Package 'SPARRAfairness'

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Title Analysis of Differential Behaviour of SPARRA Score Across Demographic Groups

Version 0.0.0.2

License GPL (>= 3)

Maintainer James Liley <james.liley@durham.ac.uk>

Description The SPARRA risk score (Scottish Patients At Risk of admission and Re-Admission) estimates yearly risk of emergency hospital admission using electronic health records on a monthly basis for most of the Scottish population. This package implements a suite of functions used to analyse the behaviour and performance of the score, focusing particularly on differential performance over demographically-defined groups. It includes useful utility functions to plot receiver-operator-characteristic, precision-recall and calibration curves, draw stock human figures, estimate counterfactual quantities without the need to re-compute risk scores, to simulate a semi-realistic dataset.

```
Encoding UTF-8

LazyData true

Depends R (>= 3.5.0), stats, graphics, grDevices, matrixStats, ranger

Imports mvtnorm,cvAUC,ggplot2,ggrepel,patchwork,scales

RoxygenNote 7.3.1

Suggests knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation no

Author Ioanna Thoma [aut] (<https://orcid.org/0000-0001-6928-2198>),
Catalina Vallejos [ctb] (<https://orcid.org/0000-0003-3638-1960>),
Louis Aslett [ctb] (<https://orcid.org/0000-0003-2211-233X>),
Jill Ireland [ctb] (<https://orcid.org/0000-0003-3578-4477>),
Simon Rogers [ctb] (<https://orcid.org/0000-0003-3578-4477>),
James Liley [cre, aut] (<https://orcid.org/0000-0002-0049-8238>)

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```

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Description

ab() Shorthand to draw a red x-y line

Usage

ab(...)

Arguments

... passed to abline()

adjusted_fdr 3

Value

No return value, draws a figure

Description

Estimates false discovery rate P(target=FALSE|score>cutoff,group=g) 'adjusted' for some category.

Usage

```
adjusted_fdr(
   scores,
   target,
   category,
   group1,
   group2,
   cutoffs = seq(min(scores, na.rm = TRUE), max(scores, na.rm = TRUE), length = 100),
   nboot = 100
)
```

Arguments

```
scores vector of risk scores
target vector of values of target (which risk score aims to predict)
category vector of categories
group1 indices of group 1
group2 indices of group 2
cutoffs score cutoffs at which to estimate metric (default 100 evenly-spaced)
nboot number of bootstrap samples for standard error
```

Details

```
Namely, calculates sum ( P(target=FALSE|score>cutoff,category=c,group=g)P(category=c|score<cutoff) ) where the sum is over categories c.
```

Value

matrix of dimension length(cutoffs)x4, with (i,2g-1)th entry the relevant fairness metric for group g at the ith cutoff value and (i,2g)th entry the approximate standard error of the (i,2g-1)th entry

```
# See vignette
```

4 adjusted_for

Description

Estimates false omission rate P(target=TRUE|score<=cutoff,group=g) 'adjusted' for some category.

Usage

```
adjusted_for(
   scores,
   target,
   category,
   group1,
   group2,
   cutoffs = seq(min(scores, na.rm = TRUE), max(scores, na.rm = TRUE), length = 100),
   nboot = 100
)
```

Arguments

```
scores vector of risk scores

target vector of values of target (which risk score aims to predict)

category vector of categories

group1 indices of group 1

group2 indices of group 2

cutoffs score cutoffs at which to estimate metric (default 100 evenly-spaced)

nboot number of bootstrap samples for standard error
```

Details

```
Namely, calculates sum ( P(\text{target=TRUE}|\text{score}<=\text{cutoff},\text{category=c,group=g})P(\text{category=c}|\text{score}<\text{cutoff})) where the sum is over categories c.
```

Value

matrix of dimension length(cutoffs)x4, with (i,2g-1)th entry the relevant fairness metric for group g at the ith cutoff value and (i,2g)th entry the approximate standard error of the (i,2g-1)th entry

```
# See vignette
```

all_data 5

all_data

All data for fairness measures

Description

This object contains all data from analysis of fairness measures in SPARRA v3 and v4.

Usage

```
all_data
```

Format

An object of class list of length 1261.

build_diff

build_diff Prepares a data frame for a ggplot object to compare differences using linear interpolation.

Description

build_diff Prepares a data frame for a ggplot object to compare differences using linear interpola-

Usage

```
build_diff(df, xvar)
```

Arguments

df data frame

name of variable to consider as 'x': interpolate over evenly spaced values of this

variable.

Value

data frame using (common) interpolated x values rather than arbitrary x values

```
# Only used internally
```

6 cal_2panel

| cal_2panel | cal_2panel Draws calibration curves (with legend) with a second |
|------------|---|
| | panel underneath showing predicted differences. |

Description

cal_2panel Draws calibration curves (with legend) with a second panel underneath showing predicted differences.

Usage

```
cal_2panel(
  cals,
  labels,
  col = 1:length(cals),
  xy_col = phs_colours("phs-magenta"),
  ci_col = col,
  highlight = NULL,
  yrange_lower = NULL,
  legend_title = ""
)
```

Arguments

| cals | list of calibration objects, output from getcal(). |
|--------------|--|
| labels | labels to use in legend |
| col | line colours |
| xy_col | line colour for x-y line, defaults to phs-magenta |
| ci_col | colours to draw confidence intervals on lower panel; NA to not draw. |
| highlight | if non-null, highlight a particular value |
| yrange_lower | y range for lower plot. If NULL, generates automatically |
| legend_title | title for legend, defaults to nothing |

Value

Silently return ggplot object

```
# See vignette
```

counterfactual_yhat 7

counterfactual_yhat

Description

Estimation of counterfactual quantities by resampling.

Usage

```
counterfactual_yhat(dat, X, x = NULL, G, g, gdash, excl = NULL, n = NULL)
```

Arguments

| dat | data frame containing variables in X, Yhat, G, excl. Variables in U are assumed to be colnames(dat)\(X U Yhat U G U excl) |
|-------|--|
| X | set of variables and values on which to 'condition'; essentially we assume that any causal pathway from G to Yhat is through X |
| X | values of variables \boldsymbol{X} on which to condition; can be null in which case we use marginal distribution of \boldsymbol{X} |
| G | grouping variable, usually a sensitive attribute |
| g | conditioned value of g |
| gdash | counterfactual value of g |
| excl | variable names to exclude from U |
| n | number of samples; if NULL return all |

Details

Counterfactual fairness is with respect to the causal graph:

where

- G=group (usually sensitive attribute);
- Yhat=outcome;
- X=set of variables through which G can act on Yhat,
- U=set of background variables;

We want the counterfactual $Yhat_{g' < -G}|X = x, G = g$ (or alternatively $(Yhat_{g' < -G}|G = g)$), using the term Yhat as it appears in the function, rather than \hat{Y} .

This can be interpreted as: the distribution of values of Yhat amongst individuals whose values of U are distribution, comparison of the counterfactual quantity above to the conditional (Yhat|G=g) isolates the difference in Yhat due to the effect of G on Yhat through X, removing any effect due to different distributions of U due to different values of G.

To estimate $Y' = Yhat_{g' \to G}|G = g$, we need to

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- 1. Compute $U' \sim (U|G = g)$
- 2. Compute the distribution X' as $X' \sim (X|U|U', G = g')$
- 3. Sample Y' ($Yhat|X \sim X', U \sim U'$)

To estimate $Y' = Yhat_{g' \to G}|X = x, G = g$, we need to

- 1. Compute $U' \sim (U|G = g, X = x)$
- 2. Compute the distribution X' as $X' \sim (X|U \sim U', G = g')$
- 3. Sample $Y' \sim (Yhat|X \sim X', U \sim U')$

This function approximates this samplying procedure as follows

- 1. Look at individuals with G = g (and optionally X = x)
- 2. Find the values of U for these individuals
- 3. Find a second set of individuals with the same values of U but for whom G = g'
- 4. Return the indices of these individuals

The values of Yhat for these individuals constitute a sample from the desired counterfactual.

Value

indices representing sample(s) from counterfactual Yhat(g' <- G) |X=x,G=g

```
set.seed(23173)
N=10000
# Background variables sampler
background_U=function(n) runif(n) # U~U(0,1)
# Structural equations
struct_G=function(u,n) rbinom(n,1,prob=u) # G|U=u ~ Bern(u)
struct_X=function(u,g,n) rbinom(n,1,prob=u*(0.5 + 0.5*g)) # X|U=u,G=g \sim Bern(u(1+g)/2)
struct_Yhat=function(u,x,n) (runif(n,0,x) + runif(n,0,u))/2 # Yhat|X,N ~ (U(0,X) + U(0,U))/2
# To see that the counterfactual 'isolates' the difference in Yhat due to the
  causal pathway from G to Yhat through X, change the definition of struct_G to
  struct_G=function(u,n) rbinom(n,1,prob=1/2) # G|U=u ~ Bern(1/2)
\# so the posterior of U|G=g does not depend on g. Note that, with this definition, the
 counterfactual Yhat{G<-1}|G=1 coincides with the conditional Yhat|G=0, since
  the counterfactual G<-1 is equivalent to just conditioning on G=1.
# By contrast, if we change struct_G back to its original definition, but
  change the definition of struct_Yhat to
# struct_Yhat=function(u,x,n) (runif(n,0,1) + runif(n,0,u))/2 # Yhat|X,N \sim (U(0,1) + U(0,U))/2
# so Yhat depends on G only through the change in posterior of U from changing g,
```

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```
# the counterfactual Yhat\{G<01\} | G=1 coincides with the conditional Yhat | G=1.
# Sample from complete causal model
U=background_U(N)
G=struct_G(U,N)
X=struct_X(U,G,N)
Yhat=struct_Yhat(U,X,N)
dat=data.frame(U,G,X,Yhat)
# True counterfactual Yhat{G <- 0}|G=1</pre>
w1=which(dat$G==1)
n1=length(w1)
UG1=dat$U[w1] # This is U|G=1
XG1=struct_X(UG1,rep(0,n1),n1)
YhatG1=struct_Yhat(UG1,XG1,n1)
# Estimated counterfactual Yhat{G <- 0}|G=1
ind_G1=counterfactual_yhat(dat,X="X",G="G",g = 1, gdash = 0)
YhatG1_resample=dat$Yhat[ind_G1]
# True counterfactual Yhat{G <- 0}|G=1,X=1</pre>
w11=which(dat$G==1 & dat$X==1)
n11=length(w11)
UG1X1=dat$U[w11] # This is U|G=1,X=1
XG1X1=struct_X(UG1X1,rep(0,n11),n11)
YhatG1X1=struct_Yhat(UG1X1,XG1X1,n11)
# Estimated counterfactual Yhat{G <- 0}|G=1
ind_G1X1=counterfactual_yhat(dat,X="X",G="G",g = 1, gdash = 0,x=1)
YhatG1X1_resample=dat$Yhat[ind_G1X1]
# Compare CDFs
x=seq(0,1,length=1000)
oldpar = par(mfrow=c(1,2))
plot(0, type="n", xlim=c(0,1), ylim=c(0,1), xlab="Value",
     ylab=expression(paste("Prop. ",hat('Y')," < x")))
lines(x,ecdf(dat\$Yhat)(x),col="black") # Unconditional CDF of Yhat
lines(x,ecdf(dat$Yhat[which(dat$G==1)])(x),col="red") # Yhat|G=1
lines(x,ecdf(dat\$Yhat[which(dat\$G==\emptyset)])(x),col="blue") \ \# \ Yhat|G=\emptyset
# True counterfactual Yhat{G <- 0}|G=1</pre>
lines(x,ecdf(YhatG1)(x),col="blue",lty=2)
# Estimated counterfactual Yhat{G <- 0}|G=1</pre>
lines(x,ecdf(YhatG1_resample)(x),col="blue",lty=3)
```

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```
legend("bottomright",
                  c(expression(paste(hat('Y'))),
                        expression(paste(hat('Y'),"|G=1")),
                        expression(paste(hat('Y'), "|G=0")),
                       expression(paste(hat(Y)[G %<-% 0],"|G=1 (true)")),</pre>
                        expression(paste(hat(Y)[G %<-% 0],"|G=1 (est.)"))),</pre>
                  col=c("black","red","blue","blue","blue"),
                  lty=c(1,1,1,2,3),
                  cex=0.5)
plot(0,type="n",xlim=c(0,1),ylim=c(0,1),xlab="Value",
             ylab=expression(paste("Prop. ",hat('Y')," < x")))</pre>
lines(x, ecdf(dat\$Yhat[which(dat\$X==1)])(x), col="black") \ \# \ CDF \ of \ Yhat|X=1)
lines(x,ecdf(dat\$Yhat[which(dat\$G==1 \& dat\$X==1)])(x),col="red") \ \# \ Yhat|G=1,X=1
\label{lines} lines(x,ecdf(dat\$Yhat[which(dat\$G==0 \& dat\$X==1)])(x),col="blue") \# Yhat|G=0,X=1 \\ lines(x,ecdf(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which(dat\$Yhat[which
# True counterfactual Yhat{G <- 0}|G=1,X=1</pre>
lines(x,ecdf(YhatG1X1)(x),col="blue",lty=2)
# Estimated counterfactual Yhat{G <- 0}|G=1,X=1
lines(x,ecdf(YhatG1X1_resample)(x),col="blue",lty=3)
legend("bottomright",
                  c(expression(paste(hat('Y|X=1'))),
                        expression(paste(hat('Y'),"|G=1,X=1")),
                        expression(paste(hat('Y'),"|G=0,X=1")),
                        expression(paste(hat(Y)[G %<-% 0],"|G=1,X=1 (true)")),
                        expression(paste(hat(Y)[G %<-% 0],"|G=1,X=1 (est.)"))),
                   col=c("black","red","blue","blue","blue"),
                  1ty=c(1,1,1,2,3),
                  cex=0.5)
# In both plots, the estimated counterfactual CDF closely matches the CDF of the
# true counterfactual.
# Restore parameters
par(oldpar)
```

dat2mat

dat2mat

Description

Generates matrices for decomposition of admission type which can be used in plot_decomp

Usage

```
dat2mat(dat, score, group1, group2, nquant = 20, cats = unique(dat$reason))
```

decomposition_matrix 11

Arguments

| dat | data frame with population data, such as output from sim_pop_data. Must in- |
|-----|---|
| | clude a column reason |

score risk scores corresponding to dat

group1 indices for group 1 group2 indices for group 2

nquant number of quantiles of code to use; default 20

cats vector of strings giving names of admission categories; default the unique values

in dat\$reason. Can include NAs.

Details

Generates two matrices with the following specifications: Each matrix corresponds to one group Columns are named with the admission types to be plotted. Any admission types including the string 'Died' are counted as deaths If the matrix has N rows, these are interpreted as corresponding to N score quantiles The (i,j)th entry of the matrix is the number of people admitted for reason i with a score greater than or equal to (j-1)/N and less than (j/N) who are in that group

Value

list with two objects matrix1 and matrix2 giving output matrices

Examples

See vignette

Description

Matrix giving frequency of admission types for various groups at various score thresholds. Row names are of the form vX_Y_qZ, where X is version (3 or 4), Y is cohort (e.g., all, over 65, island postcode) and Z is quantile (1-20) of score. Column names are cause of admission or cause of death.

Usage

decomposition_matrix

Format

An object of class data. frame with 520 rows and 41 columns.

12 drawperson

demographic_parity demographic_parity

Description

Estimates demographic parity for a risk score (essentially cumulative distribution function)

Usage

```
demographic_parity(
   scores,
   group1,
   group2,
   cutoffs = seq(min(scores, na.rm = TRUE), max(scores, na.rm = TRUE), length = 100)
)
```

Arguments

scores vector of risk scores

group1 indices of group 1

group2 indices of group 2

cutoffs score cutoffs at which to estimate DP (default 100 evenly-spaced)

Value

matrix of dimension length(cutoffs)x4, with (i,2g-1)th entry the proportion of scores in group g which are less than or equal to the ith cutoff value and (i,2g)th entry the approximate standard error of the (i,2g-1)th entry

Examples

```
# See vignette
```

drawperson drawperson

Description

Draws a simple stock image of a person.

drawperson 13

Usage

```
drawperson(
 xloc = 0,
 yloc = 0,
  scale = 1,
 headsize = 0.16,
 headangle = pi/8,
  headloc = 0.5,
  necklength = 0.1,
  shoulderwidth = 0.1,
  shouldersize = 0.05,
  armlength = 0.4,
  armangle = 7 * pi/8,
  armwidth = 0.08,
  leglength = 0.5,
  legangle = 9 * pi/10,
  legwidth = 0.15,
  torsolength = 0.4,
)
```

Arguments

xloc x-axis offset from origin y-axis offset from origin yloc scale scale upwards from 1x1 box headsize head size headangle half angle of neck in terms of head location of centre of head relative to origin with scale 1 headloc necklength neck length shoulderwidth shoulder width size radius of arc for shoulder shouldersize armlength arm length armangle angle of arm from horizontal armwidth width of arm leglength leg length legangle angle of leg from horizontal legwidth width of leg torsolength length of torso

other parameters passed to polygon()

Details

. . .

Draws a figure at a particular location. With defaults, has centre at origin and fits in 1x1 box. Dimensions customisable

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Value

invisibly returns co-ordinates

Examples

drawprop

drawprop

Description

Illustrates a proportion as a set of people who are blue rather than red.

Usage

```
drawprop(prop, ci, nxy = 10, col1 = "maroon", col2 = "lightblue", ...)
```

Arguments

| prop | the proportion to illustrate |
|------|--|
| ci | half the 95% CI width of the proportion. |
| nxy | illustrate on an n x n grid |
| col1 | colour to put the 'in' proportion |
| col2 | the other colour |
| | passed to 'plot' |

Details

Why anyone would want to think about a proportion this way is beyond the understanding of the authors, but the people have spoken.

Value

No return value, draws a figure

```
# See vignette
```

for_breakdown 15

| akdown for_breakdown |
|----------------------|
|----------------------|

Description

For a given category (e.g., 'male', 'over 65') considers

- 1. all admissions for people in that category
- 2. all admissions for people in that category for which the SPARRA score was less than some threshold (e.g., false negatives

Usage

```
for_breakdown(
  decomp_table,
  group,
  threshold,
  inc_died = TRUE,
  ldiff = 0.005,
  ci = 0.95,
  xlimit = c(-0.05, 0.35),
  ylimit = c(-0.04, 0.04)
)
```

Arguments

| decomp_table | matrix for group; see specification in description |
|--------------|--|
| group | name of group |
| threshold | cutoff, rounded to nearest 0.05 |
| inc_died | set to TRUE to include a second panel showing 'death' type admissions |
| ldiff | specifically label points this far from xy line |
| ci | set to a value <1 to draw confidence intervals at that value, or FALSE to not draw confidence intervals. |
| xlimit | limits for x axis; default c(-0.05,0.35) |
| ylimit | limits for y axis; default c(-0.04,0.04) |
| | |

Details

For each of these groups, we consider the breakdown of medical admission types. We then plot the frequency of admission types in group 1 against the difference in frequencies between group 1 and group 2 (group 2 minus group 1). An admission type which is relatively more common in group (1) indicates that, in the relevant category, the admission type tends to be associated with higher SPARRA scores (and is in a sense easier to predict). Such admission types will correspond to points below the line y=0. Admission types which are relatively more common in group 2 correspond to

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those which are relatively harder to predict. These correspond to points above the line y=0 Since points are close together, only those greater than a certain distance from 0 are marked.

Takes as an argument a matrix in which The matrix shows only data for the group in question Columns are named with the admission types to be plotted. Any admission types including the string 'Died' are counted as deaths If the matrix has N rows, these are interpreted as corresponding to N score quantiles in increasing order. The (i,j)th entry of the matrix is the number of people admitted for reason i with a score greater than or equal to (j-1)/N and less than (j/N) who are in that group

Value

```
ggplot figure (invisible)
```

Examples

```
# See vignette
```

getcal

getcal()

Description

Produces a set of points for a calibration plot.

Usage

```
getcal(
   y,
   ypred,
   n = 10,
   kernel = FALSE,
   kernel_sd = 0.05,
   alpha = 0.05,
   c0 = 0,
   c2 = 0.1
)
```

Arguments

```
y class labels, 0/1 or logical

ypred predictions Pr(Y=1), numeric vector

n number of subintervals/points

kernel set to TRUE to use kernel method

kernel_sd kernel width for kernel method; see above

alpha return a pointwise confidence envolope for conservative 1-alpha confidence in-
```

terval

getprc 17

| c0 | for computing maximum bias; assume true covariance function is of the form $a0+a1x+a2x^2$, with $ a0 , a2 (c1 does not matter)$ |
|----|---|
| c2 | for computing maximum bias; assume true covariance function is of the form $a0+a1x+a2x^2$, with $a0<0$, $a2<0$ (c1 does not matter) |

Details

Uses either a binning method or a kernel method to determine height of points.

In both methods, considers n equally spaced subintervals of (0,1)

Value

a list with components x (expected calibration), y (observed calibration), n (number of samples in bins, if relevant), lower/upper (confidence interval on y)

Examples

```
# See vignette
```

|--|

Description

Comprehensive plotting function for precision-recall curve. Also calculates AUPRC and standard error.

Usage

```
getprc(y, ypred, cv = NULL, res = 100)
```

Arguments

| У | class labels, 0/1 or logical |
|-------|--|
| ypred | predictions Pr(Y=1), numeric vector |
| CV | cross-validation fold assignments, if relevant. Changes estimate of standard error. |
| res | resolution. Returns this many equally-spaced points along the curve. Set res to null to return all points. |

Details

Rather than returning points corresponding to every cutoff, only returns a representative sample of equally-spaced points along the curve.

Does not plot anything. Object can be plotted in a default way.

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Value

list containing: ppv, ppv for res points in every cv fold; sens, sensitivity for res points in every cv fold; auc, areas under the curve for each fold and average (note length is 1 greater than number of CV folds); se, standard error for AUC in each fold and standard error for average auc (note length is 1 greater than number of CV folds)

Examples

See vignette

getroc getroc() Comprehensive plotting function for receiver-operator characteristic curve. Also calculates AUROC and standard error.

Description

Rather than returning points corresponding to every cutoff, only returns a representative sample of equally-spaced points along the curve.

Usage

```
getroc(y, ypred, cv = NULL, res = 100)
```

Arguments

| У | class labels, 0/1 or logical |
|-------|--|
| ypred | predictions Pr(Y=1), numeric vector |
| CV | cross-validation fold assignments, if relevant. Changes estimate of standard er- |
| | ror. |
| res | resolution. Returns this many equally-spaced points along the curve. Set res to |

null to return all points.

Details

SE of AUROC with no CV structure is from Hanley and McNeil 1982. SE of AUROC with CV folds is from LeDell et al 2012

Does not plot anything. Object can be plotted in a default way.

Value

list containing: spec, specificity for res points in every cv fold; sens, sensitivity for res points in every cv fold; auc, areas under the curve for each fold and average (note length is 1 greater than number of CV folds); se, standard error for AUC in each fold and standard error for average auc (note length is 1 greater than number of CV folds)

Examples

See vignette

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| <pre>groupmetric_2panel</pre> | groupmetric_2panel Draws plots of a group fairness metric with a sec- |
|-------------------------------|---|
| | ond panel underneath |

Description

groupmetric_2panel Draws plots of a group fairness metric with a second panel underneath

Usage

```
groupmetric_2panel(
  objs,
  labels = names(objs),
  col = 1:length(objs),
  yrange = NULL,
  ci_col = col,
  highlight = NULL,
  logscale = FALSE,
  lpos = c(1, 0),
  yrange_lower = NULL,
  legend_title = ""
)
```

Arguments

| objs | list of fairness objects. Each should contain sub-objects 'x', 'y' and 'ci', which specify x and y values and half-widths of confidence intervals around y. |
|--------------|---|
| labels | labels to use in legend |
| col | line colours |
| yrange | limit of y axis; defaults to 0,1 |
| ci_col | confidence envelope colours. These will be transparent. |
| highlight | if non-null, draw a point at a particular cutoff |
| logscale | if TRUE, draw with log-scale. |
| lpos | legend position; as accepted by ggplot legend.position |
| yrange_lower | y range for lower plot. If NULL, generates automatically |
| legend_title | title for legend, defaults to nothing |

Value

Silently return ggplot object

```
# See vignette
```

20 group_fairness

Description

Estimates group fairness metric according to a specification vector of the form

Usage

```
group_fairness(
   specs,
   scores,
   target,
   group1,
   group2,
   cutoffs = seq(min(scores, na.rm = TRUE), max(scores, na.rm = TRUE), length = 100)
)
```

Arguments

```
specs specification vector; see description
scores vector of risk scores
target vector of values of target (which risk score aims to predict)
group1 indices of group 1
group2 indices of group 2
cutoffs score cutoffs at which to estimate metric (default 100 evenly-spaced)
```

Details

```
c(A1,B1,C1,A2,B2,C2)
encoding a probability
P(A1,B1,C1|A2,B2,C2)
where
A1/A2 are events coded by 1:'score>= cutoff'; 0: 'score<cutoff' and NA: 1/TRUE B1/B2 are events coded by 1:'target=TRUE'; 0: 'target=FALSE' and NA: 1/TRUE C1/C2 are events coded by 1:'group=g'; and NA: 1/TRUE
For example, specs=c(NA,1,NA,0,NA,1) would encode false omission rate:
P(target=TRUE|score<cutoff,group=g)
```

Value

matrix of dimension length(cutoffs)x4, with (i,2g-1)th entry the relevant fairness metric for group g at the ith cutoff value and (i,2g)th entry the approximate standard error of the (i,2g-1)th entry

integral 21

Examples

```
# See vignette
```

integral

integral() Quick form for trapezoidal integration over range of x

Description

integral() Quick form for trapezoidal integration over range of x

Usage

```
integral(x, y = NULL)
```

Arguments

x x co-ordinates, or nx2 matrix of points

y y co-ordinates

Value

trapezoidal estimate of integral of the xth value of y over range of x.

logistic

Logistic

Description

```
Logistic function: 1/(1+exp(-x))
```

Usage

```
logistic(x)
```

Arguments

Х

argument

Value

```
value of logistic(x)
```

```
# Plot
x=seq(-5,5,length=1000)
plot(x,logistic(x),type="1")
```

phs_colours

logit

Logit

Description

```
Logit function: -\log((1/x)-1)
```

Usage

```
logit(x)
```

Arguments

Х

argument

Value

```
value of logit(x); na if x is outside (0,1)
```

Examples

```
# Plot
x=seq(0,1,length=100)
plot(x,logit(x),type="l")

# Logit and logistic are inverses
x=seq(-5,5,length=1000)
plot(x,logit(logistic(x)),type="l")
```

phs_colours

phs_colours

Description

Copied from github, "Public-Health-Scotland/phsstyles". Public Health Scotland colour scheme. Internal function.

Usage

```
phs_colours(colourname = NULL, keep_names = FALSE)
```

Arguments

colourname name of colour; usually something like phs-blue. If NULL returns all colours.

keep_names keep names of colours in return list. Defaults to false.

plot.sparraCAL 23

Value

vector of colours, optionally with names.

plot.sparraCAL

Plot function for class sparraCAL

Description

Plot function for class sparraCAL

Usage

```
## S3 method for class 'sparraCAL'
plot(
    x,
    cols = rep(phs_colours("phs-blue"), dim(x$sens)[1]),
    add = FALSE,
    add_xy_line = TRUE,
    ...
)
```

Arguments

```
x output from getcal()
cols colour to draw lines
add set to FALSE to add to existing plot
add_xy_line set to TRUE to draw an X-Y reference line.
... passed to lines()
```

Value

No return value, draws a figure

```
# See vignette
```

24 plot.sparraROC

plot.sparraPRC

Plot function for class above

Description

Plot function for class above

Usage

```
## S3 method for class 'sparraPRC'
plot(
    x,
    addauc = FALSE,
    cols = rep(phs_colours("phs-blue"), dim(x$sens)[1]),
    ...
)
```

Arguments

```
    x output from getprc()
    addauc set to TRUE to add text to the plot showing the (mean) AUC and SE.
    cols colour to draw lines
    passed to plot()
```

Value

No return value, draws a figure

Examples

```
# See vignette
```

plot.sparraROC

Plot function for class sparraROC

Description

Plot function for class sparraROC

Usage

```
## S3 method for class 'sparraROC'
plot(
    x,
    addauc = FALSE,
    cols = rep(phs_colours("phs-blue"), dim(x$sens)[1]),
    ...
)
```

plot_decomp 25

Arguments

x output from getroc()

addauc set to TRUE to add text to the plot showing the (mean) AUC and SE.

cols colour to draw lines
... passed to plot()

Value

No return value, draws a figure

Examples

See vignette

plot_decomp plot_decomp

Description

Plots a bar graph of decomposition of FORP by cause of admission

Usage

```
plot_decomp(decomp1, decomp2, threshold, labels, inc_died = TRUE)
```

Arguments

decomp1 matrix for first group; see specification in description
decomp2 matrix for second group; see specification in description

threshold score threshold to plot (between 0 and 1)

labels labels for group 1 and group 2

inc_died set to TRUE to include a second panel showing 'death' type admissions

Details

Takes two matrices as input with the following specifications: Each matrix corresponds to one group Columns are named with the admission types to be plotted. Any admission types including the string 'Died' are counted as deaths If the matrix has N rows, these are interpreted as corresponding to N score quantiles in increasing order. The (i,j)th entry of the matrix is the number of people admitted for reason i with a score greater than or equal to (j-1)/N and less than (j/N) who are in that group

Value

Silently return ggplot object

Examples

See vignette

26 prc_2panel

| prc_2panel prc_2panel Draws a PRC curve (with legend) with a second panel underneath showing precision difference. | |
|--|--|
|--|--|

Description

prc_2panel Draws a PRC curve (with legend) with a second panel underneath showing precision difference.

Usage

```
prc_2panel(
  prcs,
  labels = names(prcs),
  col = 1:length(prcs),
  highlight = NULL,
  yrange_lower = NULL,
  legend_title = ""
)
```

Arguments

list of sparraPRC objects.

labels labels to use in legend

col line colours

highlight if non-null, draw a point at a particular cutoff

yrange_lower y range for lower plot. If NULL, generates automatically

legend_title title for legend, defaults to nothing

Value

Silently return ggplot object

```
# See vignette
```

roc_2panel 27

| roc_2panel | roc_2panel Draws a ROC curve (with legend) with a second panel underneath showing sensitivity difference. |
|------------|---|
| | |

Description

roc_2panel Draws a ROC curve (with legend) with a second panel underneath showing sensitivity difference.

Usage

```
roc_2panel(
  rocs,
  labels = names(rocs),
  col = 1:length(rocs),
  xy_col = phs_colours("phs-magenta"),
  highlight = NULL,
  yrange_lower = NULL,
  legend_title = ""
)
```

Arguments

| rocs | list of sparraROC objects |
|--------------|--|
| labels | labels to use in legend; default to names of rocs. |
| col | line colours |
| xy_col | line colour for x-y line, defaults to red |
| highlight | if non-null, add a point at this cutoff |
| yrange_lower | y range for lower plot. If NULL, generates automatically |
| legend_title | title for legend, defaults to nothing |

Value

Invisibly returns plot as ggplot object

```
# See vignette
```

28 sim_pop_data

| m_pop_data sim_pop_data |
|-------------------------|
| · · |

Description

Simulates population data with a reasonably realistic joint distribution

Usage

```
sim_pop_data(
   npop,
   coef_adjust = 4,
   offset = 1,
   vcor = NULL,
   coefs = c(2, 1, 0, 5, 3, 0, 0),
   seed = 12345,
   incl_id = TRUE,
   incl_reason = TRUE
)
```

Arguments

| npop | population size |
|-------------|--|
| coef_adjust | inverse scale for all (true) coefficients (default 4): lower means that hospital admissions are more predictable from covariates. |
| offset | offset for logistic model (default 1): higher means a lower overall prevalence of admission |
| vcor | a valid $5x5$ correlation matrix (default NULL), giving correlation between variables. If 'NULL', values roughly represents realistic data. |
| coefs | coefficients of age, male sex, non-white ethnicity, number of previous admissions, and deprivation decile on hospital admissions, Default (2,1,0,5,3). Divided through by coef_adjust. |
| seed | random seed (default 12345) |
| incl_id | include an ID column (default TRUE) |
| incl_reason | include a column indicating reason for admission. |
| | |

Details

Simulates data for a range of people for the variables

- Age (age)
- Sex (sexM; 1 if male)
- Race/ethnicity (raceNW: 1 if non-white ethnicity)
- Number of previous hospital admissions (PrevAdm)

sim_pop_data 29

• Deprivation decile (SIMD: 1 most deprived, 10 least deprived. NOTE - opposite to English IMD)

- Urban-rural residence status (urban_rural: 1 for rural)
- Mainland-island residence status (mainland_island: 1 for island)
- Hospital admission (target: 1/TRUE if admitted to hospital in year following prediction date)

Can optionally add an ID column.

Optionally includes an admission reason for samples with target=1. These admission reasons roughly correspond to the first letters of ICD10 categories, and can either correspond to an admission or death. Admission reasons are simulated with a non-constant multinomial distribution which varies across age/sex/ethnicity/urban-rural/mainland-island/PrevAdm values in a randomly- chosen way. The distributions of admission reasons are *not* however chosen to reflect real distributions, nor are systematic changes in commonality of admission types across categories intended to appear realistic.

Value

data frame with realistic values.

Examples

```
# Simulate data
dat=sim_pop_data(10000)
cor(dat[,1:7])
```

See vignette

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