

Circuit Analysis with Dependent Sources

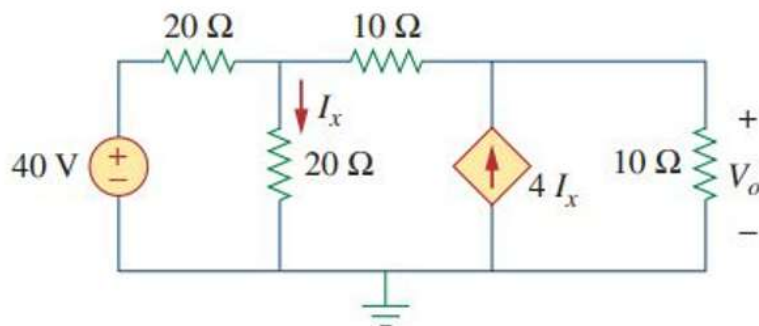
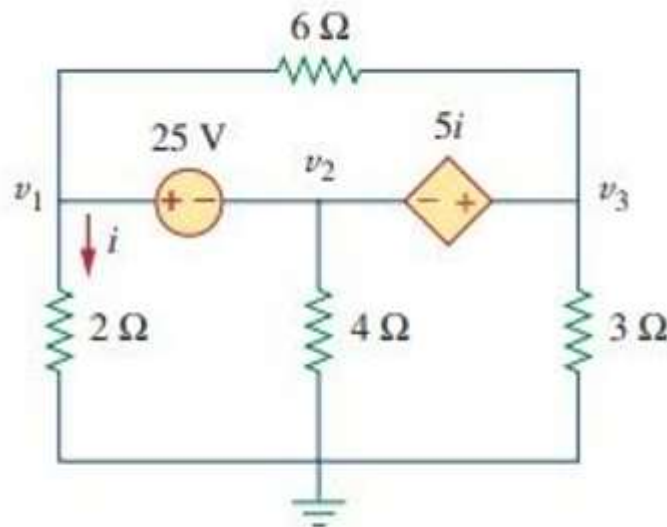
Objectives:

1. To model dependent voltage sources and current sources in LTSpice
2. To find the nodal voltages and branch currents

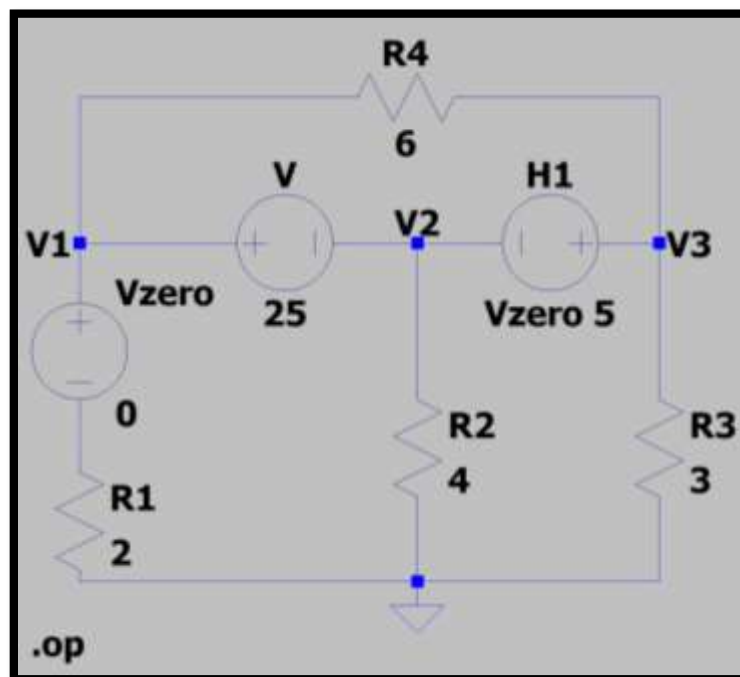
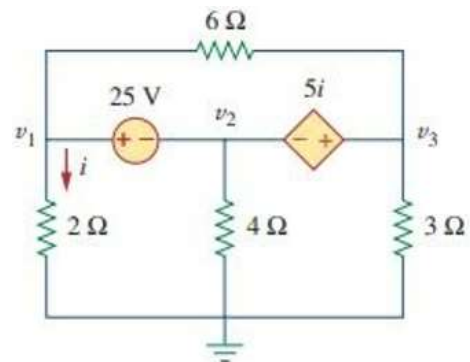
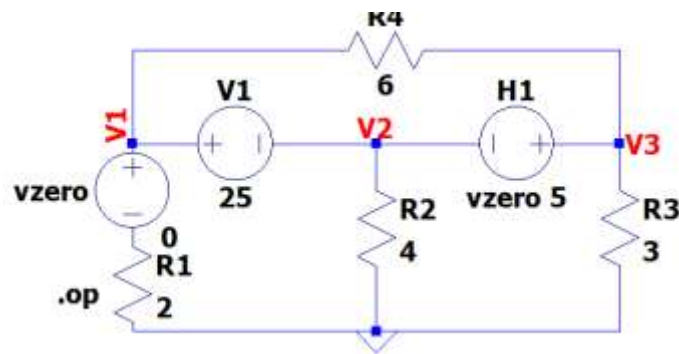
Simulation Tool:

LTSpice – dc operating point analysis and transient analysis.

Circuits:



Current Dependent Voltage Source

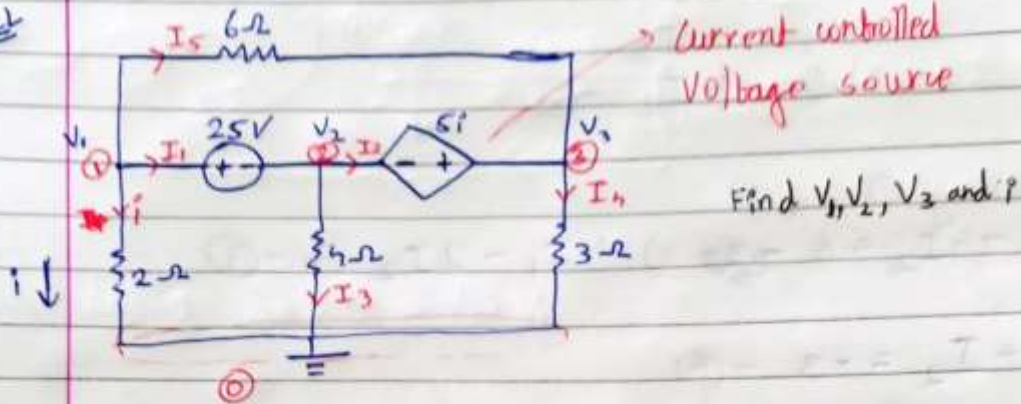


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--- Operating Point ---
V(n001):      7.6087      voltage
V(v2):        -17.3913    voltage
V(v3):         1.63043    voltage
V(v1):         7.6087     voltage
I(H1):         0.452899    device_current
I(R4):         -0.996377   device_current
I(R3):         0.543478    device_current
I(R2):         -4.34783    device_current
I(R1):         3.80435     device_current
I(Vzero):      3.80435     device_current
I(V):         -4.80072     device_current

```

KCL



→ KCL at node ①: $\sum I_{\text{entering}} = \sum I_{\text{leaving}}$
 $\Rightarrow 0 = i + I_1 + I_5$
 $\Rightarrow I_1 = -i - I_5$ — ①

→ KCL at node ②: $\sum I_{\text{entering}} = \sum I_{\text{leaving}}$
 $I_1 = I_2 + I_3$ — ②

→ Compare ① and ②,
 $-i - I_5 = I_2 + I_3$
 $\Rightarrow I_2 = -i - I_5 - I_3$ — ③

→ KCL at node ③: $\sum I_{\text{entering}} = \sum I_{\text{leaving}}$
 $I_2 + I_5 = I_4$
 $\Rightarrow I_2 = I_4 - I_5$ — ④

→ Compare ③ and ④
 $-i - I_5 - I_3 = I_4 - I_5$
 $\Rightarrow i + I_3 + I_4 = 0$
 $\Rightarrow \frac{V_1}{2} + \frac{V_2}{4} + \frac{V_3}{3} = 0$
 $\Rightarrow \boxed{6V_1 + 3V_2 + 4V_3 = 0}$ — ⑤

$$V_{12} = \boxed{V_1 - V_2 = 25V} - (6)$$

$$V_{32} = 5i = V_3 - V_2$$

$$\Rightarrow V_3 - V_2 = \frac{5V_1}{2}$$

$$\Rightarrow \boxed{2V_3 - 2V_2 - 5V_1 = 0} - (7)$$

From (6)

$$V_2 = -25 + V_1$$

Substituting V_2 in (5) and (7)

$$4V_1 + 4V_3 = 75; \quad 2V_3 - 7V_1 = -50$$

9

$$4V_3 + 9V_1 = 75$$

$$\Rightarrow 4V_3 \stackrel{(9)}{=} 14V_1 \stackrel{(9)}{=} 100$$

$$23V_1 = 175$$

$$\Rightarrow \boxed{V_1 = 7.60V}$$

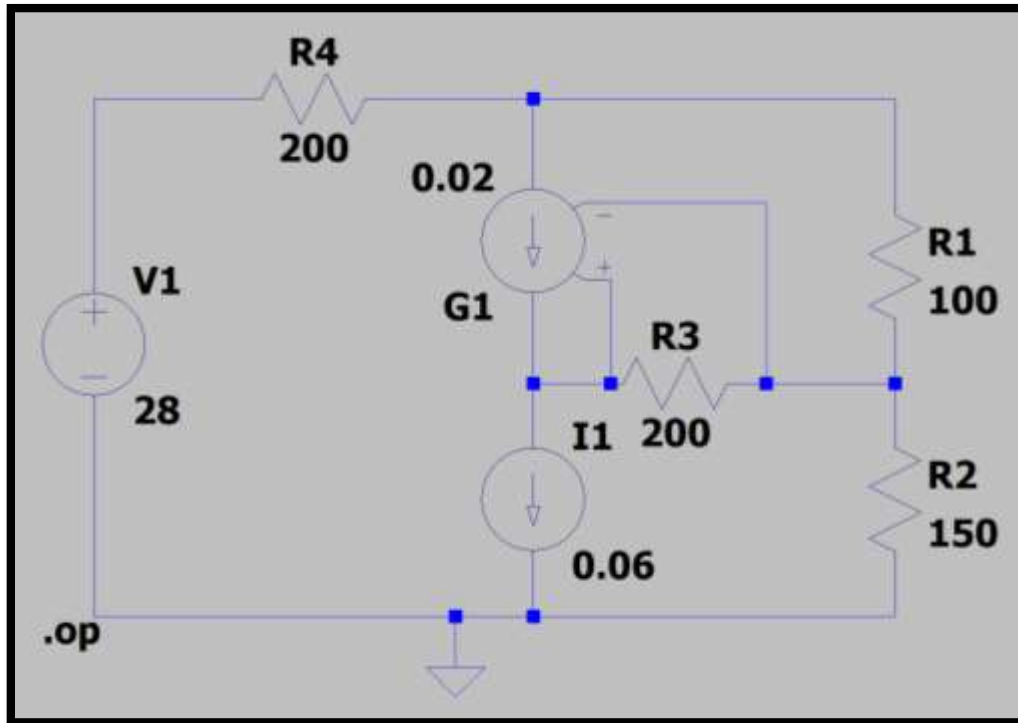
$$\Rightarrow \boxed{V_2 = -17.39}$$

$$\Rightarrow \boxed{V_3 = 1.63V}$$

$$\Rightarrow \boxed{i = 19.02A}$$

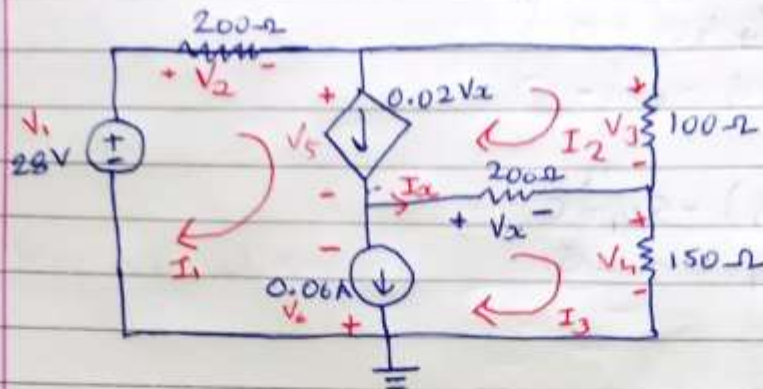
Voltage Dependent Current Source

1) Class work question



```
--- Operating Point ---  
V(n001) :      28      voltage  
V(n002) :       8      voltage  
V(n003) :       6      voltage  
V(n004) :      10      voltage  
I(I1) :      0.06      device_current  
I(R4) :       0.1      device_current  
I(R3) :      0.02      device_current  
I(R2) :      0.04      device_current  
I(R1) :      0.02      device_current  
I(G1) :      0.08      device_current  
I(V1) :     -0.1      device_current
```


KVL



KVL in loop ①: $28 + V_6 = V_2 + V_5$ — (1)

KVL in loop ②: $V_5 + V_x = V_3$
 $\Rightarrow V_5 = V_3 - V_x$ — (2)

KVL in loop ③: $0 = V_6 + V_x + V_4$ — (3)
 $\Rightarrow V_6 = -V_x - V_4$ — (3)

Substituting (2) and (3) in (1)

$$28 - V_x - V_4 = V_2 + V_3 - V_x$$

$$\Rightarrow V_2 + V_3 + V_4 = 28$$

$$\Rightarrow [200I_1 + 100I_2 + 150I_3 = 28] \text{ — (4)}$$

$$I_1 - I_2 = 0.02 V_x$$

$$V_x = I_x 200$$

$$\Rightarrow I_1 - I_2 = 0.02 (200) (I_3 - I_2)$$

$$I_x = I_3 - I_2$$

$$\Rightarrow I_1 - I_2 = 4 I_3 - 4 I_2$$

$$\Rightarrow \boxed{I_1 + 3 I_2 - 4 I_3 = 0} \quad \text{--- (5)}$$

$$\boxed{I_1 - I_3 = 0.06} \quad \text{--- (6)}$$

$$\Rightarrow 100 I_1 = 6 + 100 I_3$$

$$\text{OR } I_1 = \frac{6}{100} + I_3$$

Substituting Value of I_1 in (5) and (6)

$$\Rightarrow 100 I_2 + 350 I_3 = 16$$

$$\text{or } 100 I_2 + 100 I_3 = 2$$

$$450 I_3 = 18$$

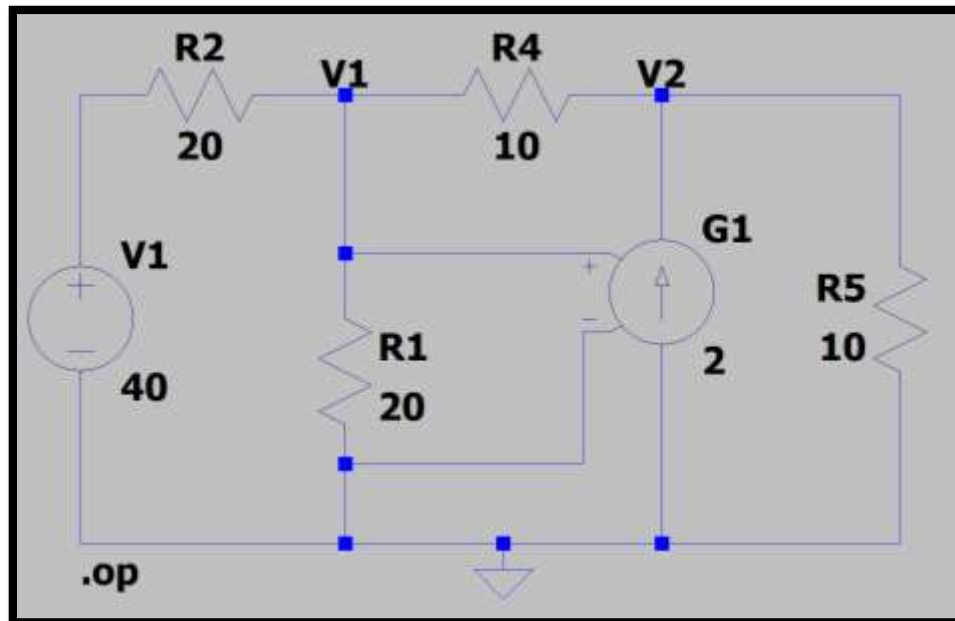
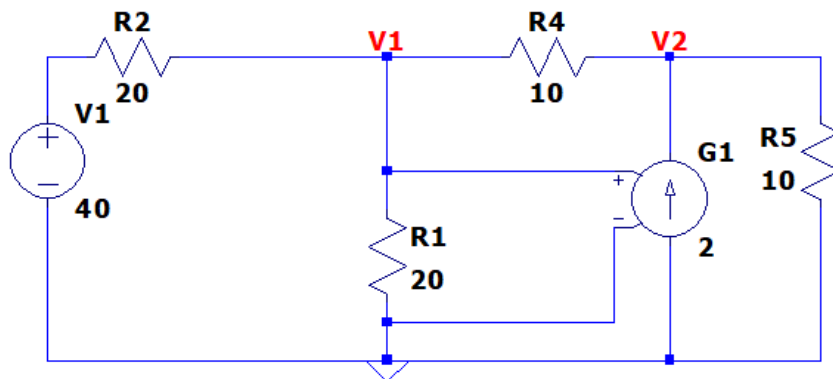
$$\Rightarrow \boxed{I_3 = 0.04 \text{ A}}$$

$$\Rightarrow \boxed{I_2 = 0.02 \text{ A}}$$

$$\Rightarrow \boxed{I_1 = 0.1 \text{ A}}$$

$$\Rightarrow \boxed{V_x = 4 \text{ V}}$$

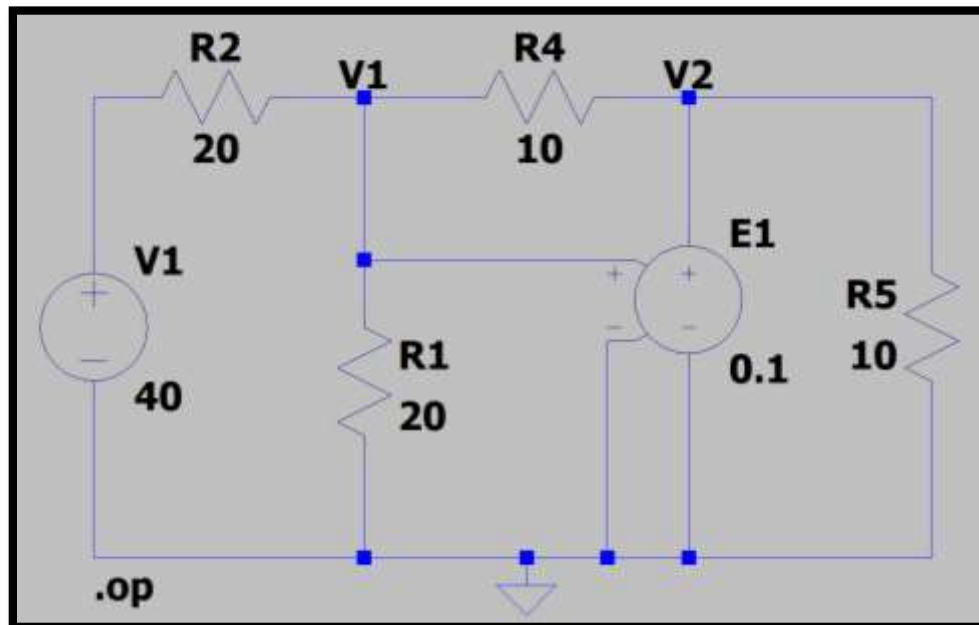
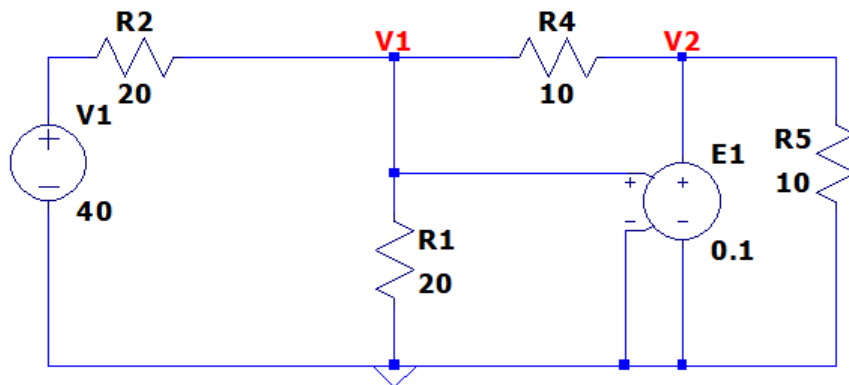
2) Practical file question



--- Operating Point ---

V(v1) :	-2.35294	voltage
V(n001) :	40	voltage
V(v2) :	-24.7059	voltage
I(R5) :	2.47059	device_current
I(R4) :	2.23529	device_current
I(R2) :	2.11765	device_current
I(R1) :	-0.117647	device_current
I(G1) :	-4.70588	device_current
I(V1) :	-2.11765	device_current

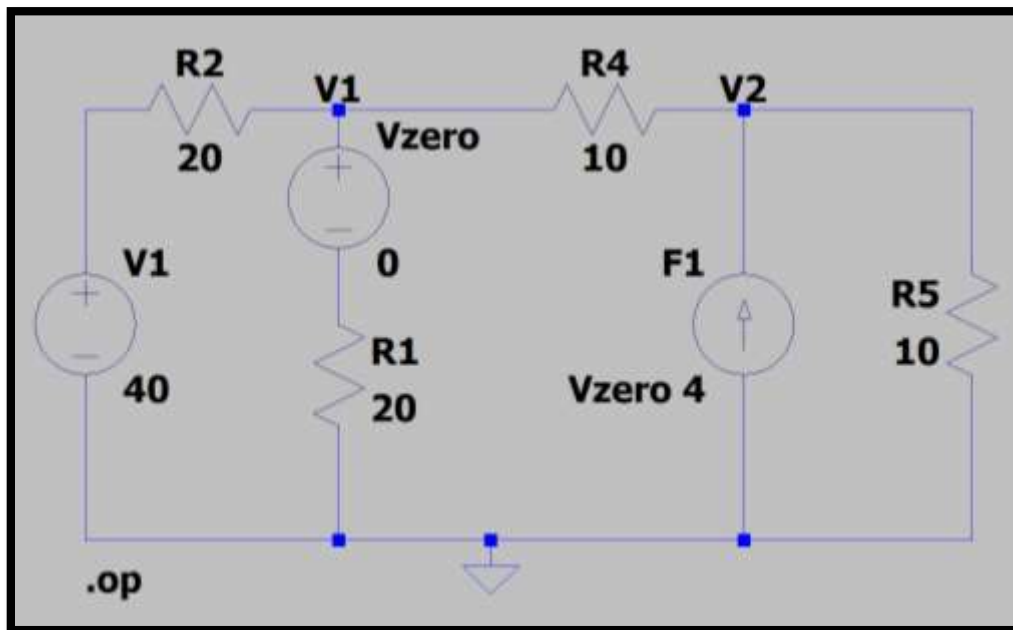
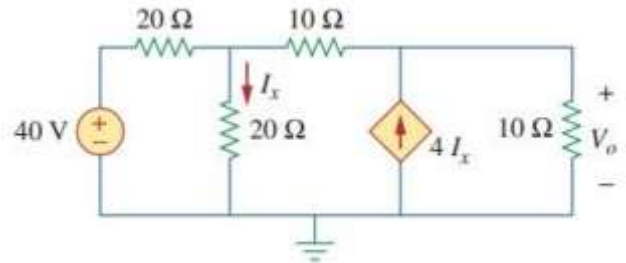
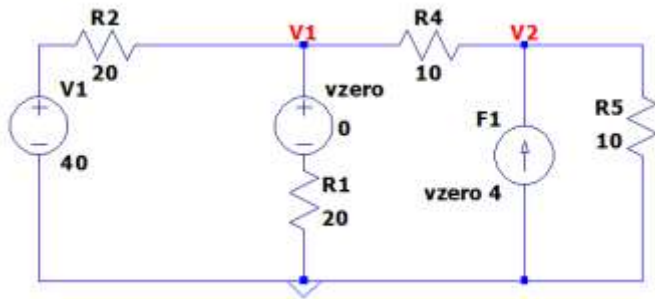
Voltage Dependent Voltage Source



--- Operating Point ---

V(v1) :	10.5263	voltage
V(n001) :	40	voltage
V(v2) :	1.05263	voltage
I(R5) :	-0.105263	device_current
I(R4) :	0.947368	device_current
I(R2) :	1.47368	device_current
I(R1) :	0.526316	device_current
I(E1) :	0.842105	device_current
I(V1) :	-1.47368	device_current

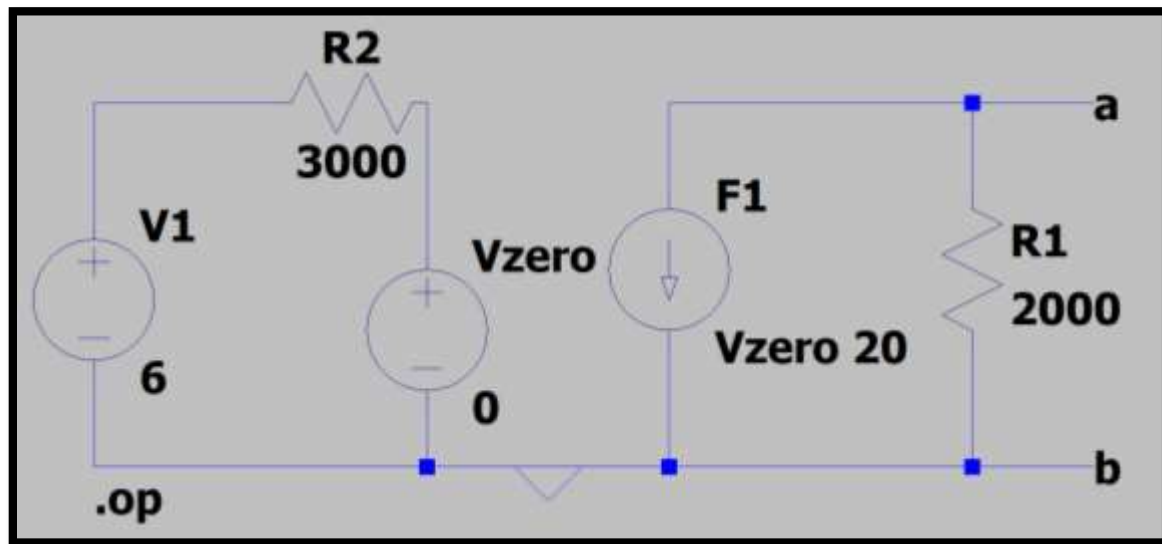
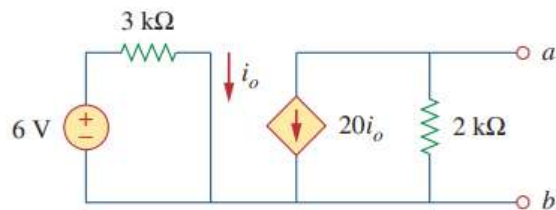
Current Dependent Current Source



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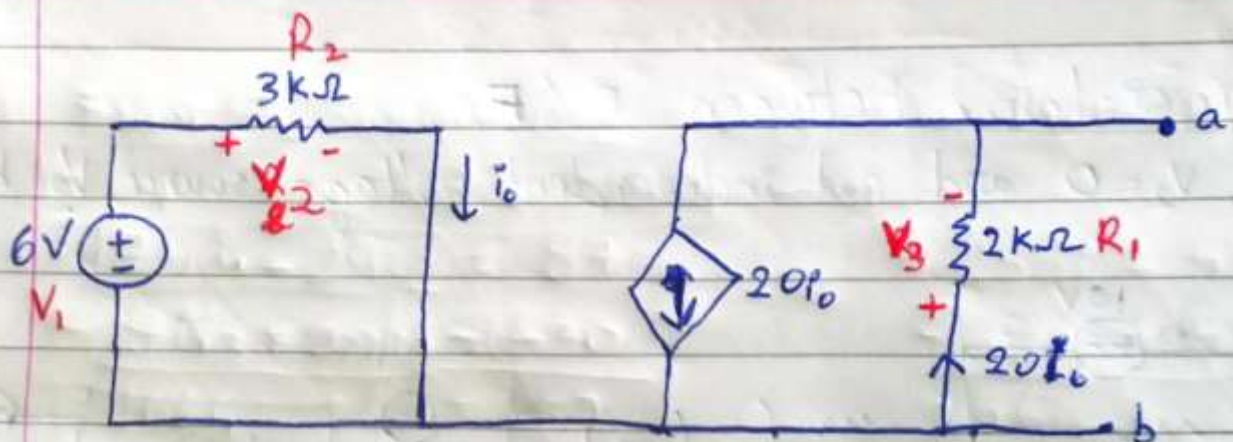
--- Operating Point ---
V(n002):      40          voltage
V(n001):      40          voltage
V(v1):        40          voltage
V(v2):        60          voltage
I(F1):        8           device_current
I(R5):       -6           device_current
I(R4):       -2           device_current
I(R2):      -3.55271e-016 device_current
I(R1):        2           device_current
I(Vzero):     2           device_current
I(V1):       4.44089e-016 device_current
  
```

Do it Yourself: Find i_o and voltage across the terminals a-b



--- Operating Point ---

```
V(n001) :      6      voltage
V(a) :      -80      voltage
V(n002) :      0      voltage
I(F1) :      0.04     device_current
I(R2) :     -0.002     device_current
I(R1) :     -0.04     device_current
I(Vzero) :     0.002   device_current
I(V1) :     -0.002     device_current
```



$$i_o = \frac{V_1}{R_2}$$

$$\Rightarrow i_o = \frac{6}{3 \times 1000}$$

$$\Rightarrow i_o = 0.002\text{A}$$

$$V_3 = 20i_o \times 2000$$

$$\Rightarrow V_3 = 4 \times \frac{2 \times 10000}{1000}$$

$$\Rightarrow V_3 = 80\text{V} = V_{ba}$$

$$\therefore V_{ab} = -80\text{V}$$