

K-Means Clustering

Unsupervised Learning

- trying to find hidden structure in unlabeled data
- no error or reward signal to evaluate a potential solution
- Common techniques: K-Means clustering, Hierarchical clustering, hidden Markov models, etc.
- It has a long history, and used in almost every field, e.g., medicine, psychology, botany, sociology, biology, archeology, marketing, insurance, libraries, etc.

Unsupervised learning

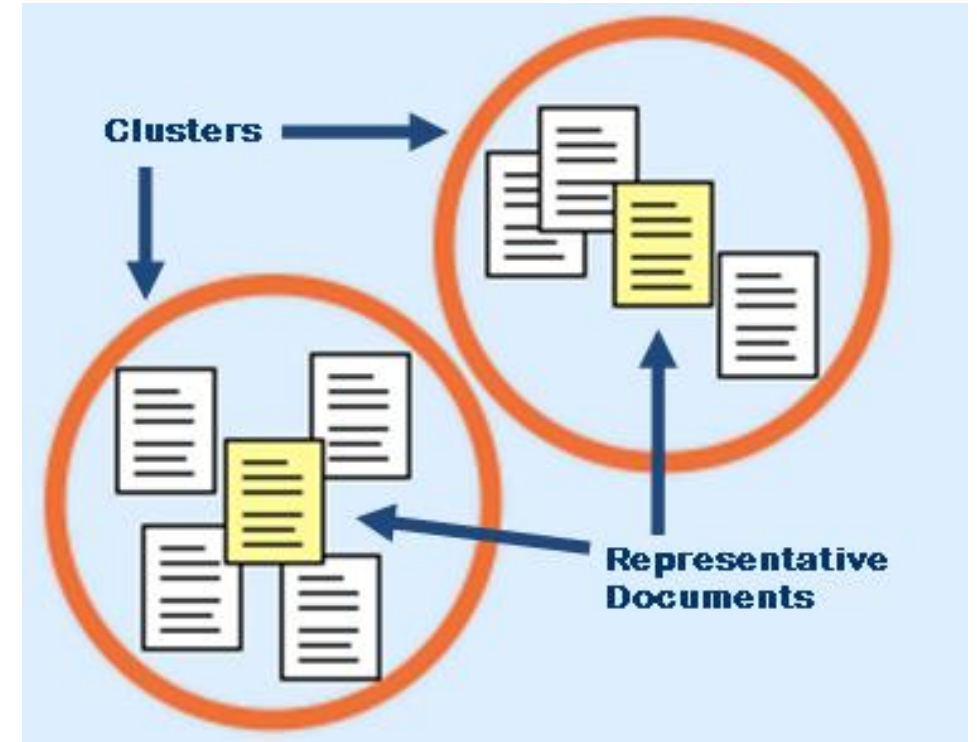
Example 1: Clothing size

- Tailor-make for each person is too expensive
- One-size-fit-all: do not work!!
- groups people of similar sizes together to make "small", "medium" and "large" T-Shirts.

Unsupervised learning

Example 2: Text document organization

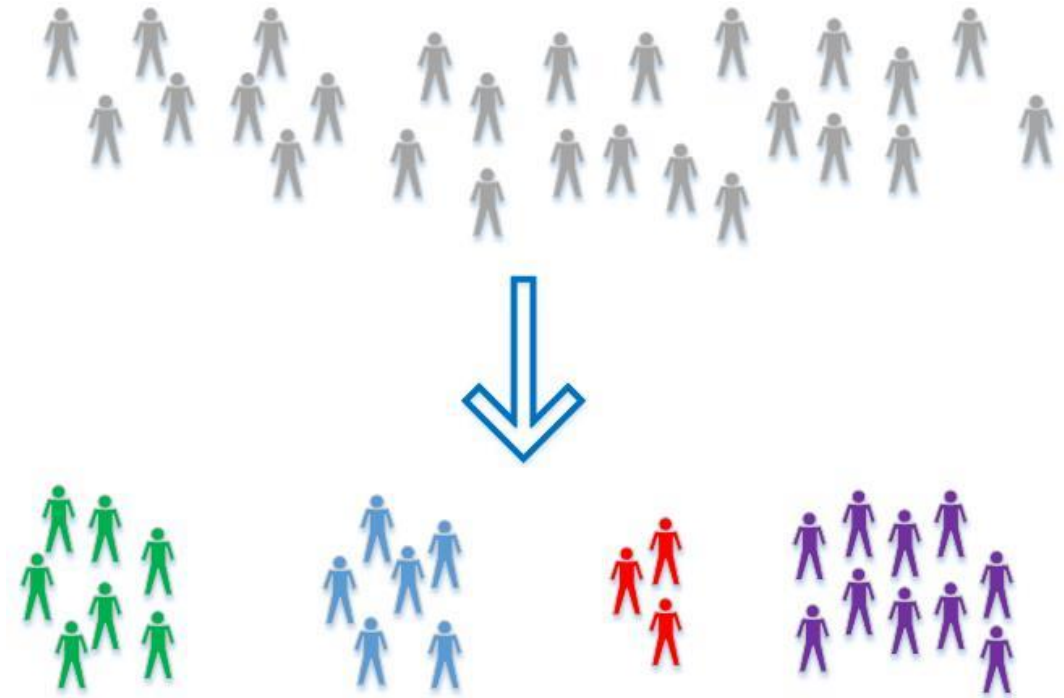
- To find groups of documents that are similar to each other based on the important terms appearing in them.



Unsupervised learning

Example 3: Target Marketing

Subdivide market into distinct subsets of customers where any subset may conceivably be selected as a segment to be reached with a particular offer.



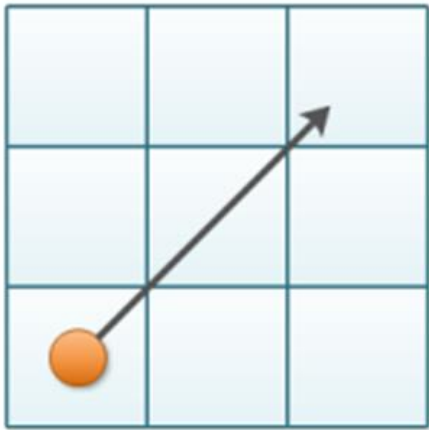
K-means clustering

- Process of partitioning data points into similarity clusters
- Unsupervised technique
- Only works for numeric data



Euclidean Distance

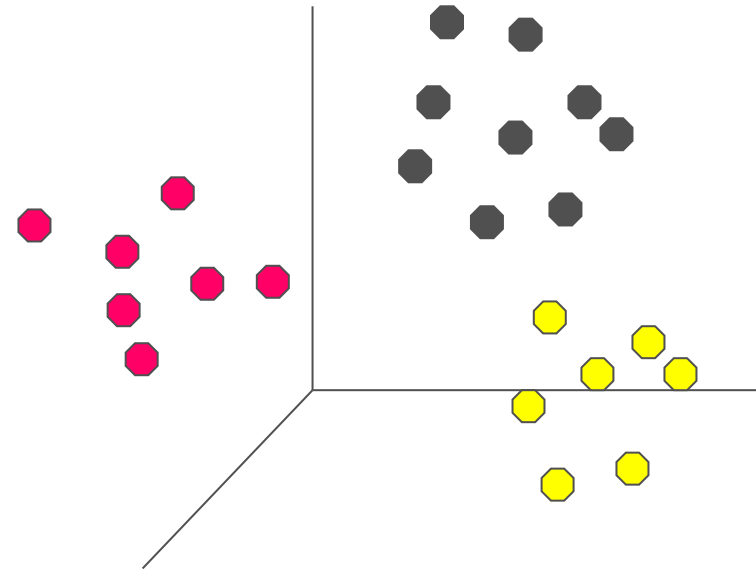
- points in a two-dimensional space to determine intra- and inter-cluster similarity.



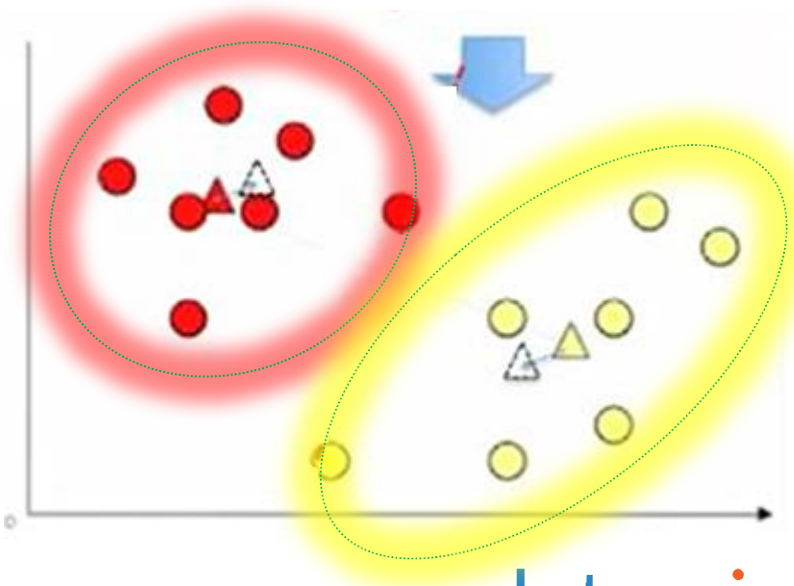
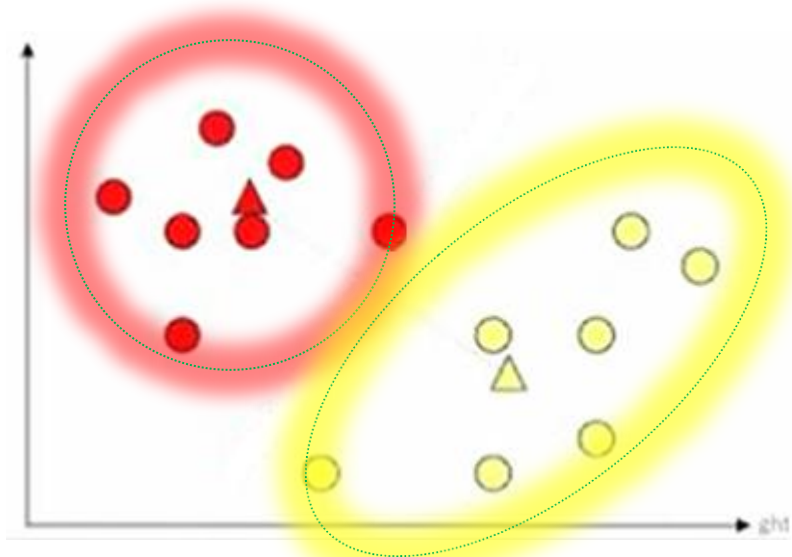
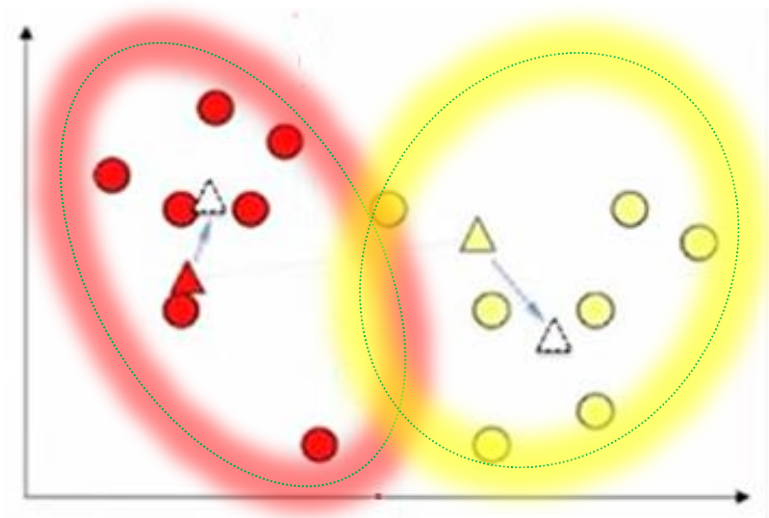
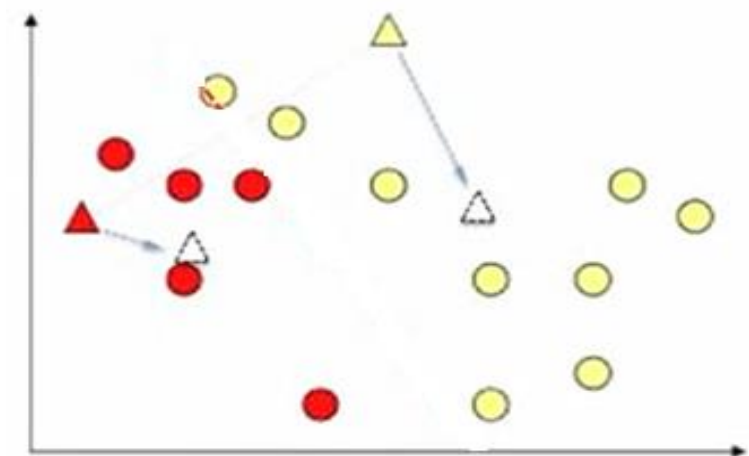
$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Intra-cluster distances
are minimized

Inter-cluster distances
are maximized



K-means clustering



K-means clustering algorithm

Suppose set of data points: $\{x_1, x_2, x_3, \dots, x_n\}$

- **Step 1:** Decide the number of clusters, $K=1,2,\dots,k$.
- **Step 2:** Place centroids at random locations
 - c_1, c_2, \dots, c_k
- **Step 3:** Repeat until convergence:
 - { for each point $x_i \longrightarrow$ find nearest centroid c_j (eg. Euclidean distance)
 \longrightarrow assign the point x_i to cluster j
 - for each cluster $j = 1 \dots k \longrightarrow$ calculate new centroid c_j
 $c_j = \text{mean of all points } x_i \text{ assigned to cluster } j \text{ in previous step}$
 - }
- **Step 4:** Stop when none of the cluster assignments change

K-means clustering

Minimizes aggregate intra-cluster distance

- Measure squared distance from point to center of its cluster.
$$\sum_j \sum_{x_j - c_i} D(c_j x_i)^2$$

Could converge to local minimum

- Different starting points \longrightarrow very different results
- Run many times with random starting points

Nearby points may not be assigned to the same cluster



K-means clustering

Strengths:

Simple: easy to understand and to implement

Efficient: Complexity: $O(t \times k \times n)$

n = number of data points,
 k = number of clusters, and
 t = number of iterations.

K-means clustering

Weaknesses:

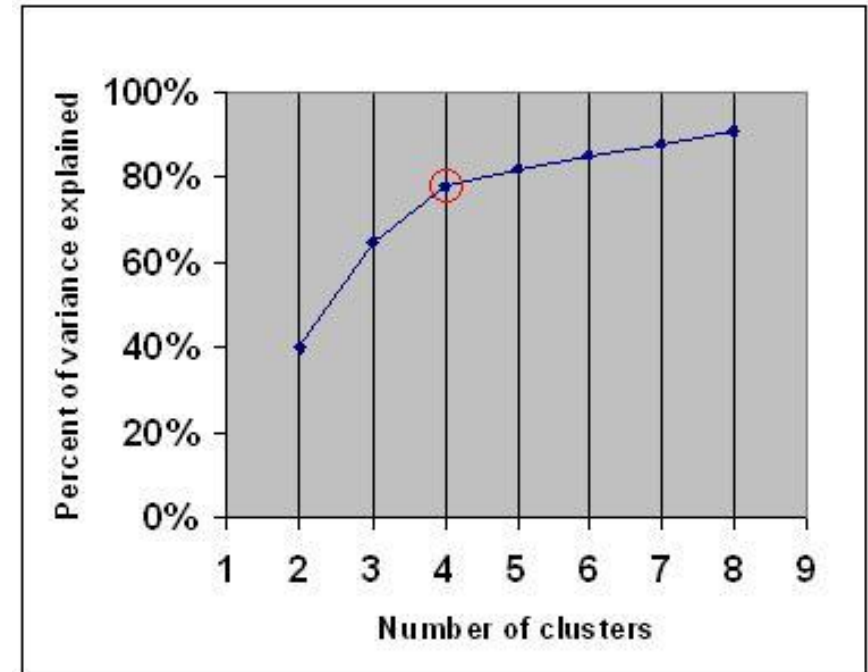
- The algorithm is only applicable if the mean is defined.
- The user needs to specify k .
- The algorithm is sensitive to **outliers**

K-Means clustering

Rule of thumb $k \approx \frac{\sqrt{n}}{2}$
n = number of data points

Elbow method

- percentage of variance explained as a function of the number of clusters
- choose a number of clusters so that adding another cluster doesn't give much better modeling of the data.



K-means clustering

Others k optimization techniques

- Silhouette
- Calinsky criterion
- Bayesian Information Criterion
- Affinity propagation (AP) clustering
- Gap statistic

Questions?