

ГУАП

КАФЕДРА № 42

ОТЧЕТ  
ЗАЩИЩЕН С ОЦЕНКОЙ \_\_\_\_\_  
ПРЕПОДАВАТЕЛЬ

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ОТЧЕТ О ЛАБОРАТОРНОЙ РАБОТЕ №4

**Дискретные сигналы. БПФ.**

Вариант 5

по курсу: Цифровая обработка и передача сигналов

РАБОТУ ВЫПОЛНИЛ

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## 1 Задание

$f = 3N$ ,  $T = 10/F$ , где  $N$  – номер по списку. Написать программу, которая позволит:

1. Провести дискретизацию функции  $u(t) = \sin(2\pi ft)$  на заданном интервале с частотой дискретизации  $3f$ .
2. Вычислить прямое и обратное быстрое преобразование Фурье исследуемой функции.
3. Произвести декодирование аудио-файла с записью тонального сигнала (Dual-Tone Multi-Frequency (DTMF)) сигнала в формате WAV PCM 16 bit, mono. Данный способ кодирования предполагает, что кодируемое значение представляется в виде пары различных частот ( $f_1/f_2$ ) в соответствии с приведенной таблицей 4.1. Затем, сигнал представляется в виде отсчетов суммы двух синусоид соответствующих частот. Для декодирования сигнала необходимо произвести прямое быстрое преобразование Фурье для имеющегося набора отсчетов и определить частоты используемых

## 2 Выполнение работы

Построим график функции и реализуем быстрое преобразование Фурье и обратное к нему.

Результат представлен на рис. 1.

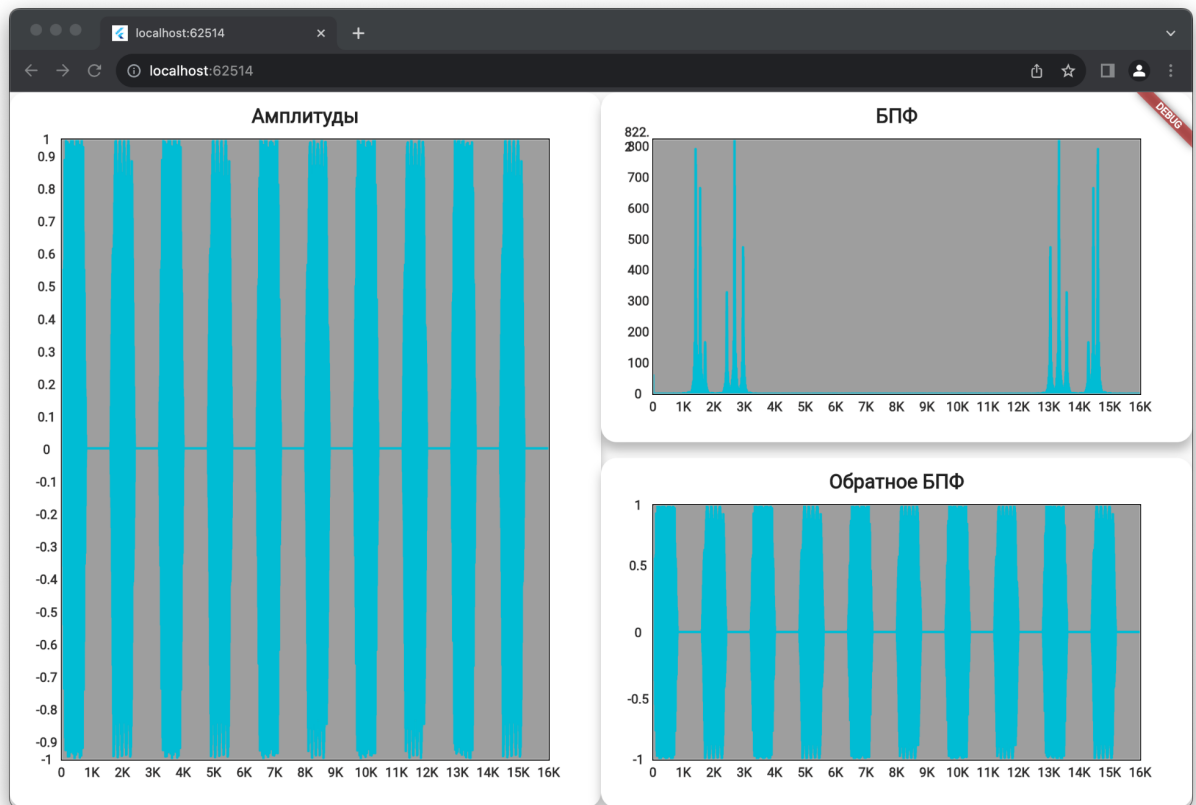


Рисунок 1 – Результат работы программы

### **3 Вывод**

В ходе выполнения лабораторной работы мы приобрели практические навыки вычисления и визуализации математических функций, эти навыки в дальнейшем могут быть полезны в анализе данных, обработке сигналов, а также в других областях, где важно понимание и работа с математическими функциями.

## ПРИЛОЖЕНИЕ

```
preview_app.dart
import 'package:extend_math/extend_math.dart';
import 'package:flutter/widgets.dart';
import 'package:lab4/logic/calculations.dart';
import 'package:ui_kit/ui_kit.dart';
```

```
class PreviewApp extends StatelessWidget {
  const PreviewApp({super.key});
```

```
  @override
```

```
  Widget build(BuildContext context) {
    return Row(
      children: [
        Expanded(
          child: Column(
            children: [
              Expanded(
                child: KitTitleContainer(
                  title: 'Амплитуды',
                  child: KitLineChart(
                    lines: [
                      KitLineData(
                        dots: Calculations.points
                          .map((e) => KitDot(e.x, e.y))
                          .toList(),
                      ),
                    ],
                  ),
                ),
              ),
            ],
          ),
        ),
      ],
    );
  }
}
```

```

    ],
  ),
),
Expanded(
  child: Column(
    children: [
      Expanded(
        child: KitTitleContainer(
          title: 'БПФ',
          child: KitLineChart(
            lines: [
              KitLineData(
                dots: Calculations.bft
                  .map((e) => KitDot(e.x, e.y))
                  .toList(),
              ),
            ],
          ),
        ),
      ),
    ],
  ),
),
const SizedBox(height: 16),
Expanded(
  child: KitTitleContainer(
    title: 'Обратное БПФ',
    child: KitLineChart(
      lines: [
        KitLineData(
          dots: Calculations.points.bft.inverseBft
            .map((e) => KitDot(e.x, e.y))
            .toList(),
        ),
      ],
    ),
  ),
),

```

```

        ],
      ),
    ),
  ),
],
),
)
],
);
}
}

```

variant.dart

```

abstract final class Variant {
  static const String filePath = 'test1.wav';
}

```

audio.dart

```

import 'package:flutter/services.dart';
import 'package:wav/wav_file.dart';

```

```

Future<List<double>> extractAudioData(String filePath) async {
  final data = await rootBundle.load('assets/test1.wav');
  final bytes = data.buffer.asUint8List();
  final waveFile = Wav.read(bytes);
  final List<double> audioData = waveFile.toMono().toList();
  return audioData;
}

```

calculations.dart

```

import 'package:complex/complex.dart';

```

```

import 'package:extend_math/extend_math.dart';

abstract final class Calculations {
  // Yep, its not good but fast!
  static late List<double> readedAudio;

  static List<Point2> get points {
    return readedAudio
      .asMap()
      .entries
      .map((e) => Point2(e.key.toDouble(), e.value))
      .toList();
  }

  static List<Point2>? cachedDft;
  static List<Point2> get dft {
    if (cachedDft != null) return cachedDft!;
    cachedDft = points.dft
      .asMap()
      .entries
      .map((e) => Point2(e.key.toDouble(), e.value.abs()))
      .toList();
    return cachedDft!;
  }

  static List<String> get match {
    final spectralComponents = points.dft;
    // Определите пороги для определения наличия частот в спектре
    double magnitudeThreshold = 200.0; // Подстройте подходящий порог
    double frequencyThreshold = 150.0; // Подстройте подходящий порог
  }
}

```



```
List<String> dtmfCodes = [];
```

```
for (int i = 1; i < spectralComponents.length - 1; i++) {
```

```
    Complex current = spectralComponents[i];
```

```
    double magnitude = current.abs();
```

```
    double frequency = i * 16000 / spectralComponents.length;
```

```
    if (magnitude > magnitudeThreshold) {
```

```
        if ((frequency % 697) < frequencyThreshold ||
```

```
            (frequency % 1209) < frequencyThreshold) {
```

```
            dtmfCodes.add('1');
```

```
        } else if ((frequency % 697) < frequencyThreshold ||
```

```
            (frequency % 1336) < frequencyThreshold) {
```

```
            dtmfCodes.add('2');
```

```
        } else if ((frequency % 697) < frequencyThreshold ||
```

```
            (frequency % 1477) < frequencyThreshold) {
```

```
            dtmfCodes.add('3');
```

```
        } else if ((frequency % 697) < frequencyThreshold ||
```

```
            (frequency % 1633) < frequencyThreshold) {
```

```
            dtmfCodes.add('A');
```

```
        } else if ((frequency % 770) < frequencyThreshold ||
```

```
            (frequency % 1209) < frequencyThreshold) {
```

```
            dtmfCodes.add('4');
```

```
        } else if ((frequency % 770) < frequencyThreshold ||
```

```
            (frequency % 1336) < frequencyThreshold) {
```

```
            dtmfCodes.add('5');
```

```
        } else if ((frequency % 770) < frequencyThreshold ||
```

```
            (frequency % 1477) < frequencyThreshold) {
```

```
            dtmfCodes.add('6');
```

```
        } else if ((frequency % 770) < frequencyThreshold ||
```

```

    (frequency % 1633) < frequencyThreshold) {
    dtmfCodes.add('B');
} else if ((frequency % 852) < frequencyThreshold ||
    (frequency % 1209) < frequencyThreshold) {
    dtmfCodes.add('7');
} else if ((frequency % 852) < frequencyThreshold ||
    (frequency % 1336) < frequencyThreshold) {
    dtmfCodes.add('8');
} else if ((frequency % 852) < frequencyThreshold ||
    (frequency % 1477) < frequencyThreshold) {
    dtmfCodes.add('9');
} else if ((frequency % 852) < frequencyThreshold ||
    (frequency % 1633) < frequencyThreshold) {
    dtmfCodes.add('C');
} else if ((frequency % 941) < frequencyThreshold ||
    (frequency % 1209) < frequencyThreshold) {
    dtmfCodes.add('*');
} else if ((frequency % 941) < frequencyThreshold ||
    (frequency % 1336) < frequencyThreshold) {
    dtmfCodes.add('0');
} else if ((frequency % 941) < frequencyThreshold ||
    (frequency % 1477) < frequencyThreshold) {
    dtmfCodes.add('#');
} else if ((frequency % 941) < frequencyThreshold ||
    (frequency % 1633) < frequencyThreshold) {
    dtmfCodes.add('D');
}
}
}

return dtmfCodes.toList();

```

```
}
```

```
static List<int> findFrequencyPeaks(  
    List<Complex> spectralComponents, int sampleRate) {  
    List<int> peaks = [];  
    double threshold =  
        200.0; // Установите подходящий порог для определения пиков  
  
    for (int i = 1; i < spectralComponents.length - 1; i++) {  
        double magnitude = spectralComponents[i].abs();  
        if (magnitude > threshold &&  
            magnitude > spectralComponents[i - 1].abs() &&  
            magnitude > spectralComponents[i + 1].abs()) {  
            double frequency = i * sampleRate / spectralComponents.length;  
            peaks.add(frequency.round());  
        }  
    }  
}  
  
return peaks;  
}
```

```
static List<String> matchFrequenciesToDTMF(List<int> frequencies) {  
    final dtmfFrequencies = {  
        697 / 1209: '1',  
        697 / 1336: '2',  
        697 / 1477: '3',  
        697 / 1633: 'A',  
        770 / 1209: '4',  
        770 / 1336: '5',  
        770 / 1477: '6',  
        770 / 1633: 'B',  
    }  
}
```

```

852 / 1209: '7',
852 / 1336: '8',
852 / 1477: '9',
852 / 1633: 'C',
941 / 1209: '*',
941 / 1336: '0',
941 / 1477: '#',
941 / 1633: 'D'
};

```

```

List<String> dtmfCodes = [];
for (int frequency in frequencies) {
    String closestFrequency = findClosestFrequency(
        frequency,
        dtmfFrequencies.keys.toList(),
    ).toString();
    dtmfCodes.add(dtmfFrequencies[closestFrequency] ?? "???");
}

return dtmfCodes;
}

```

```

static double findClosestFrequency(
    int targetFrequency, List<double> frequencies) {
    var minDifference = 99999999.0;
    late double closestFrequency;

    for (var frequency in frequencies) {
        var difference = (frequency - targetFrequency).abs();
        if (difference < minDifference) {
            minDifference = difference;

```

```

        closestFrequency = frequency;
    }
}

    return closestFrequency;
}
}

main.dart
import 'package:flutter/material.dart';
import 'package:lab4/logic/audio.dart';
import 'package:lab4/logic/calculations.dart';
import 'package:lab4/logic/variant.dart';
import 'package:lab4/ui/preview_app.dart';

void main() async {
    WidgetsFlutterBinding.ensureInitialized();
    Calculations.readedAudio = await extractAudioData(Variant.filePath);
    print(Calculations.match);
    runApp(const MainApp());
}

class MainApp extends StatelessWidget {
    const MainApp({super.key});

    @override
    Widget build(BuildContext context) {
        return const MaterialApp(
            home: Scaffold(
                body: Center(
                    child: PreviewApp(),

```

```

    ),
  ),
);
}
}

```

extend\_math.dart

```
library extend_math;
```

```

export 'src/extension/amplitude_spectrum_ext.dart';
export 'src/extension/distribution_map_ext.dart';
export 'src/extension/fft_extension.dart';
export 'src/extension/math_interval_ext.dart';
export 'src/extension/spectrum_energy_ext.dart';
export 'src/logic/list_functions.dart';
export 'src/models/point2.dart';
export 'src/models/math_interval.dart';

```

distribution\_map\_ext.dart

```
import 'dart:core';
```

```
import 'dart:math';
```

```
import '../models/point2.dart';
```

```

extension DistributionMapStatistics on Map<double, double> {
  List<Point2> get cumulativeDistribution {
    final listEntries = entries.toList();
    final res = <Point2>[Point2(listEntries.first.key - 1, 0)];
    var cumulative = listEntries.first.value;
    res.add(Point2(listEntries.first.key, cumulative));
  }
}

```

```

    for (int i = 1; i < listEntries.length; i++) {
        cumulative = (cumulative + listEntries[i].value);
        res.add(Point2(listEntries[i].key, cumulative));
    }

    res.add(Point2(listEntries.last.key + 1, 1));
    return res;
}

double calcCumulativeProbability(double x0) {
    double cumulativeProbability = 0.0;

    forEach((key, value) {
        if (key <= x0) {
            cumulativeProbability += value;
        }
    });

    return cumulativeProbability;
}

double get mean {
    double mean = 0.0;

    forEach((key, value) {
        mean += key * value;
    });

    return mean;
}

```

```
double get secondMoment {  
    double secondMoment = 0.0;  
  
    forEach((key, value) {  
        secondMoment += (key * key) * value;  
    });  
  
    return secondMoment;  
}
```

```
double get thirdMoment {  
    double thirdMoment = 0.0;  
  
    forEach((key, value) {  
        thirdMoment += (key * key * key) * value;  
    });  
  
    return thirdMoment;  
}
```

```
double get fourthMoment {  
    double fourthMoment = 0.0;  
  
    forEach((key, value) {  
        fourthMoment += (key * key * key * key) * value;  
    });  
  
    return fourthMoment;  
}
```



```

double get mode {
    double maxProbability = -1.0;
    double mode = 0;

    forEach((key, value) {
        if (value > maxProbability) {
            maxProbability = value;
            mode = key;
        }
    });

    return mode.toDouble();
}

double get median {
    final sortedEntries = entries.toList()
        ..sort((a, b) => a.key.compareTo(b.key));
    final numEntries = sortedEntries.length;

    if (numEntries % 2 == 0) {
        final middle1 = sortedEntries[numEntries ~/ 2 - 1].key;
        final middle2 = sortedEntries[numEntries ~/ 2].key;
        return (middle1 + middle2) / 2.0;
    } else {
        return sortedEntries[numEntries ~/ 2].key.toDouble();
    }
}

double get excess {
    double mean = 0.0;
    double variance = 0.0;

```

```
forEach((key, value) {  
    mean += key * value;  
});
```

```
forEach((key, value) {  
    variance += (key - mean) * (key - mean) * value;  
});
```

```
final stdDev = sqrt(variance);  
final numEntries = length.toDouble();
```

```
double excess = 0.0;  
forEach((key, value) {  
    excess += ((key - mean) * (key - mean) * (key - mean) * value) /  
        (stdDev * stdDev * stdDev);  
});
```

```
return excess / numEntries;  
}
```

```
double get variance {  
    double mean = 0.0;  
    double variance = 0.0;  
  
    forEach((key, value) {  
        mean += key * value;  
    });
```

```
forEach((key, value) {  
    variance += ((key - mean) * (key - mean)) * value;
```

```

    });

    return variance;
}

double get standardDeviation => sqrt(variance);

double get skewness {
    double thirdMoment = this.thirdMoment;
    final stdDev = standardDeviation;

    final numEntries = length.toDouble();
    double skewness = thirdMoment / (stdDev * stdDev * stdDev * numEntries);
    return skewness;
}

double get centralSecondMoment {
    double centralSecondMoment = 0.0;

    forEach((key, value) {
        centralSecondMoment += ((key - mean) * (key - mean)) * value;
    });

    return centralSecondMoment;
}

double get centralThirdMoment {
    double centralThirdMoment = 0.0;

    forEach((key, value) {
        centralThirdMoment +=

```

```

        ((key - mean) * (key - mean) * (key - mean)) * value;
    });

    return centralThirdMoment;
}

double get centralFourthMoment {
    double centralFourthMoment = 0.0;

    forEach((key, value) {
        centralFourthMoment +=
            ((key - mean) * (key - mean) * (key - mean) * (key - mean)) * value;
    });

    return centralFourthMoment;
}
}

spectrum_energy_ext.dart
import 'dart:math';

import 'package:extend_math/extend_math.dart';

extension SpectrumAmplEnergyExt on List<double> {
    double get energy {
        final total = sum(map((e) => e * e));
        final normalize = map((e) => e * sqrt(0.5 / total));
        return sum(normalize.map((e) => e * e));
    }
}

```

```

extension SpectrumPointEnergyExt on List<Point2> {
  double calculateEnergy(MathInterval interval) {
    double integral = 0;
    for (final point in this) {
      integral += pow(point.y, 2);
    }

    final energy = integral / interval.length;
    return energy;
  }
}

math_interval_ext.dart
import 'package:extend_math/extend_math.dart';

import '../utils/typedefs.dart';

extension MathIntervalExt on MathInterval {
  List<Point2> applyFx(Func1 fx, {required double step}) {
    final count = length ~/ step;
    return [
      for (var x = start; x <= end; x += length / count) Point2(x, fx(x))
    ];
  }
}

amplitude_spectrum_ext.dart
import 'dart:math';

import '../models/point2.dart';

```

```

extension AmplitudeSpectrumExtension on List<Point2> {
  double amplitudeSpectrumFor(
    double freq, {
      required double step,
    }) {
    double realPart = 0.0;
    double imagPart = 0.0;

    for (int j = 0; j < length; j++) {
      double value = this[j].y;
      double angle = 2 * pi * freq * this[j].x;
      realPart += value * cos(angle) * step;
      imagPart += value * sin(angle) * step;
    }

    return sqrt(realPart * realPart + imagPart * imagPart);
  }
}

```

```

fft_extension.dart
// ignore_for_file: prefer_const_constructors

```

```

import 'dart:math';

```

```

import 'package:complex/complex.dart';

```

```

import '../models/point2.dart';

```

```

extension DFTEExtension on List<Point2> {
  List<Complex> get dft {
    int N = length;

```

```

List<Complex> dftResult = List<Complex>.generate(N, (i) {
    Complex sum = const Complex(0.0, 0.0);
    for (int j = 0; j < N; j++) {
        double angle = 2 * pi * i * j / N;
        Complex c = Complex.polar(this[j].y, angle);
        sum += c;
    }
    return sum;
});
return dftResult;
}
}

```

```

extension InverseDFTExtension on List<Complex> {
    List<Point2> get inverseDft {
        final spectrum = this;
        int N = spectrum.length;
        List<Point2> signal = List<Point2>.generate(N, (i) {
            Complex sum = Complex(0.0, 0.0);
            for (int j = 0; j < N; j++) {
                double angle = -2 * pi * i * j / N;
                Complex c = spectrum[j] * Complex.polar(1.0, angle);
                sum += c;
            }
            return Point2(i.toDouble(), sum.real / N);
        });
        return signal;
    }
}

```

list\_functions.dart

```

double sum(Iterable<double> list) =>
    list.reduce((value, element) => value + element);

List<T> roll<T>(List<T> inputList, int shiftAmount) {
    final length = inputList.length;
    if (length == 0) {
        return inputList;
    }

    // Calculate the effective shift amount, wrapping around if necessary
    final effectiveShift = shiftAmount % length;

    if (effectiveShift == 0) {
        return inputList;
    }

    // Split the input list into two parts and rejoin them with the shift
    final startIndex = effectiveShift < 0 ? -effectiveShift : length - effectiveShift;
    final part1 = inputList.sublist(startIndex);
    final part2 = inputList.sublist(0, startIndex);
    return [...part1, ...part2];
}

typedefs.dart
typedef Func1 = double Function(double x);

math_interval.dart
final class MathInterval {
    final double start;
    final double end;

    const MathInterval(this.start, this.end);

```



```
double get length => (end - start).abs();  
}
```

point2.dart

```
class Point2 {  
  final double x;  
  final double y;  
  
  const Point2(this.x, this.y);  
  
  static const zero = Point2(0, 0);  
}
```