Package 'TriDimRegression'

September 13, 2023

```
Title Bayesian Statistics for 2D/3D Transformations
Version 1.0.2
Description Fits 2D and 3D geometric transformations via 'Stan' probabilistic programming engine (
      Stan Development Team (2021) <a href="https:">https:</a>
      //mc-stan.org>). Returns posterior distribution for individual
      parameters of the fitted distribution. Allows for computation of LOO and WAIC information cri-
      (Vehtari A, Gelman A, Gabry J (2017) <doi:10.1007/s11222-016-9696-
      4>) as well as Bayesian R-squared
      (Gelman A, Goodrich B, Gabry J, and Vehtari A (2018) <doi:10.1080/00031305.2018.1549100>).
License GPL-3
URL https://github.com/alexander-pastukhov/tridim-regression,
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BugReports https://github.com/alexander-pastukhov/tridim-regression/issues
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```

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 ${\tt TriDimRegression-package}$

The 'TriDimRegression' package.

Description

Fits 2D and 3D geometric transformations. Provides posterior via Stan. Includes computation of LOO and WAIC information criteria, R-squared.

To fit transformation, call the main function either via a formula that specifies dependent and independent variables with the data table or by supplying two tables one containing all independent variables and one containing all dependent variables.

For the 2D data, you can fit "translation" (2 parameters for translation only), "euclidean" (4 parameters: 2 for translation, 1 for scaling, and 1 for rotation), "affine" (6 parameters: 2 for translation and 4 that jointly describe scaling, rotation and sheer), or "projective" (8 parameters: affine plus 2 additional parameters to account for projection). For 3D data, you can fit "translation" (3 for translation only), "euclidean_x", "euclidean_y", "euclidean_z" (5 parameters: 3 for translation scale, 1 for rotation, and 1 for scaling), "affine" (12 parameters: 3 for translation and 9 to account for scaling, rotation, and sheer), and "projective" (15 parameters: affine plus 3 additional parameters to account for projection). transformations. For details on transformation matrices and computation of scale and rotation parameters please see vignette("transformation_matrices", package = "TriDimRegression")

Once the data is fitted, you can extract the transformation coefficients via coef function and the matrix itself via transformation_matrix. Predicted data, either based on the original data or on the new data, can be generated via predict. Bayesian R-squared can be computed with or without adjustment via R2 function. In all three cases, you have choice between summary (mean + specified quantiles) or full posterior samples. loo and waic provide corresponding measures that can be used for comparison via loo::loo_compare() function.

Author(s)

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References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.19.3. https://mc-stan.org

See Also

```
fit_transformation fit_transformation_df tridim_transformation vignette("transformation_matrices",
package = "TriDimRegression") vignette("calibration", package = "TriDimRegression")
vignette("comparing_faces", package = "TriDimRegression")
```

CarbonExample1Data

Carbon, C. C. (2013), data set #1

Description

Example 1 from the domain of aesthetics to show how the method can be utilized for assessing the similarity of two portrayed persons, actually the Mona Lisa in the world famous Louvre version and the only recently re-discovered Prado version.

Usage

CarbonExample1Data

Format

A data frame with 36 observations on the following 4 variables:

```
depV1, depV2 numeric vectors, dependent variables
indepV1, indepV2 numeric vectors, independent variables
```

Source

doi:10.18637/jss.v052.c01

CarbonExample2Data 5

CarbonExample2Data

Carbon, C. C. (2013), data set #2

Description

Example 2 originates from the area of geography and inspects the accuracy of different maps of the city of Paris which were created over the last 350 years as compared to a recent map.

Usage

CarbonExample2Data

Format

A data frame with 13 observations on the following 4 variables:

```
depV1, depV2 numeric vectors, dependent variables
indepV1, indepV2 numeric vectors, independent variables
```

Source

doi:10.18637/jss.v052.c01

CarbonExample3Data

Carbon, C. C. (2013), data set #3

Description

Example 3 focuses on demonstrating how good a cognitive map recalculated from averaged cognitive distance data fits with a related real map.

Usage

CarbonExample3Data

Format

A data frame with 10 observations on the following 4 variables:

```
depV1, depV2 numeric vectors, dependent variablesindepV1, indepV2 numeric vectors, independent variables
```

Source

doi:10.18637/jss.v052.c01

```
coef.tridim_transformation
```

Posterior distributions for transformation coefficients in full or summarized form.

Description

Posterior distributions for transformation coefficients in full or summarized form.

Usage

```
## S3 method for class 'tridim_transformation'
coef(
  object,
  summary = TRUE,
  probs = c(0.055, 0.945),
  convert_euclidean = FALSE,
   ...
)
```

Arguments

object An object of class tridim_transformation.

summary Whether summary statistics should be returned instead of raw sample values.

Defaults to TRUE

probs The percentiles used to compute summary, defaults to 89% credible interval.

convert_euclidean

Whether to convert matrix coefficients to scale(phi) and rotation(theta). Defaults

to FALSE.

. . . Unused

Value

If summary=FALSE, a list with matrix iterationsN x dimensionsN for each variable. If summary=TRUE, a data.frame with columns "dvindex" with mean for each dependent variable plus optional quantiles columns with names "dvindex_quantile".

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```
coef(euc2)
# scale and rotation coefficients
coef(euc2, convert_euclidean=TRUE)
```

EyegazeData

Eye gaze calibration data

Description

A dataset containing a monocular eye gaze recording with calibration sequence. Courtesy of Bamberger Baby Institut: BamBI.

Usage

EyegazeData

Format

A data frame with 365 rows and 6 variables:

time sample timestamp, in milliseconds

x, y recorded gaze, in internal eye tracker units

target_x, target_y location of the calibration target on the screen, in pixels

target index of the target within the sequence

Source

https://www.uni-bamberg.de/entwicklungspsychologie/transfer/babyforschung-bambi/.

Face3D_M010

Face landmarks, male, #010

Description

Face landmarks, male, #010

Usage

Face3D_M010

Format

A data frame with 64 landmarks on the following 3 variables:

8 Face3D_M244

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_M101

Face landmarks, male, #101

Description

Face landmarks, male, #101

Usage

Face3D_M101

Format

A data frame with 64 landmarks on the following 3 variables:

x, y, z numeric vectors, coordinates of face landmarks

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_M244

Face landmarks, male, #244

Description

Face landmarks, male, #244

Usage

Face3D_M244

Format

A data frame with 64 landmarks on the following 3 variables:

Face3D_M92 9

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_M92

Face landmarks, male, #092

Description

Face landmarks, male, #092

Usage

Face3D_M92

Format

A data frame with 64 landmarks on the following 3 variables:

x, y, z numeric vectors, coordinates of face landmarks

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_W070

Face landmarks, female, #070

Description

Face landmarks, female, #070

Usage

Face3D_W070

Format

A data frame with 64 landmarks on the following 3 variables:

10 Face3D_W182

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_W097

Face landmarks, female, #097

Description

Face landmarks, female, #097

Usage

Face3D_W097

Format

A data frame with 64 landmarks on the following 3 variables:

x, y, z numeric vectors, coordinates of face landmarks

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_W182

Face landmarks, female, #182

Description

Face landmarks, female, #182

Usage

Face3D_W182

Format

A data frame with 64 landmarks on the following 3 variables:

Face3D_W243

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

Face3D_W243

Face landmarks, female, #243

Description

Face landmarks, female, #243

Usage

Face3D_W243

Format

A data frame with 64 landmarks on the following 3 variables:

x, y, z numeric vectors, coordinates of face landmarks

Source

Carbon, C. C. (2012). The Bamberg DADA Face Database (BaDADA). A standardized high quality Face Database with faces of Different Affective states from Different Angles. Unpublished databank. University of Bamberg, Bamberg.

fit_transformation

Fitting Bidimensional or Tridimensional Regression / Geometric Transformation Models via Formula.

Description

Fits Bidimensional or Tridimensional regression / geometric transformation models using Stan engine. The formula described dependent and independent numeric variables in the data. See also fit_transformation_df.

For the 2D data, you can fit "translation" (2 parameters for translation only), "euclidean" (4 parameters: 2 for translation, 1 for scaling, and 1 for rotation), "affine" (6 parameters: 2 for translation and 4 that jointly describe scaling, rotation and sheer), or "projective" (8 parameters: affine plus 2 additional parameters to account for projection).

For 3D data, you can fit "translation" (3 for translation only), "euclidean_x", "euclidean_y", "euclidean_z" (5 parameters: 3 for translation scale, 1 for rotation, and 1 for scaling), "affine" (12 parameters: 3 for translation and 9 to account for scaling, rotation, and sheer), and "projective" (15 parameters: affine plus 3 additional parameters to account for projection). transformations.

For details on transformation matrices and computation of scale and rotation parameters please see vignette("transformation_matrices", package = "TriDimRegression")

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Usage

```
## S3 method for class 'formula'
fit_transformation(
  formula,
  data,
  transformation,
  priors = NULL,
  chains = 1,
  cores = NULL,
  ...
)
```

Arguments

formula a symbolic description of the model to be fitted in the format Xdep + Ydep ~

Xind + Yind, where Xdep and Ydep are dependent and Xind and Yind are inde-

pendent variables

data a data frame containing variables for the model.

transformation the transformation to be used: "translation" (both 2D and 3D), "euclidean"

(2D), "euclidean_x", "euclidean_y", "euclidean_z" (3D, rotation about, respectively, x, y, and z axis), "affine" (2D and 3D), or "projective" (2D

and 3D).

priors named list of parameters for prior distributions of parameters a (translation,

normal distribution), b (all other parameters, normal distribution), and sigma (residual variance, exponential). E.g., list("a" = c(0, 10), "b" = c(0, 1),

"sigma"=1). Default priors are "a" = c(0, max_absolute_difference_in_means(d, iv)) / 2), "b" = c(0, max_absolute_difference_in_means(d, iv)) / 2), "sigma"

= 1 * sd(dv).

chains Number of chains for sampling.

cores Number of CPU cores to use for sampling. If omitted, all available cores are

used.

... Additional arguments passed to sampling function.

Value

A tridim_transformation object

See Also

```
fit_transformation_df
```

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fit_transformation_df Fitting Bidimensional or Tridimensional Regression / Geometric Transformation Models via Two Tables.

Description

Fits Bidimensional or Tridimensional regression / geometric transformation models using Stan engine. Two sets of coordinates are supplied via iv (for an independent variable) and dv (for the dependent one). The two tables must have the same dimensions (both N×2 or N×3).

For the 2D data, you can fit "translation" (2 for translation only), "euclidean" (4 parameters: 2 for translation, 1 for scaling, and 1 for rotation), "affine" (6 parameters: 2 for translation and 4 that jointly describe scaling, rotation and sheer), or "projective" (8 parameters: affine plus 2 additional parameters to account for projection).

For 3D data, you can fit "translation" (3 for translation only), "euclidean_x", "euclidean_y", "euclidean_z" (5 parameters: 3 for translation scale, 1 for rotation, and 1 for scaling), "affine" (12 parameters: 3 for translation and 9 to account for scaling, rotation, and sheer), and "projective" (15 parameters: affine plus 3 additional parameters to account for projection). transformations.

For details on transformation matrices and computation of scale and rotation parameters please see vignette("transformation_matrices", package = "TriDimRegression")

Usage

```
fit_transformation_df(
   iv,
   dv,
   transformation,
   priors = NULL,
   chains = 1,
   cores = NULL,
   ...
)
```

Arguments

iv a data frame containing independent variable, must by numeric only, $N\times 2$ or $N\times 3$.

dv a data frame containing dependent variable, must by numeric only, N×2 or N×3.

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 $transformation \ \ the \ transformation \ to \ be \ used: \ "translation" \ (both \ 2D \ and \ 3D), \ "euclidean"$

(2D), "euclidean_x", "euclidean_y", "euclidean_z" (3D, rotation about, respectively, x, y, and z axis), "affine" (2D and 3D), or "projective" (2D

and 3D).

priors named list of parameters for prior distributions of parameters a (translation,

normal distribution), b (all other parameters, normal distribution), and sigma (residual variance, exponential). E.g., list("a" = c(0, 10), "b" = c(0, 1),

"sigma"=1). Default priors are "a" = c(0, max_absolute_difference_in_means(d, iv)) / 2), "b" = c(0, max_absolute_difference_in_means(d, iv)) / 2), "sigma"

= 1 * sd(dv).

chains Number of chains for sampling.

cores Number of CPU cores to use for sampling. If omitted, all available cores are

used.

. . . Additional arguments passed to sampling function.

Value

A tridim_transformation object

See Also

fit_transformation

Examples

```
# Geometric transformations of 2D data
euc2 <- fit_transformation_df(NakayaData[, 1:2], NakayaData[, 3:4], 'euclidean')
tr3 <- fit_transformation_df(Face3D_W070, Face3D_W097, transformation ='translation')</pre>
```

FriedmanKohlerData1

Friedman & Kohler (2003), data set #1

Description

Data from Friedman, A., & Kohler, B. (2003). Bidimensional regression: Assessing the configural similarity and accuracy of cognitive maps and other two-dimensional data sets. Psychological Methods, 8(4), 468-491. DOI: 10.1037/1082-989X.8.4.468

Usage

FriedmanKohlerData1

Format

A data frame with 4 observations on the following 4 variables:

depV1, depV2 numeric vectors, dependent variables
indepV1, indepV2 numeric vectors, independent variables

FriedmanKohlerData2

Source

doi:10.1037/1082989X.8.4.468

FriedmanKohlerData2

Friedman & Kohler (2003), data set #2

Description

Data from Friedman, A., & Kohler, B. (2003). Bidimensional regression: Assessing the configural similarity and accuracy of cognitive maps and other two-dimensional data sets. Psychological Methods, 8(4), 468-491. DOI: 10.1037/1082-989X.8.4.468

Usage

FriedmanKohlerData2

Format

A data frame with 4 observations on the following 4 variables:

depV1, depV2 numeric vectors, dependent variables
indepV1, indepV2 numeric vectors, independent variables

Source

doi:10.1037/1082989X.8.4.468

is.tridim_transformation

Checks if argument is a tridim_transformation object

Description

Checks if argument is a tridim_transformation object

Usage

 $is.tridim_transformation(x)$

Arguments

Х

An R object

Value

Logical

NakayaData NakayaData

```
loo.tridim_transformation
```

Computes an efficient approximate leave-one-out cross-validation via loo library. It can be used for a model comparison via loo::loo_compare() function.

Description

Computes an efficient approximate leave-one-out cross-validation via loo library. It can be used for a model comparison via loo::loo_compare() function.

Usage

```
## S3 method for class 'tridim_transformation' loo(x, \ldots)
```

Arguments

```
x A tridim_transformation object
... unused
```

Value

```
A named list, see loo::loo() for details.
```

Examples

```
euc2 <- fit_transformation(depV1+depV2~indepV1+indepV2,
   NakayaData, transformation = 'euclidean')
aff2 <- fit_transformation(depV1+depV2~indepV1+indepV2,
   NakayaData, transformation = 'affine')
loo::loo_compare(loo(euc2), loo(aff2))</pre>
```

NakayaData

Nakaya (1997)

Description

Nakaya, T. (1997) Statistical inferences in bidimensional regression models. Geographical Analysis, 29(2), 169-186.

Usage

NakayaData

Format

A data frame with 19 observations on the following 4 variables:

```
depV1, depV2 numeric vectors, dependent variables
indepV1, indepV2 numeric vectors, independent variables
```

Source

```
doi:10.1111/j.15384632.1997.tb00954.x
```

```
plot.tridim_transformation

*Posterior interval plots for key parameters. Uses bayesplot::mcmc_intervals.

*Uses Dayesplot::mcmc_intervals.**
```

Description

Posterior interval plots for key parameters. Uses bayesplot::mcmc_intervals.

Usage

```
## S3 method for class 'tridim_transformation'
plot(x, convert_euclidean = FALSE, ...)
```

Arguments

```
    x A tridim_transformation object
    convert_euclidean
    Whether to convert matrix coefficients to scale(phi) and rotation(theta). Defaults to FALSE.
    ... Extra parameters to be passed to bayesplot::mcmc_intervals()
```

Value

```
A ggplot object produced by bayesplot::mcmc_intervals()
```

```
predict.tridim_transformation
```

Computes posterior samples for the posterior predictive distribution.

Description

Predicted values based on the bi/tridimensional regression model object.

Usage

```
## S3 method for class 'tridim_transformation'
predict(object, newdata = NULL, summary = TRUE, probs = NULL, ...)
```

Arguments

object	An object of class tridim_transformation
newdata	An optional two column data frame with independent variables. If omitted, the fitted values are used.
summary	Whether summary statistics should be returned instead of raw sample values. Defaults to TRUE
probs	The percentiles used to compute summary, defaults to NULL (no CI).
	Unused

Value

If summary=FALSE, a numeric matrix iterationsN x observationsN x variablesN. If summary=TRUE, a data.frame with columns "dvindex" with mean for each dependent variable plus optional quantiles columns with names "dvindex_quantile".

See Also

```
fit_transformation
```

```
euc2 <- fit_transformation(depV1+depV2~indepV1+indepV2,
   NakayaData, transformation = 'euclidean')

# prediction summary
predictions <- predict(euc2)

# full posterior prediction samples
predictions <- predict(euc2, summary=FALSE)</pre>
```

```
print.tridim_transformation
```

Prints out tridim_transformation object

Description

Prints out tridim_transformation object

Usage

```
## S3 method for class 'tridim_transformation' print(x, ...)
```

Arguments

```
x A tridim_transformation object
... Unused
```

Value

Nothing, console output only.

Examples

R2

Computes R-squared using Bayesian R-squared approach. For detail refer to: Andrew Gelman, Ben Goodrich, Jonah Gabry, and Aki Vehtari (2018). R-squared for Bayesian regression models. The American Statistician, doi:10.1080/00031305.2018.1549100.

Description

Computes R-squared using Bayesian R-squared approach. For detail refer to: Andrew Gelman, Ben Goodrich, Jonah Gabry, and Aki Vehtari (2018). R-squared for Bayesian regression models. The American Statistician, doi:10.1080/00031305.2018.1549100.

Usage

```
## S3 method for class 'tridim_transformation'
R2(object, summary = TRUE, probs = c(0.055, 0.945), ...)
```

Arguments

object An object of class tridim_transformation

summary Whether summary statistics should be returned instead of raw sample values.

Defaults to TRUE

probs The percentiles used to compute summary, defaults to 89% credible interval.

... Unused.

Value

vector of values or a data.frame with summary

Examples

```
euc2 <- fit_transformation(depV1+depV2~indepV1+indepV2,
   NakayaData, transformation = 'euclidean')
R2(euc2)</pre>
```

```
summary.tridim_transformation
```

Summary for a tridim_transformation object

Description

Summary for a tridim_transformation object

Usage

```
## S3 method for class 'tridim_transformation'
summary(object, ...)
```

Arguments

object A tridim_transformation object

... Unused

Value

Nothing, console output only.

```
tridim_transformation-class
```

Class tridim_transformation.

Description

Geometric transformations fitted with the fit_transformation function represented as a tridim_transformation object with information about transformation, data dimension, call formula, and fitted stanfit object,

Details

See methods(class = "tridim_transformation") for an overview of available methods.

Slots

```
transformation A string with the transformation name. formula A formula object.

Ndim An integer with data dimension, either 2 or 3. data A list containing variables used for the sampling. stanmodel A stanmodel used for sampling. stanfit a stanfit object.
```

See Also

fit_transformation

```
waic.tridim_transformation
```

Computes widely applicable information criterion (WAIC).

Description

Computes widely applicable information criterion via loo library. It can be used for a model comparison via loo::loo_compare() function.

Usage

```
## S3 method for class 'tridim_transformation' waic(x, ...)
```

Arguments

```
x A [tridim_transformation[tridim_transformation-class() object ... unused
```

Value

```
A named list, see loo::waic() for details.
```

```
euc2 <- fit_transformation(depV1+depV2~indepV1+indepV2,
   NakayaData, transformation = 'euclidean')
aff2 <- fit_transformation(depV1+depV2~indepV1+indepV2,
   NakayaData, transformation = 'affine')
loo::loo_compare(waic(euc2), waic(aff2))</pre>
```

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