Value Iteration

In each of the paths, arrows represent which direction the agent chooses to move.

Case I: No Wind

i. Value Function

-6	-5	-4	-3	-3	-3	-3
-6	-5	-4	-3	-2	-2	-2
-6	-5	-4	-3	-2	-1	-1
-6	-5	-4	-3	-2	-1	0
-6	-5	-4	-3	-2	-1	-1
-6	-5	-4	-3	-2	-2	-2
-6	-5	-4	-3	-3	-3	-3

ii. Following the optimal policy from (3, 0)

One path to follow is: $(3,0) \to (3,1) \to (3,2) \to (3,3) \to (3,4) \to (3,5) \to (3,6)$

Another possible path to follow is: $(3,0) \land (2,1) \rightarrow (2,2) \lor (3,3) \rightarrow (3,4) \rightarrow (3,5) \rightarrow (3,6)$

Case II: Light Wind

i. Value Function

-6	-6	-6	-6	-5	-4	-3
-6	-5	-5	-5	-4	-3	-2
-6	-5	-4	-4	-3	-2	-1
-6	-5	-4	-3	-2	-1	0
-6	-5	-4	-3	-2	-1	-1
-6	-5	-4	-3	-2	-1	-2
-6	-5	-4	-3	-2	-2	-2

ii. Following the optimal policy from (3, 0)

One path to follow is: $(3,0) \to (3,1) \to (3,2) \to (3,3) \setminus (3,4) \setminus (3,5) \setminus (3,6)$

Another possible path to follow is: $(3,0) \lor (4,1) \rightarrow (4,2) \rightarrow (4,3) \lor (4,4) \rightarrow (3,5) \lor (3,6)$

Case III: Strong Wind

i. Value Function

-9	-8	-7	-6	-5	-4	-3
-8	-8	-7	-6	-5	-4	-2
-7	-7	-7	-6	-5	-3	-1
-6	-6	-6	-6	-4	-2	0
-6	-5	-5	-5	-3	-1	-1
-6	-5	-4	-4	-2	-1	-2
-6	-5	-4	-3	-2	-1	-2

ii. Following the optimal policy from (3, 0)

One path to follow is: $(3, 0) \lor (4, 1) \lor (5, 2) \lor (6, 3) \lor (5, 4) \lor (4, 5) \lor (3, 6)$

This is the only possible path following the optimal policy