

Vidyavardhini's College of Engineering and Technology, Vasai (West)

First Year Engineering

Academic Year: 2024-2025

Solution to the prevous year questions papers $[2017 - 2024]^{-1}$

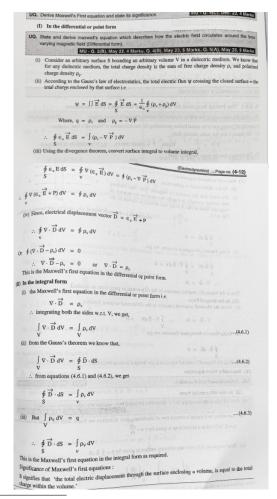
Subject: BSC102/AP Date: 20/11/2024

Module-4: Electrodynamics

Maxwell's Equations

Q.1. Explain Gauss's laws for static electric and static magnetic fields in differential and integral forms. [5 Marks] [May-2022, May-2023]

Ans:

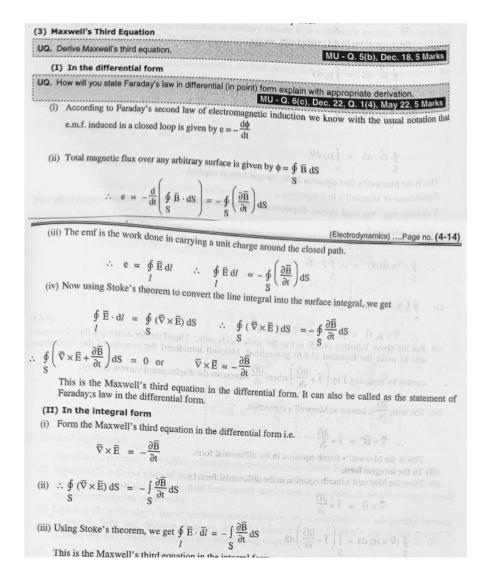


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(2) Maxwell's second equation (I) In the differential or point form	VD(日の)マモニ (日)マモ
(I) In the differential or point form	
(i) We know that the number of magnetic lines flow class- any surface normally is exactly the same as the number magnetic lines of flux leaving that surface as shown in t Fig. 4.6.1.	of the
резоргія, 4.6.1 : Ма	gnetic lines of flux entering and leaving a surfac
$ \begin{array}{lll} \therefore & \oint \overline{B} dS &= 0 \\ V & & \end{array} $	
(ii) Using Gauss's divergence theorem, we get,	
$ \oint \overline{B} dS = \oint \overline{V} \cdot \overline{B} dV = 0 $ S	
The state of the s	This is the Maxwell's first equation in the case in the case in the case in the talk and for the case in the talk and the t
This is the Maxwell's second equation in the differential or po (II) In the integral form	int form as required.
(i) From the Maxwell's second equation in the differential or	
$\nabla \cdot \overline{B} = 0$ $\therefore \int_{\mathbf{V}} \nabla \cdot \overline{B} d\mathbf{V} = \int_{\mathbf{V}}^{2a_{0} d w}$	
(ii) Using Gauss's divergence theorem, we get	
$ \oint_{S} \vec{B} \cdot d\vec{S} = 0 $	
This the Maxwell's second equation in the integral form a	6 required

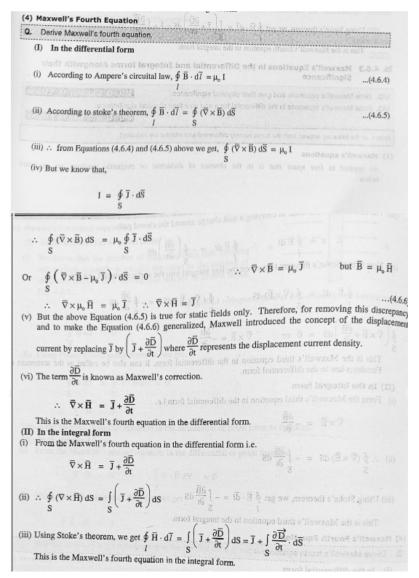
Q.2. State and derive Maxwell's equation in differential form which describes how the electric field circulates around the time-varying magnetic field. [5 Marks] [Dec-2018, May-2022, Dec-2022]

Ans:



Q.3. Obtain Ampere's circuital law for a static magnetic field in differential and integral forms. [5 Marks] Dec-2018, May-2022, Dec-2022]

Ans:



Q1. Gradient, Divergence and Curl²

- (a) What are scalar and vector fields? How is a del operator expressed? [3 Marks] [May-2019, May-2023]
- (b) If $\phi(x, y, z) = 3x^2y y^3z^2$, find $\nabla \phi$ at the point (-1, -2, 1). [3 Marks] [May-2019, May-2023]
- (c) What is the divergence of a vector field? Find the divergence of a field $\mathbf{F} = xz\hat{i} + y^2z^3\hat{j} xyz\hat{k}$ at a point (3, -1, 2). Interpret the result you obtain. [3 Marks] [May-2017, May-2022 Dec-2022, Dec-2023]
- (d) Explain the term 'curl of a vector' and state its significance. Show that the divergence of the curl of a vector is zero. [3 Marks] [Dec-17,May-2023, Dec-2023]

²Similar numericals based on the same concept were asked; however, only one example is presented here. As it is a numerical problem, students are encouraged to practice similar problems for better understanding.

Ans:

Alls:	
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2 1 2	att OCALAR FILIDA
9.1.9	A # SCALAR FIELDS:
	- A scalar field is mathematical function that assigns a
	scalar value (a single number) to each point in space.
	To Take the solid to the state of the state
	Ex: Temperature, distribution in a room, density of
	material, electric potential etc.
	# VECTOR FIELDS:
130408	- A vector field is a mothematical function that assigns
34.4.	a vector to each point in space
	Ex: Fluid velocity in pipe, electric field, etc.
	Vector hields and venymented by hinction E(X (1.2) -
100000000000000000000000000000000000000	Vector fields are represented by function $F(x, y, z) = (F_x, F_y, F_z)$ that takes three spatial coordinates as
	input and returns a vector with three components
	- whereas, scalar is represented by function f (x, y, z) that takes three spotial coordinates as input and returns a
A NIT	scalar value. The same same same
0 40 1	and ration to will standard that submer solves
616	# DELL OPERATOR (T):
	→ → → → → → → → → → → → → → → → → → →
	Doll operator is expressed as: $\overrightarrow{\nabla} = \partial \hat{i} + \partial \hat{j} + \partial \hat{k}$
	The state of the s
	- It acts like a vector and also like a differential eq
	thus it will obey rules relating to vectors as well
	as differential operator. It is used for finding:
	1) Gradient (V.+)
	ii) Pinergence (T.F)
1	Car o Cox x E)
b)	$\Phi(x,y,z) = 3x^2y - y^3z^2$
	To Lind: P. O
(Sundaram)	FOR EDUCATIONAL USE
	II'

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\oint (x,y,z) = 3x^2y - y^3z^2

\overrightarrow{\partial} = 3\hat{i} + 3\hat{j} + 3\hat{k}

\partial x \quad \partial y \quad \partial z

                                                                                                                              = \partial \phi \hat{i} + \partial \phi \hat{j} + \partial \phi \hat{k}
\partial x \partial y \partial z
                                                                  = \frac{3(3x^{2}y - y^{3}z^{2})}{3x} + \frac{3(3x^{2}y - y^{3}z^{2})}{3z} + \frac{3(3x^{2}y - y^{3}z^{2})}{2z}
= \frac{3(3x^{2}y - y^{3}z^{2})}{3z} + \frac{3(3x^{2}y - y^{3}z^{2})}{3z} + \frac{3(3x^{2}y - y^{3}z^{2})}{2z} + \frac{3(3x^{2}y - y^{3}z^{2})}{
                                                                                                                              = 12\hat{i} - 9\hat{j} + 16\hat{k}
                                                             The divergence of vector field F(x,y,z) = (Fx,Fy,Fz) is scalar value that represents flux of vector field at given point. It measures how much vector field
                                                                   divF = \overrightarrow{\nabla} \cdot F = \left( \frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z} \right) \cdot \left( \frac{xz_1^2 + y^2z_2^3}{2} - \frac{2xyz_2^2}{2} \right)
                                                                                                                                                                                           = \frac{3x^2 + 3y^2z^3 + 3(-xyz)}{3x}
                                                                                                                                                                                            = z + 2yz³ - xy

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∇ F = 2+2(-1)(2) ³ -(3(-1)	
= 2-16+3 = 2-13	
7-Fc3,-1,2) =-11 (10) 1) 1111-3 1111111	
S choras denotes	
-The negative divergence indicates that vector field is	
converging	
- It means more vectors are entering the region around this point than leaving it	
this point than leaving it	
where E = election lived	
a) - The curl of vector held F(x, y, z) = (Fx, Fy, Fz) is a	
d) - The curl of vector field $F(x, y, z) = (Fx, Fy, Fz) is a vector that measures notation or circulation of field$	
ayound a point.	
- Denoted by $\nabla \times F$ and it signifies restation, circulation	
magnetic hold etc	
7 3 1 + 3 1 + 3 R	
magnetic field etc P = 3 1 + 3 1 + 3 k 3x 3y 3z man - A man - A	
$f = F \times \hat{i} + F y \hat{j} + f z \hat{k}$	
· P. CTXF) = V. În j Promo - A BREANN	
2/2x 3/3y 3/2Z	
Fx Fy Fz	
$= \overrightarrow{\nabla} \cdot \left[\widehat{1} \left(\frac{\partial F_2 - \partial F_Y}{\partial y} \right) - \widehat{1} \left(\frac{\partial F_2 - \partial F_X}{\partial z} \right) + \widehat{R} \left(\frac{\partial F_Y - \partial F_X}{\partial z} \right) \right]$	
= \(\frac{1}{2}\)\cdot \(\frac{1}2\)\cdot \(\frac{1}2\)\cdot \(\frac{1}2\)\cdot \(\frac{1}2\)	
Pience proved, divergence of curl is zoro.	
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