Hierarchical clustering

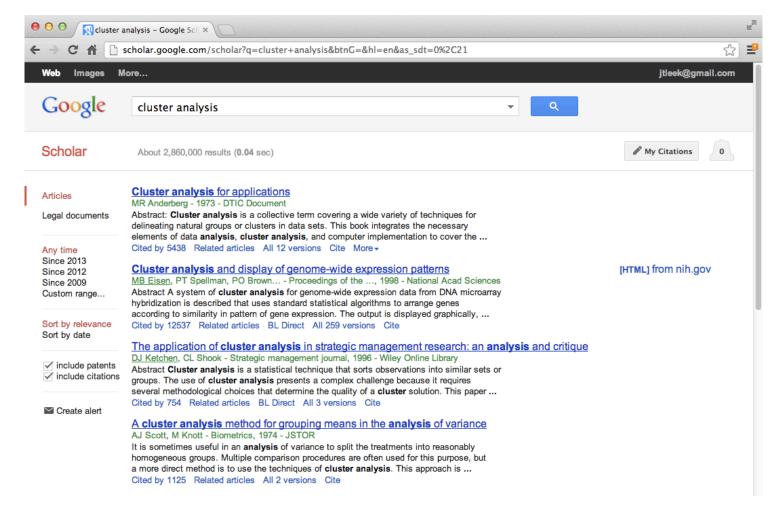
Jeffrey Leek, Assistant Professor of Biostatistics Johns Hopkins Bloomberg School of Public Health

Can we find things that are close together?

Clustering organizes things that are close into groups

- How do we define close?
- How do we group things?
- How do we visualize the grouping?
- How do we interpret the grouping?

Hugely important/impactful



http://scholar.google.com/scholar?hl=en&q=cluster+analysis&btnG=&as_sdt=1%2C21&as_sdtp=

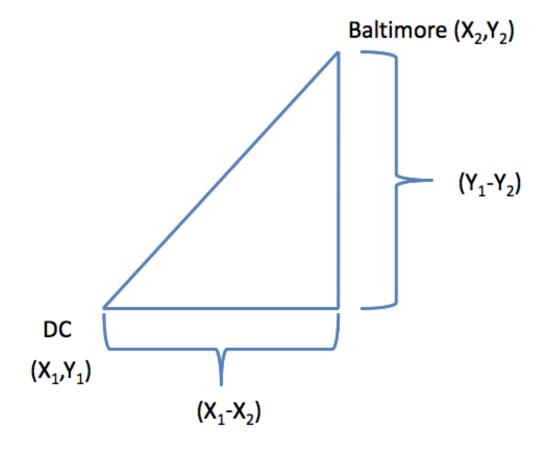
Hierarchical clustering

- An agglomerative approach
 - Find closest two things
 - Put them together
 - Find next closest
- Requires
 - A defined distance
 - A merging approach
- Produces
 - A tree showing how close things are to each other

How do we define close?

- Most important step
 - Garbage in -> garbage out
- Distance or similarity
 - Continuous euclidean distance
 - Continous correlation similarity
 - Binary manhattan distance
- Pick a distance/similarity that makes sense for your problem

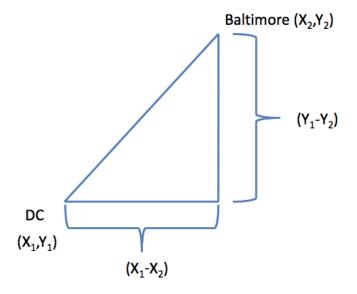
Example distances - Euclidean



http://rafalab.jhsph.edu/688/lec/lecture5-clustering.pdf

Example distances - Euclidean

$$\sqrt{(X_1-X_2)^2+(Y_1-Y_2)^2}$$

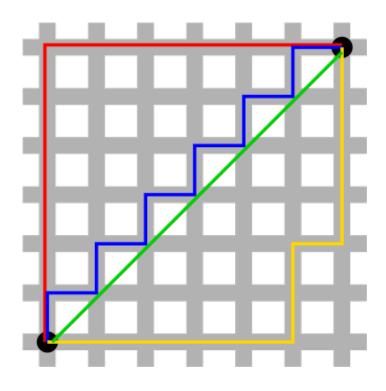


In general:

$$\sqrt{(A_1 - A_2)^2 + (B_1 - B_2)^2 + \dots + (Z_1 - Z_2)^2}$$

http://rafalab.jhsph.edu/688/lec/lecture5-clustering.pdf

Example distances - Manhattan



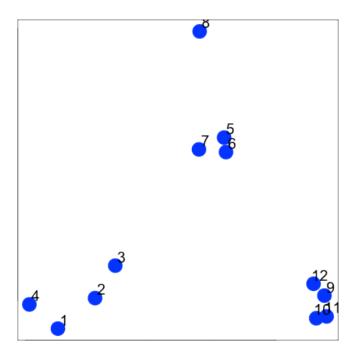
In general:

$$|A_1 - A_2| + |B_1 - B_2| + \dots + |Z_1 - Z_2|$$

http://en.wikipedia.org/wiki/Taxicab_geometry

Hierarchical clustering - example

```
set.seed(1234); par(mar=c(0,0,0,0))
x <- rnorm(12,mean=rep(1:3,each=4),sd=0.2)
y <- rnorm(12,mean=rep(c(1,2,1),each=4),sd=0.2)
plot(x,y,col="blue",pch=19,cex=2)
text(x+0.05,y+0.05,labels=as.character(1:12))</pre>
```



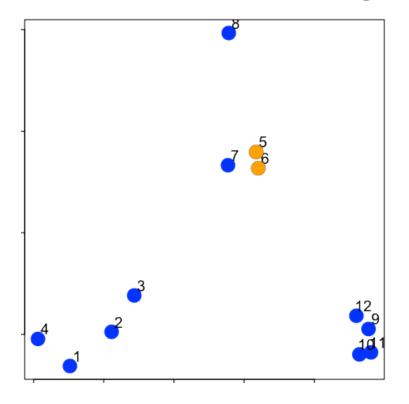
Hierarchical clustering - dist

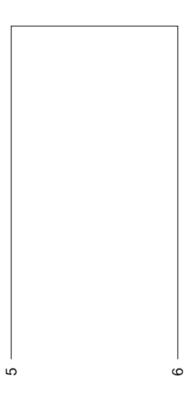
Important parameters: x,method

```
dataFrame <- data.frame(x=x,y=y)
dist(dataFrame)</pre>
```

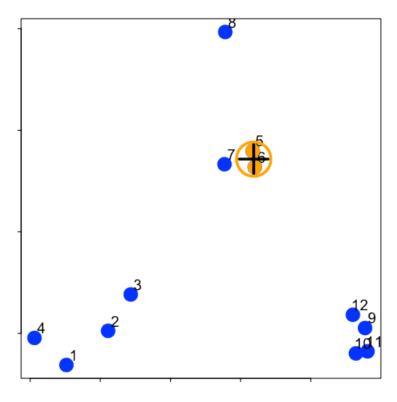
```
1 2 3 4 5 6 7 8 9 10 11
2 0.34121
3 0.57494 0.24103
4 0.26382 0.52579 0.71862
5 1.69425 1.35818 1.11953 1.80667
6 1.65813 1.31960 1.08339 1.78081 0.08150
7 1.49823 1.16621 0.92569 1.60132 0.21110 0.21667
8 1.99149 1.69093 1.45649 2.02849 0.61704 0.69792 0.65063
9 2.13630 1.83168 1.67836 2.35676 1.18350 1.11500 1.28583 1.76461
10 2.06420 1.76999 1.63110 2.29239 1.23848 1.16550 1.32063 1.83518 0.14090
11 2.14702 1.85183 1.71074 2.37462 1.28154 1.21077 1.37370 1.86999 0.11624 0.08318
12 2.05664 1.74663 1.58659 2.27232 1.07701 1.00777 1.17740 1.66224 0.10849 0.19129 0.20803
```

Hierarchical clustering - #1

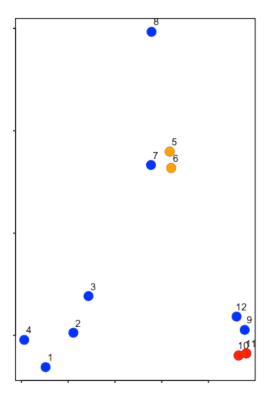


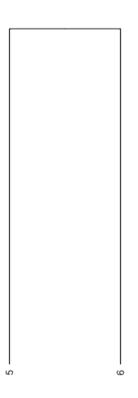


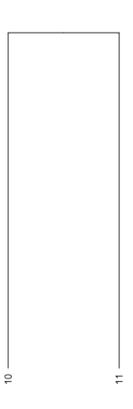
Hierarchical clustering - #2



Hierarchical clustering - #3



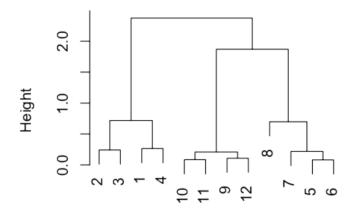




Hierarchical clustering - hclust

```
dataFrame <- data.frame(x=x,y=y)
distxy <- dist(dataFrame)
hClustering <- hclust(distxy)
plot(hClustering)</pre>
```

Cluster Dendrogram



distxy hclust (*, "complete")

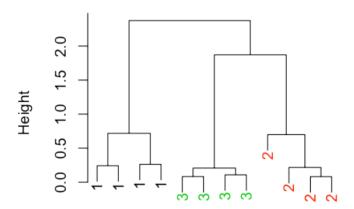
Prettier dendrograms

```
myplclust <- function( hclust, lab=hclust$labels, lab.col=rep(1,length(hclust$labels)), hang=0.1,...
 ## modifiction of plclust for plotting hclust objects *in colour*!
 ## Copyright Eva KF Chan 2009
 ## Arguments:
                  hclust object
  ##
        hclust:
  ##
        lab:
                    a character vector of labels of the leaves of the tree
        lab.col:
                    colour for the labels; NA=default device foreground colour
                  as in hclust & plclust
  ##
        hang:
 ## Side effect:
        A display of hierarchical cluster with coloured leaf labels.
 y <- rep(hclust$height,2); x <- as.numeric(hclust$merge)
 y \leftarrow y[which(x<0)]; x \leftarrow x[which(x<0)]; x \leftarrow abs(x)
 y \leftarrow y[order(x)]; x \leftarrow x[order(x)]
 plot( hclust, labels=FALSE, hang=hang, ... )
 text( x=x, y=y[hclust$order]-(max(hclust$height)*hang),
        labels=lab[hclust$order], col=lab.col[hclust$order],
        srt=90, adj=c(1,0.5), xpd=NA, ...
}
```

Hierarchical clustering - hclust

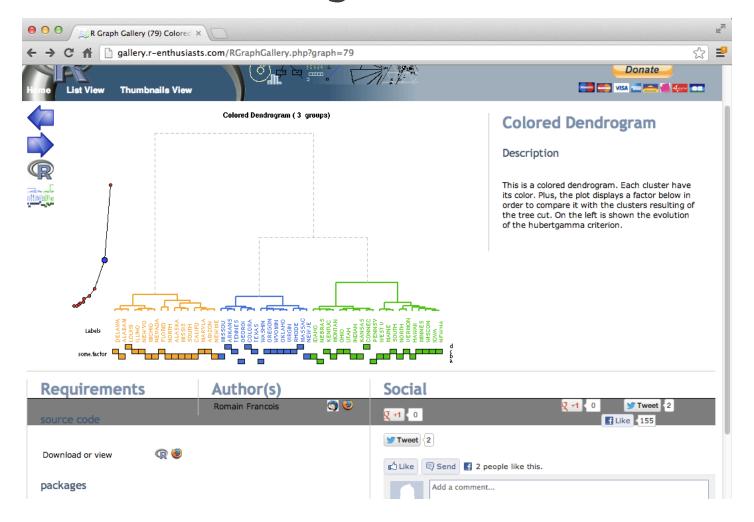
```
dataFrame <- data.frame(x=x,y=y)
distxy <- dist(dataFrame)
hClustering <- hclust(distxy)
myplclust(hClustering,lab=rep(1:3,each=4),lab.col=rep(1:3,each=4))</pre>
```

Cluster Dendrogram



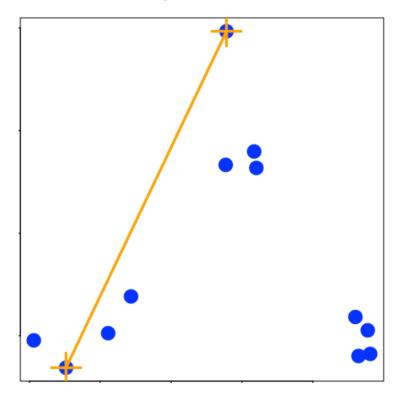
distxy hclust (*, "complete")

Even Prettier dendrograms

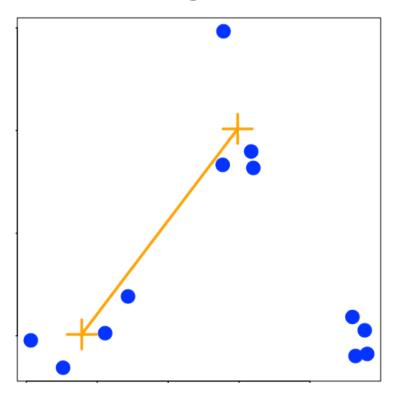


http://gallery.r-enthusiasts.com/RGraphGallery.php?graph=79

Merging points - complete

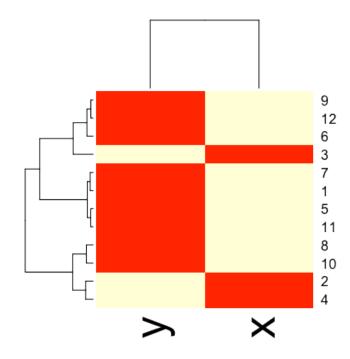


Merging points - average



heatmap()

```
dataFrame <- data.frame(x=x,y=y)
set.seed(143)
dataMatrix <- as.matrix(dataFrame)[sample(1:12),]
heatmap(dataMatrix)</pre>
```



Notes and further resources

- Gives an idea of the relationships between variables/observations
- The picture may be unstable
 - Change a few points
 - Have different missing values
 - Pick a different distance
 - Change the merging strategy
 - Change the scale of points for one variable
- But it is deterministic
- · Choosing where to cut isn't always obvious
- Should be primarily used for exploration
- Rafa's Distances and Clustering Video
- · Elements of statistical learning