# Package 'OneStep'

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Description Provide principally an eponymic function that numerically computes the Le Cam's one-step estimator for an independent and identically distributed sample. One-step estimation is asymptotically efficient (see L. Le Cam (1956) <a href="https://projecteuclid.org/euclid.bsmsp/1200501652">https://projecteuclid.org/euclid.bsmsp/1200501652</a> and can be computed faster than the maximum likelihood estimator for large observation samples, see e.g. Brouste et al. (2021) <a href="https://org/euclid.bsmsp/1200501652">doi:10.32614/RJ-2021-044</a> .
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OneStep-package One-Step Estimation

#### **Description**

Provide principally an eponymic function that numerically computes the Le Cam's one-step estimator for an independent and identically distributed sample. One-step estimation is asymptotically efficient (see L. Le Cam (1956) <a href="https://projecteuclid.org/euclid.bsmsp/1200501652">https://projecteuclid.org/euclid.bsmsp/1200501652</a>) and can be computed faster than the maximum likelihood estimator for large observation samples, see e.g. Brouste et al. (2021) <a href="https://doi.org/euclid.bsmsp/1200501652">doi:10.32614/RJ-2021-044</a>.

#### **Details**

#### The DESCRIPTION file:

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Title: One-Step Estimation

Version: 0.9.4

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other methods

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#### References

L. LeCam (1956). On the asymptotic theory of estimation and testing hypothesis. In: Proceedings of 3rd Berkeley Symposium I, pages 355-368.

# See Also

See fitdistrplus for classic MLE, MME,...

benchonestep	Performing benchmark of one-step MLE against other methods	

# Description

benchonestep performs a benchmark of one-step MLE against other methods on a given dataset. benchonestep.replicate repeats several times the procedure: data random generation and benchmark through benchonestep.

# Usage

```
benchonestep(data, distr, methods, init, weights=NULL,...)
benchonestep.replicate(nsample, nbsimu, distr, methods=NULL, echo=FALSE, ncpus=1, ...)
```

# **Arguments**

data	A numeric vector of length n
distr	A character string "name" naming a distribution for which the corresponding density function dname and the corresponding distribution function pname must be classically defined.
methods	A vector of methods: character among "mme", "mle", "onestep" (can be abbreviated).
init	A named list for the intial guess method.
weights	An optional vector of weights to be used in the fitting process. Should be NULL or a numeric vector with strictly positive integers (typically the number of occurences of each observation). If non-NULL, weighted MLE is used, otherwise ordinary MLE.
	$unused \ for \ benchone step; true \ parameters \ passed \ to \ rdistr \ for \ benchone step. \ replicate$
nsample	a numeric for the sample size.
nbsimu	a numeric for the replication number.
echo	a logical to display or not some traces of benchmarking.
ncpus	Number of processes to be used in parallel operation: typically one would fix it to the number of available CPUs.

#### Value

A matrix with estimate and time in seconds per method for benchonestep; an array with estimates, times, errors in seconds per method, per simulation for benchonestep.replicate.

#### Author(s)

Alexandre Brouste, Darel Noutsa Mieniedou, Christophe Dutang

# References

L. LeCam (1956). On the asymptotic theory of estimation and testing hypothesis. In: Proceedings of 3rd Berkeley Symposium I, pages 355-368.

#### **Examples**

```
n <- 1000
set.seed(1234)

x <- rbeta(n, 3, 2)
benchonestep(x, "beta", c("mle", "one"))</pre>
```

onestep

Executing Le Cam's one-step estimation

# **Description**

Executing Le Cam's one-step estimation based on Le Cam (1956) and Kamatani and Uchida (2015).

# Usage

```
onestep(data, distr, method, init, weights = NULL,
  keepdata = TRUE, keepdata.nb=100, control=list(), ...)
```

# Arguments

data	A numeric vector of length n
distr	A character string "name" naming a distribution for which the corresponding density function dname and the corresponding distribution function pname must be classically defined.
method	A character string coding for the fitting method: "closed formula" for explicit one-step and "numeric" for numeric computation. The default method is the "closed formula".
init	A named list for the user initial guess estimation.
weights	an optional vector of weights to compute the final likelihood. Should be NULL or a numeric vector with strictly positive integers (typically the number of occurences of each observation).

keepdata a logical. If TRUE, dataset is returned, otherwise only a sample subset is returned.

keepdata.nb When keepdata=FALSE, the length (>1) of the subset returned.

control a list of control parameters. Currently, param\_t is used when the characteris-

tic function is needed, delta is used when the subsample of size n^delta is randomly selected for the initial guess in the generic Le Cam's one step method.

... further arguments passe to mledist in case it is used.

#### **Details**

The Le Cam one-step estimation procedure is based on an initial sequence of guess estimators and a Fisher scoring step or a single Newton step on the loglikelihood function. For the user, the function onestep chooses automatically the best procedure to be used. The function OneStep presents internally several procedures depending on whether the sequence of initial guess estimators is in a closed form or not, and on whether the score and the Fisher information matrix can be elicited in a closed form. "Closed formula" distributions are treated with explicit score and Fisher information matrix (or Hessian matrix). For all other distributions, if the density function is well defined, the numerical computation (NumDeriv) of the Newton step in Le Cam's one-step is proposed with an initial sequence of guess estimators which is the sequence of maximum likelihood estimators computed on a subsample.

#### Value

onestep returns an object of class "onestep" inheriting from "fitdist" So, it is a list with the following components:

estimate the parameter estimates.

method the character string coding for the fitting method: "closed formula" for closed-

form MLE or closed-form one-step, "numeric" for numeric computation of the

one-step estimation.

sd the estimated standard errors, NA if numerically not computable or NULL if not

available.

cor the estimated correlation matrix, NA if numerically not computable or NULL if

not available.

vcov the estimated variance-covariance matrix, NULL if not available.

loglik the log-likelihood.

aic the Akaike information criterion.

bic the the so-called BIC or SBC (Schwarz Bayesian criterion).

n the length of the data set.

data the data set.

distname the name of the distribution.

dots the list of further arguments passed in ... to be used .

convergence an integer code for the convergence: 0 indicates successful convergence (from

explicit formula or not). 10 indicates an error.

discrete the input argument or the automatic definition by the function to be passed to

functions gofstat, plotdist and cdfcomp.

weights the vector of weights used in the estimation process or NULL.

nbstep the number of Newton step, 0 for closed-form MLE, 1 for one-step estimators

and 2 for two-step estimators.

delta delta parameter (used for sub-sample guess estimator).

Generic functions inheriting from "fitdist" objects:

print The print of a "onestep" object shows few traces about the fitting method and the fitted distribution.

summary The summary provides the parameter estimates of the fitted distribution, the log-likelihood, AIC and BIC statistics and when the maximum likelihood is used, the standard errors of the parameter estimates and the correlation matrix between parameter estimates.

plot The plot of an object of class "onestep" returned by fitdist uses the function plotdist. An object of class "onestep" or a list of objects of class "onestep" corresponding to various fits using the same data set may also be plotted using a cdf plot (function cdfcomp), a density plot(function denscomp), a density Q-Q plot (function qqcomp), or a P-P plot (function ppcomp).

logLik Extracts the estimated log-likelihood from the "onestep" object.

vcov Extracts the estimated var-covariance matrix from the "onestep" object.

coef Extracts the fitted coefficients from the "onestep" object.

# Author(s)

Alexandre Brouste, Christophe Dutang, Darel Noutsa Mieniedou

#### References

- L. Le Cam (1956). *On the asymptotic theory of estimation and testing hypothesis*, In: Proceedings of 3rd Berkeley Symposium I, 355-368.
- I.A. Koutrouvelis (1982). Estimation of Location and Scale in Cauchy Distributions Using the Empirical Characteristic Function, Biometrika, 69(1), 205-213.
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- K. Kamatani and M. Uchida (2015). *Hybrid multi-step estimators for stochastic differential equations based on sampled data*, Stat Inference Stoch Process, 18(2), 177-204.
- Z.-S. Ye and N. Chen (2017). *Closed-Form Estimators for the Gamma Distribution Derived From Likelihood Equations*, The American Statistician, 71(2), 177-181.

#### See Also

See Also as mledist and fitdist in fitdistrplus.

#### **Examples**

```
n <- 1000
set.seed(1234)
##1. Gamma
theta \leftarrow c(2, 3)
o.sample <- rgamma(n, shape=theta[1], rate=theta[2])</pre>
#Default method
onestep(o.sample, "gamma")
#User initial sequence of guess estimator
# See : Ye and Chen (2017)
qtmp <- sum(o.sample*log(o.sample))-sum(log(o.sample))*mean(o.sample)</pre>
alphastar <- sum(o.sample)/qtmp</pre>
betastar <- qtmp/length(o.sample)</pre>
thetastar <- list(shape=alphastar,rate=1/betastar)</pre>
onestep(o.sample, "gamma", init=thetastar)
#Numerical method (for comparison)
onestep(o.sample, "gamma", method="numeric")
##2.Beta
theta <- c(0.5, 1.5)
o.sample <- rbeta(n, shape1=theta[1], shape2=theta[2])</pre>
onestep(o.sample, "beta")
##3. Cauchy
theta \leftarrow c(2, 3)
o.sample <- rcauchy(n, location=theta[1], scale=theta[2])</pre>
onestep(o.sample, "cauchy")
#User initial sequence of guess estimator
#See Koutrouvelis (1982).
t < -1/4
Phi <- mean(exp(1i*t*o.sample))
S <- Re(Phi)
Z <- Im(Phi)</pre>
thetastar <- list(location=atan(Z/S)/t,scale=-log(sqrt(S^2+Z^2))/t)</pre>
onestep(o.sample, "cauchy", init=thetastar)
##Chi2
theta <- 5
o.sample <- rchisq(n,df=theta)</pre>
```

```
onestep(o.sample, "chisq")
#User initial sequence of guess estimator
#See Grenander (1965).
p <- n^{(2/7)}
k \leftarrow floor(n^{3/5})
Dstar <- sort(o.sample)</pre>
Dk1 <- Dstar[(1+k):n]</pre>
Dk2 <- Dstar[1:(n-k)]</pre>
sigma.star <- 1/2*sum((Dk1+Dk2)*(Dk1-Dk2)^(-p))/sum((Dk1-Dk2)^(-p))+2
onestep(o.sample, "chisq", init=list(df=sigma.star))
#Negative Binomial
theta \leftarrow c(1, 5)
o.sample <- rnbinom(n, size=theta[1], mu=theta[2])</pre>
onestep(o.sample, "nbinom")
#Generic (dweibull2)
theta <- c(0.8, 3)
dweibull2 <- function(x, shape, scale, log=FALSE)</pre>
  dweibull(x = x, shape = shape, scale = scale, log = log)
o.sample <- rweibull(n, shape = theta[1], scale = 1/theta[2])
onestep(o.sample, "weibull2", method="numeric",
  init=list(shape=1, scale=1))
```

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