

# Automata 2/2



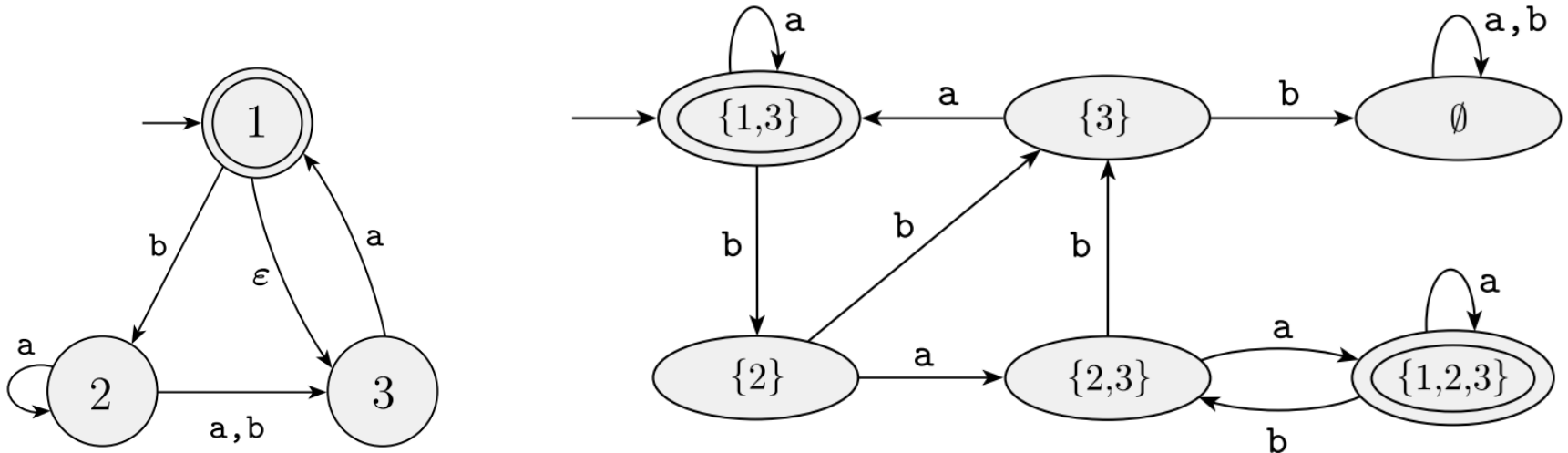
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Online lecture

# Equivalence

## Property:

Every non-deterministic automaton has an equivalent deterministic automaton and vice versa.

## Ex:



# Regular languages

## Definition:

An automaton  $M$  **recognizes** a language  $L$  if  $M$  accepts all strings in  $L$ . A language  $L$  is a **regular language** if there is a finite automaton  $M$  recognizes it.

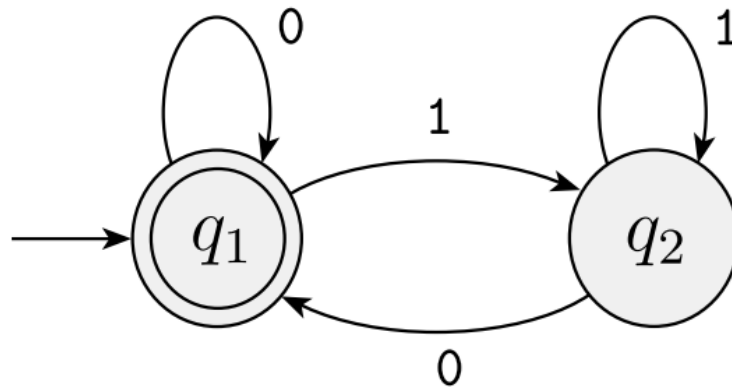
## Property:

If  $A$  and  $B$  are two regular languages, so do

- **Union:**  $A \cup B = \{x \mid x \in A \text{ or } x \in B\}$ .
- **Concatenation:**  $A \circ B = \{xy \mid x \in A \text{ and } y \in B\}$ .
- **Star:**  $A^* = \{x_1x_2 \dots x_k \mid k \geq 0 \text{ and each } x_i \in A\}$ .

# Regular languages

Ex:



$L(M) := \{ w \mid w \text{ is the empty string or ends with } 0 \}$

# Regular expressions

## Definition:

Say that  $R$  is a *regular expression* if  $R$  is

1.  $a$  for some  $a$  in the alphabet  $\Sigma$ ,
2.  $\epsilon$ ,
3.  $\emptyset$ ,
4.  $(R_1 \cup R_2)$ , where  $R_1$  and  $R_2$  are regular expressions,
5.  $(R_1 \circ R_2)$ , where  $R_1$  and  $R_2$  are regular expressions, or
6.  $(R_1^*)$ , where  $R_1$  is a regular expression.

# Regular expressions

Ex:

In the following instances, we assume that the alphabet  $\Sigma$  is  $\{0,1\}$ .

1.  $0^*10^* = \{w \mid w \text{ contains a single } 1\}$ .
2.  $\Sigma^*1\Sigma^* = \{w \mid w \text{ has at least one } 1\}$ .
3.  $\Sigma^*001\Sigma^* = \{w \mid w \text{ contains the string } 001 \text{ as a substring}\}$ .

# Regular expressions

## Property:

Any regular language can be described by a regular expression and vice versa. Thus a regular expression is equivalent to a finite automaton.

## Ex:

