

## Chapter 9

# MONTE CARLO SIMULATIONS OF LOCALIZED TRANSITIONS

### AUTHOR'S NOTE:

Please note that the BOOK BIBLIOGRAPHY was updated on February 14, 2022 to include this citation to the *lamW* R-package [1]:

Avraham Adler (2015) . lamW: Lambert-W Function, 2015. URL <https://CRAN.R-project.org/package=lamW>. R package version 2.1.1.

**Abstract** In this chapter we discuss fixed time interval MC simulations of luminescence signals produced by localized transitions in the TLT and LT models. Examples of R codes are provided for TL, CW-IRSL and LM-IRSL signals in the excited state tunneling (EST) model, and the MC results are compared with the analytical Kitis-Pagonis equations (KP-CW, KP-TL). The R codes also provide estimates for the stochastic coefficients of variation CV% for a variety of processes. This chapter concludes with a MC simulation for the LT model.

---

### Code 9.1: Vectorized MC code for tunneling TL transitions (TLT model)

```
# Vectorized MC code for tunneling transitions (TLT model)
# Original Mathematica program by Vasilis Pagonis
# R version written by Johannes Friedrich, 2018
rm(list = ls(all=T))
rho <- 5e-3
En<-1.43
s<-3.5e12
kB<-8.617e-5
deltat <- 1
```

```

times <- seq(0, 500, deltat)
# In this example time =temperature, i.e. a heating rate=1 K/s
r <- seq(0, 2, 0.1)
clusters <- 20
n0<-100
signal<-array(0,dim=c(length(times),
  ncol = length(r), clusters))
# Run MC simulation
system.time(invisible(for(c in 1:clusters)
{
  for(k in 1:length(r)){
    n <- n0
    for (t in 1:length(times)){
      P <- s*exp(-En/(kB*(t+273)))*exp(-rho^(-1/3) * r[k])
      vec<-rep(runif(n))
      n<-length(vec[vec>P*deltat])
      signal[t,k,c] <- n * P * 3 * r[k]^2 * exp(-r[k]^3) }}})
})
par(mfrow=c(1,2))
# plot an example : the result from the first cluster
matplot(signal[,1],type = "l",lty="solid",
ylab = "Partial TL glow curves for constant(r')",
ylim=c(0,3.2),xlab=expression("Temperature ["^o"C]"),lwd = 2)
legend("topleft",bty="n",legend=c("(a)", " ", "Partial TL",
"glow curves"))
#add the signals from all clusters
sum_signal <- sapply(1:clusters, function(y){
  vapply(1:length(times), function(x){
    sum(signal[x,y])
  }, FUN.VALUE = 1) })
# add the signals from all r values
TL <- rowMeans(sum_signal)
# plot and normalize the TL signal
plot( x = times, y = TL/max(TL),type = "l", lwd = 3,
ylim=c(0,1.6), xlab=expression("Temperature ["^o"C]"),
ylab="Average TL signal")
legend("topleft",bty="n",legend=c("(b)", " ",
"Sum of partial TL","glow curves"))
## plot analytical solution Kitis-Pagonis
z<-1.8
T<-times+273
TLanalyt<-exp(-rho*( (log(1+z*s*kB*((T**2.0)/
abs(En))*exp(-En/(kB*T))*(1-2*kB*T/En))**3.0))*
(En**2.0-6*(kB**2.0)*(T**2.0))*( (log(1+z*s*kB*((T**2.0)/

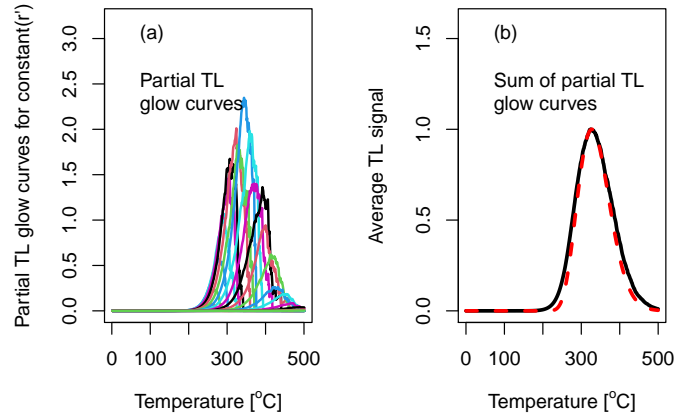
```

```

abs(En))*exp(-En/(kB*T))*(1-2*kB*T/En))**2.0)/
(En*kB*s*(T**2)*z-2*(kB**2.0)*s*z*(T**3.0)+
exp(En/(kB*T))*En)
lines(times,TLanalyt/max(TLanalyt),lty="dashed",col="red",
lwd=3)

##      user  system elapsed
##      1.63    0.00    1.62

```



**Fig. 9.1:** MC simulation of TL signals in the TLT model, for the parameters  $\rho' = 5 \times 10^{-3}$ ,  $M = 20$  MC runs,  $n_0 = 100$  initially trapped electrons,  $E = 1.43$  eV,  $s = 3.5 \times 10^{13} \text{ s}^{-1}$ . (a) Example of partial TL glow curves evaluated for each distance  $r'$ . (b) The sum of the partial TL glow curves from (a), normalized to its maximum. The dashed line in (b) represents the approximate analytical KP-TL equation from Chapter 6, also normalized to its maximum value.

---

**Code 9.2: Vectorized MC code for tunneling CW-IRSL transitions (TLT model)**

```

# Vectorized MC code for tunneling transitions (TLT model)
# Original Mathematica program by Vasilis Pagonis
# R version written by Johannes Friedrich, 2018
rm(list = ls(all=T))
rho <- 5e-3

```

```

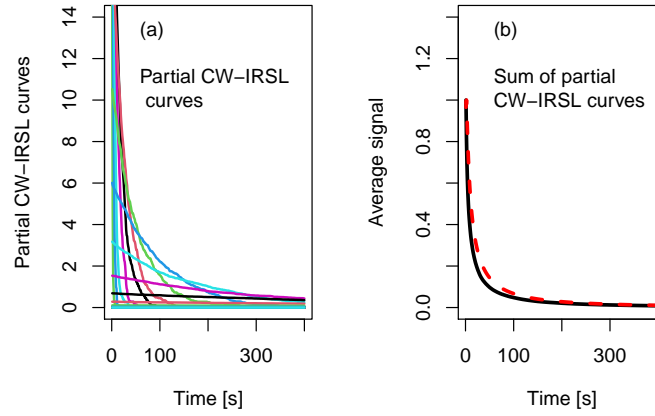
A<-2
deltat <- 1
times <- seq(1, 400, deltat)
# In this example time =temperature, i.e. a heating rate=1 K/s
r <- seq(0, 2.2, 0.1)
clusters <- 10
n0<-500
signal<-array(0,dim=c(length(times),
                      ncol = length(r), clusters))

# Run MC simulation
system.time(invisible(for(c in 1:clusters)
{
  for(k in 1:length(r)){
    n <- n0
    for (t in 1:length(times)){
      P <- A*exp(-rho^(-1/3) * r[k])
      vec<-rep(runif(n))
      n<-length(vec[vec>P*deltat])
      signal[t,k,c] <- n * P * 3 * r[k]^2 * exp(-r[k]^3) }}})
})
par(mfrow=c(1,2))
# plot an example : the result from the first cluster
matplot(signal[,1],type = "l",lty="solid",
ylab = "Partial CW-IRSL curves",
ylim=c(0,14),xlab=expression("Time [s]"),lwd = 2)
legend("topleft",bty="n",legend=c("(a)", " ", "Partial CW-IRSL",
" curves"))
#add the signals from all clusters
sum_signal <- sapply(1:clusters, function(y){
  vapply(1:length(times), function(x){
    sum(signal[x,,y])
  }, FUN.VALUE = 1) })
# add the signals from all r values
TL <- rowMeans(sum_signal)
# plot and normalize the TL signal
plot( x = times, y = TL/max(TL),type = "l", lwd = 3,
ylim=c(0,1.4), xlab=expression("Time [s]"),
      ylab="Average signal")
legend("topleft",bty="n",legend=c("(b)", " ",
"Sum of partial", "CW-IRSL curves"))
## plot analytical solution Kitis-Pagonis
z<-1.8
CWanalyt<-exp(-rho*( (log(1+z*A*times))**3.0))*
( (log(1+z*A*times))**2.0)/(1+z*A*times)

```

```
lines(times,CWanalyt/max(CWanalyt),lty="dashed",col="red",lwd=3)
```

```
##      user  system elapsed
##      1.40    0.00    1.41
```



**Fig. 9.2:** MC simulation of CW-IRSL signals in the TLT model, for the parameters  $\rho' = 5 \times 10^{-3}$ ,  $M = 10$  MC runs,  $n_0 = 500$  initially trapped electrons, and IR excitation rate  $A = 2 \text{ s}^{-1}$ . (a) Example of partial CW-IRSL curves evaluated for each distance  $r'$ . (b) The sum of the partial CW-IRSL curves from (a), normalized to its maximum. The dashed line in (b) represents the approximate analytical KP-CW equation from Chapter 6, also normalized to its maximum value (kitis and Pagonis [46]).

---

**Code 9.3: Vectorized MC code for tunneling LM-IRSL transitions (TLT model)**

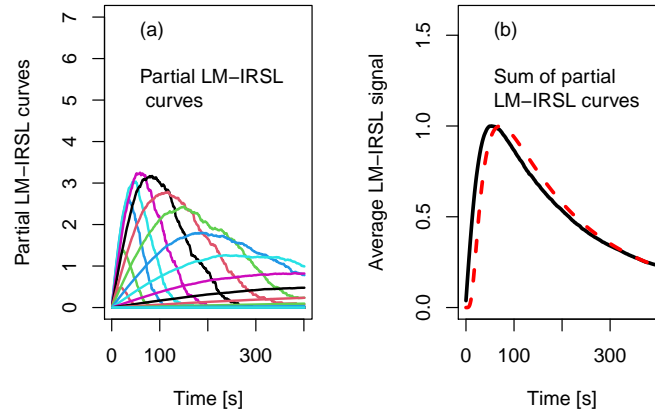
```
# Vectorized MC code for tunneling transitions (TLT model)
# Original Mathematica program by Vasilis Pagonis
# R version written by Johannes Friedrich, 2018
rm(list = ls(all=T))
rho <- 5e-3
A<-2          # IR excitation rate in s^-1
deltat <- 1
times <- seq(0, 400, deltat)
r <- seq(0, 2.2, 0.1)
```

```

clusters <- 10
n0<-500
signal<-array(0,dim=c(length(times),
ncol = length(r), clusters))
# Run MC simulation
system.time(invisible(for(c in 1:clusters)
{ for(k in 1:length(r)){
  n <- n0
  for (t in 1:length(times)){
    P <- A*t/max(times)*exp(-rho^(-1/3) * r[k])
    vec<-rep(runif(n))
    n<-length(vec[vec>P*deltat])
    signal[t,k,c] <- n * P * 3 * r[k]^2 * exp(-r[k]^3) }}}}
par(mfrow=c(1,2))
# plot an example : the result from the first cluster
matplot(signal[,1],type = "l",lty="solid",
ylab = "Partial LM-IRSL curves",
ylim=c(0,7),xlab=expression("Time [s]"),lwd = 2)
legend("topleft",bty="n",legend=c("(a)", " ", "Partial LM-IRSL",
" curves"))
#add the signals from all clusters
sum_signal <- sapply(1:clusters, function(y){
  vapply(1:length(times), function(x){
    sum(signal[x,,y])
  }, FUN.VALUE = 1) })
# add the signals from all r values
TL <- rowMeans(sum_signal)
# plot and normalize the TL signal
plot( x = times, y = TL/max(TL),type = "l", lwd = 3,
ylim=c(0,1.6), xlab=expression("Time [s]"),
ylab="Average LM-IRSL signal")
legend("topleft",bty="n",legend=c("(b)", " ",
"Sum of partial", "LM-IRSL curves"))
## plot analytical solution Kitis-Pagonis
z<-1.8
LManalyt<-exp(-rho*( (log(1+z*A*times^2/(2*max(times))))**3.0))*
times*((log(1+z*A*times^2/(2*max(times))))**2.0)/(1+z*A*times^2/
(2*max(times))))
lines(times,LManalyt/max(LManalyt),lty="dashed",col="red",lwd=3)

##      user  system elapsed
##      1.84    0.00    1.84

```



**Fig. 9.3:** MC simulation of LM-IRSL signals in the TLT model, for the parameters  $\rho' = 5 \times 10^{-3}$ ,  $M = 10$  MC runs,  $n_0 = 100$  initially trapped electrons,  $A = 2 \text{ s}^{-1}$ . (a) Example of partial LM-IRSL curves evaluated for each distance  $r'$ ; (b) The sum of the partial LM-IRSL curves from (a), normalized to its maximum. The dashed line in (b) represents the approximate analytical equation by Kitis and Pagonis [46], also normalized to its maximum value.

---

**Code 9.4: Vectorized MC code for TL in localized TL transitions (LT model)**

```
# Vectorized MC code for localized TL transitions (LT model)
rm(list = ls(all=T))
options(warn=-1)
library(matrixStats)
library(lamW)
mcruns<-100
n0<-500
s<-1e13
E<-1
kb<-8.617e-5
r<-1e2
tmax<-120
deltat<-1
times<-seq(1,tmax,deltat) #heating rate=1 K/s
nMatrix<-TLMatrix<-matrix(NA,nrow=length(times),ncol=mcruns)
nMC<-TL<-rep(NA,length(times))
```

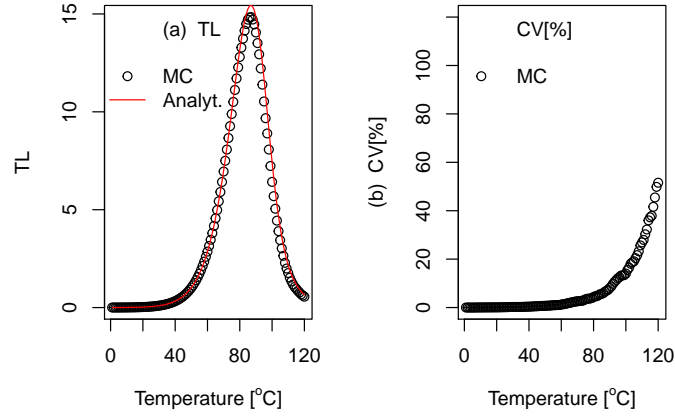
```

system.time(
  for (j in 1:mcruns){
    n<-n0
    for (t in 1:length(times)){
      vec<-rep(runif(n))
      P<-s*exp(-E/(kb*(t+273)))*n/(r+n)*deltat
      n<-length(vec[vec>P])
      nMC[t]<-n
      TL[t]<-nMC[t]*P}
    nMatrix[,j]<-nMC
    TLMatrix[,j]<-TL }
  #Find average avgn, average TL signal,CV[%]
  avgn<-rowMeans(nMatrix)
  avgTL<-rowMeans(TLMatrix)
  sd<-rowSds(TLMatrix)
  cv<-100*sd/avgTL
  # plots
  par(mfrow=c(1,2))
  pch<-c(NA,NA,1,NA)
  lty<-c(NA,NA,NA,"solid")
  col<-c(NA,NA,"black","red")
  plot(times,avgTL,ylab="TL",
        xlab=expression("Temperature ["^o"C"]))
  # plot analytical solution
  k<-function(u) {integrate(function(p){exp(-E/(kb*p))},
    300,u)[[1]]}
  y1<-lapply(times+273,k)
  x<-unlist(273+times)
  y<-unlist(y1)
  zTL<-(r/n0)-log(n0/r)+(s*y)
  lines(x-273,r*s*exp(-E/(kb*x))/(lambertW0(exp(zTL))
    +lambertW0(exp(zTL))^2),type="l",col="red")
  legend("topleft",bty="n",c("(a)  TL", " ", "MC",
    "Analyt."),pch=pch,lty=lty,col=col)
  plot(times,cv,ylab="(b)  CV[%]",ylim=c(0,120),
        xlab=expression("Temperature ["^o"C"]))
  legend("topleft",bty="n",c("CV[%]", " ", "MC"),
    pch=pch,lty=lty,col=col)

  ##      user  system elapsed
  ##      0.27    0.00    0.27

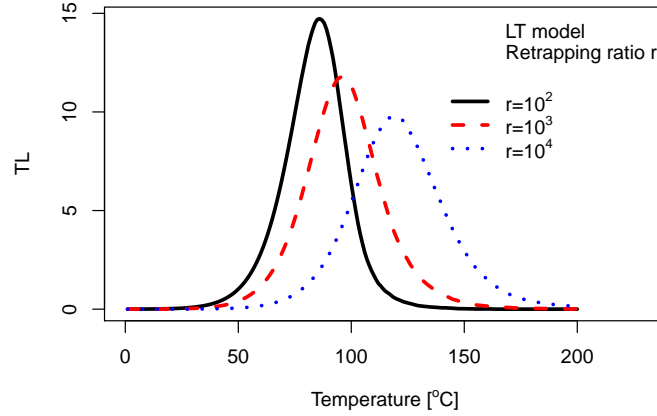
```





**Fig. 9.4:** (a) MC simulation of TL signals in the LT model, for the parameters  $r = 10^2$ ,  $M = 100$  MC runs,  $n_0 = 500$ ,  $E = 1$  eV,  $s = 10^{13} \text{ s}^{-1}$ . The solid line is the analytical solution by Kitis and Pagonis [46]. (b) The corresponding coefficient of variation  $CV[\%]$ .

retrapping ratio  $r = 10^2, 10^3, 10^4$ .



**Fig. 9.5:** MC simulation of TL signals in the LT model, for three different values of the retrapping ratio  $r = 10^2, 10^3, 10^4 \text{ cm}^{-3}$ .



# References

1. A. Adler, *lamW: Lambert-W Function* (2015). DOI 10.5281/zenodo.5874874. URL <https://CRAN.R-project.org/package=lamW>. R package version 2.1.1
2. G. Kitis, V. Pagonis, H. Carty, E. Tatsis, *Radiation protection dosimetry* **100**(1-4), 225 (2002)
3. V. Pagonis, N. Brown, G.S. Polymeris, G. Kitis, *Journal of Luminescence* **213**, 334 (2019). DOI <https://doi.org/10.1016/j.jlumin.2019.05.044>. URL <http://www.sciencedirect.com/science/article/pii/S0022231319306519>
4. G. Kitis, G.S. Polymeris, I.K. Sfampa, M. Prokic, N. Meriç, V. Pagonis, *Radiation Measurements* **84**, 15 (2016). DOI <https://doi.org/10.1016/j.radmeas.2015.11.002>. URL <http://www.sciencedirect.com/science/article/pii/S1350448715300731>
5. R.M. Bailey, *Radiation Measurements* **33**(1), 17 (2001)
6. V. Pagonis, C. Ankjærgaard, M. Jain, R. Chen, *Journal of Luminescence* **136**, 270 (2013)
7. V. Pagonis, J. Friedrich, M. Discher, A. Müller-Kirschbaum, V. Schlosser, S. Kreutzer, R. Chen, C. Schmidt, *Journal of Luminescence* **207**, 266 (2019). DOI <https://doi.org/10.1016/j.jlumin.2018.11.024>. URL <http://www.sciencedirect.com/science/article/pii/S0022231318317368>
8. G. Kitis, G.S. Polymeris, E. Sahiner, N. Meric, V. Pagonis, *Journal of Luminescence* **176**, 32 (2016). DOI <https://doi.org/10.1016/j.jlumin.2016.02.023>. URL <http://www.sciencedirect.com/science/article/pii/S0022231315305846>
9. V. Pagonis, G. Kitis, G.S. Polymeris, *Physica B: Condensed Matter* **539**, 35 (2018). DOI <https://doi.org/10.1016/j.physb.2018.03.054>. URL <http://www.sciencedirect.com/science/article/pii/S0921452618302576>
10. G.S. Polymeris, *Radiation Physics and Chemistry* **106**, 184 (2015). DOI <https://doi.org/10.1016/j.radphyschem.2014.07.003>. URL <http://www.sciencedirect.com/science/article/pii/S0969806X14002916>
11. G. Kitis, G.S. Polymeris, V. Pagonis, *Applied Radiation and Isotopes* **153**, 108797 (2019). DOI <https://doi.org/10.1016/j.apradiso.2019.05.041>. URL <http://www.sciencedirect.com/science/article/pii/S0969804319304142>
12. E. Bulur, H.Y. Göksu, *Radiation Measurements* **30**, 505 (1999). DOI 10.1016/S1350-4487(99)00207-3
13. V. Pagonis, S.M. Mian, M.L. Chithambo, E. Christensen, C. Barnold, *Journal of Physics D: Applied Physics* **42**(5), 055407 (2009). DOI 10.1088/0022-3727/42/5/055407
14. V. Pagonis, C. Ankjærgaard, M. Jain, M.L. Chithambo, *Physica B: Condensed Matter* **497**, 78 (2016)

15. V. Pagonis, G. Kitis, R. Chen, *Journal of Luminescence* **225**, 117333 (2020). DOI <https://doi.org/10.1016/j.jlumin.2020.117333>. URL <http://www.sciencedirect.com/science/article/pii/S0022231320305639>
16. M. Duval, *Ancient TL* **30**(2), 1 (2012)
17. V. Pagonis, G. Kitis, R. Chen, *Journal of Luminescence* **227**, 117553 (2020). DOI <https://doi.org/10.1016/j.jlumin.2020.117553>. URL <http://www.sciencedirect.com/science/article/pii/S0022231320310449>
18. A. Wieser, Y. Göksu, D.F. Regulla, A. Waibel, *International Journal of Radiation Applications and Instrumentation. Part D. Nuclear Tracks and Radiation Measurements* **18**(1), 175 (1991). DOI [https://doi.org/10.1016/1359-0189\(91\)90109-U](https://doi.org/10.1016/1359-0189(91)90109-U). URL <http://www.sciencedirect.com/science/article/pii/135901899190109U>
19. A.J.J. Bos, T.M. Pisters, J.M. Gómez-Ros, A. Delgado, *Radiation protection dosimetry* **47**, 473 (1993). DOI 10.1093/oxfordjournals.rpd.a081789
20. V. Pagonis, G.S. Polymeris, G. Kitis, *Radiation Measurements* **82**, 93 (2015)
21. B. Li, Z. Jacobs, R.G. Roberts, *Quaternary Geochronology* **35**, 1 (2016). DOI <https://doi.org/10.1016/j.quageo.2016.05.001>. URL <http://www.sciencedirect.com/science/article/pii/S1871101416300425>
22. G.W. Berger, *Ancient TL* **8**(3), 23 (1990)
23. A. Timar-Gabor, A. Vasiliniuc, D.A.G. Vandenberghe, C. Cosma, A.G. Wintle, *Radiation Measurements* **47**(9), 740 (2012). DOI <http://dx.doi.org/10.1016/j.radmeas.2011.12.001>. URL <http://www.sciencedirect.com/science/article/pii/S1350448711005671>
24. R. Chen, J.L. Lawless, V. Pagonis, *Radiation Measurements* **136**, 106422 (2020). DOI <https://doi.org/10.1016/j.radmeas.2020.106422>. URL <http://www.sciencedirect.com/science/article/pii/S1350448720302018>
25. S.G.E. Bowman, R. Chen, *Journal of Luminescence* **18-19**, 345 (1979). DOI [https://doi.org/10.1016/0022-2313\(79\)90136-4](https://doi.org/10.1016/0022-2313(79)90136-4). URL <http://www.sciencedirect.com/science/article/pii/0022231379901364>
26. S.V. Nikiforov, V.S. Kortov, M.G. Kazantseva, *Physics of the Solid State* **56**(3), 554 (2014). URL <https://doi.org/10.1134/S1063783414030214>
27. J. Edmund, *Effects of temperature and ionization density in medical luminescence dosimetry using al2o3:c (phd thesis, riso, denmark)*. Ph.D. thesis, Risø National Laboratory (2007). Riso-PhD-38(EN)
28. V. Pagonis, C. Ankjærgaard, A.S. Murray, M. Jain, R. Chen, J. Lawless, S. Greulich, *Journal of Luminescence* **130**(5), 902 (2010)
29. M.L. Chithambo, C. Ankjærgaard, V. Pagonis, *Physica B: Condensed Matter* **481**, 8 (2016)
30. V. Pagonis, R. Chen, M.J. W, S. B, *Journal of Luminescence* **131**(5), 1086 (2011)
31. S.V. Nikiforov, I.I. Milman, V.S. Kortov, *Radiation Measurements* **33**(5), 547 (2001). DOI [https://doi.org/10.1016/S1350-4487\(01\)00056-7](https://doi.org/10.1016/S1350-4487(01)00056-7). URL <http://www.sciencedirect.com/science/article/pii/S1350448701000567>. Proceedings of the International Symposium on Luminescent Detectors and Transformers of Ionizing Radiation
32. V. Pagonis, C. Kulp, *Journal of Luminescence* **181**, 114 (2017)
33. M. Tachiya, A. Mozumder, *Chemical Physics Letters* **28**(1), 87 (1974). DOI [https://doi.org/10.1016/0009-2614\(74\)80022-9](https://doi.org/10.1016/0009-2614(74)80022-9). URL <http://www.sciencedirect.com/science/article/pii/0009261474800229>
34. D.J. Huntley, *Journal of Physics: Condensed Matter* **18**(4), 1359 (2006)
35. B. Li, S.H. Li, *Journal of Physics D: Applied Physics* **41**(22), 225502 (2008). DOI 10.1088/0022-3727/41/22/225502
36. M. Jain, B. Guralnik, M.T. Andersen, *Journal of Physics: Condensed Matter* **24**(38), 385402 (2012)
37. N.D. Brown, E.J. Rhodes, T.M. Harrison, *Quat. Geochronol.* **42**, 31 (2017). DOI 10.1016/j.quageo.2017.07.006

38. G.S. Polymeris, N. Tsirliganis, Z. Loukou, G. Kitis, *Physica Status Solidi (a)* **203**(3), 578 (2006). DOI [10.1002/pssa.200521347](https://doi.org/10.1002/pssa.200521347). URL <https://onlinelibrary.wiley.com/doi/abs/10.1002/pssa.200521347>
39. V. Pagonis, G. Kitis, *Journal of Luminescence* **168**, 137 (2015)
40. G. Kitis, V. Pagonis, *Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms* **432**, 13 (2018). DOI <https://doi.org/10.1016/j.nimb.2018.06.029>. URL <http://www.sciencedirect.com/science/article/pii/S0168583X18304129>
41. A. Mandowski, *Journal of Physics D: Applied Physics* **38**, 17 (2005)
42. V. Pagonis, L. Blohm, M. Brengle, G. Mayonado, P. Woglam, *Radiation Measurements* **51-52**, 40 (2013). DOI <http://dx.doi.org/10.1016/j.radmeas.2013.01.025>. URL <http://www.sciencedirect.com/science/article/pii/S1350448713000450>
43. J.L. Lawless, R. Chen, V. Pagonis, *Journal of Luminescence* **226**, 117389 (2020). DOI <https://doi.org/10.1016/j.jlumin.2020.117389>. URL <http://www.sciencedirect.com/science/article/pii/S0022231320304506>
44. V. Pagonis, S. Kreutzer, A.R. Duncan, E. Rajovic, C. Laag, C. Schmidt, *Journal of Luminescence* **219**, 116945 (2020). DOI <https://doi.org/10.1016/j.jlumin.2019.116945>. URL <http://www.sciencedirect.com/science/article/pii/S0022231319322057>
45. V. Pagonis, G. E, H. M, K. C, *Radiation Measurements* **67**, 67 (2014)
46. G. Kitis, V. Pagonis, *Journal of Luminescence* **137**, 109 (2013). DOI <https://doi.org/10.1016/j.jlumin.2012.12.042>. URL <http://www.sciencedirect.com/science/article/pii/S0022231312007624>
47. V. Pagonis, A.G. Wintle, R. Chen, X.L. Wang, *Radiation Measurements* **43**, 704 (2008)
48. J. Peng, V. Pagonis, *Radiation Measurements* **86**, 63 (2016). DOI <http://dx.doi.org/10.1016/j.radmeas.2016.01.022>. URL <http://www.sciencedirect.com/science/article/pii/S1350448716300221>
49. V. Pagonis, R. Chen, G. Kitis, *Journal of Archaeological Science* **38**(7), 1591 (2011)
50. A.G. Wintle, A.S. Murray, *Radiation Measurements* **29**(1), 81 (1998). DOI [https://doi.org/10.1016/S1350-4487\(97\)00228-X](https://doi.org/10.1016/S1350-4487(97)00228-X). URL <http://www.sciencedirect.com/science/article/pii/S135044879700228X>
51. V. Pagonis, A.G. Wintle, R. Chen, *Radiation Measurements* **42**(10), 1587 (2007)
52. X.L. Wang, A.G. Wintle, Y.C. Lu, *Radiation Measurements* **41**(6), 649 (2006). DOI <https://doi.org/10.1016/j.radmeas.2006.01.001>. URL <http://www.sciencedirect.com/science/article/pii/S1350448706000941>
53. D.K. Koul, V. Pagonis, P. Patil, *Radiation Measurements* **91**, 28 (2016)