

Counterexample:

Let  $V = F^4$ . Let  $B = (e_1, e_2, e_3, e_4)$  basis of  $V$ .

Consider  $U = \{(x, y, z, z) \in F^4 : x, y, z \in F\}$  a subspace of  $V$ .

$e_1, e_2 \in U$ ,  $e_3, e_4 \notin U$

But,  $B' = (e_1, e_2)$  is NOT a basis of  $U$ .

For example we can't form  $v = (1, 1, 2, 2) \in U$  as a lin. combination of  $e_1, e_2$ .