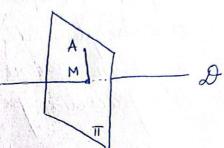
## Teminar 13 AGO

Geometrie analitica euclidiana §1) Arii, volume, distante, unghuiri

· dist 
$$(A, D) = \frac{\|\overrightarrow{AB} \times \overrightarrow{AC}\|}{\|\overrightarrow{BC}\|}$$
,  $B, C \in \mathcal{D}$  sau

dist 
$$(A,D) = dist(A,M)$$
,  
unde  $\pi \perp D$ ,  $A \in \pi$   
 $\partial \cap \pi = \{M\}$ 

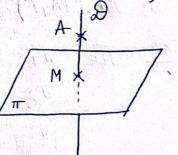


• 
$$V_{ABCD} = \frac{1}{6} |\Delta|$$
,  $\Delta = \begin{vmatrix} a_1 & a_2 & a_3 & 1 \\ b_1 & b_2 & b_3 & 1 \\ c_1 & c_2 & c_3 & 1 \\ d_1 & d_2 & d_3 & 1 \end{vmatrix}$ 

• 
$$A_1B_1C_1\Delta$$
 roplanare  $\iff \Delta = 0$ .

. dist 
$$(A_1\pi) = \frac{|a_{44} + b_{42} + c_{43} + d|}{\sqrt{a^2 + b^2 + c^2}}$$
,  $\pi \cdot a_{44} + b_{42} + c_{43} + d = 0$ 

sau dist 
$$(A, \pi) = \text{dist}(A, M)$$
,  
unde  $A \in \mathcal{D}$ ,  $\mathcal{D} \perp \pi$ ,  $\mathcal{D} \cap \pi = \{M\}$ .



inde 
$$\mathcal{D}_{1}, \mathcal{D}_{2}$$
 =  $\frac{|\angle AB|}{|AB|}, N > 1$ ,

unde  $\mathcal{D}_{1}, \mathcal{D}_{2}$  drepte necoplanare,  $A \in \mathcal{D}_{1}, \mathcal{U} = \mathcal{U}_{2}$ ,

 $N = \mathcal{U} \times \mathcal{V}$ 

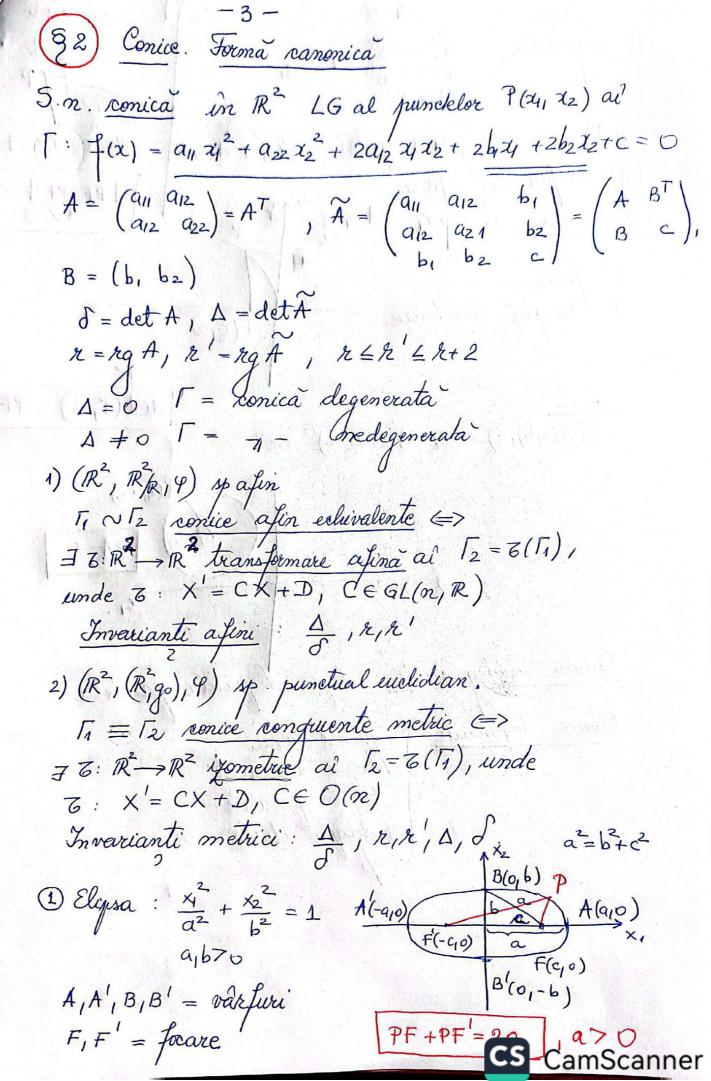
• 
$$+(\mathfrak{D}_{1},\mathfrak{B}_{2}) = +(\mathfrak{U}_{1},\mathfrak{U}_{2}) = +\varphi \in [0,T]$$
 $\cos \varphi = \frac{\angle \mathfrak{U}_{1},\mathfrak{U}_{2}}{\|\mathfrak{U}_{1}\|\|\mathfrak{U}_{2}\|}$ , unde  $\mathfrak{D}_{K} = \text{dreapta}$  orientata de  $\mathfrak{U}_{K}$ ,  $K = |i|^{2}$ 

•  $+(\pi_{1},\pi_{2}) = +(N_{1},N_{2}) = +\varphi$ 
 $\cos \varphi = \frac{\angle N_{11},N_{2}}{\|N_{1}\|\|.\|N_{2}\|}$ , unde  $\pi_{K} = \text{plan orientat}$  de  $N_{K}$ ,  $K = |i|^{2}$ 

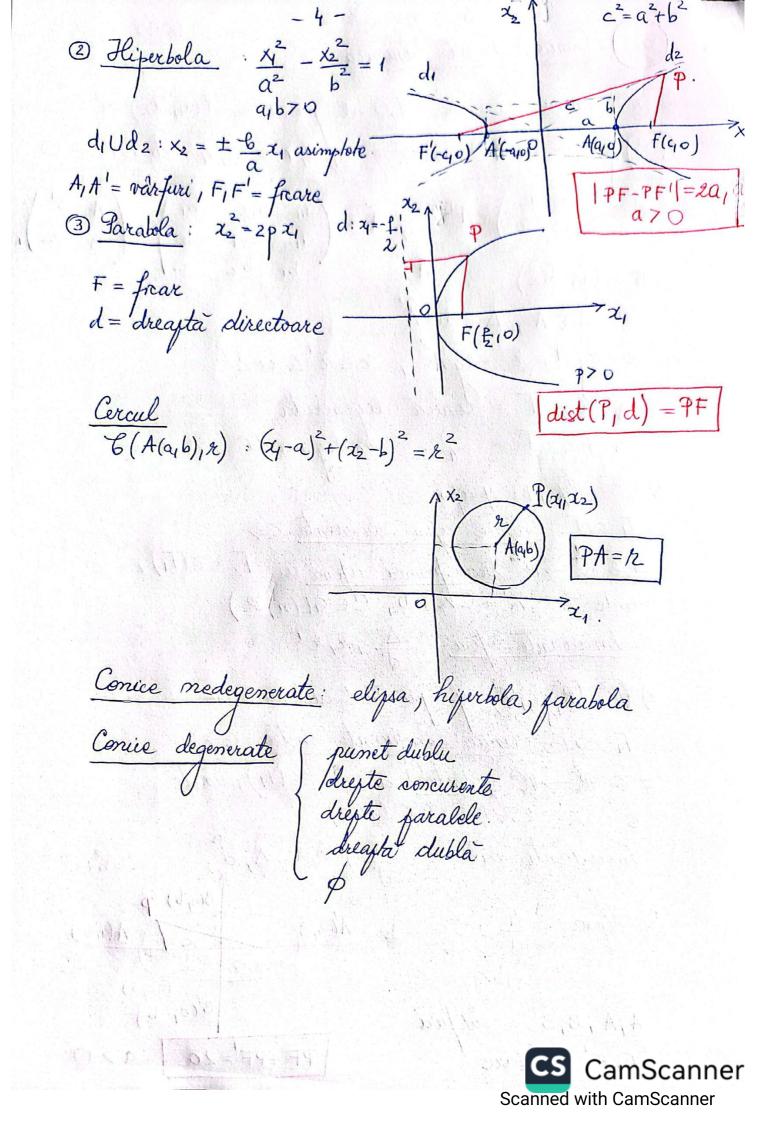
•  $+(\mathfrak{D}_{1},\pi) = +(\mathfrak{D}_{1},\mathfrak{D}_{1}') = +\varphi$ 
 $\mathfrak{D} = \text{dreapta}$  orientata de  $N_{1}$ 
 $\mathfrak{D}' = \text{proceetia}$   $p \in \pi$  a lui  $\mathfrak{D}$ .

[\$\frac{\partial\_{1}}{R\_{1}^{2}} \frac{\partial\_{2}}{\partial\_{1}} \frac{\partial\_{2}}{\partial\_{1}} \frac{\partial\_{2}}{\partial\_{2}} \frac{\partial\_

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Po s.n. centru gt F €> [YPEF ⇒ JPO(P)€ []  $d \neq 0 \Rightarrow \Gamma$  are rentru unic.  $\mathcal{P}_0(x_1^0, x_2^0)$  $\int f(x_1, x_2) = \frac{\Delta}{\delta}$ (I) Adurerea la f. canonica gt 0 +0 1 (R, R/R, 4) sp. afin.  $\mathcal{R} = \{0; q_1, e_2\} \xrightarrow{\Phi} \mathcal{R}' = \{P_0; e_1, e_2\} \xrightarrow{E} \mathcal{R}'' = \{P_0; q_1, e_2\}$ translatie a)  $\theta = X = X' + X_0$ .  $X_0 = \begin{pmatrix} \chi_1^0 \\ \chi_2^0 \end{pmatrix}$ ,  $P_0 = \text{centru}$ :  $\begin{cases} \frac{2+}{2} = 0 \\ \frac{2+}{2} = 0 \end{cases}$  $\theta (\Gamma) \cdot X^{\prime T} A X^{\prime} + \frac{A}{\sim} = 0$ b) Q: R² → R, Q(x) = XTAX forma fatratica Aducem Q la o forma canonica (met Gauss/Jacobi)  $Q(x) = \lambda_1 x_1^{2} + \lambda_2 x_2^{2}$  $G \cdot X' = CX'', C \in GL(2,\mathbb{R})$ Deci: To O(T): X = CX" + Xo (transf. afina) TNF afin echivalente  $700 + (\Gamma) = \lambda_1 x_1'' + \lambda_2 x_2'' + \Delta = 0.$ (2) (R2,90), 9) sp. punctual enclidian. a) Analog en kazul 1 6)  $Q: RO \longrightarrow R$ ,  $Q(x) = X'^T A X$ I un reper ortonormat format din versori proprii al Adiag P(X) = det (A - X Iz) = (0. =) 21/2 ex = ( lk, mk It det R=1 => refer

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6: X = RX " izometrie (det R=1 → speta 1) 30θ(Γ)=Γ : λ14"+22"+ <u>Δ</u>=0 Γ≡Γ rongruente metric. T = RX'' + XO,  $R \in SO(2)$ ,  $\left( \text{det } R = 1 \right)$  $\mathcal{R} \xrightarrow{\phi} \mathcal{R}' \xrightarrow{\delta} \mathcal{R}''$  rysere ortonormate translatie rotatie EX5  $(R^2, (R^2, g_0), \varphi)$  $\int : f(x_1 x_2) = 5x_1 + 8x_1 x_2 + 5x_2 - 18x_4 - 18x_2 + 9 = 0$ La se aduca ka o forma canonica, efectuand izometrii. Regregentare grafida EX6 Fie conica:  $\Gamma : f(x_1 x_2) = 3x_1 - 8x_1 x_2 + 3x_2 + 2x_1 + 2x_2 + 2 = 0$ La se aduca la o forma canonica, ef ixometra. Regres grafica EXT  $(R^2(R_1g_0)_{1}\varphi)$  Fix remies  $\Gamma$ : a)  $f(x_1x_2) = 3x_1 - 4x_1x_2 - 2x_1 + 4x_2 - 3 = 0$ b) f(2/12) = 42/22-322+424-1422-7=0 c) f(24,22) = 321 - 421 22 + 322 - 421 + 622 - 4 = 0 d) f(21/22) = 16xy2+4x1x2+19x2+80x1+10x+40=0 1) sa se det central rouccei 2) Sa se aduca sonica I la o forma canonica, efectuand o izometrie de speta 1. Precipati salimbarile de repere ortonormate ? Reprez. grafica: amScanner