Exercise 3

This is simple.

$$f \circ g = f \circ g'$$

$$\Rightarrow g \circ f \circ g = g \circ f \circ g'$$

$$\Rightarrow g \circ 1_B = 1_A \circ g'$$

$$\Rightarrow g = g'$$

Exercise 9

First, let $e:A\to B$ be an epimorphism in **Pos** and $b\in B$. Let $B'=B\cup \left\{b'\right\}$ be the poset that is identical to B, except that b is duplicated: We have a b' behaving idential to b in all respects, but $b'\neq b$. Let f be the inclusion from B into B' and f' identical to f except that it maps b to b' instead of b. Both are monotonic functions and therefore morphisms in **Pos**. Since $f\neq f'$ we have, since e was epi that $f\circ e\neq f'\circ e$. This, however means that $b\in e(A)$ because this is the only point where f and f' differ. Since b was chosen arbitrarily we have proven that e is a surjection.

Conversly, if $e: A \to B$ is a surjective morphism then it is epi since this is already true in **Sets** and the forgetful functor is injective.