

Weightl Corporation Problem – Assignment 3

Formulating Objective function and Constraints from the Problem:

Given,

Net profit per product;

Large = \$420

Medium = \$360

Small = \$300

Excess production capacity;

Plant 1 = 750

Plant 2 = 900

Plant 3 = 450

Available storage space;

Plant 1 = 13000 sq. ft

Plant 2 = 12000 sq. ft

Plant 3 = 5000 sq. ft

Storage space used per unit;

Large = 20 sq. ft

Medium = 15 sq. ft

Small = 12 sq. ft

Sales of each size product per day;

Large = 900

Medium = 1200

Small = 750

Let,

L1 = Large product produced in plant 1

L2 = Large product produced in plant 2

L3 = Large product produced in plant 3

M1= Medium product produced in plant 1

M2 = Medium product produced in plant 2

M3 = Medium product produced in plant 3

S1 = Small product produced in plant 1

S2 = Small product produced in plant 2

S3 = Small product produced in plant 3

WeightIt Corporation Problem – Assignment 3

Based on above information and assumptions, the objective function for the problem is as below,

$$\text{Max: } 420(L1 + L2 + L3) + 360(M1 + M2 + M3) + 300(S1 + S2 + S3)$$

OR Max: $420 L1 + 360 M1 + 300 S1 + 420 L2 + 360 M2 + 300 S2 + 420 L3 + 360 M3 + 300 S3$

Where,

Capacity $L1 + M1 + S1 \leq 750$

$$L2 + M2 + S2 \leq 900$$

$$L3 + M3 + S3 \leq 450$$

Storage $20L1 + 15M1 + 12S1 \leq 13000$

$$20L2 + 15M2 + 12S2 \leq 12000$$

$$20L3 + 15M3 + 12S3 \leq 5000$$

Sales $L1 + L2 + L3 \leq 900$

$$M1 + M2 + M3 \leq 1200$$

$$S1 + S2 + S3 \leq 750$$

Percentage $\frac{1}{750}(L1 + M1 + S1) - \frac{1}{900}(L2 + M2 + S2) = 0$

$$\frac{1}{750}(L1 + M1 + S1) - \frac{1}{450}(L3 + M3 + S3) = 0$$

OR

$$900 L1 + 900 M1 + 900 S1 - 750 L2 - 750 M2 - 750 S2 = 0;$$

$$450 L1 + 450 M1 + 450 S1 - 750 L3 - 750 M3 - 750 S3 = 0;$$

$$L1, L2, L3, M1, M2, M3, S1, S2, S3 \geq 0$$

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Dual Function for the LP Problem:

The Dual Form of the above problem is as follows;

$$\text{Min : } 750y_1 + 900y_2 + 450y_3 + 13000y_4 + 12000y_5 + 5000y_6 + 900y_7 + 1200y_8 + 750y_9$$

Where,

$$y_1 + 20y_4 + y_7 + 900y_{10} + 450y_{11} \geq 420$$

$$y_1 + 15y_4 + y_8 + 900y_{10} + 450y_{11} \geq 360$$

$$y_1 + 12y_4 + y_9 + 900y_{10} + 450y_{11} \geq 300$$

$$y_2 + 20y_5 + y_7 - 750y_{10} \geq 420$$

$$y_2 + 15y_5 + y_8 - 750y_{10} \geq 360$$

$$y_2 + 12y_5 + y_9 - 750y_{10} \geq 300$$

$$y_3 + 20y_6 + y_7 - 750y_{11} \geq 420$$

$$y_3 + 15y_6 + y_8 - 750y_{11} \geq 360$$

$$y_3 + 12y_6 + y_9 - 750y_{11} \geq 300$$