



Unit 7

Predictive Parsing

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Top Down Parsing Methods

- Simplest method is a full-backup *recursive descent* parse
- Write recursive recognizers (subroutines) for each grammar rule
 - If rule succeeds perform some action (i.e., build a tree node, emit code, etc.)
 - If rule fails, return failure. Caller may try another choice or fail
 - On failure it “backs up” which might have problem if it needs to return a lexical symbol to the input stream



Problems

- Also remember left recursion problem
- Need to backtrack , suppose that you could always tell what production applied by looking at one (or more) tokens of lookahead – called predictive parsing
- Factoring



Summary of Recursive Descent

- Simple and general parsing strategy usually coupled with simple handcrafted lexer
 - Left-recursion must be eliminated first
 - ... but that can be done automatically
- Unpopular because of backtracking
 - Thought to be too inefficient
- In practice, backtracking is eliminated by restricting the grammar



Elimination of Immediate Left Recursion

$$A \rightarrow A \alpha_1 \mid A \alpha_2 \mid \dots A \alpha_m \mid \beta_1 \mid \beta_2 \mid \beta_n$$

$$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \beta_n A'$$

$$A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \alpha_m A' \mid \varepsilon$$



Predictive Parsers

- Like recursive-descent but parser can “predict” which production to use
 - By looking at the next few tokens
 - No backtracking
- Predictive parsers accept LL(k) grammars
 - L means “left-to-right” scan of input
 - L means “leftmost derivation”
 - k means “predict based on k tokens of lookahead”
- In practice, LL(1) is used



LL(1) Languages

- In recursive-descent, for each non-terminal and input token there may be a choice of production
- LL(1) means that for each non-terminal and token there is only one production
- Can be specified via 2D tables
 - One dimension for current non-terminal to expand
 - One dimension for next token
 - A table entry contains one production



Predictive Parsing and Left Factoring

- Recall the grammar

$$E \rightarrow T + E \mid T$$
$$T \rightarrow \text{int} \mid \text{int} * T \mid (E)$$

- Hard to predict because
 - For T two productions start with int
 - For E it is not clear how to predict
- A grammar must be left-factored before use for predictive parsing

Left-Factoring Example

- Consider the grammar

$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} \mid \text{int} * T \mid (E)$$

- Factor out common prefixes of productions

$$E \rightarrow T X$$

$$X \rightarrow + E \mid \varepsilon$$

$$T \rightarrow (E) \mid \text{int} Y$$

$$Y \rightarrow * T \mid \varepsilon$$

LL(1) Parsing Table Example

- Left-factored grammar

$$E \rightarrow T X$$

$$X \rightarrow + E \mid \varepsilon$$

$$T \rightarrow (E) \mid \text{int } Y$$

$$Y \rightarrow * T \mid \varepsilon$$

- The LL(1) parsing table:

	int	*	+	()	\$
E	$T X$			$T X$		
X			$+ E$		ε	ε
T	$\text{int } Y$			(E)		
Y		$* T$	ε		ε	ε



LL(1) Parsing Table Example (Cont.)

- Consider the $[E, \text{int}]$ entry
 - “When current non-terminal is E and next input is int , use production $E \rightarrow T X$ ”
 - This production can generate an int in the first place
- Consider the $[Y, +]$ entry
 - “When current non-terminal is Y and current token is $+$, get rid of Y ”
 - Y can be followed by $+$ only in a derivation in which $Y \rightarrow \varepsilon$



LL(1) Parsing Tables. Errors

- Blank entries indicate error situations
 - Consider the $[E, *]$ entry
 - “There is no way to derive a string starting with $*$ from non-terminal E ”



Using Parsing Tables

- Method similar to recursive descent, except
 - For each non-terminal S
 - We look at the next token a
 - And chose the production shown at $[S,a]$
- We use a stack to keep track of pending non-terminals
- We reject when we encounter an error state
- We accept when we encounter end-of-input



LL(1) Parsing Algorithm

```
initialize stack = <S $> and next
repeat
  case stack of
    <X, rest> : if T[X, *next] = Y1...Yn
                  then stack ← <Y1... Yn rest>;
                  else error ();
    <t, rest>  : if t == *next ++
                  then stack ← <rest>;
                  else error ();
until stack == < >
```

LL(1) Parsing Example

Stack	Input	Action
E \$	int * int \$	T X
T X \$	int * int \$	int Y
int Y X \$	int * int \$	terminal
Y X \$	* int \$	* T
* T X \$	* int \$	terminal
T X \$	int \$	int Y
int Y X \$	int \$	terminal
Y X \$	\$	ϵ
X \$	\$	ϵ
\$	\$	ACCEPT



Constructing Parsing Tables

- LL(1) languages are those defined by a parsing table for the LL(1) algorithm
- No table entry can be multiply defined
- We want to generate parsing tables from CFG



Constructing Parsing Tables (Cont.)

- If $A \rightarrow \alpha$, where in the line of A we place α ?
- In the column of t where t can start a string derived from α
 - $\alpha \rightarrow^* t \beta$
 - We say that $t \in \text{First}(\alpha)$
- In the column of t if α is ε and t can follow an A
 - $S \rightarrow^* \beta A t \delta$
 - We say $t \in \text{Follow}(A)$



Computing First Sets

Definition: $\text{First}(X) = \{ t \mid X \rightarrow^* t\alpha \} \cup \{ \varepsilon \mid X \rightarrow^* \varepsilon \}$

Algorithm sketch (see book for details):

1. for all terminals t do $\text{First}(X) \leftarrow \{ t \}$
2. for each production $X \rightarrow \varepsilon$ do $\text{First}(X) \leftarrow \{ \varepsilon \}$
3. if $X \rightarrow A_1 \dots A_n \alpha$ and $\varepsilon \in \text{First}(A_i)$, $1 \leq i \leq n$ do
 - add $\text{First}(\alpha)$ to $\text{First}(X)$
4. for each $X \rightarrow A_1 \dots A_n$ s.t. $\varepsilon \in \text{First}(A_i)$, $1 \leq i \leq n$ do
 - add ε to $\text{First}(X)$
5. repeat steps 4 & 5 until no First set can be grown

First Sets. Example

- Recall the grammar

$$E \rightarrow T X$$

$$T \rightarrow (E) \mid \text{int } Y$$

$$X \rightarrow + E \mid \varepsilon$$

$$Y \rightarrow * T \mid \varepsilon$$

- First sets

$$\text{First}(()) = \{ (\}$$

$$\text{First}()) = \{) \}$$

$$\text{First}(\text{int}) = \{ \text{int} \}$$

$$\text{First}(+) = \{ + \}$$

$$\text{First}(*) = \{ * \}$$

$$\text{First}(T) = \{ \text{int}, (\}$$

$$\text{First}(E) = \{ \text{int}, (\}$$

$$\text{First}(X) = \{ +, \varepsilon \}$$

$$\text{First}(Y) = \{ *, \varepsilon \}$$



Computing Follow Sets

■ Definition:

$$\text{Follow}(X) = \{ t \mid S \rightarrow^* \beta X t \delta \}$$

■ Intuition

- If S is the start symbol then $\$ \in \text{Follow}(S)$
- If $X \rightarrow A B$ then $\text{First}(B) \subseteq \text{Follow}(A)$ and
 $\text{Follow}(X) \subseteq \text{Follow}(B)$
- Also if $B \rightarrow^* \varepsilon$ then $\text{Follow}(X) \subseteq \text{Follow}(A)$



Computing Follow Sets (Cont.)

Algorithm sketch:

1. $\text{Follow}(S) \leftarrow \{ \$ \}$
 2. For each production $A \rightarrow \alpha X \beta$
 - add $\text{First}(\beta) - \{\epsilon\}$ to $\text{Follow}(X)$
 3. For each $A \rightarrow \alpha X \beta$ where $\epsilon \in \text{First}(\beta)$
 - add $\text{Follow}(A)$ to $\text{Follow}(X)$
- repeat step(s) ____ until no Follow set grows

Follow Sets. Example

- Recall the grammar

$$E \rightarrow T X$$

$$T \rightarrow (E) \mid \text{int } Y$$

$$X \rightarrow + E \mid \varepsilon$$

$$Y \rightarrow * T \mid \varepsilon$$

- Follow sets

$$\text{Follow}(+) = \{ \text{int}, (\}$$

$$\text{Follow}(*) = \{ \text{int}, (\}$$

$$\text{Follow}(() = \{ \text{int}, (\}$$

$$\text{Follow}(E) = \{), \$ \}$$

$$\text{Follow}(X) = \{ \$,) \}$$

$$\text{Follow}(T) = \{ +,) , \$ \}$$

$$\text{Follow}()) = \{ +,) , \$ \}$$


$$\text{Follow}(Y) = \{ +,) , \$ \}$$

$$\text{Follow}(\text{int}) = \{ *, +,) , \$ \}$$



Constructing LL(1) Parsing Tables

- Construct a parsing table T for CFG G
- For each production $A \rightarrow \alpha$ in G do:
 - For each terminal $t \in \text{First}(\alpha)$ do
 - $T[A, t] = \alpha$
 - If $\varepsilon \in \text{First}(\alpha)$, for each $t \in \text{Follow}(A)$ do
 - $T[A, t] = \alpha$
 - If $\varepsilon \in \text{First}(\alpha)$ and $\$ \in \text{Follow}(A)$ do
 - $T[A, \$] = \alpha$



Notes on LL(1) Parsing Tables

- If any entry is multiply defined then G is not LL(1)
 - If G is ambiguous
 - If G is left recursive
 - If G is not left-factored
- Most programming language grammars are not LL(1)
- There are tools that build LL(1) tables