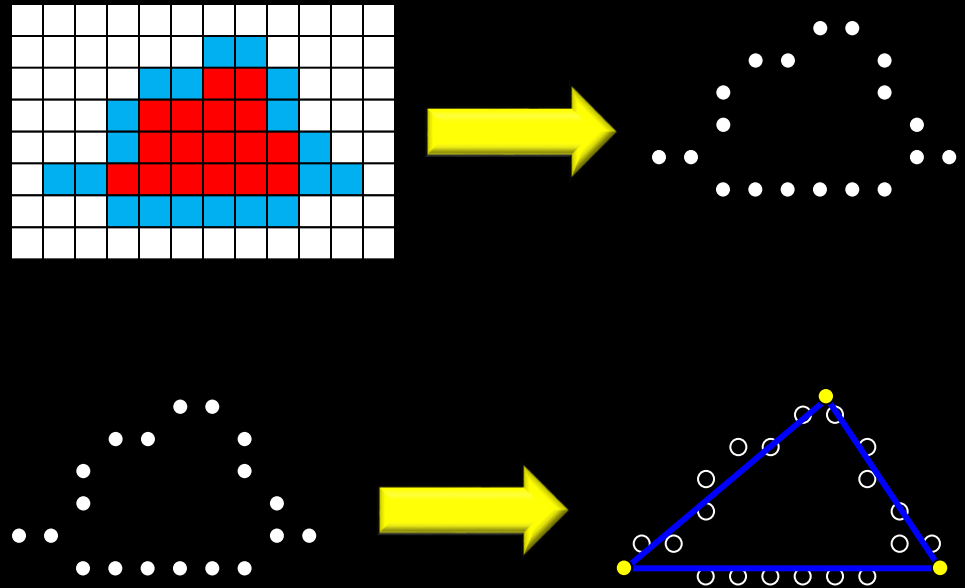


Converting to Vector Maps

Converting To Vector

- Once we have detected object borders within the occupancy grid, we can convert to polygons.
 - Consider each obstacle separately.
 - When tracing a border, build up a list of the border points for that obstacle in sequential order ... assume each grid cell is a point.
 - Then run a line-fitting algorithm

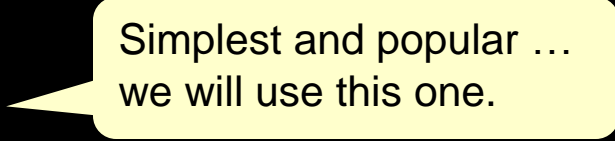


Converting To Vector

- Key issues:

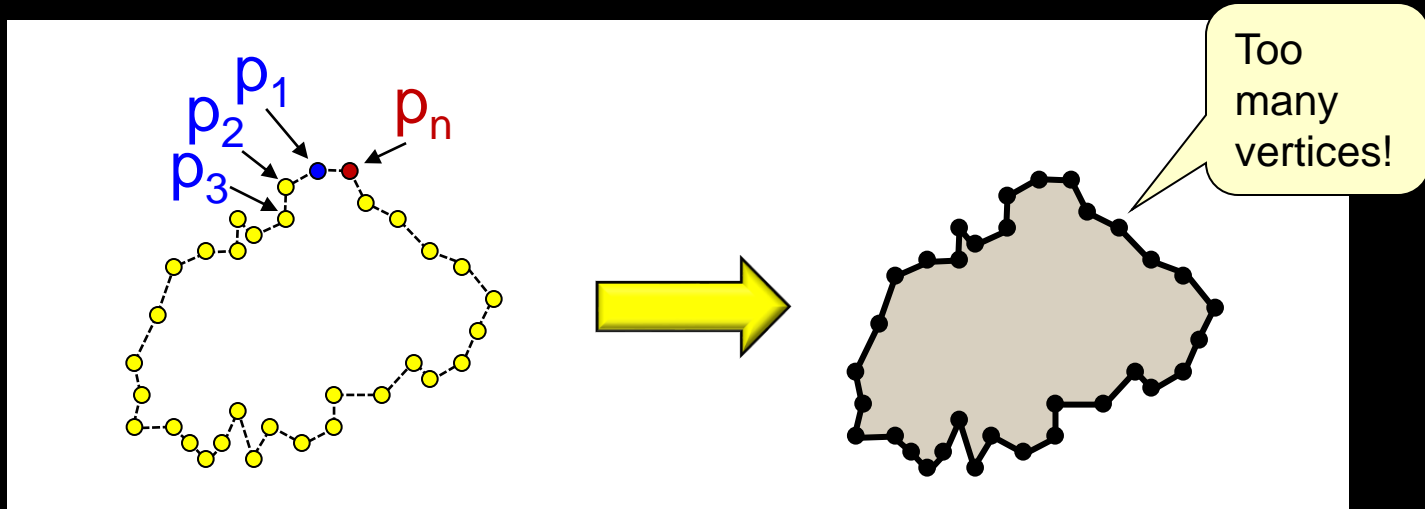
- How do we group points into line segments ?
- How can we detect and eliminate noisy data ?

- There are a variety of common techniques:

- Split & Merge
- Incremental } 
- Line Regression
- RANSAC (Random Sample Consensus)
- Hough-Transform
- EM (Expectation-Maximization)

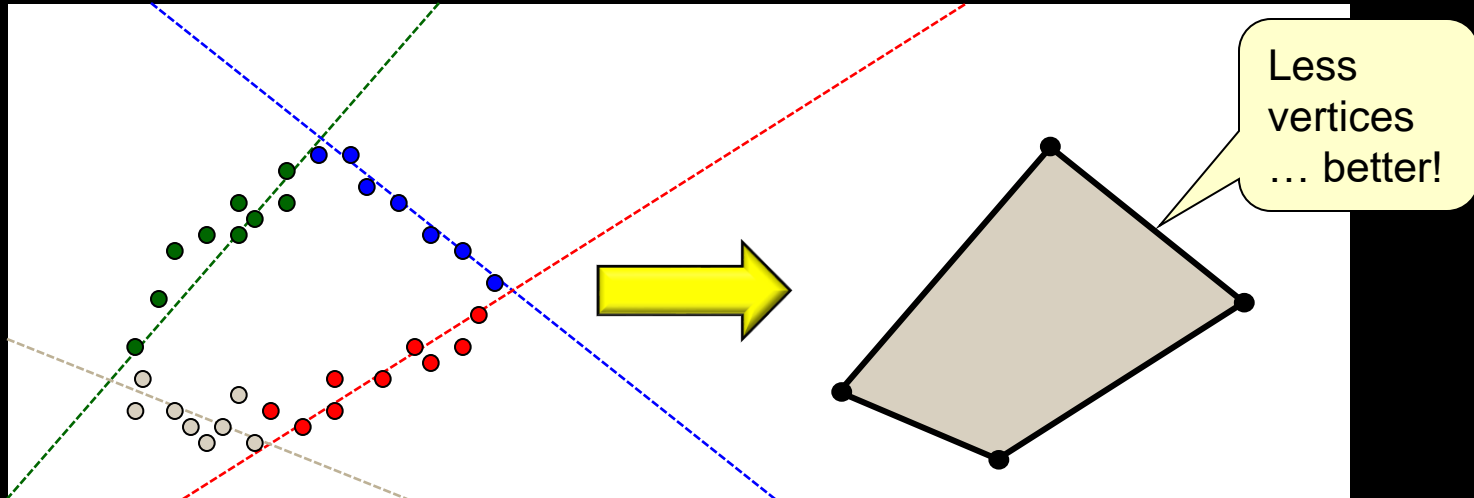
The Main Idea

- Consider a set of border points:
 - $P = \{p_1, p_2, p_3, \dots, p_n\}$ where $p_i = (x_i, y_i)$, $1 \leq i \leq n$
 - As we do a border-tracing algorithm, these points will be coming in a counter-clockwise order
- We can simply connect all points in order, but this is too many points and assumes that all points are valid.



The Main Idea

- It is better to try and “fit” lines to the data:



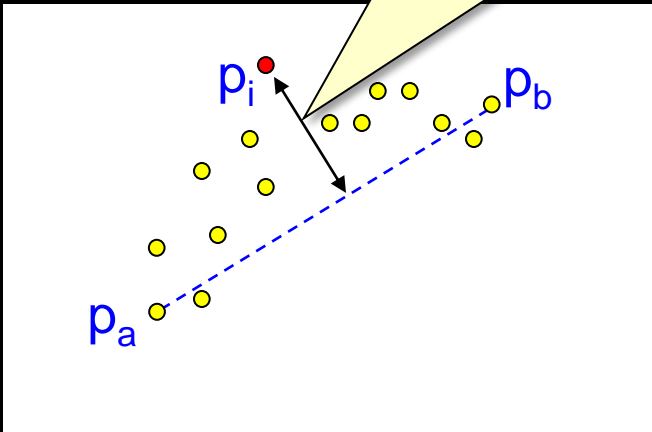
- But how do we know which points fit to a line ?
 - Assume consecutive points lie on the same line unless they are too far away from the line.

The Main Idea

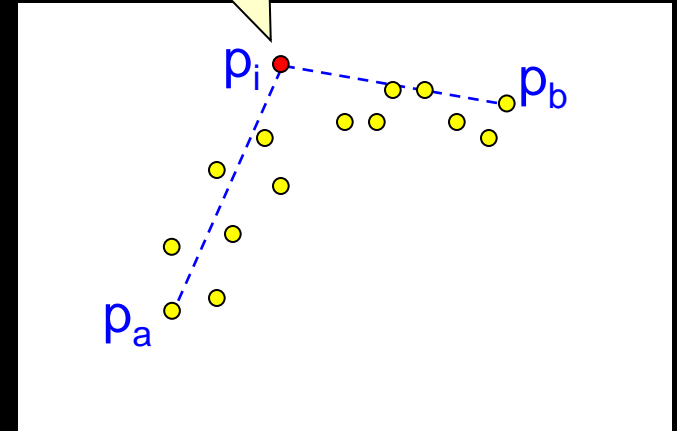
- Let p_i be point of maximum distance from line $L = \overline{p_a p_b}$

Distance from p_i to L is:

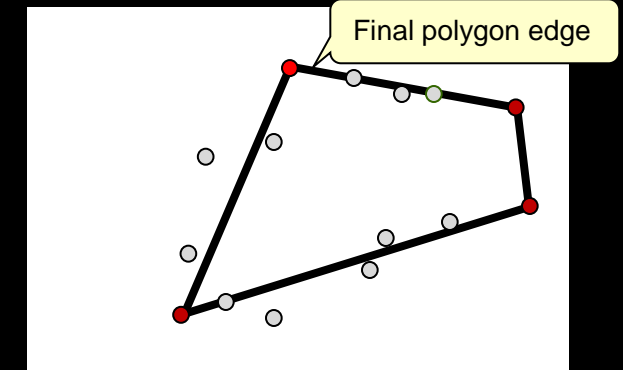
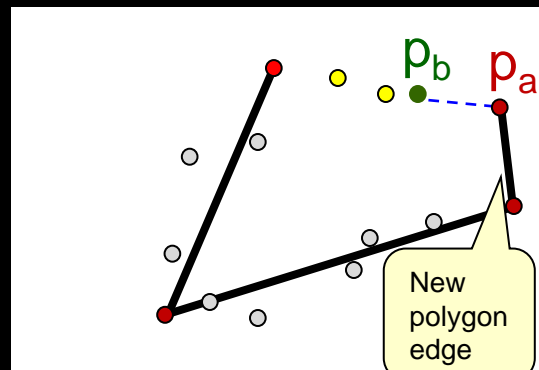
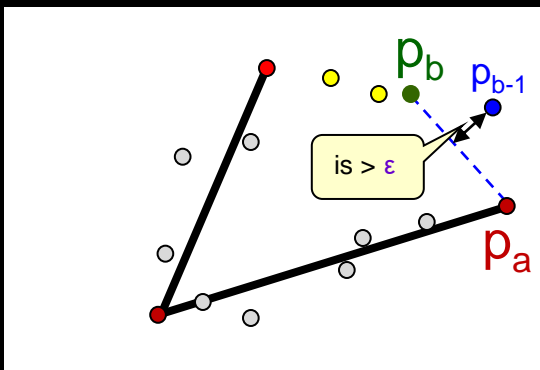
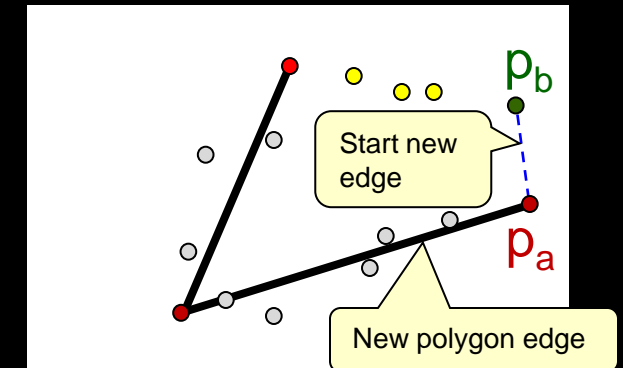
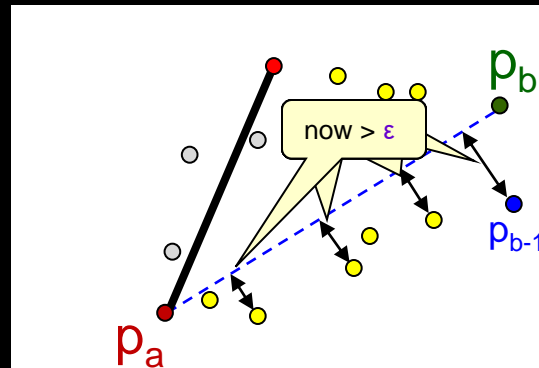
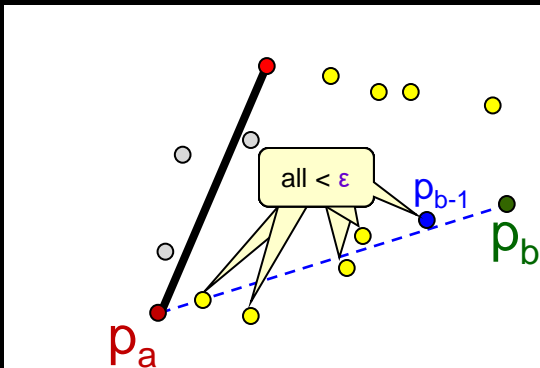
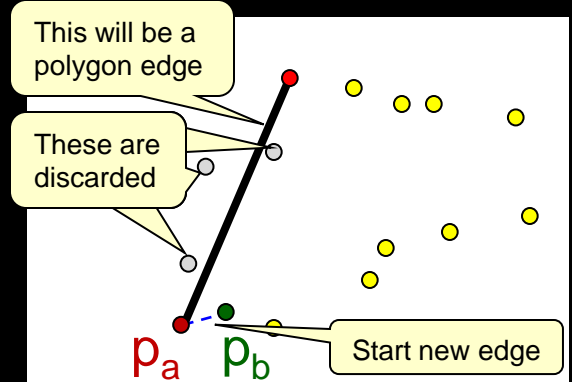
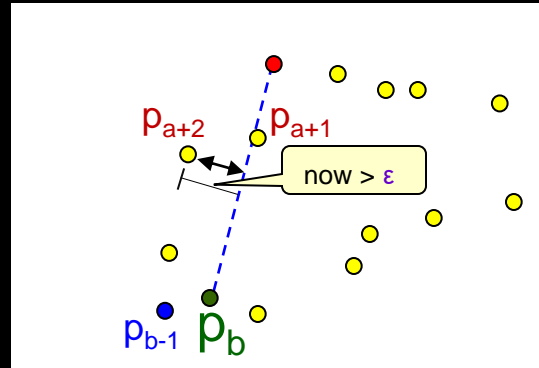
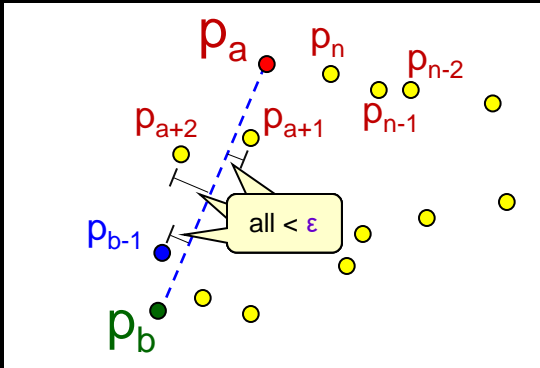
$$\frac{|(x_b - x_a)(y_a - y_i) - (x_a - x_i)(y_b - y_a)|}{\sqrt{(x_b - x_a)^2 + (y_b - y_a)^2}}$$



If p_i is too far away, then this data must represent more than one line (i.e., two distinct polygon edges).



The Incremental Algorithm



The Pseudocode

- Here is the algorithm for point set $p_1, p_2, p_3, \dots, p_n$:

```
1. Set polygon to be a new obstacle with no vertices
2. First, make sure the point set has at least 3 points, otherwise quit
3. Set a = 1, and set  $p_a$  to be the polygon's first vertex
4. FOR index b = 2 to n DO {
5.   FOR index i = a+1 to b-1 DO {
6.     IF point  $p_i$  is too far from line  $p_a p_b$  THEN {
7.       Add  $p_{b-1}$  as the next vertex of the polygon unless it is the same as the last vertex added.
8.       Set a = b-1.
9.     }
10.  }
11. }
```



Note that the pseudocode has points with indices 1 to **n** but our **Obstacle** indices go from 0 to **n**-1.

Too far means greater than some LINE_TOLERANCE (i.e., denoted as ϵ in the previous slide)

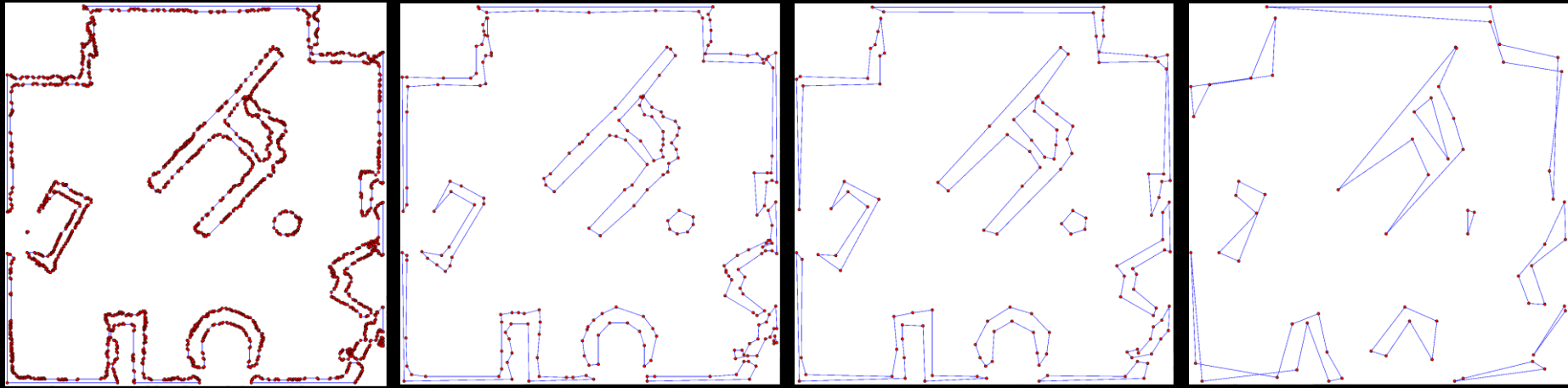


Since variable **a** has been changed, p_a must also be updated.

- Once the polygon is created, we should check to make sure it has at least three vertices. If not, we discard it since it is not a proper polygon.

The Incremental Algorithm

- By increasing the line-fit tolerance, the number of polygon vertices decreases:



Increased Line-Fit Tolerance (i.e., Error Threshold)



**Start the
Lab ...**