TEMA 12. TEODÍA CLASICA DE CAMPOS

Conidereurs in compo p(x). Trabajemes con la donidad Ragrangiana, \mathcal{L} . $L = T - V = \int \mathcal{L} d^3x$

la acción es $S = \int dt L = \int \mathcal{L} d^{h}x$

los lagrangianos típicos en OFT dependen de:

Z = Z (q, Opp q)

Consideraremos compos locales (L' depende de p y Pary x x concreto)

Principio de acción entacionaria

0 = SS = 8 Jd4x 2

Segundo término:

$$\int d^{4}x \frac{\partial \mathcal{L}}{\partial x} S(\partial_{\mu}\varphi) = \int d^{4}x \frac{\partial \mathcal{L}}{\partial x} \partial_{\mu} (8\varphi)$$

$$\mathcal{M} \partial \partial_{\mu}\varphi \partial_{\mu} (8\varphi)$$

es ma divergencia total

$$=\int_{\partial M} d\sigma_{\mu} \frac{2\chi}{\partial l \partial \mu \ell} \delta \varphi = \int_{\partial M} d^{3}\sigma_{\mu} \frac{2\chi}{\partial l \partial \mu \ell} \delta \varphi$$

Sq 10 = 0

 $\Rightarrow \frac{\partial \mathcal{L}}{\partial \varphi} - \partial \mu \left(\frac{\partial \mathcal{L}}{\partial (\partial \mu \varphi)} \right) = 0$ Eurationes de Euler-Logrange. La devidad de momento canónica es TC(X) = 22 y devidend florieltonique es H = 72 (x) q(x) - 2 El llavillonicus sera H = | d3 x 1e Veaures algunes genegles de teoriers clarices de ecupes

Compo escalon real (Higgs)

$$\frac{\partial \mathcal{L}}{\partial (\partial_{\alpha} \varphi)} = \frac{\partial}{\partial (\partial_{\alpha} \varphi)} \frac{1}{2} \left(\partial_{\alpha} \varphi \partial^{\alpha} \varphi - m^{2} \varphi^{2} \right)$$

$$\partial_{\mathbf{A}}\left(\frac{\partial \mathcal{L}}{\partial(\partial_{\mathbf{A}} \ell)}\right) = \partial_{\mathbf{A}}\partial^{\mathbf{A}} \ell = \Box \ell$$

$$\frac{\partial \chi}{\partial \varphi} = - m^2 \varphi$$

Otro ejemplos (entregable)

i)
$$Z = \frac{1}{2} \left[(\partial_{\xi} \varphi)^{2} - (\partial_{x} \varphi)^{2} \right] + \cos \varphi$$

$$= 7 \frac{\partial^2 \varphi}{\partial \xi^2} - \frac{\partial^2 \varphi}{\partial x^2} + \sin \varphi = 0 \implies (D + \sin \varphi) = 0$$

$$Sin - Gordon$$

iii)
$$Z = -\frac{t_1}{2i} \left(\frac{1}{4} \frac{1}{2} \frac{1}{4} - \frac{1}{4} \frac{1}{2} \frac{1}{4} \right)$$

$$-\frac{t_1^2}{2in} \frac{1}{2} \frac{1}{4} \frac{1}{4} \frac{1}{4} - \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4}$$

- · Obteuer la emación de Schrödinger
- · Haver el ecuntrio Y= Ne is/t

obtener

$$\mathcal{L} = -N^2 \dot{S} - \frac{L^2}{2m} \partial_1 N \partial^1 N - \frac{N^2}{2m} \partial_1 S \partial^2 S - VN^2$$

Lors emaines de Euler-Lagrange correspondientes son

$$\partial_t f + \frac{L}{m} \nabla_i (\ell P^i S) = 0 \qquad (\ell := N^2)$$

$$\partial_{L}S + L \partial_{i}S \partial^{i}S + V - \frac{t^{2}}{2m} \frac{\Delta N}{N} \qquad (\Delta := 2; \partial^{i})$$

Interpretor dichas emaciones. Observad que son i completemente equivalentes a la emación de Schröd!!