#### **Answer Key to**

# **SMC IMONST Workshop 2024**

(Day 1: Combinatorics)

# §1 Introductory Problems

| 1) | 7    | 6)  | 36    |
|----|------|-----|-------|
| 2) | 2084 | 7)  | 12    |
| 3) | 24   | 8)  | 1156  |
| 4) | 11   | 9)  | 55440 |
| 5) | 20   | 10) | 5     |

# **§2** Pigeonhole Principle

Exercise 2.6 8

**Exercise 2.7** 62

# §3 Principle of Inclusion-Exclusion

**Exercise 3.3** 33\*

#### §4 Permutations and Combinations

Exercise 4.7 36\*\*

**Exercise 4.8** 10

**Exercise 4.9** 1287

**Exercise 4.10 1.** 729 **2.** 122 **3.** 28\*\*\* **4.** 7

#### §5 Bonus Problems

| 1) | 1232 | 7)  | 14   | 13) | 43251 | 19) | 16  | 25) | 55      |
|----|------|-----|------|-----|-------|-----|-----|-----|---------|
| 2) | 63   | 8)  | 16   | 14) | 6     | 20) | 30  | 26) | 7       |
| 3) | 64   | 9)  | 3456 | 15) | 4464  | 21) | 30  | 27) | 21      |
| 4) | 198  | 10) | 216  | 16) | 30    | 22) | 0   | 28) | 1020100 |
| 5) | 10   | 11) | 60   | 17) | 1725  | 23) | 624 | 29) | 3840    |
| 6) | 15   | 12) | 56   | 18) | -     | 24) | 5   |     |         |

- \*The phrase "...8 takes German, 10 takes both..." in the original problem has been changed to "...8 takes German only, 10 takes both..." in the updated version of the handout.
- \*\*The problem originally referring to 4-tuples has been changed to 3-tuples to match the rest of the problem description.
- \*\*\*has been changed from "indistinguishable urns" to "distinguishable urns" due to duplicate question