 6, 6), 3, 3), 3)
```

tridiag_inv_unif_by_sums

Construct inverse of a tridiagonal matrix $T_n(a,b,a)$.

Description

tridiag_inv_unif_by_sums constructs inverse of a regular tridiagonal matrix T_n(a,b,a) with constant entries by a special algorithm using sums of matrix elements.

Usage

```
tridiag_inv_unif_by_sums(n, a, b)
```

Arguments

- n an order of given tridiagonal matrix.
- a value of tridiagonal matrix elements that are off-diagonal.
- b a value of tridiagonal matrix diagonal elements.

Value

The inverse of matrix $T_n(a,b,a)$.

Examples

```
tridiag_inv_unif_by_sums(5, 1, 4)
tridiag_inv_unif_by_sums(9, 10, -1)
```

Index