

1.

Trans.lp

```
/* Objective function */
```

```
min: 600 W11 + 600 W12 + 600 W13 + 625 W21 + 625 W22 + 625 W23 + 22 W12 + 14  
W12 + 30 W13 + 16 W21 + 20 W22 + 24 W23 ;
```

```
/* Demand Constraints */
```

```
W11 + W21 >= 80;
```

```
W12 + W22 >= 60;
```

```
W13 + W23 >= 70;
```

```
/* Production Constraints */
```

```
W11 + W12 + W13 <= 100;
```

```
W21 + W22 + W23 <= 120;
```

.Rmd

Untitled

Load the Constraint data

```
#install.packages("lpSolveAPI")  
library(lpSolveAPI)  
lprec <- read.lp("Trans.lp")
```

Build and Solve the model

The solution implies that the minimum optimum cost is 131750 and warehouse 1 , warehouse 3 should be shipped 80 and 20 units respectively from Plant 1. Similarly , 60 and 50 units to warehouse 2 and 3 respectively from Plant 2 (We will be producing 10 units less than the capacity).

```
solve(lprec)
## [1] 0
get.objective(lprec)
## [1] 131750
get.variables(lprec)
## [1] 80 0 20 0 60 50
get.constraints(lprec)
## [1] 80 60 70 100 110
```

2.

i.) Formulation

From the given info we see that total supply is 276 (93+88+95), whereas, the demand is 284 (30+57+48+91+58). That means company can't meet the demand with the existing setup.

$W_{ij} \geq 0$: where $i = A, B, C$ for pumps, $j = 1, 2, 3$ for wells, and $R1$ to 5 are refineries

$$\begin{aligned} Z_{\min} = & 1.52 W_{1A} + 1.60 W_{1B} + 1.40 W_{1C} + 1.70 W_{2A} + 1.63 W_{2B} + 1.55 W_{2C} + 1.45 W_{3A} + \\ & 1.57 W_{3B} + 1.30 W_{3C} + 5.15 W_{AR1} + 5.12 W_{BR1} + 5.32 W_{CR1} + 5.69 W_{AR2} + 5.47 W_{BR2} + 6.16 \\ & W_{CR2} + 6.13 W_{AR3} + 6.05 W_{BR3} + 6.25 W_{CR3} + 5.63 W_{AR4} + 6.12 W_{BR4} + 6.17 W_{CR4} + 5.80 \\ & W_{AR5} + 5.71 W_{BR5} + 5.87 W_{CR5} \end{aligned}$$

Constraints (Supply)

$$W_{1A} + W_{1B} + W_{1C} \leq 93$$

$$W_{2A} + W_{2B} + W_{2C} \leq 88$$

$$W_{3A} + W_{3B} + W_{3C} \leq 95$$

Constraints (Pumps to Refinery)

$$W_{1A} + W_{2A} + W_{3A} = W_{AR1} + W_{AR2} + W_{AR3} + W_{AR4} + W_{AR5}$$

$$W_{1B} + W_{2B} + W_{3B} = W_{BR1} + W_{BR2} + W_{BR3} + W_{BR4} + W_{BR5}$$

$$W_{1C} + W_{2C} + W_{3C} = W_{CR1} + W_{CR2} + W_{CR3} + W_{CR4} + W_{CR5}$$

Constraints (Demand)

$$W_{AR1} + W_{BR1} + W_{CR1} = 30$$

$$W_{AR2} + W_{BR2} + W_{CR2} = 57$$

$$W_{AR3} + W_{BR3} + W_{CR3} = 48$$

$$W_{AR4} + W_{BR4} + W_{CR4} = 91$$

$$W_{AR5} + W_{BR5} + W_{CR5} = 48$$

ii.) Network Diagram

W stands for well P for Pump and R for refinery

