

$$U = \{(x, y, x+y, x-y, 2x) \in F^5 : x, y \in F\}$$

$$\underbrace{W = \{ \text{n.t.} \}}_U \quad U \oplus W = F^5$$

$$\text{Let } W = \{(0, 0, a, b, c) \in F^5 : a, b, c \in F\}$$

Let (p, q, r, s, t) arbitrary element of F^5 .

$$(p, q, r, s, t) = (p, q, p+q, p-q, 2p) + (0, 0, r-p-q, s-p+q, t-2p) \in U + W$$

$$\Rightarrow U + W = F^5 \quad (1)$$

$$\begin{aligned} \text{Let arbitrary } (x, y, x+y, x-y, 2x) &\in U \\ (0, 0, a, b, c) &\in W. \end{aligned}$$

$$(x, y, x+y, x-y, 2x) = (0, 0, a, b, c) \Leftrightarrow$$

$$\Leftrightarrow x=0, y=0, a=0, b=0, c=0 \Rightarrow U \cap W = \{0\} \quad (2)$$

$$(1), (2) \Rightarrow U \oplus W = F^5$$