# Package 'pintervals'

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Type Package

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**Title** Model Agnostic Prediction Intervals

Description Provides tools for estimating model-agnostic prediction intervals using conformal prediction, bootstrapping, and parametric prediction intervals. The package is designed for ease of use, offering intuitive functions for both binned and full conformal prediction methods, as well as parametric interval estimation with diagnostic checks. Currently only working for continuous predictions. For details on the conformal and binconditional conformal prediction methods, see Randahl, Williams, and Hegre (2024) <doi:10.48550 arxiv.2410.14507="">.</doi:10.48550>
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abs\_error Absolute Error

# Description

Absolute Error

# Usage

```
abs_error(pred, truth)
```

# Arguments

pred a numeric vector of predicted values truth a numeric vector of true values

#### Value

a numeric vector of absolute errors

bindividual\_alpha  $B_{i}$ 

Bin-individual alpha function for conformal prediction

# Description

Bin-individual alpha function for conformal prediction

# Usage

```
bindividual_alpha(minqs, alpha)
```

# **Arguments**

minqs Minimum quantiles

alpha alpha level

bin\_chopper 3

bin_chopper	Bin chopper function for binned bootstrapping

# Description

Bin chopper function for binned bootstrapping

# Usage

```
bin_chopper(x, nbins, return_breaks = FALSE)
```

#### Arguments

x vector of values to be binned

nbins number of bins

return\_breaks logical indicating whether to return the bin breaks

bootstrap_inner	Bootstrap function for bootstrapping the prediction intervals
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#### **Description**

Bootstrap function for bootstrapping the prediction intervals

# Usage

```
bootstrap_inner(pred, error, nboot, alpha, lower_bound, upper_bound)
```

# **Arguments**

pred predicted value error vector of errors

nboot number of bootstrap samples

alpha confidence level

lower\_bound lower bound of the prediction interval upper\_bound upper bound of the prediction interval

#### Value

a numeric vector with the predicted value and the lower and upper bounds of the prediction interval

contiguize\_intervals Contiguize non-contiguous intervals

#### **Description**

Contiguize non-contiguous intervals

#### Usage

```
contiguize_intervals(
  pot_lower_bounds,
  pot_upper_bounds,
  empirical_lower_bounds,
  empirical_upper_bounds,
  return_all = FALSE
)
```

#### **Arguments**

```
pot_lower_bounds
Potential non-contiguous lower bounds
pot_upper_bounds
Potential non-contiguous upper bounds
empirical_lower_bounds
Observed lower bounds
empirical_upper_bounds
Observed upper bounds
return_all Return all intervals or just contiguous intervals
```

flatten\_cp\_bin\_intervals

Flatten binned conformal prediction intervals to contiguous intervals

# Description

Flatten binned conformal prediction intervals to contiguous intervals

#### Usage

```
flatten_cp_bin_intervals(lst, contiguize = FALSE)
```

### **Arguments**

lst list of binned conformal prediction intervals contiguize logical indicating whether to contiguize the intervals

grid\_finder 5

grid_finder	Grid search for lower and upper bounds of continuous conformal pre- diction intervals
	aiction intervals

# Description

Grid search for lower and upper bounds of continuous conformal prediction intervals

# Usage

```
grid_finder(
  y_min,
  y_max,
  ncs,
  ncs_function,
  y_hat,
  alpha,
  min_step = NULL,
  grid_size = NULL,
  return_min_q = FALSE,
  weighted_cp = FALSE,
  calib = NULL
)
```

# Arguments

y_min	minimum value to search
y_max	maximum value to search
ncs	vector of non-conformity scores
ncs_function	a function that takes a vector of predicted values and a vector of true values and returns a vector of non-conformity scores
y_hat	vector of predicted values
alpha	confidence level
min_step	The minimum step size for the grid search
grid_size	Alternative to min_step, the number of points to use in the grid search between the lower and upper bound
return_min_q	logical. If TRUE, the function will return the minimum quantile of the nonconformity scores for each predicted value
weighted_cp	logical. If TRUE, the function will use the weighted conformal prediction method. Default is FALSE
calib	a tibble with the predicted values and the true values of the calibration partition. Used when weighted_cp is TRUE. Default is NULL

#### Value

a tibble with the predicted values and the lower and upper bounds of the prediction intervals

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Inner function for grid search

#### **Description**

Inner function for grid search

#### Usage

```
grid_inner(
  hyp_ncs,
  y_hat,
  ncs,
  pos_vals,
  alpha,
  return_min_q = FALSE,
  weights = NULL
)
```

# Arguments

hyp\_ncs vector of hypothetical non-conformity scores

y\_hat predicted value

ncs vector of non-conformity scores

pos\_vals vector of possible values for the lower and upper bounds of the prediction inter-

val

alpha confidence level

return\_min\_q logical. If TRUE, the function will return the minimum quantile of the noncon-

formity scores for each predicted value

weights vector of weights for the weighted conformal prediction method

#### Value

a numeric vector with the predicted value and the lower and upper bounds of the prediction interval

minq\_to\_alpha

Helper for minimum quantile to alpha function

#### Description

Helper for minimum quantile to alpha function

pinterval\_bootstrap 7

#### Usage

```
minq_to_alpha(minq, alpha)
```

#### **Arguments**

minq minimum quantile alpha alpha level

pinterval\_bootstrap

Bootstrap prediction intervals

#### **Description**

This function computes bootstrapped prediction intervals with a confidence level of 1-alpha for a vector of (continuous) predicted values using bootstrapped prediction errors. The prediction errors to bootstrap from are computed using either a calibration set with predicted and true values or a set of pre-computed prediction errors from a calibration dataset or other data which the model was not trained on (e.g. OOB errors from a model using bagging). The function returns a tibble containing the predicted values along with the lower and upper bounds of the prediction intervals.

#### Usage

```
pinterval_bootstrap(
  pred,
  calib = NULL,
  calib_truth = NULL,
  error = NULL,
  error_type = c("raw", "absolute"),
  alpha = 0.1,
  n_bootstraps = 1000,
  lower_bound = NULL,
  upper_bound = NULL
)
```

# Arguments

pred	Vector of predicted values
calib	A numeric vector of predicted values in the calibration partition or a 2 column tibble or matrix with the first column being the predicted values and the second column being the truth values
calib_truth	A numeric vector of true values in the calibration partition. Only required if calib is a numeric vector
error	An optional numeric vector of pre-computed prediction errors from a calibration partition or other test data. If provided, calib will be ignored

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error_type	The type of error to use for the prediction intervals. Can be 'raw' or 'absolute'. If 'raw', bootstrapping will be done on the raw prediction errors. If 'absolute', bootstrapping will be done on the absolute prediction errors with random signs. Default is 'raw'
alpha	The confidence level for the prediction intervals. Must be a single numeric value between $0$ and $1$
n_bootstraps	The number of bootstraps to perform. Default is 1000
lower_bound	Optional minimum value for the prediction intervals. If not provided, the minimum (true) value of the calibration partition will be used
upper_bound	Optional maximum value for the prediction intervals. If not provided, the maximum (true) value of the calibration partition will be used

#### Value

A tibble with the predicted values, lower bounds, and upper bounds of the prediction intervals

#### **Examples**

```
library(dplyr)
library(tibble)
x1 <- runif(1000)
x2 <- runif(1000)
y <- rlnorm(1000, meanlog = x1 + x2, sdlog = 0.5)
df \leftarrow tibble(x1, x2, y)
df_train <- df %>% slice(1:500)
df_cal <- df %>% slice(501:750)
df_test <- df %>% slice(751:1000)
mod <- lm(log(y) \sim x1 + x2, data=df_train)
calib <- exp(predict(mod, newdata=df_cal))</pre>
calib_truth <- df_cal$y</pre>
pred_test <- exp(predict(mod, newdata=df_test))</pre>
pinterval_bootstrap(pred = pred_test,
calib = calib,
calib_truth = calib_truth,
error_type = 'raw',
alpha = 0.1,
lower_bound = 0)
```

pinterval\_boot\_bins

Bin-conditional bootstrap prediction intervals

#### **Description**

This function computes bootstrapped prediction intervals with a confidence level of 1-alpha for a vector of (continuous) predicted values using bin-conditional bootstrapped prediction errors. The prediction errors to bootstrap from are computed using either a calibration set with predicted and true values or a set of pre-computed prediction errors from a calibration dataset or other data which

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the model was not trained on (e.g. OOB errors from a model using bagging). The function returns a tibble containing the predicted values along with the lower and upper bounds of the prediction intervals.

Currently not working as intended. May be removed in future versions.

# Usage

```
pinterval_boot_bins(
  pred,
  calib,
  calib_truth = NULL,
  calib_bins = NULL,
  breaks = NULL,
  nbins = NULL,
  calib_bin_type = c("prediction", "truth"),
  error_type = c("raw", "absolute"),
  alpha = 0.1,
  n_bootstraps = 1000,
  lower_bound = NULL,
  upper_bound = NULL,
  right = TRUE
)
```

### **Arguments**

pred	Vector of predicted values
calib	A numeric vector of predicted values in the calibration partition or a 2 column tibble or matrix with the first column being the predicted values and the second column being the truth values
calib_truth	A numeric vector of true values in the calibration partition. Only required if calib is a numeric vector
calib_bins	A vector of bin identifiers for the calibration set
breaks	A vector of break points for the bins to manually define the bins. If NULL, lower and upper bounds of the bins are calculated as the minimum and maximum values of each bin in the calibration set. Must be provided if calib_bins or nbins are not provided, either as a vector or as the last column of a calib tibble.
nbins	Automatically chop the calibration set into nbins based on the true values with approximately equal number of observations in each bin. Must be provided if calib_bins or breaks are not provided.
calib_bin_type	A string specicying whether the bins are based on the predicted values ('prediction') or the true values ('truth'). Default is 'prediction'. Ignored if calib_bins is provided.
error_type	The type of error to use for the prediction intervals. Can be 'raw' or 'absolute'. If 'raw', bootstrapping will be done on the raw prediction errors. If 'absolute', bootstrapping will be done on the absolute prediction errors with random signs. Default is 'raw'

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alpha	The confidence level for the prediction intervals. Must be a single numeric value between 0 and 1
n_bootstraps	The number of bootstraps to perform. Default is 1000
lower_bound	Optional minimum value for the prediction intervals. If not provided, the minimum (true) value of the calibration partition will be used
upper_bound	Optional maximum value for the prediction intervals. If not provided, the maximum (true) value of the calibration partition will be used
right	Parameter passed to cut function to determine which side of the bin interval is closed. Default is TRUE

pinterval\_cp\_bins

Bin-conditional conformal prediction intervals for continuous predictions

#### **Description**

This function calculates bin-conditional conformal prediction intervals with a confidence level of 1-alpha for a vector of (continuous) predicted values using inductive conformal prediction on a bin-by-bin basis. The intervals are computed using either a calibration set with predicted and true values or a set of pre-computed non-conformity scores from the calibration set. In addition the function requires either a set of breaks or a vector of bin identifiers for the calibrations set, either as a standalone vector or as the third column of the calibration dataset if the calibration data is provided as a tibble. The function returns a tibble containing the predicted values along with the lower and upper bounds of the prediction intervals. Bin-conditional conformal prediction intervals are useful when the prediction error is not constant across the range of predicted values and ensures that the coverage is (approximately) correct for each bin under the assumption that the non-conformity scores are exchangeable within each bin.

#### Usage

```
pinterval_cp_bins(
 pred,
  calib = NULL,
  calib_truth = NULL,
  calib_bins = NULL,
  breaks = NULL,
  nbins = NULL,
  alpha = 0.1,
  ncs_function = "absolute_error",
  ncs = NULL,
 min_step = 0.01,
  grid_size = NULL,
  right = TRUE,
 weighted_cp = FALSE,
  contiguize = FALSE
)
```

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#### **Arguments**

pred Vector of predicted values

calib A numeric vector of predicted values in the calibration partition or a 2 or 3

column tibble or matrix with the first column being the predicted values and the second column being the truth values and (optionally) the third column being the bin values if bins are not provided as a standalone vector or if breaks are not

provided

calib\_truth A numeric vector of true values in the calibration partition

calib\_bins A vector of bin identifiers for the calibration set

breaks A vector of break points for the bins to manually define the bins. If NULL,

lower and upper bounds of the bins are calculated as the minimum and maximum values of each bin in the calibration set. Must be provided if calib\_bins or nbins are not provided, either as a vector or as the last column of a calib tibble.

nbins Automatically chop the calibration set into nbins based on the true values with

approximately equal number of observations in each bin. Must be provided if

calib\_bins or breaks are not provided.

alpha The confidence level for the prediction intervals. Must be a single numeric value

between 0 and 1

ncs\_function A function or a character string matching a function that takes two arguments,

a vector of predicted values and a vector of true values, in that order. The function should return a numeric vector of nonconformity scores. Default is 'absolute\_error' which returns the absolute difference between the predicted and true

values.

ncs An optional numeric vector of pre-computed nonconformity scores from a cal-

ibration partition. If provided, calib will be ignored. If provided, bins must be

provided in calib\_bins and breaks as well.

min\_step The minimum step size for the grid search. Default is 0.01. Useful to change if

predictions are made on a discrete grid or if the resolution of the interval is too

coarse or too fine.

grid\_size Alternative to min\_step, the number of points to use in the grid search between

the lower and upper bound. If provided, min\_step will be ignored.

right Logical, if TRUE the bins are right-closed (a,b] and if FALSE the bins are left-

closed '[a,b)'. Only used if breaks or nbins are provided.

weighted\_cp Logical, if TRUE the prediction intervals are created by bootstrapping the ncs

scores giving a higher weight to the ncs scores that are closer to the predicted

value. Default is FALSE. Experimental, so use with caution.

contiguize logical indicating whether to contiguize the intervals. TRUE will consider all

bins for each prediction using the lower and upper endpoints as interval limits to avoid non-contiguous intervals. FALSE will allows for non-contiguous intervals. TRUE guarantees at least appropriate coverage in each bin, but may suffer from over-coverage in certain bins. FALSE will have appropriate coverage in

each bin.

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#### Value

A tibble with the predicted values, the lower and upper bounds of the prediction intervals. If treat\_noncontiguous is 'non\_contiguous', the lower and upper bounds are set in a list variable called 'intervals' where all non-contiguous intervals are stored.

#### **Examples**

```
library(dplyr)
library(tibble)
x1 <- runif(1000)
x2 <- runif(1000)
y <- rlnorm(1000, meanlog = x1 + x2, sdlog = 0.5)
bin <- cut(y, breaks = quantile(y, probs = seq(0, 1, 1/4)),
include.lowest = TRUE, labels =FALSE)
df <- tibble(x1, x2, y, bin)</pre>
df_train <- df %>% slice(1:500)
df_cal <- df %>% slice(501:750)
df_test <- df %>% slice(751:1000)
mod <- lm(log(y) \sim x1 + x2, data=df_train)
calib <- exp(predict(mod, newdata=df_cal))</pre>
calib_truth <- df_cal$y</pre>
calib_bins <- df_cal$bin
pred_test <- exp(predict(mod, newdata=df_test))</pre>
pinterval_cp_bins(pred = pred_test,
calib = calib,
calib_truth = calib_truth,
calib_bins = calib_bins,
alpha = 0.1,
grid_size = 10000)
```

pinterval\_cp\_cont

Continuous Conformal Prediction Intervals

#### **Description**

This function calculates conformal prediction intervals with a confidence level of 1-alpha for a vector of (continuous) predicted values using inductive conformal prediction. The intervals are computed using either a calibration set with predicted and true values or a set of pre-computed non-conformity scores from the calibration set. The function returns a tibble containing the predicted values along with the lower and upper bounds of the prediction intervals.

# Usage

```
pinterval_cp_cont(
   pred,
   calib = NULL,
   calib_truth = NULL,
```

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```
alpha = 0.1,
ncs_function = "absolute_error",
weighted_cp = FALSE,
ncs = NULL,
lower_bound = NULL,
upper_bound = NULL,
min_step = 0.01,
grid_size = NULL,
return_min_q = FALSE
)
```

# Arguments

pred	Vector of predicted values
calib	A numeric vector of predicted values in the calibration partition or a 2 column tibble or matrix with the first column being the predicted values and the second column being the truth values
calib_truth	A numeric vector of true values in the calibration partition. Only required if calib is a numeric vector
alpha	The confidence level for the prediction intervals. Must be a single numeric value between 0 and 1
ncs_function	A function or a character string matching a function that takes two arguments, a vector of predicted values and a vector of true values, in that order. The function should return a numeric vector of nonconformity scores. Default is 'absolute_error' which returns the absolute difference between the predicted and true values.
weighted_cp	Logical. If TRUE, the function will use weighted conformal prediction. Default is FALSE. Experimental.
ncs	A numeric vector of pre-computed nonconformity scores from a calibration partition. If provided, calib will be ignored
lower_bound	Optional minimum value for the prediction intervals. If not provided, the minimum (true) value of the calibration partition will be used
upper_bound	Optional maximum value for the prediction intervals. If not provided, the maximum (true) value of the calibration partition will be used
min_step	The minimum step size for the grid search. Default is 0.01. Useful to change if predictions are made on a discrete grid or if the resolution of the interval is too coarse or too fine.
grid_size	Alternative to min_step, the number of points to use in the grid search between the lower and upper bound. If provided, min_step will be ignored.
return_min_q	Logical. If TRUE, the function will return the minimum quantile of the nonconformity scores for each predicted value. Default is FALSE. Primarily used for debugging purposes.

### Value

A tibble with the predicted values and the lower and upper bounds of the prediction intervals.

pinterval\_parametric

#### **Examples**

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```
library(dplyr)
library(tibble)
x1 <- runif(1000)
x2 <- runif(1000)
y <- rlnorm(1000, meanlog = x1 + x2, sdlog = 0.5)
df <- tibble(x1, x2, y)
df_train <- df %>% slice(1:500)
df_cal <- df %>% slice(501:750)
df_test <- df %>% slice(751:1000)
mod <- lm(log(y) \sim x1 + x2, data=df_train)
calib <- exp(predict(mod, newdata=df_cal))</pre>
calib_truth <- df_cal$y</pre>
pred_test <- exp(predict(mod, newdata=df_test))</pre>
pinterval_cp_cont(pred_test,
calib = calib,
calib_truth = calib_truth,
alpha = 0.1,
lower_bound = 0,
grid_size = 10000)
```

pinterval\_parametric Parametric prediction intervals for continuous predictions

### **Description**

This function computes parametric prediction intervals with a confidence level of 1-alpha for a vector of (continuous) predicted values using a user specified parametric distribution and parameters. The distribution can be any distribution available in R or a user defined distribution as long as a quantile function is available. The parameters should be estimated on calibration data. The prediction intervals are calculated as the quantiles of the distribution at the specified confidence level.

#### Usage

```
pinterval_parametric(
   pred,
   dist = c("norm", "lnorm", "pois", "nbinom", "gamma", "logis", "beta"),
   pars = list(),
   alpha = 0.1,
   lower_bound = NULL,
   upper_bound = NULL
)
```

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#### **Arguments**

pred	Vector of predicted values
dist	Distribution to use for the prediction intervals. Can be a character string matching any available distribution in R or a function representing a distribution. If a function is provided, it must be a quantile function (e.g. qnorm, qgamma, etc.)
pars	List of named parameters for the distribution for each prediction. See details for more information.
alpha	The confidence level for the prediction intervals. Must be a single numeric value between 0 and 1
lower_bound	Optional minimum value for the prediction intervals. If not provided, the minimum (true) value of the calibration partition will be used
upper_bound	Optional maximum value for the prediction intervals. If not provided, the maximum (true) value of the calibration partition will be used

#### **Details**

The distributions are not limited to the standard distributions available in R. Any distribution can be used as long as a quantile function is available. Users may create their own distribution functions and plug in the resulting quantile function or create compositie or mixture distributions using for instance the package 'mistr' and plug in the resulting quantile function.

The list of parameters should be constructed such that when the distribution function is called with the parameters, it returns a vector of the same length as the predictions. In most cases the parameters should ensure that the predicted value corresponds to the mean, median, or mode of the resulting distribution. Parameters relating to the prediction error should be estimated on calibration data. For example, if normal prediction intervals are desired, the mean parameter should be the predicted value and the standard deviation parameter should be the estimated standard deviation of the prediction errors in the calibration set. If the distribution is a negative binomial distribution with a fixed size parameter, the size parameter should be estimated on the calibration data and the mu parameter should be the predicted value.

#### Value

A tibble with the predicted values and the lower and upper bounds of the prediction intervals

#### **Examples**

```
library(dplyr)
library(tibble)
x1 <- runif(1000)
x2 <- runif(1000)
y <- rlnorm(1000, meanlog = x1 + x2, sdlog = 0.5)
df <- tibble(x1, x2, y)
df_train <- df %>% slice(1:500)
df_cal <- df %>% slice(501:750)
df_test <- df %>% slice(751:1000)
mod <- lm(log(y) ~ x1 + x2, data=df_train)
calib <- exp(predict(mod, newdata=df_cal))
calib_truth <- df_cal$y</pre>
```

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```
pred_test <- exp(predict(mod, newdata=df_test))

# Normal prediction intervals
pinterval_parametric(pred = pred_test,
dist = 'norm',
pars = list(mean = pred_test,
sd = sqrt(mean((calib - calib_truth)^2))))

# Log-normal prediction intervals
pinterval_parametric(pred = pred_test,
dist = 'lnorm',
pars = list(meanlog = pred_test,
sdlog = sqrt(mean((log(calib) - log(calib_truth))^2))))</pre>
```

weights\_calculator

Weights calculator for weighted conformal prediction

# **Description**

Weights calculator for weighted conformal prediction

#### Usage

```
weights_calculator(y_hat, calib)
```

#### **Arguments**

y\_hat Predicted value

calib a vector of true values of the calibration partition

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