

One-dimensional tracking (Section 11.1)

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In this example we show the phase-space plot of a ring where a single sextupole provides the non-linearity that is defined by Equation 11.3. We follow particles with increasing initial values for 1024 iterations and plot a dot at their phase-space coordinate after every iteration.

We first define the number of turns to follow and provide a selection of tunes Q to choose from and a slider to set the offset dx . Then we define the transfer matrix, which is just a rotation matrix with phase advance given by $2\pi Q$.

```
clear all;
Nturn=1024;
Qstr="0.2526";           % select tune
Q=str2double(Qstr)
```

```
Q = 0.2526
```

```
dx=0           % misalignment
```

```
dx = 0
```

```
R=@(mu)[cos(mu),sin(mu);-sin(mu),cos(mu)];
RR=R(2*pi*Q);
clf
```

With the preliminaries defined, we set the scale of the axes and loop over initial starting values x_0 .

```
hold on
axis([-1.2,1.2,-1.2,1.2]);
title(['Q = ',num2str(Q,4),',    dx = ',num2str(dx,2)]);
for x0=0.05:0.05:2
```

For each starting value we allocate an array data to hold the phase-space coordinates after each iteration and set the start coordinate, before iterating N_{turn} times. In each iteration we apply Equation 11.3 and store the coordinate in data. If the coordinate is larger than 3, we break the iteration.

```
data=zeros(2,Nturn);
x=[x0;0];           % start coordinates
for n=1:Nturn
    x=RR*[x(1);x(2)-(x(1)-dx)^2];
    if (abs(x(1))>3) break; end
    data(:,n)=x;
end
```

And finally we display the phase-space points as a black dot and give MATLAB a little time to update the display and annotate the axes.

```
plot(data(1,1:n),data(2,1:n),'k.')  
pause(0.001)  
end  
xlabel('x'); ylabel('x''')
```

