

Inside LiquidFun



Kentaro Suto
Senior Software Engineer
Google

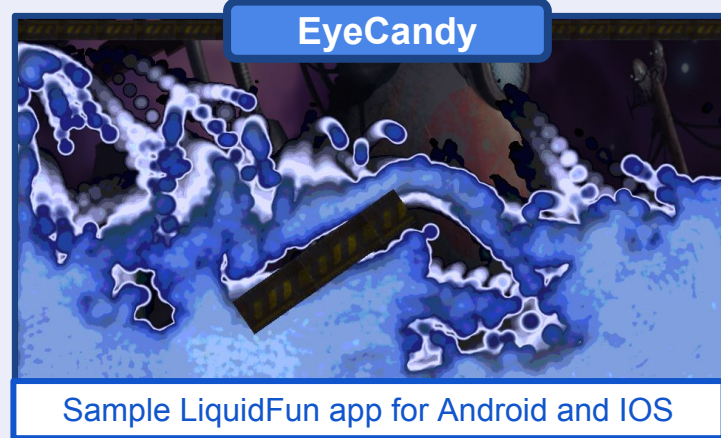
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Overview of LiquidFun

What is particle simulation?

Data structures

Simulation Algorithm



Overview of LiquidFun

- 2D rigid body and fluid simulation library
- Extension of Box2D
- Written in C++, bindings for Java, translated to JavaScript
- Runs on Android, iOS, Windows, OS X, Linux, browsers
- Distinguishing feature: particle simulation

What is particle simulation?

In particle simulation...

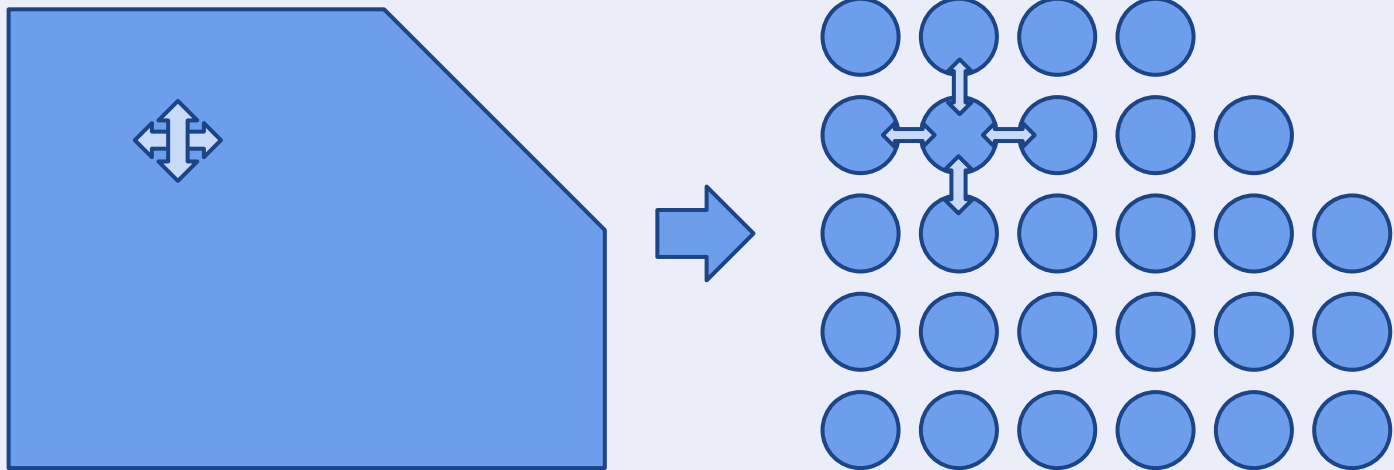
- objects are composed of particles (circles, in LiquidFun)
- physics is described by interactions between particles

Particle simulation works well with...

- Fluids--liquids and gasses

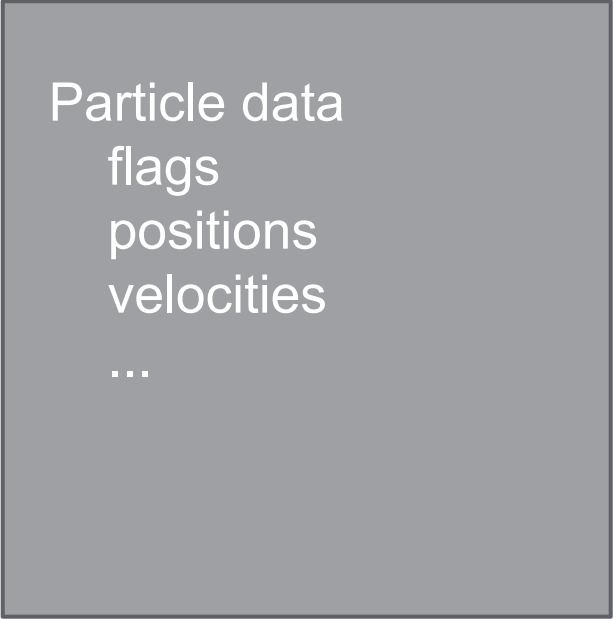
- Deformable objects

- Interactions of different materials



Particle simulation

Data structures

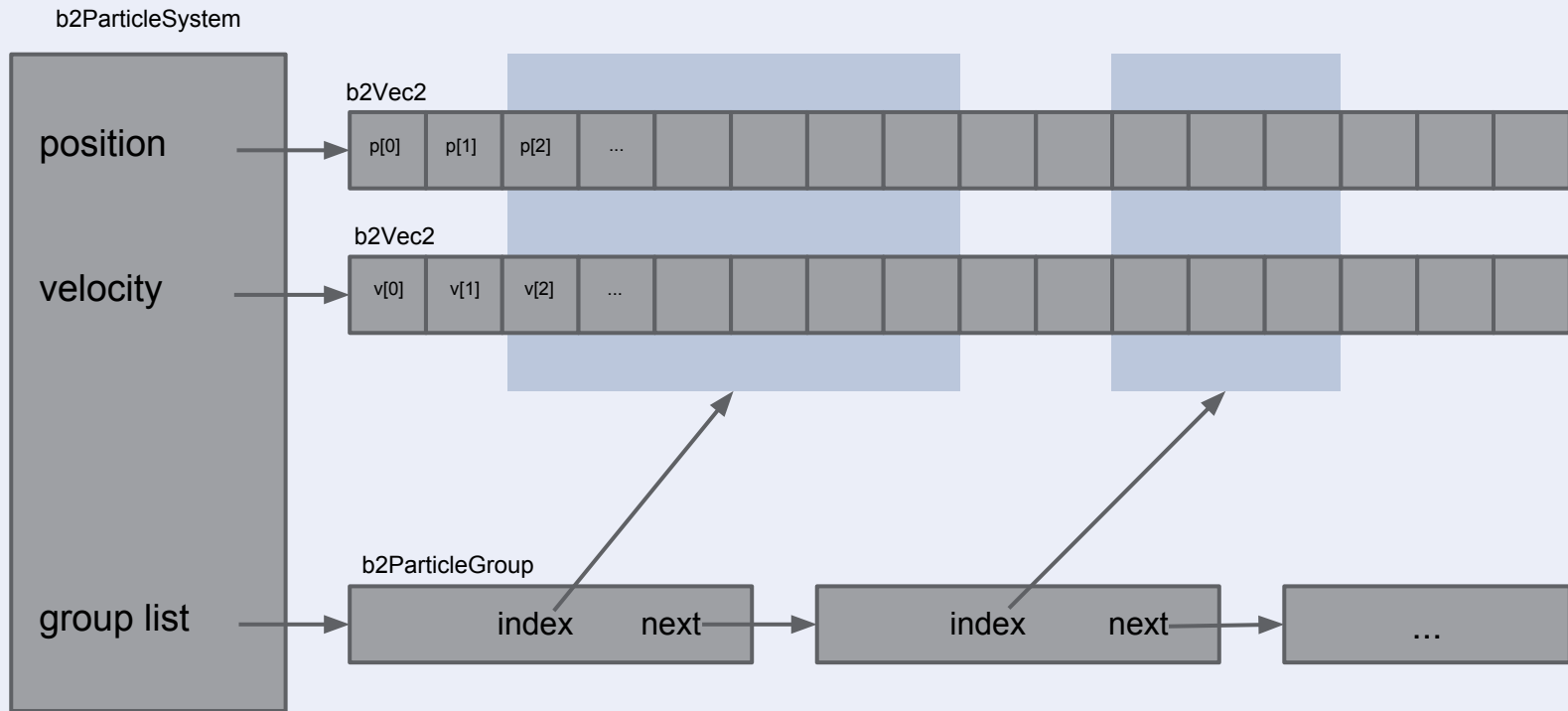


Particle data
flags
positions
velocities
...

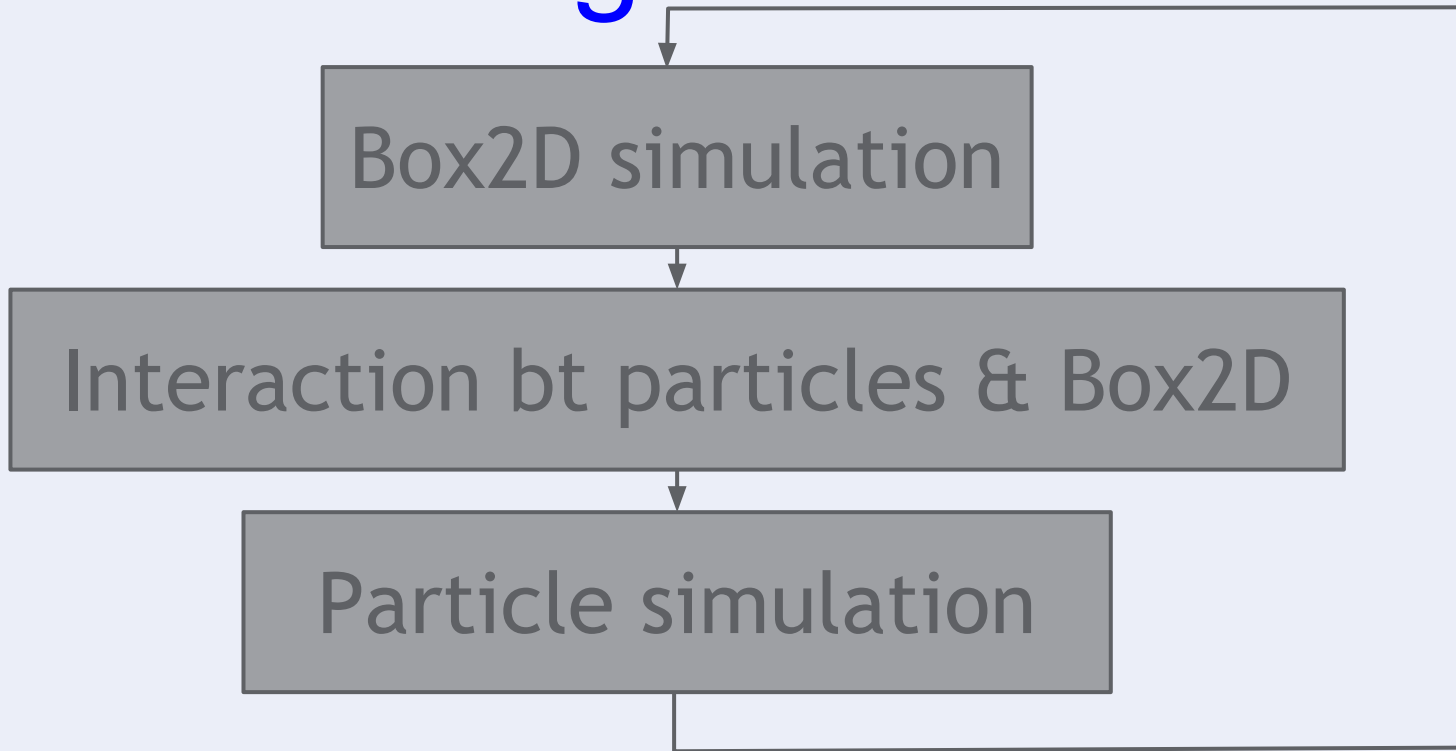


Particle group
flags
first index
last index
...

Data structures



Simulation Algorithm



Legend

$p[i]$	position of particle i
$v[i]$	velocity of particle i
Δt	simulation time step
R	particle radius
D	particle diameter = $2 \cdot R$

These symbols will be used in the next few slides.

Particle simulation

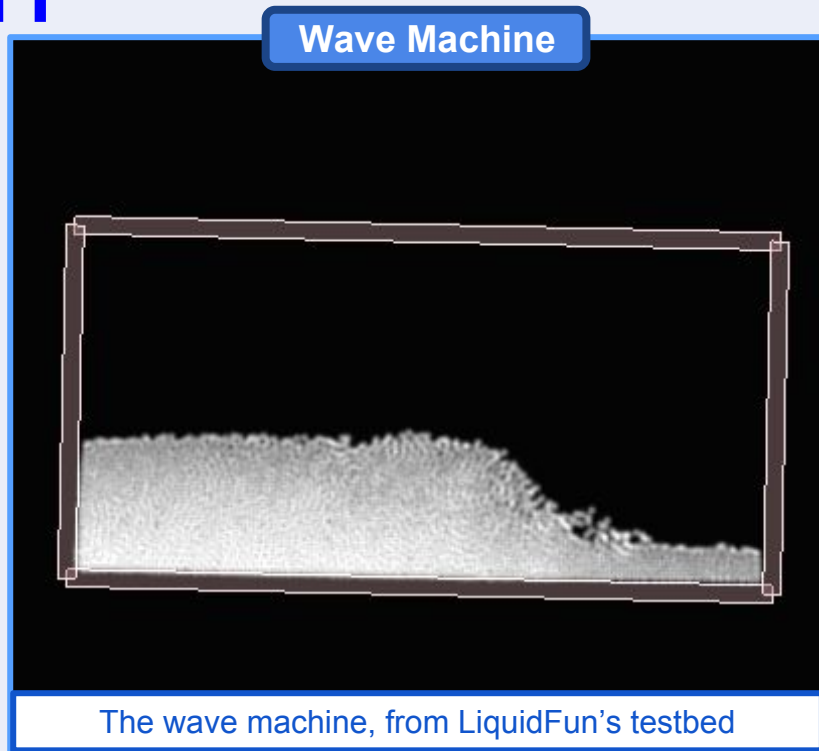
Collision detection

Apply pressure

Apply additional forces (viscous, etc.)

Restrict particle velocity (rigid, wall, etc.)

Move particles



Collision detection

Find pairs of particles closer than the particle diameter

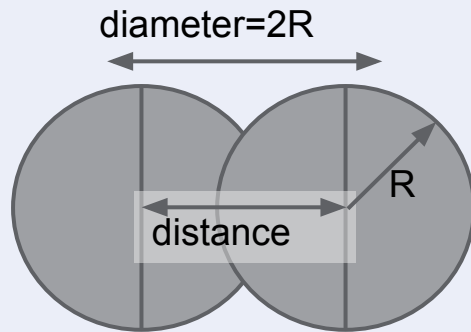
Record the following values:

i, j : indices of colliding particles

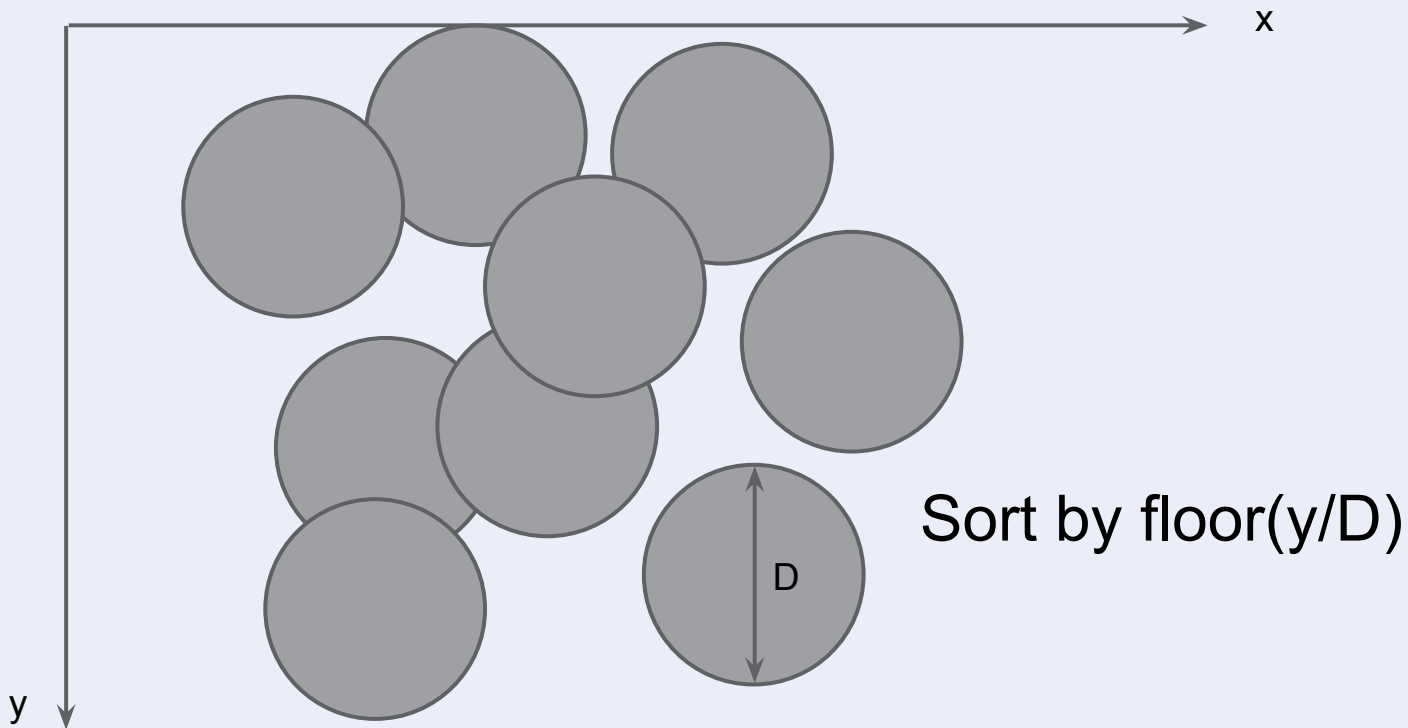
$n[i, j]$: normalized relative position

$w[i, j]$: calculated as $1 - \text{distance} / \text{diameter}$

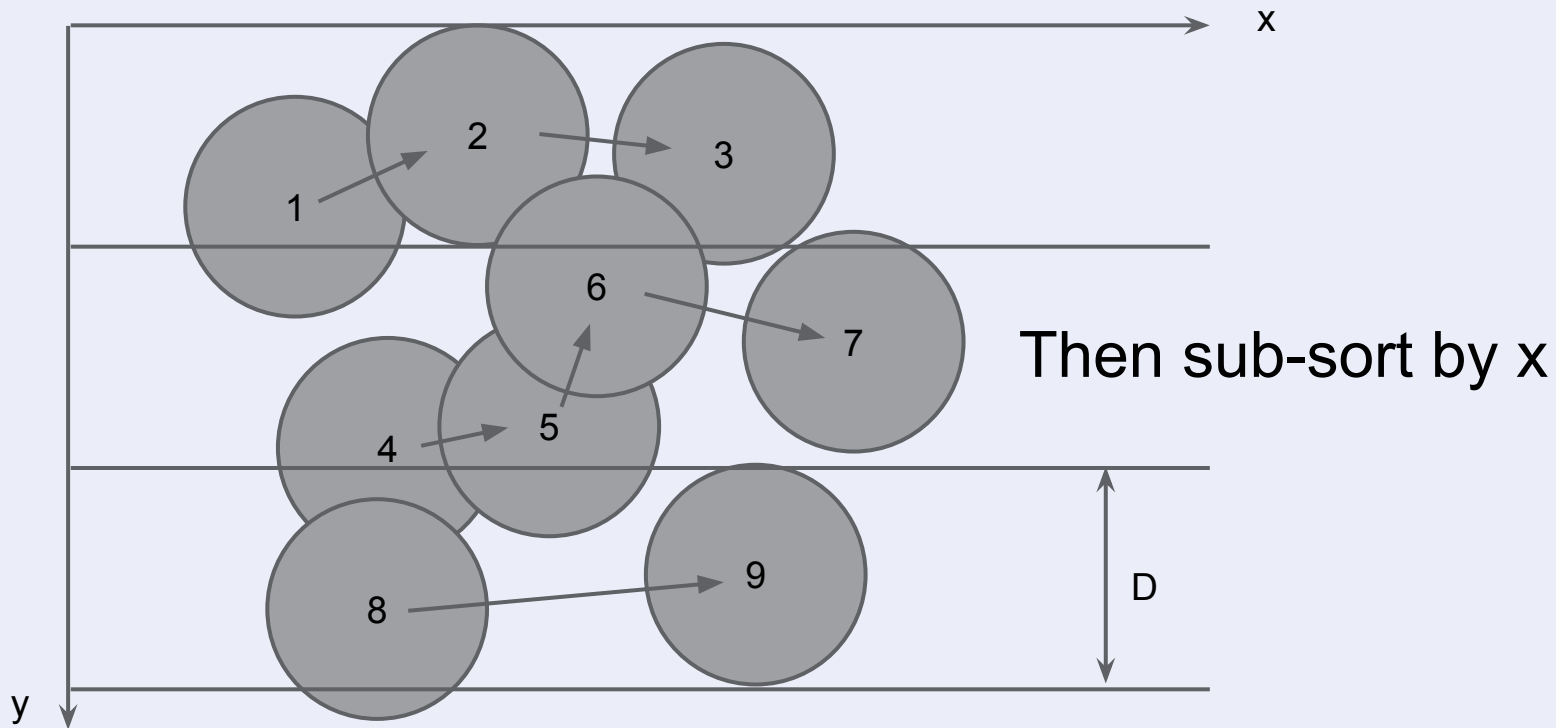
0 if barely contacting, 1 if overlapping



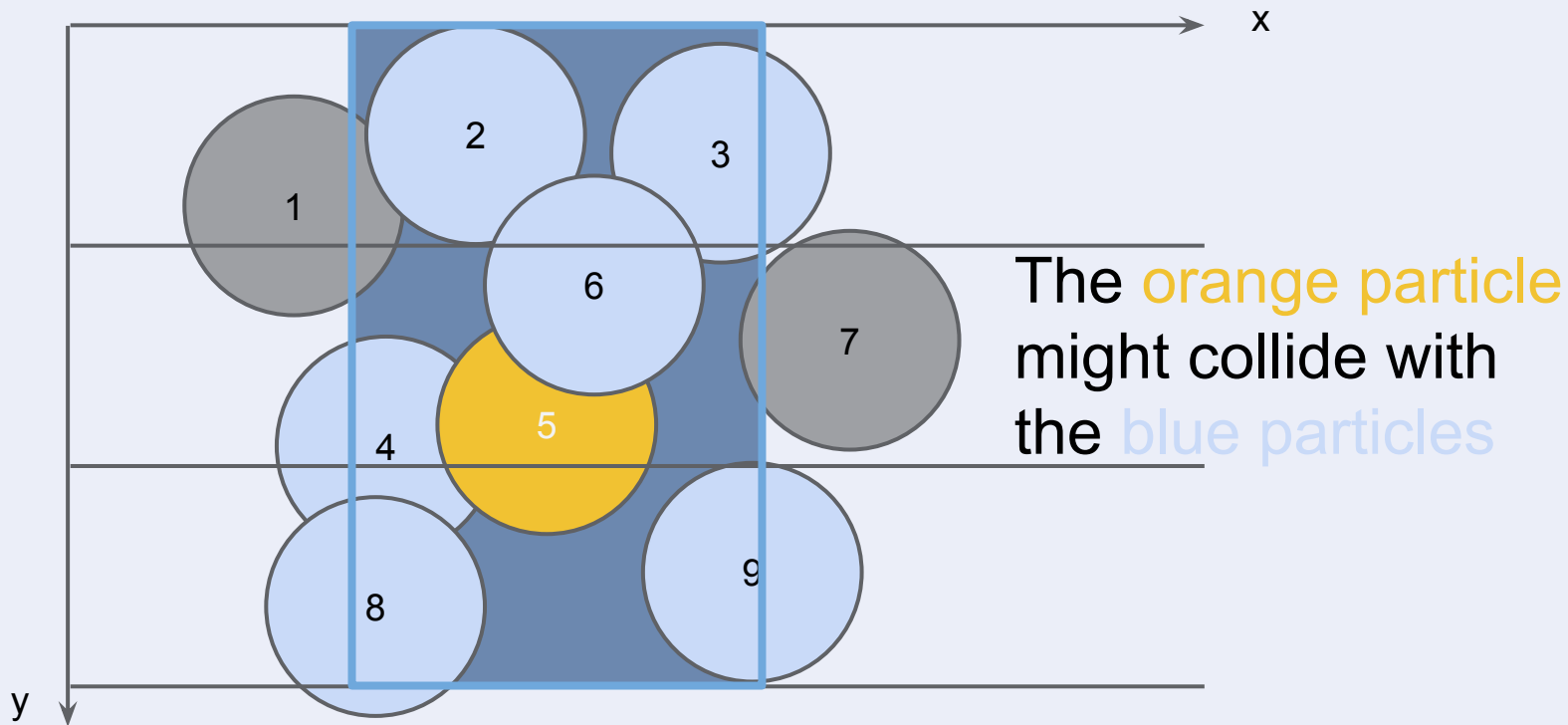
Collision detection -- particle sort



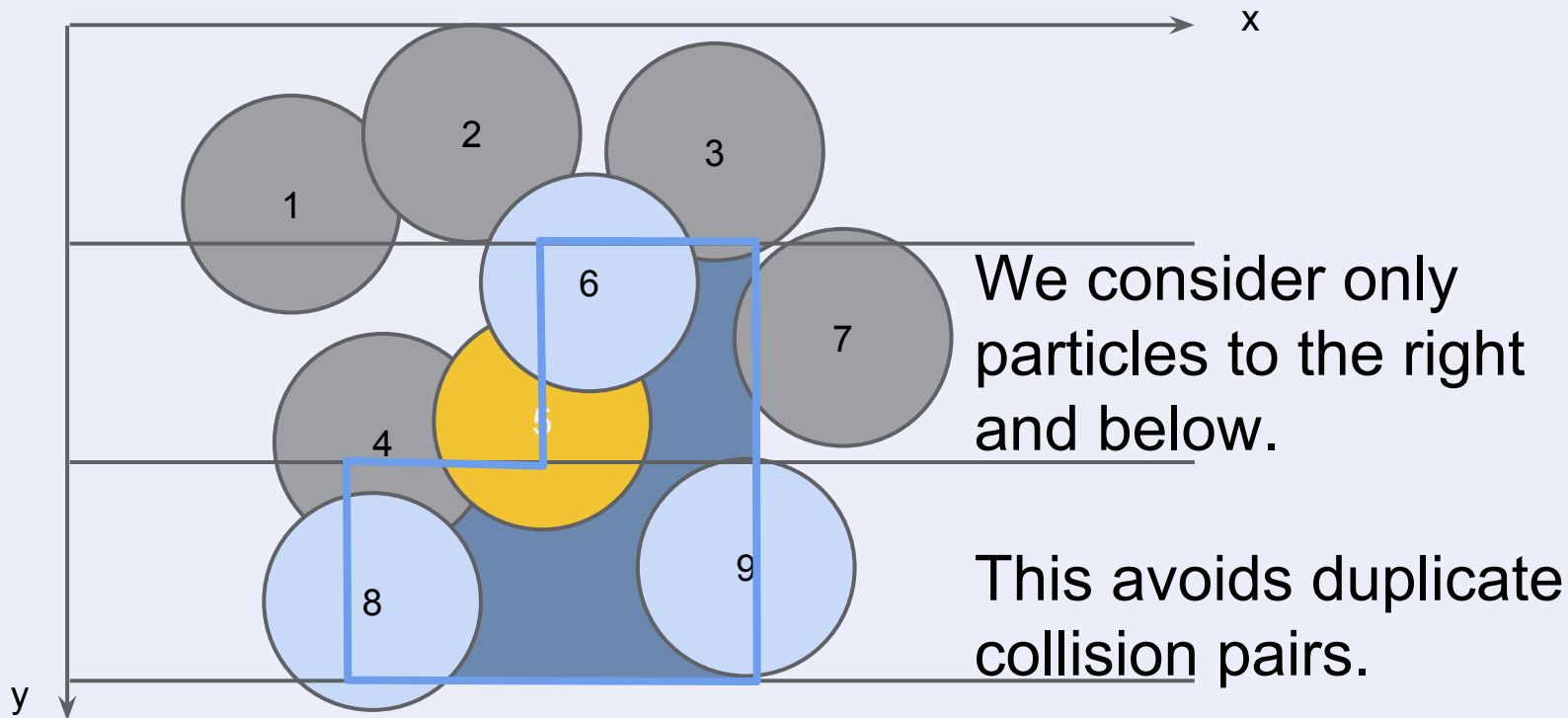
Collision detection -- particle sort



Collision detection -- broad pass collision detection



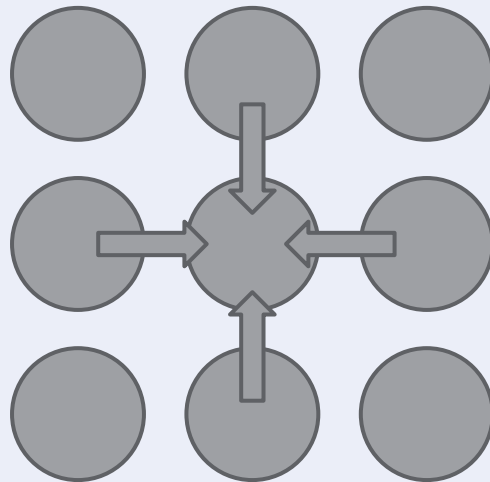
Collision detection -- broad pass collision detection



Apply Pressure

Sum up the weight of contacts for each particle

$$w[i] = \text{sum}(w[i,j],j)$$



Apply Pressure

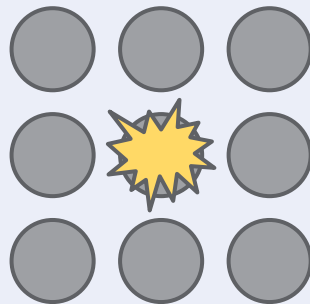
Calculate the pressure of each particle using the weight sum

$$h[i] = \max(0, \eta * (w[i] - w_0))$$

$h[i]$ pressure of particle i

η constant coefficient of weight

w_0 constant average weight

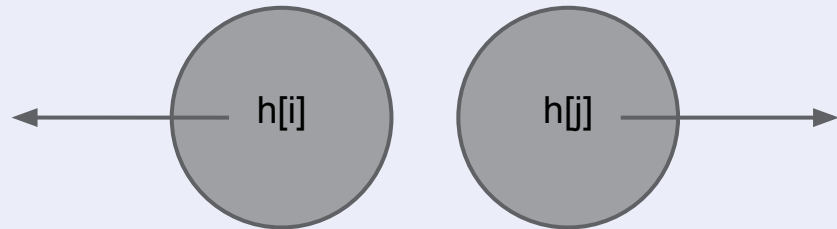


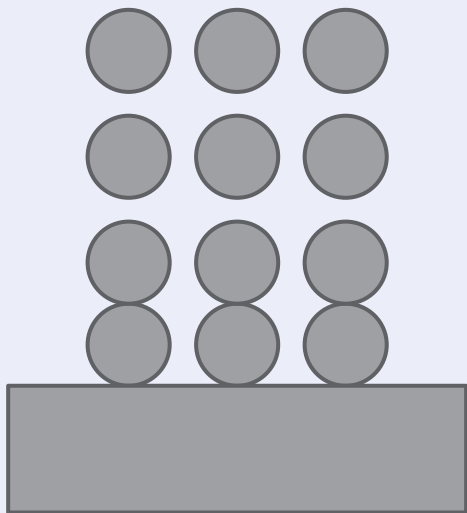
Apply Pressure

Apply a repulsive force to each contacting particle according to pressure

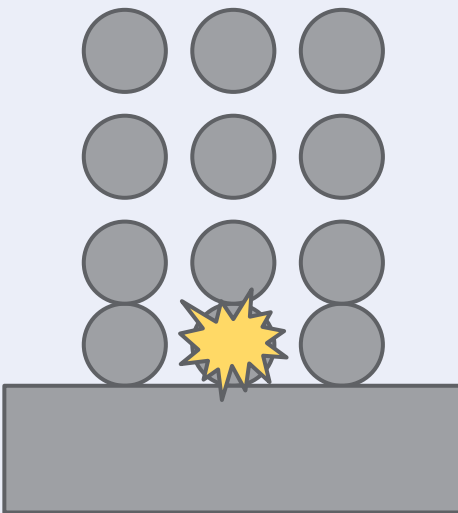
$$v[i] \leftarrow v[i] + \Delta t * a * (h[i] + h[j]) * w[i,j] * n[i,j]$$

a: constant coefficient of repulsion

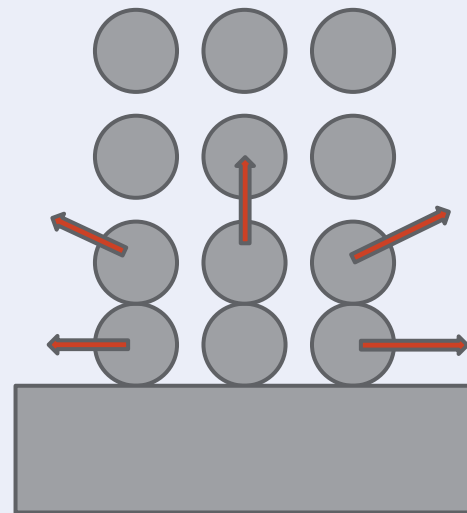




compression



pressure



force

Apply pressure

Apply Viscous Force

If a particle is viscous, mix velocity with its contacting particles

$$v[i] \leftarrow v[i] + \Delta t * \mu * (v[j] - v[i])$$

μ : constant coefficient of viscosity

Apply Spring Force

If a particle is springy, apply force to restore distance between neighboring particles

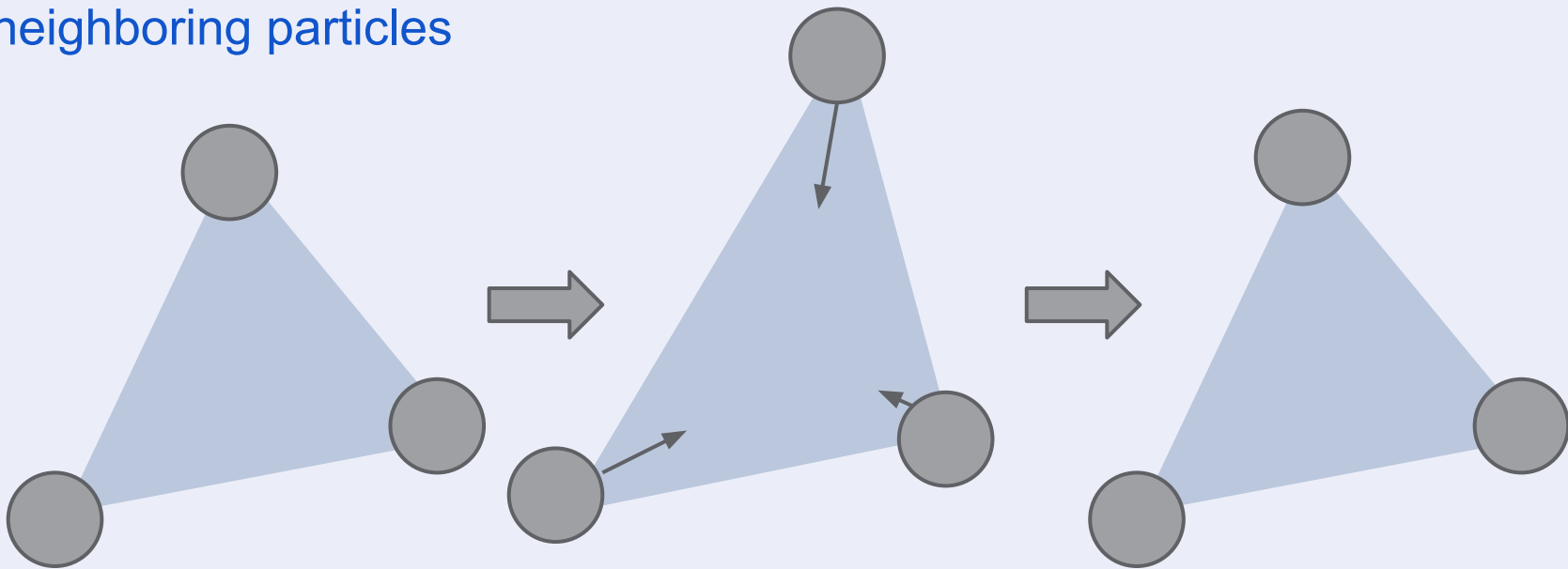
$$v[i] \leftarrow v[i] + \Delta t * k * (\text{distance}(p[j], p[i]) - L[i, j]) * n[i, j]$$

k constant spring coefficient

$L[i, j]$ initial distance

Apply Elastic Force

If a particle is elastic, apply force to restore relative positions among neighboring particles



Apply Powder Force

If a particle is powder, apply simple potential force instead of pressure

$$v[i] \leftarrow v[i] + \Delta t * c * \max(0, w[i,j] - w1) * n[i,j]$$

c: constant potential coefficient

w1: constant threshold weight

Apply Tensile Force

If a particle is tensile, apply force to simulate surface tension

$$\begin{aligned}w[i] &= \text{sum}(w[i,j], j) \\s[i] &= \text{sum}((1 - w[i,j]) * w[i,j] * n[i,j], j) \\A[i] &= a * (w[i] + w[j] - 2 * w_0) \\B[i] &= b * \text{dot}(s[j] - s[i], n[i,j]) \\v[i] &\leftarrow v[i] - \Delta t * (A[i] + B[i]) * n[i,j]\end{aligned}$$

a, b : constant coefficients
 w_0 : constant average weight

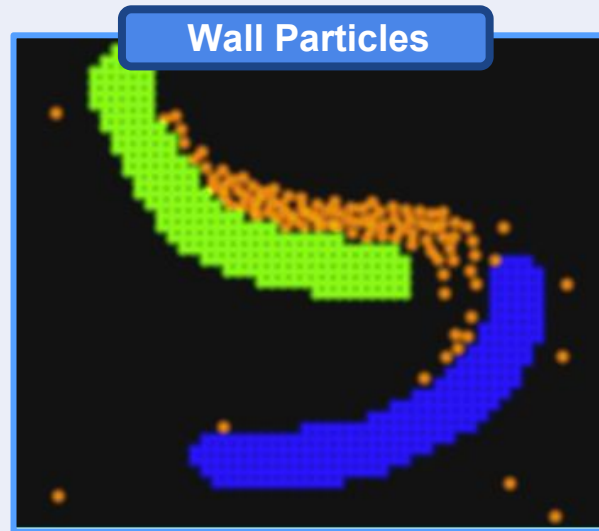
Tensile Particles



Restrict Particle Velocity

For wall particles, set velocity to zero.

$$v[i] \leftarrow 0$$



Restrict Particle Velocity

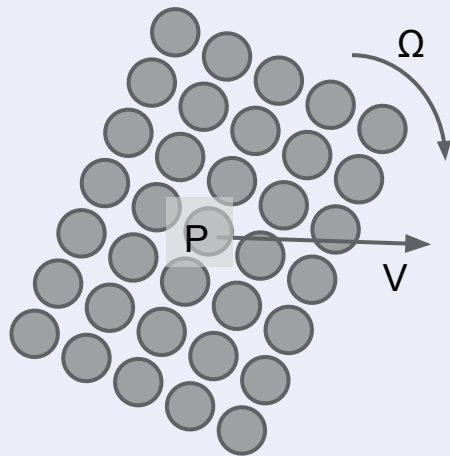
For particles in a rigid group, set velocities to maintain relative positions.

$$v[i] \leftarrow V + \text{cross}(\Omega, p[i] - P)$$

V : linear velocity of the group

Ω : angular velocity of the group

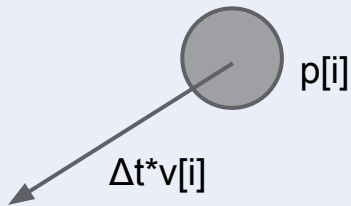
P : center of mass of the group



Move Particles

Use velocity to update particle positions

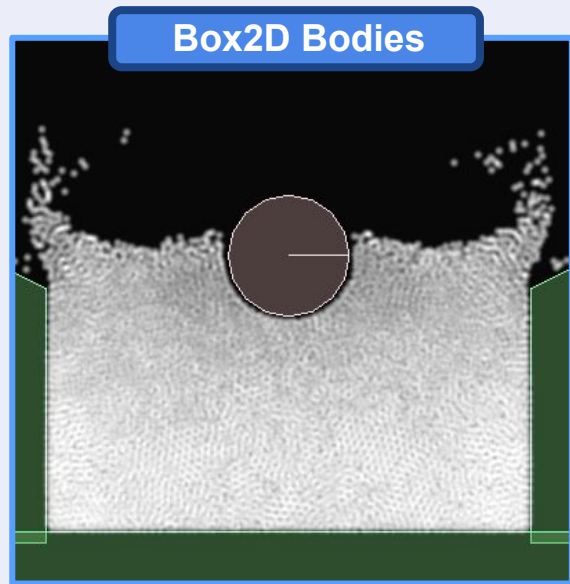
$$p[i] \leftarrow p[i] + \Delta t * v[i]$$

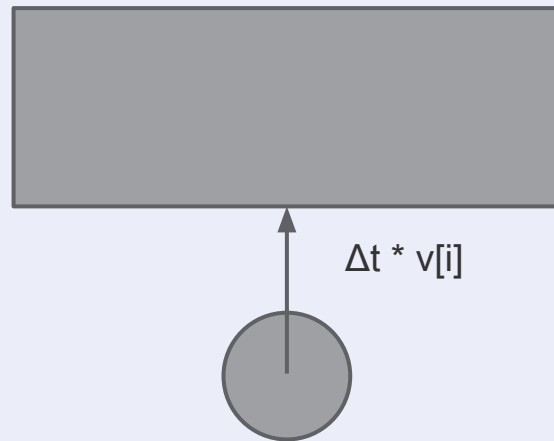
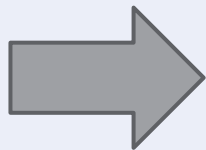
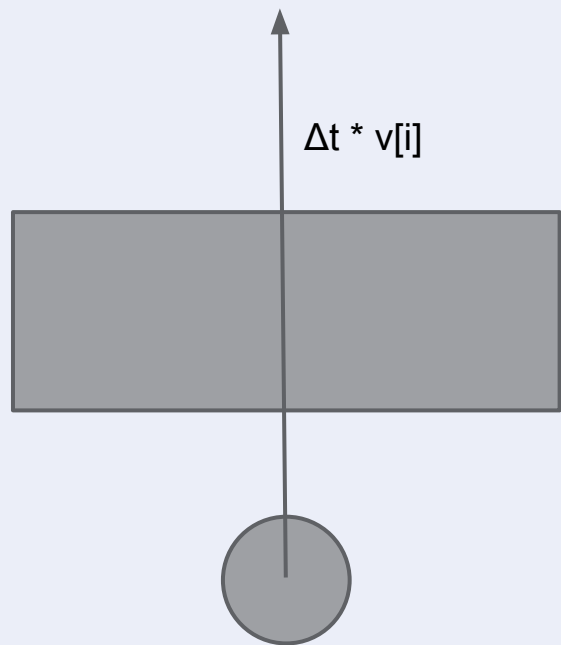


Interaction with Box2D

Prevent penetration:

If a particle is about to penetrate a Box2D body during this step, stop the particle at the surface

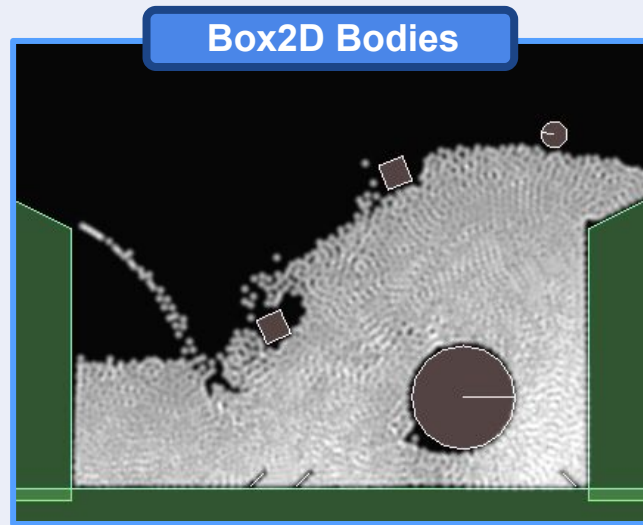


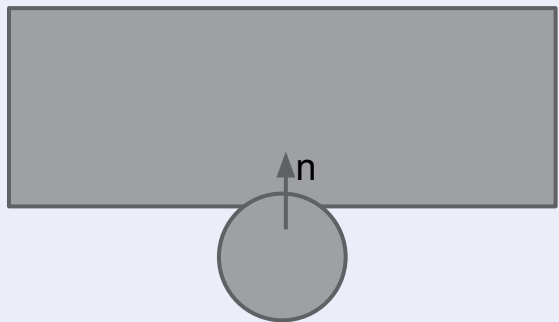


Prevent penetration

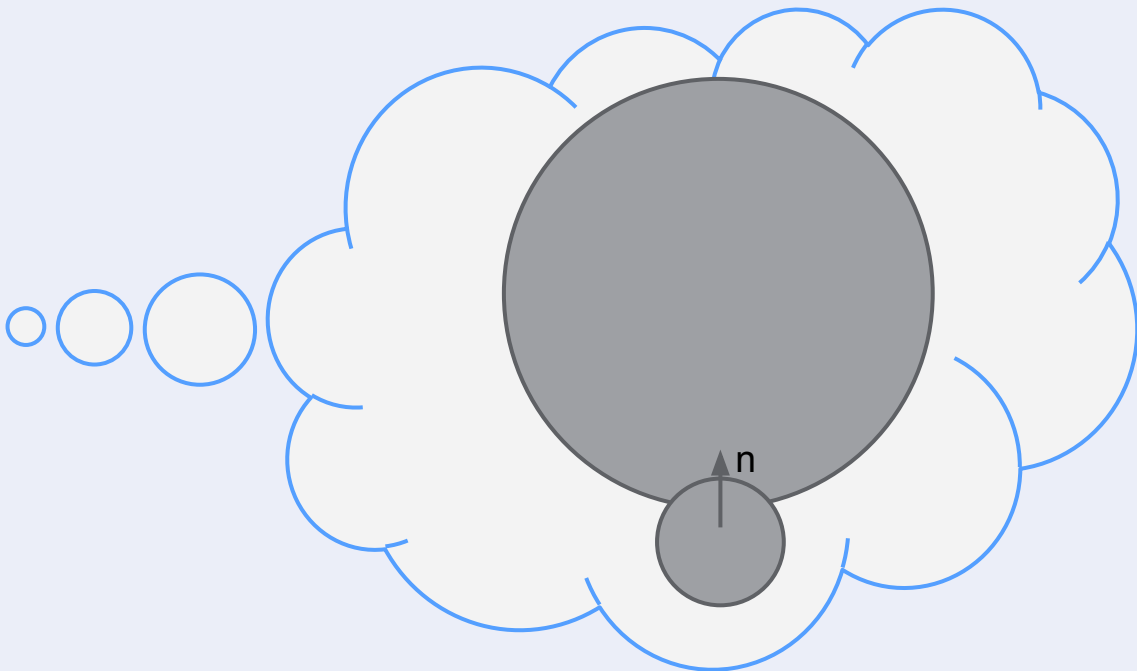
Interaction with Box2D

If a particle is in contact with a Box2D body, execute the subsequent particle simulation as if the particle is in contact with another particle





Continuous contact



contact with a pretend particle

Summary

- Particle systems are suitable for fluids, deformable objects, and interactions between different materials
- Collision testing is made tractable by ordering the particles top-to-bottom, left-to-right
- Viscous, spring, elastic, powder, and tensile forces can be added to create different kinds of particles