

# Conditional Probability Voting Algorithm Based on Heterogeneity of Mimic Defense System

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# About the paper

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# Abstract

- ➊ In recent years network attacks have been increasing rapidly, and it is difficult to defend against these attacks, especially attacks at unknown vulnerabilities or backdoors.
- ➋ As a novel method, Mimic defense architecture has been proposed to solve these cyberspace security problems by using the principle of dynamic heterogeneous redundant variants.
- ➌ Choosing appropriate variants and voting algorithm according to heterogeneities of these variants become the key issue of designing mimic defense architecture.
- ➍ This paper analyzes the system failure probability and scalability of 3 different voting algorithms- MHA, MVA, CPVA, and decide which one is the best.

# Variants

Mimic defense system can be considered a restrict version of N-variant systems, because it adopts the basic idea of running multiple variants of the same program in parallel.

- 1 Variants are usually composed of a series of components, such as CPU, operating system, middleware, application, etc.
- 2 Each component is composed of several modules. For example, the application can be divided into module 1, module 2, . . . , module M, etc.
- 3 A module is atomic, and its implementations are different from each other.
- 4 Each variant can be represented by a module implementation vector  $z^i = (g_1^i g_2^i \dots g_N^i)$ , where N is the number of modules contained in a variant and each module may have several implementations.

# Variants

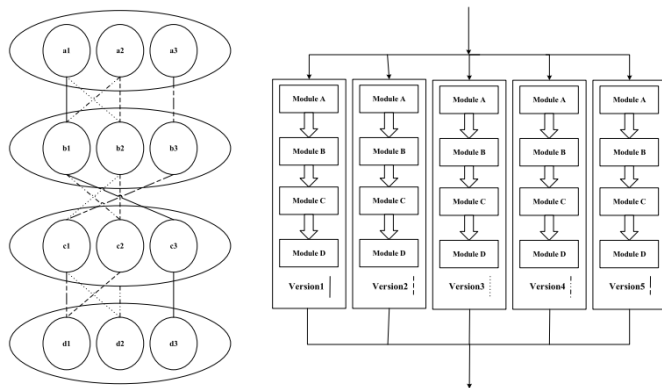


Figure: A typical mimic defense instance

# Variants

The mimic defense system shown in above figure can be described by a matrix as shown below.

$$\begin{pmatrix} z^1 \\ z^2 \\ z^3 \\ z^4 \\ z^5 \end{pmatrix} = \begin{pmatrix} a_1 & b_1 & c_3 & d_3 \\ a_2 & b_2 & c_2 & d_1 \\ a_1 & b_2 & c_1 & d_2 \\ a_2 & b_1 & c_2 & d_2 \\ a_3 & b_3 & c_1 & d_1 \end{pmatrix}$$

# Heterogeneous Variants

- ➊ Mimic defense system requires the variants to be heterogeneous to each other, not just applications, but also including CPU, OS, middleware and so on.
- ➋ For a large system which is common in mimic defense system, it is hard to realize totally heterogeneous.

There are mainly three kinds of algorithms to choose variants:

- ➊ maximum heterogeneous algorithm (MHA)
- ➋ optimal mean distance algorithm (OMDA)
- ➌ random seeds scheduling method

# Heterogeneous Variants

## 2-level similarity

Suppose there are three variants (1, 2, 3), the 2-level similarities are referred to the similarities for 1&2, 1&3, 2&3. The sum of similarities is lower, the system is considered to be safer.

- 1 As the number of working variants grows, 2-level similarity become less important.
- 2 Heterogeneity will reach max when there are 3 variants in the mimic system, and the heterogeneity will drop as variants number increase more than 3.



# Classic Model

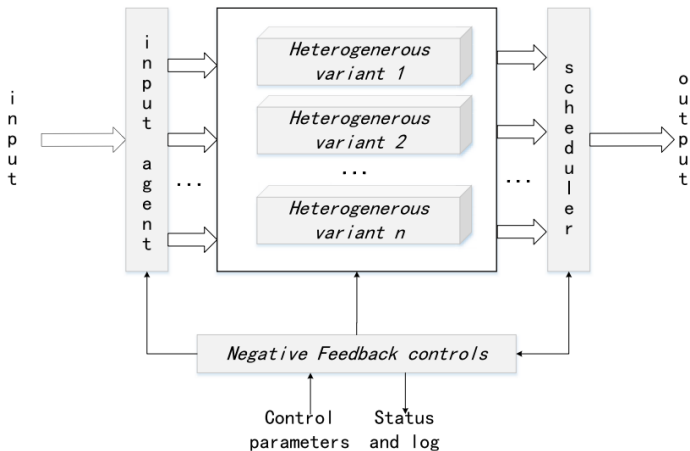


Figure: Classic model of mimic defense architecture

# Assumptions

- ➊ Input agent, Scheduler, and Feedback controller are safe from network attacks.
- ➋ Each vulnerability/backdoor of the system have the same probability being attacked.
- ➌ When the high-level vulnerability/backdoor is attacked, the variants who share the vulnerability will generate the same output.
- ➍ Only one vulnerability / back door can be attacked at a time, and the attacked variant will be cleaned in a short time.

The probability of successfully attacking each module is  $\beta_i$ , which should satisfy  $\sum_i \sum_{\psi_i} \beta_i = 1$ ,  $\psi_i$  is the number of implementations for module  $i$ .

# Binary Division Vectors

## Module diversity $\psi_i$

The implementation number of the module  $g_i$ , which can be calculated by formula  $|\bigcup_i g_k^i|$ . Implementation set is  $(a_1 a_1 a_1 a_2 a_3)^T$ , then union the contents and get the set  $\{a_1 a_2 a_3\}$ , which contain 3 elements, so the diversity of module a is 3.

## Binary division vector $\eta_i^k$

- 1 In a module, divide the same implementations into one group and other implementations into another group, and use a vector to represent. Assign corresponding values in the vector of the same implementations to 1 and others to 0.
- 2 For example, the implementation of  $g_1$  is  $(a_1 a_1 a_1 a_2 a_3)^T$ , then there are 3 binary division vectors for module  $g_1$ , the binary division vector of  $a_2$  is  $(00010)^T$ ,  $a_3$  is  $(00001)^T$ ,  $a_1$  is  $(11100)^T$ .

# Binary Division Vectors

## Complement binary division vector $\sim\eta_i^k$

which is reversing every element in the binary division vector. Based on the binary division vector  $(11100)^T$  of module implementation  $a_1$ , reverse all the elements in it, and its complement vector will be  $(00011)^T$ .

## Isomorphic number of binary division vector $\lambda_i^k$

The number of elements whose value is equal to 1. There are three 1 in the binary division vector of module implementation  $a_1$ , which is  $(11100)^T$ , then there are three  $a_1$ , and Isomorphic number of  $(11100)^T$  is 3.

# Maximum heterogeneous algorithm

① It is based on 2-level similarity.

②  $\text{system failure probability} = \frac{\text{no. of similarities}}{\text{no. of vulnerabilities}} \cdot$

③ 
$$\begin{pmatrix} z^1 \\ z^2 \\ z^3 \\ z^4 \\ z^5 \end{pmatrix} = \begin{pmatrix} a_1 & b_1 & c_3 & d_3 \\ a_2 & b_2 & c_2 & d_1 \\ a_1 & b_2 & c_1 & d_2 \\ a_2 & b_1 & c_2 & d_2 \\ a_3 & b_3 & c_1 & d_1 \end{pmatrix}$$

④  $\text{system failure probability} = \frac{0+1+1+0+1+2+1+1+1+0}{9} = \frac{8}{12} = \frac{3}{4}$

# Important Property

- 1 If there are  $T$  executions in the mimic defense system, there will be atleast 1 implementation whose isomorphic number is not less than  $\lfloor \frac{T+1}{2} \rfloor$ .
- 2 In order to reduce the failure probability of mimic defense system, add different implementation of a module or balance the same implementation of a module so that its maximum implementation is less than  $\lfloor \frac{T+1}{2} \rfloor$ .

# Majority voting algorithm

- 1 Divide the variants by their results, put variants with the same result into a group  $G_k$ . According to the hypothesis only one vulnerability/backdoor is attacked at a time, so there are usually 2 groups, suppose they are  $G_1$  and  $G_2$ .
- 2 If  $|G_1| > |G_2|$ , then select the result of  $G_1$  as the final output; otherwise, select the result of  $G_2$  as the final output.
- 3 Clean the variants which have been arbitrated to be abnormal.

# Majority voting algorithm

- 1  $V_g = \text{NULL}$
- 2 for  $i = 1: N$
- 3 for  $k = 1: \psi_i$
- 4 If( $\lambda_i^k \geq \lfloor \frac{T+1}{2} \rfloor$ )
- 5 add  $i$  in  $V_g$
- 6 endfor
- 7 endfor
- 8  $\text{msum} = 0$
- 9 for each index in  $U_g$
- 10  $\text{msum} = \text{msum} + \beta_k$
- 11 endfor



# Conditional probability voting algorithm

- 1 The variants which generated the same results are divided into one group  $G_k$ , generally there are only two groups, assumed as  $G_1$  and  $G_2$ .
- 2 If there is the same implementation of one module in both  $G_1$  and  $G_2$ , the same module implementation in the  $G_1$  and  $G_2$  need to be removed, then we can get two eliminated sets  $G'_1$  and  $G'_2$ , that is  $(z^i - \bigcap_{j \in G_2} z^j)$  and  $(z^i - \bigcap_{j \in G_1} z^j)$ .
- 3 If there are multiple implementations of one module in  $G'_1$  or  $G'_2$ , we use intersection to eliminate different module implementations, we can get two eliminated sets  $G''_1$  and  $G''_2$ , that is  $\bigcap_{i \in G_1} (z^i - \bigcap_{j \in G_2} z^j)$  and  $\bigcap_{i \in G_2} (z^i - \bigcap_{j \in G_1} z^j)$ .

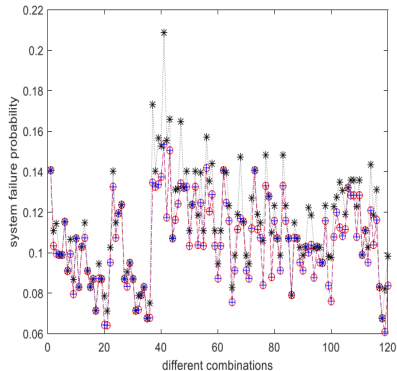
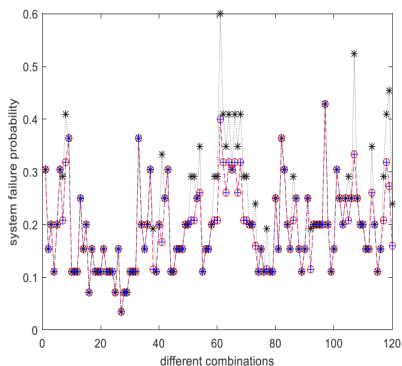
# Conditional probability voting algorithm

- ④ Calculation  $\beta_{G_1}$  and  $\beta_{G_2}$ ,  $\beta_{G_1} = \sum_k \beta_k$ , if  $k \in \bigcap_{i \in G_1} (z^i - \bigcap_{j \in G_2} z^j)$ ,  $\beta_{G_2} = \sum_k \beta_k$ , if  $k \in \bigcap_{i \in G_2} (z^i - \bigcap_{j \in G_1} z^j)$ .
- ⑤ If  $\beta_{G_1} > \beta_{G_2}$ , the result of  $G_2$  shall be used, otherwise, the result of  $G_1$  shall be used.
- ⑥ Clean the abnormal variants which have generated wrong result.

# Conditional probability voting algorithm

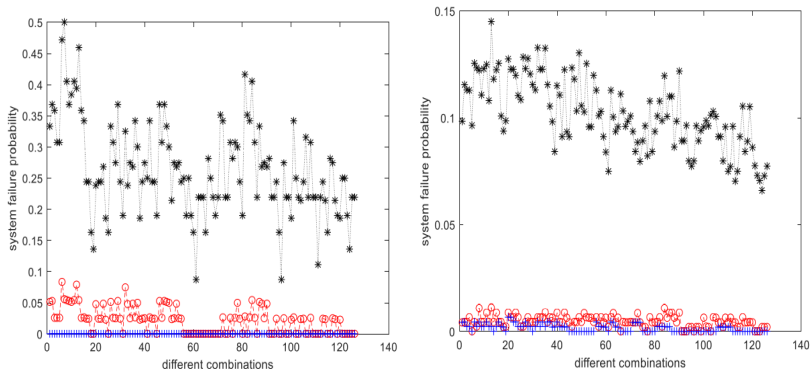
```
1   $G_u = \text{NULL}$ 
2  for i = 1: N
3    for k = 1:  $\psi_i$ 
4      if( $\lambda_i^k \geq \lfloor \frac{T+1}{2} \rfloor$ )
5         $G_u = \text{union}(G_u, \eta_i^k)$ 
6      endif
7    endfor
8  endfor
9  csum = 0
10  $G_L = G_S = \text{NULL}$ 
11 for each vctorl in  $G_u$ 
12   for i = 1: N
13     for k = 1:  $\psi_i$ 
14       if(vctorl ==  $\eta_i^k$ )
15         add i in  $G_L$ 
16       else if( $\sim \text{vctorl} == \eta_i^k$ )
17         add i in  $G_S$ 
18       endif
19     endfor
20   endfor
21   lsum = ssum = 0
22   for each k in  $G_L$ 
23     lsum = lsum +  $\beta_k$ 
24   endfor
25   for each k in  $G_S$ 
26     ssum = ssum +  $\beta_k$ 
27   endfor
28   if lsum < ssum
29     csum = csum + lsum
30   else
31     csum = csum + ssum
32   endif
33 endfor
```

# Results for 3-variants experiment



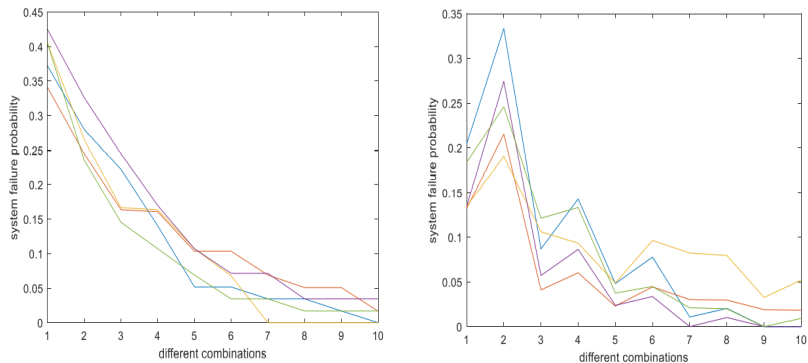
**Figure:** System failure probabilities of MHA, MVA and CPVA when  $N=10$   $M=5$  and  $N=100$   $M=10$

# Results for 5-variants experiment



**Figure:** System failure probabilities of MHA, MVA and CPVA when  $N=10$   $M=10$  and  $N=100$   $M=10$

# Results for scalability experiment



**Figure:** System failure probabilities of CPVA and MVA with variants increase

# Performance analysis

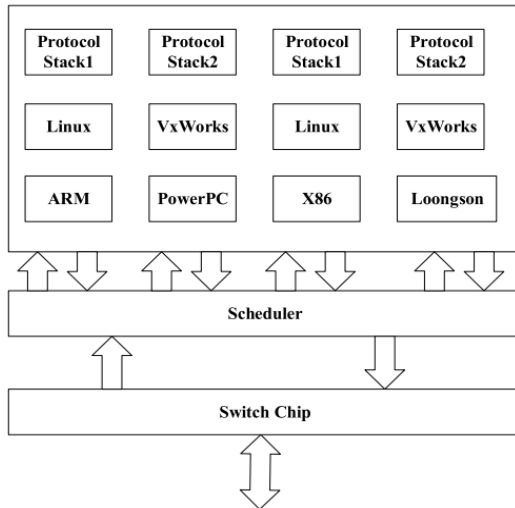


Figure: Mimic defense architecture for control panel of ethernet switch.