

Parallel Execution in CUDA (Part 2)

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Overview

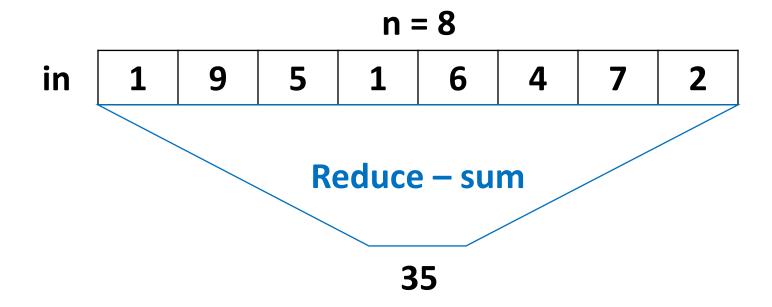
Apply knowledge of parallel execution in CUDA to write a fast CUDA program doing "reduction"

- The "reduction" task
- Sequential implementation
- Parallel implementation
 - Kernel function 1st version
 - Kernel function 2nd version: reduce warp divergence
 - Kernel function 3rd version: reduce warp divergence + ...

The "reduction" task

Input: an array in of n numbers

Output: sum (or product, max, min, ...) of these numbers



Reduction algorithm

Sum reduction sequential:

```
sum = 0;
for (int i = 0;i < N;i++){
    sum += input[i];
}</pre>
```

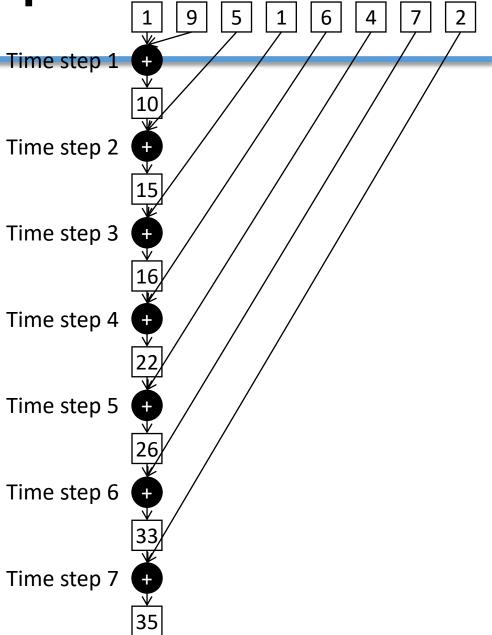
General form of a reduction sequential:

```
acc = IDENTITY;
for (int i = 0;i < N;i++){
   acc = Operator(acc, input[i]);
}</pre>
```

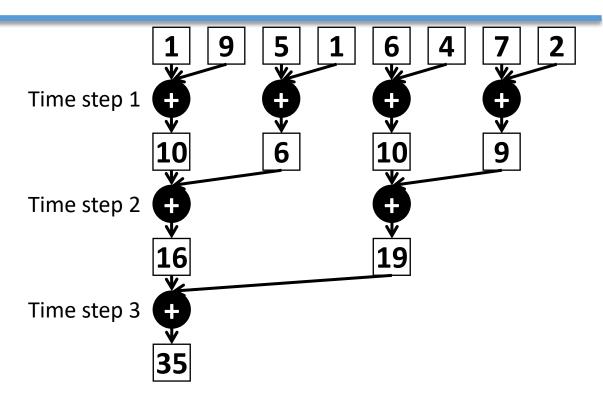
Sequential implementation

```
int reduceOnHost(int *in, int n)
{
   int s = in[0];
   for (int i = 1; i < n; i++)
      s += in[i];
   return s;
}</pre>
```

Time (# time steps): 7 = n-1 = O(n)Work (# pluses): 7 = n-1 = O(n)



Parallel implementation – idea



Time: ? Work: ?

6

Parallel implementation – idea

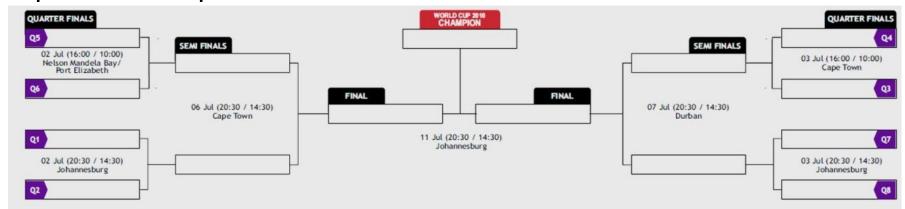
- For N input values, the reduction tree performs
- N/2 + N/4 + N/8 + ... + 1 = N 1 operations
 - In Log(N) steps 1,000,000 input values take 20 steps
- Assuming that we have enough execution resources
 Mức độ song song trung bình
 Average Parallelism (N-1)/Log(N))
 - - For N = 1,000,000, average parallelism is 50,000
 - However, peak resource requirement is 500,000
 - This is not resource efficient không tận dụng tối đa tài nguyên
 - This is a work-efficient parallel algorithm
 - The amount of work done is comparable to the an efficient sequential algorithm
 - Many parallel algorithms are not work efficient

Reduction trees

- Order of performing the operations will be changed (sequential → parallel)
 - Operator must be associative cần tính kết hợp
 - Serial
 - ((((((3 max 1) max 7) max 0) max 4) max 1) max 6) max 3
 - Paralell
 - ((3 max 1) max (7 max 0)) max ((4 max 1) max (6 max 3))
- We also need rearranges the order of the operands
 - Operator to be commutative cần tính giao hoán

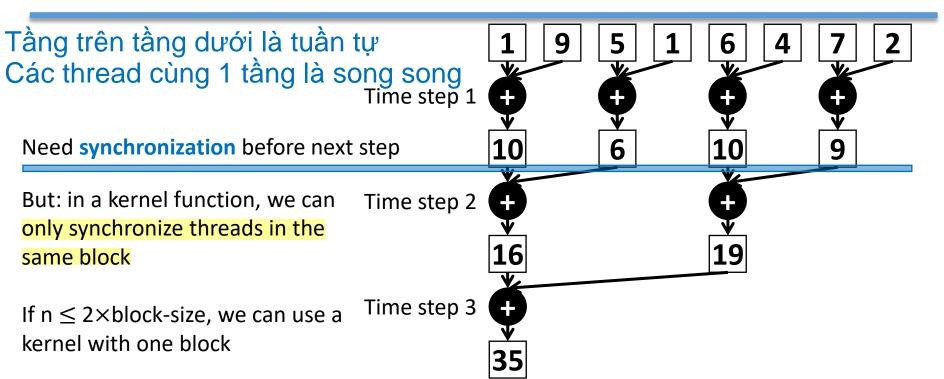
Parallel Reduction in Real life

Sports & Competitions: Max reduction



- Also use to process large input data sets (Google and Hadoop MapReduce frameworks)
 - There is no required order of processing elements in a data set (associative and commutative)
 - Partition the data set into smaller chunks
 - Have each thread to process a chunk
 - Use a reduction tree to summarize the results from each chunk into the final answer

Parallel implementation – idea

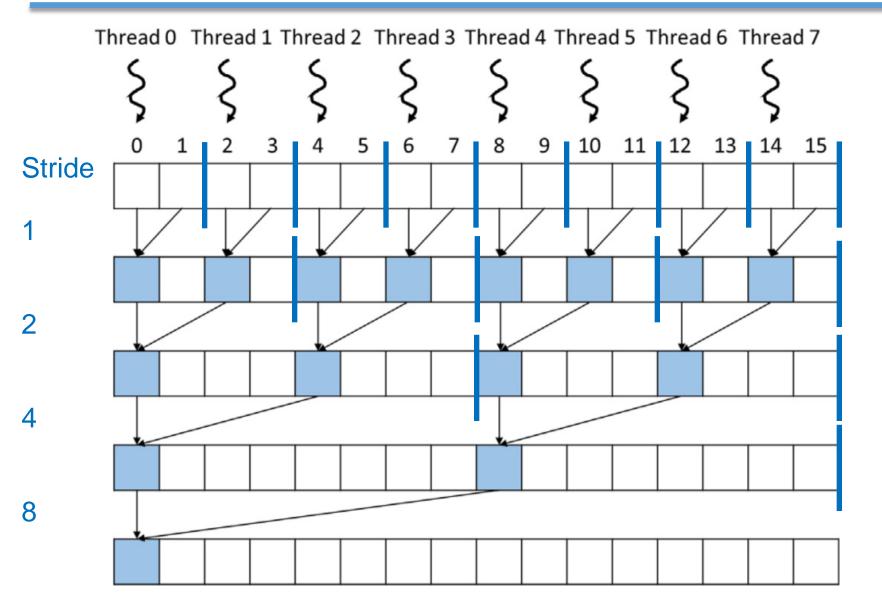


If $n > 2 \times block$ -size, what should we do?

Time: $3 = \log_2 n = O(\log_2 n)$

Work: 7 = n-1 = O(n) = work of the sequential version (Later, we will see tasks in which parallel implementations need to do more work than sequential)

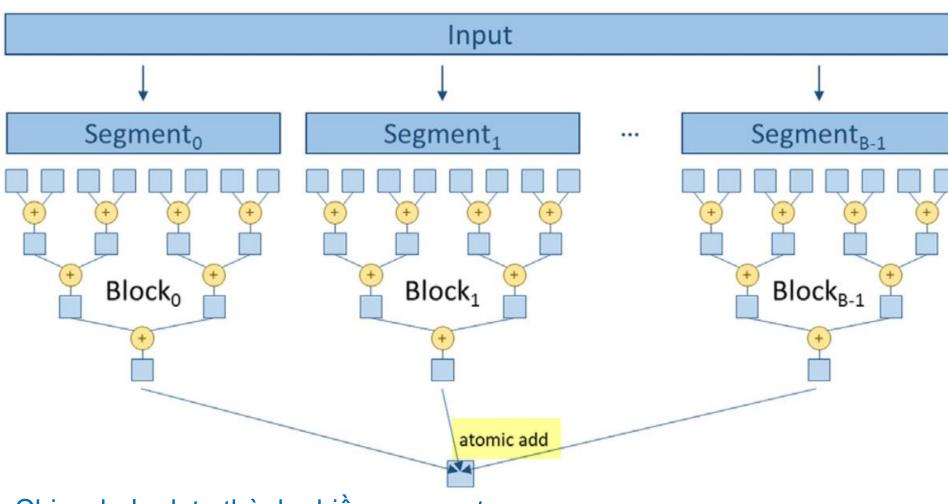
A simple reduction kernel



A simple reduction kernel

```
int i = 2 * threadIdx.x;
  for (int stride = 1; stride <= blockDim.x; stride *= 2) {</pre>
      if (threadIdx.x % stride == 0)
         in[i] += in[i + stride];
      __syncthreads();
  if (threadIdx.x == 0)
      *out = in[0];
```

Hierarchical reduction for bigger input

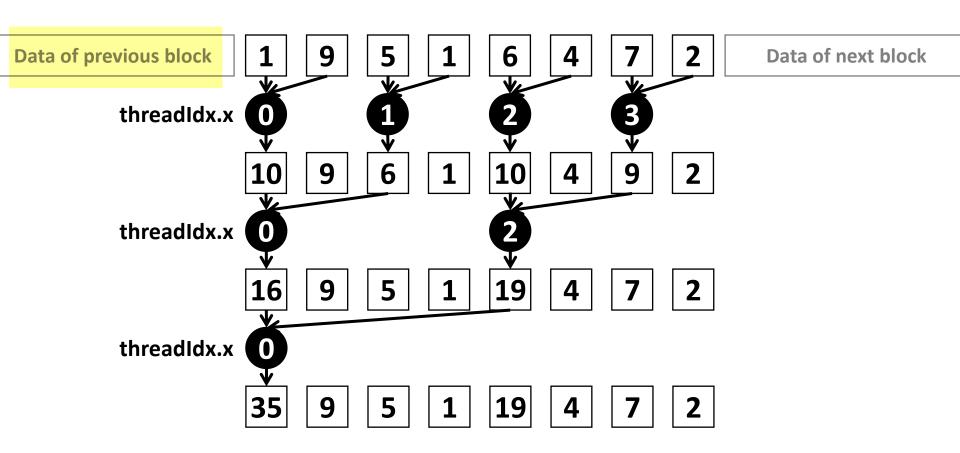


Chia whole data thành nhiều segments:

- Mỗi segment áp dụng reduction song song

Parallel implementation – idea to reduce within each block

Consider a block of 4 threads



blockldx * blockDim * 2 + threadIdx * 2

Hierarchical reduction for arbitrary input length

```
__global__    void reduceBlksKernel1(int* in, int* out, int n){
    int i = blockIdx.x * 2 * blockDim.x + 2 * threadIdx.x;
   for (int stride = 1; stride <= blockDim.x; stride *= 2){</pre>
        if (threadIdx.x % stride == 0)
            if (i + stride < n)</pre>
                in[i] += in[i + stride];
        __syncthreads(); // Synchronize within each block
    if (threadIdx.x == 0)
        atomicAdd(out, in[blockIdx.x * 2 * blockDim.x]);
```

Assume: $2 \times block$ -size = 2^k

In each block, how many diverged warps? (not consider blocks in the edge)

- Stride = 1:
 - All threads are "on"
 - → No diverged warp
- Stride = 2:
 - Only threads with threadIdx.x % 2 == 0 are "on"
 - → All warps are diverged
- Stride = 4, 8, ..., 32:

All warps are diverged

• Stride = 64, 128, ...: Khi stride tăng, thì số warp phân kỳ giảm dần đến khi chỉ còn 1

diverged warps decrease to 1

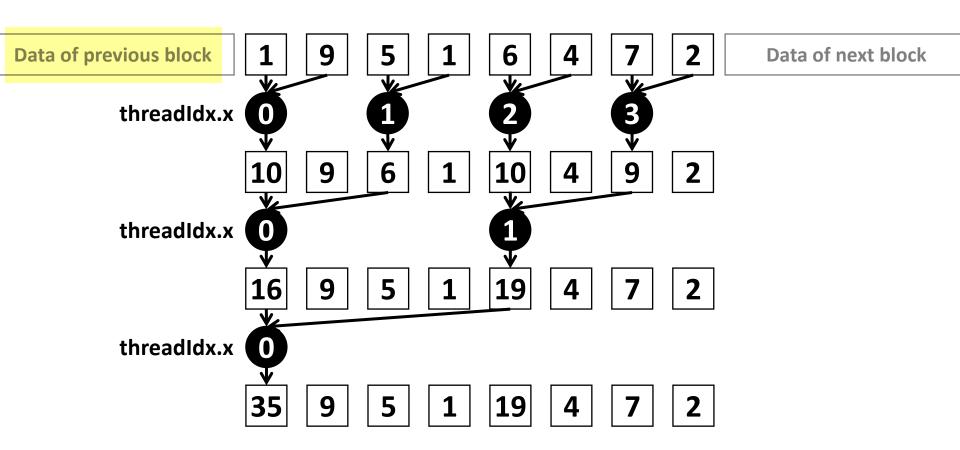
Kernel function – 2nd version: reduce warp divergence

- Idea: reduce # diverged warps in each step by rearranging threads so that "on" threads are first adjacent threads
- Example: consider a block of 128 threads
 - Stride = 1: All 128 threads are "on"
 - Stride = 2: First 64 threads are "on", the rest are "off"
 - Stride = 4: First 32 threads are "on", the rest are "off"

• ...

Kernel function - 2nd version: reduce warp divergence

Consider a block of 4 threads



Kernel function – 2nd version: reduce warp divergence

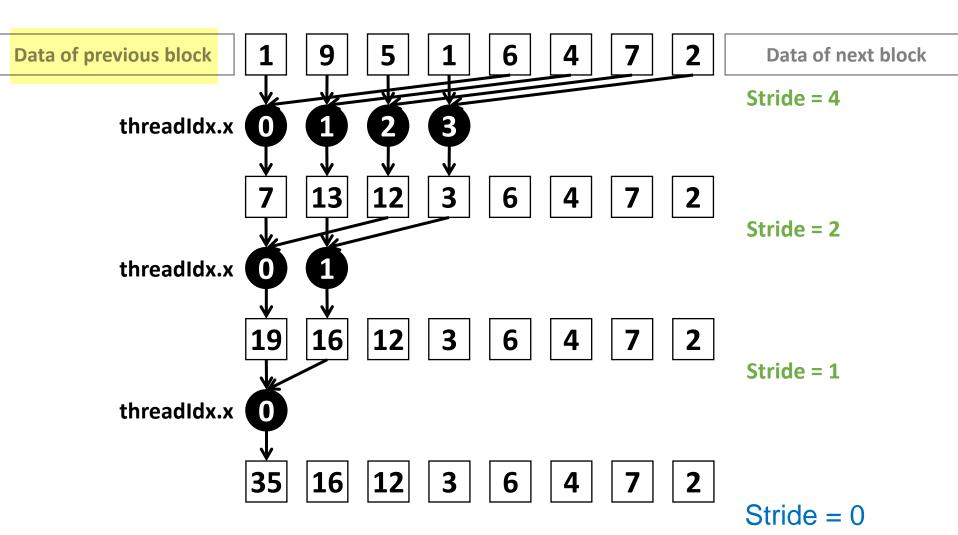
```
_global__ void reduceOnDevice2(int *in, int *out, int n)
   int numElemsBeforeBlk = blockIdx.x * blockDim.x * 2;
   for (int stride = 1; stride < 2 * blockDim.x; stride *= 2)</pre>
       int i = numElemsBeforeBlk + ...;
       if (threadIdx.x ...)
           if (i + stride < n)</pre>
               in[i] += in[i + stride];
       __syncthreads(); // Synchronize within each block
   if (threadIdx.x == 0)
       out[blockIdx.x] = in[numElemsBeforeBlk];
```

Kernel function – 2nd version: reduce warp divergence

```
_global__ void reduceOnDevice2(int *in, int *out, int n)
   int numElemsBeforeBlk = blockIdx.x * blockDim.x * 2;
  for (int stride = 1; stride < 2 * blockDim.x; stride *= 2)</pre>
       int i = numElemsBeforeBlk + threadIdx.x * 2 * stride;
       if (threadIdx.x < blockDim.x / stride)</pre>
           if (i + stride < n)</pre>
               in[i] += in[i + stride];
       __syncthreads(); // Synchronize within each block
   if (threadIdx.x == 0)
       out[blockIdx.x] = in[numElemsBeforeBlk];
      => Phải dùng atomicAdd
```

Kernel function - 3rd version: reduce warp divergence +?

Consider a block of 4 threads



Kernel function - 3rd version: reduce warp divergence +?

Code: your next homework ;-)

Reference

- [1] Wen-Mei, W. Hwu, David B. Kirk, and Izzat El Hajj. Programming Massively Parallel Processors: A Hands-on Approach. Morgan Kaufmann, 2022
- [2] Cheng John, Max Grossman, and Ty McKercher. *Professional Cuda C Programming*. John Wiley & Sons, 2014



THE END