

QMM_Assignment_2

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2024-09-22

```
library(lpSolve)
```

```
## Warning: package 'lpSolve' was built under R version 4.3.3
```

```
A12 <- matrix(c(20,900,420,15,1200,360,12,750,300), nrow = 3, ncol = 3, byrow = TRUE)
colnames(A12) <- (c('Space_Req', 'Sales Forecast(PerDay)', 'Profit'))
rownames(A12) <- (c('Large', 'Medium', 'Small'))
A12
```

```
##           Space_Req Sales Forecast(PerDay) Profit
## Large           20              900         420
## Medium          15             1200         360
## Small           12              750         300
```

```
A12 = matrix(c(750,900,450), nrow = 3, ncol = 1, byrow = TRUE)
colnames(A12)=(c('Excess Capacity'))
rownames(A12)=(c('Plant1', 'Plant2', 'Plant3'))
A12
```

```
##           Excess Capacity
## Plant1              750
## Plant2              900
## Plant3              450
```

Let L_1 , M_1 , S_1 = Number of large, medium, and small units produced at Plant 1
 L_2 , M_2 , S_2 = Number of large, medium, and small units produced at Plant 2
 L_3 , M_3 , S_3 = Number of large, medium, and small units produced at Plant 3

The objective function is

$$\text{Max } Z = 420(L_1 + L_2 + L_3) + 360(M_1 + M_2 + M_3) + 300(S_1 + S_2 + S_3)$$

Rearranging this, the objective becomes

$$\text{Max } Z = 420L_1 + 360M_1 + 300S_1 + 420L_2 + 360M_2 + 300S_2 + 420L_3 + 360M_3 + 300S_3$$

subject to the following constraints.,

Production Capacity Constraints:

$$L1 + M1 + S1 \leq 750$$

$$L2 + M2 + S2 \leq 900$$

$$L3 + M3 + S3 \leq 450$$

Storage Space Constraints:

$$20L1 + 15M1 + 12S1 \leq 13000$$

$$20L2 + 15M2 + 12S2 \leq 12000$$

$$20L3 + 15M3 + 12S3 \leq 5000$$

Sales Forecast Constraints:

$$L1 + L2 + L3 \leq 900$$

$$M1 + M2 + M3 \leq 1200$$

$$S1 + S2 + S3 \leq 750$$

Capacity Usage Equality:

$$(L1 + M1 + S1) * (100/750) = (L2 + M2 + S2) * (100/900) = (L3 + M3 + S3) * (100/450)$$

Non negativity constraints:

$$L1, L2, L3, M1, M2, M3, S1, S2, S3 \geq 0$$

#Objective Function

Object <- c(420, 360, 300, 420, 360, 300, 420, 360, 300)

#Constraints

```

Cnstrants  <- matrix(c(

  # Production capacity
  1, 1, 1, 0, 0, 0, 0, 0, 0, # Plant 1
  0, 0, 0, 1, 1, 1, 0, 0, 0, # Plant 2
  0, 0, 0, 0, 0, 0, 1, 1, 1, # Plant 3

  # Storage
  20, 15, 12, 0, 0, 0, 0, 0, 0, # Plant 1
  0, 0, 0, 20, 15, 12, 0, 0, 0, # Plant 2
  0, 0, 0, 0, 0, 0, 20, 15, 12, # Plant 3

  # Sales forecast
  1, 0, 0, 1, 0, 0, 1, 0, 0, # Large units
  0, 1, 0, 0, 1, 0, 0, 1, 0, # Medium units
  0, 0, 1, 0, 0, 1, 0, 0, 1, # Small units

  6, 6, 6, -5, -5, -5, 0, 0, 0,
  0, 0, 0, 1, 1, 1, -2, -2, -2,
  3, 3, 3, 0, 0, 0, -5, -5, -5

), nrow=12, byrow=TRUE)
Cnstrants

```

```

##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
## [1,]    1    1    1    0    0    0    0    0    0
## [2,]    0    0    0    1    1    1    0    0    0
## [3,]    0    0    0    0    0    0    1    1    1
## [4,]   20   15   12    0    0    0    0    0    0
## [5,]    0    0    0   20   15   12    0    0    0
## [6,]    0    0    0    0    0    0   20   15   12
## [7,]    1    0    0    1    0    0    1    0    0
## [8,]    0    1    0    0    1    0    0    1    0
## [9,]    0    0    1    0    0    1    0    0    1
## [10,]   6    6    6   -5   -5   -5    0    0    0
## [11,]    0    0    0    1    1    1   -2   -2   -2
## [12,]    3    3    3    0    0    0   -5   -5   -5

```

#Define the constraint direction

```

Direct<-c("<=","<=","<=","<=","<=","<=","<=","<=","<=","=","=","=")
Direct

```

```

## [1] "<=" "<=" "<=" "<=" "<=" "<=" "<=" "<=" "<=" "=" "=" "="

```

RHS of the constraints

```

RHS <- c(750, 900, 450, 13000, 12000, 5000, 900, 1200, 750, 0, 0, 0)
RHS

```

```
## [1] 750 900 450 13000 12000 5000 900 1200 750 0 0 0
```

```
#Solve the linear programming problem  
linear_prog_result <-lp("max", Object, Cnstrants, Direct, RHS)  
linear_prog_result
```

```
## Success: the objective function is 696000
```

```
#Values of decision variables  
linear_prog_result$solution
```

```
## [1] 516.6667 177.7778 0.0000 0.0000 666.6667 166.6667 0.0000 0.0000  
## [9] 416.6667
```