# Package 'xegaPermGene'

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```
Version 1.0.0.0
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Description An implementation of
     representation-dependent gene level operations for
     genetic algorithms with genes which represent permutations:
     initialization of genes, mutation and crossover.
     The crossover operation provided is position-based crossover
     (Syswerda, G., Chap. 21 in Davis, L. (1991, ISBN:0-442-00173-8).
     For mutation, several variants are included: Order-based mutation
     (Syswerda, G., Chap. 21 in Davis, L. (1991, ISBN:0-442-00173-8),
     randomized Lin-Kernighan heuristics
     (Croes, G. A. (1958) <doi:10.1287/opre.6.6.791> and
      Lin, S. and Kernighan. B. W. (1973)
     <doi:10.1287/opre.21.2.498>),
     and randomized greedy operators.
     A random mix operator for mutation selects a mutation variant
     randomly.
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```

**Title** Operations on Permutation Genes

2 Decay

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Decay	Exponential decay.	_

# Description

Exponential decay.

# Usage

Decay(t, lambda = 0.05)

# Arguments

Number of objects. t

Exponential decay constant. lambda

# Value

Vector with t elements with values of exponential decay.

### See Also

Other Utility: without()

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### **Examples**

```
Decay(5, 0.4)
Decay(10, 0.4)
```

1FxegaPermGene

Generate local functions and objects.

### **Description**

1FxegaPermGene is a list of functions which contains a definition of all local objects required for the use of genetic operators with the We refer to this object as local configuration.

# Usage

1FxegaPermGene

#### **Format**

An object of class list of length 21.

# **Details**

We use the local function list (the local configuration) for

- replacing all constants by constant functions.
   Rationale: We need one formal argument (the local function list IF) and we can dispatch multiple functions. E.g. 1F\$verbose()
- 2. for dynamically binding a local function with a definition from a proper function factory. E.g. the selection methods lf\$SelectGene and SelectMate.
- 3. for gene representation specific special functions: lf\$InitGene, lF\$DecodeGene, lf\$EvalGene lf\$ReplicateGene, ...

### See Also

 $Other\ Configuration:\ xegaPermCrossoverFactory(),\ xegaPermMutationFactory()$ 

without

Returns elements of vector x without elements in y.

# Description

Returns elements of vector x without elements in y.

# Usage

```
without(x, y)
```

# Arguments

x Vector.y Vector.

#### Value

Vector.

#### See Also

```
Other Utility: Decay()
```

# **Examples**

```
a<-sample(1:15,15, replace=FALSE)
b<-c(1, 3, 5)
without(a, b)</pre>
```

xegaPermCross2Gene

Position based crossover of 2 genes.

# Description

xegaPermCross2Gene determines a random subschedule of random length.

It copies the random subschedule into a new gene. The rest of the positions of the new scheme is filled with the elements of the other gene to complete the permutation. This is done for each gene.

# Usage

```
xegaPermCross2Gene(gg1, gg2, 1F)
```

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# **Arguments**

gg1	Permutation.
gg2	Permutation.

1F Local configuration of the genetic algorithm.

#### Value

List of 2 permutations.

#### References

Syswerda, G. (1991): Schedule Optimization Using Genetic Algorithms. In: Davis, L. (Ed.): Handbook of Genetic Algorithms, Chapter 21, p. 343. Van Nostrand Reinhold, New York. (ISBN:0-442-00173-8)

#### See Also

```
Other Crossover: xegaPermCrossGene()
```

# **Examples**

```
gene1<-xegaPermInitGene(1FxegaPermGene)
gene2<-xegaPermInitGene(1FxegaPermGene)
xegaPermDecodeGene(gene1, 1FxegaPermGene)
xegaPermDecodeGene(gene2, 1FxegaPermGene)
newgenes<-xegaPermCross2Gene(gene1, gene2)
xegaPermDecodeGene(newgenes[[1]], 1FxegaPermGene)
xegaPermDecodeGene(newgenes[[2]], 1FxegaPermGene)</pre>
```

xegaPermCrossGene

Position based crossover of 2 genes.

# **Description**

xegaPermCrossGene determines a random subschedule of random length.

It copies the random subschedule into a new gene. The rest of the positions of the new scheme is filled with the elements of the other gene to complete the permutation.

#### Usage

```
xegaPermCrossGene(gg1, gg2, lF)
```

# Arguments

gg1	Permutation.
gg2	Permutation.

1F Local configuration of the genetic algorithm.

#### Value

A list of 2 permutations.

#### References

Syswerda, G. (1991): Schedule Optimization Using Genetic Algorithms. In: Davis, L. (Ed.): Handbook of Genetic Algorithms, Chapter 21, p. 343. Van Nostrand Reinhold, New York. (ISBN:0-442-00173-8)

#### See Also

Other Crossover: xegaPermCross2Gene()

### **Examples**

```
gene1<-xegaPermInitGene(1FxegaPermGene)
gene2<-xegaPermInitGene(1FxegaPermGene)
xegaPermDecodeGene(gene1, 1FxegaPermGene)
xegaPermDecodeGene(gene2, 1FxegaPermGene)
newgenes<-xegaPermCrossGene(gene1, gene2)
xegaPermDecodeGene(newgenes[[1]], 1FxegaPermGene)</pre>
```

xegaPermCrossoverFactory

Configure the crossover function of a genetic algorithm.

# Description

xegaPermCrossoverFactory implements the selection of one of the crossover functions in this package by specifying a text string. The selection fails ungracefully (produces a runtime error), if the label does not match. The functions are specified locally.

Current support:

- 1. Crossover functions with two kids:
  - (a) "Cross2Gene" returns xegaPermCross2Gene.
- 2. Crossover functions with one kid:
  - (a) "CrossGene" returns xegaPermCrossGene.

# Usage

```
xegaPermCrossoverFactory(method = "Cross2Gene")
```

# **Arguments**

method

A string specifying the crossover function.

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# Value

A crossover function for genes.

# See Also

Other Configuration: 1FxegaPermGene, xegaPermMutationFactory()

# **Examples**

```
XGene<-xegaPermCrossoverFactory("Cross2Gene")
gene1<-xegaPermInitGene(lFxegaPermGene)
gene2<-xegaPermInitGene(lFxegaPermGene)
XGene(gene1, gene2, lFxegaPermGene)</pre>
```

xegaPermDecodeGene

Decode a permutation.

# Description

xegaPermDecodeGene decodes a permutation gene.

#### **Usage**

```
xegaPermDecodeGene(gene, 1F)
```

#### **Arguments**

gene Permutation.

1F Local configuration of the genetic algorithm.

### **Details**

xegaPermDecodeGene is the identy function.

### Value

A permutation gene.

```
g<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(g)</pre>
```

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xegaPermGene

Package xegaPermGene.

### Description

Genetic operations for permutation genes.

#### **Details**

Permutation genes are a representation of a tour of a Traveling Salesman Problem (TSP).

For permutation genes, the xegaPermGene package provides

- Gene initiatilization.
- Decoding of parameters.
- Mutation functions as well as a function factory for configuration.
- Crossover functions as well as a function factory for configuration.

# **Permutation Gene Representation**

A permutation gene is a named list with at least the following elements:

- \$gene1: The gene must be a permutation vector.
- \$fit: The fitness value of the gene (for EvalGeneDet and EvalGeneU) or the mean fitness (for stochastic functions evaluated with EvalGeneStoch).
- \$evaluated: Boolean. Has the gene been evaluated?
- \$evalFail: Boolean. Has the evaluation of the gene failed?

#### Abstract Interface of a Problem Environment for the TSP

A problem environment penv for the TSP must provide:

- \$name(): Returns the name of the problem environment.
- \$genelength(): The number of bits of the binary coded real parameter vector. Used in InitGene.
- \$dist(): The distance matrix of the TSP.
- \$cities(): A list of city names or 1:numberOfCities.
- \$f(permutation, gene, 1F): Returns the fitness of the permutation (the length of a tour).
- \$solution(): The minimal tour length (if known).
- \$path(): An optimal TSP tour.
- \$show(permutation): Prints the tour with the distances and the cumulative distances between the cities.
- TSP Heuristics:
  - \$greedy(startposition, k): Computes a greedy tour of length k.

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- \$kBestgreedy(k): Computes the best greedy tour of length k.
- \$rnd20pt(permutation, maxTries): Generate a new permutation by a random 2-change.
   maxTries is the maximal number of trials to find a better permutation. \$rnd20pt either returns a better permutation or, if no better permutation can be found in maxTries attempts, the original permutation.

\$LinKernighan(permutation, maxTries): Returns a permutation generated by a random sequence of 2-changes with improving performance. The optimality criterion of the k Lin-Kernighan heuristics is replaced by the necessity of finding a sequence of random 2-changes with strictly increasing performance.

#### **Abstract Interface of Mutation Functions**

Each mutation function has the following function signature:

```
newGene<-Mutate(gene, 1F)</pre>
```

All local parameters of the mutation function configured are expected in the local configuration 1F.

## **Local Constants of Mutation Functions**

The local constants of a mutation function determine the behavior of the function.

Constant	Default	Used in
<pre>1F\$BitMutationRate1()</pre>	0.005	xegaPermMutateGeneOrderBased
lF\$Lambda()	0.05	xegaPermMutateGenekInversion
		xegaPermMutateGenekGreedy
		xegaPermMutateGeneBestGreedy
lF\$max2Opt()	100	xegaPermMutateGene2Opt
		xegaPermMutateGenekOptLK

#### **Abstract Interface of Crossover Functions**

The signatures of the abstract interface to the 2 families of crossover functions are:

```
ListOfTwoGenes<-Crossover2(gene1, gene2, 1F)
newGene<-Crossover(gene1, gene2, 1F)
```

#### The Architecture of the xegaX-Packages

The xegaX-packages are a family of R-packages which implement eXtended Evolutionary and Genetic Algorithms (xega). The architecture has 3 layers, namely the user interface layer, the population layer, and the gene layer:

- The user interface layer (package xega) provides a function call interface and configuration support for several algorithms: genetic algorithms (sga), permutation-based genetic algorithms (sgPerm), derivation free algorithms as e.g. differential evolution (sgde), grammar-based genetic programming (sgp) and grammatical evolution (sge).
- The population layer (package xegaPopulation) contains population related functionality as well as support for population statistics dependent adaptive mechanisms and parallelization.

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- The gene layer is split in a representation independent and a representation dependent part:
  - The representation indendent part (package xegaSelectGene) is responsible for variants
    of selection operators, evaluation strategies for genes, as well as profiling and timing
    capabilities.
  - 2. The representation dependent part consists of the following packages:
    - xegaGaGene for binary coded genetic algorithms.
    - xegaPermGene for permutation-based genetic algorithms.
    - xegaDfGene for derivation free algorithms as e.g. differential evolution.
    - xegaGpGene for grammar-based genetic algorithms.
    - xegaGeGene for grammatical evolution algorithms.

The packages xegaDerivationTrees and xegaBNF support the last two packages: xegaBNF essentially provides a grammar compiler and xegaDerivationTrees an abstract data type for derivation trees.

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#### **URL**

<a href="https://github.com/ageyerschulz/xegaPermGene">https://github.com/ageyerschulz/xegaPermGene</a>

# Installation

From CRAN by install.packages('xegaPermGene')

#### Author(s)

Andreas Geyer-Schulz

xegaPermInitGene

Initialize a gene with a permutation of integers

### **Description**

xegaPermInitGene generates a random permutation with a given length n.

# Usage

```
xegaPermInitGene(1F)
```

### **Arguments**

1F

Local configuration of the genetic algorithm.

# **Details**

In the permutation representation of package xegaPerm, gene is a list with

- 1. \$evaluated: Boolean: TRUE if the fitness is known.
- 2. \$fit: The fitness of the genotype of \$gene1.
- 3. \$gene1: The permutation (the genetopye).

This representation makes several code optimizations and generalizations easier.

#### Value

A permutation gene.

# **Examples**

```
xegaPermInitGene(lFxegaPermGene)
```

xegaPermMutateGene2Opt

Mutate a gene (by a random 2-Opt move).

# Description

xegaPermMutateGene20pt mutates a permutation. The per position mutation rate is given by MutationRate().

#### Usage

```
xegaPermMutateGene2Opt(gene, 1F)
```

# Arguments

gene A Permutation.

1F Local configuration of the genetic algorithm.

# **Details**

This operator is an implementation of the 2-Opt move due to Croes (1958).

Two edges are exchanged, if the exchange improves the result.

#### Value

A Permutation.

# References

Croes, G. A. (1958): A Method for Solving Traveling-Salesman Problems. Operations Research, 6(6), pp. 791-812. <doi:10.1287/opre.6.6.791>

#### See Also

Other Mutation: xegaPermMutateGeneBestGreedy(), xegaPermMutateGeneGreedy(), xegaPermMutateGeneOrderBased xegaPermMutateGenekInversion(), xegaPermMutateGenekOptLK(), xegaPermMutateMix()

# **Examples**

```
gene1<-xegaPermInitGene(1FxegaPermGene)
xegaPermDecodeGene(gene1, 1FxegaPermGene)
gene<-xegaPermMutateGene2Opt(gene1, 1FxegaPermGene)
xegaPermDecodeGene(gene, 1FxegaPermGene)</pre>
```

xegaPermMutateGeneBestGreedy

*Mutate a gene (by inserting a greedy path at start of random length k).* 

#### **Description**

xegaPermMutateGeneGreedy mutates a permutation by inserting a greedy path of length k at a random position start. The mutation rate for a gene is given by MutationRate().

# Usage

```
xegaPermMutateGeneBestGreedy(gene, 1F)
```

# **Arguments**

gene A Permutation.

1F Local configuration of the genetic algorithm.

#### **Details**

The path length k is expontially decaying with exponential decay constant 1F\$lambda().

### Value

A Permutation

### See Also

Other Mutation: xegaPermMutateGene20pt(), xegaPermMutateGeneGreedy(), xegaPermMutateGeneOrderBased(), xegaPermMutateGenekInversion(), xegaPermMutateGenekOptLK(), xegaPermMutateMix()

#### **Examples**

```
gene1<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(gene1, lFxegaPermGene)
gene<-xegaPermMutateGeneGreedy(gene1, lFxegaPermGene)
xegaPermDecodeGene(gene, lFxegaPermGene)</pre>
```

xegaPermMutateGeneGreedy

Mutate a gene (by inserting a greedy path at start of random length k).

# Description

xegaPermMutateGeneGreedy mutates a permutation by inserting a greedy path of length k at a random position start. The mutation rate for a gene is given by MutationRate().

### Usage

```
xegaPermMutateGeneGreedy(gene, 1F)
```

#### Arguments

gene A Permutation.

1F Local configuration of the genetic algorithm.

### **Details**

The path length k is expontially decaying with exponential decay constant lambda.

#### Value

A Permutation.

#### See Also

Other Mutation: xegaPermMutateGene20pt(), xegaPermMutateGeneBestGreedy(), xegaPermMutateGeneOrderBased() xegaPermMutateGenekInversion(), xegaPermMutateGenekOptLK(), xegaPermMutateMix()

```
gene1<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(gene1, lFxegaPermGene)
gene<-xegaPermMutateGeneGreedy(gene1, lFxegaPermGene)
xegaPermDecodeGene(gene, lFxegaPermGene)</pre>
```

xegaPermMutateGenekInversion

Mutate a gene (k random inversions).

#### **Description**

xegaPermMutateGenekInversion performs k random inversions. The number of inversions is expontially decaying with exponential decay constant lambda.

# Usage

```
xegaPermMutateGenekInversion(gene, 1F)
```

#### **Arguments**

gene A Permutation.

1F Local configuration of the genetic algorithm.

#### **Details**

The only difference to the order based mutation operator (Syswerda, 1991) is the exponential decay in the number of inversions.

- 1. The indices of a random subschedule are extracted.
- 2. The subschedule is extracted, permuted, and reinserted.

### Value

A Permutation.

#### References

Syswerda, G. (1991): Schedule Optimization Using Genetic Algorithms. In: Davis, L. (Ed.): Handbook of Genetic Algorithms, Chapter 21, pp. 332-349. Van Nostrand Reinhold, New York.

#### See Also

Other Mutation: xegaPermMutateGene20pt(), xegaPermMutateGeneBestGreedy(), xegaPermMutateGeneGreedy(), xegaPermMutateGeneOrderBased(), xegaPermMutateGenekOptLK(), xegaPermMutateMix()

```
gene1<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(gene1, lFxegaPermGene)
gene<-xegaPermMutateGenekInversion(gene1, lFxegaPermGene)
xegaPermDecodeGene(gene, lFxegaPermGene)</pre>
```

xegaPermMutateGenekOptLK

Mutate a gene (by a random Lin-Kernighan k-OPT move).

# **Description**

xegaPermMutateGenekOptLK mutates a permutation. The mutation rate of a gene is given by MutationRate().

#### Usage

```
xegaPermMutateGenekOptLK(gene, 1F)
```

# Arguments

gene A Permutation.

1F Local configuration of the genetic algorithm.

#### **Details**

This operator is an implementation of the random k-Opt move version of the Lin-Kernighan heuristic.

A sequence of random 2-Opt moves, all of which improve the result is executed.

#### Value

A Permutation.

### References

Lin, S. and Kernighan. B. W. (1973): An Effective Heuristic Algorithm for the Traveling-Salesman Problem. Operations Research, 21(2), pp. 791-812. <doi:10.1287/opre.21.2.498>

# See Also

Other Mutation: xegaPermMutateGene20pt(), xegaPermMutateGeneBestGreedy(), xegaPermMutateGeneGreedy(), xegaPermMutateGeneOrderBased(), xegaPermMutateGenekInversion(), xegaPermMutateMix()

```
gene1<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(gene1, lFxegaPermGene)
gene<-xegaPermMutateGenekOptLK(gene1, lFxegaPermGene)
xegaPermDecodeGene(gene, lFxegaPermGene)</pre>
```

xegaPermMutateGeneOrderBased

Mutate a gene (generalized order based mutation).

## Description

xegaPermMutateGene mutates a permutation. The per position mutation rate is given by 1F\$BitMutationRate1().

### Usage

```
xegaPermMutateGeneOrderBased(gene, 1F)
```

#### **Arguments**

gene A Permutation.

1F Local configuration of the genetic algorithm.

#### **Details**

This operator is an implementation of a generalized order based mutation operator (Syswerda, 1991).

- 1. The indices of a random subschedule are extracted.
- 2. The subschedule is extracted, permuted, and reinserted.

# Value

A Permutation.

### References

```
Syswerda, G. (1991): Schedule Optimization Using Genetic Algorithms. In: Davis, L. (Ed.): Handbook of Genetic Algorithms, Chapter 21, pp. 332-349. Van Nostrand Reinhold, New York. (ISBN:0-442-00173-8)
```

#### See Also

```
Other Mutation: xegaPermMutateGene2Opt(), xegaPermMutateGeneBestGreedy(), xegaPermMutateGeneGreedy(), xegaPermMutateGenekInversion(), xegaPermMutateGenekOptLK(), xegaPermMutateMix()
```

```
gene1<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(gene1, lFxegaPermGene)
gene<-xegaPermMutateGeneOrderBased(gene1, lFxegaPermGene)
xegaPermDecodeGene(gene, lFxegaPermGene)</pre>
```

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xegaPermMutateMix

Mutation by a random mutation function.

# **Description**

A mutation function is randomly selected from the following list: xegaPermMutateGeneOrder-Based, xegaPermMutateGenekInversion, xegaPermMutateGene2Opt, xegaPermMutateGenekOptLK, xegaPermMutateGeneGreedy, xegaPermMutateGeneBestGreedy.

#### Usage

```
xegaPermMutateMix(gene, 1F)
```

### **Arguments**

gene A permutation.

1F Local configuration.

#### Value

A permutation.

### See Also

Other Mutation: xegaPermMutateGene20pt(), xegaPermMutateGeneBestGreedy(), xegaPermMutateGeneGreedy(), xegaPermMutateGeneVoltK()

# **Examples**

```
gene1<-xegaPermInitGene(lFxegaPermGene)
xegaPermDecodeGene(gene1, lFxegaPermGene)
gene<-xegaPermMutateMix(gene1, lFxegaPermGene)
xegaPermDecodeGene(gene, lFxegaPermGene)</pre>
```

xegaPermMutationFactory

Configure the mutation function of a genetic algorithm.

#### **Description**

xegaPermMutationFactory implements the selection of one of the gene mutation functions in this package by specifying a text string. The selection fails ungracefully (produces a runtime error), if the label does not match. The functions are specified locally.

# **Current Support:**

- 1. "MutateGene" returns xegaPermMutateGeneOrderBased.
- $2. \ \ "Mutate Gene Order Based" \ returns \ xega Perm Mutate Gene Order Based.$
- 3. "MutateGenekInversion" returns xegaPermMutateGenekInversion.
- 4. "MutateGene2Opt" returns xegaPermMutateGene2Opt.
- 5. "MutateGenekOptLK" returns xegaPermMutateGenekOptLK.
- 6. "MutateGeneGreedy" returns xegaPermMutateGeneGreedy.
- 7. "MutateGeneBestGreedy" returns xegaPermMutateGeneBestGreedy.
- 8. "MutateGeneMix" returns xegaPermMutateMix.

# Usage

```
xegaPermMutationFactory(method = "MutateGene")
```

# **Arguments**

method

The name of the mutation method.

# Value

A permutation based mutation function.

#### See Also

```
Other Configuration: 1FxegaPermGene, xegaPermCrossoverFactory()
```

#### **Examples**

xegaPermMutationFactory(method="MutateGene")

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