

Question 1: NFA to DFA

The RegEx for this NFA is: $x^*y\{1\}x^*z^*$

The NFA has 4 states: a, b, c, d. Therefore the corresponding DFA has the state set:

$$\{\emptyset, \{a\}, \{b\}, \{c\}, \{d\}, \{a,b\}, \{a,c\}, \{a,d\}, \{b,c\}, \{b,d\}, \{c,d\}, \\ \{a,b,c\}, \{a,c,d\}, \{b,c,d\}, \{a,b,c,d\}\}$$

The accept states for the DFA are:

$$\{\{c\}, \{a,c\}, \{b,c\}, \{c,d\}, \{a,b,c\}, \{a,c,d\}, \{a,b,c,d\}\}$$

$$\epsilon\text{-closure}(a) = \{a\}$$

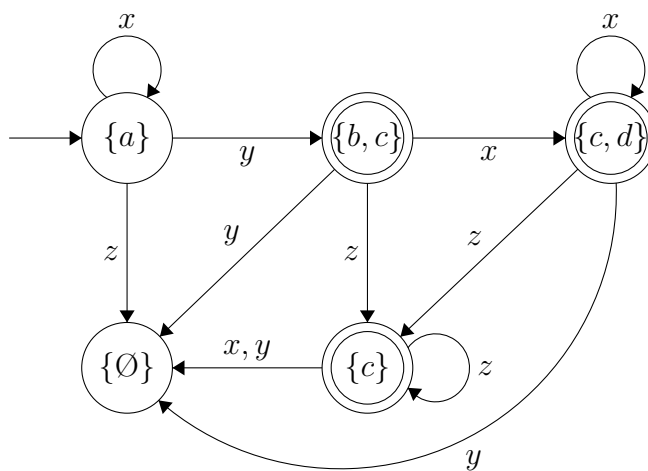
$$\epsilon\text{-closure}(b) = \{b,c,d\}$$

$$\epsilon\text{-closure}(c) = \{c\}$$

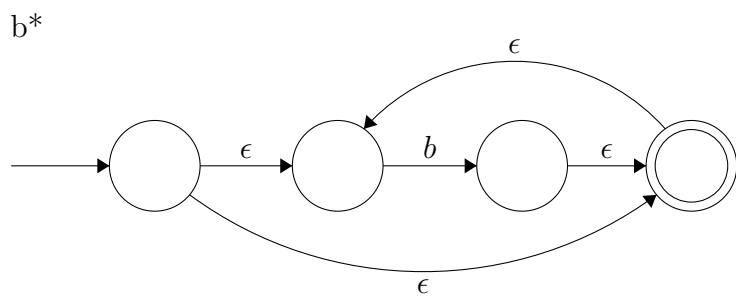
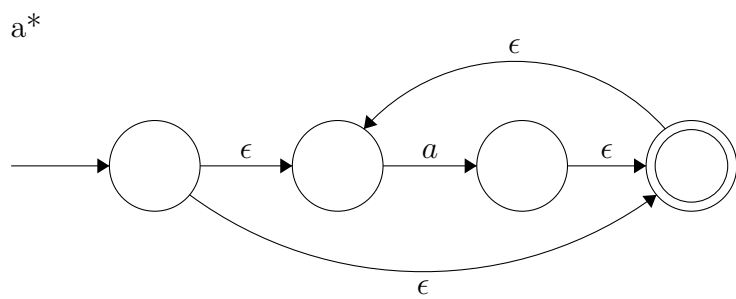
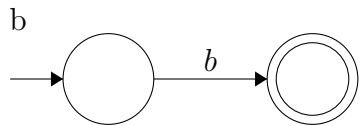
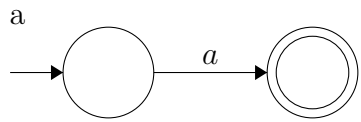
$$\epsilon\text{-closure}(d) = \{c,d\}$$

	State	x	y	z
Transitions	$\{a\}$	$\{a\}$	$\{b,c\}$	\emptyset
	$\{b,c,d\}$	$\{c,d\}$	\emptyset	\emptyset
	$\{c\}$	\emptyset	\emptyset	$\{c\}$
	$\{c,d\}$	$\{c,d\}$	\emptyset	$\{c\}$

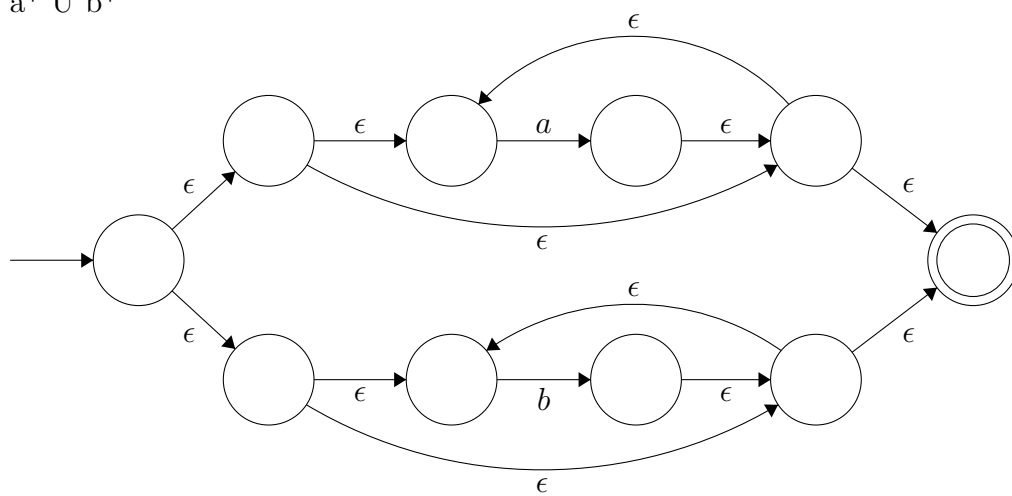
Turning all of this into a graphical representation of the corresponding DFA we get:



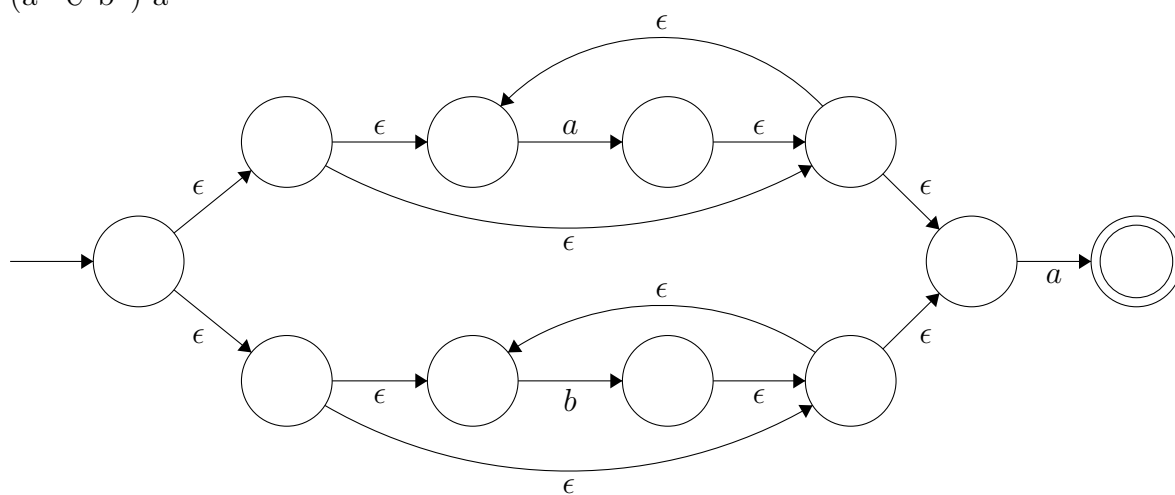
Question 2: RegEx to NFA



$a^* \cup b^*$



$(a^* \cup b^*) a$



Question 3: Binary Additive Arithmetic

The RegEx for the Binary Additive Arithmetic language is:

$$(0? + 1(1 + 0)^*)(+|-)(0? + 1(1 + 0)^*)$$

The corresponding NFA for this language is:

