

Part 1 Simulation Exercise

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Introduction

In this project exponential distribution is compared with the Central Limit Theorem. The properties of the distribution of the mean of forty exponentials are illustrated via simulation and associated explanatory text. The simulation is performed one thousands times and results for mean and variance across simulations are compared to theoretical values.

Simulations

In this paragraph, 1000 simulations of 40 exponentials are performed. Then the mean is taken across exponentials for each simulation separately.

Sample Mean versus Theoretical Mean

The Central Limit Theorem states that the sample average is approximately normally distributed with a mean given by the population mean (as number of variables tends towards infinity).

Theoretical mean is:

```
## [1] 5
```

Sample mean is:

```
## [1] 5.00402
```

It can be seen that sample mean is approximately equal to theoretical mean.

Sample Variance versus Theoretical Variance

The Central Limit Theorem states that the sample mean is approximately normally distributed with a variance given by the standard error of the mean (as number of variables tends towards infinity). Theoretical variance in this case is population variance divided by \sqrt{n} .

Theoretical mean is:

```
## [1] 0.7905694
```

Sample mean is:

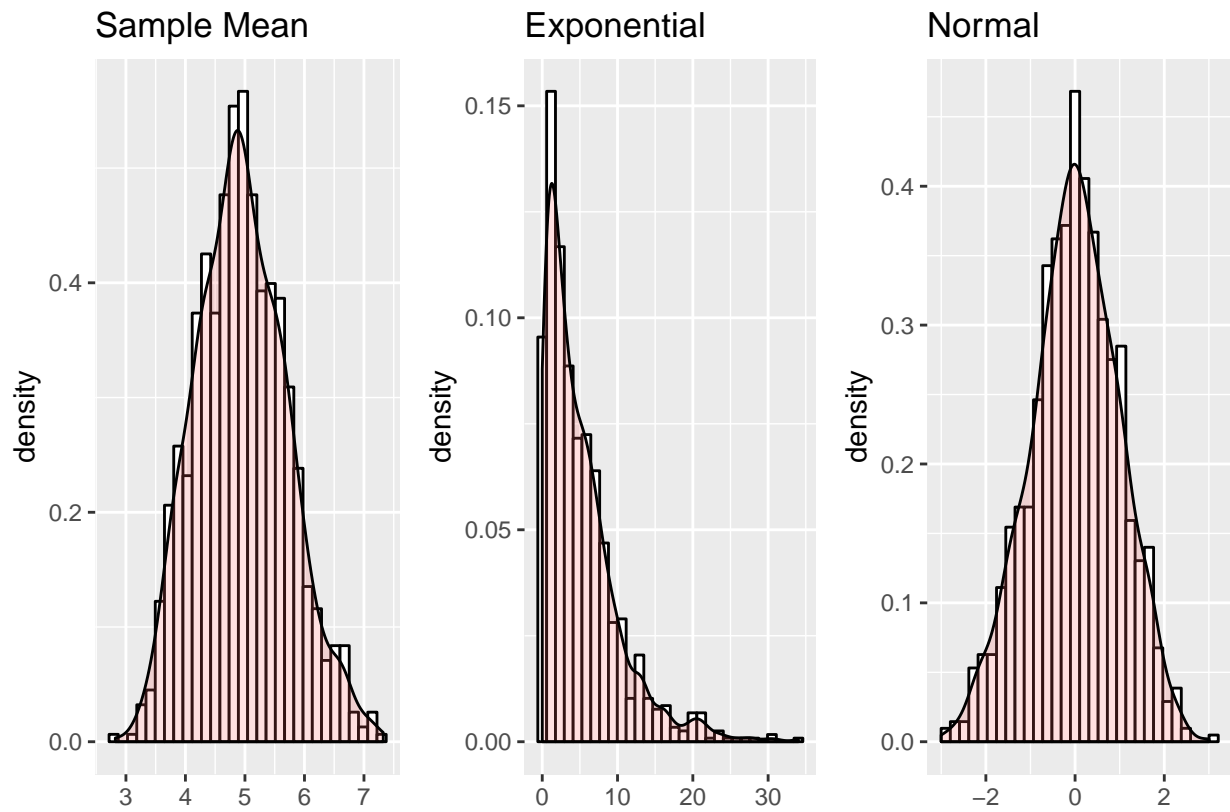
```
## [1] 0.7830184
```

It can be seen that simulation sample variance is approximately equal to theoretical variance.

Distribution

Below data distribution for sample means, exponentially distributed and normally distributed data is shown:

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.  
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```



It can be seen that sample mean distribution looks more like normally distributed data rather than the original exponential distribution.