

The Boolean Satisfiability (SAT) Problem, SAT Solver Technology, and Equivalence Verification

Priyank Kalla



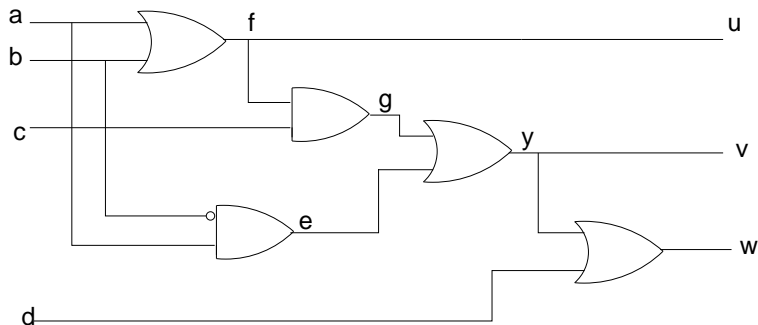
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What is Boolean Satisfiability (SAT)?

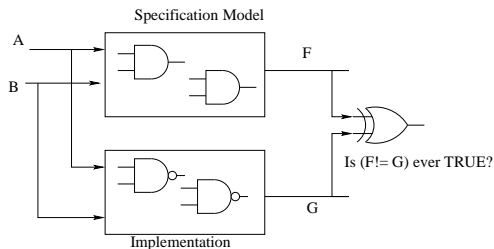
- Given a Boolean formula $f(x_1, \dots, x_n)$, find an assignment to x_1, \dots, x_n s.t. $f = 1$
- Otherwise, prove that such an assignment does not exist: problem is infeasible!
- There may be many SAT assignments: find an assignment, or enumerate all assignments (ALL-SAT)
- The formula f is given in **conjunctive normal form** (CNF), SAT solvers operate CNF representation of f
- Any decidable decision problem can be formulated and solved as SAT
- SAT is fundamental, has wide applications in many areas: hardware & software verification, graph theory, combinatorial optimization, artificial intelligence, VLSI design automation, cryptography/cryptanalysis, planning, scheduling, many more....

- Simulation vector generation: Given the circuit below, find an assignment to primary inputs s.t. $u = 1, v = 1, w = 0$, or prove that one does not exist
- Translate the circuit into CNF, and solve SAT



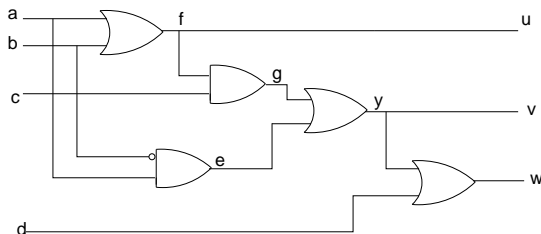
SAT in Equivalence checking

- Prove infeasibility of the miter!
 - Find an assignment to the inputs s.t. $(F \neq G) = 1$ (bug)
 - If no assignment (infeasible), circuits are equivalent
- Model checking: find an assignment s.t. a property is satisfied/falsified



- A Boolean formula $f(x_1, \dots, x_n)$ over propositional variables $x_1, \dots, x_n \in \{0, 1\}$, using propositional connectives \neg, \vee, \wedge , parenthesis, and implications \implies, \iff
 - Example: $f = ((\neg x_1 \wedge x_2) \vee x_3) \wedge (\neg x_2 \vee x_3)$
- A CNF formula representation of f is:
 - a conjunction of **clauses**
 - each clause is a disjunction of literals
 - each literal is a variable or its negation (complement)
- Example: $f = (\neg x_1 \vee x_2)(\neg x_2 \vee x_3 \vee \neg x_4)(x_1 \vee x_2 \vee x_3 \vee \neg x_4)$
- Alternate notation $f = (x'_1 + x_2)(x'_2 + x_3 + x'_4)(x_1 + x_2 + x_3 + x'_4)$
- Any Boolean formula (circuit) can be encoded into CNF

Encode a Circuit to CNF



$$f = a \vee b$$

$$f \iff a \vee b \text{ (equality is a double-implication)}$$

$$\begin{aligned} \text{CNF : } & (f \implies (a \vee b)) \wedge ((a \vee b) \implies f) \\ & (\neg f \vee (a \vee b)) \wedge (\neg(a \vee b) \vee f) \\ & (\neg f \vee (a \vee b)) \wedge ((\neg a \wedge \neg b) \vee f) \text{ (CNF?)} \\ & (\neg f \vee (a \vee b)) \wedge (\neg a \vee f)(\neg b \vee f) \end{aligned}$$

Circuit to CNF: Implication to Clauses

In general, if $f = OP(a, b)$, the CNF representation is:

- $f \iff OP(a, b)$, further simplified as:
- $(f \implies OP(a, b)) \wedge (OP(a, b) \implies f)$
- Translate implication to Boolean formula: $a \implies b$ means $(a' + b)$ is TAUTOLOGY.

- For $f = a \wedge b$, CNF: $(\neg f + a)(\neg f + b)(\neg a + \neg b + f)$
- For $f = a \oplus b$, CNF:
 $(\neg f + a + b)(f + \neg a + b)(f + a + \neg b)(\neg f + \neg a + \neg b)$
- For the previous circuit, we need to further constrain $u = 1, v = 1, w = 0$ to solve the simulation vector generation problem. Encode constraints $u = 1, v = 1, w = 0$ into CNF as $(u)(v)(w')$
- Conjoin ALL clauses (constraints) and invoke a SAT solver to find a solution

- In general, SAT is **NP-complete**. No polynomial-time algorithm exists to solve SAT (in theory).
- The restricted 2-SAT problem, where every clause contains only 2 literals, can be solved in polynomial time.
- Circuit-to-CNF: Recall, 2-input AND/OR gates need a 3-literal clause for modeling the constraint.
 - Circuit-SAT is therefore also NP-complete.
- However, modern SAT solvers are a success story in Computer Science and Engineering. Efficient heuristics and implementation tricks make SAT solvers very efficient.
- EDA gave a big impetus to SAT solving
- Many large problems can be solved very quickly by SAT solvers.
- So, how is a CNF SAT formula solved?

- An assignment can make a clause satisfied or unsatisfied
- Since $f = C_1 \wedge C_2 \wedge \dots \wedge C_n$, try to SATISFY each clause C_i
- The first approach by Davis & Putnam [DP 1960]: based on unit clause, pure literal and resolution rules
- Later Davis, Logemann, Loveland [DLL 1962] proposed an alternative backtrack-based search algorithm
- These algorithms are now known as DPLL algorithms
- Modern solvers are highly sophisticated: conflict-driven clause learning (CDCL) and search-space pruning, among many efficient heuristics

Satisfy a clause

A clause is satisfied if any literal is assigned to 1. E.g. for $x_2 = 0$, clause $(x_1 \vee \neg x_2 \vee \neg x_3) = 1$.

Satisfy a clause

A clause is unsatisfied if all literals are assigned to 0. E.g. the assignment of $x_1 = 0, x_2 = x_3 = 1$, makes clause $(x_1 \vee \neg x_2 \vee \neg x_3)$ unsatisfied.

Unit clause

A clause containing a single unassigned literal, and all other literals assigned to 0. E.g., the assignment $x_1 = 0, x_3 = 1$, makes $(x_1 \vee \neg x_2 \vee \neg x_3) = (0 \vee \neg x_2 \vee 0)$ a unit clause. Unit clause forces a necessary assignment ($x_2 = 0$) for the formula to be TRUE.

- Formula f is satisfied, if all clauses are satisfied; f is unsatisfied, if at least one clause is unsatisfied.

- A literal is **pure** if it appears only as a positive literal, or only as a negative literal.
 - $f = (\neg x_1 \vee x_2) \wedge (x_3 \vee \neg x_2) \wedge (x_4 \vee \neg x_5) \wedge (x_5 \vee \neg x_4)$
 - x_1, x_3 are pure literals.
- Clauses containing pure literals can be easily satisfied.
 - Assign pure literals to the values that satisfy the clauses
 - Pure literals do not cause inconsistent value assignments (or conflicts) to variables.
- Iteratively apply **unit clause propagation** and **pure literal** simplification on the CNF formula

- Resolution Rule: Given clauses $(x \vee \alpha)$ and $(\neg x \vee \beta)$, infer $(\alpha \vee \beta)$
 - $RES(x \vee \alpha, \neg x \vee \beta) = (\alpha \vee \beta)$
- The DP algorithm was resolution-based

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 - Apply resolution rules between every pair of clauses $(x \vee \alpha)$ and $(\neg x \vee \beta)$; simplify f

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Terminate when **empty clause (UNSAT)** or **empty formula (SAT)**

Deduce SAT/UNSAT by Resolution: Example

$$(x_1 \vee \neg x_2 \vee \neg x_3) \wedge (\neg x_1 \vee \neg x_2 \vee \neg x_3) \wedge (x_2 \vee x_3) \wedge (x_3 \vee x_4) \wedge (x_3 \vee \neg x_4)$$

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$$(\neg x_2 \vee \neg x_3) \wedge (x_2 \vee x_3) \wedge (x_3 \vee x_4) \wedge (x_3 \vee \neg x_4)$$

$$(\neg x_3 \vee x_3) \wedge (x_3 \vee x_4) \wedge (x_3 \vee \neg x_4)$$

$$(x_3)$$

Deduce SAT/UNSAT by Resolution: Example

$$(x_1 \vee \neg x_2 \vee \neg x_3) \wedge (\neg x_1 \vee \neg x_2 \vee \neg x_3) \wedge (x_2 \vee x_3) \wedge (x_3 \vee x_4) \wedge (x_3 \vee \neg x_4)$$

$$(\neg x_2 \vee \neg x_3) \wedge (x_2 \vee x_3) \wedge (x_3 \vee x_4) \wedge (x_3 \vee \neg x_4)$$

$$(\neg x_3 \vee x_3) \wedge (x_3 \vee x_4) \wedge (x_3 \vee \neg x_4)$$

$$(x_3)$$

Satisfiable!

- The [DP 1960] approach using resolution was inefficient
- Then the [DLL 1962] was introduced:
 - Select a variable x , assign either $x = 0$ or $x = 1$ [decision assignment]
 - Simplify formula with unit propagation, pure literal rules [deduce]
 - If conflict, then backtrack [diagnose]
 - If cannot backtrack further, return UNSAT
 - If formula satisfied, return SAT
 - Otherwise, proceed with another decision

$$f = (a + b' + d)(a + b' + e)(b' + d' + e')(a + b + c + d)(a + b + c + d')(a + b + c' + e)(a + b + c' + e')$$

$$f = (a + b' + d)(a + b' + e)(b' + d' + e')(a + b + c + d)(a + b + c + d')(a + b + c' + e)(a + b + c' + e')$$

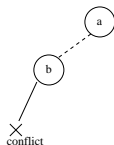
$$a = 0$$



DPLL Example

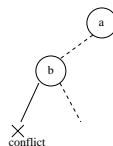
$$f = (a + b' + d)(a + b' + e)(b' + d' + e')(a + b + c + d)(a + b + c + d')(a + b + c' + e)(a + b + c' + e')$$

$a = 0$, $b = 1$, conflict,
backtrack, change last
decision!



$$f = (a + b' + d)(a + b' + e)(b' + d' + e')(a + b + c + d)(a + b + c + d')(a + b + c' + e)(a + b + c' + e')$$

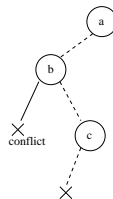
$$a = 0, b = 0$$



DPLL Example

$$f = (a + b' + d)(a + b' + e)(b' + d' + e')(a + b + c + d)(a + b + c + d')(a + b + c' + e)(a + b + c' + e')$$

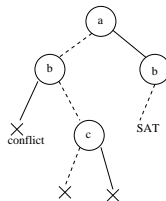
$a = 0, b = 0, c = 0,$
conflict, backtrack!



DPLL Example

$$f = (a + b' + d)(a + b' + e)(b' + d' + e')(a + b + c + d)(a + b + c + d')(a + b + c' + e)(a + b + c' + e')$$

$$a = 1, b = 0$$



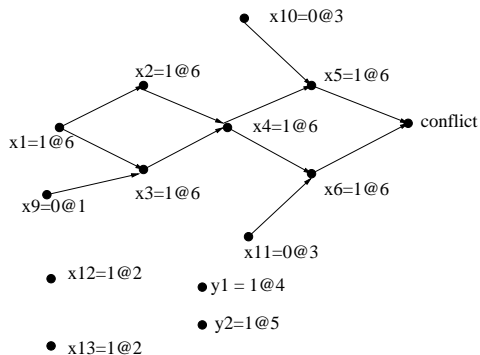
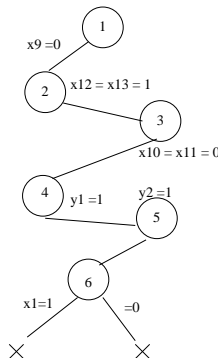
- Previous example shows a chronological backtrack based binary search
- Modern SAT solvers analyze decisions and conflicts to dynamically **learn** clauses
 - Conflict Driven Clause Learning (CDCL)
 - Solver learns more clauses, and appends them to the original CNF
 - More constraints help to prune the search
 - Results in a **non-chronological** backtrack-based search
 - The approach is still complete: Will find SAT, or will prove UNSAT
- There are also “incomplete” solvers, that rely on local search
 - Heuristics to guide the search, but search not exhaustive
 - May find a SAT solution if one exists, but cannot prove UNSAT
- There are also SAT pre-processors
 - Input CNF \mathcal{F}_1 , output CNF \mathcal{F}_2 , $\text{size}(\mathcal{F}_1) > \text{size}(\mathcal{F}_2)$

- Modern CDCL-solvers: based on DPLL, but do quite a bit more
 - Learn new constraints while encountering conflicts
 - Enable **non-chronological backtracking**, thus pruning search-space
 - Branching heuristics: which variable to branch on ($x_i = 0$? or $x_i = 1$?)
 - Heuristics for search re-starts
 - Efficient management of clause-database: minimize learnt clauses, discard unused learnt clauses
- Concept of CDCL from [GRASP, Joao Marques-Silva and Karem Sakallah]
- Read GRASP report on class website

$$(x'_1 + x_2)(x'_1 + x_3 + x_9)(x'_2 + x'_3 + x_4)(x'_4 + x_5 + x_{10})(x'_4 + x_6 + x_{11}) \\ (x'_5 + x'_6)(x_1 + x_7 + x'_{12})(x_1 + x_8)(x'_7 + x'_8 + x'_{13})(y_1 + z_1)(y_2 + z_2)$$

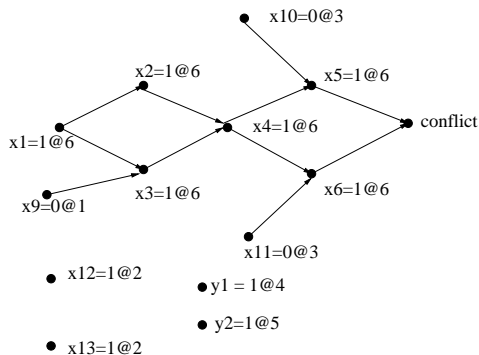
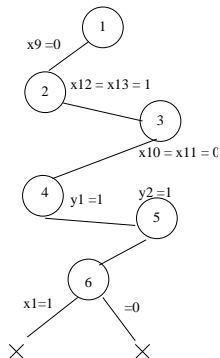
CDCL & Non-Chronological Backtracking [From GRASP]

$$(x'_1 + x_2)(x'_1 + x_3 + \textcolor{red}{x_9})(x'_2 + x'_3 + x_4)(x'_4 + x_5 + x_{10})(x'_4 + x_6 + x_{11}) \\ (x'_5 + x'_6)(x_1 + x_7 + x'_{12})(x_1 + x_8)(x'_7 + x'_8 + x'_{13})(y_1 + z_1)(y_2 + z_2)$$



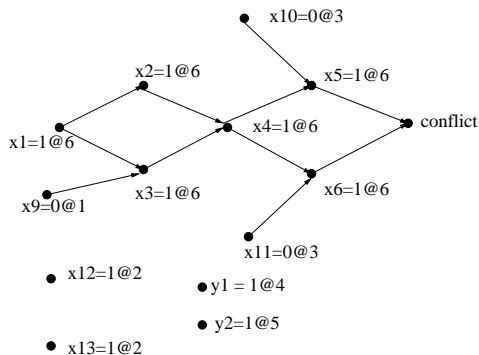
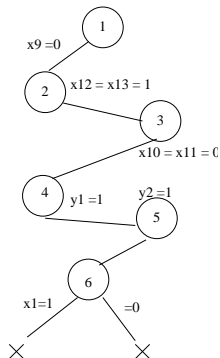
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$$(x'_1 + x_2)(x'_1 + x_3 + \textcolor{red}{x_9})(x'_2 + x'_3 + x_4)(x'_4 + x_5 + x_{10})(x'_4 + x_6 + x_{11}) \\ (x'_5 + x'_6)(x_1 + x_7 + \textcolor{red}{x'_{12}})(x_1 + x_8)(x'_7 + x'_8 + \textcolor{red}{x'_{13}})(y_1 + z_1)(y_2 + z_2)$$



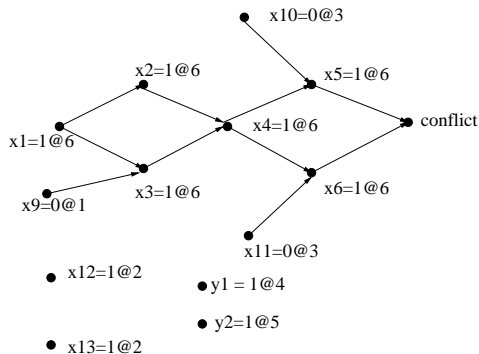
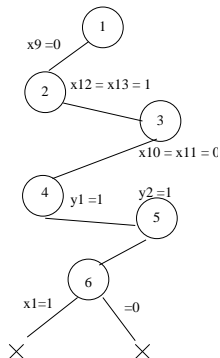
CDCL & Non-Chronological Backtracking [From GRASP]

$$(x'_1 + x_2)(x'_1 + x_3 + \textcolor{red}{x}_9)(x'_2 + x'_3 + x_4)(x'_4 + x_5 + \textcolor{red}{x}_{10})(x'_4 + x_6 + \textcolor{red}{x}_{11}) \\ (x'_5 + x'_6)(x_1 + x_7 + \textcolor{red}{x}'_{12})(x_1 + x_8)(x'_7 + x'_8 + \textcolor{red}{x}'_{13})(\textcolor{blue}{y}_1 + z_1)(\textcolor{blue}{y}_2 + z_2)$$



CDCL & Non-Chronological Backtracking [From GRASP]

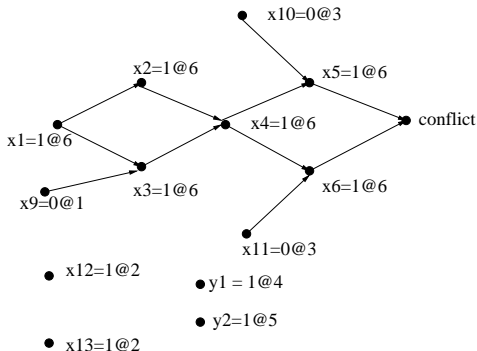
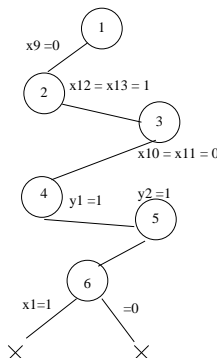
$$(\textcolor{red}{x}'_1 + x_2)(\textcolor{red}{x}'_1 + x_3 + \textcolor{red}{x}_9)(x'_2 + x'_3 + x_4)(x'_4 + x_5 + \textcolor{red}{x}_{10})(x'_4 + x_6 + \textcolor{red}{x}_{11}) \\ (x'_5 + x'_6)(\textcolor{blue}{x}_1 + x_7 + \textcolor{red}{x}'_{12})(\textcolor{blue}{x}_1 + x_8)(x'_7 + x'_8 + \textcolor{red}{x}'_{13})(\textcolor{blue}{y}_1 + z_1)(\textcolor{blue}{y}_2 + z_2)$$



CDCL & Non-Chronological Backtracking [From GRASP]

$$(\overset{\text{red}}{x'_1} + x_2)(\overset{\text{red}}{x'_1} + x_3 + \overset{\text{red}}{x_9})(x'_2 + x'_3 + x_4)(x'_4 + x_5 + \overset{\text{red}}{x_{10}})(x'_4 + x_6 + \overset{\text{red}}{x_{11}}) \\ (x'_5 + x'_6)(\overset{\text{blue}}{x_1} + x_7 + \overset{\text{red}}{x'_{12}})(\overset{\text{blue}}{x_1} + x_8)(x'_7 + x'_8 + \overset{\text{red}}{x'_{13}})(\overset{\text{blue}}{y_1} + z_1)(\overset{\text{blue}}{y_2} + z_2)$$

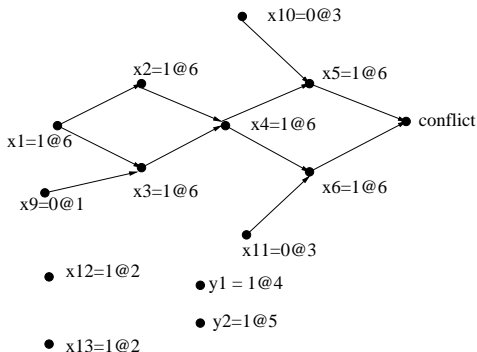
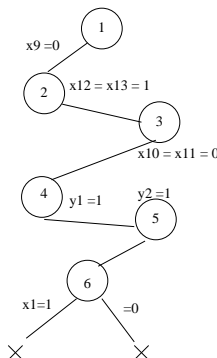
Conflict: $(x'_9 \wedge x_{12} \wedge x_{13} \wedge x'_{10} \wedge x'_{11} \wedge y_1 \wedge y_2 \wedge x_1) \implies \text{FALSE}$



CDCL & Non-Chronological Backtracking [From GRASP]

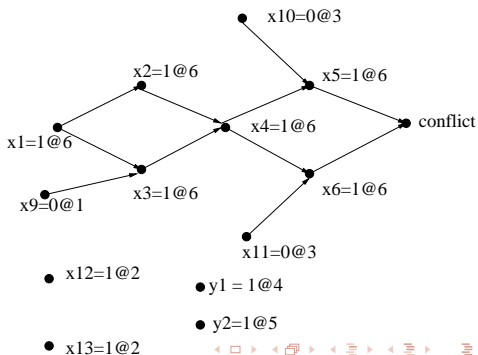
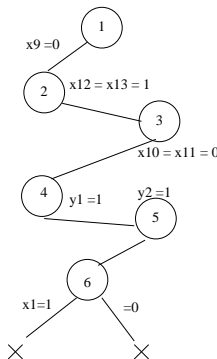
$$(\overset{\text{red}}{x'_1} + x_2)(\overset{\text{red}}{x'_1} + x_3 + \overset{\text{red}}{x_9})(x'_2 + x'_3 + x_4)(x'_4 + x_5 + \overset{\text{red}}{x_{10}})(x'_4 + x_6 + \overset{\text{red}}{x_{11}}) \\ (x'_5 + x'_6)(\overset{\text{blue}}{x_1} + x_7 + \overset{\text{red}}{x'_{12}})(\overset{\text{blue}}{x_1} + x_8)(x'_7 + x'_8 + \overset{\text{red}}{x'_{13}})(\overset{\text{blue}}{y_1} + z_1)(\overset{\text{blue}}{y_2} + z_2)$$

Is the learnt Clause = $(x_9 \vee x'_{12} \vee x'_{13} \vee x_{10} \vee x_{11} \vee y'_1 \vee y'_2 \vee x'_1)$?



CDCL: Analyze the cause of conflict

- From the conflict-node in the implication graph, traverse back to *antecedents* (or root nodes x_1, x_9, x_{10}, x_{11})
- Note that x_{12}, x_{13}, y_1, y_2 are *unreachable*
- Conflict clause can be simplified:
 - From $(x_9 \vee x'_{12} \vee x'_{13} \vee x_{10} \vee x_{11} \vee y'_1 \vee y'_2 \vee x'_1)$
 - To $(x_9 \vee x_{10} \vee x_{11} \vee x'_1)$

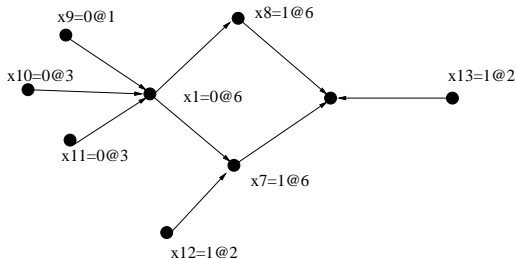


Conflict-Driven Clause Learning (CDCL) solvers

- Add learnt clause to original CNF
- Chronological backtrack: revert last assignment from $x_1 = 1$ to $x_1 = 0$

$$(x'_1 + x_2)(x'_1 + x_3 + x_9)(x'_2 + x'_3 + x_4)(x'_4 + x_5 + x_{10})(x'_4 + x_6 + x_{11}) \\ (x'_5 + x'_6)(x_1 + x_7 + x'_{12})(x_1 + x_8)(x'_7 + x'_8 + x'_{13})(y_1 + z_1)(y_2 + z_2)$$

Assignment on Learnt Clause: $(x_9 \vee x_{10} \vee x_{11} \vee x'_1)$

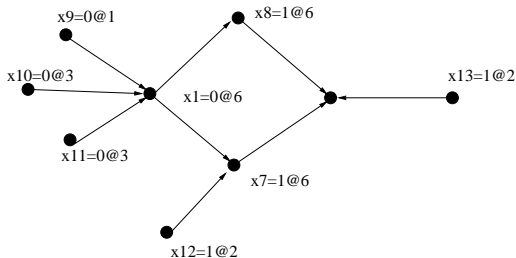


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- Add learnt clause to original CNF
- Chronological backtrack: revert last assignment from $x_1 = 1$ to $x_1 = 0$

$$(\color{blue}{x'_1} + x_2)(\color{blue}{x'_1} + x_3 + \color{red}{x_9})(x'_2 + x'_3 + x_4)(x'_4 + x_5 + \color{red}{x_{10}})(x'_4 + x_6 + \color{red}{x_{11}}) \\ (x'_5 + x'_6)(\color{red}{x_1} + x_7 + \color{red}{x'_{12}})(\color{red}{x_1} + x_8)(x'_7 + x'_8 + \color{red}{x'_{13}})(\color{blue}{y_1} + z_1)(\color{blue}{y_2} + z_2)$$

Assignment on Learnt Clause: ($\color{red}{x_9} \vee \color{red}{x_{10}} \vee \color{red}{x_{11}} \vee \color{blue}{x'_1}$)



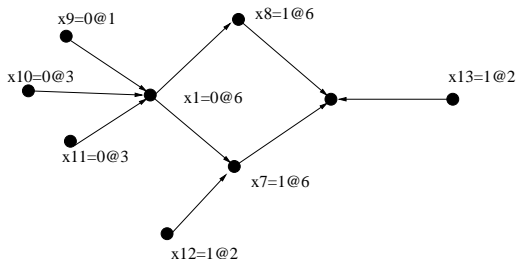
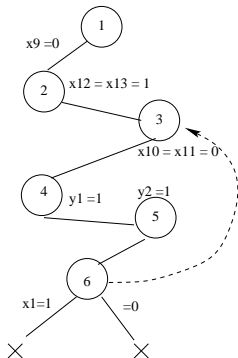
$x_1 = 0$ also leads to a **conflict**. Learn new clause?

$$(x'_1 + x_2)(x'_1 + x_3 + x_9)(x'_2 + x'_3 + x_4)(x'_4 + x_5 + x_{10})(x'_4 + x_6 + x_{11}) \\ (x'_5 + x'_6)(x_1 + x_7 + x'_{12})(x_1 + x_8)(x'_7 + x'_8 + x'_{13})(y_1 + z_1)(y_2 + z_2)$$

First learnt/conflict clause $CC_1: (x_9 \vee x_{10} \vee x_{11} \vee x'_1)$

- New conflict clause also derived from implication graph
- $CC_2: (x_9 \vee x'_{12} \vee x'_{13} \vee x_{10} \vee x_{11})$
- Decision on x_1, y_1, y_2 does not affect the CNF SAT!
- Non-Chronological backtrack:
 - To the MAX decision-level in the conflict clause!
 - Backtrack to Decision-Level 3, undo x_{10} or x_{11}

$$CC_2: (\textcolor{red}{x_9} \vee \textcolor{red}{x'_{12}} \vee \textcolor{red}{x'_{13}} \vee \textcolor{red}{x_{10}} \vee \textcolor{red}{x_{11}})$$



- Recent techniques can identify more conflict clauses
- Identify unique implication points (UIPs)
- Decision heuristics: Branch on high-activity literals [GRASP]
 - Activity: A score for every literal
 - The number of occurrences of a literal in the formula
- As conflict clauses are added, activity changes
- After n conflicts, multiply activity by $f < 1$, or *rescore*
 - VSIDS heuristic: Variable State Independent Decaying Sum [CHAFF]

A List of CDCL SAT solvers

- GRASP, circa 1996, from Silva and Sakallah
- zCHAFF 2001, from Princeton, Prof. Sharad Malik
- BerkMin 2002
- MiniSAT, 2004 (?) from Cadence Berkeley Labs
- PicoSAT and Lingeling, from Prof. Armin Biere, Univ. Linz
- Please visit www.satisfiability.org

- CNF: $\mathcal{F} = (a' + b')(a' + b)(a + b')(a + b)(x + y)(y + z)$
 - Note that \mathcal{F} is UNSAT
 - Identify a **minimum** number of clauses that make \mathcal{F} UNSAT
 - This subset of clauses is the *UNSAT Core*, or MIN-UNSAT
 - Helps to identify the causes for UNSAT
- $(a' + b')(a' + b)(a + b')(a + b)$ is the UNSAT core in \mathcal{F}
- UNSAT core may not be unique
- UNSAT cores have many applications in verification
- Study of UNSAT cores and applications: Good class project option!

- Where does SAT fail?
- For hard UNSAT instances, such as equivalence verification

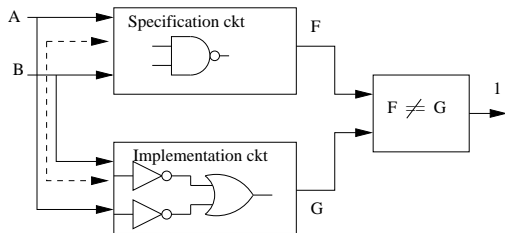


Figure: Miter the circuits F, G

- Prove UNSAT, or find a counter-example
- Limitations: No internal structural equivalences
- EDA-techniques: Circuit-SAT, AIG-reductions, constraint-learning

What Next?

How to improve SAT for Circuit Equivalence Verification?

AND-INVERT-GRAPH (AIG) based Reductions!