Started on Sunday, 26 November 2023, 5:30 PM

State Finished

Completed on Sunday, 26 November 2023, 6:24 PM

**Time taken** 53 mins 57 secs

**Grade 9.00** out of 10.00 (**90**%)

Question 1

Correct

Mark 1.00 out of 1.00

Remove flag

The integral  $\int_{-\infty}^{\infty} a^2 e^{-a^2} da$  evaluates to

Select one:

- O 0
- $\frac{\sqrt{\pi}}{2\sqrt{2}}$
- $\odot$   $\frac{\sqrt{\pi}}{2}$
- $\sqrt{\frac{\pi}{2}}$

Your answer is correct.

The correct answer is:  $\frac{\sqrt{\pi}}{2}$ 

Question 2

Correct

Mark 1.00 out of 1.00

SER of M -ary QAM for  $SNR = \rho$  is

Select one:

- $\qquad 4\left(1-\frac{1}{\sqrt{M}}\right)Q\left(\sqrt{\frac{\rho}{(M-1)}}\right)$
- $\bigcirc \quad \left(1 \frac{1}{\sqrt{M}}\right) Q\left(\sqrt{\frac{3\rho}{(M-1)}}\right)$
- $\bigcirc 4\left(1-\frac{1}{M}\right)Q\left(\sqrt{\frac{3\rho}{(\sqrt{M}-1)}}\right)$

Your answer is correct.

The correct answer is:  $4\left(1-\frac{1}{\sqrt{M}}\right)Q\left(\sqrt{\frac{3\rho}{(M-1)}}\right)$ 

Question 3

Incorrect

Mark 0.00 out of 1.00

Remove flag

Let  $x_i$  denote i.i.d. zero-mean Gaussian random variables with  $\sigma = 2$ . Then,  $\sum_{i=1}^{N} x_i^2$  equals the random variable

#### Select one:

- $\chi_N^2$  ×
- $\frac{1}{2}\chi_N^2$
- $2\chi_N^2$
- $4\chi_N^2$

Your answer is incorrect.

The correct answer is:  $4\chi_N^2$ 

# Question 4

Correct

Mark 1.00 out of 1.00

 $\ensuremath{\mathbb{P}}$  Flag question

The PDF of  $\chi_N^2$ -Central chi-squared RV with N degrees of freedom is

## Select one:

$$\frac{1}{2^{\frac{N}{2}-1}\Gamma(\frac{N}{2})} x^{\frac{N}{2}} e^{-\frac{1}{2}x}, \ x \ge 0$$

$$\frac{1}{\frac{N}{2^{\frac{N}{2}}\Gamma(N)}} x^{\frac{N}{2}-1} e^{-x}, \ x \ge 0$$

$$\frac{1}{2^{\frac{1}{2}}\Gamma(\frac{1}{2})} x^{\frac{N}{2}-1} e^{-\frac{1}{2}x}, \ x \ge 0$$

Your answer is correct.

The correct answer is:  $\frac{1}{2^{\frac{N}{2}}\Gamma\left(\frac{N}{2}\right)}x^{\frac{N}{2}-1}e^{-\frac{1}{2}x}$ ,  $x\geq 0$ 

Question **5** 

Correct

Mark 1.00 out of 1.00

The  $P_D$  for the random signal detection problem is

# Select one:

$$\frac{\Gamma\left(\frac{N}{2},\frac{\gamma}{\sigma^2+\sigma_S^2}\right)}{\Gamma\left(\frac{N}{2}\right)}$$

$$\bigcirc \quad Q\left(\frac{\gamma}{\sigma^2 + \sigma_s^2}\right)$$

$$\frac{\Gamma\left(\frac{N}{2}, \frac{\gamma}{\sigma^2}\right)}{\Gamma\left(\frac{N}{2}\right)}$$

Your answer is correct.

The correct answer is:  $Q_{\chi_N^2} \left( \frac{\gamma}{\sigma^2 + \sigma_\sigma^2} \right)$ 

Question 6

Correct

Mark 1.00 out of 1.00

Let U denote a central  $\chi^2_{50}$  RV. Then, variance of U equals

#### Select one:

- ◎ 100 ✔
- 2500
- **200**
- 400

Your answer is correct.

The correct answer is: 100

Question 7

Correct

Mark 1.00 out of 1.00

The GLRT problem described in lectures is

### Select one:

- $\mathcal{H}_0: \bar{\mathbf{y}} = \bar{\mathbf{v}}, \mathcal{H}_1: \bar{\mathbf{y}} = A\bar{\mathbf{s}} + \bar{\mathbf{v}}, \text{ where } A, \bar{\mathbf{s}} \text{ are unknown}$
- $\mathcal{H}_0: \bar{\mathbf{y}} = \bar{\mathbf{v}}, \mathcal{H}_1: \bar{\mathbf{y}} = A\bar{\mathbf{s}} + \bar{\mathbf{v}}$ , where  $\bar{\mathbf{s}}$  is unknown and A is unknown
- $\mathcal{H}_0: \bar{\mathbf{y}} = \bar{\mathbf{v}}, \mathcal{H}_1: \bar{\mathbf{y}} = A\bar{\mathbf{s}} + \bar{\mathbf{v}}, \text{ where } A \text{ is unknown and } \bar{\mathbf{s}} \text{ is known}$
- $\mathcal{H}_0: \bar{\mathbf{y}} = \bar{\mathbf{v}}, \mathcal{H}_1: \bar{\mathbf{y}} = A\bar{\mathbf{s}} + \bar{\mathbf{v}}, \text{ where } A, \bar{\mathbf{s}} \text{ are known}$

Your answer is correct.

The correct answer is:  $\mathcal{H}_0: \bar{\mathbf{y}} = \bar{\mathbf{v}}, \mathcal{H}_1: \bar{\mathbf{y}} = A\bar{\mathbf{s}} + \bar{\mathbf{v}}$ , where A is unknown and  $\bar{\mathbf{s}}$  is known

Question 8

Correct

Mark 1.00 out of 1.00

Consider  $\gamma=4,\,\sigma^2=4,\,\bar{\mathbf{s}}=[1\quad -1\quad 1\quad -1]^T$ .  $P_{FA}$  for the GLRT described in class is

# Select one:

- $Q = 2Q\left(\frac{1}{\sqrt{2}}\right)$
- $QQ(\sqrt{2})$
- 2Q(1) 

  ✓

Q(2)

Your answer is correct.

The correct answer is: 2Q(1)

Question 9

Correct

Mark 1.00 out of 1.00

#### Cognitive Radio allows

#### Select one:

- Secondary users to always access licensed spectrum
- Primary users to access spectrum only in limited slots
- Primary users to sense the spectrum before accessing
- ullet Secondary users to access licensed spectrum when there is a spectral hole  $\checkmark$

## Your answer is correct.

The correct answer is: Secondary users to access licensed spectrum when there is a spectral hole

Question 10

Correct

Mark 1.00 out of 1.00

The probability of detection for spectrum sensing for  $N=10,\,\sigma^2=2,\,\sigma_s^2=10,$  is

Select one:

- $\bigcirc \quad Q_{\chi^2_{20}}\left(\frac{\gamma}{12}\right)$
- $Q_{\chi_{10}^2}\left(\frac{\gamma}{12}\right)$
- $Q_{\chi_{10}^2}\left(\frac{\gamma}{6}\right)$

Your answer is correct.

The correct answer is:  $Q_{\chi^2_{20}}\left(\frac{\gamma}{6}\right)$ 

Finish review