# Regression in the real world

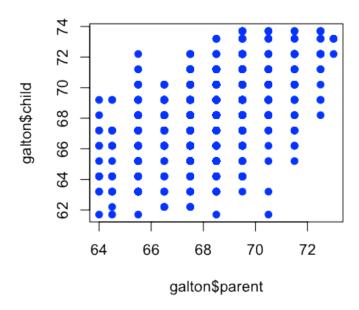
Jeffrey Leek, Assistant Professor of Biostatistics Johns Hopkins Bloomberg School of Public Health

## Things to pay attention to

- Confounders
- Complicated interactions
- Skewness
- Outliers
- Non-linear patterns
- Variance changes
- Units/scale issues
- Overloading regression
- · Correlation and causation

## The ideal data for regression

```
library(UsingR); data(galton)
plot(galton$parent,galton$child,col="blue",pch=19)
```



#### Confounders

**Confounder**: A variable that is correlated with both the outcome and the covariates

- · Confounders can change the regression line
- · They can even change the sign of the line
- They can sometimes be detected by careful exploration

#### Example - Millenium Development Goal 1



#### GOAL 1 **Eradicate Extreme Poverty and Hunger**

**FACT SHEET** 

#### **TARGETS**

- 1. Halve, between 1990 and 2015, the proportion of people whose income is less than \$1 a day
- 2. Achieve full and productive employment and decent work for all, including women and young people
- 3. Halve, between 1990 and 2015, the proportion of people who suffer from hunger

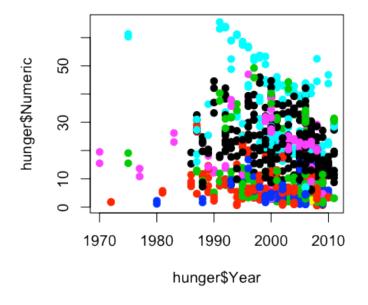
http://www.un.org/millenniumgoals/pdf/MDG\_FS\_1\_EN.pdf

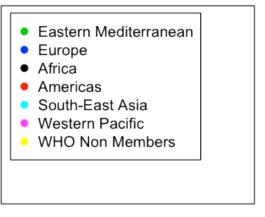
#### WHO childhood hunger data

```
Indicator Data. Source
                                                            Country
                                                                                            WHO.region
                                                                       Sex Year
   Children aged <5 years underweight (%) NLIS 312819 Afghanistan
                                                                      Male 2004 Eastern Mediterranean
   Children aged <5 years underweight (%) NLIS 312819 Afghanistan Female 2004 Eastern Mediterranean
   Children aged <5 years underweight (%) NLIS 312361
                                                            Albania
                                                                      Male 2000
                                                                                                Europe
   Children aged <5 years underweight (%) NLIS 312361
                                                            Albania Female 2000
                                                                                                Europe
   Children aged <5 years underweight (%) NLIS 312879
                                                            Albania Female 2005
                                                                                                Europe
10 Children aged <5 years underweight (%) NLIS 312879
                                                            Albania
                                                                     Male 2005
                                                                                                Europe
   Display. Value Numeric Low High Comments
2
            32.7
                    32.7
                          NA
                                NA
                                         NA
            33.0
                    33.0
4
                          NA
                                NA
                                         NA
            19.6
                    19.6
                          NA
                                NA
                                         NA
            14.2
8
                    14.2
                          NA
                                         NA
                                NA
9
             5.8
                     5.8
                          NA
                                NA
                                         NA
                                                                                             6/30
10
             7.3
                     7.3
                          NA
                                NA
                                         NA
```

#### Hunger over time by region

```
par(mfrow=c(1,2))
plot(hunger$Year,hunger$Numeric,col=as.numeric(hunger$WHO.region),pch=19)
plot(1:10,type="n",xaxt="n",yaxt="n",xlab="",ylab="")
legend(1,10,col=unique(as.numeric(hunger$WHO.region)),legend=unique(hunger$WHO.region),pch=19)
```





### Region correlated with year

```
anova(lm(hunger$Year ~ hunger$WHO.region))
```

```
Analysis of Variance Table

Response: hunger$Year

Df Sum Sq Mean Sq F value Pr(>F)
hunger$WHO.region 6 623 103.8 2.25 0.037 *
Residuals 851 39315 46.2

---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

### Region correlated with hunger

```
anova(lm(hunger$Numeric ~ hunger$WHO.region))
```

```
Analysis of Variance Table

Response: hunger$Numeric

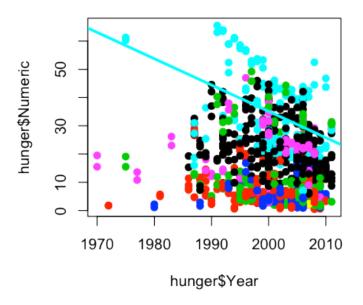
Df Sum Sq Mean Sq F value Pr(>F)
hunger$WHO.region 6 75042 12507 127 <2e-16 ***

Residuals 851 83853 99
---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

#### Including region - a complicated interaction

```
plot(hunger$Year,hunger$Numeric,pch=19,col=as.numeric(hunger$WHO.region))
lmRegion <- lm(hunger$Numeric ~ hunger$Year + hunger$WHO.region + hunger$Year*hunger$WHO.region )
abline(c(lmRegion$coeff[1] + lmRegion$coeff[6],lmRegion$coeff[2]+ lmRegion$coeff[12]),col=5,lwd=3)</pre>
```



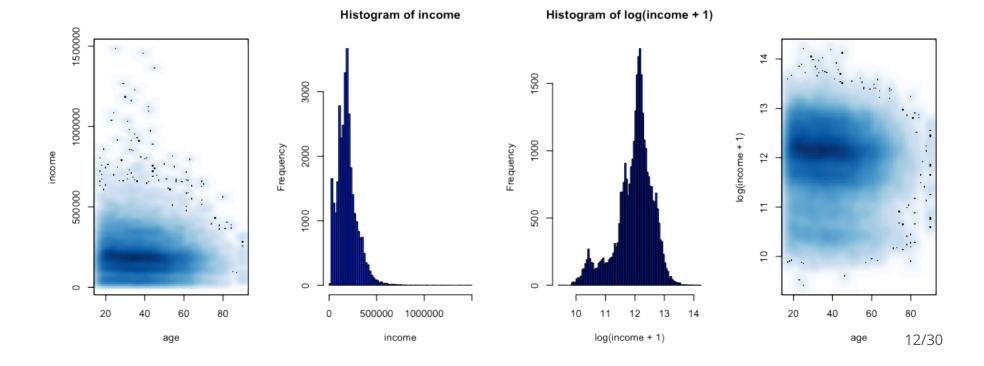
#### Income data

```
download.file("http://archive.ics.uci.edu/ml/machine-learning-databases/adult/adult.data","./data/i
incomeData <- read.csv("./data/income.csv",header=FALSE)
income <- incomeData[,3]
age <- incomeData[,1]</pre>
```

http://archive.ics.uci.edu/ml/datasets/Census+Income

## Logs to address right-skew

```
par(mfrow=c(1,4))
smoothScatter(age,income)
hist(income,col="blue",breaks=100)
hist(log(income+1),col="blue",breaks=100)
smoothScatter(age,log(income+1))
```



#### **Outliers**

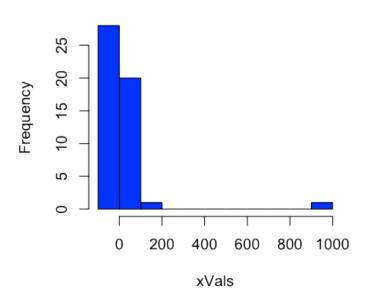
"outliers" ... are data points that do not appear to follow the pattern of the other data points.

A dataset that is 44% outliers

#### **Example - extreme points**

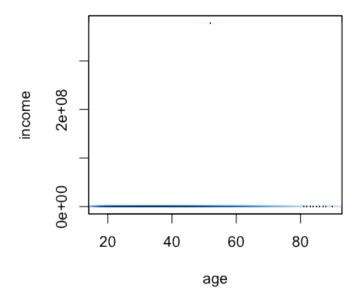
```
set.seed(1235)
xVals <- rcauchy(50)
hist(xVals,col="blue")</pre>
```

#### Histogram of xVals



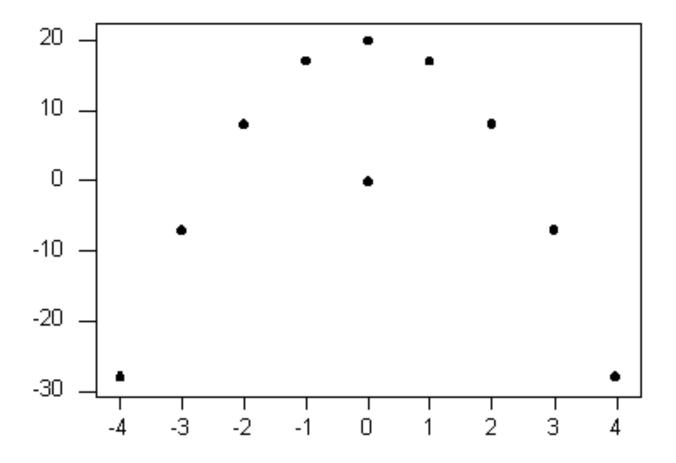
#### Example - Outliers may be real

```
# Add Tim Cook, CEO of Apple 2011 income
age <- c(age,52)
income <- c(income,378e6)
smoothScatter(age,income)</pre>
```



http://www.macworld.com/article/2023491/apple-gives-tim-cook-51-percent-salary-increase.html 15/30

## Example - Does not fit the trend

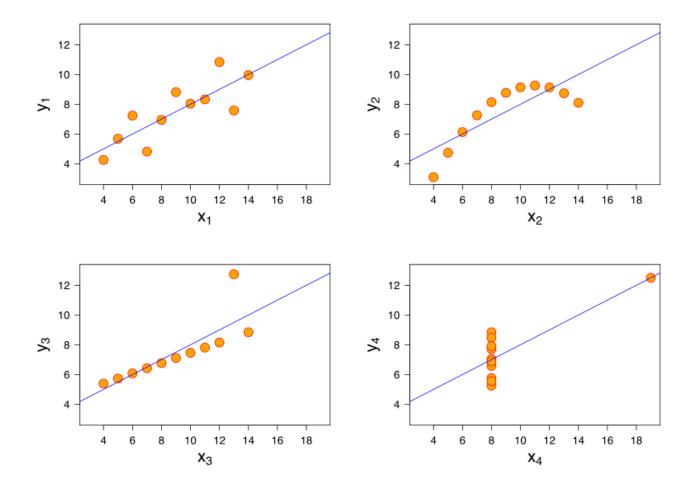


A dataset that is 44% outliers

### Outliers - what you can do

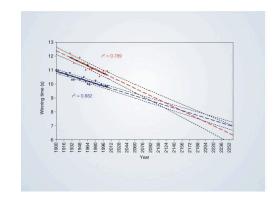
- If you know they aren't real/of interest, remove them (but changes question!)
- Alternatively
  - Sensitivity analysis is it a big difference if you leave it in/take it out?
  - Logs if the data are right skewed (lots of outliers)
  - Robust methods we've been doing averages, but there are more robust approaches (Robust,rlm)

## A line isn't always the best summary



http://en.wikipedia.org/wiki/Linear\_regression

## You can end up saying some pretty silly stuff



#### http://www.nature.com/nature/journal/v431/n7008/fig\_tab/431525a\_F1.html

"We are students aged 16–18 in a Texas high school. Our biology teacher Vidya Rajan asked us to comment on the paper by A. J. Tatem and colleagues (Nature 431, 525; 2004); we believe the projection on which it is based is riddled with flaws..." http://www.nature.com/nature/journal/v432/n7014/full/432147c.html

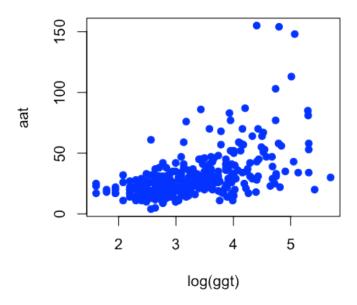
"They omit to mention, however, that (according to their analysis) a far more interesting race should occur in about 2636, when times of less than zero seconds will be recorded" http://www.nature.com/nature/journal/v432/n7014/full/432147b.html

## Variance changes

```
bupaData <- read.csv("ftp://ftp.ics.uci.edu/pub/machine-learning-databases/liver-disorders/bupa.dat

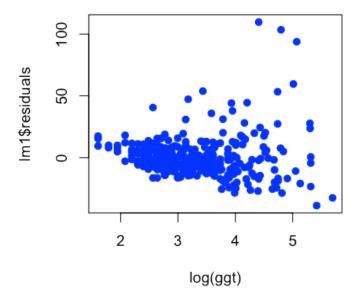
ggt <- bupaData[,5]; aat <- bupaData[,3]

plot(log(ggt),aat,col="blue",pch=19)</pre>
```



#### Plot the residuals

```
lm1 <- lm(aat ~ log(ggt))
plot(log(ggt),lm1$residuals,col="blue",pch=19)</pre>
```

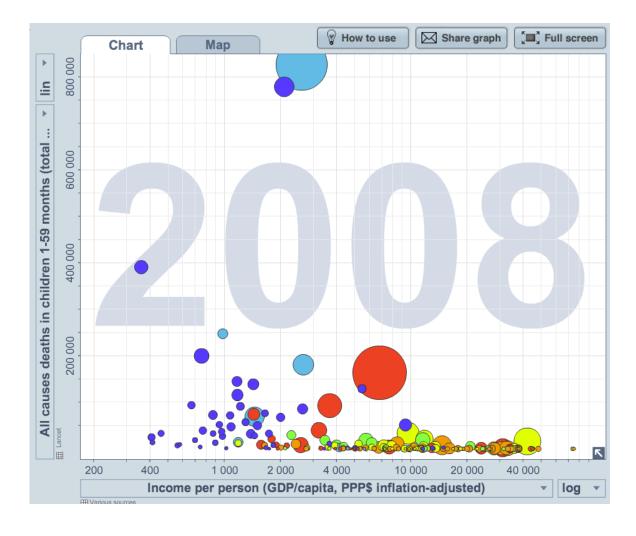


Power (a.k.a. Box-Cox) transform

## Changing variance - what you can do

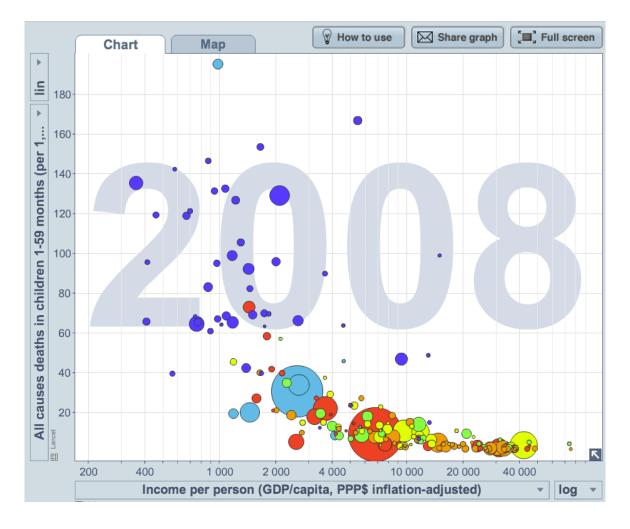
- There is a long literature on this problem (heteroskedasticity)
- · A few examples
  - Box-Cox Transform
  - Variance stabilizing transform
  - Weighted least squares
  - Huber-white standard errors

#### Variation in units



All Deaths

#### Relative units



Per 1000 Deaths

#### When there is variation in units

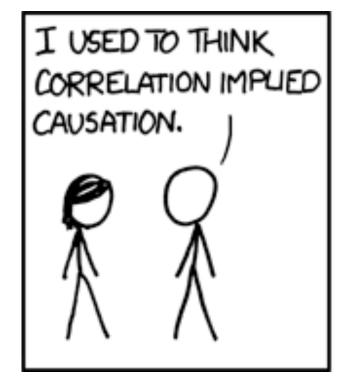
- Standardize, but keep track
  - Affects model fits
  - Affects interpretation
  - Affects inference

### Overloading regression

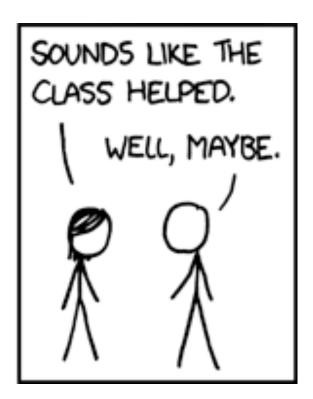
$$AMR_{it} = \alpha + \beta_1 PRIV_{it} + \beta_2 GDP_{it} + \beta_3 LIB_{it} + \beta_4 TRADE_{it} + \beta_5 DEM_{it} + \beta_6 WAR_{it} + \beta_7 DEP_{it} + \beta_8 URBAN_{it} + \beta_9 EDUC_{it} + \mu_i + \varepsilon_{it}$$

http://bit.ly/YiB5Um http://wmbriggs.com/blog/?p=7026

#### **Correlation and Causation**

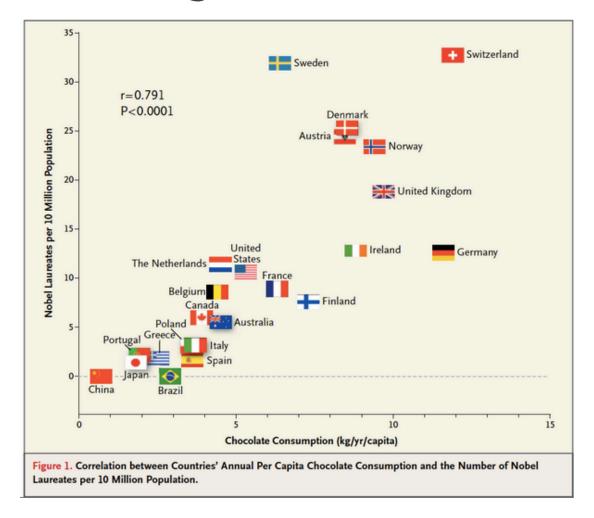






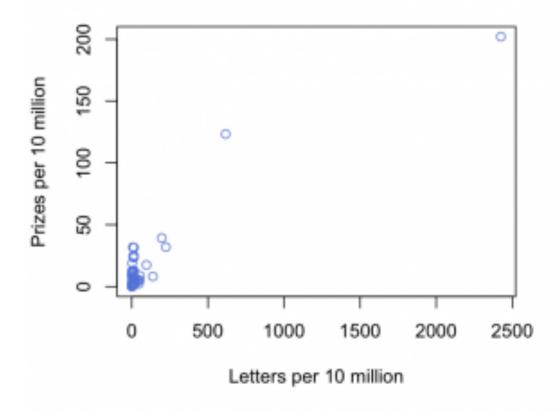
http://xkcd.com/552/

## Even when looking for associations



http://www.nejm.org/doi/full/10.1056/NEJMon1211064

## Again, it can get silly



http://www.statschat.org.nz/2012/10/12/even-better-than-chocolate/

#### Correlation vs. Causation

- Use caution when interpreting regression results
- Be critical of surprising associations
- Consider alternative explanations