

Skip list

Okay! Let's explain this in a very simple way.

This is about a Skiplist – a special data structure that works like a linked list + shortcuts for faster search.

✔ What is a Skiplist?

- Imagine a normal sorted linked list → slow search because you go one by one.
- Skiplist adds extra "fast lanes" (levels) so you can skip multiple nodes at once.
- Each node can appear on 1 or more levels randomly.

So operations like search, add, erase become $O(\log n)$ instead of $O(n)$.

✔ Step-by-step what's happening

We start with an empty Skiplist.

1 skiplist.add(1)

- Add 1 to the list
- It's inserted at some random levels (maybe level 1, maybe higher)

Now skiplist has:

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1

2 skiplist.add(2)

- Add 2
- Also placed at random levels (but always after 1, because it's sorted)

Now:

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1 2

3 skiplist.add(3)

- Add 3
- Goes after 2

Now:

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1 2 3

4 skiplist.search(0) False

- Search for 0
- Traverse skiplist, but $0 < 1$, so not found → returns False

5 skiplist.add(4)

- Add 4
- Goes after 3

Now:

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1 2 3 4

6 skiplist.search(1) True

- Search for 1
- Found in skiplist → returns True

7 skiplist.erase(2) True


- Removes 2 from all levels

- After erase:

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1 3 4

- Returns True because it existed and got removed.

 skiplist.search(2) False

- Search for 2
- Not found anymore (we erased it) → returns False

So the final Skiplist

After all operations:

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1 3 4

- 0 never existed
- 2 was erased
- 1, 3, 4 remain



Why random levels?

Each node randomly decides how many levels it appears on.

- Higher levels = fewer nodes = fast jumps
- Lower levels = all nodes = exact order

So you get logarithmic search speed similar to a balanced BST but easier to implement.

Would you like me to:

-  Draw a visual skiplist with multiple levels showing how 2 gets erased?
-  Or give a real-world analogy (like express lanes on a highway)?

Got it! Let's explain how adding works in a Skiplist with a simple example.

✓ Current Skiplist

Right now it contains sorted numbers:

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```
30 40 50 60 70 90
```

Since it's a Skiplist, it's not just a single linked list — it has multiple levels:

pgsqlCopyEdit

```
Level 3:  30 ----- 60 ----- 90
Level 2:  30 ----- 50 ----- 70 ----- 90
Level 1: 30  40  50  60  70  90
```

(Higher levels have fewer "express" nodes; Level 1 has all nodes.)

✓ We want to add 80 and 45

Let's insert them one by one.

1 Adding 80

- Skiplist is sorted, so 80 should go between 70 and 90.

Steps:

1. Start from the top level, move forward until just before 90.
2. Drop down a level and do the same.
3. Finally, at level 1, insert `80` before `90` .

So now the bottom level is:

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```
30 40 50 60 70 80 90
```

- Random levels will decide if `80` also appears in level 2 or 3 (like a coin toss).
Maybe:

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```
Level 3:  30 ----- 60 ----- 90
Level 2:  30 ----- 50 ----- 70 ----- 80 ----- 90
```

Level 1: 30 40 50 60 70 80 90

2 Adding 45

- Should go between 40 and 50.

Steps:

1. Start at the top level, move past 30 and 40 , stop before 50 .
2. Drop down, do the same.
3. Insert 45 before 50 at level 1.

Now the bottom level is:

30 40 45 50 60 70 80 90

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Again, random levels decide if it appears in higher levels. Maybe:

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Level 3: 30 ----- 60 ----- 90
Level 2: 30 ----- 50 ----- 70 ----- 80 ----- 90
Level 1: 30 40 45 50 60 70 80 90

Or it could also appear on level 2 if the randomization allows:

pgsql

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Level 2: 30 --- 45 --- 50 --- 70 --- 80 --- 90

✓ Final Skiplist after insertion

Now it has:

30 40 45 50 60 70 80 90

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And its higher levels still keep shortcuts for faster search.

✓ Key idea

- Search for where the new value fits (like binary search in a layered linked list).

- Insert it in the correct position at level 1.
- Randomly promote it to higher levels.

That's why Skiplist stays balanced on average.

Would you like me to draw a visual diagram with multiple levels showing BEFORE and AFTER inserting 80 & 45? Or also explain how the random coin toss promotion works?