

\mathbb{R}^2 subspace of \mathbb{C}^2 ?

No, it's not closed under scalar multiplication.

Assume, $x = (1, 0) \in \mathbb{R}^2$, $\lambda = i \in \mathbb{C}$

$$\lambda x = (i, 0) \notin \mathbb{R}^2$$