Homework 12: Indicator Random Variables

- 1. You randomly throw 6 balls into 10 different baskets. Let X be the number of balls which land in the first basket, and let Y be the number of baskets which are empty.
 - (a) Find $f_X(x)$.
 - (b) Find E(X).
 - (c) Find E(Y). (Hint. Let I_j be the indicator of the event "basket j is empty". Note that Y is the sum of the I_j 's.)
- 2. From a group of 9 math majors and 6 physics majors (no double majors), 4 are randomly selected for the Putnam Competition team. Let M be the number of math majors on the team. Find E(M) in two ways:
 - (a) Use the definition of E(M). (You will need to first find $f_M(m)$.)
 - (b) Use indicator random variables. Specifically, let I_j be the indicator of the event "the *j*-th person selected is a math major". Use the fact that $M = I_1 + I_2 + I_3 + I_4$.
- 3. A population of n people vote in an election. d vote democratic and n-d vote republican. In the next election, the probability of a democratic voter switching to republican is p_1 , and the probability of a republican voter switching to democratic is p_2 . Let X be the number of democratic votes in the second election. Find E(X).