

Assignment 5

Digital Communication System-I

May 2023

Please answer the following questions:

Consider a cascaded binary symmetric channel (BSC) in Figure 1 to answer Q1-Q2.

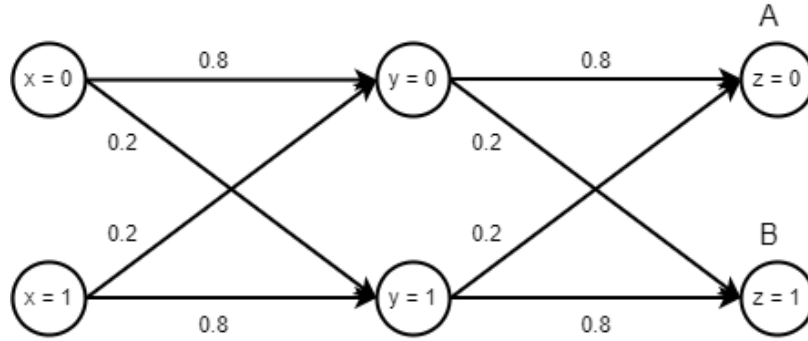


Figure 1: Cascaded BSC

Q 1: Find out the probability $Pr(z = 1)$ and $Pr(z = 0)$ at node A and B, respectively, if a priori probability is given as $Pr(x = 0) = 0.3$ and $Pr(x = 1) = 0.7$.

- (a) 0.572,0.428
- (b) 0.428,0.572
- (c) 0.56,0.44
- (d) 0.44,0.56

Q 2: MAP decision rule is same as the ML decision rule if $Pr(y = 0|x = 1) = Pr(y = 1|x = 0) = 0.5$.

- (a) True
- (b) False

Q 3: Why do we need optimum detection rule in communication system?

- (a) Minimize the energy consumption
- (b) Effective use of channel bandwidth
- (c) Minimize the probability of error
- (d) To detect and correct the error

Q 4: If the bit error probability for BPSK modulated signal with coherent detection over an AWGN channel with the power spectral density of the channel noise is $N_0/2$ is 0.1587 then find out the SNR (in dB) in the AWGN channel. The two signals $s_1(t)$ and $s_2(t)$ are assumed to be equi-probable with bit energy E_b ?

- (a) 10 dB

- (b) 5
- (c) -3 dB
- (d) 2 dB

Q 5: The vector representations of the binary equiprobable orthogonal signal set is given as $S_1 = (\sqrt{2E_b}, 0)$ and $S_2 = (0, \sqrt{2E_b})$. What is their error probability over the AWGN channel?

- (a) $Q\left(\sqrt{\frac{2E_b}{N_0}}\right)$
- (b) $Q\left(\sqrt{\frac{4E_b}{N_0}}\right)$
- (c) $Q\left(\sqrt{\frac{E_b}{N_0}}\right)$
- (d) $Q\left(\sqrt{\frac{E_b}{2N_0}}\right)$

Q 6: Probability of error depends on which of the following factor(s)?

- (a) Euclidean distances among signal vectors in signal space diagram
- (b) Positions of signal vectors in signal space diagram
- (c) Both (a) and (b)
- (d) None of these

Q 7: Assume a binary antipodal signalling scheme $s_1(t) = \sqrt{E_b}$ and $s_2(t) = -\sqrt{E_b}$, with a priori probability of $s_1(t) = 0.2$ and of $s_2(t) = 0.8$ over an AWGN channel with the power spectral density of the channel noise is $N_0/2$. Find out the threshold (r_{th}) for the decision region

- (a) $r_{th} = \frac{0.1N_0}{\sqrt{E_b}}$
- (b) $r_{th} = \frac{0.4N_0}{\sqrt{E_b}}$
- (c) $r_{th} = \frac{0.69N_0}{\sqrt{E_b}}$
- (d) $r_{th} = \frac{0.38N_0}{\sqrt{E_b}}$

Q 8: Which of the following statement about the Q function is correct?

- (a) Q function is an even function
- (b) $Q(x)$ is a decreasing function for $x > 0$
- (c) Both (a) and (b)
- (d) None of the above

Q 9: Which of the following expressions represent(s) the ML decision rule for AWGN vector channel?

- (a) $\hat{m} = \arg \min_{1 \leq m \leq M} \|r - s_m\|^2$
- (b) $\hat{m} = \arg \max_{1 \leq m \leq M} \left(\int_0^T r(t)s_m(t)dt + \frac{1}{2} \int_0^T |s_m(t)|^2 dt \right)$
- (c) $\hat{m} = \arg \max_{1 \leq m \leq M} \|r - s_m\|^2$
- (d) None of the above

Q 10: Consider the following signal

$$s(t) = \begin{cases} \frac{A}{T} \sin(2\pi f_c t), & \text{if } 0 \leq t \leq T \\ 0, & \text{otherwise} \end{cases}$$

What is the output of the matched filter at $t = T$?

(a) $\frac{A^2}{2T^2} \sin(4\pi f_c T)$

(b) $\frac{A^2}{2T} \cos(2\pi f_c T)$

(c) $\frac{A^2}{2T} - \frac{A^2}{2T} \sin(4\pi f_c T)$

(d) $\frac{A^2}{2T} - \frac{A^2}{8\pi f_c T^2} \sin(4\pi f_c T)$