

Vacuum calculations (Section 13.5.3)

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Here we describe a minimal version of the vacuum calculation code `vaktrak`, discussed in

- Volker Ziemann, *Vacuum tracking*, SLAC-PUB-5962, 1992.

It determines the longitudinal profile of the pressure and gasflow along a linear vacuum system in the regime of conduction limited flow. Such a vacuum system of n elements is defined by a $n \times 6$ array, where the first column contains a code, describing the type of element, the second element contains a repeat-code for that element, and the next four entries are related to the length, conductance c or C , pump speed s or S , and outgassing rate q of the respective element. Here is a short summary, but check out the details in Section 13.5.3.

supported codes with ordering: CODE,repeat,L,c,s,q

Conductance only: 1, rep, L, c, 0, 0

Short pump: 2, 1, 0, 0, S, 0

Short gas source: 3, 1, 0, 0, 0, dQ

Generic element: 4, rep, L, c, s, q

Larger systems can be assembled from short sections with `repmat()` and `flip()`.

We start the simulation by defining functions that return the 3×3 matrices for the conductance, a short pump, and a short gas source.

```
clear all; close all
conduc=@(C)[1,-1/C,0; 0,1,0; 0,0,1]; % matrix for conductance
pump=@(S)[1,0,0;-S,1,0;0,0,1];      % matrix for short pump
outgas=@(dQ)[1,0,0;0,1,dQ;0,0,1];    % matrix for gas source, leak
```

Now we define a section `vaksys` of our vacuum system, defined by a localized outgassing source (code=3), a pipe, made of 100 segments, 10 cm long each, and a short pump with a pump pseed of 100 l/s.

```
vaksys=[ 3,      1,      0,      0,      0,      1e-6; % outgas, dQ
         1,     100,     0.1,     10,      0,      0;   % conductance, c
         2,      1,      0,      0,     100,      0] % pump, S
```

```
vaksys = 3x6
    3.0000    1.0000         0         0         0    0.0000
    1.0000   100.0000    0.1000   10.0000         0         0
    2.0000    1.0000         0         0   100.0000         0
```

The vacuum system `v` consists of two sections `vaksys` of which the second one is traversed in the reverse order. Finally we repeat this system 2 times and call the entire system `beamline`, just as we did for the beam optical systems in Chapter 3.

```
v=[vaksys; flip(vaksys,1)];
beamline=repmat(v,2,1)           % description of the complete system
```

```
beamline = 12x6
    3.0000    1.0000         0         0         0    0.0000
    1.0000   100.0000    0.1000   10.0000         0         0
    2.0000    1.0000         0         0   100.0000         0
    2.0000    1.0000         0         0   100.0000         0
    1.0000   100.0000    0.1000   10.0000         0         0
    3.0000    1.0000         0         0         0    0.0000
    3.0000    1.0000         0         0         0    0.0000
    1.0000   100.0000    0.1000   10.0000         0         0
    2.0000    1.0000         0         0   100.0000         0
    2.0000    1.0000         0         0   100.0000         0
    :
    :
```

The following lines are needed for accounting purposes: `nlines` are the number of lines in the beamline, `nmat` is the number of matrices and `Racc` will be filled with all the transfer matrices from the start of the system to the end of each segment, while `spos` keeps track of the longitudinal position of segments.

```
nlines=size(beamline,1);           % number of elements in beamline
nmat=sum(beamline(:,2))+1;          % number of matrices, incl repeat count
Racc=zeros(3,3,nmat);              % accumulated transfer matrices
Racc(:,:,1)=eye(3);                 % initialize the first one
spos=zeros(nmat,1);                 % array for element (end-)positions
```

In the next snippet we loop over all lines in the beamline and then over all segments and then assign `Rcurr` to the 3×3 matrix for the appropriate element (as specified by the code in the first column of beamline). After these loops, we left-multiply `Rcurr` to the transfer matrix up to the previous element `Racc(:,:,ic-1)` and update `spos`. Finally we give the transfer matrix that takes us to the end the name `R0`.

```
ic=1;
for line=1:nlines                    % loop over elements
    for seg=1:beamline(line,2)      % and over the segments of each element
        ic=ic+1;                    % element counter
        Rcurr=eye(3);                % initialize to unit matrix
        switch beamline(line,1)     % brach according to element
            case 1                    % pure conductance
                C=beamline(line,4)/beamline(line,3); % C=c/L
                Rcurr=conduc(C);      % large C
            case 2                    % short pump, zero length
                Rcurr=pump(beamline(line,5));      % large S
            case 3                    % point-like gas source, zero length
                Rcurr=outgas(beamline(line,6));    % large dQ
            case 4                    % generic element, c,s,q,L are all given
                Rcurr=csqL(beamline(line,4),beamline(line,5),...
                    beamline(line,6),beamline(line,3));
            otherwise
                disp('unsupported code')
        end
        Racc(:,:,ic)=Rcurr*Racc(:,:,ic-1); % add new element
        spos(ic)=spos(ic-1)+beamline(line,3); % update the position
    end
end
```

```

end
R0=Racc(:, :, end); % alias for the start-to-end matrix

```

If we assume that the entire system is flanged off at the ends (gasflow: $Q_l=Q_r=0$), we can find the equilibrium pressure on the left end P_l and at the right end P_r from R_0 . From this we construct the 3×1 vector with the initial condition P_{0r} and propagate it through the vacuum system in the loop over k .

```

Pr=-R0(2,3)/R0(2,1);
Pl=R0(1,3)-R0(1,1)*R0(2,3)/R0(2,1);
P0r=[Pr;0;1]; % vector at start
pressure=zeros(nmat,1); gasflow=pressure; % allocate memory
for k=1:nmat % loop over all elements
    PP=Racc(:, :, k)*P0r; % and calculate [P;Q;1] at end of each element
    pressure(k)=PP(1); % stuff into arrays used for plotting
    gasflow(k)=PP(2);
end

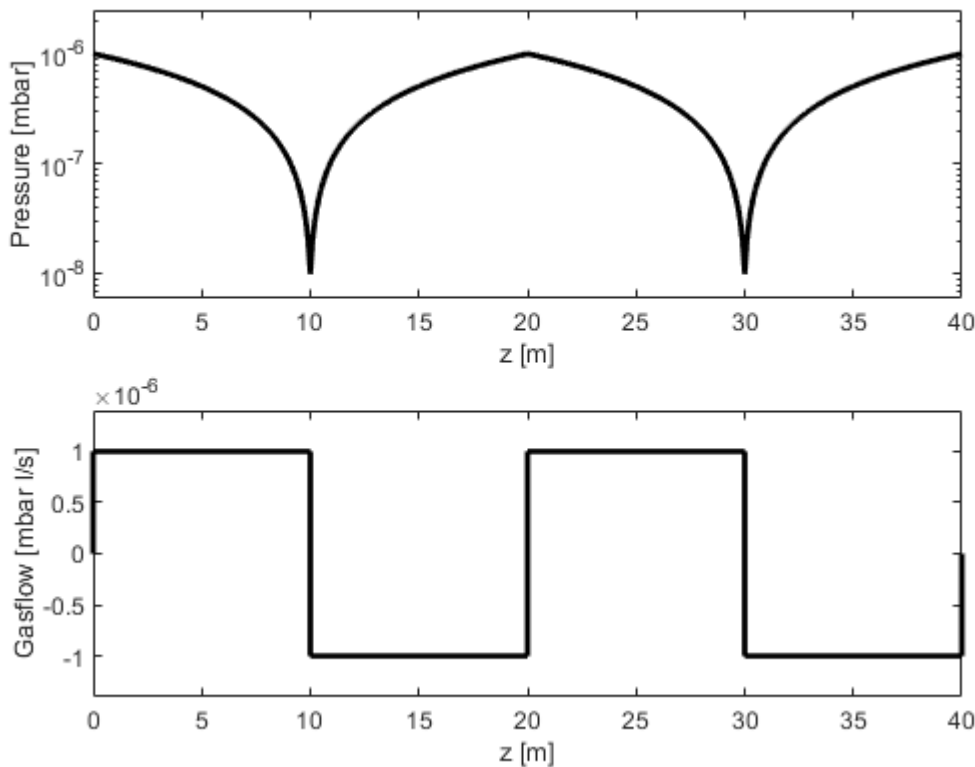
```

At this point we are ready to display the pressure profile along our vacuum system in the top plot and the corresponding gas flow in the bottom plot.

```

subplot(2,1,1); semilogy(spos,pressure,'k','LineWidth',2);
xlim([0,spos(end)]); ylim([0.6*min(pressure),2.5*max(pressure)])
xlabel('z [m]'); ylabel('Pressure [mbar]');
subplot(2,1,2); plot(spos,gasflow,'k','LineWidth',2);
xlim([0,spos(end)]); ylim([1.4*min(gasflow),1.4*max(gasflow)])
xlabel('z [m]'); ylabel('Gasflow [mbar l/s]')

```



Now define your own vacuum system and simulate it.

Appendix

here we define a function `csql()` that receives the per-meter conductance c , the per-meter pump speed s , the per-meter outgassing q , and the length L of an element and returns the transfer matrix from Equation 13.3.

```
function R=csql(c,s,q,L)
R=eye(3);
sq=sqrt(s/c); cc=cosh(sq*L); ss=sinh(sq*L);
R(1,1)=cc;
R(1,2)=-ss/(c*sq);
R(1,3)=-q*(cc-1)/s;
R(2,1)=-c*sq*ss;
R(2,2)=cc;
R(2,3)=q*ss/sq;
end
```