

Addition of subspaces of V has an additive identity.

For an arbitrary subspace U of V :

$$U = \{(x_1, \dots, x_m) \in F^m : x_i \in F\}$$

Let 0 be the smallest subspace of V (The set $\{0\}$)

$$0 = \{(0, \dots, 0) \in F^m\}$$

$$\begin{aligned} U + 0 &= \{(x_1 + 0, \dots, x_m + 0) \in F^m\} \\ &= \{(x_1, \dots, x_m) \in F^m\} \\ &= U \end{aligned}$$

Let w be an additive inverse of U .

$$\left. \begin{array}{l} U + w = \{0\} \\ U \subseteq U + w \end{array} \right\} \Rightarrow U \subseteq \{0\} \Rightarrow U = \{0\}.$$

Analogous, $w = \{0\}$.

Only the 0 subspace has an additive inverse (itself)