

# Multi-Stage Rocket Optimization Analysis

Stage\_Opt Analysis Report

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## 1 Introduction

This report presents a comprehensive analysis of multi-stage rocket optimization using various state-of-the-art optimization algorithms. The optimization process aims to maximize payload capacity by finding optimal stage configurations while satisfying various constraints including total delta-v requirements and structural mass ratios Kumar et al. [2013].

Our approach incorporates multiple optimization techniques from recent literature Silva et al. [2022], Wang et al. [2021]:

- **Particle Swarm Optimization (PSO)**: Based on the work of Kumar et al. [2013], this method simulates the collective behavior of particle swarms to explore the solution space effectively. Recent applications in micro-launch vehicles Andrews and Hall [2012] have demonstrated its effectiveness in rocket trajectory optimization.
- **Differential Evolution (DE)**: Following the methodology presented by Wang et al. [2021], this algorithm employs vector differences for mutation operations, making it particularly effective for handling the multi-constraint nature of rocket stage optimization.
- **Genetic Algorithm (GA)**: Inspired by evolutionary processes and implemented following principles from Silva et al. [2022], this method uses selection, crossover, and mutation operators to evolve optimal solutions. We include both standard and adaptive variants to enhance exploration capabilities.
- **Basin-Hopping**: A hybrid global optimization technique that combines local optimization with Monte Carlo sampling, effective for problems with multiple local optima Andrews and Hall [2012].

- **Sequential Least Squares Programming (SLSQP)**: A gradient-based optimization method for constrained nonlinear problems, particularly useful for fine-tuning solutions in smooth regions of the search space Wang et al. [2021].

## 2 Problem Formulation

The optimization problem involves finding the optimal distribution of total delta-v ( $\Delta V$ ) across multiple stages while considering:

- Structural coefficients ( $\epsilon$ ) for each stage
- Specific impulse (ISP) variations between stages
- Mass ratio constraints Silva et al. [2022]
- Total delta-v requirement Kumar et al. [2013]

## 3 Methodology

Each optimization method was implemented with specific adaptations for rocket stage optimization Wang et al. [2021]:

### 3.1 Particle Swarm Optimization

Following Kumar et al. [2013], our PSO implementation uses adaptive inertia weights and local topology to balance exploration and exploitation. The algorithm has shown particular effectiveness in handling the nonlinear constraints of rocket trajectory optimization Andrews and Hall [2012].

### 3.2 Differential Evolution

Based on the approach outlined in Wang et al. [2021], our DE implementation uses adaptive mutation rates and crossover operators specifically tuned for multi-stage rocket optimization. The algorithm effectively handles the coupling between stage configurations and overall system performance.

### 3.3 Genetic Algorithm

Implementing concepts from Silva et al. [2022], our GA variants use specialized crossover and mutation operators that maintain the feasibility of

solutions while exploring the design space effectively. The adaptive version dynamically adjusts population size and genetic operators based on solution diversity and convergence behavior.

## 4 Results and Analysis

The following methods were evaluated, sorted by their achieved payload ratio Kumar et al. [2013]:

Table 1: Optimization Methods Performance Comparison

Method	Payload Ratio	$\lambda_1$	$\lambda_2$
DE	0.0788		
PSO	0.0788		
ADAPTIVE-GA	0.0781		
GA	0.0665		
BASIN-HOPPING	0.0437		
SLSQP	0.0437		

## 5 Stage Configuration Analysis

The following configurations were found for each method:

- DE
- PSO
- ADAPTIVE-GA
- GA
- BASIN-HOPPING
- SLSQP

## 6 Conclusion

The optimization analysis revealed that DE achieved the best payload ratio of 0.0788. This result demonstrates the effectiveness of modern optimization techniques in solving complex rocket design problems.

The comparative analysis shows that different algorithms exhibit varying strengths:

- PSO excels in handling the nonlinear nature of the problem Kumar et al. [2013]
- DE shows robust performance in maintaining constraint feasibility Wang et al. [2021]
- Evolutionary approaches provide good exploration of the design space Silva et al. [2022]

These results provide valuable insights for future rocket design optimization studies and highlight the importance of choosing appropriate optimization methods for specific design challenges.

## References

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