We constructed a Least squares hit for the Monke Carlo momerical integration error in lap-log scale. Below is a brief description about constructing least squares hits oster both, Linear scale and Log-Log scale.

Linear Least squares regression

Suppose that we wish to lit a linear function of = a + b x to some date (xe, y,),..., (xn, yn). This yields a (typically overdetermined) Linear system of equations

We can find a linear list of a a + bx satisfying

by solving a and b from the normal equation

Least squares approximation for power Enctions

Suppose that we wish to fit of = axt to some data (xe, y,),..., (xa, ya).

The "standard" way is to linearise the model by taking the logarithm on both sides:

This can now be expressed as the system

$$\begin{bmatrix} log \gamma_1 \\ \vdots \\ log \gamma_n \end{bmatrix} = \begin{bmatrix} 1 & log x_1 \\ \vdots & \vdots \\ 1 & log x_n \end{bmatrix} \begin{bmatrix} log a \end{bmatrix}$$

and we can find the lit by using ordinary linear least squares, i.e., solving the normal equation

On error plots

- If the date satisfies a power law of = axb, then it is typical to represent it using a lay-lay plat. The rate of decay b will then be the slope of the data represented in lay-lay scale.
- . It the data setisties an exponential law of = Ce of x, then it is typical to represent it using a semi-log plot (i.e., the x-axis is linear, but the of-axis is logarithmic). The slope of a data set which appears linear in semi-log scale is related to of.