

5)

$$h_i(\bar{r}_{ij}, \bar{r}_{ik}, \theta_{jikh}) = \lambda \cdot \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot (\cos \theta_{jikh} + \frac{1}{3})^2$$

$$\cos \theta_{jikh} = \frac{\bar{r}_{ij}^2 + \bar{r}_{ik}^2 - \bar{r}_{jk}^2}{2 \times \bar{r}_{ij} \times \bar{r}_{ik}}$$

$$* \frac{\partial h_i}{\partial \bar{r}_{ij}} = \lambda \cdot \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot (-\bar{r})(\bar{r}_{ij}-a)^{-2} \cdot (\cos \theta_{jikh} + \frac{1}{3})^2$$

$$+ \lambda \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot 2(\cos \theta_{jikh} + \frac{1}{3}) \cdot \left(\frac{\bar{r}_{ij}^2 - \bar{r}_{ik}^2 + \bar{r}_{jk}^2}{2 \times \bar{r}_{ij} \times \bar{r}_{ik}} \right)$$

$$= \lambda \cdot \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot (\cos \theta_{jikh} + \frac{1}{3}) \left[\left(\frac{\bar{r}_{ij}^2 - \bar{r}_{ik}^2 + \bar{r}_{jk}^2}{\bar{r}_{ij} \times \bar{r}_{ik}} \right) - \bar{r}(\bar{r}_{ij}-a)^{-2} (\cos \theta_{jikh} + \frac{1}{3}) \right]$$

$$* \frac{\partial h_i}{\partial \bar{r}_{ik}} = \lambda \cdot \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot (-\bar{r})(\bar{r}_{ik}-a)^{-2} \cdot (\cos \theta_{jikh} + \frac{1}{3})^2$$

$$+ \lambda \cdot \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot 2(\cos \theta_{jikh} + \frac{1}{3}) \cdot \left(\frac{\bar{r}_{ik}^2 - \bar{r}_{ij}^2 + \bar{r}_{jk}^2}{2 \times \bar{r}_{ik} \times \bar{r}_{ij}} \right)$$

$$= \lambda \cdot \exp[\bar{r}(\bar{r}_{ij}-a)^{-1} + \bar{r}(\bar{r}_{ik}-a)^{-1}] \cdot (\cos \theta_{jikh} + \frac{1}{3}) \cdot \left[\left(\frac{\bar{r}_{ik}^2 - \bar{r}_{ij}^2 + \bar{r}_{jk}^2}{\bar{r}_{ik} \times \bar{r}_{ij}} \right) - \bar{r}(\bar{r}_{ik}-a)^{-2} (\cos \theta_{jikh} + \frac{1}{3}) \right]$$