

# gradient descent for multi-variable functions

## Problem 1

$$J(\theta_1, \theta_0) = \theta_1^2 + \theta_0^2 + 2$$

$$\alpha = 0.25, \quad \text{initial point } \begin{bmatrix} \theta_0 = 2 \\ \theta_1 = 4 \end{bmatrix}, \quad 10 \text{ iterations}$$

Write a Matlab script that will help you find an approximation for  $\begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$  that minimizes  $J(\theta_1, \theta_0)$ , given the above  $\alpha$  and initial point and number of iterations.

What is your guess? Looking at the progression of  $\begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$  values, what point do you think actually minimizes  $J(\theta_1, \theta_0)$ ?

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## Problem 2

$$J(\theta_1, \theta_0) = 38\theta_1^2 + 3\theta_0^2 + 20\theta_1\theta_0 - 42\theta_1 - 12\theta_0 + 14$$

$$\alpha = 0.01, \quad \text{initial point } \begin{bmatrix} \theta_0 = 1.5 \\ \theta_1 = 0.5 \end{bmatrix}, \quad 5 \text{ iterations}$$

Write a Matlab script that will help you find an approximation for  $\begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$  that minimizes  $J(\theta_1, \theta_0)$ , given the above  $\alpha$  and initial point and number of iterations.

What is your guess? Looking at the progression of  $\begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$  values, what point do you think actually minimizes  $J(\theta_1, \theta_0)$ ?

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### Problem 3

$$J(\theta_2, \theta_1, \theta_0) = \theta_2^2 + 0.25\theta_1^2 + 3\theta_0^2 + 2\theta_2\theta_0 + \theta_1\theta_0 - 2\theta_0 + 3$$

$$\alpha = 0.2, \quad \text{initial point } \begin{bmatrix} \theta_0 = 3 \\ \theta_1 = 4 \\ \theta_2 = 5 \end{bmatrix}, \quad 100 \text{ iterations}$$

Write a Matlab script that will help you find an approximation for  $\begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \end{bmatrix}$  that minimizes  $J(\theta_2, \theta_1, \theta_0)$ , given the above  $\alpha$  and initial point and number of iterations.

What is your guess? Looking at the progression of  $\begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \end{bmatrix}$  values, what point do you think actually minimizes  $J(\theta_2, \theta_1, \theta_0)$ ?

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