

Machine Learning techniques for predicting molecular properties

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Abstract—The high computational cost of quantum chemistry calculations have prompted the use of less expensive machine learning methods for predicting molecular properties in chemical compound space. Finding good feature representations for molecules is hard, in part because of the graph-like structure geometry of the molecules that need to be represented as high dimensional vectors. [Add what this paper is about](#)

Index Terms—thesis proposal, candidacy exam write-up, EDIC, EPFL

I. INTRODUCTION

The discovery of new molecular materials in chemistry has the potential of solving many of the problems we face today. Having a system which predicts both accurately and at a small computational cost the properties of new materials is highly desirable and has applications ranging from novel drugs discovery, water purification to efficient materials design for high energy transmission and storage [1].

II. BACKGROUND WORK

[This write-up serves two purposes. First, it forms the basis for your candidacy exam. As such you should summa-](#)

Proposal submitted to committee: June 13th, 2009; Candidacy exam date: June 20th, 2009; Candidacy exam committee: Exam president, thesis director, co-examiner.

This research plan has been approved:

Date: _____

Doctoral candidate: _____
(name and signature)

Thesis director: _____
(name and signature)

Thesis co-director: _____
(if applicable) (name and signature)

Doct. prog. director: _____
(B. Falsafi) (signature)

size the three papers selected by your advisor and yourself, and analyze as well as discuss them critically. Second, the write-up is also your thesis proposal. Therefore, the last one or two pages should be dedicated to your own preliminary work. A road-map of how you plan to advance the state of the art in your chosen area should also be given. For further details please consult the document “PhD Candidacy Exam Overview.” You can find the latest version at <http://phd.epfl.ch/page57746-en.html>. Describe briefly the context, the problem, shortcomings in prior approaches, and your proposed approach and solution. Forecast results. Background — Describe the three papers in detail, the problem they tackle, the solutions and results, and their shortcomings, and how they relate to your work. This part builds the basis for the oral candidacy exam.

A. Learning Invariant Representations of Molecules for Atomization Energy prediction

Representing Molecules

While domain specific descriptors for molecules exist [5], recent work [4] has proposed to predict properties of a molecule of size N only from the 3D positions of the atoms R_i $i \in 1..N$ and their nuclear charge Z_i $i \in 1..N$. This has prompted the introduction of the Coloumb Matrix descriptor, whose individual entries appear in the Schroedinger equation. It is defined by a $N \times N$ matrix with entries given by:

$$M(i, j) = \begin{cases} 0.5 * Z_i^{2.4} & \text{if } i = j \\ Z_i * Z_j / |R_i - R_j| & \text{otherwise} \end{cases} \quad (1)$$

where $R_i - R_j$ represents the distance between the atoms i and j .

The dimensionality of the Coloumb Matrix is given by the number of atoms in a molecule. Since that varies across molecules in a dataset, one common trick is to pad with 0's the matrices corresponding to small molecules until they reach the maximum molecule size in a dataset. This limits the size of the molecules that can be used, since the descriptor has complexity $O(N^2)$, where N is the number of atoms.

Desired properties of descriptor Due to the graph-like structure of the molecules, finding a fixed size representation is difficult. The desired properties of a molecular descriptor are invariance to translation and rotation of the molecule and invariance to the indexing of the atoms.

Solved using sorted or Random Coloumb While the Coloumb Matrix representations solves the rotation and translation invariance through the use of distances between atoms

$R_i - R_j$, invariance in atom indexing still needs to be tackled since any permutation of atom indexes results in a valid Coloumb descriptor. Two variations of the descriptor are proposed in [3]. The first one, called Sorted Coloumb, uses the permutation of the atoms given by the sorting of the row norms of a valid Coloumb matrix. Any molecule has a unique representation given by the Sorted Coloumb matrix. The second representations is based on the idea that the norms of the rows can have very similar values in practice and the sorting, therefore also the atom indexing, is subject to small noise. The new descriptor, Random Coloumb Matrices is a collection of Sorted Coloumb matrices. For every molecule, approximatively 10 Randomly Sorted Coloumb matrices are drawn. One Random Sorted Coloumb Marix is obtained by sorting the set of rows was sorted according to their norm at which a small Gaussian noise was added. New predictions can be made by averging the prediction results.

Reach state of the art result at the time. The current new value is 1.5 using Bag of Bonds. The performane of the descriptors was evaluated on predicting the atomization energy on a dataset of 7165 molecules with at most 23 atoms per atom. The predicted values range from -800 to -2000 kcal/mol. The splitting of the data into 5 folds for cross validation is done using stratified sampling. The molecules were clustered into 5 sets with similar atomization energy levels and the folds were created by randomly selecting one molecule from each bucket.

While this is a good strategy for obtaining good generalization performance, in normal machine learning practice we should not touch the test dataset. If we test the performance on a new molecule whose atomization energy is not within the bounds present in the training dataset, it is likely that the prediction will not be very accurate. Moreover, if we have a molecule with more atoms than present in the dataset, we would need to retrain our model with a descriptor of diferent size. The same problem appears across chemical compound space if we try to predict the atomization energy of a molecule with the same number of atoms but with different atom types composition. In general, we do not have guarantees that the a molecule with similar atom composition and similar atom type have target prediction in the same range as our training set.

For experimental evaluation of the performance of descriptors, both kernel ridge regression and multy layer feed forwards networks were tried. The best test performance of 3.1 kcal/mol MAE was obtained using a neural network with Randomly Sorted Coloumb matrix. The improvement was three fold with respect to the previous state of the art, which gave a MAE of 9kcal/mol. A performance level is 1kcal/mol to reach chemical accuracy. [Maybe put this as footnote](#) Later work [2], improved upon this result by reducing the current state-of-the-art to only 1.5kcal/mol using a bag of bonds descriptor with Laplacian kernel.

Difficulty of training a neural network, maybe cite tricks of the trade While recently Neural Nets (especially deep networks) have achieved state-of-the-art in many fields ranging from computer vision, natural language processing and speech recognition, one of the main challenges they pose is the

difficulty in training for people without a lot of experiences with nnets in particular.

Cite here Neural nets tricks fo the trade In order to obtain the competitive performance of 3.1kcal/mol using neural nets, multiple tricks have been used, inspired from cite here NN. First of all, taking the real entries of the Coloumb matrix as input to the neural net proved to perform poorly. For this, a binarization step was performed which added an extra dimensionality to the dataset. Specifically, if $x \in R^D$ represents a flatten Coloumb matrix, it is mapped to a new binarized descriptor $y \in R^{D \times M}$ such that $y_i \in R^{1 \times M}$ is computed by taking shifted versions of x_i entry that are passed through a sigmoidal function

$$y_i = [\dots, \tanh(\frac{x_i - \theta}{\theta}), \tanh(\frac{x_i}{\theta}), \tanh(\frac{x_i + \theta}{\theta})] \quad (2)$$

Depending on the range of every x_i , the size of y_i can vary acrosss dimensions if we ignore saturated values. Other parameters that are selected using cross validation are the number of hidden units per layer, the number of layers, the learning rate.

B. Self-Taught Learning: Transfer Learning from Unlabeled Data

Present the different machine learning framewroks that exists, with picture. It is a two part optimization problem. - First find bases - Then find new activations for the old ones. Through experimental results - since they were tested on a range of problems from image, text and sound.

C. Information-Theoretic Regret Bounds for Gaussian Process Optimization in the Bandit Setting

Optimizing an unknown function is an important problem.

Optimization of a black box function that is expensive to evaluate is a common problem with applications ranging from active user modelling, hierarchical reinforcement learning and more recently, hyper parameter optimization of machine learning models. This problem can be posed as a multi-armed bandit problem where the function to be estimated is either drawn from a Gaussian Process or has low norm in reproducing Kernel Hilbert space.

Often done using Gaussian processes in a Bayesian setting. Many heuristic have been proposed for defining an acquisition function. Few is known for its conergence.

Among the common used acquisition functions we note the probabily of improvement, maximum expected improvement or upper confidence bound acquisition, with the latter two experimentally shown to perform better in practice. Besides their practical success, few is known in practice about their convergence properties for finite and infinte input dimensional space.

Sublinear converge rates are proven for GP-UCP. The bound is in two steps. First bound it on the information gain, then on the spectral of the kernel matrix which is further bound on the spectral operator.

Since RKHS is not relevant to our current setup, it will be skiped from the previous explanation.

1) *Gaussian Processes basics:* A Gaussian Process (GP) defines a distribution over functions f , $f \sim GP(u(x), k(x, x'))$, in a similar way in which probability densities define distributions over random variables. It is fully specified by its mean and its covariance matrix. In a Bayesian setting, we assume our function f is sampled from a Gaussian with prior $GP(0, k(x, x'))$, where k is the kernel or covariance matrix. The most common kernel types are the linear, squared exponential and Matern kernel. For T sampled points with noise, we have $y_t = f(x_t) + \epsilon_t$, where $\epsilon_t \in N(0, \sigma^2)$. The posterior over f , conditioned on the $y_{1:T}$ and $x_{1:T}$ in the presence of noise is given by $P(f_T | y_{1:T}, x_{1:T}) = N(u_T(x), \sigma_T^2(x))$, where:

- K_T is positive definite with entries $k(x, x'), x, x' \in A_T$
- $k_T(x) = [k(x_1, x), \dots, k(x_T, x)]^T$
- $k_T(x, x') = k(x, x') - k_T(x)^T (K_T + \sigma^2 I)^{-1} k_T(x')$
- $u_T(x) = k_T(x)^T (K_T + \sigma^2 I)^{-1} y_T$
- $\sigma^2(x) = k_T(x, x)$

2) *Information Gain and Experimental Design:* Unlike function optimization where the goal is to find the maximum of a function, in experimental design the goal is to find a good approximation of the function globally with few samples as possible. We note that the same algorithm can not be employed for both tasks, since in function optimization we might want to avoid sampling in certain regions where we are confident that the function has very small values.

For a sampled set A , we define $y_A = f_A + \epsilon_A$, $f_A = [f(x)]_{x \in A}$ and the noise $\epsilon_A \sim N(0, \sigma^2 I)$. The information gain as

$$I(y_A; f) = H(y_A) - H(y_A | f) \quad (3)$$

where $H(y_A)$ and $H(y_A | f)$ represent the entropy or uncertainty in y_A and the uncertainty in y_A if we know f . In other words, information gain expresses the reduction in uncertainty about f given y_A . [Shouldn't it be the other way around?](#)

Using the fact that for a Gaussian $H(N(u, \sigma)) = \frac{1}{2} \log |I + \sigma^{-2} K_A|$ we can rewrite $I(y_A; f) = I(y_A; f_A) = \frac{1}{2} \log |2\pi e \Sigma|$

3) *GP-UCB:*

4) *Regret Bounds:*

5) *Bounding the regret using Information Gain:*

6) *Bounding the Information Gain using the spectral :*

7) *Bounding the Information gain using the spectral :* Although convergence rates are proven for infinite input dimensional spaces, the complexity of the GP step that incorporates the inversion of the covariance matrix makes it cubic in the number of samples T , which makes it often impractical for high dimensional input.

III. RESEARCH PROPOSAL

A.

Proposing a new descriptor which is invariant to permutations of the atom. 2.6+/- or 2.1 with noise. (still gives comparable accuracy to same DFT models)

B.

Propose of augmenting the data sets more easily and make the cross validation less sensitive to splitting -at the moment : take non H atoms, then sort then do CV.

Pose the problem as one of the semi supervised, self taught learning etc problems and try to make it generalize across compound space, or learn new embeddings of the atoms.

Although the use of Gaussian processes in material design is not new, its major drawback is the computational bottleneck. In our scenario, this can be used for tuning the hyper-parameters of the model trained. Here the input dimensionality is given by the nbr of the hyper parameters (learning rate, activation fct, nbr hidden layers) used and the fct to be minimized is the cross validation error. The result presented in the previous subsection were obtained like that. Talk if we have time about bayesian neural nets, were simpler models outperform more easy models just be using hyper parameter optimization instead of grid search.

[Write how you propose to advance the state of the art given the background. What is new technically? How does it improve over prior work? Summarize, suggest an approximate timeline, and list references.](#)

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