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**Grade 10.00** out of 10.00 (**100**%)

Question **1** 

Correct

Mark 1.00 out of 1.00

 $\ensuremath{\mathbb{V}}$  Flag question

Consider the multiple transmit antenna channel estimation model given by  $\bar{\mathbf{y}} = \mathbf{X}\bar{\mathbf{h}} + \bar{\mathbf{v}}$ , with,  $\mathbf{X}, \bar{\mathbf{y}}$  denoting the pilot matrix, output vector, respectively and  $\bar{\mathbf{v}}$  denoting the additive noise vector comprising of zero-mean i.i.d. Gaussian noise samples of variance  $\sigma^2$ . The channel coefficients are zero-mean i.i.d. Gaussian with variance  $\sigma_h^2$ . The error covariance of the MMSE estimate of the channel vector  $\bar{\mathbf{h}}$  is

### Select one:

$$\bigcirc \quad \left(\frac{\mathbf{x}^T\mathbf{x}}{\sigma_h^2} + \frac{\mathbf{I}}{\sigma^2}\right)^{-1}$$

$$\bigcirc \left(\frac{\mathbf{x}\mathbf{x}^T}{\sigma_h^2} + \frac{1}{\sigma^2}\right)^{-1}$$

$$\bigcirc \quad \left(\frac{\sigma^2}{\sigma_h^2} \mathbf{X} \mathbf{X}^T + \mathbf{I}\right)^{-1}$$

# Your answer is correct.

The correct answer is:  $\left(\frac{\mathbf{x}^T\mathbf{x}}{\sigma^2} + \frac{1}{\sigma_h^2}\right)^{-1}$ 

Question **2** 

Correct

Mark 1.00 out of 1.00

The expression for the

### MMSE estimate h is

## Select one:

$$E\{\bar{\mathbf{h}}\}$$

$$E\{\bar{\mathbf{h}}|\bar{\mathbf{x}}\}$$

Your answer is correct.

The correct answer is:  $E\{\bar{\mathbf{h}}|\bar{\mathbf{y}}\}$ 

Question **3** 

Correct

Mark 1.00 out of 1.00

Your answer is correct.

The correct answer is: cross-covariance matrix

Question **6** 

Correct

Mark 1.00 out of 1.00

The MISO channel estimation problem can be formulated as

### Select one:

$$\begin{bmatrix}
y(1) \\
y(2) \\
\vdots \\
y(N)
\end{bmatrix} = \begin{bmatrix}
\bar{\mathbf{x}}(1) \\
\bar{\mathbf{x}}(2) \\
\vdots \\
\bar{\mathbf{x}}(N)
\end{bmatrix} \bar{\mathbf{h}} + \begin{bmatrix}
v(1) \\
v(2) \\
\vdots \\
v(N)
\end{bmatrix}$$

$$\underbrace{\begin{bmatrix} y(1) \\ y(2) \\ \vdots \\ y(N) \end{bmatrix}}_{\bar{\mathbf{v}}} = \underbrace{\begin{bmatrix} \bar{\mathbf{x}}(1) \\ \bar{\mathbf{x}}(2) \\ \vdots \\ \bar{\mathbf{x}}(N) \end{bmatrix}}_{\bar{\mathbf{x}}} \bar{\mathbf{h}}^T + \underbrace{\begin{bmatrix} v(1) \\ v(2) \\ \vdots \\ v(N) \end{bmatrix}}_{\bar{\mathbf{v}}}$$

$$\begin{bmatrix}
y(1) \\
y(2) \\
\vdots \\
y(N)
\end{bmatrix} = \begin{bmatrix}
\bar{\mathbf{x}}^T(1) \\
\bar{\mathbf{x}}^T(2) \\
\vdots \\
\bar{\mathbf{x}}^T(N)
\end{bmatrix} \bar{\mathbf{h}}^T + \begin{bmatrix}
v(1) \\
v(2) \\
\vdots \\
v(N)
\end{bmatrix}$$

$$\underbrace{\begin{bmatrix} y(1) \\ y(2) \\ \vdots \\ y(N) \end{bmatrix}}_{\bar{\mathbf{v}}} = \underbrace{\begin{bmatrix} \bar{\mathbf{x}}^T(1) \\ \bar{\mathbf{x}}^T(2) \\ \vdots \\ \bar{\mathbf{x}}^T(N) \end{bmatrix}}_{\bar{\mathbf{x}}} \bar{\mathbf{h}} + \underbrace{\begin{bmatrix} v(1) \\ v(2) \\ \vdots \\ v(N) \end{bmatrix}}_{\bar{\mathbf{v}}}$$

Your answer is correct.

The correct answer is:

$$\underbrace{\begin{bmatrix} y(1) \\ y(2) \\ \vdots \\ y(N) \end{bmatrix}}_{\bar{\mathbf{y}}} = \underbrace{\begin{bmatrix} \bar{\mathbf{x}}^{T}(1) \\ \bar{\mathbf{x}}^{T}(2) \\ \vdots \\ \bar{\mathbf{x}}^{T}(N) \end{bmatrix}}_{\bar{\mathbf{x}}} \bar{\mathbf{h}} + \underbrace{\begin{bmatrix} v(1) \\ v(2) \\ \vdots \\ v(N) \end{bmatrix}}_{\bar{\mathbf{v}}}$$

Question 7

Correct

Mark 1.00 out of 1.00

Consider a multi-antenna channel estimation scenario with N=4 pilot vectors, with the pilot matrix  $\mathbf{X}$  and receive vector  $\mathbf{\bar{y}}$  given below

$$\mathbf{X} = \begin{bmatrix} 1 & 1 \\ -1 & 1 \\ 1 & -1 \\ -1 & -1 \end{bmatrix}, \bar{\mathbf{y}} = \begin{bmatrix} -2 \\ 1 \\ -1 \\ -2 \end{bmatrix}$$

Let the channel coefficients be i.i.d. Gaussian with variance  $\sigma_h^2 = 1$  and noise variance  $\sigma^2 = 2$ . The MMSE estimate of the channel vector  $\bar{\mathbf{h}}$  is

# Select one:

$$\begin{bmatrix} -\frac{4}{3} \\ -\frac{2}{3} \end{bmatrix}$$

$$\begin{bmatrix} \frac{2}{3} \\ -\frac{1}{3} \end{bmatrix}$$

Your answer is correct.

The correct answer is:  $\begin{bmatrix} -\frac{1}{3} \\ \frac{1}{3} \end{bmatrix}$ 

Question  ${\bf 8}$ 

Correct

Mark 1.00 out of 1.00

▼ Flag question

Consider a multi-antenna channel estimation scenario with N=4 pilot vectors, with the pilot matrix X given below

$$\mathbf{X} = \begin{bmatrix} 1 & 1 \\ -1 & 1 \\ 1 & -1 \\ -1 & -1 \end{bmatrix}$$

Let the channel coefficients be i.i.d. Gaussian with variance  $\sigma_h^2 = 1$  and noise variance  $\sigma^2 = 2$ . The error covariance of the LMMSE estimate of  $\bar{\mathbf{h}}$  is,

Select one:

$$\begin{bmatrix}
\frac{1}{2} & 0 \\
0 & \frac{1}{2}
\end{bmatrix}$$

Your answer is correct.

The correct answer is:  $\begin{bmatrix} \frac{1}{3} & 0 \\ 0 & \frac{1}{3} \end{bmatrix}$ 

Question **9** 

Correct

Mark 1.00 out of 1.00

ℙ Flag question

Consider a multi-antenna channel estimation scenario with N=4 pilot vectors, with the pilot matrix  $\mathbf{X}$  and receive vector  $\mathbf{\bar{y}}$  given below

$$\mathbf{X} = \begin{bmatrix} 1 & 1 \\ -1 & 1 \\ 1 & -1 \\ -1 & -1 \end{bmatrix}, \bar{\mathbf{y}} = \begin{bmatrix} -2 \\ 1 \\ -1 \\ -2 \end{bmatrix}$$

Let the channel coefficients be i.i.d. zero-mean Gaussian with variance  $\sigma_h^2 = 1$ . The LMMSE estimate as the noise variance  $\sigma^2 \rightarrow 0$  is

Select one:

$$\begin{bmatrix} -\frac{1}{2} \\ -1 \end{bmatrix}$$

$$\begin{bmatrix} -\frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$$

$$\begin{bmatrix} -\frac{1}{4} \\ 1 \end{bmatrix}$$

Your answer is correct.

The correct answer is:  $\begin{bmatrix} -\frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$ 

Question 10

Correct

Mark 1.00 out of 1.00

▼ Flag question

Consider the fading channel estimation problem where the output symbol is y(k) = hx(k) + v(k), with h, x(k), v(k) denoting the real channel coefficient, pilot symbol and noise sample respectively. Let  $\bar{\mathbf{x}} = [x(1) \quad x(2) \quad ... \quad x(N)]^T$  denote the pilot vector of transmitted pilot symbols and  $\bar{\mathbf{y}} = [y(1) \quad y(2) \quad ... \quad y(N)]^T$  denote the corresponding received symbol vector. Let v(k) be IID Gaussian noise with zero-mean and variance  $\sigma^2$ . Let the channel coefficient h be Gaussian with mean  $\mu_h$  and variance  $\sigma_h^2$ . The MMSE estimate  $\hat{h}$  of the channel coefficient h is

Select one:

$$\bigcirc \quad \frac{\frac{\mathbf{x}^T\mathbf{y}}{\sigma^2} + \frac{\mu_h}{\sigma_h^2}}{\frac{\|\mathbf{x}\|^2}{\sigma^2} + \frac{1}{\sigma_h^2}} \quad \checkmark$$

$$\frac{\mathbf{x}^T \mathbf{y}}{\frac{\sigma_h^2}{\sigma_h^2} + \frac{\mu_h}{\sigma^2}}$$

$$\frac{\mathbf{x}^T \mathbf{y}}{\sigma^2 \|\mathbf{x}\|^2} + \frac{\mu_h}{\sigma_h^2}$$

$$\frac{\|\mathbf{x}\|^2}{\sigma^2} + \frac{1}{\sigma_h^2}$$

$$\frac{\frac{\mathbf{x}^T \mathbf{y}}{\sigma^2}}{\frac{N}{\sigma^2} + \frac{1}{\sigma^2}}$$

Your answer is correct.

The correct answer is: 
$$\frac{\frac{\mathbf{x}^T\mathbf{y}}{\sigma^2} + \frac{\mu_h}{\sigma_h^2}}{\frac{\|\mathbf{x}\|^2}{\sigma^2} + \frac{1}{\sigma_h^2}}$$

Finish review