Indian Statistical Institute

BSDS Ist Year

Academic Year 2024 - 2025: Semester I

Course: Probability Theory I

Instructor: Antar Bandyopadhyay

Assignment #4

Date Given: September 11, 2024 Date Due: September 19, 2024 Total Points: 10

- **3.1.4** In a World Series, teams A and B play until one team has won four games. Assume that each game played is won by team A with probability p, independently of all previous games.
 - (a) For g=4 through 7, find a formula in terms of p and q=1-p for the probability that team A wins in q games.
 - (b) What is the probability that team A wins the World Series, in terms of p and q?
 - (c) Use your formula to evaluate this probability for p = 1/2 and p = 2/3.
 - (d) Let X be a Binomial (7, p) random variable. Explain why $\mathbf{P}(A \text{wins}) = \mathbf{P}(X \ge 4)$ using an intuitive argument. Verify algebraically that this is true.
 - (e) Let G represent the number of games played. What is the distribution of G?
- **3.4.14** In independent repetation of a Bernoulli(p) trials let V_n be the number of trials required to produce either n successes or n failures, whichever comes first. Find the distribution of V_n .

3.6.2 A deck of standard 52 cards is shuffled and dealt. Find the probabilities of the following events and give reasons supporting your answers

(a) the tenth card is a queen;

(b) the twentieth card is a spade;

(c) the last five cards are spades;

(d) The last king appears on the 48-th card.

2.2.10 A probability class has 30 students. As part of an assignment, each student tosses an unbiased coin 200 times and records the number of heads. What is the chance that no student gets exactly 100 heads? Write a formula and give reasons behind your answer. Can you use R-programming to give an approximation of what the value is?

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