Practical Machine Learning - Final Project

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### Assignment

Using devices such as Jawbone Up, Nike FuelBand, and Fitbit it is now possible to collect a large amount of data about personal activity relatively inexpensively. These type of devices are part of the quantified self movement - a group of enthusiasts who take measurements about themselves regularly to improve their health, to find patterns in their behavior, or because they are tech geeks. One thing that people regularly do is quantify how much of a particular activity they do, but they rarely quantify how well they do it. In this project, your goal will be to use data from accelerometers on the belt, forearm, arm, and dumbell of 6 participants. They were asked to perform barbell lifts correctly and incorrectly in 5 different ways. More information is available from the website here: [<http://groupware.les.inf.puc-rio.br/har>](http://groupware.les.inf.puc-rio.br/har) (see the section on the Weight Lifting Exercise Dataset).

#### Data

The training data for this project are available here:

[<https://d396qusza40orc.cloudfront.net/predmachlearn/pml-training.csv>](https://d396qusza40orc.cloudfront.net/predmachlearn/pml-training.csv)

#### The test data are available here:

[<https://d396qusza40orc.cloudfront.net/predmachlearn/pml-testing.csv>](https://d396qusza40orc.cloudfront.net/predmachlearn/pml-testing.csv)

The data for this project come from this source: [<http://groupware.les.inf.puc-rio.br/har>](http://groupware.les.inf.puc-rio.br/har). If you use the document you create for this class for any purpose please cite them as they have been very generous in allowing their data to be used for this kind of assignment.

#### What you should submit

The goal of your project is to predict the manner in which they did the exercise. This is the "classe" variable in the training set. You may use any of the other variables to predict with. You should create a report describing how you built your model, how you used cross validation, what you think the expected out of sample error is, and why you made the choices you did. You will also use your prediction model to predict 20 different test cases.

#### Final Project Steps

1. Load the *testing* and *training* data from online repositories supplied for the assignment
2. Using nearZeroVar function to remove sparse columns from the *testing* and *training* data sets
3. Removing the columns containing NA only from both, *training* and *testing* data set
4. Removing the last column from the *testing* data set (Result ID) and replacing it with a column called *classe* supplying the same levels of factors and populating the column with dummy data. This column would never be used, but is required for the random forest algorithm to be there.
5. Removing columns 1 through 6 from both *training* and *testing* data sets to assure that there are no discrepancies exist between *training* and *testing* data sets: factor levels are the same and classes of columns are the same.
6. Coercing classes for all fields between *training* and *testing* data frames to be the same, thus, at this stage, making *training* and *testing* data sets supplied for the assignment to be processed identically and having identical data types, factors, classes, and etc. between the data sets.
7. Sub splitting training dataset supplied for the assignment into *my\_training* and *my\_testing* data sets to assure that cross-validation requirement for the assignment is addressed.
8. Train the treeFit model using *my\_training* data set (classification tree) and run predictions using *my\_testing* data set. The accuracy of the model is in low seventy percent.
9. Train the rfFit model using *my\_training* data set (random forest algorythm) and run predictions using *my\_testing* data set. The accuracy of the mode is better than 99%. Thus, rfFit should be used for prediction on the *testing* data set supplied for the assignment.
10. Calculate prediction using rfFit model build using *my\_training* data set and *testing* data set supplied for the assignment. Print out results. Use the results to populate the quiz.
11. Out of sample erro was calculated using *my\_testing* data set instead of *testing* data set. The problem was that *classe* column was not provided as part of the data set, but I used *classe* variable. The general principle of calculating out of sample error would be exaclty the same but using *testing* data set provided for the assignment.

#### Code and explanations

Load librarires and set working directory

library(caret)

## Warning: package 'caret' was built under R version 3.2.3

## Loading required package: lattice  
## Loading required package: ggplot2

## Warning: package 'ggplot2' was built under R version 3.2.2

library(rpart)  
library(randomForest)

## Warning: package 'randomForest' was built under R version 3.2.3

## randomForest 4.6-12  
## Type rfNews() to see new features/changes/bug fixes.

set.seed(212121)

Download data files if not already downloaded

# Set appropriate working directory  
# setwd('C:\\Users\\db345c\\Desktop\\Practical Machine Learning\\Final\_Project')  
setwd('C:\\Users\\Aleksey\\Documents\\School\\coursera\\Practical\_Machine\_Learning\\Final\_Project')  
  
# Check if the files exist locally, if not - download  
training.url <- "https://d396qusza40orc.cloudfront.net/predmachlearn/pml-training.csv"  
testing.url <- "https://d396qusza40orc.cloudfront.net/predmachlearn/pml-testing.csv"  
  
if(!file.exists("pml-training.csv")) {  
 download.file(training.url, "pml-training.csv")  
}  
  
if(!file.exists("pml-testing.csv")){  
 download.file(testing.url, "pml-testing.csv")  
}

Loading data files into memory

# Load training and testing data sets  
training <- read.csv("pml-training.csv", na.strings = c("NA","", "#DIV/0!"))  
testing <- read.csv("pml-testing.csv", na.strings = c("NA","", "#DIV/0!"))  
  
# cleanup unused variables  
rm(training.url, testing.url)

Prepare the data to be consumed by the prediction algorythms

# identifying sparsely populated columns using nearZeroVar function  
# from testing and training data sets  
# Identical changes need to be made to testing and training data sets  
to\_skip <- nearZeroVar(training)  
training <- training[, -to\_skip]  
testing <- testing[, -to\_skip]  
  
# cleanup unused variables  
rm(to\_skip)  
  
# removing columns containing NA's only  
# Identical changes need to be made to testing and training data sets  
col\_lst <- colSums(is.na(training)) == 0  
training <- training[, col\_lst]  
testing <- testing[, col\_lst]  
  
# adjusting data - remove column 59 from the testing data (not needed)  
testing <- testing[, -c(59)]  
  
# creating simple dummy data with 5 levels identical to those in training data set  
# iterate throug the data frame using sample function to select a sample of size 1 from  
# vector called levels. The classe variable was not provided as part of the testing  
# data set, this is why I have to add a dummy classe variable.  
train\_levels <- levels(training$classe)  
v <- vector(mode="character", length=0)  
for (i in testing[,1]) {  
 x <- sample(train\_levels, size=1, replace = TRUE)  
 v <- c(v, x)  
}  
  
# apppending dummy data (as factor) with the same factors and number of factors as in the training data  
# as well as with the same name (simply for convenience)  
testing$classe <- as.factor(v)  
  
# Remove remove index, factor, and several date columns from training and testing data set  
testing <- testing[, -c(1:6)]  
training <- training[, -c(1:6)]  
  
# cleanup unused variables  
rm(col\_lst, v, train\_levels, x)

Explore data frames to identify discrepancies in field's class types

# Explore training and testing data to assure that all fields in both training and testing  
# data sets have identical classes for each of the fields.  
str(training)

## 'data.frame': 19622 obs. of 53 variables:  
## $ roll\_belt : num 1.41 1.41 1.42 1.48 1.48 1.45 1.42 1.42 1.43 1.45 ...  
## $ pitch\_belt : num 8.07 8.07 8.07 8.05 8.07 8.06 8.09 8.13 8.16 8.17 ...  
## $ yaw\_belt : num -94.4 -94.4 -94.4 -94.4 -94.4 -94.4 -94.4 -94.4 -94.4 -94.4 ...  
## $ total\_accel\_belt : int 3 3 3 3 3 3 3 3 3 3 ...  
## $ gyros\_belt\_x : num 0 0.02 0 0.02 0.02 0.02 0.02 0.02 0.02 0.03 ...  
## $ gyros\_belt\_y : num 0 0 0 0 0.02 0 0 0 0 0 ...  
## $ gyros\_belt\_z : num -0.02 -0.02 -0.02 -0.03 -0.02 -0.02 -0.02 -0.02 -0.02 0 ...  
## $ accel\_belt\_x : int -21 -22 -20 -22 -21 -21 -22 -22 -20 -21 ...  
## $ accel\_belt\_y : int 4 4 5 3 2 4 3 4 2 4 ...  
## $ accel\_belt\_z : int 22 22 23 21 24 21 21 21 24 22 ...  
## $ magnet\_belt\_x : int -3 -7 -2 -6 -6 0 -4 -2 1 -3 ...  
## $ magnet\_belt\_y : int 599 608 600 604 600 603 599 603 602 609 ...  
## $ magnet\_belt\_z : int -313 -311 -305 -310 -302 -312 -311 -313 -312 -308 ...  
## $ roll\_arm : num -128 -128 -128 -128 -128 -128 -128 -128 -128 -128 ...  
## $ pitch\_arm : num 22.5 22.5 22.5 22.1 22.1 22 21.9 21.8 21.7 21.6 ...  
## $ yaw\_arm : num -161 -161 -161 -161 -161 -161 -161 -161 -161 -161 ...  
## $ total\_accel\_arm : int 34 34 34 34 34 34 34 34 34 34 ...  
## $ gyros\_arm\_x : num 0 0.02 0.02 0.02 0 0.02 0 0.02 0.02 0.02 ...  
## $ gyros\_arm\_y : num 0 -0.02 -0.02 -0.03 -0.03 -0.03 -0.03 -0.02 -0.03 -0.03 ...  
## $ gyros\_arm\_z : num -0.02 -0.02 -0.02 0.02 0 0 0 0 -0.02 -0.02 ...  
## $ accel\_arm\_x : int -288 -290 -289 -289 -289 -289 -289 -289 -288 -288 ...  
## $ accel\_arm\_y : int 109 110 110 111 111 111 111 111 109 110 ...  
## $ accel\_arm\_z : int -123 -125 -126 -123 -123 -122 -125 -124 -122 -124 ...  
## $ magnet\_arm\_x : int -368 -369 -368 -372 -374 -369 -373 -372 -369 -376 ...  
## $ magnet\_arm\_y : int 337 337 344 344 337 342 336 338 341 334 ...  
## $ magnet\_arm\_z : int 516 513 513 512 506 513 509 510 518 516 ...  
## $ roll\_dumbbell : num 13.1 13.1 12.9 13.4 13.4 ...  
## $ pitch\_dumbbell : num -70.5 -70.6 -70.3 -70.4 -70.4 ...  
## $ yaw\_dumbbell : num -84.9 -84.7 -85.1 -84.9 -84.9 ...  
## $ total\_accel\_dumbbell: int 37 37 37 37 37 37 37 37 37 37 ...  
## $ gyros\_dumbbell\_x : num 0 0 0 0 0 0 0 0 0 0 ...  
## $ gyros\_dumbbell\_y : num -0.02 -0.02 -0.02 -0.02 -0.02 -0.02 -0.02 -0.02 -0.02 -0.02 ...  
## $ gyros\_dumbbell\_z : num 0 0 0 -0.02 0 0 0 0 0 0 ...  
## $ accel\_dumbbell\_x : int -234 -233 -232 -232 -233 -234 -232 -234 -232 -235 ...  
## $ accel\_dumbbell\_y : int 47 47 46 48 48 48 47 46 47 48 ...  
## $ accel\_dumbbell\_z : int -271 -269 -270 -269 -270 -269 -270 -272 -269 -270 ...  
## $ magnet\_dumbbell\_x : int -559 -555 -561 -552 -554 -558 -551 -555 -549 -558 ...  
## $ magnet\_dumbbell\_y : int 293 296 298 303 292 294 295 300 292 291 ...  
## $ magnet\_dumbbell\_z : num -65 -64 -63 -60 -68 -66 -70 -74 -65 -69 ...  
## $ roll\_forearm : num 28.4 28.3 28.3 28.1 28 27.9 27.9 27.8 27.7 27.7 ...  
## $ pitch\_forearm : num -63.9 -63.9 -63.9 -63.9 -63.9 -63.9 -63.9 -63.8 -63.8 -63.8 ...  
## $ yaw\_forearm : num -153 -153 -152 -152 -152 -152 -152 -152 -152 -152 ...  
## $ total\_accel\_forearm : int 36 36 36 36 36 36 36 36 36 36 ...  
## $ gyros\_forearm\_x : num 0.03 0.02 0.03 0.02 0.02 0.02 0.02 0.02 0.03 0.02 ...  
## $ gyros\_forearm\_y : num 0 0 -0.02 -0.02 0 -0.02 0 -0.02 0 0 ...  
## $ gyros\_forearm\_z : num -0.02 -0.02 0 0 -0.02 -0.03 -0.02 0 -0.02 -0.02 ...  
## $ accel\_forearm\_x : int 192 192 196 189 189 193 195 193 193 190 ...  
## $ accel\_forearm\_y : int 203 203 204 206 206 203 205 205 204 205 ...  
## $ accel\_forearm\_z : int -215 -216 -213 -214 -214 -215 -215 -213 -214 -215 ...  
## $ magnet\_forearm\_x : int -17 -18 -18 -16 -17 -9 -18 -9 -16 -22 ...  
## $ magnet\_forearm\_y : num 654 661 658 658 655 660 659 660 653 656 ...  
## $ magnet\_forearm\_z : num 476 473 469 469 473 478 470 474 476 473 ...  
## $ classe : Factor w/ 5 levels "A","B","C","D",..: 1 1 1 1 1 1 1 1 1 1 ...

str(testing)

## 'data.frame': 20 obs. of 53 variables:  
## $ roll\_belt : num 123 1.02 0.87 125 1.35 -5.92 1.2 0.43 0.93 114 ...  
## $ pitch\_belt : num 27 4.87 1.82 -41.6 3.33 1.59 4.44 4.15 6.72 22.4 ...  
## $ yaw\_belt : num -4.75 -88.9 -88.5 162 -88.6 -87.7 -87.3 -88.5 -93.7 -13.1 ...  
## $ total\_accel\_belt : int 20 4 5 17 3 4 4 4 4 18 ...  
## $ gyros\_belt\_x : num -0.5 -0.06 0.05 0.11 0.03 0.1 -0.06 -0.18 0.1 0.14 ...  
## $ gyros\_belt\_y : num -0.02 -0.02 0.02 0.11 0.02 0.05 0 -0.02 0 0.11 ...  
## $ gyros\_belt\_z : num -0.46 -0.07 0.03 -0.16 0 -0.13 0 -0.03 -0.02 -0.16 ...  
## $ accel\_belt\_x : int -38 -13 1 46 -8 -11 -14 -10 -15 -25 ...  
## $ accel\_belt\_y : int 69 11 -1 45 4 -16 2 -2 1 63 ...  
## $ accel\_belt\_z : int -179 39 49 -156 27 38 35 42 32 -158 ...  
## $ magnet\_belt\_x : int -13 43 29 169 33 31 50 39 -6 10 ...  
## $ magnet\_belt\_y : int 581 636 631 608 566 638 622 635 600 601 ...  
## $ magnet\_belt\_z : int -382 -309 -312 -304 -418 -291 -315 -305 -302 -330 ...  
## $ roll\_arm : num 40.7 0 0 -109 76.1 0 0 0 -137 -82.4 ...  
## $ pitch\_arm : num -27.8 0 0 55 2.76 0 0 0 11.2 -63.8 ...  
## $ yaw\_arm : num 178 0 0 -142 102 0 0 0 -167 -75.3 ...  
## $ total\_accel\_arm : int 10 38 44 25 29 14 15 22 34 32 ...  
## $ gyros\_arm\_x : num -1.65 -1.17 2.1 0.22 -1.96 0.02 2.36 -3.71 0.03 0.26 ...  
## $ gyros\_arm\_y : num 0.48 0.85 -1.36 -0.51 0.79 0.05 -1.01 1.85 -0.02 -0.5 ...  
## $ gyros\_arm\_z : num -0.18 -0.43 1.13 0.92 -0.54 -0.07 0.89 -0.69 -0.02 0.79 ...  
## $ accel\_arm\_x : int 16 -290 -341 -238 -197 -26 99 -98 -287 -301 ...  
## $ accel\_arm\_y : int 38 215 245 -57 200 130 79 175 111 -42 ...  
## $ accel\_arm\_z : int 93 -90 -87 6 -30 -19 -67 -78 -122 -80 ...  
## $ magnet\_arm\_x : int -326 -325 -264 -173 -170 396 702 535 -367 -420 ...  
## $ magnet\_arm\_y : int 385 447 474 257 275 176 15 215 335 294 ...  
## $ magnet\_arm\_z : int 481 434 413 633 617 516 217 385 520 493 ...  
## $ roll\_dumbbell : num -17.7 54.5 57.1 43.1 -101.4 ...  
## $ pitch\_dumbbell : num 25 -53.7 -51.4 -30 -53.4 ...  
## $ yaw\_dumbbell : num 126.2 -75.5 -75.2 -103.3 -14.2 ...  
## $ total\_accel\_dumbbell: int 9 31 29 18 4 29 29 29 3 2 ...  
## $ gyros\_dumbbell\_x : num 0.64 0.34 0.39 0.1 0.29 -0.59 0.34 0.37 0.03 0.42 ...  
## $ gyros\_dumbbell\_y : num 0.06 0.05 0.14 -0.02 -0.47 0.8 0.16 0.14 -0.21 0.51 ...  
## $ gyros\_dumbbell\_z : num -0.61 -0.71 -0.34 0.05 -0.46 1.1 -0.23 -0.39 -0.21 -0.03 ...  
## $ accel\_dumbbell\_x : int 21 -153 -141 -51 -18 -138 -145 -140 0 -7 ...  
## $ accel\_dumbbell\_y : int -15 155 155 72 -30 166 150 159 25 -20 ...  
## $ accel\_dumbbell\_z : int 81 -205 -196 -148 -5 -186 -190 -191 9 7 ...  
## $ magnet\_dumbbell\_x : int 523 -502 -506 -576 -424 -543 -484 -515 -519 -531 ...  
## $ magnet\_dumbbell\_y : int -528 388 349 238 252 262 354 350 348 321 ...  
## $ magnet\_dumbbell\_z : int -56 -36 41 53 312 96 97 53 -32 -164 ...  
## $ roll\_forearm : num 141 109 131 0 -176 150 155 -161 15.5 13.2 ...  
## $ pitch\_forearm : num 49.3 -17.6 -32.6 0 -2.16 1.46 34.5 43.6 -63.5 19.4 ...  
## $ yaw\_forearm : num 156 106 93 0 -47.9 89.7 152 -89.5 -139 -105 ...  
## $ total\_accel\_forearm : int 33 39 34 43 24 43 32 47 36 24 ...  
## $ gyros\_forearm\_x : num 0.74 1.12 0.18 1.38 -0.75 -0.88 -0.53 0.63 0.03 0.02 ...  
## $ gyros\_forearm\_y : num -3.34 -2.78 -0.79 0.69 3.1 4.26 1.8 -0.74 0.02 0.13 ...  
## $ gyros\_forearm\_z : num -0.59 -0.18 0.28 1.8 0.8 1.35 0.75 0.49 -0.02 -0.07 ...  
## $ accel\_forearm\_x : int -110 212 154 -92 131 230 -192 -151 195 -212 ...  
## $ accel\_forearm\_y : int 267 297 271 406 -93 322 170 -331 204 98 ...  
## $ accel\_forearm\_z : int -149 -118 -129 -39 172 -144 -175 -282 -217 -7 ...  
## $ magnet\_forearm\_x : int -714 -237 -51 -233 375 -300 -678 -109 0 -403 ...  
## $ magnet\_forearm\_y : int 419 791 698 783 -787 800 284 -619 652 723 ...  
## $ magnet\_forearm\_z : int 617 873 783 521 91 884 585 -32 469 512 ...  
## $ classe : Factor w/ 5 levels "A","B","C","D",..: 5 1 2 3 3 1 3 5 4 1 ...

Coherce field classes to be the same between two data frames: *testing* and *training*

# coherce training and testing data to the same data types and fix factors in testing  
for (i in 1:length(testing)) {  
 for(j in 1:length(training)) {  
 if( length(grep(names(training[i]), names(testing)[j])) == 1) {  
 class(testing[j]) <- class(training[i])  
 }   
 }   
}  
  
# fix coersion that failed in previous step (this is required!!!)  
for (i in 1:length(testing)) {  
 if (class(training[, i]) != class(testing[, i])) {  
 ### try fixing coersion, so testing and training data frames match  
 class(training[, i]) <- class(testing[, i])  
 }  
}

Split *training* data set into *my\_training* and *my\_testing* data sets.

# Partition data into two two sets - training and testing  
# Identical changes need to be made to testing and training data sets  
inTrain <- createDataPartition(y=training$classe, p=0.6, list=FALSE)  
my\_training <- training[inTrain,]  
my\_testing <- training[-inTrain,]  
  
# cleanup unused variables  
rm(inTrain, i, j)

Generate tree and run prediction. Accuracy is quite low.

# Build decision tree model and run predictions  
set.seed(212121)  
treeFit <- rpart(classe ~., data=my\_training, method="class")  
treePredicted <- predict(treeFit, my\_testing, type="class")  
# print confusion matrix for treePredicted vs. my\_testing$classe  
confusionMatrix(treePredicted, my\_testing$classe)

## Confusion Matrix and Statistics  
##   
## Reference  
## Prediction A B C D E  
## A 1973 215 27 57 29  
## B 75 836 116 109 106  
## C 66 206 1110 206 182  
## D 81 120 80 827 87  
## E 37 141 35 87 1038  
##   
## Overall Statistics  
##   
## Accuracy : 0.7372   
## 95% CI : (0.7273, 0.7469)  
## No Information Rate : 0.2845   
## P-Value [Acc > NIR] : < 2.2e-16   
##   
## Kappa : 0.6675   
## Mcnemar's Test P-Value : < 2.2e-16   
##   
## Statistics by Class:  
##   
## Class: A Class: B Class: C Class: D Class: E  
## Sensitivity 0.8840 0.5507 0.8114 0.6431 0.7198  
## Specificity 0.9416 0.9358 0.8981 0.9439 0.9532  
## Pos Pred Value 0.8575 0.6731 0.6271 0.6921 0.7758  
## Neg Pred Value 0.9533 0.8967 0.9575 0.9310 0.9379  
## Prevalence 0.2845 0.1935 0.1744 0.1639 0.1838  
## Detection Rate 0.2515 0.1066 0.1415 0.1054 0.1323  
## Detection Prevalence 0.2933 0.1583 0.2256 0.1523 0.1705  
## Balanced Accuracy 0.9128 0.7433 0.8548 0.7935 0.8365

Generate Random Forest and run prediction. Accuracy is more than 99%

rfFit <- randomForest(classe ~., data=my\_training)  
rfPredicted <- predict(rfFit, my\_testing, type="class")  
confusionMatrix(rfPredicted, my\_testing$classe)

## Confusion Matrix and Statistics  
##   
## Reference  
## Prediction A B C D E  
## A 2232 13 0 0 0  
## B 0 1502 9 0 0  
## C 0 3 1359 12 0  
## D 0 0 0 1273 3  
## E 0 0 0 1 1439  
##   
## Overall Statistics  
##   
## Accuracy : 0.9948   
## 95% CI : (0.9929, 0.9962)  
## No Information Rate : 0.2845   
## P-Value [Acc > NIR] : < 2.2e-16   
##   
## Kappa : 0.9934   
## Mcnemar's Test P-Value : NA   
##   
## Statistics by Class:  
##   
## Class: A Class: B Class: C Class: D Class: E  
## Sensitivity 1.0000 0.9895 0.9934 0.9899 0.9979  
## Specificity 0.9977 0.9986 0.9977 0.9995 0.9998  
## Pos Pred Value 0.9942 0.9940 0.9891 0.9976 0.9993  
## Neg Pred Value 1.0000 0.9975 0.9986 0.9980 0.9995  
## Prevalence 0.2845 0.1935 0.1744 0.1639 0.1838  
## Detection Rate 0.2845 0.1914 0.1732 0.1622 0.1834  
## Detection Prevalence 0.2861 0.1926 0.1751 0.1626 0.1835  
## Balanced Accuracy 0.9988 0.9940 0.9956 0.9947 0.9989

Printing predictions for the test data set supplied for the final project

# printing the answer for the quiz  
finalAnswer <- predict(rfFit, testing, type="class")  
print(finalAnswer)

## 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20   
## B A B A A E D B A A B C B A E E A B B B   
## Levels: A B C D E

Caclulating out of sample eror

# The classe variable was not provided as a part of the testing data set supplied  
# for this assignment, but it was recommended to use classe variable to predict on.  
# The principle of calculating out of sample error would be the same as calculating   
# in sample error, but with testing data set (if classe variable was provied).   
# I used my\_training data set to caclulate in sample error.  
# I expect out of sample error to be slightly larger by a percent or two.  
error\_rate = sum((my\_testing$classe != rfPredicted) / length(rfPredicted))  
print(paste0("The in-sample error rate is: ", error\_rate))

## [1] "The in-sample error rate is: 0.00522559265867958"

print(paste0("The out of sample error rate should be grater than: ", error\_rate))

## [1] "The out of sample error rate should be grater than: 0.00522559265867958"

# The END