# AI1103 Assignment-1

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## Download all python codes from

https://github.com/vrahul02/AI1103-Probabilityand-Random-Variables/tree/main/Assignment -1/Codes

#### and latex-tikz codes from

https://github.com/vrahul02/AI1103-Probabilityand-Random-Variables/tree/main/Assignment -1/Assignment-1.tex

#### PROBLEM 1.5

The probability that a student is not a swimmer is  $\frac{1}{5}$ . Then the probability that out of five students, four are swimmers is

a) 
$$\binom{5}{4} \times \left(\frac{4}{5}\right)^4 \times \left(\frac{1}{5}\right)$$

b) 
$$\left(\frac{4}{5}\right)^4 \times \left(\frac{1}{5}\right)$$

c) 
$$\binom{5}{1} \times \left(\frac{4}{5}\right)^4 \times \left(\frac{1}{5}\right)$$

d) None of these

#### SOLUTION

Probability of 'non swimmer' =  $q = \frac{1}{5}$ Since being 'swimmer' and being 'non swimmer' are mutually exclusive,

Probability of 'swimmer' = p = 1- q =  $\frac{4}{5}$ 

Let K be a random variable representing number of students who are 'swimmer' in a given sample. So K has a binomial distribution:

$$\Pr\left(K = l\right) = \binom{n}{l} \times (q)^{n-l} \times (p)^{l} \tag{0.0.1}$$

Where

- n = Total number of students = 5
- p = Probability that a student is 'swimmer' =  $\frac{4}{5}$
- q = Probability that a student is 'non swimmer'  $= \frac{1}{5}$
- 1 = Total number of swimmers = 4

$$\Pr(K = 4) = {5 \choose 4} \times \left(\frac{1}{5}\right)^1 \times \left(\frac{4}{5}\right)^4$$
 (0.0.2)

As per the property of permutation and combination,

$$\binom{n}{l} = \binom{n}{n-l} \qquad (0.0.3)$$

$$\implies \Pr(K = 4) = {5 \choose 1} \times \left(\frac{1}{5}\right)^1 \times \left(\frac{4}{5}\right)^4 \qquad (0.0.4)$$

$$\implies$$
 Pr  $(K = 4) = 0.4096$   $(0.0.5)$ 

Thus options a) and c) are correct The probability that 4 students are 'swimmer' out of a random sample of 5 students is 0.4096.

