Triangular linear systems

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$$
\begin{cases}
a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \cdots & \cdots + a_{1n}x_n = b_1 \\
\qquad a_{22}x_2 + a_{23}x_3 + \cdots & \cdots + a_{2n}x_n = b_2 \\
\qquad\qquad a_{33}x_3 + \cdots & + a_{3n}x_n = b_3 \\
\qquad\qquad\qquad \ddots & \vdots \qquad \vdots \\
\qquad\qquad\qquad a_{ii}x_i + a_{i,i+1}x_{i+1} + & \cdots + a_{in}x_n = b_i \\
\qquad\qquad\qquad\qquad \ddots & \vdots \qquad \vdots \\
 & a_{n-1,n-1}x_{n-1} + a_{n-1,n}x_n = b_{n-1} \\
 & a_{nn}x_n = b_n
\end{cases}
$$

The solution x is obtained by *backward-substitution*
(we find $x_n, \ldots, x_1$ from bottom to top).

In the dual situation, when we find the solution from top to bottom,
we have the *forward-substitution*.