

## **Applied AI & ML Industry Projects Lab (AAM-IPL)**

Transforming Learning into Industry Solutions



#### Week-8

# Linear Discriminant Analysis Overview and Project Announcement

V Semester - ML and AIUP, Aug-Oct 2024

Session Date and Time: 9th Nov 2024 10:30 AM IST - 12:00 Noon IST

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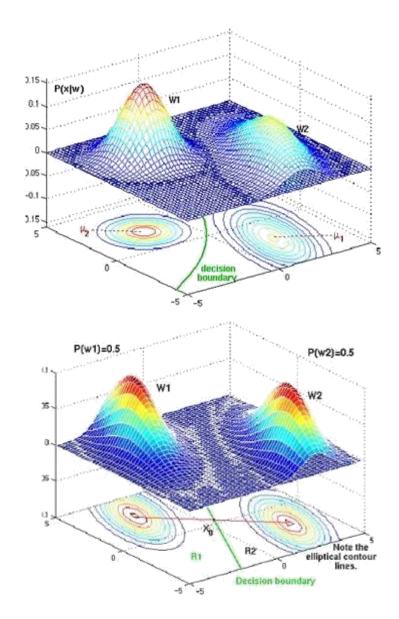
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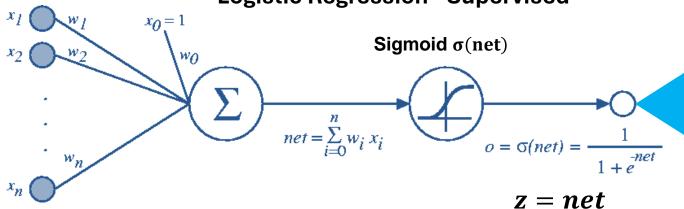
#### **Lecture Outline**



- Classification
- Classification Recap
- Challenges of Clear Class Separation: Beyond Probabilities and Margins
- Discriminant Functions
- Probability and Likelihood in Discriminant Functions
- LDA and GDA Overview
- Discriminant Analysis Classification Rule Derivation
- LDA/GDA Efficiency Metrics
- LDA/GDA Peer Comparison
- Key Takeaways
- Project Announcement
- Project Implementation Steps
- Project Demo
- Q&A

#### **Classical Classification**

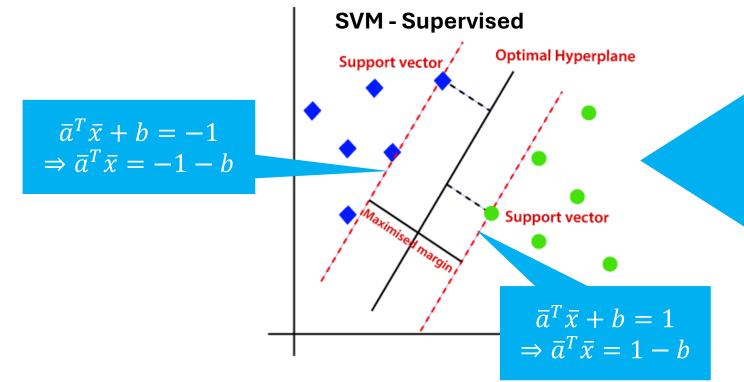
#### **Logistic Regression - Supervised**



#### **Class Probabilities**

• 
$$P(y = 1 \mid \bar{x}) = \frac{1}{\left(1 + e^{-\bar{x}^T \bar{w}}\right)}$$

• 
$$P(y = 0 \mid \bar{x}) = \frac{e^{-\bar{x}^T \bar{w}}}{\left(1 + e^{-\bar{x}^T \bar{w}}\right)}$$



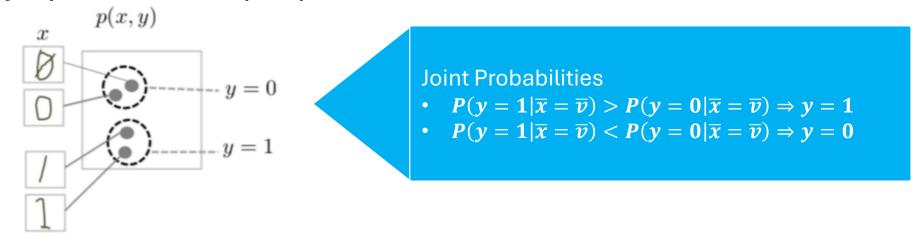
#### **Decision Boundary**

• 
$$f(\bar{x}, b) = \bar{a}^T \bar{x} + b > 0 \Rightarrow y = 1$$

• 
$$f(\bar{x},b) = \bar{a}^T\bar{x} + b < 0 \Rightarrow y = 0$$

#### **Classical Classification**

#### Naïve Bayes (Generative Model) - Supervised



- Given a set of features and labeled training data, new instances is classified into predefined category
- Key Terms
  - Feature Space The n-dimensional space where data points (feature vectors) reside
  - Class Boundaries Hypothetical boundaries that separate instances of different classes
- Often assign instances to classes based on probabilities derived from training data, or by optimizing a boundary that separates the classes
  - **Probability-Based Approach** Algorithms like Logistic Regression and Naive Bayes classify based on calculated class probabilities
  - **Decision Boundary-based Approach -** Algorithms like SVM directly optimize boundaries that separate classes in feature space

## **Classifier Categories - Recap**

- Probabilistic Classifiers
  - Given dataset  $\mathcal{D} = \{(\bar{x}_i, y_i)\}_{i=1}^N$
  - Goal is to compute the class posterior  $p(y = c \mid \overline{x})$  which models the mapping  $y = f(\overline{x})$
- Generative Classifiers
  - Given dataset  $\mathcal{D} = \{(\bar{x}_i, y_i)\}_{i=1}^N$
  - Goal is to model how the data is generated for each class using joint probability  $p(y, \overline{x} | \theta)$
  - Assumes each class has a certain data distribution that is defined by a parameter set  $oldsymbol{ heta}$
  - $\theta$  represents each class's data distribution characteristics
    - Class conditional distribution  $p(\bar{x}|y=c;\theta)$
    - Class prior probability  $p(y = c; \theta)$
  - The joint probability of class label y, feature vector  $\bar{x}$  given class parameter set  $\theta$  is  $p((y, \bar{x})|\theta)$
  - Class-conditional density  $p(\bar{x} \mid y = c; \theta)$  models the likelihood of observing a feature vector  $\bar{x}$  given a specific class y = c and parameter  $\theta$
  - Bayes' Theorem  $p(y = c \mid \bar{x}) = \frac{p(\bar{x}; y = c) \times p(y = c)}{p(\bar{x} = \bar{x}_i)}$
  - Applying Bayes' theorem, the posterior probability  $p(y=c|\overline{x};\theta) \propto p(\overline{x};c) \times p(y=c)$
  - This posterior probability represents the probability of class c for the observed feature vector  $\bar{x}$
  - Feature vector  $\bar{x}$  is generated for each class using class-conditional density  $p(x|y=c;\theta) \Rightarrow$  Generative Classifier
  - $\theta$  is estimated by fitting the model to training data by maximizing the joint log-likelihood
  - $\theta^* = arg \max_{i} log(p(y_i, \overline{x}_i | \theta))$

## **Classifier Categories - Recap**

- Discriminative Classifier
  - Given dataset  $\mathcal{D} = \{(\bar{x}_i, y_i)\}_{i=1}^N$
  - Goal is to compute the discriminative probability  $p(y=c|\bar{x})$  directly from the training data
  - The model is usually fit to training data by maximising the conditional log-likelihood

• 
$$\theta^* = arg \max_{\theta} \sum_{i} log(p(y_i|x_i,\theta))$$

# Challenges of Clear Class Separation: Beyond Probabilities and Margins

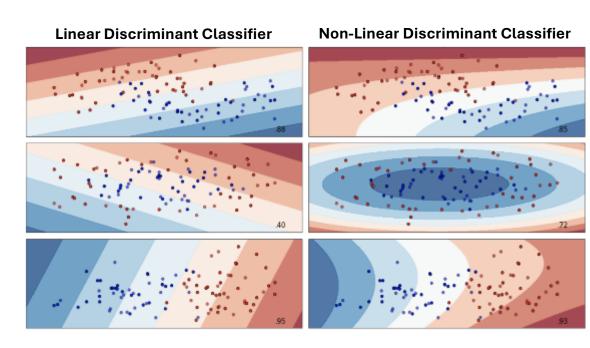
- Probability and decision boundary optimization-based methods are effective in general
- But aren't always ideal for maximizing the multi-class separation for overlapping complex datasets

Is there a better approach to maximize the spread between overlapping classes to reduce misclassification risk and maximizing multi-class separation?



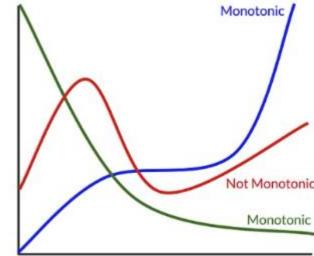
#### **Discriminant Functions**

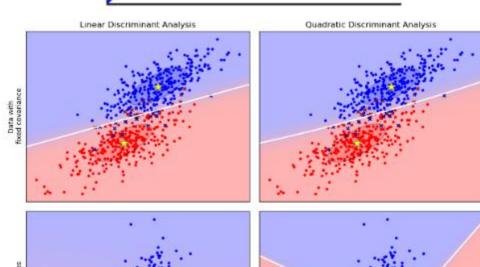
- Statistical mathematical functions to separate data points into different categories
- Assigns a score to each class for a given data point, the data point is assigned to the class with the highest score
- Data distribution plays a key role in defining the discriminant functions
- Based on the assumption that data follows/generated from a distributions like normal distribution
- Decision boundaries are defined based on statistical characteristics of data distribution
  - Mean, covariance
- Covariance describes the degree to which features vary together
  - Represented by covariance matrix for each class
- It is a statistical canonical form of multi-class classifiers

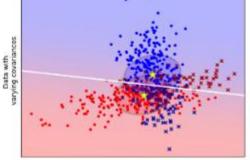


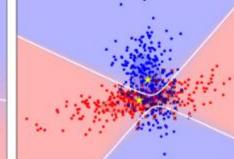
#### **Discriminant Functions**

- Simplifies class probabilities with an equivalent function that assigns a score to each class  $c_i$  for a given  $\overline{x}$ 
  - $g_i(\bar{x}) = f(P(c_i|\bar{x})), i = 1,2,...k$
  - f(.) Monotonically Increasing Function
    - If  $x_1 < x_2$ ,  $\Rightarrow f(x_1) \le f(x_2)$
    - f(x) can increase or stay constant but never decreases
  - $g_i(\bar{x})$  Discriminant Function of class i
- $\overline{x} \in c_l$ 
  - if  $g_l(\overline{x}) > g_j(\overline{x}) \ \forall j \neq i \text{ and } i, j = 1, 2, ... k$
  - $g_l(\overline{x}) = arg \max_{1 \le i \le k} g_i(\overline{x}) \Rightarrow \overline{x} \in c_l$
- Types
  - Linear Discriminants Linear boundaries between classes
  - Non-linear Discriminants Flexible boundaries for higher dimensional datasets







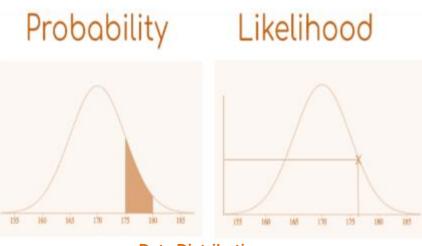


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## **Probability and Likelihood in Discriminant Functions**

- Probability is the likelihood of a possible result
- Likelihood is the process of determining the best data distribution for a given situation/data
- The discriminant scores are derived from log-likelihood functions of each class
- Likelihoods incorporate mean and covariance of each class
- The discriminant functions maximize the likelihood
- A point belonging to a particular class is decided by taking mean and covariance of each class into account
- Probability measures the fitness of data given a specific distribution
- Likelihood measures the fitness of a model given some data

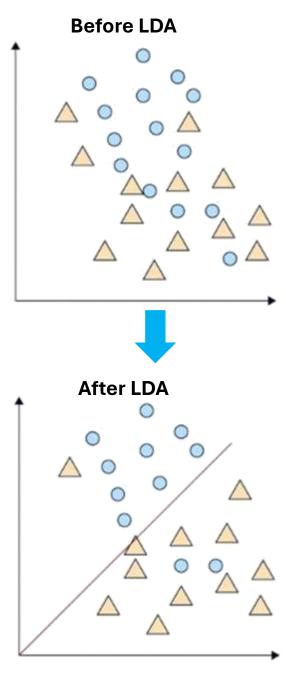
Probability	Likelihood
Predicts the chance of future or unknown outcomes	Measures how well a model or parameter explains observed data
Fixed model, variable data	Fixed data, variable model parameters
Used in predictive contexts, like Bayesian inference	Used in parameter estimation, like MLE
"Given a fair die, what's the probability of rolling a 3?"	"Given the rolls we observed, how likely is it that this die is fair?"



**Data Distributions** 

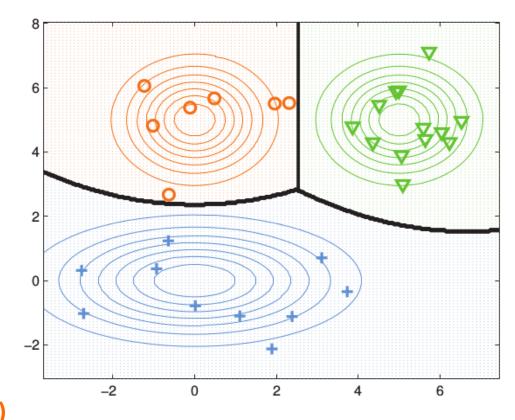
# **Linear Discriminant Analysis - LDA**

- A supervised learning model
- Uses linear discriminants to find a linear combination of features for multi-class separate
- Simplifies the discriminant function to a linear form
- Classes have the same geometric shape and orientation in the feature space
- Underlying Assumptions
  - Distribution Normality Each class is normally distributed
  - Distribution Covariance All classes share the same covariance matrix
- Models the difference between classes by focusing on maximizing the variance between them
- Shared covariance leads to linear decision boundaries
- Decision boundary is a line/hyperplane that lies midway between the means of the two classes



## **Gaussian Discriminant Analysis - GDA**

- Generalization of LDA allowing for different covariances for classes
- Underlying Assumptions
  - Distribution Normality Each class is normally distributed
  - Distribution Covariance Each class is allowed to have its own covariance matrix
- Shape and orientation of each class in the feature space can vary
- Models more complex class distributions with more parameters to estimate the covariance for each class individually
- Decision boundary is quadratic and curves based on the relative shape and spread of each class's covariance
- Individual covariances lead to flexible (quadratic/non-linear) decision boundaries



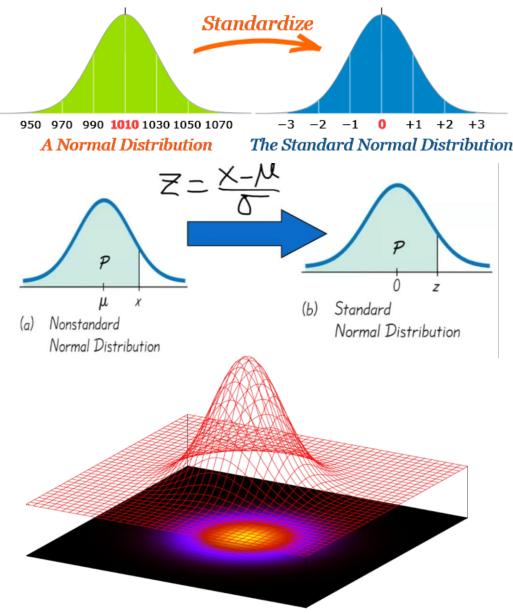
- Data is assumed to have Normal distribution  $\Rightarrow$  Gaussian Distribution  $\mathcal{N}(\mu, \sigma)$
- PDF of a univariate continuous variable  $X \in \mathbb{R}$  with Gaussian distribution  $X \sim \mathcal{N}(\mu, \sigma^2)$

• PDF - 
$$f_X(x) = P_X(X = x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\left(\frac{(x-\mu)^2}{2\sigma^2}\right)}$$

- Mean  $E\{X\} = \mu$
- Variance  $E\{(X-\mu)^2\} = \sigma^2$
- PDF of Multi-variate continuous variable  $\bar{X} \in \mathbb{R}^n$  with Gaussian Distribution  $\bar{X} \sim \mathcal{N}(\bar{\mu}, R)$

• PDF - 
$$f_{\bar{X}}(\bar{x}) = P_{\bar{X}}(\bar{x}) = \frac{1}{\sqrt{(2\pi)^n |R|}} e^{-\frac{1}{2}(\bar{x} - \bar{\mu})^T R^{-1}(\bar{x} - \bar{\mu})}$$

- Mean  $E\{\bar{X}\} = \bar{\mu}$
- Covariance Matrix  $E\{(\bar{x} \bar{\mu})(\bar{x} \bar{\mu})^T\} = R \in \mathbb{R}^{n \times n}, R = R^T, R \ge 0$
- *n* number of variables/dimensions/features
- Consider two classes of multi-variate (n-variate) Gaussian distributions
  - $\mathcal{C}_0: \mathcal{N}_{\mathcal{C}_0}(\bar{\mu}_0, R)$
  - $\mathcal{C}_1$ :  $\mathcal{N}_{\mathcal{C}_1}(\bar{\mu}_1, R)$
  - Class Prior Probabilities:  $p_0$ ,  $p_1$



Likelihoods of two classes

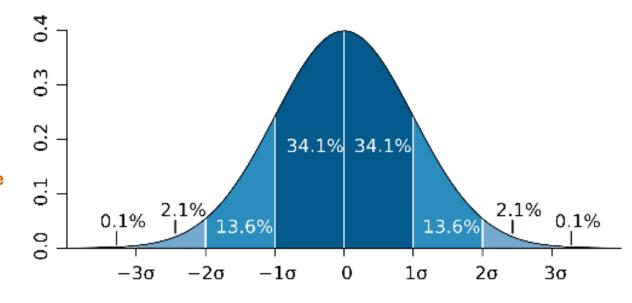
• 
$$p(\bar{x}; \mathcal{C}_0) = \frac{1}{\sqrt{(2\pi)^n |R|}} e^{-\frac{1}{2}(\bar{x} - \bar{\mu}_0)^T R^{-1}(\bar{x} - \bar{\mu}_0)}$$

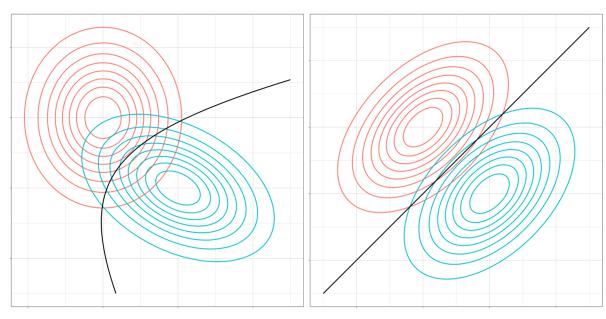
• 
$$p(\bar{x}; \mathcal{C}_1) = \frac{1}{\sqrt{(2\pi)^n |R|}} e^{-\frac{1}{2}(\bar{x} - \bar{\mu}_1)^T R^{-1}(\bar{x} - \bar{\mu}_1)}$$

- Choosing the class for classification
  - Maximum likelihood rule choose the class that maximizes the posterior probability
- Posterior probabilities
  - For generative classifier,  $p(y=c|\overline{x};\theta) \propto p(\overline{x};c) \times p(y=c)$
  - Class  $C_0 \Rightarrow p(y = C_0 | \overline{x}; \theta_{C_0}) \propto p(\overline{x}; C_0) \times p_0$
  - Class  $C_1 \Rightarrow p(y = C_1 | \overline{x}; \theta_{C_1}) \propto p(\overline{x}; C_1) \times p_1$
- Choose  $C_0: p(\overline{x}; C_0) \times p_0 \ge p(\overline{x}; C_1) \times p_1$

• 
$$\frac{1}{\sqrt{(2\pi)^n|R|}}e^{-\frac{1}{2}(\bar{x}-\bar{\mu}_0)^TR^{-1}(\bar{x}-\bar{\mu}_0)} \ge \frac{1}{\sqrt{(2\pi)^n|R|}}e^{-\frac{1}{2}(\bar{x}-\bar{\mu}_1)^TR^{-1}(\bar{x}-\bar{\mu}_1)}$$

- Taking natural log both sides
- $\ln p_0 \frac{1}{2}(\bar{x} \bar{\mu}_0)^T R^{-1}(\bar{x} \bar{\mu}_0) \ge \ln p_1 \frac{1}{2}(\bar{x} \bar{\mu}_1)^T R^{-1}(\bar{x} \bar{\mu}_1)$
- $\Rightarrow \ln p_0 \frac{1}{2} (\bar{x} \bar{\mu}_0)^T R^{-1} (\bar{x} \bar{\mu}_0) \ge \ln p_1 \frac{1}{2} (\bar{x} \bar{\mu}_1)^T R^{-1} (\bar{x} \bar{\mu}_1)$
- $\Rightarrow \ln p_0 \ln p_1 \ge \frac{1}{2} (\bar{x} \bar{\mu}_0)^T R^{-1} (\bar{x} \bar{\mu}_0) \frac{1}{2} (\bar{x} \bar{\mu}_1)^T R^{-1} (\bar{x} \bar{\mu}_1)$
- $\Rightarrow ln \frac{p_0}{n_1} \ge \frac{1}{2} (\bar{x} \bar{\mu}_0)^T R^{-1} (\bar{x} \bar{\mu}_0) \frac{1}{2} (\bar{x} \bar{\mu}_1)^T R^{-1} (\bar{x} \bar{\mu}_1)$





• 
$$\Rightarrow (\bar{x} - \bar{\mu}_0)^T R^{-1} (\bar{x} - \bar{\mu}_0) - (\bar{x} - \bar{\mu}_1)^T R^{-1} (\bar{x} - \bar{\mu}_1) \le 2 \ln \frac{p_0}{p_1}$$

• 
$$(\bar{x} - \bar{\mu}_0)^T R^{-1} (\bar{x} - \bar{\mu}_0)$$
,  $(\bar{x} - \bar{\mu}_1)^T R^{-1} (\bar{x} - \bar{\mu}_1)$  are quadratic forms

• 
$$\Rightarrow (\bar{x}^T - \bar{\mu}_0^T)R^{-1}(\bar{x} - \bar{\mu}_0) - (\bar{x}^T - \bar{\mu}^T)R^{-1}(\bar{x} - \bar{\mu}_1) \le 2 \ln \frac{p_0}{p_1}$$

• 
$$\Rightarrow (\bar{x}^T - \bar{\mu}_0^T)R^{-1}\bar{x} - (\bar{x}^T - \bar{\mu}_0^T)R^{-1}\bar{\mu}_0 - (\bar{x}^T - \bar{\mu}_1^T)R^{-1}\bar{x} + (\bar{x}^T - \bar{\mu}_1^T)R^{-1}\bar{\mu}_1 \le 2 \ln \frac{p_0}{p_1}$$

$$\bullet \Rightarrow \bar{x}^T R^{-1} \bar{x} - \bar{\mu}_0^T R^{-1} \bar{x} - \bar{x}^T R^{-1} \bar{\mu}_0 + \bar{\mu}_0^T R^{-1} \bar{\mu}_0 - \bar{x}^T R^{-1} \bar{x} + \bar{\mu}_1^T R^{-1} \bar{x} + \bar{x}^T R^{-1} \bar{\mu}_1 - \bar{\mu}_1^T R^{-1} \bar{\mu}_1 \le 2 \ln \frac{p_0}{p_1}$$

• 
$$(ABC)^T = C^T B^T A^T$$
 and  $A^T = B$  and  $B^T = A \Rightarrow A = B$ 

• 
$$\Rightarrow (\bar{x}^T R^{-1} \bar{\mu}_0)^T = \bar{\mu}_0^T R^{-1} \bar{x}$$
 and  $(\bar{\mu}_0^T R^{-1} \bar{x})^T = \bar{x}^T R^{-1} \bar{\mu}_0 \Rightarrow \bar{\mu}_0^T R^{-1} \bar{x} = \bar{x}^T R^{-1} \bar{\mu}_0$ 

• 
$$\Rightarrow (\bar{x}^T R^{-1} \bar{\mu}_1)^T = \bar{\mu}_1^T R^{-1} \bar{x}$$
 and  $(\bar{\mu}_1^T R^{-1} \bar{x})^T = \bar{x}^T R^{-1} \bar{\mu}_1 \Rightarrow \bar{\mu}_1^T R^{-1} \bar{x} = \bar{x}^T R^{-1} \bar{\mu}_1$ 

• 
$$\Rightarrow -2\bar{\mu}_0^T R^{-1}\bar{x} + \bar{\mu}_0^T R^{-1}\bar{\mu}_0 + 2\bar{\mu}_1^T R^{-1}\bar{x} - \bar{\mu}_1^T R^{-1}\bar{\mu}_1 \le 2 \ln \frac{p_0}{p_1}$$

$$\bullet \Rightarrow 2(\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1 \leq 2 \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1} \\ \Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} + \frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) \leq \ln \frac{p_0}{p_1}$$

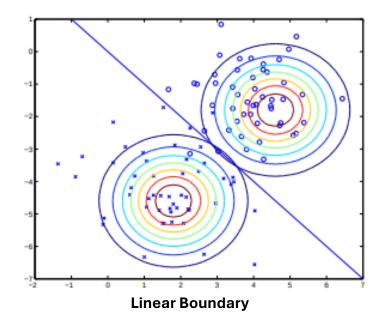
• 
$$\frac{1}{2}(\bar{\mu}_0^T R^{-1}\bar{\mu}_0 - \bar{\mu}_1^T R^{-1}\bar{\mu}_1) = -\frac{1}{2}(\bar{\mu}_1 - \bar{\mu}_0)^T R^{-1}(\bar{\mu}_1 + \bar{\mu}_0)$$

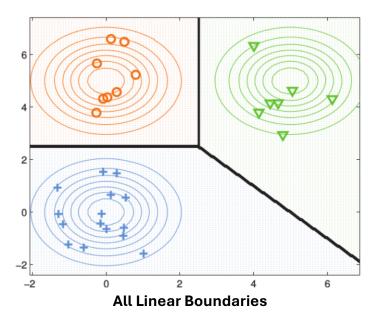
• 
$$\Rightarrow (\bar{\mu}_1^T - \bar{\mu}_0^T)R^{-1}\bar{x} - \frac{1}{2}(\bar{\mu}_1 - \bar{\mu}_0)^T R^{-1}(\bar{\mu}_1 + \bar{\mu}_0) \le \ln \frac{p_0}{p_1}$$

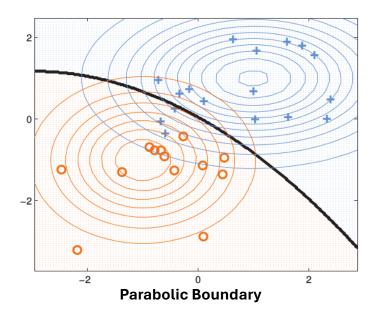
• 
$$\Rightarrow (\bar{\mu}_1 - \bar{\mu}_0)^T R^{-1} \left( \bar{x} - \frac{1}{2} (\bar{\mu}_1 + \bar{\mu}_0) \right) \leq \ln \frac{p_0}{p_1} \Rightarrow (\bar{\mu}_0 - \bar{\mu}_1)^T R^{-1} \left( \bar{x} - \frac{1}{2} (\bar{\mu}_1 + \bar{\mu}_0) \right) \geq \ln \frac{p_0}{p_1}$$

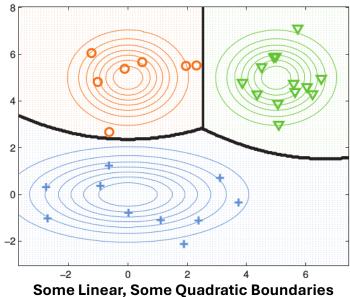
• Choose 
$$C_0: (\overline{\mu}_0 - \overline{\mu}_1)^T R^{-1} \left( \overline{x} - \frac{1}{2} (\overline{\mu}_1 + \overline{\mu}_0) \right) \ge \ln \frac{p_0}{p_1}$$

- Simplifying, GDA classification rule reduces to:
  - Choose  $C_0$ :  $\overline{h}^T(\overline{x} \widetilde{\mu}) \ge ln \frac{p_1}{p_0}$
  - Choose  $C_1$ :  $\overline{h}^T(\overline{x} \widetilde{\mu}) < ln \frac{p_1}{p_0}$
  - $\overline{h} = R^{-1}(\overline{\mu}_0 \overline{\mu}_1)$
  - $\widetilde{\mu} = \frac{1}{2}(\overline{\mu}_0 + \overline{\mu}_1)$
- $\overline{h}^T(\overline{x}-\widetilde{\mu})$ =  $\ln \frac{p_1}{p_0}$  is a Linear Equation  $\Rightarrow$  Hyperplane  $\Rightarrow$  Linear Classifier









## **Efficiency Metrics**

- Training Time
  - LDA and GDA have relatively low computational complexity, as they involve calculating mean and covariance for each class
  - For LDA with shared covariance, complexity is  $O(Nd^2)$ 
    - N Number of training samples
    - *d* feature dimension
- Prediction Time
  - Linear Proportional to number of feature dimensions
- Accuracy
  - The percentage of correctly classified instances out of the total instances.
- Precision
  - The ratio of true positives to the sum of true positives and false positives
- Recall Sensitivity
  - The ratio of true positives to the sum of true positives and false negatives
- F1 Score
  - The harmonic mean of precision and recall
  - Between 0 and 1
    - 1 Perfect precision and recall model correctly identifies all true positives with no false positives or false negatives
    - 0 Model is entirely ineffective for positive class detection
- ROC-AUC
  - Measures the model's ability to distinguish between classes across different thresholds
  - A higher AUC indicates better performance, with a value of 1 indicating perfect classification

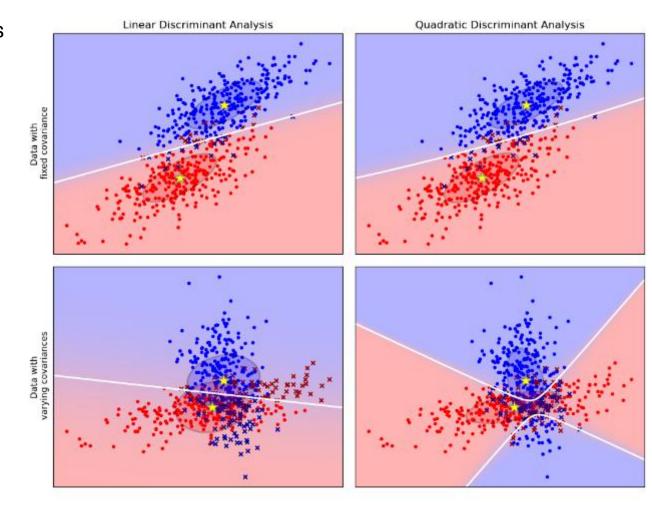
## **Key Takeaways**

#### LDA

- Best suited for problems where class distributions have equal covariance
- Linear decision boundaries and high efficiency make it suitable for high-dimensional datasets

#### • GDA

- Flexible in handling different covariance matrices for each class, leading to quadratic decision boundaries
- Better suited for problems with complex, nonlinear class boundaries



#### **Project Announcement**

- Algorithm of Application
  - LDA/GDA
- Project Title
  - Inferring Breast Cancer/Malignancy from Diagnosis Data and Classification Models Comparative Analysis
- Project Objective
  - Implement LDA/GDA for inferring breast cancer disease and analyze comparative classification models performance you have learnt in AAM-IPL on the Breast Cancer Wisconsin Dataset
  - Optionally, use wine data set from scikit-learn and see the comparative performance of all classification models you have learnt in AAM-IPL
- Dataset Breast Cancer
  - Description:
    - Implements an LDA/GDA classifier to predict the class of breast tumor (breast cancer) from the provided dataset – malignant or benign.
    - The dataset should be used for training a SVM classifier and evaluate its performance using various metrics such as accuracy, precision, recall, F1-score.
  - Dataset Details:
    - The breast cancer dataset consists of 569 samples, each representing a patient with a set of features
  - Data Source/Published By:
    - Breast Cancer Wisconsin (Diagnostic) UCI Machine Learning Repository
    - Nuclear feature extraction for breast tumor diagnosis | Semantic Scholar
    - Supported by CS Department, University of Wisconsin-Madison
  - Features & Data Download Link
    - o Breast Cancer Wisconsin (Diagnostic) UCI Machine Learning Repository
    - Alternatively, you can load the data directly using sklearn datasets as shown on the side code snippet

```
from sklearn.datasets import load_breast_cancer
import pandas as pd

# Load the dataset
data = load_breast_cancer()
X = pd.DataFrame(data.data,
columns=data.feature_names)
y = pd.Series(data.target, name="target")
```

#### **Project Announcement**

- Dataset Wine Data
  - Description:
    - The Wine dataset contains information about chemical analysis of wines from the Italian region of Piedmont, which are produced by three different cultivars. This dataset is widely used for classification tasks, particularly for distinguishing wine types based on chemical properties.
  - Dataset Details:
    - Number of Instances: 178
    - Number of Features: 13 (not including the target class)
    - Target: The dataset has 3 classes, corresponding to three wine cultivars (Class 0, Class 1, and Class 2)
  - Data Source/Published By:
    - Published By: This dataset was made available by the UCI Machine Learning Repository.
    - Original Source: Forina, M., et al. (1991) in "PARVUS An Extendible Package for Data Exploration, Classification and Correlation"
  - Features
    - Alcohol, Malic acid, Ash, Alcalinity of ash, Magnesium, Total phenols, Flavanoids
    - Non-flavanoid phenols, Proanthocyanins, Color intensity, Hue
    - OD280/OD315 of diluted wines, Proline
    - Each feature represents a chemical property used to classify the wine samples
  - Data Download Link
    - You can download the Wine dataset from the UCI Machine Learning Repository
       <u>UCI Wine Dataset</u>
    - Alternatively, you can load the data directly using sklearn datasets as below

```
from sklearn.datasets import load_wine
import pandas as pd

# Load the dataset
data = load_wine()
X = pd.DataFrame(data.data,
columns=data.feature_names)
y = pd.Series(data.target, name="target")
```

## **Project Implementation Steps**

- 1.Import necessary libraries
- Load and preprocess dataset
- Split dataset into training and test sets
- Standardize features
- Define models
- Initialize results list
- Define function to add watermark to plots
- Train models and evaluate
- Convert results to data frame
- Plotting metrics and times with AAM-IPL watermark
- Plot combined ROC curves with AAM-IPL watermark
- Plot combined confusion matrices with AAM-IPL watermark
- Generate the PDF of code and output of project Jupyter file



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# **Project Implementation Demo**







# Interested in building a Gen AI application? Reach out to <a href="mailto:venkat@brillium.in">venkat@brillium.in</a>

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