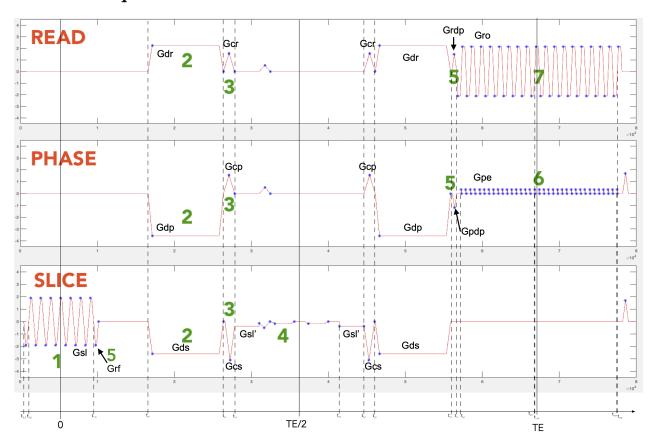
### 1 Pulse sequence



## 2 General analytic form

$$b_{ij} = \gamma^{2} \Big[ G_{1i} G_{1j} \tau_{11} + (G_{1i} G_{2j} + G_{2i} G_{1j}) \tau_{12} + (G_{1i} G_{3j} + G_{3i} G_{1j}) \tau_{13} + \\ + (G_{1i} G_{4j} + G_{4i} G_{1j}) \tau_{14} + (G_{1i} G_{5j} + G_{5i} G_{1j}) \tau_{15} + (G_{1i} G_{6mj} + G_{6mi} G_{1j}) \tau_{16m} + \\ + (G_{1i} G_{71j} + G_{71i} G_{1j}) \tau_{171} + G_{2i} G_{2j} \tau_{22} + (G_{2i} G_{3j} + G_{3i} G_{2j}) \tau_{23} + \\ + (G_{2i} G_{4j} + G_{4i} G_{2j}) \tau_{24} + (G_{2i} G_{5j} + G_{5i} G_{2j}) \tau_{25} + (G_{2i} G_{6mj} + G_{6mi} G_{2j}) \tau_{26m} + \\ + (G_{2i} G_{71j} + G_{71i} G_{2j}) \tau_{271} + G_{3i} G_{3j} \tau_{33} + (G_{3i} G_{4j} + G_{4i} G_{3j}) \tau_{34} + \\ + (G_{3i} G_{5j} + G_{5i} G_{3j}) \tau_{35} + (G_{3i} G_{6mj} + G_{6mi} G_{3j}) \tau_{36m} + (G_{3i} G_{71j} + G_{71i} G_{3j}) \tau_{371} + \\ + G_{4i} G_{4j} \tau_{44} + (G_{4i} G_{5j} + G_{5i} G_{4j}) \tau_{45} + (G_{4i} G_{6mj} + G_{6mi} G_{4j}) \tau_{46m} + \\ + (G_{4i} G_{71j} + G_{71i} G_{4j}) \tau_{471} + G_{5i} G_{5j} \tau_{55} + (G_{5i} G_{6mj} + G_{6mi} G_{5j}) \tau_{56m} + (G_{5i} G_{71j} + G_{71i} G_{5j}) \tau_{571} \\ + G_{6mi} G_{6mj} \tau_{6m6m} + (G_{6i} G_{71j} + G_{71i} G_{6j}) \tau_{671} + G_{71i} G_{71j} \tau_{7171} + \\ + (G_{7mi} G_{7(m+1)j} + G_{7(m+1)i} G_{7mj}) \tau_{7m7(m+1)} \Big]$$

# 3 Diagonal terms

For the read direction we have:  $G_1=0$ ;  $G_2=G_{dr}$ ;  $G_3=G_{cr}$ ;  $G_4=0$ ;  $G_5=G_{rdp}$ ;  $G_6=0$ ;  $G_7=G_{ro}$  which gives the following for the diagonal readout term

$$b_{rr} = \gamma^2 \left( G_{dr}^2 \tau_{22} + 2G_{dr} G_{cr} \tau_{23} + 2G_{dr} G_{rdp} \tau_{25} + 2G_{dr} G_{ro} \tau_{271} + G_{cr}^2 \tau_{33} + 2G_{cr} G_{rdp} \tau_{35} + 2G_{cr} G_{ro} \tau_{371} + G_{rdp}^2 \tau_{55rp} + 2G_{rdp} G_{ro} \tau_{5rp71} + G_{ro}^2 (\tau_{7171} + \tau_{7m7(m+1)}) \right)$$
(2)

taking into account refocused gradient pairs we get:

$$b_{rr} = \gamma^2 \left( G_{dr}^2 \tau_{22} + 2G_{dr} G_{cr} \tau_{23} + G_{cr}^2 \tau_{33} + G_{rdp}^2 \tau_{55rp} + 2G_{rdp} G_{ro} \tau_{5rp71} + G_{ro}^2 (\tau_{7171} + \tau_{7m7(m+1)}) \right)$$
(3)

For the phase direction we have:  $G_1=0$ ;  $G_2=G_{dp}$ ;  $G_3=G_{cp}$ ;  $G_4=0$ ;  $G_5=G_{pdp}$ ;  $G_6=G_{pe}$ ;  $G_7=0$  which gives the following for the diagonal phase-encoding

$$b_{pp} = \gamma^2 (G_{dp}^2 \tau_{22} + 2G_{dp}G_{cp}\tau_{23} + 2G_{dp}G_{pdp}\tau_{25} + 2G_{dp}G_{pe}\tau_{26m} + G_{cp}^2\tau_{33} + 2G_{cp}G_{pdp}\tau_{35} + G_{cp}G_{pe}\tau_{36m} + G_{pdp}^2\tau_{55rp} + 2G_{pdp}G_{pe}\tau_{5rp6m} + G_{pe}^2\tau_{6m6m})$$
(4)

taking into account refocused gradient pairs we get:

$$b_{pp} = \gamma^2 (G_{dp}^2 \tau_{22} + 2G_{dp}G_{cp}\tau_{23} + G_{cp}^2 \tau_{33} + G_{pdp}^2 \tau_{55rp} + 2G_{pdp}G_{pe}\tau_{5rp6m} + G_{pe}^2 \tau_{6m6m})$$
 (5)

For the slice direction we have:  $G_1 = G_{sl}$ ;  $G_2 = G_{ds}$ ;  $G_3 = G_{cs}$ ;  $G_4 = G'_{sl}$ ;  $G_5 = G_{rf}$ ;  $G_6 = 0$ ;  $G_7 = 0$  which gives the following for the diagonal slice-select:

$$b_{ss} = \gamma^2 \left( \frac{14}{3} G_{sl}^2 \tau_{11} + G_{sl} G_{ds} \tau_{12} + G_{sl} G_{cs} \tau_{13} + G_{sl} G'_{sl} \tau_{14} + G_{sl} G_{rf} \tau_{15} + G_{ds}^2 \tau_{22} + 2G_{ds} G_{cs} \tau_{23} + G_{ds} G'_{sl} \tau_{24} + G_{ds} G_{rf} \tau_{25} + G_{cs}^2 \tau_{33} + G_{cs} G'_{sl} \tau_{34} + 2G_{cs} G_{rf} \tau_{35} + G'_{sl}^2 \tau_{44} + G'_{sl} G_{rf} \tau_{45} + G_{rf}^2 \tau_{55} \right)$$

$$(6)$$

with refocused gradient pairs one arrives to:

$$b_{ss} = \gamma^2 \left( \frac{14}{3} G_{sl}^2 \tau_{11} + G_{ds}^2 \tau_{22} + 2G_{ds} G_{cs} \tau_{23} + G_{ds} G_{sl}' \tau_{24} + G_{ds} G_{rf} \tau_{25} + G_{cs}^2 \tau_{33} + G_{cs} G_{sl}' \tau_{34} + 2G_{cs} G_{rf} \tau_{35} + \frac{1}{4} G_{sl}'^2 \tau_{44} + G_{sl}' G_{rf} \tau_{45} + \frac{1}{4} G_{rf}^2 \tau_{55s} \right)$$

$$(7)$$

## 4 Off-diagonal terms

Summarizing all gradients together in one place:

$G_{1r} = 0$	$G_{1p} = 0$	$G_{1s} = G_{sl}$
$G_{2r} = G_{dr}$	$G_{2p} = G_{dp}$	$G_{2s} = G_{ds}$
$G_{3r} = G_{cr}$	$G_{3p} = G_{cp}$	$G_{3s} = G_{cs}$
$G_{4r} = 0$	$G_{4p} = 0$	$G_{4s} = G'_{sl}$
$G_{5r} = G_{rdp}$	$G_{5p} = G_{pdp}$	$G_{5s} = G_{rf}$
$G_{6r} = 0$	$G_{6p} = G_{pe}$	$G_{6s} = 0$
$G_{7r} = G_{ro}$	$G_{7p} = 0$	$G_{7s} = 0$

Then starting from the read-out/phase term plugging the gradients  $G_r$  and  $G_p$  into equation Eq. 1:

$$b_{rp} = b_{pr} = \gamma^2 \Big( G_{dr} G_{dp} \tau_{22} + (G_{dr} G_{cp} + G_{cr} G_{dp}) \tau_{23} + (G_{dr} G_{pdp} + G_{rdp} G_{dp}) \tau_{25} + G_{dr} G_{pe} \tau_{26m} + G_{ro} G_{dp} \tau_{271} + G_{cr} G_{cp} \tau_{33} + (G_{cr} G_{pdp} + G_{rdp} G_{cp}) \tau_{35} + G_{cr} G_{pe} \tau_{36m} + G_{ro} G_{cp} \tau_{371} + G_{rdp} G_{pdp} \tau_{55rp} + G_{rdp} G_{pe} \tau_{5rp6m} + G_{ro} G_{pdp} \tau_{5rp71} + G_{pe} G_{ro} \tau_{6m71} \Big)$$

$$(8)$$

taking into account refocused gradient pairs we get:

$$b_{rp} = b_{pr} = \gamma^2 \Big( G_{dr} G_{dp} \tau_{22} + (G_{dr} G_{cp} + G_{cr} G_{dp}) \tau_{23} + G_{cr} G_{cp} \tau_{33} + G_{rdp} G_{pdp} \tau_{55rp} + G_{rdp} G_{pe} \tau_{5rp6m} + G_{ro} G_{pdp} \tau_{5rp71} + G_{pe} G_{ro} \tau_{6m71} \Big)$$

$$(9)$$

the read-out/slice select term gives:

$$b_{rs} = b_{sr} = \gamma^{2} \left( G_{dr} G_{sl} \tau_{12} + G_{cr} G_{sl} \tau_{13} + G_{rdp} G_{sl} \tau_{15} + G_{ro} G_{sl} \tau_{171} + G_{dr} G_{ds} \tau_{22} + \right.$$

$$\left. + \left( G_{dr} G_{cs} + G_{cr} G_{ds} \right) \tau_{23} + \frac{1}{2} G_{ds} G'_{sl} \tau_{24} + \left( \frac{1}{2} G_{dr} G_{rf} + G_{rdp} G_{ds} \right) \tau_{25} + G_{ds} G_{ro} \tau_{271} + \right.$$

$$\left. + G_{cr} G_{cs} \tau_{33} + \frac{1}{2} G_{cr} G'_{sl} \tau_{34} + \left( G_{cr} G_{rf} + \frac{1}{2} G_{rdp} G_{cs} \right) \tau_{35} + G_{rdp} G'_{sl} \tau_{45} + \right.$$

$$\left. + G_{ro} G'_{sl} \tau_{471} + \frac{1}{2} G_{rdp} G_{rf} \tau_{55rp} + \frac{1}{2} G_{ro} G_{rf} \tau_{5s71} \right)$$

$$(10)$$

again by taking into account refocused gradient pairs the expression simplifies to:

$$b_{rs} = b_{sr} = \gamma^2 \Big( (G_{dr}G_{cs} + G_{cr}G_{ds})\tau_{23} + G_{dr}G'_{sl}\tau_{24} + (G_{dr}G_{rf})\tau_{25} + G_{cr}G_{cs}\tau_{33} + \frac{1}{2}G_{cr}G'_{sl}\tau_{34} + \frac{1}{2}G_{cr}G_{rf}\tau_{35} + \frac{1}{2}G_{rdp}G_{rf}\tau_{55rp} + \frac{1}{2}G_{ro}G_{rf}\tau_{5s71} \Big)$$

$$(11)$$

and the last term the phase/slice select:

$$b_{sp} = b_{ps} = \gamma^2 \left( G_{sl} G_{dp} \tau_{12} + G_{sl} G_{cp} \tau_{13} + G_{sl} G_{pdp} \tau_{15} + G_{sl} G_{pe} \tau_{16m} + G_{dp} G_{ds} \tau_{22} + \right.$$

$$+ \left. \left( G_{ds} G_{cp} + G_{ds} G_{cp} \right) \tau_{23} + \frac{1}{2} G_{dp} G'_{sl} \tau_{24} + \left( \frac{1}{2} G_{dp} G_{rf} + G_{ds} G_{pdp} \right) \tau_{25} + G_{pe} G_{ds} \tau_{26m} + \right.$$

$$+ \left. G_{cp} G_{cs} \tau_{33} + \frac{1}{2} G_{cp} G'_{sl} \tau_{34} + \left( \frac{1}{2} G_{cp} G_{rf} + G_{pdp} G_{cs} \right) \tau_{35} + G_{pe} G_{cs} \tau_{36m} + G_{pdp} G'_{sl} \tau_{45} + \right.$$

$$+ \left. G_{pe} G'_{sl} \tau_{46m} + \frac{1}{2} G_{pdp} G_{rf} \tau_{55rp} + \frac{1}{2} G_{pe} G_{rf} \tau_{5s6m} \right)$$

$$(12)$$

with refocused gradient pairs gives final expression:

$$b_{sp} = b_{ps} = \gamma^2 \left( G_{dp} G_{ds} \tau_{22} + (G_{ds} G_{cp} + G_{ds} G_{cp}) \tau_{23} + \frac{1}{2} G_{dp} G'_{sl} \tau_{24} + \frac{1}{2} G_{dp} G_{rf} \tau_{25} + G_{cp} G_{cs} \tau_{33} + \frac{1}{2} G_{cp} G'_{sl} \tau_{34} + \frac{1}{2} cp G_{rf} \tau_{35} + \frac{1}{2} G_{pdp} G_{rf} \tau_{55rp} + \frac{1}{2} G_{pe} G_{rf} \tau_{5s6m} \right)$$

$$(13)$$

#### 5 Timing multipliers

$$\tau_{11} = \delta_1^3 \tag{14}$$

$$\tau_{22} = \delta_2^2 \left( \Delta_2 - \frac{1}{3} \delta_2 \right) + \frac{1}{30} \epsilon^3 - \frac{1}{6} \delta_2 \epsilon^2, \qquad \Delta_2 = t_{22} - t_{21}$$
 (15)

$$\tau_{23} = \delta_2 \delta_3 \Delta_3, \qquad \Delta_3 = t_{32} - t_{31}$$
(16)

$$\tau_{24} = \delta_2 \delta_4 \Delta_4, \qquad \Delta_4 = t_{42} - t_{41} \tag{17}$$

$$\tau_{25} = \frac{1}{2} \delta_5 \delta_2 \Delta_2, \qquad \Delta_2 = t_{22} - t_{21} \qquad (18)$$

$$\tau_{33} = \delta_3^2 \left( \Delta_3 - \frac{1}{3} \delta_3 \right) + \frac{1}{30} \epsilon^3 - \frac{1}{6} \delta_3 \epsilon^2, \qquad \Delta_3 = t_{32} - t_{31}$$
 (19)

$$\tau_{34} = \delta_3 \delta_4 \Delta_4, \qquad \Delta_4 = t_{42} - t_{41} \tag{20}$$

$$\tau_{35} = \frac{1}{2}\delta_5\delta_3\Delta_3, \qquad \Delta_3 = t_{32} - t_{31} \tag{21}$$

$$\tau_{44} = \delta_4^2 \left( \Delta_4 - \frac{1}{3} \delta_4 \right) + \frac{1}{30} \epsilon_4^3 - \frac{1}{6} \delta_4 \epsilon^2, \qquad \Delta_4 = t_{42} - t_{41}$$
 (22)

$$\tau_{45} = \frac{1}{2}\delta_5 \delta_4 \Delta_4, \qquad \Delta_4 = t_{42} - t_{41} \tag{23}$$

$$\tau_{55rp} = \delta_5^2 \left( \Delta_{5rp} - \frac{1}{3} \delta_5 \right) + \frac{1}{30} \epsilon^3 - \frac{1}{6} \delta_5 \epsilon^2, \qquad \Delta_{5rp} = \text{TE} - t_{5rp}$$
 (24)

$$\tau_{55s} = \delta_5^2 \left( \Delta_{5s} - \frac{1}{3} \delta_5 \right) + \frac{1}{30} \epsilon^3 - \frac{1}{6} \delta_5 \epsilon^2, \qquad \Delta_{5s} = \text{TE} - t_{5s}$$
 (25)

$$\tau_{5rp6m} = \epsilon' \delta_{5rp} \sum_{m=1}^{\text{res}/2} (\Delta_{6m} - \epsilon'), \qquad \Delta_{6m} = \text{TE} - t_{6i} \qquad (26)$$

$$\tau_{5s6m} = -\epsilon' \delta_{rf} \sum_{m=1}^{\text{res}/2} (\Delta_{6m} - \epsilon'), \qquad \Delta_{6m} = \text{TE} - t_{6i} \qquad (27)$$

$$\tau_{5rp71} = \delta_5 \left[ \delta_7 \left( \Delta_{75} - \frac{1}{4} \delta_7 \right) + \frac{1}{12} \epsilon'^2 - \frac{1}{2} \delta_7 \epsilon' \right], \qquad \Delta_{75} = \Delta_{71} = \text{TE} - t_{71}$$
 (28)

$$\tau_{5s71} = \delta_5 \left[ \delta_7 \left( \Delta_{75} - \frac{1}{4} \delta_7 \right) + \frac{1}{12} \epsilon'^2 - \frac{1}{2} \delta_7 \epsilon' \right], \qquad \Delta_{75} = \Delta_{71} = \text{TE} - t_{71}$$
 (29)

$$\tau_{6m6m} = \epsilon'^2 \sum_{m=1}^{\text{res}/2} \left[ (2m-1)\Delta_{6m} - (m\frac{67}{30} - 1)\epsilon' \right], \qquad \Delta_{6m} = \text{TE} - t_{6i}$$
 (30)

$$\tau_{6m71} = \frac{1}{4} \epsilon' \left( \delta_7 \Delta_{71} - \frac{1}{60} \epsilon'^2 \right), \qquad \Delta_{71} = \Delta_{75} = \text{TE} - t_{71}$$
 (31)

$$\tau_{7171} = \frac{1}{4} \left[ \delta_7^2 \left( \Delta_{71} - \frac{1}{3} \delta_7 \right) + \frac{1}{30} \epsilon'^3 - \frac{1}{2} \delta_7^2 \epsilon' \right], \qquad \Delta_{71} = \Delta_{75} = \text{TE} - t_{71}$$
 (32)

$$\tau_{7m7(m+1)} = \left(\frac{\text{res}}{2} - 1\right) \left[\frac{1}{12}\delta_7^3 + \frac{1}{60}\epsilon' + \frac{1}{4}\delta_7^2\epsilon' - \frac{1}{12}\delta_7\epsilon'^2\right], \qquad \text{res} = 34$$
 (33)