# Package 'survregVB'

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Version 0.0.1
<b>Description</b> Implements Bayesian inference in accelerated failure time (AFT) models for right-censored survival times assuming a log-logistic distribution. Details of the variational Bayes algorithms, with and without shared frailty, are described in Xian et al. (2024) <doi:10.1007 s11222-023-10365-6=""> and Xian et al. (2024) <doi:10.48550 arxiv.2408.00177="">, respectively.</doi:10.48550></doi:10.1007>
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## Description

Calculates parameter  $\alpha^*$  of  $q^*(b)$  to optimize the evidence based lower bound (ELBO) in survregVB. fit and survregVB. frailty. fit.

#### Usage

```
alpha_star(alpha_0, delta)
```

## Arguments

alpha\_0 The shape hyperparameter  $\alpha_0$  of the prior distribution of the scale parameter, b. delta A binary vector indicating right censoring.

#### Value

```
Parameter \alpha^* of q^*(b).
```

```
survregVB.fit
survregVB.frailty.fit
```

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dnase

Subset of rhDNase from the survival package

#### **Description**

The dnase dataset is a subset of the rhDNase dataset from the survival package. It is included in this package under the LGPL ( $\geq 2$ ) license.

#### Usage

dnase

#### **Format**

A data frame with 767 observations on the following variables:

```
trt treatment arm: 0=placebo, 1= rhDNase
```

fev forced expriatory volume at enrollment, a measure of lung capacity

infect an infection that required the use of intravenous antibiotics

**time** difference between the date of entry into the study and the date of last follow-up capped at 169 days

#### **Source**

```
survival package. https://cran.r-project.org/package=survival
```

elbo

Calculates the variational Bayes convergence criteria, evidence lower bound (ELBO), optimized in survregVB.fit.

#### Description

Calculates the variational Bayes convergence criteria, evidence lower bound (ELBO), optimized in survregVB.fit.

#### Usage

```
elbo(
y,
X,
delta,
alpha_0,
omega_0,
mu_0,
v_0,
```

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```
alpha,
omega,
mu,
Sigma,
expectation_b
```

## Arguments

У	A vector of observed log-transformed survival times.
X	A design matrix including covariates with first column of ones to represent the intercept.
delta	A binary vector indicating right censoring.
alpha_0	The shape hyperparameter $\alpha_0$ of the prior distribution of the scale parameter, $b$ .
omega_0	The shape hyperparameter $\omega_0$ of the prior distribution of the scale parameter, $b$ .
mu_0	Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
alpha	The shape parameter $\alpha^*$ of $q^*(b)$ .
omega	The scale parameter $\omega^*$ of $q^*(b)$ .
mu	Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.
Sigma	Parameter $\Sigma^*$ of $q^*(\beta)$ , a covariance matrix.
expectation_b	The expected value of $b$ .

## See Also

```
survregVB.fit
```

elbo_cluster	Calculates the variational Bayes convergence criteria, evidence lower
	bound (ELBO), optimized in survregVB.frailty.fit.

## Description

 $Calculates \ the \ variational \ Bayes \ convergence \ criteria, \ evidence \ lower \ bound \ (ELBO), \ optimized \ in \ survregVB. \ frailty. \ fit.$ 

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## Usage

```
elbo_cluster(
 у,
Х,
 delta,
  alpha_0,
 omega_0,
 mu_0,
 v_0,
 lambda_0,
  eta_0,
  alpha,
 omega,
 mu,
  Sigma,
  tau,
  sigma,
  lambda,
  eta,
 expectation_b,
  cluster
)
```

## Arguments

lambda

A vector of observed log-transformed survival times.
A design matrix including covariates with first column of ones to represent the intercept.
A binary vector indicating right censoring.
The shape hyperparameter $\alpha_0$ of the prior distribution of the scale parameter, $b$ .
The shape hyperparameter $\omega_0$ of the prior distribution of the scale parameter, $b$ .
Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
The shape hyperparameter $\lambda_0$ of the prior distribution of the frailty variance, $\sigma_{\gamma}^2$ .
The scale hyperparameter $\eta_0$ of the prior distribution of the frailty variance, $\sigma_{\gamma}^2$ .
The shape parameter $\alpha^*$ of $q^*(b)$ .
The scale parameter $\omega^*$ of $q^*(b)$ .
Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.
Parameter $\Sigma^*$ of $q^*(\beta)$ , a covariance matrix.
Parameter $\tau^*$ of $q^*(\gamma_i)$ , a vector of means.
Parameter $\sigma_i^{2*}$ of $q^*(\gamma_i)$ , a vector of variance.

The shape parameter  $\lambda^*$  of  $q^*(\sigma_{\gamma}^2)$ .

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eta The scale parameter  $\eta^*$  of  $q^*(\sigma_{\gamma}^2)$ .

expectation\_b The expected value of b.

cluster A numeric vector indicating the cluster assignment for each observation.

#### Value

The evidence lower bound (ELBO).

#### See Also

```
survregVB.fit
```

eta_star	Calculates parameter $\eta^* * of q^* * (\sigma^2_\gamma)$ to optimize the evidence
	based lower bound (ELBO) in survregVB.frailtv.fit.

## Description

Calculates parameter  $\eta^*$  of  $q^*(\sigma^2_\gamma)$  to optimize the evidence based lower bound (ELBO) in survregVB. frailty. fit.

### Usage

```
eta_star(eta_0, tau, sigma)
```

#### **Arguments**

eta\_0 The scale hyperparameter  $\eta_0$  of the prior distribution of the frailty variance,  $\sigma_{\gamma}^2$ .

tau Parameter  $\tau^*$  of  $q^*(\gamma_i)$ , a vector of means.

sigma Parameter  $\sigma_i^{2*}$  of  $q^*(\gamma_i)$ , a vector of variance.

#### Value

```
Parameter \eta^* of q^*(\sigma_{\gamma}^2).
```

```
survregVB.frailty.fit
```

lambda\_star 7

lambda_star	Calculates parameter $\lambda$ * of $q$ * $(\sigma^2 - \gamma)$ to optimize the evidence based lower bound (ELBO) in survregVB. frailty.fit.

## Description

Calculates parameter  $\lambda^*$  of  $q^*(\sigma^2_\gamma)$  to optimize the evidence based lower bound (ELBO) in survegVB.frailty.fit.

## Usage

```
lambda_star(lambda_0, K)
```

#### **Arguments**

lambda\_0 The shape hyperparameter  $\lambda_0$  of the prior distribution of the frailty variance,  $\sigma_{\gamma}^2$ . K The number of clusters.

#### Value

```
Parameter \lambda^* of q^*(\sigma_{\gamma}^2).
```

#### See Also

```
survregVB.frailty.fit
```

lung\_cancer

Subset of GSE102287: African American (AA) Patients

## Description

This dataset is a subset of the GSE102287 dataset that includes only characteristics of patients who are identified as African American (AA).

## Usage

```
lung_cancer
```

## **Format**

A data frame with 60 observations on selected patient characteristics:

```
patient Patient identification number.
age Patient age.
Stage Lung cancer stage (I, II, III).
time Survival time in days.
gender Gender of the patient.
smoking 0 = Never smoked, 1 = Has smoked.
status 0 = Alive, 1 = Death due to lung cancer.
```

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#### **Source**

Gene Expression Omnibus (GEO), Accession: GSE102287. https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSE102287

#### References

Mitchell, K. A., Zingone, A., Toulabi, L., Boeckelman, J., & Ryan, B. M. (2017). Comparative Transcriptome Profiling Reveals Coding and Noncoding RNA Differences in NSCLC from African Americans and European Americans. Clinical cancer research: an official journal of the American Association for Cancer Research, 23(23), 7412–7425. doi:10.1158/1078-0432.CCR-17-0527.

mu_star	Calculates parameter $\mu^* * of q^* * (\beta)$ to optimize the evidence based lower bound (ELBO) in survregVB.fit.
	iower vound (ELDO) in SurviegVD.TIL.

## Description

Calculates parameter  $\mu^*$  of  $q^*(\beta)$  to optimize the evidence based lower bound (ELBO) in survregVB. fit.

#### Usage

```
mu_star(y, X, delta, mu_0, v_0, alpha, omega, mu, Sigma, expectation_b)
```

#### Arguments

У	A vector of observed log-transformed survival times.
X	A design matrix including covariates with first column of ones to represent the intercept.
delta	A binary vector indicating right censoring.
mu_0	Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
alpha	The shape parameter $\alpha^*$ of $q^*(b)$ .
omega	The scale parameter $\omega^*$ of $q^*(b)$ .
mu	Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.
Sigma	Parameter $\Sigma^*$ of $q^*(\beta)$ , a covariance matrix.
expectation_b	The expected value of $b$ .

#### Value

```
Parameter \mu^* of q^*(\beta).
```

```
survregVB.fit
```

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mu_star_cluster	mu_star_cluster	
-----------------	-----------------	--

## Description

Calculates parameter  $\mu^*$  of  $q^*(\beta)$  to optimize the evidence based lower bound (ELBO) in survregVB. frailty. fit.

## Usage

```
mu_star_cluster(
   y,
   X,
   delta,
   mu_0,
   v_0,
   alpha,
   omega,
   mu,
   Sigma,
   tau,
   expectation_b,
   cluster
)
```

## Arguments

у	A vector of observed log-transformed survival times.
X	A design matrix including covariates with first column of ones to represent the intercept.
delta	A binary vector indicating right censoring.
mu_0	Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
alpha	The shape parameter $\alpha^*$ of $q^*(b)$ .
omega	The scale parameter $\omega^*$ of $q^*(b)$ .
mu	Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.
Sigma	Parameter $\Sigma^*$ of $q^*(\beta)$ , a covariance matrix.
tau	Parameter $\tau^*$ of $q^*(\gamma_i)$ , a vector of means.
expectation_b	The expected value of $b$ .
cluster	A numeric vector indicating the cluster assignment for each observation.

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#### Value

```
Parameter \mu^* of q^*(\beta)
```

#### See Also

```
survregVB.frailty.fit
```

omega_star	Calculates parameter $\omega$ $$ * of $\hat{q}$ * $(b)$ to optimize the evidence based
	lower bound (ELBO) in survregVB.fit.

## Description

Calculates parameter  $\omega^*$  of  $q^*(b)$  to optimize the evidence based lower bound (ELBO) in survregVB.fit.

## Usage

```
omega_star(y, X, delta, omega_0, mu, expectation_b)
```

## Arguments

y A vector of observed log-transformed survival times.

X A design matrix including covariates with first column of ones to represent the

intercept.

delta A binary vector indicating right censoring.

omega\_0 The shape hyperparameter  $\omega_0$  of the prior distribution of the scale parameter, b.

mu Parameter  $\mu^*$  of  $q^*(\beta)$ , a vector of means.

 ${\tt expectation\_b} \quad \text{The expected value of } b.$ 

## Value

```
Parameter \omega^* of q^*(b).
```

```
survregVB.fit
```

omega\_star\_cluster 11

omega_star_cluster	Calculates parameter $\omega^* * of q^* * (b)$ to optimize the evidence based lower bound (ELBO) in survregVB.frailty.fit.

## **Description**

Calculates parameter  $\omega^*$  of  $q^*(b)$  to optimize the evidence based lower bound (ELBO) in survregVB. frailty. fit.

#### Usage

```
omega_star_cluster(y, X, delta, omega_0, mu, tau, expectation_b, cluster)
```

#### **Arguments**

у	A vector of observed log-transformed survival times.
X	A design matrix including covariates with first column of ones to represent the intercept.
delta	A binary vector indicating right censoring.
omega_0	The shape hyperparameter $\omega_0$ of the prior distribution of the scale parameter, $b$ .
mu	Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.

tau Parameter  $\tau^*$  of  $q^*(\gamma_i)$ , a vector of means.

 ${\tt expectation\_b} \quad \text{The expected value of } b.$ 

cluster A numeric vector indicating the cluster assignment for each observation.

#### Value

```
Parameter \omega^* of q^*(b).
```

#### See Also

```
survregVB.frailty.fit
```

sigma_squared_star	Calculates parameter $\sigma^2*_i$ of $q^**(\gamma_i)$ for $i=1,,K$
	clusters to optimize the evidence based lower bound (ELBO) in survregVB.frailty.fit.

## Description

Calculates parameter  $\sigma_i^{2*}$  of  $q^*(\gamma_i)$  for i=1,...,K clusters to optimize the evidence based lower bound (ELBO) in survregVB.frailty.fit.

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#### Usage

```
sigma_squared_star(
   y,
   X,
   delta,
   alpha,
   omega,
   mu,
   tau,
   lambda,
   eta,
   expectation_b,
   cluster
)
```

#### **Arguments**

y A vector of observed log-transformed survival times.

X A design matrix including covariates with first column of ones to represent the

intercept.

delta A binary vector indicating right censoring.

alpha The shape parameter  $\alpha^*$  of  $q^*(b)$ .

The scale parameter  $\omega^*$  of  $q^*(b)$ .

mu Parameter  $\mu^*$  of  $q^*(\beta)$ , a vector of means.

tau Parameter  $\tau^*$  of  $q^*(\gamma_i)$ , a vector of means.

lambda The shape parameter  $\lambda^*$  of  $q^*(\sigma^2_{\gamma})$ . eta The scale parameter  $\eta^*$  of  $q^*(\sigma^2_{\gamma})$ .

expectation\_b The expected value of b.

cluster A numeric vector indicating the cluster assignment for each observation.

#### Value

Parameter vector  $\sigma_i^{2*}$  of  $q^*(\gamma_i)$  for all clusters.

```
survregVB.frailty.fit
```

Sigma\_star 13

Sigma_star	Calculates parameter $\Sigma^*$ of $q^* * (\beta)$ to optimize the evidence based lower bound (ELBO) in survegyB. fit.
	tower bound (ELDO) in Sui Vi egvb. 11t.

## Description

Calculates parameter  $\Sigma^*$  of  $q^*(\beta)$  to optimize the evidence based lower bound (ELBO) in survregVB.fit.

## Usage

```
Sigma_star(y, X, delta, v_0, alpha, omega, mu, expectation_b)
```

## Arguments

у	A vector of observed log-transformed survival times.
X	A design matrix including covariates with first column of ones to represent the intercept.
delta	A binary vector indicating right censoring.
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
alpha	The shape parameter $\alpha^*$ of $q^*(b)$ .
omega	The scale parameter $\omega^*$ of $q^*(b)$ .
mu	Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.
expectation_b	The expected value of <i>b</i> .

## Value

```
Parameter \Sigma^* of q^*(\beta).
```

### See Also

```
survregVB.fit
```

Sigma_star_cluster	Calculates parameter $\Sigma^* * of \ q^* * (\beta)$ to optimize the evidence based lower bound (ELBO) in survregVB.frailty.fit.

## Description

Calculates parameter  $\Sigma^*$  of  $q^*(\beta)$  to optimize the evidence based lower bound (ELBO) in survregVB. frailty. fit.

Sigma\_star\_cluster

#### Usage

```
Sigma_star_cluster(
   y,
   X,
   delta,
   v_0,
   alpha,
   omega,
   mu,
   tau,
   expectation_b,
   cluster
)
```

#### **Arguments**

y A vector of observed log-transformed survival times.

X A design matrix including covariates with first column of ones to represent the

intercept.

delta A binary vector indicating right censoring.

 $v_0$  The precision (inverse variance) hyperparameter  $v_0$ , of the prior distribution of

the vector of coefficients,  $\beta$ .

alpha The shape parameter  $\alpha^*$  of  $q^*(b)$ .

omega The scale parameter  $\omega^*$  of  $q^*(b)$ .

mu Parameter  $\mu^*$  of  $q^*(\beta)$ , a vector of means.

tau Parameter  $\tau^*$  of  $q^*(\gamma_i)$ , a vector of means.

 ${\tt expectation\_b} \quad \text{The expected value of } b.$ 

cluster A numeric vector indicating the cluster assignment for each observation.

#### Value

```
Parameter \Sigma^* of q^*(\beta).
```

```
survregVB.frailty.fit
```

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simulation_frailty	Simulated data incorporating shared frailty effects to model clustered
	time-to-event data.

#### **Description**

Simulated data incorporating shared frailty effects to model clustered time-to-event data.

#### Usage

```
simulation_frailty
```

#### **Format**

A dataframe with 75 observations grouped into 15 clusters, each with 5 individuals.

x1 Continuous covariate from N(1, 0.2<sup>2</sup>)

x2 Binary covariate from Bernoulli (0.5)

Time True survival time

**Time.15** Observed survival time accounting for uniformly distributed right censoring time from uniform(0,u)

delta Event indicator for uncensored data (always 1 in this simulation.)

**delta.15** Event indicator after censoring (1 = event, 0 = censored).

**cluster** Cluster ID (1–15), indicating group-level frailty.

@references Xian, C., Souza, C. P. E. de, He, W., Rodrigues, F. F., & Tian, R. (2024). Fast variational bayesian inference for correlated survival data: An application to invasive mechanical ventilation duration analysis. https://doi.org/10.48550/ARXIV.2408.00177

simulation\_nofrailty Simulated data without shared frailty effects to model unclustered time-to-event data.

#### **Description**

Simulated data without shared frailty effects to model unclustered time-to-event data.

#### Usage

```
simulation_nofrailty
```

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#### **Format**

A dataframe with 300 observations.

x1 Continuous covariate from N(1, 0.2^2)

x2 Binary covariate from Bernoulli (0.5)

Time True survival time

**Time.10** Observed survival time accounting for uniformly distributed right censoring time from uniform(0,48)

**Time.30** Observed survival time accounting for uniformly distributed right censoring time from uniform(0,17)

delta Event indicator for uncensored data (always 1 in this simulation.)

**delta.10** Event indicator for T.10 (1 = event, 0 = censored).

**delta.30** Event indicator for T.30 (1 = event, 0 = censored).

@references Xian, C., Souza, C. P. E. de, He, W., Rodrigues, F. F., & Tian, R. (2024). Variational Bayesian analysis of survival data using a log-logistic accelerated failure time model. Statistics and Computing, 34(2). https://doi.org/10.1007/s11222-023-10365-6

summary.survregVB

Summary for Variational Bayes log-logistic AFT models.

#### **Description**

Produces a summary of a fitted Variational Bayes Parametric Survival Regression Model for a Log-Logistic AFT Model

#### Usage

```
## S3 method for class 'survregVB'
summary(object, ci = 0.95, ...)
```

#### **Arguments**

object The result of a survregVB fit.

ci The significance level for the credible intervals. (Default:0.95).

... For future arguments.

## Value

An object of class summary.survregVB with components:

- ELBO: The final value of the Evidence Lower Bound (ELBO) at the last iteration.
- alpha: The shape parameter  $\alpha^*$  of  $q^*(b)$ .
- omega: The scale parameter  $\omega^*$  of  $q^*(b)$ .

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- mu: Parameter  $\mu^*$  of  $q^*(\beta)$ , a vector of means.
- Sigma: Parameter  $\Sigma^*$  of  $q^*(\beta)$ , a covariance matrix.
- na.action: A missing-data filter function, applied to the model.frame, after any subset argument has been used.
- iterations: The number of iterations performed by the VB algorithm: before converging or reaching max\_iteration.
- n: The number of observations.
- call: The function call used to invoke the survregVB method.
- not\_converged: A boolean indicating if the algorithm converged.
  - TRUE: If the algorithm did not converge prior to achieving max\_iteration.
  - NULL: If the algorithm converged successfully.
- estimates: A matrix with one row for each regression coefficient, and one row for the scale parameter. The columns contain:
  - Value: The estimated value based on the posterior distribution mean.
  - Lower CI: The lower bound of the credible interval.
  - Upper CI: The upper bound of the credible interval.

If called with shared frailty, the object also contains components:

- lambda: The shape parameter  $\lambda^*$  of  $q^*(\sigma_{\gamma}^2)$ .
- eta: The scale parameter  $\eta^*$  of  $q^*(\sigma^2_{\gamma})$ .
- tau: Parameter  $\tau_i^*$  of  $q^*(\gamma_i)$ , a vector of means.
- sigma: Parameter  $\sigma_i^{2*}$  of  $q^*(\gamma_i)$ , a vector of variance.

The estimates component will contain an additional row for the frailty, the estimated variance based on the posterior mean for the random intercepts.

#### See Also

survregVB

survregVB	Variational Bayesian Analysis of Survival Data Using a Log-Logistic
	Accelerated Failure Time Model

#### **Description**

Applies a mean-field Variational Bayes (VB) algorithm to infer the parameters of an accelerated failure time (AFT) survival model with right-censored survival times following a log-logistic distribution.

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#### Usage

```
survregVB(
  formula,
  data,
  alpha_0,
  omega_0,
  mu_0,
  v_0,
  lambda_0,
  eta_0,
  na.action,
  cluster,
  max_iteration = 100,
  threshold = 1e-04
)
```

#### **Arguments**

formula	A formula object, with the response on the left of a ~ operator, and the covariates on the right. The response must be a survival object of type right, as returned by the Surv function.
data	A data.frame in which to interpret the variables named in the formula and cluster arguments.
alpha_0	The shape hyperparameter $\alpha_0$ of the prior distribution of the scale parameter, $b$ .
omega_0	The shape hyperparameter $\omega_0$ of the prior distribution of the scale parameter, b.
mu_0	Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
lambda_0	The shape hyperparameter $\lambda_0$ of the prior distribution of the frailty variance, $\sigma_{\gamma}^2$ .
eta_0	The scale hyperparameter $\eta_0$ of the prior distribution of the frailty variance, $\sigma_{\gamma}^2$ .
na.action	A missing-data filter function, applied to the model.frame, after any subset argument has been used. (Default:options()\$na.action).
cluster	An optional variable which clusters the observations to introduce shared frailty for correlated survival data.
max_iteration	The maximum number of iterations for the variational inference optimization. If reached, iteration stops. (Default:100)
threshold	The convergence threshold for the evidence based lower bound (ELBO) optimization. If the difference between the current and previous ELBO's is smaller than this threshold, iteration stops. (Default:0.0001)

#### **Details**

The goal of survregVB is to maximize the evidence lower bound (ELBO) to approximate posterior distributions of the AFT model parameters using the VB algorithms with and without shared frailty proposed in Xian et al. (2024) doi:10.1007/s11222-023-10365-6 and doi:10.48550/ARXIV. 2408.00177 respectively.

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#### Value

An object of class survregVB.

#### References

Xian, C., Souza, C. P. E. de, He, W., Rodrigues, F. F., & Tian, R. (2024). "Variational Bayesian analysis of survival data using a log-logistic accelerated failure time model." Statistics and Computing, 34(2). https://doi.org/10.1007/s11222-023-10365-6

Xian, C., Souza, C. P. E. de, He, W., Rodrigues, F. F., & Tian, R. (2024). "Fast variational bayesian inference for correlated survival data: An application to invasive mechanical ventilation duration analysis." https://doi.org/10.48550/ARXIV.2408.00177

#### See Also

```
survregVB.object
```

#### **Examples**

```
# Data frame containing survival data
fit <- survregVB(</pre>
 formula = survival::Surv(time, infect) ~ trt + fev,
 data = dnase,
 alpha_0 = 501,
 omega_0 = 500,
 mu_0 = c(4.4, 0.25, 0.04),
 v_0 = 1,
 max_iteration = 100,
 threshold = 0.0005
)
summary(fit)
# Call the survregVB function with shared frailty
fit2 <- survregVB(</pre>
 formula = survival::Surv(Time.15, delta.15) ~ x1 + x2,
 data = simulation_frailty,
 alpha_0 = 3,
 omega_0 = 2,
 mu_0 = c(0, 0, 0),
 v_0 = 0.1
 lambda_0 = 3,
 eta_0 = 2,
 cluster = cluster,
 max_iteration = 100,
 threshold = 0.01
summary(fit2)
```

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	iational Bayesian Analysis of Survival Data Using a Log-Logistic elerated Failure Time Model
--	---

## Description

Called by survregVB to do the actual parameter and ELBO computations. This routine does no checking that the arguments are the proper length or type.

## Usage

```
survregVB.fit(
    Y,
    X,
    alpha_0,
    omega_0,
    mu_0,
    v_0,
    max_iteration = 100,
    threshold = 1e-04
)
```

#### Arguments

Υ	A Surv object containing 2 columns: time and event.
X	A design matrix including covariates with first column of ones to represent the intercept.
alpha_0	The shape hyperparameter $\alpha_0$ of the prior distribution of the scale parameter, $b$ .
omega_0	The shape hyperparameter $\omega_0$ of the prior distribution of the scale parameter, $b$ .
mu_0	Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
max_iteration	The maximum number of iterations for the variational inference optimization. If reached, iteration stops. (Default:100)
threshold	The convergence threshold for the evidence based lower bound (ELBO) optimization. If the difference between the current and previous ELBO's is smaller than this threshold, iteration stops. (Default:0.0001)

#### **Details**

Implements the Variational Bayes algorithm proposed in the paper "Variational Bayesian analysis of survival data using a log-logistic accelerated failure time model."

For right-censored survival time  $T_i$  of the  $i_{th}$  subject in a sample, i=1,...,n, the log-logistic AFT model is specified as follows:

$$\log(T_i) = X_i^T \beta + bz_i$$
, where

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•  $X_i$  is a column vector of length  $p, p \ge 2$  containing p-1 covariates and a constant one to incorporate the intercept (i.e.,  $X_i = (1, x_{i1}, ..., x_{i(p-1)})^T$ ),

- $\beta$  is the corresponding vector of coefficients for the fixed effects,
- $z_i$  is a random variable following a standard logistic distribution, and
- *b* is a scale parameter.

#### Value

A list containing results of the fit.

#### References

Xian, C., Souza, C. P. E. de, He, W., Rodrigues, F. F., & Tian, R. (2024). "Variational Bayesian analysis of survival data using a log-logistic accelerated failure time model." Statistics and Computing, 34(2). https://doi.org/10.1007/s11222-023-10365-6

#### See Also

```
survregVB
```

#### **Examples**

```
fit <- survregVB.fit(
   Y = survival::Surv(simulation_nofrailty$Time, simulation_nofrailty$delta),
   X = matrix(c(rep(1, 300), simulation_nofrailty$x1, simulation_nofrailty$x2), nrow = 300),
   alpha_0 = 11,
   omega_0 = 10,
   mu_0 = c(0, 0, 0),
   v_0 = 1
)</pre>
```

survregVB.frailty.fit Variational Bayesian Analysis of Correlated Survival Data Using a Log-Logistic Accelerated Failure Time Model

#### Description

Called by survregVB to do the actual parameter and ELBO computations for correlated survival data with shared frailty (a random intercept). This routine does no checking that the arguments are the proper length or type.

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#### Usage

```
survregVB.frailty.fit(
   Y,
   X,
   alpha_0,
   omega_0,
   mu_0,
   v_0,
   lambda_0,
   eta_0,
   cluster,
   max_iteration = 100,
   threshold = 1e-04
)
```

#### **Arguments**

Υ	A Surv object containing 2 columns: time and event.
X	A design matrix including covariates with first column of ones to represent the intercept.
alpha_0	The shape hyperparameter $\alpha_0$ of the prior distribution of the scale parameter, $b$ .
omega_0	The shape hyperparameter $\omega_0$ of the prior distribution of the scale parameter, $b$ .
mu_0	Hyperparameter $\mu_0$ , a vector of means, of the prior distribution of the vector of coefficients, $\beta$ .
v_0	The precision (inverse variance) hyperparameter $v_0$ , of the prior distribution of the vector of coefficients, $\beta$ .
lambda_0	The shape hyperparameter $\lambda_0$ of the prior distribution of the frailty variance, $\sigma_\gamma^2$ .
eta_0	The scale hyperparameter $\eta_0$ of the prior distribution of the frailty variance, $\sigma_\gamma^2$ .
cluster	An optional variable which clusters the observations to introduce shared frailty for correlated survival data.
max_iteration	The maximum number of iterations for the variational inference optimization. If reached, iteration stops. (Default: $100$ )
threshold	The convergence threshold for the evidence based lower bound (ELBO) optimization. If the difference between the current and previous ELBO's is smaller than this threshold, iteration stops. (Default: $0.0001$ )

#### **Details**

Implements the Variational Bayes algorithm with random intercepts proposed in the paper "Fast variational bayesian inference for correlated survival data: An application to invasive mechanical ventilation duration analysis".

For right-censored survival time  $T_{ij}$  of the  $j_{th}$  subject from the  $i_{th}$  cluster in the sample, in a sample, i=1,...,K and  $j=1,...,n_i$ , the shared-frailty log-logistic AFT model is specified as follows:  $\log(T_{ij}) = \gamma_i + X_{ij}^T \beta + b \epsilon_{ij}$ , where

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•  $X_{ij}$  is a column vector of length  $p, p \ge 2$  containing p-1 covariates and a constant one to incorporate the intercept (i.e.,  $X_i = (1, x_{ij1}, ..., x_{ij(p-1)})^T$ ),

- $\beta$  is the corresponding vector of coefficients for the fixed effects,
- $\gamma_i$  is a random intercept for the  $i_{th}$  cluster,
- ullet  $\epsilon_{ij}$  is a random variable following a standard logistic distribution, and
- *b* is a scale parameter.

#### Value

A list containing results of the fit.

#### References

Xian, C., Souza, C. P. E. de, He, W., Rodrigues, F. F., & Tian, R. (2024). "Fast variational bayesian inference for correlated survival data: An application to invasive mechanical ventilation duration analysis." https://doi.org/10.48550/ARXIV.2408.00177

#### See Also

```
survregVB
```

#### **Examples**

```
fit <- survregVB.frailty.fit(
  X = matrix(c(rep(1, 75), simulation_frailty$x1, simulation_frailty$x2), nrow = 75),
  Y = survival::Surv(simulation_frailty$Time, simulation_frailty$delta),
  alpha_0 = 3,
  omega_0 = 2,
  mu_0 = c(0, 0, 0),
  v_0 = 0.1,
  lambda_0 = 3,
  eta_0 = 2,
  cluster = simulation_frailty$cluster
)</pre>
```

survregVB.object

Variational Bayes Accelererated Failure Time Survival Model Object

#### **Description**

This class of objects is returned by the survregVB function to represent a fitted parametric log-logistic accelerated failure time (AFT) survival model. Objects of this class have methods for the functions print and summary.

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#### **Details**

For approximate posterior distributions:

- $q^*(\beta)$ , a  $N_p(\mu^*, \Sigma^*)$  density function, and
- $q^*(b)$ , an Inverse-Gamma $(\alpha^*, \omega^*)$  density function,

the components of this class are:

- ELBO: The final value of the Evidence Lower Bound (ELBO) at the last iteration.
- alpha: The shape parameter  $\alpha^*$  of  $q^*(b)$ .
- omega: The scale parameter  $\omega^*$  of  $q^*(b)$ .
- mu: Parameter  $\mu^*$  of  $q^*(\beta)$ , a vector of means.
- Sigma: Parameter  $\Sigma^*$  of  $q^*(\beta)$ , a covariance matrix.
- na.action: A missing-data filter function, applied to the model.frame, after any subset argument has been used.
- iterations: The number of iterations performed by the VB algorithm: before converging or reaching max\_iteration.
- n: The number of observations.
- call: The function call used to invoke the survregVB method.
- not\_converged: A boolean indicating if the algorithm converged.
  - TRUE: If the algorithm did not converge prior to achieving max\_iteration.
  - NULL: If the algorithm converged successfully.

If survregVB was called with shared frailty (with the cluster argument), for approximate posterior distributions:

- $q^*(\sigma_{\gamma}^2)$ , an Inverse-Gamma $(\lambda^*, \eta^*)$  density function,
- $q^*(\gamma_i)$ , a  $N(\tau_i^*, \sigma_i^{2*})$  density function, for i=1,...,K clusters, and

the additional components are present:

- lambda: The shape parameter  $\lambda^*$  of  $q^*(\sigma_{\gamma}^2)$ .
- eta: The scale parameter  $\eta^*$  of  $q^*(\sigma_{\gamma}^2)$ .
- tau: Parameter  $\tau_i^*$  of  $q^*(\gamma_i)$ , a vector of means.
- sigma: Parameter  $\sigma_i^{2*}$  of  $q^*(\gamma_i)$ , a vector of variance.

tau\_star 25

tau_star	Calculates parameter $\tau$ * _i of $q$ * $(\gamma_i)$ for $i=1,,K$ clusters to optimize the evidence based lower bound (ELBO) in Survived R frailty fit
	survregVB.frailty.fit.

## Description

Calculates parameter  $\tau_i^*$  of  $q^*(\gamma_i)$  for i=1,...,K clusters to optimize the evidence based lower bound (ELBO) in survregVB.frailty.fit.

## Usage

```
tau_star(y, X, delta, alpha, omega, mu, tau, sigma, expectation_b, cluster)
```

## Arguments

у	A vector of observed log-transformed survival times.
X	A design matrix including covariates with first column of ones to represent the intercept.
delta	A binary vector indicating right censoring.
alpha	The shape parameter $\alpha^*$ of $q^*(b)$ .
omega	The scale parameter $\omega^*$ of $q^*(b)$ .
mu	Parameter $\mu^*$ of $q^*(\beta)$ , a vector of means.
tau	Parameter $\tau^*$ of $q^*(\gamma_i)$ , a vector of means.
sigma	Parameter $\sigma_i^{2*}$ of $q^*(\gamma_i)$ , a vector of variance.
expectation_b	The expected value of $b$ .
cluster	A numeric vector indicating the cluster assignment for each observation.

## Value

Parameter vector  $\tau_i^*$  of  $q^*(\gamma_i)$  for i=1,...,K clusters.

```
survregVB.frailty.fit
```

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