## Information theory: HW #3 code listing

```
1: {-# LANGUAGE FlexibleContexts
2: {-# LANGUAGE MultiWayIf
                                       #-}
3: {-# LANGUAGE OverloadedStrings
                                       #-}
4: {-# LANGUAGE ScopedTypeVariables #-}
5: {-# LANGUAGE TemplateHaskell
6: {-# LANGUAGE TupleSections
                                       #-}
                                       #-}
7: {-# LANGUAGE TypeApplications
                                       #-}
8: {-# LANGUAGE ViewPatterns
                                      #-}
10: -- | Homework 3
12: module Archivers () where
13:
14: import qualified Base
                                              as B (Show (..))
                     Codec.Compression.GZip (CompressParams (..))
15: import
16: import qualified Codec.Compression.GZip as Z
                     Control.Exception
17: import
                                              (assert)
                     Control.Lens
                                              (makeLenses, to, use, uses, view, (\%=), (+=),
                                              (.=), (<>=), (^.), _1, _2, _3)
(MonadWriter, Writer, runWriter, tell)
19:
20: import
                     Control.Monad.Writer
21: import
                     Data.Bifunctor
                                              (first. second)
22: import
                     Data.Bits
                                              (testBit)
23: import qualified Data.ByteString
                                              as BS
24: import qualified Data.ByteString.Char8
                                              as BSC
25: import qualified Data.ByteString.Lazy
                                              as BSL
26: import
                     Data.List
                                              (dropWhileEnd, findIndex, last, nub, (!!))
27: import qualified Data.Map.Strict
28: import
                     Data.Maybe
                                              (fromJust, mapMaybe)
29: import
                     Data.Number.BigFloat
                                              (BigFloat (..), Prec50, PrecPlus20)
                     Data.Ord
                                              (comparing)
30: import
31: import
                     Data.Ratio
                                              (denominator, numerator, (%))
32: import qualified Data.Text
                                              as T
33: import
                     Data.Word
                                              (Word16)
                     Numeric
                                              (showGFloat)
34: import
                                              hiding ((%))
35: import
                     Universum
36:
37: type String = [Char]
38:
39: dropEnd :: Int -> [a] -> [a]
40: dropEnd i xs = take (length xs - i) xs
41:
42: takeEnd :: Int -> [a] -> [a]
43: takeEnd i xs = drop (length xs - i) xs
45: log2 :: Floating a => a -> a
46: log2 k = log k / log 2
47: \log 2' = \log 2 . from Integral
48:
49: proverb :: ByteString
50: proverb =
       encodeUtf8
51:
            ("Love_the_heart_that_hurts_you,_but_never_hurt_the_heart_that_loves_you." :: Text)
52:
53:
54: testProverb :: ByteString
55: testProverb =
       encodeUtf8
56:
            ("if_we_cannot_do_as_we_would_we_should_do_as_we_can" :: Text)
57:
58:
59: loremIpsum :: ByteString
60: loremIpsum = encodeUtf8 (
61:
        "Lorem ipsum dolor sit amet, consectetur adipiscing elit. \
        \Cras ornare diam nec interdum mollis. Phasellus tortor felis, ∖
62:
63:
        \dapibus eu bibendum eu, commodo quis erat. Vestibulum fringilla, \
64:
        \purus semper eleifend laoreet, sem dui volutpat lectus, sed ullamcorper \
        \ante neque id lectus. Nulla ullamcorper egestas nisl, at convallis \
65:
        \leo tempus vel. Sed mi lacus, aliquam ullamcorper purus vitae, vulputate \
66:
        ∖dignissim ipsum. Nam in est eu quam maximus blandit. Integer nec iaculis ∖
67:
68:
        \felis. Vestibulum ut cras amet. " :: Text)
69:
70:
71: newtype Logger w a = Logger
        { getLogger :: Writer [w] a
72:
        } deriving (Functor, Applicative, Monad, MonadWriter [w])
73:
74:
75: fromWord8 :: [Word8] -> [Char]
76: fromWord8 = map (chr . fromIntegral)
```

```
78: ----
 79: -- Huffman
 80: -----
 82: data HuffmanTrace = HuffmanTrace
        { hCurChar
                      :: Char
 83:
         , hProb
                       :: Ratio Int
 84:
         , hCodeWord :: String
 85:
         , hMsgLength :: Int
 86:
 87:
 88:
 89: instance Show HuffmanTrace where
         show HuffmanTrace {..} =
 90:
             intercalate
 91:
 92:
                 [[hCurChar], show hProb, hCodeWord, show hMsgLength]
 93:
 95: huffman :: BSC.ByteString -> Logger HuffmanTrace ((Map Char (String,Int)),String)
 96: huffman input = encode 0 []
      where
 97:
 98:
         encode i s | i >= BSC.length input = pure (table1, s)
99:
         encode i s = do
             let c = input `BSC.index` i
100:
101:
                 (codeWord,m) = table1 M.! c
                 cl = length codeWord
102:
                 s' = s ++ codeWord
103:
                 hProb = m % n
104:
105:
                 hMsqLength = length s'
             tell $ [HuffmanTrace {hCurChar = c, hCodeWord = codeWord, ..}]
106:
107:
             encode (i+1) s'
         n = BSC.length input
108:
         firstPass :: Map Char Int
109:
         firstPass = BSC.foldr' (M.alter (pure . maybe 1 (+1))) M.empty input
110:
111:
         calcWords :: [(Double,[(Char,Int)])]
         calcWords =
112:
             map ((k, x) \rightarrow (fromIntegral x / fromIntegral n, [(k, 0)]))  M.assocs firstPass
113:
         calcCodeWordDo [(p,x)] = assert (p == 1) x
114:
115:
         calcCodeWordDo (sortOn fst -> ((p0,lefts):(p1,rights):xs)) =
116:
             let inc = map (second (+1))
             in calcCodeWordDo $ sortOn fst $ (p0 + p1, inc lefts ++ inc rights):xs
117:
         codeWords :: [(Char, String)]
118:
         codeWords = let res = sortOn snd $ calcCodeWordDo calcWords
    in foldl' codeNext [] res
119:
120:
         codeNext [] (c,l) = [(c, replicate l '0')]
121:
122:
         codeNext xs@((\_,pr):\_) (c,l) =
             let -- generates next codeword after pr of length l
    nextWord = let pr' = dropEnd 1 $ dropWhileEnd (== '1') pr
123:
124:
                             in pr' ++ "1" ++ replicate (l - length pr' - 1) '0'
125:
126:
             in (c,nextWord):xs
         table1 = M.fromList $ map ((c,s) \rightarrow (c,(s,firstPass M.! c))) codeWords
127:
128:
129: runHuffman x = do
         let ((tbl1, str), tbl2) = runWriter $ getLogger $ huffman x
130.
         forM_ (M.assocs tbl1) print
forM_ tbl2 print
131:
132:
133:
134:
136: -- Adaptive arithmetic fixed precision
137: ----
138:
139: data ArithmState = ArithmState
                    :: Word16
140:
         { _aLow
         , _aHigh
                     :: Word16
141:
         , _aWord
142:
                     :: [Bool]
         , _aLetters :: [Word8]
143:
144:
           _aGLog
                     :: Double
         } deriving Show
145:
146:
147: makeLenses ''ArithmState
148:
149: data ArithmTrace = ArithmTrace
150:
        { aCurChar
                      :: [Char]
         , aProb
                       :: Rational
151:
         , aCodeWord :: String
152:
         , aMsgLength :: Int
153:
154:
155:
156: type ArithM a = StateT ArithmState (Writer [ArithmTrace]) a
158: instance Show ArithmTrace where
```

```
show ArithmTrace {..} =
159:
160:
             intercalate
161:
                  ["", aCurChar, show aProb, aCodeWord, show aMsgLength, ""]
162:
163:
164: convertToBits :: (Bits a) => a -> Int -> [Bool]
165: convertToBits x i = reverse $ map (\i -> testBit x i) [0 .. i-1]
166:
167: arithmStep :: Map Word8 Rational -> Word8 -> ArithM ()
168: arithmStep prob w = do
169:
         low <- use aLow
170:
         (delta :: Double) <- uses a High \$ from Integral . (\xspace x - \xspace x - \xspace w)
171:
         let member = M.member w prob
             letter = bool 0xff w member
172:
173:
             cast = fromRational . toRational
             p, p' :: Word16
174:
             p = round $
175:
176:
                  delta
                  M.foldrWithKey
177 •
178:
                      (\w' pr acc -> bool acc (acc + cast pr) (w' < letter))
                      0.0
179:
180:
                      prob
             p' = p + round (delta * cast (prob M.! letter))
181:
182:
             matches =
                  maximum $ 0:
183:
184:
                  filter
185:
                      (\in -> all (\j -> testBit p j == testBit p' j) [16-i .. 15])
186:
                      [1 .. 16]
187:
             sameBits = take matches $ convertToBits p 16
             low', high'
188:
                          :: Word16
             low' = shiftL p matches
189:
             high' | matches == 0 = p'
190:
191:
                    | otherwise = let s = shiftL p' matches
                                   in s . | . (s - 1)
192:
193: --
           traceShowM p
           traceShowM p
194: --
195: --
           traceShowM sameBits
196:
         aLow .= low
197:
         aHigh .= high
198:
         aWord <>= sameBits
         when member $ aLetters %= (letter:)
199:
200:
         l <- uses aWord length</pre>
          aGLog += (- (log2 (cast $ prob M.! letter))) \\ tell $ [ArithmTrace (chr' letter) (prob M.! letter) (map (bool '0' '1') sameBits) l] 
201:
202:
203:
         newLetters <- uses aLetters $ \letters -> filter (not . (`elem` letters)) [0..0xff]
204:
205:
         let probWithEscape =
206:
                  M.fromList $ map (\i -> (i, 1 / (fromIntegral $ length newLetters)))    newLetters
207:
         when (letter /= w) $ arithmStep probWithEscape w
208:
       where
         chr'
              0xff = "esc'
209:
         chr' x
210:
                   = [chr $ fromIntegral x]
211:
212: finalizeArith :: ArithM ()
213: finalizeArith = do
         high <- uses aHigh fromIntegral
214:
215:
         low <- uses aLow fromIntegral</pre>
         curL <- uses aWord length
216:
         let delta, deltaP ::
217:
             delta = high - low
218:
             deltaP = delta / 0xffff
219:
         bits <- uses aGLog $ \l ->
220:
             take (1 + (ceiling l) - curL) $
221:
             convertToBits @Word16 (round $ low + delta / 2) 16
222:
223:
         aWord <>= bits
224:
         l <- uses aWord length</pre>
         tell $ [ArithmTrace "final" 0 (map (bool '0' '1') bits) l]
225:
226:
227: runAdaptiveArithm :: ByteString -> ArithM ()
228: runAdaptiveArithm input = do
         forM_[0..BS.length input-1]  \k -> do
229:
             letters <- use aLetters
230:
             let n = fromIntegral $ length letters
231:
232:
                  probM = M.fromList $
233:
                      map (second (/(n+1))) $
234:
                      (0xff, 1):
235:
                      (map (\l -> (l, fromIntegral $ length $ filter (==l) letters)) $ nub letters)
236:
             arithmStep probM $ BS.index input k
237:
         finalizeArith
238:
239: execAdaptiveArithm x =
         runWriter $ (runStateT (runAdaptiveArithm x) (ArithmState 0 0xffff [] [] 0))
240:
```

```
242: ---
243: -- Enumerative
244: -----
245:
246: factorial :: Integer -> Integer
247: factorial 1 = 1
248: factorial 0 = 1
249: factorial x = x * factorial (x-1)
250:
251: enumerative :: BS.ByteString -> Integer
252: enumerative input = l1+l2
253:
      where
254:
        n = fromIntegral $ BS.length input
255:
         chars = BS.unpack input
         unique = nub chars
256:
257:
         occurences =
258:
             M.fromList $
             map (\i -> (i, fromIntegral $ length $ filter (== i) chars)) unique
259.
         comp, compcomp, comp' :: [Integer]
260:
261:
         comp = reverse $
262:
                sort $ map (\i -> fromMaybe 0 $ M.lookup i occurences) [0 .. 0xff]
         m = length comp
263:
264:
         compcomp = map (fromIntegral . length) $ group comp
         comp' = filter (> 0) comp
265:
266:
         l2 = ceiling $
              log2' $ foldr (\x acc -> acc `div` (factorial x)) (factorial n) comp'
267:
         l11 = ceiling $ log2' $ n * product comp'
268:
269:
         l12 = ceiling $
               log2'
270:
               foldr (\x acc -> acc `div` (factorial x))
271:
                      (factorial $ fromIntegral $ length comp)
272:
273:
                     compcomp
274:
         l1 = l11 + l12
275:
276:
277:
278: -- Universal coding
279: ------
280:
281: bin' :: Int -> [Bool]
282: bin' x = drop 1 $ dropWhile not $ convertToBits x 32
283:
284: unar :: Int -> [Bool]
285: unar n = replicate (n-1) True ++ [False]
286:
287: elias :: Int -> [Bool]
288: elias n = p1 + p2 + p3
      where
289:
290:
         p1 = unar $ 2 + length p2
        p2 = bin' $ length p3
p3 = bin' n
291:
292:
293:
294: mon :: Int -> [Bool]
295: mon n = p1 ++ p2
      where
296:
297:
        p1 = unar $ length p2 + 1
         p2 = bin' n
298:
299:
300: ----
301: -- LZ-77
302: -----
303:
304:
305: data LZ77State = LZ77State
        { _lzDict :: [Word8]
306:
            _lzWord :: [Bool]
307:
         } deriving Show
309:
310: makeLenses ''LZ77State
311:
312: data LZ77Trace = LZ77Trace
         { lzFlag
313:
                       :: Bool
314:
           lzCurString :: String
315:
         , lzDist
                       :: Maybe Int
         , lzLength
316:
                        :: Int
         , lzCodeWord
317:
                       :: [Bool]
318:
          lzBits
                       :: Int
319:
           lzMsgLength :: Int
320:
321:
322: instance Show LZ77Trace where
```

241:

```
show LZ77Trace {..} =
323:
324:
             intercalate
325:
                    ' '' ''
                  [
326:
                    showBool lzFlag
327:
                  , lzCurString
328:
                  , showMaybe lzDist
329:
                  , show lzLength
330:
                  , concatMap showBool lzCodeWord
                  , show lzBits
332:
                  , show lzMsgLength
333:
334:
335:
           where
336:
             showBool False = "0"
337:
338:
             showBool True = "1"
339:
             showMaybe Nothing
340:
             showMaybe (Just a) = show a
341:
342: type LZ77M a = StateT LZ77State (Writer [LZ77Trace]) a
343:
344: lz77Do :: (Int -> [Bool]) -> BS.ByteString -> Int -> Int -> LZ77M () 345: lz77Do uni input _ i | i >= BS.length input = pure ()
                         i | i >= BS.length input = pure ()
346: lz77Do uni input window i = do
         bestMatch <- uses lzDict workingInputs
347:
           traceShowM bestMatch
348: --
349: --
           traceShowM =<< uses lzDict (map (first fromWord8) . subwords)</pre>
         maybe onNewWord onMatch bestMatch
350:
351:
         stripDictionary
         lz77Do uni input window $ i + maybe 1 (length . fst) bestMatch
352:
353:
       where
354:
         onMatch (match,i) = do
355:
              let lzFlag = True
                  lzCurString = fromWord8 match
356:
                  lzLength = length match
357:
             lzDist <- uses lzDict $ \d -> length d - i
358:
359:
             dictSizeLog <
                  uses lzDict $ ceiling . log2' . (+1) . fromIntegral . length
360:
361: --
                traceShowM lzCurString
                traceShowM =<< uses lzDict length
362: --
363:
              let lzCodeWord =
364:
                      lzFlag
                      convertToBits lzDist dictSizeLog ++
365:
366:
                      uni lzLength
                  lzBits = length lzCodeWord
367:
             lzWord <>= (lzCodeWord)
368:
             lzMsqLength <- uses lzWord length</pre>
369:
370:
              tell $ [LZ77Trace {lzDist = Just lzDist,..}]
             lzDict <>= match
371:
372:
         onNewWord = do
             let lzCodeWord = lzFlag : convertToBits (fromJust $ head input') 8
373:
374:
                  lzFlag = False
                  lzCurString :: String
375:
                  lzCurString = fromWord8 $ take 1 input'
376:
377:
                  lzDist = Nothing
                  lzLength = 0
378:
                  lzBits = length lzCodeWord
379:
             lzWord <>= lzCodeWord
380:
              lzMsgLength <- uses lzWord length</pre>
381:
              tell $ [LZ77Trace {..}]
382:
              lzDict <>= [fromJust $ head input']
383:
         workingInputs :: [Word8] -> Maybe ([Word8], Int)
384:
385:
         workingInputs dict
386:
              let filtered = filter (\((pr, _) -> pr `isPrefixOf` input') $
387:
                      subwords dict
388:
             in bool (Just $ maximumBy (comparing (length . fst)) filtered)
389:
                      Nothing
390:
                      (null filtered)
         stripDictionary = do
391:
              l <- uses lzDict length</pre>
392:
             when (l > window) $ lzDict %= drop (l - window)
393:
         input' = BS.unpack $ BS.drop i input
394:
         tails' xs = dropEnd 1 (tails xs)
inits' xs = concatMap (\((str, i)\))
                                                    [0 ..]
395:
                                              `zip`
                                          i) -> drop 1 $ (,i) <$> inits str) xs
396:
397:
         subwords :: [a] -> [([a], Int)]
                                         . tails'
398:
         subwords = reverse . inits'
399:
400: lz77Encode :: (Int -> [Bool]) -> BS.ByteString -> Int -> LZ77M ()
401: lz77Encode uni bs w = lz77Do uni bs w 0
402:
403: execLz77 :: (Int -> [Bool]) -> ByteString -> Int -> (((), LZ77State), [LZ77Trace])
404: execLz77 u x w = runWriter $ (runStateT (lz77Encode u x w) (LZ77State [] []))
```

```
405:
406: lz770ther x = map ((u,w) -> (toUniS u, w, exec (toUni u) w)) testData
407:
        toUni 0 = unar
408:
409:
        toUni 1 = mon
410:
        toUni 2 = elias
        toUniS 0 = "Unary"
411:
        toUniS 1 = "Levenshtein"
412:
        toUniS 2 = "Elias"
413:
                              | \ uni <- \ [0..2], \ w <- \ [50,100,200,500,1000,2000,4000]]
        testData = [(uni, w)
414:
415:
        exec uni w = (execLz77 uni x w) ^. _1 . _2 . lzWord . to length
416:
417: -----
               ______
418: -- LZ78 (LZW)
419: -----
420:
421: data LzwState = LzwState
        { _lzwDict :: [[Word8]]
422:
           -
lzwWord :: [Bool]
423.
        } deriving Show
424:
425:
426: makeLenses ''LzwState
427:
428: data LzwTrace = LzwTrace
        { lzwNewWord
                      :: Maybe String
429:
                       :: String
430:
          lzwMatch
        , lzwWordId
                       :: Int
431:
        , lzwCodeWord :: [Bool]
432:
        , lzwBits
433:
                        :: Int
          lzwMsgLength :: Int
434:
435:
436:
437: instance Show LzwTrace where
        show LzwTrace {..} =
438:
439:
            intercalate
440:
                  ....
                [
441:
                , fromMaybe "" lzwNewWord
442:
443:
                , lzwMatch
                , show lzwWordId
444:
445:
                , concatMap showBool lzwCodeWord
                , show lzwBits
446:
447:
                  show lzwMsgLength
448:
449:
          where
450:
            showBool False = "0"
451:
            showBool True = "1"
452:
453:
454: type LzwM a = StateT LzwState (Writer [LzwTrace]) a
455:
456:
457: lzwDo :: BS.ByteString -> Int -> LzwM ()
458: lzwDo input i | i >= BS.length input = pure ()
459: lzwDo input i = do
        matchIndex <- uses lzwDict workingInputs</pre>
460:
        (match :: [Word8]) <- uses lzwDict (!! matchIndex)</pre>
461:
        let matchLen | match == [92] = 0
462:
                      otherwise = length match
463:
        dictSizeLog <-
464:
465:
            uses lzwDict $ ceiling . log2'
                                            . pred . fromIntegral . length
        let lzwCodeWord = convertToBits matchIndex dictSizeLog ++
466:
467:
                (if matchIndex == 0
468:
                 then convertToBits (fromJust $ head input') 8
469:
                 else [])
470:
            lzwBits = length $ lzwCodeWord
        lzwWord <>= lzwCodeWord
471:
472:
        let newWord = let w = take (matchLen + 1) input'
                      in bool (Just w) Nothing (w == match)
473:
            lzwNewWord = fromWord8 <$> newWord
474:
            lzwWordId = matchIndex
475:
            lzwMatch | match == [92] = ""
476:
                      | otherwise = fromWord8 match
477:
478:
        lzwMsgLength <- uses lzwWord length</pre>
479:
        whenJust newWord $ \w -> lzwDict <>= [w]
480:
        tell $ [LzwTrace{...}]
481:
        lzwDo input $ i + (bool (length match) 1 $ matchIndex == 0)
482:
483:
        workingInputs :: [[Word8]] -> Int
        workingInputs dict =
484:
485:
            fromMaybe 0 $
486:
            getLast $
```

```
487:
             mconcat $
488:
             map Last $
             map (\n -> findIndex (\w -> length w == n \&\& w `isPrefixOf` input') dict)
489:
                 [0..length dict-1]
490:
491:
         input' = BS.unpack $ BS.drop i input
492:
493: lzwEncode :: BS.ByteString -> LzwM ()
494: lzwEncode bs = lzwDo bs 0
495:
496: execLzw :: ByteString -> (((), LzwState), [LzwTrace])
497: execLzw x = runWriter $ (runStateT (lzwEncode x) (LzwState [BS.unpack "\\"] []))
498:
499: ------
500: -- PPMA
501: ------
502:
503: data PpmState = PpmState
         { _pLetters :: [Word8]
504:
                     :: Double
505.
            _pGLog
         } deriving Show
506:
507:
508: makeLenses ''PpmState
509:
510: data PpmTrace = PpmTrace
         { pCurChar
511:
                         :: Char
512:
         , pContextTimes :: [Int]
         , pContext
513:
                         :: [Char]
        , pEscProbs
514:
                         :: [Ratio Int]
515:
          pCharProb
                         :: Ratio Int
516:
517:
518: type PpmM a = StateT PpmState (Writer [PpmTrace]) a
519:
520: instance Show PpmTrace where
         show PpmTrace {..} =
521:
             intercalate
522:
                 "|"
[ ""
523:
524:
525:
                 , [pCurChar]
                 , bool (show pContext) "#" (null pContext)
526:
                 , intercalate "," (map show pContextTimes
, intercalate "," (map showRat pEscProbs)
527:
                                    (map show pContextTimes)
528:
529:
                   showRat pCharProb
530:
531:
           where showRat r = \text{show (numerator r)} ++ "/" ++ \text{show (denominator r)}
532:
533:
534: ppmCalculate :: Int -> ByteString -> Int -> PpmM ()
                    input i | i >= BS.length input = pure ()
535: ppmCalculate
536: ppmCalculate \overline{d} input i = do
537:
         history <- use pLetters
538:
         let c = BS.index input i
             maxD = min d (length history `div` 2)
539:
540 .
             startContext :: [Word8]
541:
             startContext
                 fromMaybe [] $ head $
542:
                 mapMaybe (\d' -> dropEnd 1 . view _2 <$>
543:
                                   head (findSubstring history $ takeEnd d' history)) $
544:
                 reverse [0..maxD]
545:
             -- Input: exceptions list (match <> c), string s
546:
547:
             -- Output: probability p_t(a|s), new exceptions
             calcProb :: [[Word8]] -> [Word8] -> (Ratio Int, [[Word8]])
548:
549:
             calcProb exs s
                 let \tau = filter (\( ,match, ) -> not (match `elem` exs)) $
550:
                          findSubstring (dropEnd (length s) history) s
551:
                 \tau sa = \text{filter ((== c) . view } \_3) \ \tau in (length \tau sa \% (length \tau + 1),
552:
553:
554:
                    concatMap (tails . view _2) τ)
555:
             calcEscProb :: [[Word8]] -> [Word8] -> Ratio Int
556:
             calcEscProb exs s
                 let \tau = filter (\(_, match,_) -> not (match `elem` exs)) $
557:
                          findSubstring (dropEnd (length s) history) s
558:
                 in 1 % (length \tau + 1)
559:
560:
             encodeEscapes probs ms exs s = do
                 let (prob, nextExc) = calcProb exs s
561:
562:
                     matchN = length $ findSubstring history s
                      probEsc = calcEscProb exs s
563:
                      probs' = probEsc:probs
564:
                     ms' = matchN:ms
565:
                     nonMetProb = 1 % (256 - (length $ nub $ history))
| prob /= 0 -> (probs,ms',prob)
566:
567:
                       length s > 0 -> encodeEscapes probs' ms' (nub \ exs++nextExc) \ drop 1 s
568:
```

```
| otherwise -> (probs',ms',nonMetProb)
569:
570:
             r@(probs,matchNs,prob) = encodeEscapes [] [] [] startContext
           traceM $ "MaxD: " <> show maxD
571: --
           traceM $ "Start context: " <> show (fromWord8 startContext)
572: --
573: --
           traceShowM r
574:
         tell [PpmTrace (chr $ fromIntegral c)
575:
                         (reverse matchNs)
                         (fromWord8 startContext)
576:
577:
                         (reverse probs)
578:
                         prob]
579:
         pLetters <>= [c]
         pGLog += (- (log2 (fromRational . toRational $ product probs * prob)))
580:
581:
         ppmCalculate d input $ i + 1
582:
583: -- | For a text and pattern it returns the list of matches -- index of
584: -- start and the next char after the match.
585: findSubstring :: (Eq a) => [a] -> [d] -> [(Int, [a], a)]
586: findSubstring t pat
         mapMaybe (\(i,m) -> guard (pat `isPrefixOf` m) >> pure (i, m, last m)) $
587 .
         map (second $ take l) $
588:
         filter ((>= l) . length . snd) $
[0..] `zip` tails t
589:
590:
       where
591:
592:
         l = length pat + 1
593:
594: execPpm :: Int -> ByteString -> (((), PpmState), [PpmTrace])
595: execPpm d x = runWriter $ (runStateT (ppmCalculate d x 0) (PpmState [] 0))
596:
597: ppmBytes p w = 1 + ceiling ( pGLog $ snd $ fst $ execPpm w p)
598:
600: -- Burrows-Wheeler
601:
602:
603: bwTransform :: (Show a, Ord a) => [a] -> ([a], Int)
604: bwTransform input = (lastCol, fromJust $ findIndex (==input) mapped)
605:
      where
         n = length input
606:
607:
         cycled = cycle input
         mapped = sort  map (\dot i \rightarrow take n \ drop i \ cycled) [0..n-1] 
608:
609:
         lastCol = map last mapped
610:
611: data MtfState = MtfState
         { _mtfLetters :: [Word8]
612:
            _mtfOutput :: [Bool]
613:
         } deriving Show
614:
615:
616: makeLenses ''MtfState
617:
618: data MtfTrace = MtfTrace
        { mtfCurChar
                       :: Char
619:
         , mtfNew
620:
                         :: Bool
         , mtfDist
                         :: Int
621:
        , mtfDiff
622:
                         :: Int
623:
        , mtfCodeWord :: [Bool]
                         :: Int
        , mtfBits
624:
625:
         , mtfMsgLength :: Int
         }
626:
627:
628: instance Show MtfTrace where
         show MtfTrace {..} =
629:
             intercalate
630:
                 <u>"</u>|""
631:
632:
                 , [mtfCurChar]
633:
                  , showBool mtfNew
634:
                 , show mtfDist
635:
636:
                 , show mtfDiff
                  , concatMap showBool mtfCodeWord
637:
                 , show mtfBits
638:
                  , show mtfMsgLength
639:
640:
641:
642:
           where
             showBool False = "0"
643:
             showBool True = "1"
644:
645:
646: type MtfM a = StateT MtfState (Writer [MtfTrace]) a
647:
648:
649: findIndexLast pred xs =
         (i \rightarrow length xs - i - 1) <$> (findIndex pred $ reverse xs)
650:
```

```
652: -- | MTF encoding, straight-forward
653: mtfEncode :: (Int -> [Bool]) -> ByteString -> Int -> MtfM ()
654: mtfEncode _ bs i | i >= BS.length bs = pure ()
655: mtfEncode u bs i = do
656:
         history <- use mtfLetters
         let c = BS.index bs i
657:
             mtfNew = not $ c `elem` history
658:
             foundIx = findIndexLast (== c) history
659:
             diffAbsent = (length $ nub history) + 256 - fromIntegral c
660:
             diffPresent i = length $ nub $ drop (i + 1) history
661:
             diff = maybe diffAbsent diffPresent foundIx
662:
663:
             distAbsent = length history + 256 - fromIntegral c
664:
             \mbox{dist} = \mbox{maybe distAbsent ($\setminus j$ -> $i$ - $j$ + 1) foundIx}
665:
             codeWord = u \$ diff + 1
         mtfOutput <>= codeWord
666:
         mtfLetters <>= [c]
667:
         mtfMsgLength <- uses mtfOutput length
668:
         tell [MtfTrace (chr $ fromIntegral c) mtfNew dist diff codeWord (length codeWord) mtfMsgLength]
669.
670:
         mtfEncode u bs $ succ i
671:
673: execMtf :: (Int -> [Bool]) -> ByteString -> (((), MtfState), [MtfTrace])
674: execMtf u bs = runWriter $ (runStateT (mtfEncode u bs 0) (MtfState [] []))
675:
676:
677:
678: data MtfSimpleState = MtfSimpleState
        { _mtfsLetters :: [Word8]
679:
           _mtfsOutput :: [Word8]
680:
         } deriving Show
681:
682:
683: makeLenses ''MtfSimpleState
684:
685: -- Just forms the string for encoding with enumerative later
686: mtfEncodeEsc :: [Word8] -> State MtfSimpleState ()
687: mtfEncodeEsc [] = pure ()
688: mtfEncodeEsc (c:xs) = do
689:
         history <- use mtfsLetters
690:
         let foundIx = findIndexLast (== c) history
             diffAbsent = fromIntegral $ ord '\\'
691:
             diffPresent i = fromIntegral $ length $ nub $ drop (i + 1) history
692:
             diff :: Word8
693:
694:
             diff = maybe diffAbsent diffPresent foundIx
         mtfsOutput <>= [diff]
695:
         mtfsLetters <>= [c]
696:
         mtfEncodeEsc xs
697:
698:
699: runMtfs bs = execState (mtfEncodeEsc $ BS.unpack bs) $ MtfSimpleState [] []
700:
701: ---
702: -- Zlib/Gzip
703: ---
704:
705: gzipCompress :: ByteString -> ByteString
706: gzipCompress =
707:
         BSL.toStrict
708:
         Z.compressWith
709:
             (Z.defaultCompressParams
              { compressLevel = Z.bestCompression
710:
711:
                compressMemoryLevel = Z.maxMemoryLevel
              })
712:
713:
         BSL.fromStrict
```

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Validate