

## Question 1: Problem 3

Stable: Bubble sort, Insertion sort, Merge sort, Counting sort, Radix Sort

Not Stable: Quick sort, Heap sort, Selection sort

Can be made stable: All non-stable can be made into stable by taking into account the positions of the elements prior to the sort

## Question 2: Problem 4

Yes, *SELECTION* with groups of 3 does find the  $k$ -th smallest element, however it will not run in linear time since we don't reduce the subproblems as efficiently as with groups of 5. With groups of 3 we are still left with subproblems of size  $n$  whereas with groups of 5 and larger the problem get reduced to size of less than  $n$ .

### Question 3: Problem 7

QUICKSORT: Depending on implementation, chooses either the first or last element of array as pivot.

SELECTION: Just as QUICKSORT, chooses either the first or last element as pivot.

RANDOMIZED SELECTION: The pivot is chosen at random uniformly using a random number generator from (start,end)

## Question 4: Problem 21

For a vertex to be a cut vertex as a function of its discovery time, for two nodes,  $u, v$ , where  $u$  is a parent and  $v$  is a child. Let  $d[v]$  be the discovery time for a node  $v$ . Let  $L[u]$  be the lowest node that can be reached from any vertex. Then if  $L[v] \geq d[u]$  then  $u$  is a cut vertex.