

PERFORMANCE METRICS

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Overview

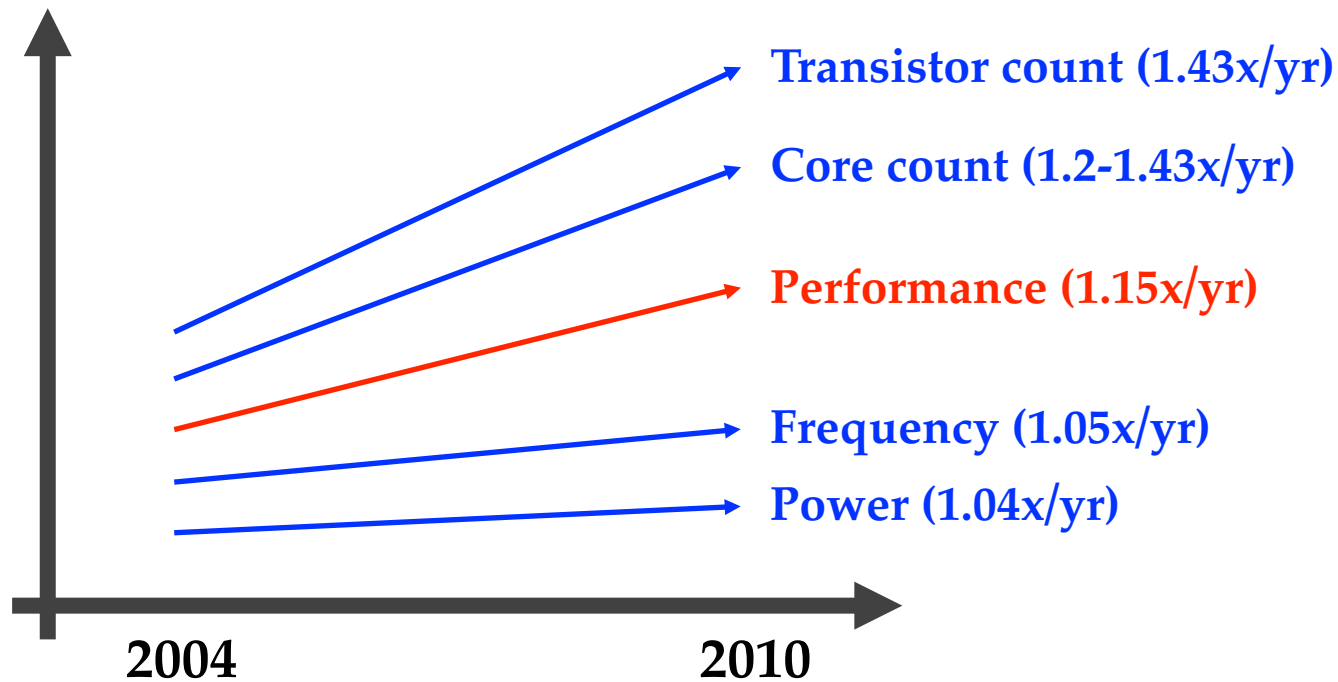
- Announcement
 - ▣ Jan. 17th: Homework 1 release (due on Jan. 30th)
- This lecture
 - ▣ Technology trends
 - ▣ Measuring performance
 - ▣ Principles of computer design
 - ▣ Power and energy
 - ▣ Cost and reliability

Technology Trends (Historical Data)

- IC logic Technology: on-chip transistor count doubles every 18-24 months (Moore's Law)
 - ▣ Transistor density increases by 35% per year
 - ▣ Die size increases 10-20% per year
- DRAM Technology
 - ▣ Chip capacity increases 25-40% per year
- Flash Storage
 - ▣ Chip capacity increases 50-60% per year

Technology Trends (Historical Data)

□ Recent Microprocessor Trends



Source: Micron University Symposium

Performance Trends

- How to measure performance?
 - ▣ **Latency or response time:** the time between start and completion of an event (e.g., milliseconds for disk access)
 - ▣ **Bandwidth or throughput:** the total amount of work done in a given time (e.g., megabytes per second for disk transfer)
- Which one grows faster?
 - ▣ **Bandwidth, by at least the square of latency improvement rate.**
- Which one is better? latency or throughput?

Measuring Performance

- Which one is better (faster)?

Car

- Delay=10m
- Capacity=4p
- Throughput=0.4PPM

Bus

- Delay=30m
- Capacity=30p
- Throughput=1PPM

It really depends on your needs (goals).

Measuring Performance

- What program to use for measuring performance?
- Benchmarks Suites
 - A set of representative programs that are likely relevant to the user
 - Examples:
 - SPEC CPU 2006: CPU-oriented programs (for desktops)
 - SPECweb: throughput-oriented (for servers)
 - EEMBC: embedded processors/workloads

Summarizing Performance Numbers

- How to capture the behavior of multiple programs with a single number

	Comp-A	Comp-B	Comp-C
Prog-1	10	5	25
Prog-2	5	10	20
Prog-3	25	10	25

- ❖ AM: Arithmetic Mean (good for times and latencies)

$$\frac{1}{n} \sum_{i=1}^n x_i$$

Summarizing Performance Numbers

- How to capture the behavior of multiple programs with a single number

	Comp-A	Comp-B	Comp-C
Prog-1	1/10	1/5	1/25
Prog-2	1/5	1/10	1/20
Prog-3	1/25	1/10	1/25

- ❖ HM: Harmonic Mean (good for rates and throughput)

$$\frac{n}{\sum_{i=1}^n \frac{1}{x_i}}$$

Summarizing Performance Numbers

- How to capture the behavior of multiple programs with a single number

	Comp-A	Comp-B	Comp-C
Prog-1	10/10	10/5	10/25
Prog-2	5/5	5/10	5/20
Prog-3	25/25	25/10	25/25

- ❖ GM: Geometric Mean (good for speedups)

$$\left(\prod_{i=1}^n x_i \right)^{1/n}$$

The Processor Performance

- Clock cycle time ($CT = 1 / \text{clock frequency}$)
 - ▣ Influenced by technology and pipeline
- Cycles per instruction (CPI)
 - ▣ Influenced by architecture
 - ▣ IPC may be used instead ($IPC = 1 / CPI$)
- Instruction count (IC)
 - ▣ Influenced by ISA and compiler
- CPU time = $IC \times CPI \times CT$

Example Problem

- Find the average CPI of a load/store machine when running an application that results in the following statistics

Instruction Type	Frequency	Cycles
Load	20%	2
Store	20%	2
Branch	20%	2
ALU	40%	1

$$\text{CPI} = 0.2 \times 2 + 0.2 \times 2 + 0.2 \times 2 + 0.4 \times 1 = 1.6$$

Example Problem

- Find the average CPI of a load/store machine when running an application that results in the following statistics

Instruction Type	Frequency	Cycles
Load	20%	2
Store	20%	2
Branch	20%	2
ALU	40%	1

- ❖ 50% of the branches can be combined with ALU instructions and executed as Branch-ALU fused in 2 cycles. What is the new average CPI?

Example Problem

- Find the average CPI of a load/store machine when running an application that results in the following statistics

Instruction Type	Frequency	Cycles
Load	22%	2
Store	22%	2
Branch	11%	2
ALU	33%	1
Branch-ALU	12%	2

- ❖ 80% of the branches can be combined with ALU instructions and executed as Branch-ALU fused in 2 cycles. What is the new average CPI? $\text{CPI} = 1.67$

The Processor Performance

- Points to note

- ▣ Performance = 1 / execution time

- ▣ AM(IPCs) = 1 / HM(CPIs)

- ▣ GM(IPCs) = 1 / GM(CPIs)

$$\frac{1}{n} \sum_{i=1}^n x_i \qquad \frac{n}{\sum_{i=1}^n \frac{1}{x_i}} \qquad \left(\prod_{i=1}^n x_i \right)^{1/n}$$

Speedup vs. Percentage

- Speedup = old execution time / new execution time
- Improvement = (new performance - old performance) / old performance
- My old and new computers run a particular program in 80 and 60 seconds; compute the followings
 - ▣ speedup = $80/60$
 - ▣ percentage increase in performance = 33%
 - ▣ reduction in execution time = $20/80 = 25\%$

Example Problem

- A new computer has an IPC that is 20% worse than the old one. However, it has a clock speed that is 30% higher than the old one. If running the same binaries on both machines. What speedup is the new computer providing? $\text{Speedup} = 1 / 0.96 = 1.04$

	OLD	NEW
IPC	1	0.8
Frequency	1	1.3
IC	1	1
CPI	1/1	1/0.8 = 1.25
CT	1/1	1/1.3 ~ 0.77
CPU Time	1	~0.96

Principles of Computer Design

- Designing better computer systems requires better utilization of resources
 - ▣ Parallelism
 - Multiple units for executing partial or complete tasks
 - ▣ Principle of locality (temporal and spatial)
 - Reuse data and functional units
 - ▣ Common Case
 - Use additional resources to improve the common case

Amdahl's Law

- The law of diminishing returns

$$\text{Execution time}_{\text{new}} = \text{Execution time}_{\text{old}} \times \left((1 - \text{Fraction}_{\text{enhanced}}) + \frac{\text{Fraction}_{\text{enhanced}}}{\text{Speedup}_{\text{enhanced}}} \right)$$

$$\text{Speedup}_{\text{overall}} = \frac{\text{Execution time}_{\text{old}}}{\text{Execution time}_{\text{new}}} = \frac{1}{(1 - \text{Fraction}_{\text{enhanced}}) + \frac{\text{Fraction}_{\text{enhanced}}}{\text{Speedup}_{\text{enhanced}}}}$$

Example Problem

- Our new processor is 10x faster on computation than the original processor. Assuming that the original processor is busy with computation 40% of the time and is waiting for IO 60% of the time, what is the overall speedup?

$$f=0.4 \quad s=10$$

$$\text{Speedup} = 1 / (0.6 + 0.4/10) = 1/0.64 = 1.5625$$

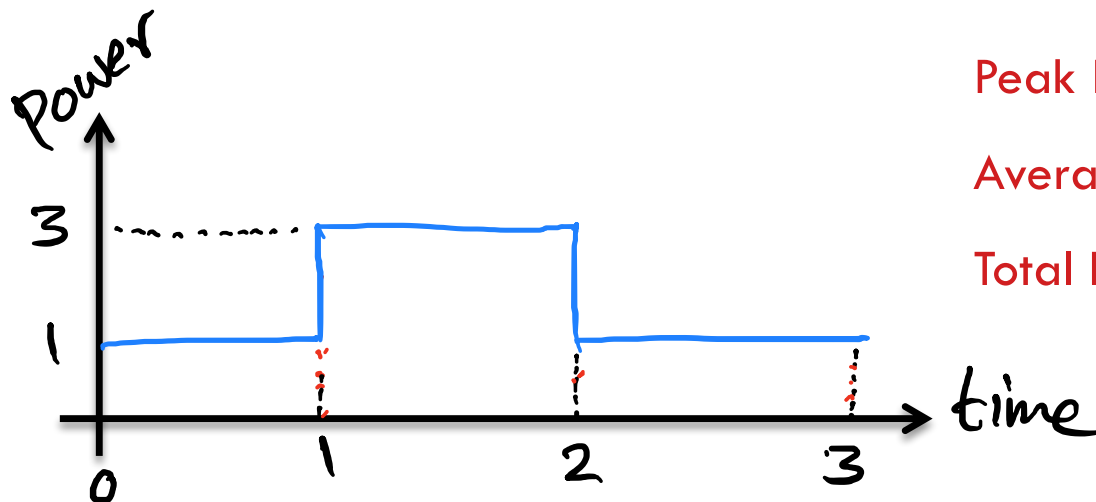
Power and Energy

Power and Energy

- Power = Voltage x Current ($P = VI$)
 - ▣ Instantaneous rate of energy transfer (Watt)
- Energy = Power x Time ($E = PT$)
 - ▣ The cost of performing a task (Joule)

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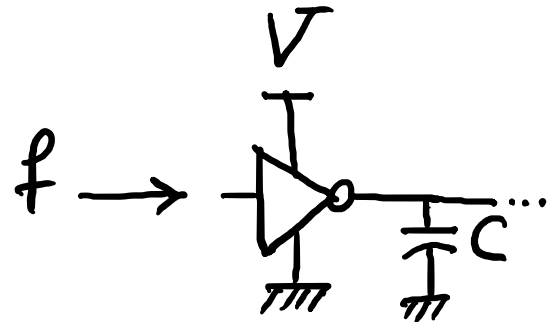
Peak Power = 3W

Average Power = 1.66W

Total Energy = 5J

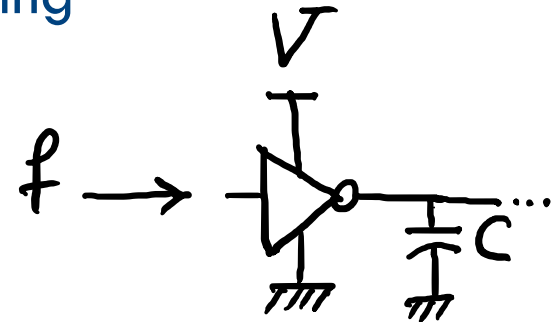
CPU Power and Energy

- All consumed energy is converted to heat
 - ▣ CPU power is the rate of heat generation
 - ▣ Excessive peak power may result in burning the chip
- Static and dynamic energy components
 - $\text{Energy} = (\text{Power}_{\text{Static}} + \text{Power}_{\text{Dynamic}}) \times \text{Time}$
 - $\text{Power}_{\text{Static}} = \text{Voltage} \times \text{Current}_{\text{Static}}$
 - $\text{Power}_{\text{Dynamic}} = \text{Activity} \times \text{Capacitance} \times \text{Voltage}^2 \times \text{Frequency}$



Power Reduction Techniques

- Reducing capacitance (C)
 - ▣ Requires changes to physical layout and technology
- Reducing voltage (V)
 - ▣ Negative effect on frequency
 - ▣ Opportunistically power gating (wakeup time)
 - ▣ Dynamic voltage and frequency scaling
- Reducing frequency (f)
 - ▣ Negative effect on CPU time
 - ▣ Clock gating in unused resources
- Points to note
 - ▣ Utilization directly effects dynamic power
 - ▣ Lowering power does NOT mean lowering energy



Example Problem

- For a processor running at 100% utilization and consuming 60W, 30% of the power is attributed to leakage. What is the total power dissipation when the processor is running at 50% utilization?

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- @100%
 - ▣ $\text{Power} = 18\text{W} + 42\text{W} = 60\text{W}$
- @50%
 - ▣ $\text{Power} = 18\text{W} + 21\text{W} = 39\text{W}$

Example Problem

- A processor consumes 80W of dynamic power and 20W of static power at 3GHz. It completes a program in 20 seconds. What is the energy consumption if frequency scales down by 20%?

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- @3GHz
 - ▣ $\text{Energy} = (80\text{W} + 20\text{W}) \times 20\text{s} = 2000\text{J}$
- @2.4GHz
 - ▣ $\text{Energy} = (0.8 \times 80\text{W} + 20\text{W}) \times 20/0.8 = 2100\text{J}$

Example Problem

- A processor consumes 80W of dynamic power and 20W of static power at 3GHz. It completes a program in 20 seconds. What is the energy consumption if frequency scales down by 20%?
- What is the energy consumption if voltage and frequency scale down by 20%?

Example Problem

- A processor consumes 80W of dynamic power and 20W of static power at 3GHz. It completes a program in 20 seconds. What is the energy consumption if frequency scales down by 20%?
- What is the energy consumption if voltage and frequency scale down by 20%?
- @ 80%V and 80%f
 - $\text{Energy} = (80 \times 0.8^2 \times 0.8 + 20 \times 0.8) \times 20 / 0.8 = 1424\text{J}$

Cost and Reliability

Cost of Integrated Circuit

- Cost of die

- ▣
$$\frac{\text{wafer cost}}{\text{dies per wafer} \times \text{die yield}}$$

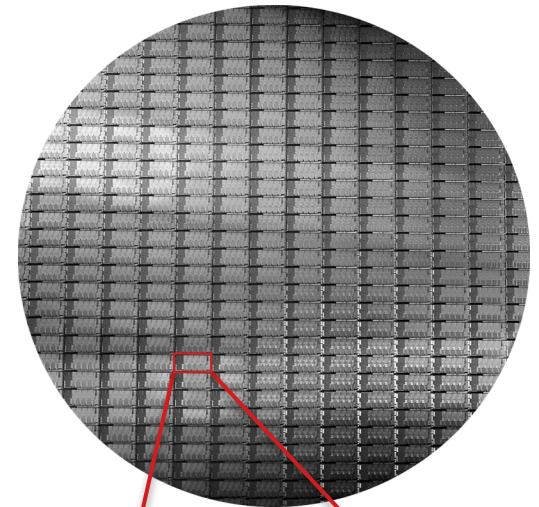
- Yield of die

- ▣
$$\frac{\text{wafer yield}}{(1 + \text{defect per unit area} \times \text{die area})^N}$$

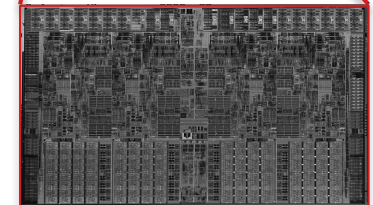
- N: process-complexity factor

- Specified by chip manufacturer

Example wafer



Die



Example Problem

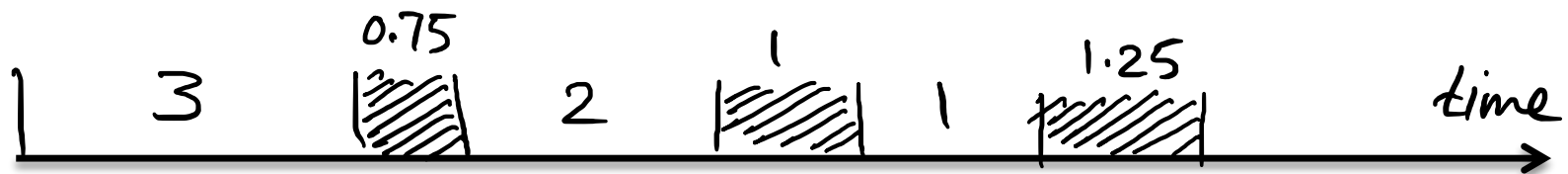
- Defect rate for a 144mm^2 die is 0.5 per cm^2 .
Assuming that we use a 40nm technology node ($N=11$) with 100% wafer yield, find the die yield.

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Assuming that we use a 40nm technology node ($N=11$) with 100% wafer yield, find the die yield.
- Die yield = $1 / (1 + 0.5 \times 1.44)^{11}$

Dependability

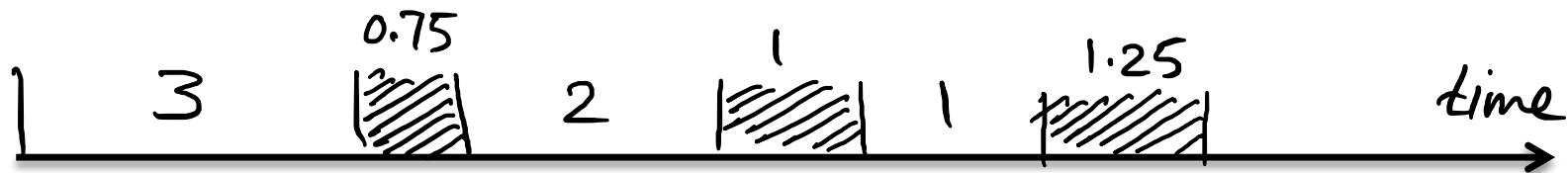
- A measure of system's reliability and availability
- System reliability
 - A measure of continuous service (time-to-failure)
 - Mean Time To Failure (MTTF)
 - Mean Time To Repair (MTTR)



- System availability

Dependability

- A measure of system's reliability and availability
- System reliability
 - A measure of continuous service (time-to-failure)
 - Mean Time To Failure (MTTF) = $(3+2+1)/3 = 2$
 - Mean Time To Repair (MTTR) = $(0.75+1+1.25)/3 = 1$



- System availability

$$\frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} = 2/(2+1) = 0.67$$