# Package 'flexrsurv'

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Description Package for parametric relative survival analyses. It allows to model non-linear and non-proportional effects and both non proportional and non linear effects, using splines (B-spline and truncated power basis), Weighted Cumulative Index of Exposure effect, with correction model for the life table. Both non proportional and non linear effects are described in Remontet, L. et al. (2007) <doi:10.1002 sim.2656=""> and Mahboubi, A. et al. (2011) <doi:10.1002 sim.4208="">.</doi:10.1002></doi:10.1002>
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flexrsurv-package

Package for flexible relative survival analyses

## **Description**

flexrsurv is a package for parametric relative survival analyses. The package implements non-linear, non-proportional effects and both non proportional and non linear effects, using splines (B-spline and truncated power basis), Weighted Cumulative Index of Exposure effect, with correction model for the life table. Both non proportional and non linear effects are described in Remontet et al. (2007) doi:10.1002/sim.2656 and Mahboubi et al. (2011) doi:10.1002/sim.4208.

The main function is flexrsurv()

#### Author(s)

Michel Grzebyk and Isabelle Clerc-Urmès, with contributions from the CENSUR working survival group.

Maintainer: <michel.grzebyk@inrs.fr>

#### References

Mahboubi, A., M. Abrahamowicz, et al. (2011). "Flexible modeling of the effects of continuous prognostic factors in relative survival." Stat Med 30(12): 1351-1365. doi:10.1002/sim.4208

Remontet, L., N. Bossard, et al. (2007). "An overall strategy based on regression models to estimate relative survival and model the effects of prognostic factors in cancer survival studies." Stat Med 26(10): 2214-2228. doi:10.1002/sim.2656

#### See Also

flexrsurv

flexrsurv

Fit Relative Survival Model

## **Description**

flexrsurv is used to fit relative survival regression model. Time dependent variables, non-proportionnal (time dependent) effects, non-linear effects are implemented using Splines (B-spline and truncated power basis). Simultaneously non linear and non proportional effects are implemented using approaches developed by Remontet et al.(2007) and Mahboubi et al. (2011).

## Usage

```
flexrsurv(formula=formula(data),
   data=parent.frame(),
   knots.Bh,
   degree.Bh=3,
   Spline=c("b-spline", "tp-spline", "tpi-spline"),
   log.Bh=FALSE,
   bhlink=c("log", "identity"),
  Min_T=0,
   Max_T=NULL,
   model=c("additive", "multiplicative"),
   rate=NULL,
   weights=NULL,
   na.action=NULL,
   int_meth=c("GL", "CAV_SIM", "SIM_3_8", "BOOLE", "BANDS"),
   npoints=20,
   stept=NULL,
   bands=NULL,
   init=NULL,
   initbyglm=TRUE,
   initbands=bands,
   optim.control=list(trace=100, REPORT=1, fnscale=-1, maxit=25),
   optim_meth=c("BFGS", "CG", "Nelder-Mead", "L-BFGS-B", "SANN", "Brent"),
  control.glm=list(epsilon=1e-8, maxit=100, trace=FALSE, epsilon.glm=1e-1, maxit.glm=25),
   vartype = c("oim", "opg", "none"),
   debug=FALSE
   )
flexrsurv.ll(formula=formula(data),
   data=parent.frame(),
   knots.Bh=NULL,
   degree.Bh=3,
   Spline=c("b-spline", "tp-spline", "tpi-spline"),
   log.Bh=FALSE,
   bhlink=c("log", "identity"),
```

```
Min_T=0,
Max_T=NULL,
model=c("additive","multiplicative"),
rate=NULL,
weights=NULL,
na.action=NULL,
int_meth=c("GL", "CAV_SIM", "SIM_3_8", "BOOLE", "GLM", "BANDS"),
npoints=20,
stept=NULL,
bands=NULL,
init=NULL,
optim.control=list(trace=100, REPORT=1, fnscale=-1, maxit=25),
optim_meth=c("BFGS", "CG", "Nelder-Mead", "L-BFGS-B", "SANN", "Brent"),
vartype = c("oim", "opg", "none"),
debug=FALSE
)
```

#### **Arguments**

formula	a formula object, with the response on the left of a ~ operator, and the terms
	on the right. The response must be a survival object as returned by the Surv
	function.

data a data.frame in which to interpret the variables named in the formula.

knots.Bh the internal breakpoints that define the spline used to estimate the baseline hazard. Typical values are the mean or median for one knot, quantiles for more

knots.

degree .Bh degree of the piecewise polynomial of the baseline hazard. Default is 3 for cubic

splines.

Spline a character string specifying the type of spline basis. "b-spline" for B-spline

basis, "tp-spline" for truncated power basis and "tpi-spline" for monotone (in-

creasing) truncated power basis.

log.Bh logical value: if TRUE, an additional basis equal to log(time) is added to the

spline bases of time.

bhlink logical value: if TRUE, log of baseline hazard is modelled, if FALSE, the base-

line hazard is out of the log.

Min\_T minimum of time period which is analysed. Default is max(0.0, min(bands)

).

Max\_T maximum of time period which is analysed. Default is max(c(bands, timevar))

model character string specifying the type of model for both non-proportionnal and non

linear effects. The model method=="additive" assumes effects as explained in Remontet et al.(2007), the model method=="multiplicative" assumes effects

as explained in Mahboubi et al. (2011).

rate an optional vector of the background rate for a relevant comparative population

to be used in the fitting process. Should be a numeric vector (for relative survival model). rate is evaluated in the same way as variables in formula, that is first

in data and then in the environment of formula.

weights an optional vector of weights to be used in the fitting process. Should be NULL

or a numeric vector. If not null, the total likelihood is the weighted sum of

individual likelihood.

na.action a missing-data filter function, applied to the model.frame, after any subset argu-

ment has been used. Default is options()\$na.action.

int\_meth character string specifying the the numerical integration method. Possible values

are "GL" for Gauss-Legendre quadrature, "CAV\_SIM" for Cavalieri-Simpson's rule, "SIM\_3\_8" for the Simpson's 3/8 rule, "BOOLE" for the Boole's rule, or

"BANDS" for the midpoint rule with specified bands.

npoints number of points used in the Gauss-Legendre quadrature (when int\_meth="GL").

stept scalar value of the time-step in numerical integration. It is required only when

int\_meth="CAV\_SIM" or "SIM\_3\_8" or "BOOLE". If no value is supplied, Max\_T/500

is used.

bands bands used to split data in the numerical integration when int\_meth="BANDS".

init starting values of the parameters.

initbyglm a logical value indicating indicating how are found or refined init values. If

TRUE, the fitting method described in Remontet et al.(2007) is used to find or refine starting values. This may speedup the fit. If FALSE, the maximisation of the likelihood starts at values given in init. If init=NULL, the starting values correspond to a constant net hazard equal to the ratio of the number of event

over the total number of person-time.

initbands bands used to split data when initbyglm=TRUE.

optim.control a list of control parameters passed to the optim() function. optim\_meth method to be used to optimize the likelihood. See optim.

control.glm a list of control parameters passed to the glm() function when method="glm".

vartype character string specifying the type of variance matrix computed by flexrsurv:

the inverse of the hessian matrix computed at the MLE estimate (ie. the inverse of the observed information matrix) if vartype="oim", the inverse of the outer product of the gradients if vartype="opg". The variance is not computed when

vartype="none".

debug control the volum of intermediate output

#### Details

A full description of the additive and the multiplicative both non-linear and non-proportional models is given respectively in Remontet (2007) and Mahboubi (2011).

flexrsurv. ll is the workhorse function: it is not normally called directly.

#### Value

flexrsurv returns an object of class "flexrsurv". An object of class "flexrsurv" is a list containing at least the following components:

coefficients a named vector of coefficients

loglik the log-likelihood

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var estimated covariance matrix for the estimated coefficients

informationMatrix

estimated information matrix

bhlink the linkk of baseline hazard: if "identity" baseline = sum g0\_i b\_i(t); if "log"

 $log(baseline) = sum g0_i b_i(t);$ 

init vector of the starting values supplied

converged logical, Was the optimizer algorithm judged to have converged?

linear.predictors

the linear fit on link scale (not including the baseline hazard term if bhlink =

"identity")

fitted.values the estimated value of the hazard rate at each event time, obtained by transform-

ing the linear predictors by the inverse of the link function

cumulative.hazard

the estimated value of the cumulative hazard in the time interval

call the matched call
formula the formula supplied
terms the terms object used
data the data argument
rate the rate vector used
time the time vector used

workingformula the formula used by the fitter

optim.control the value of the optim.control argument supplied control.glm the value of the control.glm argument supplied

method the name of the fitter function used

#### References

Mahboubi, A., M. Abrahamowicz, et al. (2011). "Flexible modeling of the effects of continuous prognostic factors in relative survival." Stat Med 30(12): 1351-1365. doi:10.1002/sim.4208

Remontet, L., N. Bossard, et al. (2007). "An overall strategy based on regression models to estimate relative survival and model the effects of prognostic factors in cancer survival studies." Stat Med 26(10): 2214-2228. doi:10.1002/sim.2656

#### See Also

```
print.flexrsurv, summary.flexrsurv, logLik.flexrsurv, predict.flexrsurv, NPH, NLL, and NPHNLL.
```

# Examples

```
if (requireNamespace("relsurv", quietly = TRUE)) {
```

```
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
# get the death rate at event (or end of followup) from slopop for rdata
rdata$iage <- findInterval(rdata$age*365.24+rdata$time, attr(slopop, "cutpoints")[[1]])
rdata$iyear <- findInterval(rdata$year+rdata$time, attr(slopop, "cutpoints")[[2]])
therate <- rep(-1, dim(rdata)[1])</pre>
for( i in 1:dim(rdata)[1]){
 therate[i] <- slopop[rdata$iage[i], rdata$iyear[i], rdata$sex[i]]</pre>
rdata$slorate <- therate
# change sex coding
rdata$sex01 <- rdata$sex -1
# fit a relative survival model with a non linear effect of age
fit <- flexrsurv(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
                 rate=slorate, data=rdata,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Max_T=5400,
                 Spline = "b-spline",
                 initbyglm=TRUE,
                 initbands=seq(0, 5400, 100),
                 int_meth= "BANDS",
                 bands=seq(0, 5400, 50)
                 )
summary(fit)
# fit a relative survival model with a non linear & non proportional effect of age
fit2 <- flexrsurv(Surv(time,cens)~sex01+NPHNLL(age, time, Knots=60,</pre>
                                                Knots.t = 1850, Degree.t = 3),
                 rate=slorate, data=rdata,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Spline = "b-spline",
                 initbyglm=TRUE,
                 int_meth= "BOOLE",
                 step=50
                 )
summary(fit2, correlation=TRUE)
}
```

flexrsurvclt

Fit Relative Survival Model and Correct Life Tables

#### Description

flexrsurvclt is used to fit relative survival regression model. transition package.

## Usage

```
flexrsurvclt(formula=formula(data),
formula.table=NULL,
data=parent.frame(),
Id,
baselinehazard=TRUE,
firstWCEIadditive=FALSE,
knots.Bh,
degree.Bh=3,
intercept.Bh=TRUE,
Spline=c("b-spline", "tp-spline", "tpi-spline"),
log.Bh=FALSE,
bhlink=c("log", "identity"),
Min_T=0,
Max_T=NULL,
model=c("additive", "multiplicative"),
rate,
logit_start,
logit_end,
logit_start_byperiod = NULL,
logit_end_byperiod = NULL,
weights_byperiod = NULL,
Id_byperiod = NULL,
contrasts.table = NULL,
knots.table=c(-2.5,0,2.5),
degree.table=3,
Spline.table=c("restricted B-splines"),
Spline.CLT=R2bBSplineBasis(knots=c(-2.5,0,2.5), degree=3),
model_correction = c("cohort", "period"),
weights=NULL,
na.action=NULL,
datacontrol=NULL,
Idcontrol,
ratecontrol,
logit_startcontrol,
logit_endcontrol,
logit_start_byperiodcontrol = NULL,
logit_end_byperiodcontrol = NULL,
weights_byperiodcontrol = NULL,
```

```
Id_byperiodcontrol = NULL,
weightscontrol=NULL,
int_meth=c("GL", "CAV_SIM", "SIM_3_8", "BOOLE", "GLM", "BANDS"),
bands=NULL,
npoints=20,
stept=NULL,
init=NULL,
initbyglm=TRUE,
initbands=bands,
optim.control=list(trace=100, REPORT=1, fnscale=-1, maxit=25),
optim_meth=c("BFGS", "CG", "Nelder-Mead", "L-BFGS-B", "SANN", "Brent"),
Coptim.control=list(),
lower = -Inf,
upper = Inf,
control.glm=list(epsilon=1e-8, maxit=100, trace=FALSE,
epsilon.glm=.1, maxit.glm=25),
vartype = c("oim", "opg", "none"),
varmethod = c("optim", "numDeriv.hessian", "numDeriv.jacobian"),
numDeriv.method.args=list(eps=5e-7, d=0.001,
zero.tol=sqrt(.Machine$double.eps/7e-4), r=4, v=2),
debug=FALSE
   )
flexrsurvclt.ll(formula=formula(data),
formula.table=NULL,
data=parent.frame(),
Id,
baselinehazard=TRUE,
firstWCEIadditive=FALSE,
knots.Bh,
degree.Bh=3,
Spline=c("b-spline", "tp-spline", "tpi-spline"),
log.Bh=FALSE,
bhlink=c("log", "identity"),
intercept.Bh=TRUE,
Min_T=0,
Max_T=NULL,
model=c("additive", "multiplicative"),
rate,
logit_start,
logit_end,
logit_start_byperiod = NULL,
logit_end_byperiod = NULL,
weights_byperiod = NULL,
Id_byperiod = NULL,
contrasts.table = NULL,
knots.table=c(-2.5,0,2.5),
degree.table=3,
```

```
Spline.table=c("restricted B-splines"),
Spline.CLT=R2bBSplineBasis(knots=c(-2.5,0,2.5), degree=3),
model_correction = c("cohort", "period"),
weights=NULL,
na.action=NULL,
datacontrol=NULL,
Idcontrol,
ratecontrol,
logit_startcontrol,
logit_endcontrol,
logit_start_byperiodcontrol = NULL,
logit_end_byperiodcontrol = NULL,
weights_byperiodcontrol = NULL,
Id_byperiodcontrol = NULL,
weightscontrol=NULL,
int_meth=c("GL", "CAV_SIM", "SIM_3_8", "BOOLE", "GLM", "BANDS"),
bands=NULL,
npoints=20,
stept=NULL,
init=NULL,
optim.control=list(trace=100, REPORT=1, fnscale=-1, maxit=25),
Coptim.control= list(),
optim_meth=c("BFGS", "CG", "Nelder-Mead", "L-BFGS-B", "SANN", "Brent"),
lower = -Inf,
upper = Inf,
vartype = c("oim", "opg", "none"),
varmethod = c("optim", "numDeriv.hessian", "numDeriv.jacobian"),
numDeriv.method.args=list(eps=5e-7, d=0.001,
  zero.tol=sqrt(.Machine$double.eps/7e-4), r=4, v=2),
debug=FALSE
   )
```

#### **Arguments**

formula a formula object, with the response on the left of a ~ operator, and the terms

on the right. The response must be a survival object as returned by the Surv

function.

formula.table a formula object, with empty left hand side, and the terms on the right. This is

the formula of the proportional part of the correction model for the table table

data a data frame in which to interpret the variables named in the formulas.

Id vector whose unique values defines the Ids of the subjects.

baselinehazard if FALSE, no baseline hazard in the model

firstWCEIadditive

if TRUE, the first WCEI term in the formula is considered as the baseline

knots.Bh the internal breakpoints that define the spline used to estimate the baseline haz-

ard. Typical values are the mean or median for one knot, quantiles for more

knots.

degree.Bh	degree of the piecewise polynomial of the baseline hazard. Default is 3 for cubic splines.
intercept.Bh	TRUE if the first bases is included in the baseline hazard. Default is TRUE.
Spline	a character string specifying the type of spline basis. "b-spline" for B-spline basis, "tp-spline" for truncated power basis and "tpi-spline" for monotone (increasing) truncated power basis.
log.Bh	logical value: if TRUE, an additional basis equal to log(time) is added to the spline bases of time.
bhlink	character string specifying the link function of the baseline hazard: Default is bhlink="log" for including the baseline in the exponential; if bhlink="identity", the baseline hazard is out of the exponential.
Min_T	minimum of time period which is analysed. Default is $max(0.0, min(bands))$ .
Max_T	maximum of time period which is analysed. Default is max(c(bands, timevar))
model	character string specifying the type of model for both non-proportional and non linear effects. The model method=="additive" assumes effects as explained in Remontet et al.(2007), the model method=="multiplicative" assumes effects as explained in Mahboubi et al. (2011).
rate	a vector of the background rate for a relevant comparative population to be used in the fitting process. Should be a numeric vector (for relative survival model). rate is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.
logit_start	a vector of the logit of the cumulative hazard at the start of the interval in the life table. logit_start is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.
logit_end	a vector of the logit of the cumulative hazard at the end of the interval in the life table. logit_end is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.
logit_start_by	period, logit_end_byperiod, weights_byperiod, Id_byperiod A REMPLIR
knots.table	the internal breakpoints on the logit scale that define the knots of the spline used to estimate the correction model of the life table.
degree.table	degree of the piecewise polynomial of the spline used to estimate the correction model of the life table. Default is 3 for cubic splines.
contrasts.tabl	e an optional list. See the contrasts.arg of model.matrix().
Colina table	
Spline.table	a character string specifying the type of spline basis of the the correction model of the life table. In this version, only "restricted B-splines" is available. "restricted B-splines" are B-spline basis with linear extrapolation + 2nd derivative at boundaries == 0.
Spline.CLT	a S4 object with method deriv() and evaluate(). The spline basis of the correction of the life table can be specified either by the parameters (knots.table, degree.table) or an S4 object that ca be used for this purpose. IMPORTANT: the coef of the first basis is constraints to one and evaluate(deriv(spline_B), left_boundary_knots) == 1

model\_correction

character string specifying A COMPLETER. method\_correction="cohort"

when the provided logit are those of the survival of individuals; method\_correction="period"

when the provided logit are those of the survival fuction of age distribution by

period.

weights an optional vector of weights to be used in the fitting process. Should be NULL

or a numeric vector. If not null, the total likelihood is the weighted sum of

individual likelihood.

na.action a missing-data filter function, applied to the model.frame. If NULL, default is

options()\$na.action.

datacontrol a data.frame in which to interpret the variables named in the formula for the

control group.

Idcontrol, ratecontrol, logit\_startcontrol, logit\_endcontrol, weightscontrol

Id, rate, logit of the cumulative hazard at the start and the end of the intervalle

in the life table, and weights for the control group

logit\_start\_byperiodcontrol, logit\_end\_byperiodcontrol, weights\_byperiodcontrol, Id\_byperiodcontrol

A REMPLIR

int\_meth character string specifying the the numerical integration method. Possible val-

ues are "GL" for Gauss-Legendre method, "CAV\_SIM" for Cavalieri-Simpson's rule, "SIM\_3\_8" for the Simpson's 3/8 rule, "BOOLE" for the Boole's rule, or

"BANDS" for the midpoint rule with specified bands.

bands bands used to split data in the numerical integration when int\_meth="BANDS").

npoints number of points used in the numerical integration when int\_meth="GL").

stept scalar value of the time-step in numerical integration. It is required only when

int\_meth="CAV\_SIM" or "SIM\_3\_8" or "BOOLE". If no value is supplied, Max\_T/500

is used.

init starting values of the parameters.

initbyglm a logical value indicating indicating how are found or refined init values. If

TRUE, the fitting method described in Remontet et al.(2007) is used to find or refine starting values. This may speedup the fit. If FALSE, the maximisation of the likelihood starts at values given in init. If init=NULL, the starting values correspond to a constant net hazard equal to the ratio of the number of event

over the total number of person-time.

initbands bands used to split data when initbyglm=TRUE.

optim.control a list of control parameters passed to the optim() function. optim\_meth method to be used to optimize the likelihood. See optim.

Coptim. control a list of control parameters passed to the constrOptim() function See constrOptim.

lower, upper Bounds on the variables for the "L-BFGS-B" method, or bounds in which to

search for method "Brent". See optim.

control.glm a list of control parameters passed to the glm() function when method="glm".

vartype character string specifying the type of variance matrix computed by flexrsurv:

the inverse of the hessian matrix computed at the MLE estimate (ie. the inverse of the observed information matrix) if vartype="oim", the inverse of the outer product of the gradients if vartype="opg". The variance is not computed when

vartype="none".

varmethod character string specifying the method to compute the hessian matrix when

vartype="oim". If varmethod="oim", the hessian matrixe is computed by optim. If varmethod="numDeriv.hessian", the hessian matrix is computed by

numDeriv: hessian with method="Richardson". If varmethod="numDeriv.jacobian", the hessian matrixe is computed by numDeriv: jacobian with method="Richardson".

numDeriv.method.args

arguments passed to numDeriv: hessian or numDeriv: jacobian when varmethod="numDeriv.hessian" or varmethod="numDeriv.jacobian". Arguments not specified remain with

their default values as specified in details. See numDeriv: grad for details about

these parameters.

debug control the volum of intermediate output

#### **Details**

A full description of the additive and the multiplicative both non-linear and non-proportional models is given respectively in Remontet (2007) and Mahboubi (2011).

flexrsurv. 11 is the workhorse function: it is not normally called directly.

#### Value

flexrsurv returns an object of class "flexrsurv". An object of class "flexrsurv" is a list containing at least the following components:

coefficients a named vector of coefficients

loglik the log-likelihood

var estimated covariance matrix for the estimated coefficients

informationMatrix

estimated information matrix

bhlink the linkk of baseline hazard: if "identity" baseline = sum g0\_i b\_i(t); if "log"

 $log(baseline) = sum g0_i b_i(t);$ 

init vector of the starting values supplied

converged logical, Was the optimlizer algorithm judged to have converged?

linear.predictors

the linear fit on link scale (not including the baseline hazard term if bhlink =

"identity")

fitted.values the estimated value of the hazard rate at each event time, obtained by transform-

ing the linear predictors by the inverse of the link function

cumulative.hazard

the estimated value of the cumulative hazard in the time interval

call the matched call
formula the formula supplied
terms the terms object used
data the data argument
rate the rate vector used

```
time the time vector used

workingformula the formula used by the fitter

optim.control the value of the optim.control argument supplied

control.glm the value of the control.glm argument supplied

method the name of the fitter function used
```

#### References

Mahboubi, A., M. Abrahamowicz, et al. (2011). "Flexible modeling of the effects of continuous prognostic factors in relative survival." Stat Med 30(12): 1351-1365. doi:10.1002/sim.4208

Remontet, L., N. Bossard, et al. (2007). "An overall strategy based on regression models to estimate relative survival and model the effects of prognostic factors in cancer survival studies." Stat Med 26(10): 2214-2228. doi:10.1002/sim.2656

#### See Also

```
print.flexrsurv, summary.flexrsurv, logLik.flexrsurv, predict.flexrsurv, NPH, NLL, and NPHNLL.
```

#### **Examples**

```
if (requireNamespace("relsurv", quietly = TRUE) & requireNamespace("date", quietly = TRUE)) {
library(date)
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
# get the death rate at event (or end of followup) from slopop for rdata
rdata$iage <- findInterval(rdata$age*365.24+rdata$time, attr(slopop, "cutpoints")[[1]])
rdata$iyear <- findInterval(rdata$year+rdata$time, attr(slopop, "cutpoints")[[2]])
therate <- rep(-1, dim(rdata)[1])
for( i in 1:dim(rdata)[1]){
  therate[i] <- slopop[rdata$iage[i], rdata$iyear[i], rdata$sex[i]]</pre>
rdata$slorate <- therate
# get the logit_start and logit_end
# logit start at age 18
tmpsurv <- Surv(rep(0, length(rdata$time)), rdata$time, rdata$cens)</pre>
HH <- getHazardFromTable(tmpsurv, startdate=rdata$year,</pre>
```

```
startage=rdata$age*365.25 , matchdata=rdata, ratetable=slopop,
       age="age", year="year",
       rmap=list(sex=sex),
       agemin=18,
     ratename = "poprate", cumrateendname ="cumrateend", cumrateentername ="cumrateenter"
rdata$slorate <- HH$poprate
rdata$logit_start <- log(exp(HH$cumrateenter)-1)</pre>
rdata$logit_end <- log(exp(HH$cumrateend)-1)</pre>
rdata$Id <- 1:dim(rdata)[1]</pre>
# change sex coding
rdata$sex01 <- rdata$sex -1
# fit a relative survival model with a non linear effect of age
# without correction of life table
# partial likelihood
fit00 <- flexrsurvclt(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
                      rate=slorate,
      data=rdata,
      knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Max_T=5400,
                 Spline = "b-spline",
                 initbyglm=TRUE,
                 initbands=seq(0, 5400, 100),
                 int_meth= "BANDS",
                 bands=seq(0, 5400, 50)
summary(fit00)
# fit a relative survival model with a non linear effect of age
# without correction of life table
   full likelihood
fit0 <- flexrsurvclt(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
                                            rate=slorate,
           logit_start=logit_start,
                    logit_end=logit_end,
data=rdata,
Id=Id,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Max_T=5400,
                 Spline = "b-spline",
                 initbyglm=TRUE,
                 initbands=seq(0, 5400, 100),
```

```
int_meth= "BANDS",
                 bands=seq(0, 5400, 50)
                 )
summary(fit0)
# fit a relative survival model with a non linear effect of age
# with correction of life table
  full likelihood
fit1 <- flexrsurvclt(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
                 rate=slorate,
                     logit_start=logit_start,
                    logit_end=logit_end,
data=rdata,
Id=Id,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Max_T=5400,
                 Spline = "b-spline",
             Spline.CLT=flexrsurv:::R2bBSplineBasis(knots=c(-2.5,0,2.5), degree=3),
                 initbyglm=TRUE,
                 initbands=seq(0, 5400, 100),
                 int_meth= "BANDS",
                 bands=seq(0, 5400, 50)
summary(fit1)
print(coef(fit1))
# fit a relative survival model with a non linear effect of age
# with correction of life table, strabified by sex
    full likelihood
fit2 <- flexrsurvclt(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
    formula.table= ~sex,
                 rate=slorate,
                     logit_start=logit_start,
                    logit_end=logit_end,
data=rdata,
Id=Id,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Max_T=5400,
                 Spline = "b-spline",
             Spline.CLT=flexrsurv:::R2bBSplineBasis(knots=c(-2.5,0,2.5), degree=3),
                 initbyglm=TRUE,
                 initbands=seq(0, 5400, 100),
                 int_meth= "BANDS",
                 bands=seq(0, 5400, 50)
summary(fit2)
AIC(fit0, fit1, fit2)
```

}

```
getBrassHazardFromTable
```

Compute expected hazards with respect to a corrected reference life table

# Description

returns the cumulative hazard and the hazard rate of subjects in a reference life table

#### Usage

# Arguments

Υ	An object with interval data. It can be an object of class Surv with arguments time, time2 and event or a two-column matrix with starting time in the first column and ending time in the second column.
startdate	a numeric vector such that as.Date(startadate) is interpreted as the date of the start (when $Y[,]==0$ ).
startage	a numeric vector of age in days the start (when Y[,]==0).
matchdata	an optional data.frame in which to interpret the additional variables to be mapped to the ratetable variables.
ratetable	an object of class ratetable, ie a table of event rates.
age, year	character values of the names of the age and period variables in the rate table.
rmap	an optional list that maps data set names to the ratetable names. See survexp an example bellow.
agemin	numeric value of the age at which the cumulative hazard starts.
scale	numeric value to scale agemin.
ratename, cumra	teendname, cumrateentername, idname
	names of the returned variables

```
origin, format passed to as.Date

left.open logical, passed to findInterval

SplineBrass Spline basis used to transform the rates

verbose logical, if true the progression of the computation is output.
```

#### **Details**

The cumulative rates are computed using survexp.

#### Value

A data. frame with 3 columns with the rate at the ending time, the cumulative rate from agemin up to the starting time and upt to the ending time.

#### See Also

getHazardFromTable for the cumulative hazard and the hazard rate of subjects in a reference life table. survexp

#### **Examples**

```
if (requireNamespace("relsurv", quietly = TRUE) & requireNamespace("date", quietly = TRUE)) {
library(date)
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
tmpsurv <- Surv(rep(0, length(rdata$time)), rdata$time, rdata$cens)</pre>
HH <- getPseudoHazardFromTable(tmpsurv, startdate=rdata$year,</pre>
               startage=rdata$age*365.24 , matchdata=rdata, ratetable=slopop,
               age="age", year="year",
               rmap=list(sex=sex),
               agemin=18, scale=365.24,
               ratename = "poprate",
               cumrateendname ="cumrateend",
               cumrateentername ="cumrateenter",
               idname="Id_byperiod"
summary(HH)
```

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getHazardFromTable	computes expected hazards with respect to a reference life table
--------------------	--

# Description

returns the cumulative hazard and the hazard rate of subjects in a reference life table

## Usage

#### **Arguments**

Υ	An object with interval data. It can be an object of class Surv with arguments time, time2 and event or a two-column matrix with starting time in the first column and ending time in the second column.
startdate	a numeric vector such that as.Date(startadate) is interpreted as the date of the start (when $Y[,]==0$ ).
startage	a numeric vector of age in days the start (when Y[,]==0).
matchdata	an optional data.frame in which to interpret the additional variables to be mapped to the ratetable variables.
ratetable	an object of class ratetable, ie a table of event rates.
age, year	character values of the names of the age and period variables in the rate table.
rmap	an optional list that maps data set names to the ratetable names. See survexp an example bellow.
agemin	numeric value of the age at which the cumulative hazard starts.
scale	numeric value to scale agemin.
ratename, cumrateendname, cumrateentername	
	names of the returned variables
origin, format	arguments passed as.Date
left.open	logical, passed to findInterval
verbose	logical, if true the progression of the computation is output.

## **Details**

The cumulative rates are computed using survexp.

#### Value

A data. frame with 3 columns with the rate at the ending time, the cumulative rate from agemin up to the starting time and upt to the ending time.

#### See Also

getPseudoHazardFromTable for the cumulative hazard in each period of a reference life table. getBrassHazardFromTable for the cumulative hazard in a corrected reference life table. survexp

## **Examples**

```
if (requireNamespace("relsurv", quietly = TRUE) & requireNamespace("date", quietly = TRUE)) {
library(date)
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
tmpsurv <- Surv(rep(0, length(rdata$time)), rdata$time, rdata$cens)</pre>
HH <- getHazardFromTable(tmpsurv, startdate=rdata$year,</pre>
               startage=rdata$age*365.24 , matchdata=rdata, ratetable=slopop,
               age="age", year="year",
               rmap=list(sex=sex),
               agemin=18, scale=365.24,
               ratename = "poprate",
               cumrateendname ="cumrateend",
               cumrateentername ="cumrateenter"
summary(HH)
```

getPseudoHazardFromTable

Computes expected hazards with respect to a reference life table

## **Description**

return the cumulative pseudo hazard and the hazard rate of subjects in a reference life table

#### Usage

## **Arguments**

Y	An object with interval data. It can be an object of class Surv with arguments time, time2 and event or a two-column matrix with starting time in the first column and ending time in the second column.
startdate	a numeric vector such that as.Date(startadate) is interpreted as the date of the start (when $Y[,]==0$ ).
startage	a numeric vector of age in days the start (when $Y[,]==0$ ).
matchdata	an optional data.frame in which to interpret the additional variables to be mapped to the ratetable variables.
ratetable	an object of class ratetable, ie a table of event rates.
age, year	character values of the names of the age and period variables in the rate table.
rmap	an optional list that maps data set names to the ratetable names. See survexp an example bellow.
agemin	numeric value of the age at which the cumulative hazard starts.
scale	numeric value to scale agemin.
ratename, cumra	teendname, cumrateentername, idname
	names of the returned variables
origin, format	passed to as.Date
left.open	logical, passed to findInterval
verbose	logical, if true the progression of the computation is output.

## **Details**

The cumulative rates are computed using survexp.

## Value

A data. frame with 3 columns with the rate at the ending time, the cumulative rate from agemin up to the starting time and upt to the ending time.

#### See Also

getHazardFromTable for the cumulative hazard and the hazard rate of subjects in a reference life table. survexp

22 logLik.flexrsurv

#### **Examples**

```
if (requireNamespace("relsurv", quietly = TRUE) & requireNamespace("date", quietly = TRUE)) {
library(date)
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
tmpsurv <- Surv(rep(0, length(rdata$time)), rdata$time, rdata$cens)</pre>
HH <- getPseudoHazardFromTable(tmpsurv, startdate=rdata$year,</pre>
               startage=rdata$age*365.24 , matchdata=rdata, ratetable=slopop,
               age="age", year="year",
               rmap=list(sex=sex),
               agemin=18, scale=365.24,
               ratename = "poprate",
               cumrateendname ="cumrateend",
               cumrateentername ="cumrateenter",
               idname="Id_byperiod"
               )
summary(HH)
}
```

logLik.flexrsurv

Log-Likelihood and the number of observations for a flexrsuv fit.

## **Description**

Function to extract Log-Likelihood and the number of observations from a flexrsuv or flexrsuvclt fit.

#### Usage

```
## S3 method for class 'flexrsurv'
logLik(object, ...)
## S3 method for class 'flexrsurv'
nobs(object, ...)
```

#### **Arguments**

```
object any object of class flexrsuv results of a flexrsurv fit.
... not used
```

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# Value

logLik returns a standard logLik object (see logLik) nobs returns a single number, normally an integer.

# See Also

logLik, nobs.

 $\mathsf{NLL}$ 

Non Log-Linear effect

# Description

Generate the spline basis matrix for non log-linear effect.

# Usage

```
NLL(x,
    Spline = c("b-spline", "tp-spline", "tpi-spline"),
    Knots = NULL,
    Degree = 3,
    Intercept = FALSE,
    Boundary.knots = range(x),
    Keep.duplicates = TRUE,
    outer.ok = TRUE,
    ...)
```

## **Arguments**

x	the predictor variable.
Spline	a character string specifying the type of spline basis. "b-spline" for B-spline basis, "tp-spline" for truncated power basis and "tpi-spline" for monotone (increasing) truncated power basis.
Knots	the internal breakpoints that define the spline used to estimate the NLL effect. By default there are none.
Degree	degree of splines which are considered.
Intercept	a logical value indicating whether intercept/first basis of spline should be considered.
Boundary.knots	range of variable which is analysed.
Keep.duplicates	
	Should duplicate interior knots be kept or removed. Defaults is FALSE, which removes duplicate knots with a warning if duplicate interior knots are found.
outer.ok	logical indicating how are managed $x$ values outside the knots. If FALSE, return NA, if TRUE, return 0 for the corresponding $x$ values.
	not used

24 NPH

#### **Details**

NLL is based on package orthogonalsplinebasis

#### See Also

NPH and NPHNLL.

NPH

Non Proportional Hazard effect

# **Description**

Generate the design matrix of spline basis for non proportional effect.

#### Usage

```
NPH(x,
    timevar,
    Spline = c("b-spline", "tp-spline", "tpi-spline"),
    Knots.t = NULL,
    Degree.t = 3,
    Intercept.t = TRUE,
    Boundary.knots.t = c(0, max(timevar)),
    Keep.duplicates.t = TRUE,
    outer.ok = TRUE,
    ...)
```

## **Arguments**

x the predictor variable.

timevar the time variable.

Spline a character string specifying the type of spline basis. "b-spline" for B-spline

basis, "tp-spline" for truncated power basis and "tpi-spline" for monotone (in-

creasing) truncated power basis.

Knots.t the internal breakpoints that define the spline used to estimate the NPH effect.

By default there are none.

Degree.t degree of splines which are considered.

Intercept.t a logical value indicating whether intercept/first basis of spline should be con-

sidered.

Boundary.knots.t

range of time period which is analysed. By default it is c(0, max(timevar)).

Keep.duplicates.t

Should duplicate interior knots be kept or removed. Defaults is FALSE, which removes duplicate knots with a warning if duplicate interior knots are found.

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```
outer.ok logical indicating how are managed timevar values outside the knots. If FALSE, return NA, if TRUE, return 0 for the corresponding timevar values.
... not used
```

#### **Details**

NPH is based on package orthogonalsplinebasis

#### See Also

NLL, and NPHNLL.

**NPHNLL** 

Non Proportional Hazard and Non Log-Linear effect

## **Description**

Generate the design matrix of spline basis for both non log-linear and non proportional effect.

## Usage

```
NPHNLL(x,
       timevar,
       model = c("additive", "multiplicative"),
       Spline = c("b-spline", "tp-spline", "tpi-spline"),
       Knots = NULL,
       Degree = 3,
       Intercept = FALSE,
       Boundary.knots = range(x),
       Knots.t = NULL,
       Degree.t = 3,
       Intercept.t = (model == "multiplicative"),
       Boundary.knots.t = c(0, max(timevar)),
       outer.ok = TRUE,
       Keep.duplicates = TRUE,
       xdimnames = ":XxXxXXxXxX ",
       tdimnames = ":TtTtTTtT")
```

#### Arguments

the predictor variable.

timevar the time variable.

model character string specifying the type of model for both non-proportionnal and non

linear effects. The model method=="additive" assumes effects as explained in Remontet et al.(2007), the model method=="multiplicative" assumes effects

as explained in Mahboubi et al. (2011).

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Spline a character string specifying the type of spline basis. "b-spline" for B-spline

basis, "tp-spline" for truncated power basis and "tpi-spline" for monotone (in-

creasing) truncated power basis.

Knots the internal breakpoints that define the spline used to estimate the NLL part of

effect. By default there are none.

Degree degree of splines of variable which are considered.

Intercept a logical value indicating whether intercept/first basis of spline should be con-

sidered.

Boundary.knots range of variable which is analysed.

Knots.t the internal breakpoints that define the spline used to estimate the NPH part of

effect. By default there are none.

Degree.t degree of splines of time variable which are considered.

Intercept.t a logical value indicating whether intercept/first basis of spline should be con-

sidered.

Boundary.knots.t

range of time period which is analysed.

Keep.duplicates

Should duplicate interior knots be kept or removed. Defaults is FALSE, which removes duplicate knots with a warning if duplicate interior knots are found.

outer.ok logical indicating how are managed timevar or x values outside the knots. If

FALSE, return NA, if TRUE, return 0 for the corresponding timevar or x values.

xdimnames string to build dimnames of x bases

tdimnames string to build dimnames of timevar bases

#### **Details**

NPHNLL is based on package orthogonalsplinebasis

#### References

Mahboubi, A., M. Abrahamowicz, et al. (2011). "Flexible modeling of the effects of continuous prognostic factors in relative survival." Stat Med 30(12): 1351-1365. doi:10.1002/sim.4208

Remontet, L., N. Bossard, et al. (2007). "An overall strategy based on regression models to estimate relative survival and model the effects of prognostic factors in cancer survival studies." Stat Med 26(10): 2214-2228. doi:10.1002/sim.2656

#### See Also

NPH and NLL.

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predict.flexrsurv

Predictions for a relative survival model

#### Description

Predict linear predictors, hazard and cumulative hazard for a model fitted by flexrsuv

## Usage

#### **Arguments**

object	the results of a flexrsurv fit.
newdata	Optional new data at which to do predictions. If absent predictions are for the data frame used in the original fit.
type	the type of predicted value. Choices are the linear predictor ("lp", "log", "loghazard", "lograte"), the hazard ("rate", "hazard", "hazardrate", "risk") or the cumulative hazard ("cum", "cumulative.hazard", "cumulative").
se.fit	if TRUE, pointwise standard errors are produced for the predictions (not available for cumulative hazard).
ci.fit	if TRUE, confidence intervale are produced for the predictions.
level	Confidence level.
na.action	function determining what should be done with missing values in newdata. The default is to predict NA.
	For future methods

## **Details**

For cumulative hazard, the cumulative hazard is computed from 0 until the given end time. The cumulative hazard is computed using the same numerical integration method as the one used to fit the model.

#### Value

a vector or a list containing the predictions (element "fit") and their standard errors (element "se.fit") if the se.fit option is TRUE.

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#### Note

To work correctly, arguments Boundary.knots and Boundary.knots.t must be included in the call to NPH(), NLL() and NPHNLL() in the formula of flexrsurv

#### See Also

```
predict, flexrsurv, flexrsurvclt
```

## **Examples**

```
if (requireNamespace("relsurv", quietly = TRUE)) {
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
# get the death rate at event (or end of followup) from slopop for rdata
rdata$iage <- findInterval(rdata$age*365.24+rdata$time, attr(slopop, "cutpoints")[[1]])
rdata$iyear <- findInterval(rdata$year+rdata$time, attr(slopop, "cutpoints")[[2]])
therate <- rep(-1, dim(rdata)[1])</pre>
for( i in 1:dim(rdata)[1]){
 therate[i] <- slopop[rdata$iage[i], rdata$iyear[i], rdata$sex[i]]</pre>
}
rdata$slorate <- therate
# change sex coding
rdata$sex01 <- rdata$sex -1
# centering age
rdata$agec <- rdata$age- 60
# fit a relative survival model with a non linear effect of age
fit <- flexrsurv(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
                 rate=slorate, data=rdata,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Spline = "b-spline",
                 initbyglm=TRUE,
                 int_meth= "BOOLE",
                 step=50
summary(fit, correlation=TRUE)
```

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```
newrdata <- rdata
newrdata$age <- rep(60, length(rdata$age))</pre>
newrdata$sex <- factor(newrdata$sex, labels=c("m", "f"))</pre>
linpred <- predict(fit, newdata=newrdata, type="lp", ci.fit=TRUE)</pre>
predhazard <- predict(fit, newdata=newrdata, type="hazard" , ci.fit=TRUE)</pre>
predcumhazard <- predict(fit, newdata=newrdata, type="cum", ci.fit=TRUE)</pre>
require(ggplot2)
tmp <- cbind(newrdata, linpred)</pre>
glp <- ggplot(tmp, aes(time, colour=sex))</pre>
glp + geom_ribbon(aes(ymin = lwr, ymax = upr, fill=sex)) +
   geom_line(aes(y=fit)) +
   scale_fill_manual(values = alpha(c("blue", "red"), .3))
tmp <- cbind(newrdata, predhazard)</pre>
glp <- ggplot(tmp, aes(time, colour=sex))</pre>
glp + geom_ribbon(aes(ymin = lwr, ymax = upr, fill=sex)) +
   geom_line(aes(y=fit)) +
   scale_fill_manual(values = alpha(c("blue", "red"), .3))
tmp <- cbind(newrdata, predcumhazard)</pre>
glp <- ggplot(tmp, aes(time, colour=sex))</pre>
glp + geom_ribbon(aes(ymin = lwr, ymax = upr, fill=sex)) +
   geom_line(aes(y=fit)) +
   scale_fill_manual(values = alpha(c("blue", "red"), .3))
}
```

predictCLT

Predictions for relational life table model

## Description

Predict the relational model for a life table correction model fitted by flexrsuvclt or for specified knots, degree and coefficients

#### Usage

```
predictCLT (...)

## S3 method for class 'flexrsurvclt'
predictCLT(object, newdata= NULL,
   type = c("clt", "correction"),
   se.fit=FALSE, na.action=na.pass, newcoef = NULL, ...)

## Default S3 method:
predictCLT(knots, degree, newdata, newcoef, ...)
```

30 predictCLT

#### Arguments

object the results of a flexrsurvelt fit. newdata Optional new vector of logarithm of the cumulative distribution odds (LCDO) at which to do predictions. If absent predictions are for values of the LCDO used in the original fit (logit\_end parameter in the call to flexrsuvclt)). newcoef Optional new coefficients for which to do predictions. If absent predictions are for the coefficients of the fitted model in object. the type of predicted value. Choices are "clt" or "correction" to compute the type corrected logarithm of the cumulative distribution odds. se.fit if TRUE, pointwise standard errors are produced for the predictions (not yet implemented). knots and degree of the relational model. knots, degree na.action function determining what should be done with missing values in newdata. The default is to predict NA. For future methods . . .

#### **Details**

predictCLT with knots and degree arguments computes corrected values of .

#### Value

a vector or a list containing the predicted relational model (element "fit") and their standard errors (element "se.fit") if the se.fit option is TRUE.

#### See Also

```
predict.flexrsurvclt, flexrsurv, flexrsurvclt
```

# Examples

```
if (requireNamespace("relsurv", quietly = TRUE) & requireNamespace("date", quietly = TRUE)) {
library(date)
# data from package relsurv
data(rdata, package="relsurv")

class(rdata$year)<-"integer"

# rate table from package relsurv
data(slopop, package="relsurv")

# get the death rate at event (or end of followup) from slopop for rdata
rdata$iage <- findInterval(rdata$age*365.24+rdata$time, attr(slopop, "cutpoints")[[1]])</pre>
```

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```
rdata$iyear <- findInterval(rdata$year+rdata$time, attr(slopop, "cutpoints")[[2]])
therate <- rep(-1, dim(rdata)[1])</pre>
for( i in 1:dim(rdata)[1]){
 therate[i] <- slopop[rdata$iage[i], rdata$iyear[i], rdata$sex[i]]</pre>
}
rdata$slorate <- therate
# get the logit_start and logit_end
# logit start at age 18
tmpsurv <- Surv(rep(0, length(rdata$time)), rdata$time, rdata$cens)</pre>
HH <- getHazardFromTable(tmpsurv, startdate=rdata$year,</pre>
       startage=rdata$age*365.25 , matchdata=rdata, ratetable=slopop,
       age="age", year="year",
       rmap=list(sex=sex),
       agemin=18,
     ratename = "poprate", cumrateendname ="cumrateend", cumrateenter"
rdata$slorate <- HH$poprate
rdata$logit_start <- log(exp(HH$cumrateenter)-1)</pre>
rdata$logit_end <- log(exp(HH$cumrateend)-1)</pre>
rdata$Id <- 1:dim(rdata)[1]</pre>
# change sex coding
rdata$sex01 <- rdata$sex -1
# fit a relative survival model with a non linear effect of age
# with correction of life table
# full likelihood
fit1 <- flexrsurvclt(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3,</pre>
                                            Boundary.knots = c(24, 95)),
                 rate=slorate,
                     logit_start=logit_start,
                    logit_end=logit_end,
data=rdata,
Id=Id,
                 knots.Bh=1850, # one interior knot at 5 years
                 degree.Bh=3,
                 Max_T=5400,
                 Spline = "b-spline",
             Spline.CLT=flexrsurv:::R2bBSplineBasis(knots=c(-2.5,0,2.5), degree=3),
                 initbyglm=TRUE,
                 initbands=seq(0, 5400, 100),
                 int_meth= "BANDS",
                 bands=seq(0, 5400, 50)
```

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```
corrected_logit_end <- predictCLT(fit1)

try_logit_end <- predictCLT(knots=c(-2.5,0,2.5), degree=3, newcoef = c(0.5, 2),
newdata = rdata$logit_end )

plot(rdata$logit_end, corrected_logit_end)
points(rdata$logit_end, try_logit_end, col = 2)
}</pre>
```

predictSpline

Generic method for prediction of spline function

## **Description**

Predict a spline function by specifying its type, knots, degree and coefficients

## Usage

```
predictSpline (object, x, ...)

## Default S3 method:
predictSpline(object=c("b-spline", "tp-spline"),
x, knots, degree, keep.duplicates = FALSE, coef=1, ...)
```

## **Arguments**

object the type of spline to be predicted ("b-spline", the default, or "tp-spline")

x Vector of values at wich to predict the spline function.

knots, degree knots and degree of the relational model.

keep.duplicates

Should duplicate interior knots be kept or removed. Defaults is FALSE, which removes duplicate knots with a warning if duplicate interior knots are found.

coef vector of coefficient of the spline function.

... not used

#### **Details**

```
predictSpline.
```

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## Value

A vector the evaluated spline function with same length as x.

#### See Also

```
predict.flexrsurvclt, flexrsurv, flexrsurvclt
```

## **Examples**

```
predspline <- predictSpline("b-spline",
x= seq(from=-3, to = 3, by=.1),
coef = .5 * 1:5,
knots=c(-3,0,3), degree=3)
plot(seq(from=-3, to = 3, by=.1), predspline)</pre>
```

print.flexrsurv

Print a Short Summary of a Relative Survival Model

# Description

Print number of observations, number of events, the formula, the estimated coeficients and the log likelihood.

#### Usage

```
## S3 method for class 'flexrsurv'
print(x,
          digits = max(3, getOption("digits") - 3), ...)
```

## **Arguments**

```
    the result of a call to the flexrsuv function.
    the minimum number of significant digits to be printed in values, see print. default.
    other options
```

#### See Also

The default method print.default, and help for the function flexrsurv, flexrsurvclt.

34 summary.flexrsurv

summary.flexrsurv Summarizing Flexible Relative Survival Model Fits	
---	--

## **Description**

summary methods for class flexrsurv. Produces and prints summaries of the results of a fitted Relative Survival Model

#### Usage

#### **Arguments**

object	an object of class "flexrsurv", usually, a result of a call to flexrsurv.
x	$an \ object \ of \ class \ "summary.flexrsurv", usually, a \ result \ of \ a \ call \ to \ summary.flexrsurv.$
correlation	logical; if TRUE, the correlation matrix of the estimated parameters is returned and printed.
symbolic.cor	logical. If TRUE, print the correlations in a symbolic form (see symnum) rather than as numbers.
digits	the number of significant digits to use when printing.
signif.stars	logical. If TRUE, 'significance stars' are printed for each coefficient.
• • •	further arguments passed to or from other methods.

## **Details**

print.summary.glm tries to be smart about formatting the coefficients, standard errors, etc. and additionally gives 'significance stars' if signif.stars is TRUE.

Correlations are printed to two decimal places (or symbolically): to see the actual correlations print summary(object)\$correlation directly.

The dispersion of a GLM is not used in the fitting process, but it is needed to find standard errors. If dispersion is not supplied or NULL, the dispersion is taken as 1 for the binomial and Poisson families, and otherwise estimated by the residual Chisquared statistic (calculated from cases with non-zero weights) divided by the residual degrees of freedom.

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#### Value

The function summary.flexrsurv computes and returns a list of summary statistics of the fitted flexible relative survival model given in object. The returned value is an object of class "summary.flexrsurv", which a list with components:

call the "call" component from object. the "terms" component from object. terms the matrix of coefficients, standard errors, z-values and p-values. coefficients the estimated covariance matrix of the estimated coefficients. cov correlation (only if correlation is true.) the estimated correlations of the estimated coefficients. symbolic.cor (only if correlation is true.) the value of the argument symbolic.cor. loglik the "loglik" component from object. df.residual the "df.residual" component from object.

#### See Also

```
summary, flexrsurv, flexrsurvclt.
```

#### **Examples**

```
if (requireNamespace("relsurv", quietly = TRUE)) {
# data from package relsurv
data(rdata, package="relsurv")
# rate table from package relsurv
data(slopop, package="relsurv")
# get the death rate at event (or end of followup) from slopop for rdata
rdata$iage <- findInterval(rdata$age*365.24+rdata$time, attr(slopop, "cutpoints")[[1]])
rdata$iyear <- findInterval(rdata$year+rdata$time, attr(slopop, "cutpoints")[[2]])
therate <- rep(-1, dim(rdata)[1])</pre>
for( i in 1:dim(rdata)[1]){
 therate[i] <- slopop[rdata$iage[i], rdata$iyear[i], rdata$sex[i]]</pre>
rdata$slorate <- therate
# change sex coding
rdata$sex01 <- rdata$sex -1
# fit a relative survival model with a non linear effetc of age
fit <- flexrsurv(Surv(time,cens)~sex01+NLL(age, Knots=60, Degree=3),</pre>
                 rate=slorate, data=rdata,
                 knots.Bh=1850, # one interior knot at 5 years
```

36 WCEI

WCEI

Weighted cumulative exposure index

## **Description**

Generate the spline basis matrix for Weighted cumulative exposure index.

## Usage

```
WCEI(x,
    timevar,
    fromT=0,
    Spline.WCEI=NULL,
    Spline = c("m-spline", "b-spline", "tp-spline", "tpi-spline"),
    Knots.t = NULL,
    Degree.t = 3,
    Intercept.t = TRUE,
    Boundary.knots.t = range(c(timevar, fromT)),
    Keep.duplicates.t = TRUE,
    outer.ok = TRUE,
    ...)
```

## **Arguments**

timevar the time variable.

fromT Time at which starts exposure

Spline.WCEI a S4 object with method deriv(), evaluate() and predict().

Spline a character string specifying the type of spline basis. "b-spline" for B-spline basis, "tp-spline" for truncated power basis and "tpi-spline" for monotone (increasing) truncated power basis.

Knots.t the internal breakpoints that define the spline used to estimate the WCEI effect.

By default there are none.

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Degree.t degree of splines which are considered.

Intercept.t a logical value indicating whether intercept/first basis of spline should be con-

sidered.

Boundary.knots.t

range of variable which is analysed.

Keep.duplicates.t

Should duplicate interior knots be kept or removed. Defaults is FALSE, which removes duplicate knots with a warning if duplicate interior knots are found.

outer.ok logical indicating how are managed x values outside the knots. If FALSE, return

NA, if TRUE, return 0 for the corresponding x values.

... not used

#### **Details**

WCEI is based on package orthogonalsplinebasis

#### See Also

NLL NPH and NPHNLL.

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