Package 'BayesTwin'

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BayesTwin

Bayesian analysis of item-level twin data

Description

This package can be used to perform bayesian analysis of item-level twin data. Simulatenously with the biometric model (ACE/ADE or AE), an item response theory (IRT) model is estimated to take into account properties of the measurement scale. Functions are included in the package that help plot relevant information in figures and compute posterior statistics such as HPD intervals.

Caution! The subroutines of this package rely on the program JAGS, which can be freely obtained from http://mcmc-jags.sourceforge.net.

Details

Package: BayesTwin
Type: Package
Version: 0.1.0
Date: 2017-01-06
License: GPL-2

The main function IRT_twin can be used to analyse item-level twin data under the ACE, ADE or AE model. Simultaneously with the biometric model, an item response theory (IRT) measurement model is estimated. For dichotomous item data, the 1 parameter model (1PL) or the 2 parameter model (2PL) can be used and for polytomous item data, the partial credit model (PCM) or the generalized partial credit model (GPCM). Optionally, genotype by environment interaction (GxE) can be estimated and/or covariates can be included in the analysis. GxE is assessed in the case that the unique environment features as latent (i.e., unmeasured) variable, using the parametrization as described in Schwabe & van den Berg (2014, 2016) and Schwabe, Boomsma & van den Berg (2017). The function returns MCMC samples as well as posterior means, standard deviations and 95% HPD intervals for all variance components. Objects returned from the function are assigned the class "Bayestwin" which has its own summary method that can be used to summarize the output. The function plotbayestwin can be used to create sampling plots or plot posterior distributions and the function geplot to plot the 95% credibility region of the GxE interaction effect.

The function simulate_twin_data can be used to simulate item-level twin data under all common biometric models (ACE/ADE or AE). For the simulation of the item data, a 1PL, 2PL, PCM or GPCM can be used. Optionally, the data can be simulated with GxE, using the parametrization as described in Schwabe & van den Berg (2014, 2016) and Schwabe, Boomsma & van den Berg (2017).

Note

To work, this packages requires the program JAGS to be in the PATH variable. JAGS can be freely obtained from http://mcmc-jags.sourceforge.net.

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Author(s)

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References

Schwabe, I. & van den Berg, S.M. (2014). Assessing Genotype by Environment Interaction in Case of Heterogeneous Measurement Error, Behavior Genetics, 44 (4), 394-406.

Molenaar, D. & Dolan, C.V. (2014). Testing Systematic Genotype by Environment Interactions Using Item Level Data, Behavior Genetics, 44(3), 212-231.

Schwabe, I., Jonker, W. & van den Berg, S.M. (2016). Genes, Culture and Conservatism - A Psychometric-Genetic Approach, Behavior Genetics, 46 (4), 516-52.

Schwabe, I., Boomsma, D.I. & van den Berg, S.M. (2017). Increased Environmental Sensitivity in High Mathematics Performance. Learning and Individual Differences, 54, 196-201.

Examples

```
data(results)
summary(results)
#Using the output to obtain the 95% HPD for additive genetic variance
HPD(results$samples_var_a)
#Using the output to obtain the 90% HPD for all item difficulty parameters
apply(results\$samples_item_b, 1, function (x) HPD(x, 0.90))
##Simulate Item-level twin data under the 1PL Rasch model
data = simulatetwin(irt_model = "1PL", var_a = 0.5, var_c = 0.3, ge_beta0 = log(0.2),
                    ge = TRUE)
data_mz = data\$y_mz
data_dz = data\$y_dz
##Analyse the simulated data under an 1PL model with GxE
results = IRTtwin(data_mz, data_dz, 1:20, 21:40, ge = TRUE)
##Summarize results:
summary(results)
#Using the output to obtain the 95% HPD for additive genetic variance
HPD(results$samples_var_a)
#Using the output to obtain the 90% HPD for all item difficulty parameters
apply(results\$samples_item_b, 1, function (x) HPD(x, 0.90))
##Plot trace lines for var(A)
plotbayestwin(results$samples_var_a, type = "trace")
##Plot posterior distribution of var(A)
plotbayestwin(results$samples_var_a)
```

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```
##Plot 95% credibility region of GxE interaction effect
geplot(results$var_a, results$samples_beta0, results$samples_beta1)
## End(Not run)
```

geplot

Plots 95% credibility interval of GxE interaction

Description

This function plots the 95% credibility region of a GxE interaction effect.

Usage

```
geplot(var_a, samples_beta0, samples_beta1, main, xlab, ylab, col, ...)
```

Arguments

var_a	A single value representing the posterior point estimate for genetic variance
samples_beta0	A vector representing draws from the posterior distribution of beta0, as produced by the main function IRT_twin of this package
samples_beta1	A vector representing draws from the posterior distribution of beta1, as produced by the main function IRT_twin of this package
main	An overall title for the plot
xlab	A title for the x axis
ylab	A title for the y axis
col	Color of the lines
	Further arguments for the default S3 plot method

Details

The 95 % credibility region for the GxE interaction effect is displayed for the entire range of estimated genotypic values in the interval of -2 and 2 standard deviations of the posterior point estimate of genetic variance.

The function expects as input the posterior point estimate for genetic variance and two vectors representing draws from the posterior distributions of beta0 and beta1 respectively, as produced by the main function IRT_twin of this package.

Value

Plot of the 95% credibility region of the GxE interaction.

Author(s)

Inga Schwabe

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Examples

```
#Using the output to plot the 95% credibility region
data(results)
geplot(results$var_a, results$samples_beta0, results$samples_beta1)
```

HPD

Calculate highest posterior density interval

Description

This function calculates the Bayesian highest posterior density interval (HPD) based on a parameters' posterior sample.

Usage

```
HPD(sample, cred_int = 0.95)
```

Arguments

sample A vector representing draws from the target distribution of the paramter of in-

terest, as produced by the main function IRT_twin of this package.

cred_int The desired accuracy of the HPD. Default value is 0.95 for 95%.

Details

The highest posterior density interval (HPD, see e.g. Box & Tia, 1992) contains the required mass such that all points within the interval have a higher probability density than points outside of the interval.

The function expects as input a vector representing draws from the target distribution of the paramter of interest, such as produced by the main function IRT_twin of this package.

The result is a vector consisiting of two values, the first value representing the lower bound of the HPD and the second value representing the upper bound.

Value

A vector of length 2 with the lower (first value) and upper (second value) bound of the HPD.

Author(s)

Inga Schwabe

References

Box, G., & Tiao, G. (1992). Bayesian inference in statistical analysis. New York: John Wiley & Sons.

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Examples

```
data(results)
#Obtain the 95% HPD for additive genetic variance
HPD(results$samples_var_a)
#Obtain the 90% HPD for all item difficulty parameters
apply(results$samples_item_b, 1, function (x) HPD(x, 0.90))
```

IRTtwin

Bayesian analysis of item-level twin data

Description

Bayesian analysis of item-level twin data under the AE, ACE or ADE model. Covariates can be included an a GxE interaction effect can be estimated.

Usage

Arguments

data_mz Phenotypic as well as covariate data of MZ twins in matrix form.

data_dz Phenotypic as well as covariate data of DZ twins in matrix form.

twin1_datacols_p

Columns of data_mz or respectively data_dz in which phenotypic data is stored for the first twin of all MZ and DZ twins, e.g. c(1,2,3) if they are stored in the first three columns or c(20:40) if stored in column 20 through 40.

twin2_datacols_p

Columns of data_mz or respectively data_dz in which phenotypic data is stored for the second twin of all MZ and DZ twins.

twin1_datacols_cov

Columns of data_mz or respectively data_dz in which covariate data is stored for the first twin of all MZ and DZ twins.

twin2_datacols_cov

Columns of data_mz or respectively data_dz in which covariate data is stored for the second twin of all MZ and DZ twins.

decomp_model Choice of the biometric model under which the data is analyzed, either "ACE", "ADE" or "AE". Default model is "ACE" model.

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irt_model	Choice of the measurement (IRT) model under which the item data is simulated. "1PL" = 1 PL model, "2PL" = 2PL model, "PCM" = Partial credit model, "GPCM" = Generalized partial credit model
ge	Indication whether data is analyzed with (ge = TRUE) or without (ge = FALSE) GxE. Default value is FALSE.
n_iter	Total number of MCMC iterations (without burn-in period). Default number is 5.000
n_burnin	Total number of burn-in iterations for the MCMC analysis. Default number is 7.000
n_chains	Number of MCMC chains. Default number is 1.
fit_stats	Should be set to TRUE when fit statistics are needed (e.g., DIC, BIC). In this case, multiple chains need to be used (the parameter n_chains should be set to at least 2)
var_prior	Choice of prior distributions used for the variance components, either "INV_GAMMA" for an inverse gamma distribution or "UNIF" for uniform distribution. For a low total phenotypic variance, uniform prior distributions are recommended. Default value is "INV_GAMMA".
N_cov	Number of covariates. Default value is 0.
inits	Initial values for the MCMC analysis. Default is NULL.
Nk	Number of categories in case of polytomous item data. As the default IRT model is a 1PL, the default value is set 0.

Details

Bayesian analysis of item-level twin data under all common biometric models (i.e., A(C)E, ADE) with or without genotype by environment interaction (GxE). For the simulation of dichotomous item data, the one parameter logistic model (1PL) or the 2 parameter logistisc model (2PL) can be used. For polytomous item data, the partial credit model (PCM) or the generalized partial credit model (GPCM) can be used. Optionally, covariates can be included in the analysis.

GxE is defined modelled as heterogeneous unique-environmental variance and is defined as $\sigma^2 Eij = exp(\beta 0 + \beta 1Aij)$ under the ACE model and as $\sigma^2 Eij = exp(\beta 0 + \beta 1Gij)$ under the ADE model where $\beta 0$ refers to an intercept (unique-environmental variance when Aij or respectively Gij = 0) and $\beta 1$ represents the GxE interaction effect. Aij represents the genotypic value for twin j from family i, likewise G represents the total genotypic value (both additive and non-additive genetic effects) for twin j from family i. For more detail see Schwabe & van den Berg (2014), Behavior Genetics, 44(4), 394-406 and Schwabe, Boomsma & van den Berg (2017), Learning and Individual Differences, 54, 196-201.

Value

Output of the class "bayestwin" including samples, posterior point estimates, standard deviations and the 95% HPD interval for variance components and, if applicable, regression parameters. Call str(results) if the output of IRT_twin is stored in an object called results to see a list of all stored variables.

Results are printed on the fly for variance components and, if applicable, regression parameters.

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Author(s)

Inga Schwabe

Examples

```
data(results)
#Summarize results
summary(results)
##Plot posterior distribution of var(A)
plotbayestwin(results$samples_var_a)
##Plot 95% credibility region of GxE interaction effect
geplot(results$var_a, results$samples_beta0, results$samples_beta1)
## Not run:
##Simulate data
data = simulate(irt_model = "1PL", var_a = 0.5, var_c = 0.3, ge_beta0 = log(0.2),
                ge = TRUE)
data_mz = data\$y_mz
data_dz = data y_dz
##Run analysis
results = IRTtwin(data_mz, data_dz, 1:20, 21:40, ge = TRUE)
##Summarize results:
summary(results)
##Plot trace lines for var(A)
plotbayestwin(results$samples_var_a, type = "trace")
##Plot posterior distribution of var(A)
plotbayestwin(results$samples_var_a)
##Plot 95% credibility region of GxE interaction effect
geplot(results$var_a, results$samples_beta0, results$samples_beta1)
## End(Not run)
```

plotbayestwin

Summary plots of BayesTwin MCMC-objects

Description

plotbayestwin returns either a density or trace plot for the target parameter.

Usage

```
plotbayestwin(sample, t = "density", main, xlab, ylab, legend = TRUE, lines = TRUE, ...)
```

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Arguments

sample	A vector representing draws from the posterior distribution of the parameter of interest, as produced by the main function IRT_twin of this package
t	Type of plot that is produced, either "density" to get a histogram of the posterior distribution or "trace"to get a trace plot. Default value is "density"
main	An overall title for the plot
xlab	A title for the x axis
ylab	A title for the y axis
legend	Indicating if a legend should be added. Default value is TRUE.
lines	Indicating if lines for mean, median and lower and upper limit of the 95% HPD should be added. Default value is TRUE
• • •	Further arguments for the generic S3 method histogram (for the density plot) or plot (for the trace plot) method

Details

Creates either a density or trace plot for the target parameter.

The function expects as input a vector representing draws from the posterior distributions of the parameter of interest, as produced by the main function IRT_twin of this package.

Author(s)

Inga Schwabe

Examples

```
data(results)
##Plot posterior distribution of var(A)
plotbayestwin(results$samples_var_a)
```

results

Sample output of a BayesTwin analysis

Description

Sample MCMC output from IRTtwin of an analysis of simulated data. The data were simulated and analysed using an ACE and 1 PL model including genotype-environment interaction (GxE).

Usage

```
data(results)
```

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Format

An bayestwin object

Source

Schwabe, I. (submitted for publication). BayesTwin - An R Package for Bayesian Inference of Item-Level Hierarchical Twin Data.

Description

Simulation of item-level twin data under the AE, ACE or ADE model with or without genotype by environment interaction (GxE).

Usage

```
simulatetwin(n_mz = 140, n_dz = 360, var_a = 0.5, var_c = 0.3, var_e = 0.2, var_d = 0, model = "ACE", n_items = 20, n_cat = 0, ge = FALSE, ge_beta0 = 0, ge_beta1 = 0, irt_model = "1PL")
```

Arguments

n_mz	Number of monozygotic (MZ) twin pairs. Default value is 140.
n_dz	Number of dizygotic (DZ) twin pairs. Default value is 360.
var_a	Variance explained by additive genetic influences. Default value is 0.5.
var_c	Variance explained by shared environmental influences. Default value is 0.3.
var_e	Variance explained by unique environmental influences. Default value is 0.2.
var_d	Variance explained by dominance genetic influences. As the default model is an "ACE" model, the default value is set to 0 .
model	Biometric model used for the simulation, either "ACE", "ADE" or "AE". Default model is "ACE" model.
n_items	Number of test items. Default value is 20.
n_cat	Number of categories for the simulation of polytomous item data. As the default IRT model is a 1PL, the default is set 0 .
ge	Indication whether data is simulated with (ge = TRUE) or without (ge = FALSE) GxE. Default value is FALSE
ge_beta0	When data is simulated with $ge = TRUE$, average environmental variance (when $A = 0$) has to be defined. Default value is 0.
ge_beta1	When data is simulated with ge = TRUE, the GxE interaction parameter has to be defined. Default value is 0.
irt_model	Choice of the measurement (IRT) model under which the item data is simulated. $"1PL" = 1$ PL model, $"2PL" = 2PL$ model, $"PCM" = Partial$ credit model, $"GPCM" = Generalized$ partial credit model.

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Details

Item twin data is simulated under all common biometric models (i.e., A(C)E, ADE) with or without genotype by environment interaction (GxE). Data is simulated with an average phenotypic value of 0. For the simulation of dichotomous item data, the 1 PL or 2 PL can be used. For polytomous item data with three or more categories, the partial credit model (PCM) or the generalized partial credit model (GPCM) can be used.

Genotype by environment interaction is defined modelled as heterogeneous unique-environmental variance and is defined as $\sigma^2 Eij = exp(\beta 0 + \beta 1Aij)$ under the ACE model and as $\sigma^2 Eij = exp(\beta 0 + \beta 1Gij)$ under the ADE model where $\beta 0$ refers to an intercept (unique-environmental variance when Aij or respectively Gij = 0) and $\beta 1$ represents the GxE interaction effect. Aij represents the genotypic value for twin j from family i, likewise G represents the total genotypic value (both additive and non-additive genetic effects) for twin j from family i. For more detail see Schwabe & van den Berg (2014, 2016) or Schwabe, Boomsma & van den Berg (2017).

Value

Two matrices are returned, y_mz for MZ twin pairs and y_dz for DZ twin pairs. For a total of n_items , the result is a matrix of n_mz rows for the i-th MZ family and $2*n_items$ columns with the item answers of the first (columns $1:n_items$) and second twin (columns $n_items + 1:2*n_items$) of a family. For example, $y_mz[1,22]$ is the response of the first twin from family 1 to item 22 and $y_mz[1,23]$ is the response of the second twin 2 from family 1 to item 1 if $n_items = 22$. The same logic applies to the data of DZ families.

Author(s)

Inga Schwabe

References

Schwabe, I. & van den Berg, S.M. (2014). Assessing Genotype by Environment Interaction in Case of Heterogeneous Measurement Error, Behavior Genetics, 44 (4), 394-406.

Schwabe, I., Jonker, W. & van den Berg, S.M. (2016). Genes, Culture and Conservatism - A Psychometric-Genetic Approach, Behavior Genetics, 46 (4), 516-52.

Schwabe, I., Boomsma, D.I. & van den Berg, S.M. (2017). Increased Environmental Sensitivity in High Mathematics Performance. Learning and Individual Differences, 54, 196-201.

Examples

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```
## End(Not run)
```

summary.bayestwin

Summary statistics for BayesTwin analysis

Description

summary.bayestwin produces summary statistics for variance components and, if applicable, regression parameters: The posterior point estimate and its standard deviation and the 95% HPD.

Usage

```
## S3 method for class 'bayestwin'
summary(object, ...)
```

Arguments

object An object storing output from the main function IRT_twin
... Further arguments for the default S3 summary method

Author(s)

Inga Schwabe

Examples

```
data(results)
summary(results)
```

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