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## 1. Summary

- Our goal is to develop a robust object detection system to detect faces with or without occlusions in real time.
- Particularly, we address the following problems:
  - How to derive an appropriate boosting algorithm for face detection?
  - How to represent non-face training data for reducing false positives?
  - How to handle occlusions without compromising in efficiency?
- Our contributions
  - A *soft-boost* technique combining Bhattacharyya weak learners with soft margins.
  - A *reinforcement* training procedure to reduce false-positive rates by uniformly stage-wise adding non-face training data.
  - An *evidence cascading* approach to distinguish occluded faces from non-face patterns.

## 2. Boosting with Soft Margins

- Notations:
  - $L$  training data:  $D = \{(\mathbf{x}_i, y_i), \dots, (\mathbf{x}_l, y_l)\} = D^+ \cup D^-$ .
  - Strong classifier:  $H(\mathbf{x}) = \text{sign}(f(\mathbf{x})) = \text{sign}(\sum_{i=1}^T \alpha_i h_i(\mathbf{x}))$ .
  - Weight distribution at the  $r$ th iteration:  $\mathbf{w}_r = (w_r(1), \dots, w_r(l))$ .

- An error upper bound for AdaBoost:

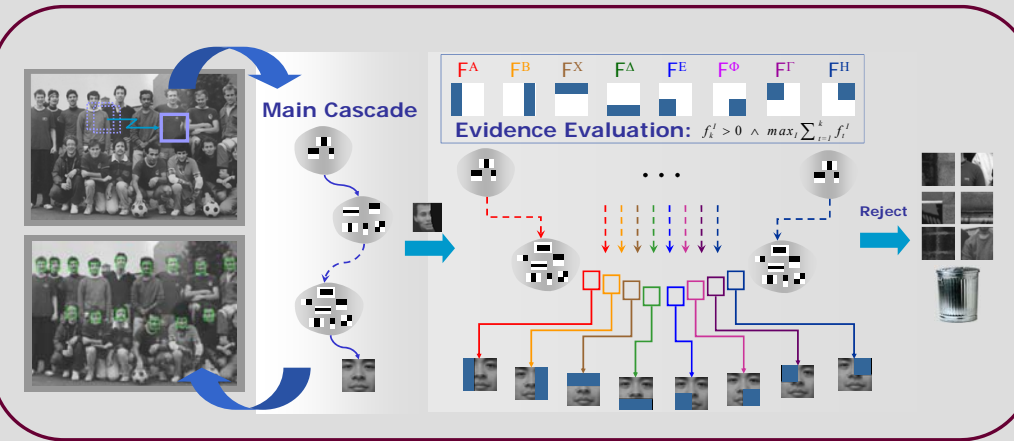
$$\frac{1}{l} \sum_{i=1}^l \frac{1}{2} |y_i - H(\mathbf{x}_i)| \leq \frac{1}{l} \sum_{i=1}^l \exp(-y_i f(\mathbf{x}_i)) = \prod_{i=1}^T Z_i,$$

where  $Z_i = \sum_{j=1}^m w_j(i) \exp(-\alpha_j y_i h_j(\mathbf{x}_i))$ .

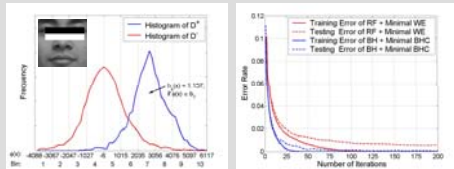
### 2.1 Bhattacharyya (BH) Weak Learners

- We start with a set of projection directions,  $\Phi = \{\phi_i\}_{i=1}^m$ .
  - $\phi$  is uniquely defined by a *Rectangle Feature* (RF).
  - $\phi$  defines a histogram of  $D$  over a partition of  $m$  equal-size bins  $\{b_k\}_{k=1}^m$ .
- Define  $\mathbf{i}_k(\phi)$  as indexes of training  $D$  data being projected by  $\phi$  into bin  $b_k$ , i.e.,  $\mathbf{i}_k(\phi) = \{i | \mathbf{x}_i \in D, \phi(\mathbf{x}_i) \in b_k\}$ . Analogously,  $\mathbf{i}_k^+(\phi)$  and  $\mathbf{i}_k^-(\phi)$  are defined for  $D^+$  and  $D^-$ , respectively.
- The values of the weighted positive and negative histograms in bin  $b_k$  can be evaluated by:  $p_k^+(\phi) = \sum_{i \in \mathbf{i}_k^+(\phi)} w(i)$  and  $p_k^-(\phi) = \sum_{i \in \mathbf{i}_k^-(\phi)} w(i)$ .
- Suppose  $h_\phi(\mathbf{x}) = s_k$  (for some bin  $b_k$ ). Then, we have
 
$$Z = \sum_{i=1}^m \sum_{k=1}^m w(i) \exp(-\alpha y_i s_k).$$

$$\frac{dZ}{ds_k} = 0 \Rightarrow s_k^* = \frac{1}{\alpha} \ln \sqrt{p_k^+(\phi) / p_k^-(\phi)}$$
 and  $Z^* = 2 \sum_{k=1}^m \sqrt{p_k^+(\phi) p_k^-(\phi)}$ .
- Summarize the observations as follows.
  - The *goodness* of a weak learner  $h_\phi$  can be measured by its corresponding Bhattacharyya Coefficient.
  - We can *re-scale*  $h_\phi$  by multiplying with  $\alpha$  such that the selection of weak learner and its coefficient can be decided *simultaneously*.
  - A weak learner  $h_\phi$  of coefficient 1 can be defined by projection  $\phi$ :
 
$$h_\phi(\mathbf{x}) = \ln \sqrt{p_k^+(\phi) / p_k^-(\phi)}, \text{ for all } \mathbf{x} \in D \text{ and } \phi(\mathbf{x}) \in b_k.$$

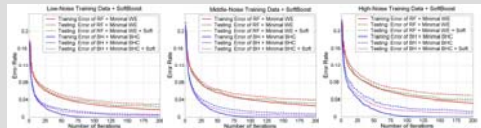


### 2.2 BH Learners vs. Rectangle Features

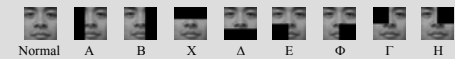


### 2.3 SoftBoost

- Some observations:
  - While the data become noisier, the gaps (overfitting) between training and testing error become larger.
  - The noisier the data, the larger performance difference between the two resulting classifiers (RF and BH).
  - For the classifier using BH weak learners, the problem of overfitting is more serious.
- We apply LP<sub>Reg</sub>-AdaBoost (Rätsch et al., 2001) to achieve soft margins via linear programming.
  - While the data are noisier or the number of iterations are increasing, the improvements are appreciable.
  - Furthermore, the improvements for RF are even more noticeable!



## 3. Detecting Faces with Occlusions



- To detect occluded faces, adopting a more lenient policy solves this problem to some degree, but the false positive rates increase.
- A naïve approach is to train a view-based system, i.e., train one detector for each type of occluded faces. → time-consuming.

### 3.1 Reinforcement Training

- Reinforcement training is used for a boosted cascade.
- A large number of false positives are often generated in the earlier stages of a cascade. At each stage, we use *k-means clustering* to divide false positives from the latest sub-cascade into 6 clusters, and uniformly select non-face training data from each cluster.

### 3.2 Evidence Cascading

- Distinguishing a rejected occluded face from non-face patterns is vital in our approach---The clues lie in the *evidence* left behind when a testing sample is rejected.
- Let  $O_I$  denote the occluded region of the type-I occluded faces. We define the largest subset of  $\Phi$  disjoint from  $O_I$  by:
 
$$\Phi_I = \{\phi | \phi \in \Phi \text{ and } \phi \cap O_I = \emptyset\}, \text{ for } I = A, B, \dots, H.$$
- The *evidence* of a testing pattern  $\mathbf{x}$  at the  $k$ th stage is defined by

$$\mathbf{e}_k(\mathbf{x}) = (f_k^A(\mathbf{x}), f_k^B(\mathbf{x}), \dots, f_k^H(\mathbf{x})) \text{ and } f_k^I(\mathbf{x}) = \sum_i \beta_i h_i(\mathbf{x}).$$

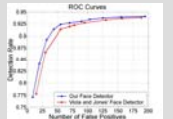
where  $\sum_i$  involves only those weak learners that the involving projections do not intersect with  $O_I$ .

- The main ideas of *cascading-with-evidence*:
  - The main cascade  $M$  is designed to replace the original cascade detector. Besides the frontal faces detection,  $M$  also stage-wise accumulates evidence, which is useful when a pattern is rejected.
  - Since each  $\beta_i h_i(\mathbf{x})$  has been evaluated in the computation of  $H_k(\mathbf{x})$ , the evidence vector  $\mathbf{e}_k(\mathbf{x})$  is *easier to derive*.
  - Assume a type-A occluded face  $\mathbf{x}$  is rejected at stage  $k$ . The positive response of  $f_k^A(\mathbf{x})$  in evidence indicates  $\mathbf{x}$  as a type-A occluded face. Such a property is *not shared* by most true non-face samples.
  - Unlike a view-based system, only patterns with positive responses are dispatched into the corresponding detectors.

## 4. Experimental Results

- The regular cascade to detect frontal faces contains 21 stages with 872 BH weak learners.
- 10,000 face samples and 10,000 non-face samples are used in training.
- Averagely, a pattern is classified by 5.36 BH weak learners.
- The main cascade contains 18 stages. Each occluded cascade contains from 23 to 28 stages.
- Since a BH weak learner may be associated with more than one type, the number of weak learners in each stage of main cascade is still *manageable*.
- The first three stages of  $M$  consist of 7, 9, 12 weak learners respectively.
- Our system is more robust to detect faces with exaggerated expressions, since only partial information is extracted to detect faces in occluded cascades.

Stage	1	2	3	4
Weak learner #	2	4	5	8
Passing rate (PR)	35.8	39.2	40.5	41.7
Cumulative PR	35.8	14.0	5.7	2.4



### 4.1 Detection Results

