Autonomous Underwater Vehicle: A Surveillance Protocol

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Preface

This project is an attempt at combining all of my major skills into creating a simulation, imaging, perception and control pipeline for Autonomous Underwater Vehicles (AUV). As such, creating this project involves creating a number of pipelines.

The first pipeline is the signal simulation pipeline. The signal simulation pipeline involves sea-floor point-cloud creation and simulating the signals received by the sensor arrays of the AUV. The signals recorded by the sensor-arrays on the AUV contains information from the surrounding environment. The imaging pipeline performs certain operations on the recorded signals to obtain acoustic images of the surrounding environment. To that end, this pipeline involves the topics of signal processing, linear algebra, signals and systems.

As such, the second pipeline is the imaging pipeline. The inputs to the imaging pipeline is the signals recorded by the different sensor-arrays of the AUV, in addition to the parameters of the AUV and its components. This pipeline involves match-filtering, focussing and beamforming operations to create acoustic images of the surrounding environment. Depending on the number of ULAs present, the imaging pipeline is responsible for creating multiple acoustic images in real-time. Thus, this pipeline involves the topics of Digital Signal Processing, Match-Filtering, Estimation and Detection Theory and so on.

The images created by the imaging pipeline are fed to the perception-to-control pipeline. This pipeline takes in the image formed created from the ULA signals, parameters of AUV and its components, and some historical data, it provides instructions regarding the movement of the AUV. The mapping from the inputs to the controls is called policy. Learning policies is a core part of reinforcement learning. Thus, this pipeline mainly involves the topics of reinforcement learning. And since we'll be using convolutional neural nets and transformers for learning the policies, this pipeline involves a significant amount of machine and deep learning.

The final result is an AUV that is primarily trained to map an area of the sea-floor in a constant surveillance mode. The RL-trained policy will also be trained to deal with different kinds of sea-floor terrains: those containing hills, valleys, and path-obstructing features. Due to the resource constrained nature of the marine vessel, we also prioritize efficient policies in the policy-training pipeline.

The project is currently written in C++. And since there is non-trivial amount of training and adaptive features in the pipelines, we'll be using LibTorch (the C++ API of PyTorch) to enable computation graphs, backpropagation and thereby, learning in our AUV pipeline. However, for the sections where a computation graph is not required we will be writing templated STL code.

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Part I AUV Components & Setup

Chapter 1

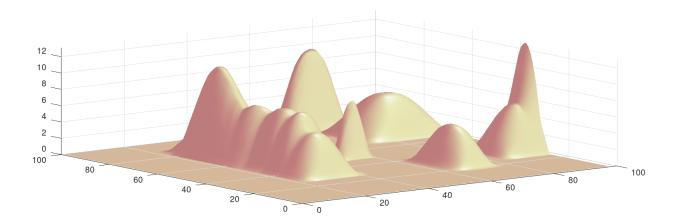
Underwater Environment

Overview

All physical matter in this framework is represented using point-clouds. Thus, the sea-floor also is represented using a number of 3D points. In addition to the coordinates, the points also have the additional property of "reflectivity". It is the impulse response of that point.

Sea-floors in real-life are rarely flat. They often contain valleys, mountains, hills and much richer geographical features. Thus, training an agent to function in such environments call for the creation of similar structures in our simulations.

To simplify things, we shall take a more constrained and structured approach. We start by creating different classes of structures and produce instantiations of those structures on the sea-floor. These structures are defined in such a way that the shape and size can be parameterized to enable creation of random sea-floors.



1.1 Underwater Hills

The most basic approach to creating this is to create a flat seafloor, where all the points have the same height. While this is a good place to start, it is good to bring in some realism to the seafloor. To that end, we shall have some rolling hills as the sea-floor. Each "hill"

is created using the method outlined in Algorithm 1. The method involves deciding the location of the hills, the dimension of the hills and then designing a hill by combining an exponential function and a cosine function. We're aiming to essentially produce gaussian-looking sea-floor hills. After the creation, this becomes the set of points representing the lowest set of points in the overall seafloor structure.

Algorithm 1 Hill Creation

```
1: Input: Mean vector m, Dimension vector d, 2D points P
  2: Output: Updated P with hill heights
  3: num\_hills \leftarrow numel(\mathbf{m}_x)
  4: H \leftarrow \text{Zeros tensor of size } (1, \text{numel}(\mathbf{P}_x))
 5: for i=1 to num_hills do
6: x_{\text{norm}} \leftarrow \frac{\frac{\pi}{2}(\mathbf{P}_x - \mathbf{m}_x[i])}{\mathbf{d}_x[i]}
            y_{\text{norm}} \leftarrow \frac{\frac{\pi}{2}(\mathbf{P}_y - \mathbf{m}_y[i])}{\mathbf{d}_y[i]}
  7:
           h_x \leftarrow \cos(x_{\text{norm}}) \cdot e^{\frac{|x_{\text{norm}}|}{10}}
           h_y \leftarrow \cos(y_{\text{norm}}) \cdot e^{\frac{|y_{\text{norm}}|}{10}}
  9:
            h \leftarrow \mathbf{d}_z[i] \cdot h_x \cdot h_y
10:
            Apply boundary conditions:
11:
            if x_{\text{norm}} > \frac{\pi}{2} or x_{\text{norm}} < -\frac{\pi}{2} or y_{\text{norm}} > \frac{\pi}{2} or y_{\text{norm}} < -\frac{\pi}{2} then
12:
13:
            end if
14:
            H \leftarrow H + h
15:
16: end for
17: \mathbf{P} \leftarrow \text{concatenate}([\mathbf{P}, H])
```

1.2 Scatterer Definition

The sea-floor is represented by a single object of the class ScattererClass.

```
Class Declaration
  template <typename T>
  class ScattererClass
  public:
      // members
      std::vector<std::vector<T>> coordinates;
      std::vector<T> reflectivity;
11
      // Constructor
      ScattererClass() {}
14
      // Constructor
      ScattererClass(std::vector<std::vector<T>> coordinates_arg,
                   std::vector<T>
                                   reflectivity_arg):
                    coordinates(std::move(coordinates_arg)),
18
                    reflectivity(std::move(reflectivity_arg)) {}
19
      // Save to CSV
```

```
void save_to_csv();

;
```

1.3 Sea-Floor Setup Script

Following is the function that will setup the sea-floor script.

```
void fSeaFloorSetup(ScattererClass<double>& scatterers){
      // auto save_files
                              {false};
                    save_files
                                           {false};
      const auto
                                           {true};
      const auto
                    hill_creation_flag
      // sea-floor bounds
             bed_width
                            {100.00};
      auto
      auto
             bed_length
                            {100.00};
      // creating tensors for coordinates and reflectivity
11
      vector<vector<double>>
                                   box_coordinates;
      vector<double>
                                   box_reflectivity;
14
      // scatter density
              bed_width_density {static_cast<double>( 10.00)};
      auto
16
              bed_length_density {static_cast<double>( 10.00)};
      auto
18
      // setting up coordinates
19
              xpoints
                         {linspace<double>(0.00,
      auto
20
                                         bed_width,
                                         bed_width * bed_width_density)};
22
              ypoints
                         {linspace<double>(0.00,
23
      auto
24
                                         bed_length,
                                         bed_length * bed_length_density)};
       if(save_files) fWriteVector(xpoints, "../csv-files/xpoints.csv");
                                                                           // verified
26
      if(save_files) fWriteVector(ypoints, "../csv-files/ypoints.csv");
                                                                           // verified
      // creating mesh
      auto [xgrid, ygrid] = meshgrid(std::move(xpoints), std::move(ypoints));
30
       if(save_files) fWriteMatrix(xgrid, "../csv-files/xgrid.csv"); // verified
31
      if(save_files) fWriteMatrix(ygrid, "../csv-files/ygrid.csv");
                                                                           // verified
33
      // reshaping
34
                     {reshape(xgrid, xgrid.size()*xgrid[0].size())};
      auto
              X
35
      auto
                     {reshape(ygrid, ygrid.size()*ygrid[0].size())};
       if(save_files) fWriteVector(X, "../csv-files/X.csv");
                                                                           // verified
37
                                           "../csv-files/Y.csv");
                                                                           // verified
      if(save_files) fWriteVector(Y,
38
39
      // creating heights of scatterers
      if(hill_creation_flag){
41
          // setting up hill parameters
                 num_hills
                               {10};
          // setting up placement of hills
                 points2D
                           {concatenate<0>(X, Y)};
                                                                               // verified
          auto
          auto
                 min2D
                                       {min<1, double>(points2D)};
                                                                              // verified
                                       {max<1, double>(points2D)};
                                                                               // verified
          auto
                 max2D
49
```

```
hill_2D_center
                                         \{\min 2D + \setminus
          auto
50
                                         rand({2, num_hills}) * (max2D - min2D)}; // verified
51
52
          // setup: hill-dimensions
                  hill_dimensions_min
                                        {transpose(vector<double>{5, 5, 2})); // verified
          auto
                                        {transpose(vector<double>{30, 30, 10})}; // verified
          auto
                  hill_dimensions_max
                                        {hill_dimensions_min + \
                 hill_dimensions
          auto
                                         rand({3, num_hills}) * (hill_dimensions_max -
                                             hill_dimensions_min)};
                                                                                   // verified
58
          // function-call: hill-creation function
59
          fCreateHills(hill_2D_center,
60
                      hill_dimensions,
                      points2D);
62
63
          // setting up floor reflectivity
          auto floorScatter_reflectivity
                                                {std::vector<double>(Y.size(), 1.00)};
66
          // populating the values of the incoming argument
67
          scatterers.coordinates = std::move(points2D);
68
          scatterers.reflectivity = std::move(floorScatter_reflectivity);
70
71
      else{
72
          // assigning flat heights
74
                         {std::vector<double>(Y.size(), 0)};
          auto
75
          // setting up floor coordinates
77
                  floorScatter_coordinates
78
          auto
                                                {concatenate<0>(X, Y, Z)};
          auto
                  floorScatter_reflectivity
                                                {std::vector<double>(Y.size(), 1)};
79
          // populating the values of the incoming argument
                                    = std::move(floorScatter_coordinates);
          scatterers.coordinates
82
          scatterers.reflectivity = std::move(floorScatter_reflectivity);
83
       }
85
   }
86
```

Chapter 2

Transmitter

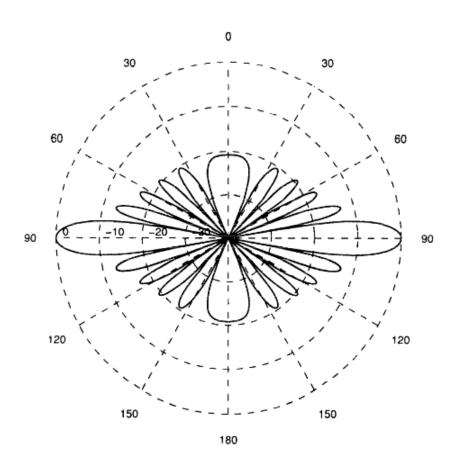


Figure 2.1: Beampattern of a Transmission Uniform Linear Array

Overview

Probing systems are those systems that send out a signal, listen to the reflection and infer qualitative and quantitative qualities of the environment, matter or object, it was trying to infer information about. The transmitter is one of the most fundamental components of probing systems. As the name suggests, the transmitter is the equipment responsible for sending out the probing signal into the medium.

A transmitter is any device or circuit that converts information into a signal and sends it out onto some media like air, cable, water or space. The components of a transmitter are usually as follows

- 1. Input: Information containing signal such as voice, data, video etc
- 2. Process: Encode/modulate the information onto a carrier signal, which can be electromagnetic wave or mechanical wave.
- 3. Transmission: The signal is then transmitted onto the media with electro-mechanical equipment.

Transmitters are of many kinds. But the ones that we will be considering will be directed transmitters, which means that these transmitters have an associated beampattern. To the uninitiated, this means that the power of the transmitted signal is not transmitted in all directions equally. A beampattern is a graphical representation of the power received by an ideal receiver when placed at different angles.

Transmitters made out of a linear-array of individual transmitters use beamforming to "direct" the major power of the transmitter. These kind of systems have well studied beampatterns which can be utilized in our simulations. These kind of studies and inculcating that in our pipelines produce accurate signal simulation pipelines. For now, we stick to a very simple model of a transmitter. We assume that the transmitter sends out the power equally into a particular cone from the AUV position.

2.1 Transmission Signal

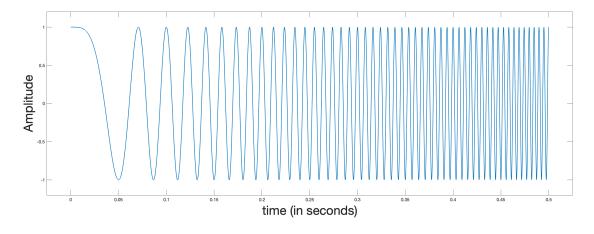


Figure 2.2: Linear Frequency Modulated Wave

The resolution of any probing system is fundamentally tied to the signal bandwidth. A higher bandwidth corresponds to finer resolution $\frac{\text{speed-of-sounds}}{2*\text{bandwidth}}$. Thus, for perfect resolution, an infinite bandwidth is in order. However, infinite bandwidth is impossible for obvious reasons: hardware limitations, spectral regulations, energy limitations and so on.

This is where Linear Frequency Modulation (LFM), also called a "chirp," becomes valuable. An LFM signal linearly sweeps a limited bandwidth over a relatively long duration. This technique spreads the signal's energy in time while retaining the resolution benefits of

the bandwidth. After matched filtering (or pulse compression), we essentially produce pulses corresponding to a base-band LFM of same bandwidth. Overall, LFM is a practical compromise between finite bandwidth and desired performance.

One of the best parts about the resolution depending only on the bandwidth is that it allows us to deploy techniques that would help us improve SNRs without virtually increasing the bandwidth at all. Much of the noise in submarine environments are in and around the baseband region (around frequency, 0). Since resolution depends purely on bandwidth, and LFM can be transmitted at a carrier-frequency, this means that processing the returns after low-pass filtering and basebanding allows us to get rid of the submarine noise, since they do not occupy the same frequency-coefficients. The end-result, thus, is improved SNR compared to use baseband LFM.

Due to all of these advantages, LFM waves are ubiquitous in probing systems, from sonar to radar. Thus, for this project too, the transmitter will be using LFM waves as probing signals, to probe the surrounding submarine environment.

2.2 Transmitter Class Definition

The transmitter is represented by a single object of the class TransmitterClass.

```
template <typename T>
   class TransmitterClass{
   public:
       // A shared pointer to the configuration object
5
       std::shared_ptr<svr::AUVParameters> config_ptr;
6
       // physical/intrinsic properties
8
       std::vector<T>
                         location;
                                               // location tensor
9
                         pointing_direction; // pointing direction
       std::vector<T>
10
11
       // basic parameters
12
       std::vector<T>
                                               // transmitted signal (LFM)
                         signal;
      Τ
                         azimuthal_angle;
                                               // transmitter's azimuthal pointing direction
      Т
                         elevation_angle;
                                               // transmitter's elevation pointing direction
      Т
                         azimuthal_beamwidth; // azimuthal beamwidth of transmitter
16
      Т
                         elevation_beamwidth; // elevation beamwidth of transmitter
17
      Τ
                         range;
                                               // a parameter used for spotlight mode.
18
       // transmitted signal attributes
20
      Т
                         f_low;
                                               // lowest frequency of LFM
21
      Т
                                               // highest frequency of LFM
                         f_high;
22
      Т
                                               // center frequency of LFM
23
                                               // bandwidth of LFM
      Т
                         bandwidth;
24
                         speed_of_sound {1500}; // speed of sound
25
       // shadowing properties
27
                         azimuthQuantDensity;
                                                   // quantization of angles along the
       int
28
          azimuth
                                                   // quantization of angles along the
       int
                         elevationQuantDensity;
          elevation
      Т
                                                   // range-cell size when shadowing
                         rangeQuantSize;
30
       Т
                         azimuthShadowThreshold; // azimuth thresholding
31
       Т
                         elevationShadowThreshold; // elevation thresholding
```

```
33
       // shadowing related
                                              // box indicating whether a scatter for a
      std::vector<T>
                         checkbox;
35
          range-angle pair has been found
      std::vector<std::vector<std::vector<T>>> finalScatterBox; // a 3D tensor where the
          third dimension represnets the vector length
      std::vector<T> finalReflectivityBox; // to store the reflectivity
37
       // constructor
      TransmitterClass() = default;
40
41
       // Deleting copy constructors/assignment
42
      TransmitterClass(const TransmitterClass& other)
                                                              = delete;
43
      TransmitterClass& operator=(TransmitterClass& other) = delete;
45
       // Creating move-constructor and move-assignment
46
      TransmitterClass(TransmitterClass&& other)
                                                               = default;
      TransmitterClass& operator=(TransmitterClass&& other) = default;
48
49
      // member-functions
50
      auto updatePointingAngle(std::vector<T> AUV_pointing_vector);
51
       auto subset_scatterers(const ScattererClass<T>& seafloor,
52
```

2.3 Transmitter Setup Scripts

The following script shows the setup-script

```
template <typename T>
   void fTransmitterSetup(TransmitterClass<T>& transmitter_fls,
                        TransmitterClass<T>& transmitter_portside,
                        TransmitterClass<T>& transmitter_starboard)
   {
       // Setting up transmitter
6
                                                           // sampling frequency
      Т
              sampling_frequency
                                    {160e3};
                                                           // first frequency of LFM
      Τ
              f1
                                    {50e3};
       Τ
              f2
                                    {70e3};
                                                           // second frequency of LFM
                                    {(f1 + f2)/2.00};
       Т
                                                           // finding center-frequency
10
       Т
              bandwidth
                                    {std::abs(f2 - f1)}; // bandwidth
11
              pulselength
                                    {5e-2};
                                                           // time of recording
       // building LFM
14
       auto
              timearray
                             {linspace<T>(0.00,}
                                         pulselength,
                                         std::floor(pulselength * sampling_frequency))};
17
       auto
              K
                             {f2 - f1/pulselength}; // calculating frequency-slope
18
                             {cos(2 * std::numbers::pi * \
19
       auto
              Signal
                              (f1 + K*timearray) * \
                              timearray)};
                                                    // frequency at each time-step, with f1
21
       // Setting up transmitter
       auto
            location
                                                {std::vector<T>(3, 0)};
                                                                             // location of
24
          transmitter
              azimuthal_angle_fls
                                                                              // initial
                                                {0};
          pointing direction
                                                {90};
                                                                              // initial
              azimuthal_angle_port
```

```
pointing direction
              azimuthal_angle_starboard
                                                                             // initial
                                               {-90};
          pointing direction
2.8
                                                                             // initial
              elevation_angle
                                               {-60};
29
          pointing direction
30
                                                                             // azimuthal
      Т
              azimuthal_beamwidth_fls
                                               {20};
          beamwidth of the signal cone
32
      Τ
              azimuthal_beamwidth_port
                                               {20};
                                                                             // azimuthal
          beamwidth of the signal cone
                                                                             // azimuthal
      Т
              azimuthal_beamwidth_starboard
                                               {20};
33
          beamwidth of the signal cone
                                                                             // elevation
              elevation_beamwidth_fls
                                               {20};
35
          beamwidth of the signal cone
              elevation_beamwidth_port
                                                                             // elevation
      Т
                                                {20};
          beamwidth of the signal cone
              elevation_beamwidth_starboard
                                                                              // elevation
37
      Т
                                               {20};
          beamwidth of the signal cone
              azimuthQuantDensity
                                               {10}; // number of points, a degree is split
39
          into quantization density along azimuth (used for shadowing)
                                               {10}; // number of points, a degree is split
              elevationQuantDensity
40
          into quantization density along elevation (used for shadowing)
              rangeQuantSize
                                               {10}; // the length of a cell (used for
41
          shadowing)
42
      Τ
              azimuthShadowThreshold
                                               {1};
                                                       // azimuth threshold
                                                                               (in degrees)
43
              elevationShadowThreshold
                                                       // elevation threshold (in degrees)
                                               {1};
44
45
      // transmitter-fls
47
      transmitter_fls.location
                                            = location;
                                                                             // Assigning
48
          location
      transmitter_fls.signal
                                           = Signal;
                                                                             // Assigning
          signal
      transmitter_fls.azimuthal_angle
                                           = azimuthal_angle_fls;
                                                                             // assigning
50
          azimuth angle
51
      transmitter_fls.elevation_angle
                                           = elevation_angle;
                                                                             // assigning
          elevation angle
      transmitter_fls.azimuthal_beamwidth = azimuthal_beamwidth_fls;
                                                                             // assigning
52
          azimuth-beamwidth
      transmitter_fls.elevation_beamwidth = elevation_beamwidth_fls;
                                                                             // assigning
          elevation-beamwidth
      // updating quantization densities
54
      transmitter_fls.azimuthQuantDensity
                                              = azimuthQuantDensity;
                                                                          // assigning
55
          azimuth quant density
      transmitter_fls.elevationQuantDensity = elevationQuantDensity;
                                                                          // assigning
56
          elevation quant density
                                              = rangeQuantSize;
                                                                          // assigning
57
      transmitter_fls.rangeQuantSize
          range-quantization
      transmitter_fls.azimuthShadowThreshold = azimuthShadowThreshold; //
58
          azimuth-threshold in shadowing
      transmitter_fls.elevationShadowThreshold = elevationShadowThreshold; //
          elevation-threshold in shadowing
      // signal related
60
      transmitter_fls.f_low
                                              = f1;
                                                             // assigning lower frequency
61
      transmitter_fls.f_high
                                               = f2;
                                                             // assigning higher frequency
62
```

```
transmitter_fls.fc
                                                              // assigning center frequency
                                               = fc;
63
                                               = bandwidth; // assigning bandwidth
       transmitter_fls.bandwidth
64
65
66
       // transmitter-portside
67
       transmitter_portside.location
                                                                                // Assigning
                                                   = location;
68
           location
       transmitter_portside.signal
                                                   = Signal;
                                                                                // Assigning
69
           signal
70
       transmitter_portside.azimuthal_angle
                                                   = azimuthal_angle_port;
                                                                                // assigning
           azimuth angle
       transmitter_portside.elevation_angle
                                                   = elevation_angle;
                                                                                // assigning
71
           elevation angle
       transmitter_portside.azimuthal_beamwidth = azimuthal_beamwidth_port; // assigning
72
           azimuth-beamwidth
       transmitter_portside.elevation_beamwidth = elevation_beamwidth_port; // assigning
           elevation-beamwidth
       // updating quantization densities
74
       transmitter_portside.azimuthQuantDensity = azimuthQuantDensity;
                                                                                // assigning
75
           azimuth quant density
       transmitter_portside.elevationQuantDensity = elevationQuantDensity;
                                                                                // assigning
           elevation quant density
                                                 = rangeQuantSize;
       transmitter_portside.rangeQuantSize
                                                                                // assigning
           range-quantization
       transmitter_portside.azimuthShadowThreshold = azimuthShadowThreshold; //
           azimuth-threshold in shadowing
       transmitter_portside.elevationShadowThreshold = elevationShadowThreshold; //
79
           elevation-threshold in shadowing
       // signal related
80
       transmitter_portside.f_low
81
                                                   = f1;
                                                                                // assigning
           lower frequency
       transmitter_portside.f_high
                                                   = f2;
                                                                                // assigning
           higher frequency
                                                                                // assigning
       transmitter_portside.fc
                                                   = fc;
83
           center frequency
       transmitter_portside.bandwidth
                                                  = bandwidth;
                                                                                // assigning
           bandwidth
85
86
       // transmitter-starboard
       transmitter_starboard.location
                                                      = location;
                                                                                    //
88
           assigning location
       transmitter_starboard.signal
                                                      = Signal;
                                                                                    //
89
           assigning signal
       transmitter_starboard.azimuthal_angle
                                                      = azimuthal_angle_starboard; //
90
           assigning azimuthal signal
       transmitter_starboard.elevation_angle
                                                      = elevation_angle;
91
       transmitter_starboard.azimuthal_beamwidth
                                                      = azimuthal_beamwidth_starboard;
92
       transmitter_starboard.elevation_beamwidth
                                                      = elevation_beamwidth_starboard;
93
       // updating quantization densities
94
       transmitter_starboard.azimuthQuantDensity
                                                                                     //
95
                                                      = azimuthQuantDensity;
           assigning azimuth-quant-density
       transmitter_starboard.elevationQuantDensity
                                                      = elevationQuantDensity;
96
       transmitter_starboard.rangeQuantSize
                                                      = rangeQuantSize;
97
       transmitter_starboard.azimuthShadowThreshold = azimuthShadowThreshold;
98
       transmitter_starboard.elevationShadowThreshold = elevationShadowThreshold;
99
       // signal related
100
       transmitter_starboard.f_low
                                                                                     //
                                                      = f1;
101
           assigning lower frequency
```

```
transmitter_starboard.f_high
                                                      = f2;
                                                                                     //
102
           assigning higher frequency
       transmitter_starboard.fc
                                                      = fc;
103
           assigning center frequency
       transmitter_starboard.bandwidth
                                                      = bandwidth;
                                                                                     //
104
           assigning bandwidth
105
   }
106
```

Chapter 3

Uniform Linear Array

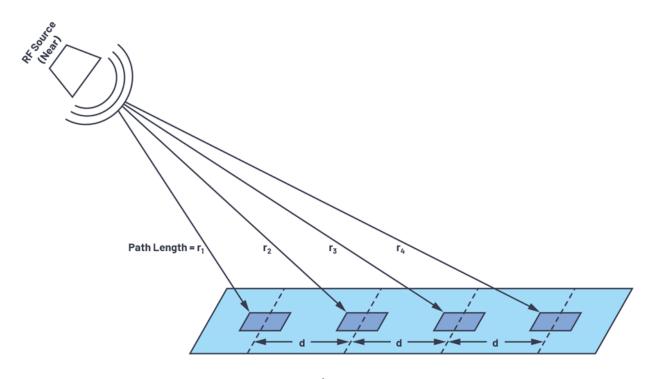


Figure 3.1: Uniform Linear Array

Overview

A Uniform Linear Array (ULA) is a common antenna or sensor configuration in which multiple elements are arranged in a straight line with equal spacing between adjacent elements. This geometry simplifies both the analysis and implementation of array signal processing techniques. In a ULA, each element receives a version of the incoming signal that differs only in phase, depending on the angle of arrival. This phase difference can be exploited to steer the array's beam in a desired direction (beamforming) or to estimate the direction of arrival (DOA) of multiple sources. The equal spacing also leads to a regular phase progression across the elements, which makes the array's response mathematically tractable and allows the use of tools like the discrete Fourier transform (DFT) to analyze spatial frequency content.

The performance of a ULA depends on the number of elements and their spacing. The spacing is typically chosen to be half the wavelength of the signal to avoid spatial aliasing, also called grating lobes, which can introduce ambiguities in DOA estimation. Increasing the number of elements improves the array's angular resolution and directivity, meaning it can better distinguish closely spaced sources and focus energy more narrowly. ULAs are widely used in radar, sonar, wireless communications, and microphone arrays due to their simplicity, predictable behavior, and compatibility with well-established signal processing algorithms. Their linear structure also makes them easier to implement in hardware compared to more complex array geometries like circular or planar arrays.

3.1 ULA Class Definition

The following is the class used to represent the uniform linear array

```
template <typename T>
  class ULAClass
   public:
      // intrinsic parameters
      std::size_t
                                                                                   // number
                                           num_sensors;
          of sensors
                                   inter_element_spacing;
                                                                            // space between
          sensors
      std::vector<std::vector<T>> coordinates;
                                                                            // coordinates
          of each sensor
                                    sampling_frequency;
                                                                            // sampling
9
          frequency of the sensors
                                   recording_period;
                                                                            // recording
10
          period of the ULA
      std::vector<T>
                                                                            // location of
                                    location;
11
          first coordinate
      // derived
      std::vector<T>
                                    sensor_direction;
14
      std::vector<std::vector<T>> signal_matrix;
      // decimation related
17
                                                                    // the new decimation
      int
                        decimation_factor;
18
          factor
                                                                    // the new sampling
                         post_decimation_sampling_frequency;
          frequency
                         lowpass_filter_coefficients_for_decimation; // filter-coefficients
      std::vector<T>
20
          for filtering
21
      // imaging related
22
      T range_resolution;
                                       // theoretical range-resolution = $\frac{c}{2B}$
23
      T azimuthal_resolution;
                                       // theoretical azimuth-resolution =
          $\frac{\lambda}{(N-1)*inter-element-distance}$
      T range_cell_size;
                                       // the range-cell quanta we're choosing for
          efficiency trade-off
         azimuth_cell_size;
                                       // the azimuth quanta we're choosing
26
      std::vector<T> azimuth_centers; // tensor containing the azimuth centeres
      std::vector<T> range_centers; // tensor containing the range-centers
28
                                       // the frame-size corresponding to a range cell in a
      int frame_size;
29
          decimated signal matrix
30
```

```
std::vector<std::vector<complex<T>>> mulFFTMatrix; // the matrix containing the
          delays for each-element as a slot
                                            matchFilter; // torch tensor containing the
      std::vector<complex<T>>
32
          match-filter
      int num_buffer_zeros_per_frame;
                                                          // number of zeros we're adding
33
          per frame to ensure no-rotation
      std::vector<std::vector<T>> beamformedImage;
                                                          // the beamformed image
34
                                                          // the cartesian version of
      std::vector<std::vector<T>> cartesianImage;
35
          beamformed image
36
      // Artificial acoustic-image related
37
      std::vector<std::vector<T>> currentArtificialAcousticImage; // acoustic image
38
          directly produced
39
40
      // Basic Constructor
41
      ULAClass() = default;
42
43
      // constructor
44
      ULAClass(const int
                            num_sensors_arg,
45
               const auto
                           inter_element_spacing_arg,
               const auto& coordinates_arg,
47
               const auto& sampling_frequency_arg,
48
               const auto& recording_period_arg,
               const auto& location_arg,
               const auto& signalMatrix_arg,
51
               const auto& lowpass_filter_coefficients_for_decimation_arg):
52
                 num_sensors(num_sensors_arg),
                  inter_element_spacing(inter_element_spacing_arg),
                  coordinates(std::move(coordinates_arg)),
55
                  sampling_frequency(sampling_frequency_arg),
56
                  recording_period(recording_period_arg),
                  location(std::move(location_arg)),
58
                  signal_matrix(std::move(signalMatrix_arg)),
59
                  lowpass_filter_coefficients_for_decimation(std::move(lowpass_filter_coefficients_for_decimation)
60
      {
61
62
          // calculating ULA direction
63
          sensor_direction = std::vector<T>{coordinates[1][0] - coordinates[0][0],
                                            coordinates[1][1] - coordinates[0][1],
                                            coordinates[1][2] - coordinates[0][2]};
66
67
          // normalizing
68
                                    {std::norm(std::inner_product(sensor_direction.begin(),
          auto norm_value_temp
                                                                sensor_direction.end(),
70
                                                                sensor_direction.begin(),
                                                                0.00));
          // dividing
74
          if (norm_value_temp != 0) {sensor_direction = sensor_direction /
              norm_value_temp;}
      }
77
78
      // // deleting copy constructor/assignment
79
      // ULAClass<T>(const ULAClass<T>& other)
                                                                 = delete;
80
      // ULAClass<T>& operator=(const ULAClass<T>& other)
                                                                 = delete;
81
      ULAClass<T>(ULAClass<T>&& other)
                                                              = delete;
82
      ULAClass<T>& operator=(const ULAClass<T>& other)
                                                              = default;
```

```
84
      // member-functions
85
              buildCoordinatesBasedOnLocation();
      void
86
      void
              buildCoordinatesBasedOnLocation(const std::vector<T>& new_location);
87
      void
              init(const TransmitterClass<T>& transmitterObj);
88
              nfdc_CreateMatchFilter(const TransmitterClass<T>& transmitterObj);
      void
      void
              simulate_signals(const ScattererClass<T>& seafloor,
90
                              const std::vector<std::size_t> scatterer_indices,
```

3.2 ULA Setup Scripts

The following script shows the setup-script for Uniform Linear Arrays

```
template <typename T>
  void fULASetup(ULAClass<T>& ula_fls,
                 ULAClass<T>&
                                ula_portside,
                 ULAClass<T>&
                                ula_starboard)
   {
5
      // setting up ula
6
      auto
              num_sensors
                                        {static_cast<int>(32)};
                                                                         // number of sensors
              sampling_frequency
                                        {static_cast<T>(160e3)};
                                                                         // sampling frequency
8
              inter_element_spacing
                                        {1500/(2*sampling_frequency)};
                                                                         // space between
9
          samples
                                        {10e-2};
      Т
              recording_period
                                                                         // sampling-period
10
      // building the direction for the sensors
              ULA_direction
                                        {std::vector<T>({-1, 0, 0})};
13
      auto
      auto
              ULA_direction_norm
                                        {norm(ULA_direction)};
                                        {ULA_direction = ULA_direction/ULA_direction_norm;}
      if (ULA_direction_norm != 0)
      ULA_direction
                                        ULA_direction * inter_element_spacing;
16
17
      // building coordinates for sensors
            ULA_coordinates
                                        {transpose(ULA_direction) * \
19
                                         linspace<double>(0.00,
2.0
                                                         num_sensors -1,
                                                         num_sensors)};
23
       // coefficients of decimation filter
24
              lowpassfiltercoefficients {std::vector<T>{0.0000, 0.0000, 0.0000, 0.0000,
          0.0000, 0.0000, 0.0001, 0.0003, 0.0006, 0.0015, 0.0030, 0.0057, 0.0100, 0.0163,
          0.0251, 0.0364, 0.0501, 0.0654, 0.0814, 0.0966, 0.1093, 0.1180, 0.1212, 0.1179,
          0.1078, 0.0914, 0.0699, 0.0451, 0.0192, -0.0053, -0.0262, -0.0416, -0.0504,
          -0.0522, -0.0475, -0.0375, -0.0239, -0.0088, 0.0057, 0.0179, 0.0263, 0.0303,
          0.0298, 0.0253, 0.0177, 0.0086, -0.0008, -0.0091, -0.0153, -0.0187, -0.0191,
          -0.0168, -0.0123, -0.0065, -0.0004, 0.0052, 0.0095, 0.0119, 0.0125, 0.0112,
          0.0084,\ 0.0046,\ 0.0006,\ -0.0031,\ -0.0060,\ -0.0078,\ -0.0082,\ -0.0075,\ -0.0057,
          -0.0033, -0.0006, 0.0019, 0.0039, 0.0051, 0.0055, 0.0050, 0.0039, 0.0023, 0.0005,
          -0.0012, -0.0025, -0.0034, -0.0036, -0.0034, -0.0026, -0.0016, -0.0004, 0.0007,
          0.0016, 0.0022, 0.0024, 0.0023, 0.0018, 0.0011, 0.0003, -0.0004, -0.0011,
          -0.0015, -0.0016, -0.0015}};
      // assigning values
2.7
      ula_fls.num_sensors
                                                                                     //
                                                       = num sensors:
2.8
          assigning number of sensors
       ula_fls.inter_element_spacing
                                                       = inter_element_spacing;
          assigning inter-element spacing
```

```
ula_fls.coordinates
                                                       = ULA_coordinates;
                                                                                     //
           assigning ULA coordinates
      ula_fls.sampling_frequency
                                                       = sampling_frequency;
                                                                                     11
31
           assigning sampling frequencys
      ula_fls.recording_period
                                                       = recording_period;
                                                                                     //
           assigning recording period
      ula_fls.sensor_direction
                                                       = ULA_direction;
                                                                                     // ULA
33
          direction
      ula_fls.lowpass_filter_coefficients_for_decimation = lowpassfiltercoefficients; //
           storing coefficients
35
36
      // assigning values
37
                                                                                         //
      ula_portside.num_sensors
                                                           = num_sensors;
38
           assigning number of sensors
      ula_portside.inter_element_spacing
                                                           = inter_element_spacing;
                                                                                         //
39
           assigning inter-element spacing
      ula_portside.coordinates
                                                           = ULA_coordinates;
40
           assigning ULA coordinates
      ula_portside.sampling_frequency
                                                           = sampling_frequency;
                                                                                         //
           assigning sampling frequencys
      ula_portside.recording_period
                                                           = recording_period;
                                                                                         //
42
          assigning recording period
      ula_portside.sensor_direction
                                                           = ULA_direction;
                                                                                         //
43
          ULA direction
      ula_portside.lowpass_filter_coefficients_for_decimation = lowpassfiltercoefficients;
44
          // storing coefficients
45
46
      // assigning values
47
      ula_starboard.num_sensors
                                                                                            //
                                                               = num_sensors;
           assigning number of sensors
      ula_starboard.inter_element_spacing
                                                               = inter_element_spacing;
           assigning inter-element spacing
      ula_starboard.coordinates
                                                              = ULA_coordinates;
                                                                                             //
50
           assigning ULA coordinates
      ula_starboard.sampling_frequency
                                                               = sampling_frequency;
51
           assigning sampling frequencys
      ula_starboard.recording_period
                                                               = recording_period;
                                                                                            //
          assigning recording period
      ula_starboard.sensor_direction
                                                               = ULA_direction;
                                                                                             //
53
          ULA direction
      ula_starboard.lowpass_filter_coefficients_for_decimation =
54
          lowpassfiltercoefficients; // storing coefficients
   }
```

Chapter 4

Autonomous Underwater Vehicle

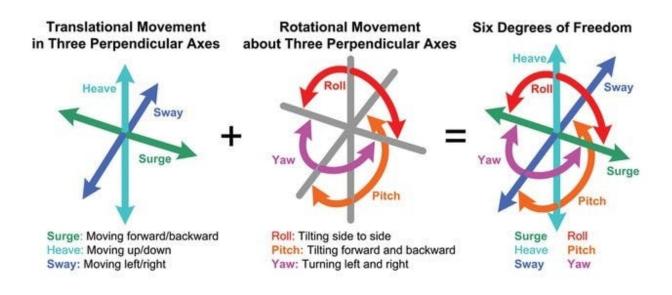


Figure 4.1: AUV degrees of freedom

Overview

Autonomous Underwater Vehicles (AUVs) are robotic systems designed to operate underwater without direct human control. They navigate and perform missions independently using onboard sensors, processors, and preprogrammed instructions. They are widely used in oceanographic research, environmental monitoring, offshore engineering, and military applications. AUVs can vary in size from small, portable vehicles for shallow water surveys to large, torpedo-shaped platforms capable of deep-sea exploration. Their autonomy allows them to access environments that are too dangerous, remote, or impractical for human divers or tethered vehicles.

The navigation and sensing systems of AUVs are critical to their performance. They typically use a combination of inertial measurement units (IMUs), Doppler velocity logs

(DVLs), pressure sensors, magnetometers, and sometimes acoustic positioning systems to estimate their position and orientation underwater. Since GPS signals do not penetrate water, AUVs must rely on these onboard sensors and occasional surfacing for GPS fixes. They are often equipped with sonar systems, cameras, or other scientific instruments to collect data about the seafloor, water column, or underwater structures. Advanced AUVs can also implement adaptive mission planning and obstacle avoidance, enabling them to respond to changes in the environment in real time.

The applications of AUVs are diverse and expanding rapidly. In scientific research, they are used for mapping the seafloor, studying marine life, and monitoring oceanographic parameters such as temperature, salinity, and currents. In the commercial sector, AUVs inspect pipelines, subsea infrastructure, and offshore oil platforms. Military and defense applications include mine countermeasure operations and underwater surveillance. The development of AUVs continues to focus on increasing endurance, improving autonomy, enhancing sensor payloads, and reducing costs, making them a key technology for exploring and understanding the underwater environment efficiently and safely.

4.1 AUV Class Definition

The following is the class used to represent the uniform linear array

```
template <typename T>
2 class AUVClass{
g public:
      // Intrinsic attributes
      std::vector<T> location;
                                             // location of vessel
      std::vector<T>
                       velocity;
                                             // velocity of the vessel
7
      std::vector<T> acceleration;
                                             // acceleration of vessel
8
      std::vector<T> pointing_direction; // AUV's pointing direction
Q
10
      // uniform linear-arrays
11
                                             // front-looking SONAR ULA
      ULAClass<T> ULA_fls;
      ULAClass<T>
                                             // mounted ULA [object of class, ULAClass]
                        ULA_portside;
                                             // mounted ULA [object of class, ULAClass]
      ULAClass<T>
                       ULA_starboard;
      // transmitters
16
      TransmitterClass<T> transmitter_fls;
                                                    // transmitter for front-looking SONAR
17
      TransmitterClass<T> transmitter_portside;
                                                    // portside transmitter
      TransmitterClass<T> transmitter_starboard; // starboard transmitter
19
2.0
      // derived or dependent attributes
21
                                                             // matrix containing the
      std::vector<std::vector<T>> signalMatrix_1;
          signals obtained from ULA_1
      std::vector<std::vector<T>> largeSignalMatrix_1;
                                                             // matrix holding signal of
          synthetic aperture
      std::vector<std::vector<T>> beamformedLargeSignalMatrix; // each column is the
          beamformed signal at each stop-hop
25
      // plotting mode
26
      bool plottingmode; // to suppress plotting associated with classes
27
28
      // spotlight mode related
29
      std::vector<std::vector<T>> absolute_coords_patch_cart; // cartesian coordinates of
```

```
patch
31
      // Synthetic Aperture Related
32
      std::vector<std::vector<T>> ApertureSensorLocations; // sensor locations of
33
         aperture
      // functions
35
      void syncComponentAttributes();
      void init(svr::ThreadPool& thread_pool);
      void simulate_signal(const ScattererClass<T>& seafloor,
38
                       svr::ThreadPool&
                                               thread_pool);
39
      void subset_scatterers(const ScattererClass<T>& seafloor,
40
                         svr::ThreadPool&
                                                thread_pool,
41
                         std::vector<std::size_t>& fls_scatterer_indices,
42
                         std::vector<std::size_t>& portside_scatterer_indices,
43
                         std::vector<std::size_t>& starboard_scatterer_indices);
      void step(T time_step);
46
  };
47
48
  /*----
  Aim: update attributes
50
51
  template <typename T>
```

4.2 AUV Setup Scripts

The following script shows the setup-script for Uniform Linear Arrays

```
template <typename T>
  void fAUVSetup(AUVClass<T>& auv) {
      // building properties for the auv
             location
                                  {std::vector<T>{0, 50, 30}};
                                                                   // starting location
      auto
                                  {std::vector<T>{5, 0, 0}};
                                                                   // starting velocity
             velocity
      auto
      auto
             pointing_direction {std::vector<T>{1, 0, 0}};
                                                                   // pointing direction
      // assigning
      auv.location
                           = std::move(location);
                                                               // assigning location
      auv.velocity
                           = std::move(velocity);
                                                               // assigning velocity
11
      auv.pointing_direction = std::move(pointing_direction); // assigning pointing
          direction
  }
```

Part II Signal Simulation Pipeline

Part III Imaging Pipeline

Part IV Perception & Control Pipeline

Appendix A

General Purpose Templated Functions

A.1 CSV File-Writes

```
#pragma once
2 /*----
 writing the contents of a vector a csv-file
  template <typename T>
  void fWriteVector(const vector<T>& inputvector,
                  const string&
                                            filename){
      // opening a file
      std::ofstream fileobj(filename);
      if (!fileobj) {return;}
11
      // writing the real parts in the first column and the imaginary parts int he second
      if constexpr(std::is_same_v<T, std::complex<double>> ||
14
                 std::is_same_v<T, std::complex<float>> ||
                 std::is_same_v<T, std::complex<long double>>){
         for(int i = 0; i<inputvector.size(); ++i){</pre>
17
             // adding entry
             fileobj << inputvector[i].real() << "+" << inputvector[i].imag() << "i";</pre>
             // adding delimiter
             if(i!=inputvector.size()-1) {fileobj << ",";}</pre>
                                     {fileobj << "\n";}
             else
      else{
         for(int i = 0; i<inputvector.size(); ++i){</pre>
             fileobj << inputvector[i];</pre>
             if(i!=inputvector.size()-1) {fileobj << ",";}</pre>
                                     {fileobj << "\n";}
30
      // return
35
      return;
```

```
writing the contents of a matrix to a csv-file
   template <typename T>
40
   auto fWriteMatrix(const std::vector<std::vector<T>> inputMatrix,
41
                   const string
                                                   filename){
42
      // opening a file
44
      std::ofstream fileobj(filename);
      // writing
      if (fileobj){
48
          for(int i = 0; i<inputMatrix.size(); ++i){</pre>
49
              for(int j = 0; j<inputMatrix[0].size(); ++j){</pre>
                  fileobj << inputMatrix[i][j];</pre>
51
                  if (j!=inputMatrix[0].size()-1) {fileobj << ",";}</pre>
                  else
                                                   {fileobj << "\n";}
              }
          }
55
56
      else{
          cout << format("File-write to {} failed\n", filename);</pre>
59
60
61 }
   /*-----
   writing complex-matrix to a csv-file
63
64
65 template <>
   auto fWriteMatrix(const std::vector<std::vector<std::complex<double>>> inputMatrix,
67
                    const string
68
      // opening a file
69
       std::ofstream fileobj(filename);
70
71
      // writing
72
       if (fileobj){
          for(int i = 0; i<inputMatrix.size(); ++i){</pre>
              for(int j = 0; j<inputMatrix[0].size(); ++j){</pre>
                  fileobj << inputMatrix[i][j].real() << "+" << inputMatrix[i][j].imag() <<</pre>
                  if (j!=inputMatrix[0].size()-1) {fileobj << ",";}</pre>
                                                   {fileobj << "\n";}
                  else
78
              }
79
          }
       }
81
       else{
82
          cout << format("File-write to {} failed\n", filename);</pre>
83
   }
85
```

A.2 abs

```
#include <vector>
                  // for vectors
  #include <algorithm> // for std::transform
  /*-----
  y = abs(vector)
  -----*/
  template <typename T>
  auto abs(const std::vector<T>& input_vector)
     // creating canvas
     auto canvas {input_vector};
     // calculating abs
     std::transform(canvas.begin(),
                canvas.end(),
19
                canvas.begin(),
                [](auto& argx){return std::abs(argx);});
22
     // returning
23
     return std::move(canvas);
25 }
  /*-----
26
  y = abs(matrix)
  template <typename T>
  auto abs(const std::vector<std::vector<T>> input_matrix)
30
31 {
     // creating canvas
     auto canvas {input_matrix};
34
     // applying element-wise abs
     std::transform(input_matrix.begin(),
                input_matrix.end(),
                input_matrix.begin(),
38
                [](auto& argx){return std::abs(argx);});
30
     // returning
41
     return std::move(canvas);
42
  }
```

A.3 Boolean Comparators

```
return argx < static_cast<T>(scalar);
15
                 });
16
17
     // returning
18
     return std::move(canvas);
19
20 }
  /*-----
21
  template <typename T, typename U>
  auto operator<=(const std::vector<T>& input_vector,
24
              const
                                    scalar)
25
26 {
     // creating canvas
27
     auto canvas {std::vector<bool>(input_vector.size())};
28
29
     // transforming
30
     std::transform(input_vector.begin(), input_vector.end(),
31
                 canvas.begin(),
32
                 [&scalar](const auto& argx){
33
                    return argx <= static_cast<T>(scalar);
                 });
36
     // returning
37
     return std::move(canvas);
38
  }
39
  // -----
40
41 template <typename T, typename U>
42 auto operator>(const std::vector<T>& input_vector,
             const U
                                   scalar)
43
44
     // creating canvas
45
     auto canvas
                   {std::vector<bool>(input_vector.size())};
     // transforming
48
     std::transform(input_vector.begin(), input_vector.end(),
49
                 canvas.begin(),
                 [&scalar](const auto& argx){
51
                    return argx > static_cast<T>(scalar);
                });
55
     // returning
     return std::move(canvas);
56
57 }
-----*/
59
  template <typename T, typename U>
60
  auto operator>=(const std::vector<T>& input_vector,
61
              const
                                    scalar)
63
     // creating canvas
64
     auto canvas {std::vector<bool>(input_vector.size())};
65
     // transforming
67
     std::transform(input_vector.begin(), input_vector.end(),
                 canvas.begin(),
                 [&scalar](const auto& argx){
                    return argx >= static_cast<T>(scalar);
71
                });
72
```

```
// returning
return std::move(canvas);
// returning
// return std::move(canvas);
// returning
// returni
```

A.4 Concatenate Functions

```
#pragma once
  /*----
  input = [vector, vector],
  output = [vector]
6 template <std::size_t axis, typename T>
  auto concatenate(const std::vector<T>& input_vector_A,
                const std::vector<T>& input_vector_B) -> std::enable_if_t<axis == 1,</pre>
                    std::vector<T> >
9
      // creating canvas vector
10
      auto
            num_elements {input_vector_A.size() + input_vector_B.size()};
11
                         {std::vector<T>(num_elements, (T)0) };
      auto
      // filling up the canvas
      std::copy(input_vector_A.begin(), input_vector_A.end(),
              canvas.begin());
      std::copy(input_vector_B.begin(), input_vector_B.end(),
17
              canvas.begin()+input_vector_A.size());
18
19
      // moving it back
20
      return std::move(canvas);
22
23 }
  /*-----
  input = [vector, vector],
  output = [matrix]
26
  -----*/
27
 template <std::size_t axis, typename T>
  auto concatenate(const std::vector<T>& input_vector_A,
                const std::vector<T>&
                                     input_vector_B) -> std::enable_if_t<axis == 0,</pre>
30
                    std::vector<std::vector<T>> >
31
      // throwing error dimensions
32
      if (input_vector_A.size() != input_vector_B.size())
33
         std::cerr << "concatenate:: incorrect dimensions \n";</pre>
      // creating canvas
36
           canvas
                     {std::vector<std::vector<T>>(
      auto
37
         2, std::vector<T>(input_vector_A.size())
      )};
40
      \ensuremath{//} filling up the dimensions
41
      std::copy(input_vector_A.begin(), input_vector_A.end(), canvas[0].begin());
      std::copy(input_vector_B.begin(), input_vector_B.end(), canvas[1].begin());
43
      // moving it back
      return std::move(canvas);
  }
48
```

```
/*----
  input = [vector, vector, vector],
  output = [matrix]
51
52
  template <std::size_t axis, typename T>
  auto concatenate(const std::vector<T>& input_vector_A,
                const std::vector<T>& input_vector_B,
55
                const std::vector<T>& input_vector_C) -> std::enable_if_t<axis == 0,</pre>
56
                   std::vector<std::vector<T>> >
57
      // throwing error dimensions
58
      if (input_vector_A.size() != input_vector_B.size() ||
59
         input_vector_A.size() != input_vector_C.size())
         std::cerr << "concatenate:: incorrect dimensions \n";</pre>
62
      // creating canvas
63
      auto
          canvas {std::vector<std::vector<T>>(
         3, std::vector<T>(input_vector_A.size())
65
      )};
66
67
      // filling up the dimensions
      std::copy(input_vector_A.begin(), input_vector_A.end(), canvas[0].begin());
      std::copy(input_vector_B.begin(), input_vector_B.end(), canvas[1].begin());
70
      std::copy(input_vector_C.begin(), input_vector_C.end(), canvas[2].begin());
      // moving it back
73
      return std::move(canvas);
74
75
76
 /*----
77
78 input = [matrix, vector],
  output = [matrix]
  -----*/
  template <std::size_t axis, typename T>
81
  auto concatenate(const std::vector<std::vector<T>>& input_matrix,
                const std::vector<T>
                                               input_vector) -> std::enable_if_t<axis</pre>
83
                   == 0, std::vector<std::vector<T>> >
84
      // creating canvas
85
      auto canvas
                    {input_matrix};
87
      // adding to the canvas
88
      canvas.push_back(input_vector);
89
      // returning
91
     return std::move(canvas);
92
  }
93
```

A.5 Conjugate

A.6 Convolution

```
#pragma once
  namespace svr {
      /*-----
      1D convolution of two vectors
      > implemented through fft
      template <typename T1, typename T2>
      auto conv1D(const std::vector<T1>& input_vector_A,
                  const std::vector<T2>& input_vector_B)
11
         // resulting type
         using T3 = decltype(std::declval<T1>() * std::declval<T2>());
         // creating canvas
         auto canvas_length
                                {input_vector_A.size() + input_vector_B.size() - 1};
         // calculating fft of two arrays
         auto
                fft_A
                          {svr::fft(input_vector_A, canvas_length)};
         auto
                fft_B
                          {svr::fft(input_vector_B, canvas_length)};
         // element-wise multiplying the two matrices
                         {fft_A * fft_B};
         auto fft_AB
         // finding inverse FFT
         auto convolved_result {ifft(fft_AB)};
         // returning
         return std::move(convolved_result);
29
      }
30
      template <>
32
      auto conv1D(const std::vector<double>& input_vector_A,
33
                 const std::vector<double>& input_vector_B)
         // creating canvas
36
               canvas_length
                                 {input_vector_A.size() + input_vector_B.size() - 1};
         auto
         // calculating fft of two arrays
         auto
               \mathtt{fft}_{-}\mathtt{A}
                         {svr::fft(input_vector_A, canvas_length)};
40
```

```
{svr::fft(input_vector_B, canvas_length)};
         auto
               fft_B
         // element-wise multiplying the two matrices
43
               fft_AB
                       \{fft_A * fft_B\};
         auto
44
         // finding inverse FFT
               convolved_result {ifft(fft_AB)};
         // returning
         return std::move(convolved_result);
50
51
52
      /*-----
53
      1D convolution of two vectors
54
      > implemented through fft
55
56
      template <typename T1, typename T2>
      auto conv1D_fftw(const std::vector<T1>& input_vector_A,
58
                     const std::vector<T2>& input_vector_B)
59
60
      {
         // resulting type
         using T3 = decltype(std::declval<T1>() * std::declval<T2>());
62
63
         // creating canvas
                               {input_vector_A.size() + input_vector_B.size() - 1};
         auto canvas_length
66
         // calculating fft of two arrays
67
         auto fft_A {svr::fft(input_vector_A, canvas_length)};
         auto
               {\tt fft}_{\tt B}
                         {svr::fft(input_vector_B, canvas_length)};
70
         \ensuremath{//} element-wise multiplying the two matrices
71
         auto fft_AB
                       \{fft_A * fft_B\};
         // finding inverse FFT
74
         auto convolved_result {svr::ifft(fft_AB, fft_AB.size())};
75
         // returning
77
         return std::move(convolved_result);
78
      }
79
      /*-----
81
      Long-signal Conv1D
82
      improvements:
83
        > make an inplace version of this
      -----*/
85
      template <std::size_t L, typename T>
86
      auto conv1D_long(const std::vector<T>& input_vector_A,
87
                      const std::vector<T>& input_vector_B)
89
         // fetching dimensions
90
                                   {std::max(input_vector_A.size(),
91
         const auto maxlength
                                           input_vector_B.size())};
         const auto filter_size {std::min(input_vector_A.size(),
93
                                           input_vector_B.size())};
                                  {L + filter_size - 1};
         const auto block_size
               auto
                     num_blocks
                                   {2 + static_cast<std::size_t>(
96
         const
            (maxlength - block_size)/L
         )};
98
```

```
// obtaining references
100
           const auto& large_vector
                                        {input_vector_A.size() >= input_vector_B.size() ? \
101
                                         input_vector_A
                                                             : input_vector_B};
                  auto& small_vector
                                        {input_vector_A.size() < input_vector_B.size() ? \</pre>
           const
103
                                         input_vector_A
                                                            : input_vector_B};
104
           // setup
106
                                        {static_cast<std::size_t>(0)};
           auto
107
                  starting_index
                                        {static_cast<std::size_t>(0)};
           auto
                  ending_index
           auto
                  length_left_to_fill
                                        {ending_index - starting_index};
109
           auto
                 canvas
                                        {std::vector<double>(block_size, 0)};
                 finaloutput
                                        {std::vector<double>(maxlength, 0)};
           auto
111
           auto
                  block_conv_output_size {L + 2 * filter_size -2};
                 block_conv_output
                                        {std::vector<double>(block_conv_output_size, 0)};
113
           auto
114
           // block-wise processing
           for(auto bid = 0; bid < num_blocks; ++bid)</pre>
116
117
              // estimating indices
118
              starting_index
                                        L*bid;
119
              ending_index
                                        std::min(starting_index + block_size - 1,maxlength -
120
                  1);
              length_left_to_fill = ending_index - starting_index;
121
              // copying to the common-block
              std::copy(large_vector.begin() + starting_index,
124
                       large_vector.begin() + ending_index + 1,
                       canvas.begin());
126
127
              // performing convolution
128
              block_conv_output = svr::conv1D_fftw(canvas,
129
                                                    small_vector);
130
131
              // discarding edges and writing values
              std::copy(block_conv_output.begin() + filter_size-2,
133
                       block_conv_output.begin() + filter_size-2 +
                           std::min(static_cast<int>(L-1),
                           static_cast<int>(length_left_to_fill)) + 1,
                       finaloutput.begin()+starting_index);
           }
136
137
           // returning
138
           return std::move(finaloutput);
139
140
       }
141
142
       // /*-----
143
       // 1D convolution of two vectors
       // > implemented through fft
145
146
147
       // template <typename T1, typename T2>
       // auto conv1D(const std::vector<T1>& input_vector_A,
       //
                       const
                               std::vector<T2>& input_vector_B)
149
       // {
150
       //
             // resulting type
151
       //
             using T3 = decltype(std::declval<T1>() * std::declval<T2>());
152
             // creating canvas
       //
154
       //
             auto
                     canvas_length
                                       {input_vector_A.size() + input_vector_B.size() - 1};
```

```
156
      //
            // calculating fft of two arrays
157
                   fft_A {svr::fft(input_vector_A, canvas_length)};
      //
            auto
158
      //
            auto
                   fft_B
                            {svr::fft(input_vector_B, canvas_length)};
160
            // element-wise multiplying the two matrices
                           {fft_A * fft_B};
      //
            auto fft_AB
162
163
      //
            // finding inverse FFT
165
            auto convolved_result {ifft(fft_AB)};
166
      //
            // returning
167
            return std::move(convolved_result);
      //
168
      // }
169
170
171
      /*-----
173
174
      Short-conv1D
       -----*/
175
      // template <std::size_t shortsize,</pre>
176
      //
                   typename
                               T1,
177
      //
                               T2>
                   typename
178
                             T1,
      template <typename
179
                 typename
                             T2>
             conv1D_short(const std::vector<T1>& input_vector_A,
      auto
181
                       const std::vector<T2>& input_vector_B)
182
183
          // resulting type
184
          using T3 = decltype(std::declval<T1>() * std::declval<T2>());
185
186
          // creating canvas
187
                                 {input_vector_A.size() + input_vector_B.size() - 1};
          auto canvas_length
188
189
          // calculating fft of two arrays
190
          auto
                fft_A
                          {svr::fft(input_vector_A, canvas_length)};
          auto
                fft_B
                          {svr::fft(input_vector_B, canvas_length)};
192
193
          // element-wise multiplying the two matrices
                         {fft_A * fft_B};
          auto fft_AB
196
          // finding inverse FFT
197
          auto convolved_result {ifft(fft_AB)};
198
         // returning
200
          // return std::move(convolved_result);
2.01
          return convolved_result;
202
203
204
205
206
207
      /*-----
      1D Convolution of a matrix and a vector
208
209
210
      template <typename T>
      auto conv1D(const
                         std::vector<std::vector<T>>& input_matrix,
211
                   const
                         std::vector<T>&
                                                    input_vector,
212
                          std::size_t&
                                                     dim)
                   const
213
      {
214
```

```
// getting dimensions
215
            const auto& num_rows_matrix
                                                   {input_matrix.size()};
216
                                                   {input_matrix[0].size()};
            const auto& num_cols_matrix
217
            const auto& num_elements_vector
                                                  {input_vector.size()};
218
219
           // creating canvas
                               {std::vector<std::vector<T>>()};
            auto canvas
221
222
            // creating output based on dim
            if (dim == 1)
224
225
               // performing convolutions row by row
226
               for(auto row = 0; row < num_rows_matrix; ++row)</pre>
227
228
                   cout << format("\t\t row = {}/{}\n", row, num_rows_matrix);
                   auto bruh {conv1D(input_matrix[row], input_vector)};
230
                   auto bruh_real {svr::real(std::move(bruh))};
231
232
                   canvas.push_back(
233
234
                           svr::real(
                               std::move(bruh_real)
236
                   );
237
               }
           }
           else{
240
               std::cerr << "svr_conv.hpp | conv1D | yet to be implemented \n";</pre>
241
242
243
           // returning
244
           return std::move(canvas);
245
246
       }
247
248
249
        1D Convolution of a matrix and a vector (in-place)
251
252
    }
253
```

A.7 Coordinate Change

```
// finding azimuthal and elevation angles
16
               azimuthal_angles {svr::atan2(xysplat[1],
17
                                        xysplat[0]) \
18
                                * 180.00/std::numbers::pi};
19
         auto
               elevation_angles {svr::atan2(cartesian_vector[2],
                                        xysplat_lengths) \
2.1
                                * 180.00/std::numbers::pi};
                               {norm(cartesian_vector)};
         auto
               rho_values
         // creating tensor to send back
25
               spherical_vector {std::vector<T>{azimuthal_angles,
26
                                           elevation_angles,
27
                                           rho_values}};
28
29
         // moving it back
30
         return std::move(spherical_vector);
31
32
      /*-----
33
      y = cart2sph(vector)
34
      -----*/
      template <typename T>
36
      auto cart2sph_inplace(std::vector<T>& cartesian_vector){
37
38
         // splatting the point onto xy-plane
         auto xysplat {cartesian_vector};
40
         xysplat[2]
                    = 0;
41
         // finding splat lengths
43
         auto
               xysplat_lengths
                              {norm(xysplat)};
44
         // finding azimuthal and elevation angles
               azimuthal_angles {svr::atan2(xysplat[1], xysplat[0]) *
            180.00/std::numbers::pi};
               elevation_angles {svr::atan2(cartesian_vector[2],
48
         auto
                                        xysplat_lengths) * 180.00/std::numbers::pi};
         auto
               rho_values
                               {norm(cartesian_vector)};
50
51
         // creating tesnor
         cartesian_vector[0] = azimuthal_angles;
         cartesian_vector[1]
                              elevation_angles;
54
         cartesian_vector[2] = rho_values;
55
56
      /*-----
     y = cart2sph(input_matrix, dim)
58
      -----*/
59
60
      template <typename T>
      auto cart2sph(const std::vector<std::vector<T>>& input_matrix,
61
                const
                        std::size_t
62
      {
63
         // fetching dimensions
         const auto& num_rows {input_matrix.size()};
         const auto& num_cols {input_matrix[0].size()};
66
         // checking the axis and dimensions
         if (axis == 0 && num_rows != 3) {std::cerr << "cart2sph: incorrect num-elements
            n'';
         if (axis == 1 && num_cols != 3) {std::cerr << "cart2sph: incorrect num-elements
            n";}
```

```
71
           // creating canvas
72
                             {std::vector<std::vector<T>>(
           auto
                  canvas
73
              num_rows,
74
              std::vector<T>(num_cols, 0)
           )};
           // if axis = 0, performing operation column-wise
           if(axis == 0)
80
              for(auto col = 0; col < num_cols; ++col)</pre>
81
               ₹
82
                  // fetching current column
                         curr_column {std::vector<T>({input_matrix[0][col],
                                                      input_matrix[1][col],
85
                                                      input_matrix[2][col]})};
                  // performing inplace transformation
88
                  cart2sph_inplace(curr_column);
89
90
                  // storing it back
                  canvas[0][col]
                                      curr_column[0];
                  canvas[1][col]
                                      curr_column[1];
93
                  canvas[2][col] =
                                      curr_column[2];
              }
           }
96
           // if axis == 1, performing operations row-wise
97
           else if(axis == 0)
98
99
               std::cerr << "cart2sph: yet to be implemented \n";
100
           }
           else
               std::cerr << "cart2sph: yet to be implemented \n";</pre>
104
           }
105
           // returning
107
           return std::move(canvas);
108
109
       }
111
       // -----
112
       template <typename T>
113
              sph2cart(const std::vector<T> spherical_vector){
       auto
114
115
           // creating cartesian vector
116
                  cartesian_vector {std::vector<T>(spherical_vector.size(), 0)};
           auto
117
           // populating
           cartesian_vector[0]
                                    spherical_vector[2] * \
120
                                     cos(spherical_vector[1] * std::numbers::pi / 180.00) * \
121
                                     cos(spherical_vector[0] * std::numbers::pi / 180.00);
           cartesian_vector[1]
                                     spherical_vector[2] * \
                                     cos(spherical_vector[1] * std::numbers::pi / 180.00) * \
124
                                     sin(spherical_vector[0] * std::numbers::pi / 180.00);
           cartesian_vector[2]
                                     spherical_vector[2] * \
126
                                     sin(spherical_vector[1] * std::numbers::pi / 180.00);
128
           // returning
129
```

```
130     return std::move(cartesian_vector);
131     }
132 }
```

A.8 Cosine

```
#pragma once
   /*-----
  y = cos(input_vector)
  template <typename T>
  auto cos(const std::vector<T>& input_vector)
      // created canvas
                       {input_vector};
      auto canvas
      // calling the function
      std::transform(input_vector.begin(), input_vector.end(),
                   canvas.begin(),
                   [](auto& argx){return std::cos(argx);});
      // returning the output
      return std::move(canvas);
17
  }
18
19
  y = cosd(input_vector)
20
  template <typename T>
  auto cosd(const std::vector<T> input_vector)
23
  {
24
      // created canvas
25
      auto canvas
                       {input_vector};
26
2.7
      // calling the function
28
      std::transform(input_vector.begin(),
                   input_vector.end(),
30
                   input_vector.begin(),
31
                   [](const auto& argx){return std::cos(argx * 180.00/std::numbers::pi);});
      // returning the output
34
      return std::move(canvas);
35
  }
```

A.9 Data Structures

```
struct TreeNode {
   int val;
   TreeNode *left;
   TreeNode *right;
   TreeNode() : val(0), left(nullptr), right(nullptr) {}
   TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
   TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
};
```

```
struct ListNode {
   int val;
   ListNode *next;
   ListNode() : val(0), next(nullptr) {}
   ListNode(int x) : val(x), next(nullptr) {}
   ListNode(int x, ListNode *next) : val(x), next(next) {}
};
```

A.10 Editing Index Values

```
#pragma once
  /*-----
  Matlab's equivalent of A[A < 0.5] = 0
  // template <typename T, typename BooleanVector, typename U>
  // auto edit(std::vector<T>&
                                           input_vector,
            BooleanVector
                                           bool_vector,
  //
              const U
                                           scalar)
  // {
10 //
         // throwing an error
  //
         if (input_vector.size() != bool_vector.size())
  //
            std::cerr << "edit: incompatible size\n";</pre>
14 //
         // overwriting input-vector
15 //
        std::transform(input_vector.begin(), input_vector.end(),
16 //
                      bool_vector.begin(),
17 //
                      input_vector.begin(),
18 //
                      [&scalar](auto& argx, auto argy){
19 //
                          if(argy == true) {return static_cast<T>(scalar);}
  //
                                            {return argx;}
                      });
21
23 //
         // no-returns since in-place
 template <typename T, typename U>
  auto edit(std::vector<T>&
                                         input_vector,
           const std::vector<bool>&
                                         bool_vector,
           const U
28
  {
29
      // throwing an error
30
      if (input_vector.size() != bool_vector.size())
31
          std::cerr << "edit: incompatible size\n";</pre>
32
33
      // overwriting input-vector
      std::transform(input_vector.begin(), input_vector.end(),
                   bool_vector.begin(),
36
                   input_vector.begin(),
37
                   [&scalar](auto& argx, auto argy){
                        if(argy == true) {return static_cast<T>(scalar);}
                        else
                                         {return argx;}
40
                   });
      // no-returns since in-place
43
   }
44
```

```
/*-----
  accumulate version of edit, instead of just placing values
47
48
  THings to add
49
      - ensuring template only accepts int, std::size_t and similar for T2
      - bring in histogram method to ensure SIMD
51
  template <typename T1,
            typename T2>
54
  auto edit_accumulate(std::vector<T1>&
                                            input_vector,
55
                      const std::vector<T2>& indices_to_edit,
56
                      const std::vector<T1>& new_values)
57
58 {
      // certain checks
59
      if (indices_to_edit.size() != new_values.size())
60
         std::cerr << "svr::edit | edit_accumulate | size-disparity occured \n";</pre>
62
      // going through each and accumulating
63
      for(auto i = 0; i < input_vector.size(); ++i){</pre>
         const auto target_index {static_cast<std::size_t>(indices_to_edit[i])}; //
         const auto new_value {new_values[i]};
         input_vector[target_index] += new_value;
67
      // no-return since in-place
70
  }
```

A.11 Equality

```
#pragma once
  /*-----
  template <typename T, typename U>
  auto operator==(const std::vector<T>& input_vector,
              const U&
                                  scalar)
     // setting up canvas
     auto canvas {std::vector<bool>(input_vector.size())};
10
     // writing to canvas
11
     std::transform(input_vector.begin(), input_vector.end(),
                 canvas.begin(),
                 [&scalar](const auto& argx){
                     return argx == scalar;
                 });
     // returning
18
     return std::move(canvas);
19
  }
```

A.12 Exponentiate

#pragma once

```
y = abs(vector)
  -----*/
  template <typename T>
  auto exp(const std::vector<T>& input_vector)
    // creating canvas
    auto canvas
               {input_vector};
10
11
    // transforming
    std::transform(canvas.begin(), canvas.end(),
12
             canvas.begin(),
13
              [](auto& argx){return std::exp(argx);});
    // returning
16
    return std::move(canvas);
17
  }
```

A.13 FFT

```
#pragma once
  namespace svr {
     /*-----
     For type-deductions
     template <typename T>
     struct fft_result_type;
     // specializations
9
      template <> struct fft_result_type<double>{
10
         using type = std::complex<double>;
      template <> struct fft_result_type<std::complex<double>>{
13
         using type = std::complex<double>;
14
      template <> struct fft_result_type<float>{
        using type = std::complex<float>;
      template <> struct fft_result_type<std::complex<float>>{
         using type = std::complex<float>;
20
     };
21
22
      template <typename T>
      using fft_result_t = typename fft_result_type<T>::type;
24
25
      /*----
26
     y = fft(x, nfft)
         > calculating n-point dft where n-value is explicit
28
29
     template<typename T>
31
     auto fft(const std::vector<T>& input_vector,
           const size_t
                                    nfft)
32
         // throwing an error
         if (nfft < input_vector.size()) {std::cerr << "size-mistmatch\n";}</pre>
         if (nfft <= 0)</pre>
                                     {std::cerr << "size-mistmatch\n";}
36
```

```
37
          // fetching data-type
38
          using RType = fft_result_t<T>;
39
          using baseType = std::conditional_t<std::is_same_v<T, std::complex<double>>,
40
                                              double.
41
                                              T>;
43
          // canvas instantiation
          std::vector<RType> canvas(nfft);
                 nfft_sqrt
                              {static_cast<RType>(std::sqrt(nfft))};
46
          auto
                 finaloutput
                               {std::vector<RType>(nfft, 0)};
47
48
          // calculating index by index
          for(int frequency_index = 0; frequency_index<nfft; ++frequency_index){</pre>
50
             RType accumulate_value;
51
             for(int signal_index = 0; signal_index < input_vector.size(); ++signal_index){</pre>
                 accumulate_value += \
                    static_cast<RType>(input_vector[signal_index]) * \
54
                    static_cast<RType>(std::exp(-1.00 * std::numbers::pi * \
55
                                             (static_cast<baseType>(frequency_index)/static_cast<baseType>(n
                                             static_cast<baseType>(signal_index)));
57
58
             finaloutput[frequency_index] = accumulate_value / nfft_sqrt;
          }
61
          // returning
62
          return std::move(finaloutput);
63
      }
64
65
      /*-----
66
      y = fft(std::vector<double> nfft) // specialization
      -----*/
68
      #include <fftw3.h>
                              // for fft
69
      template <>
70
      auto fft(const std::vector<double>& input_vector,
71
              const std::size_t
72
73
          if (nfft < input_vector.size())</pre>
             throw std::runtime_error("nfft must be >= input_vector.size()");
          if (nfft <= 0)</pre>
76
             throw std::runtime_error("nfft must be > 0");
77
78
          // FFTW real-to-complex output
          std::vector<std::complex<double>> output(nfft);
80
81
          // Allocate input (double) and output (fftw_complex) arrays
          double* in = reinterpret_cast<double*>(fftw_malloc(sizeof(double) * nfft));
          fftw_complex* out =
             reinterpret_cast<fftw_complex*>(fftw_malloc(sizeof(fftw_complex) * (nfft/2 +
             1)));
          // Copy input and zero-pad if needed
86
          for (std::size_t i = 0; i < nfft; ++i) {</pre>
             in[i] = (i < input_vector.size()) ? input_vector[i] : 0.0;</pre>
90
          // Create FFTW plan and execute
91
```

```
fftw_plan plan = fftw_plan_dft_r2c_1d(static_cast<int>(nfft), in, out,
              FFTW_ESTIMATE);
          fftw_execute(plan);
93
94
          // Copy FFTW output to std::vector<std::complex<double>>
95
          for (std::size_t i = 0; i < nfft/2 + 1; ++i) {</pre>
              output[i] = std::complex<double>(out[i][0], out[i][1]);
          // Optional: fill remaining bins with zeros to match full nfft size
          for (std::size_t i = nfft/2 + 1; i < nfft; ++i) {</pre>
100
              output[i] = std::complex<double>(0.0, 0.0);
101
          }
102
103
          // Cleanup
104
          fftw_destroy_plan(plan);
          fftw_free(in);
106
          fftw_free(out);
107
108
          // filling up the other half of the output
109
                        halfpoint {static_cast<std::size_t>(nfft/2)};
          const auto
110
          std::transform(
111
                                       // first half (skip DC)
              output.begin() + 1,
              output.begin() + halfpoint, // end of first half
113
                                   // start writing from last element backward (skip
              output.rbegin(),
114
                  Nyquist)
              [](const auto& x) { return std::conj(x); }
115
          );
116
117
          // returning
118
          return std::move(output);
119
       }
120
121
       /*-----
       y = ifft(x, nfft)
124
                             -----*/
       template<typename T>
126
       auto ifft(const
                         std::vector<T>& input_vector)
128
          // fetching data-type
          using RType = fft_result_t<T>;
130
          using baseType = std::conditional_t<std::is_same_v<T, std::complex<double>>,
131
                                               double,
132
                                               T>;
133
134
          // setup
135
          auto nfft
                            {input_vector.size()};
136
          // canvas instantiation
138
          std::vector<RType> canvas(nfft);
139
                                {static_cast<RType>(std::sqrt(nfft))};
140
          auto
                 nfft_sqrt
141
          auto
                  finaloutput
                                {std::vector<RType>(nfft, 0)};
142
          // calculating index by index
143
          for(int frequency_index = 0; frequency_index<nfft; ++frequency_index){</pre>
              RType accumulate_value;
145
              for(int signal_index = 0; signal_index < input_vector.size(); ++signal_index){</pre>
146
                  accumulate_value += \
147
                     static_cast<RType>(input_vector[signal_index]) * \
148
```

```
static_cast<RType>(std::exp(1.00 * std::numbers::pi * \
149
                                                (static_cast<baseType>(frequency_index)/static_cast<baseType>(
150
                                                static_cast<baseType>(signal_index)));
               }
               finaloutput[frequency_index] = accumulate_value / nfft_sqrt;
153
           // returning
           return std::move(finaloutput);
157
158
159
       /*-----
160
       y = ifft()
161
       using fftw
162
163
       // #include <fftw3.h>
164
       // #include <vector>
165
       // #include <complex>
166
167
       // #include <stdexcept>
       // #include <algorithm>
168
169
       // // template <typename T>
170
       // auto ifft(const std::vector<std::complex<double>>& input_vector,
171
       //
                   const std::size_t
                                                          nfft.)
       // {
173
             if (nfft <= 0)
       //
174
                 throw std::runtime_error("nfft must be > 0");
       //
175
       //
              if (input_vector.size() < nfft/2 + 1)</pre>
176
       //
                 throw std::runtime_error("input spectrum must have at least nfft/2+1
177
           bins");
       //
              // Output: real-valued time-domain signal
179
              std::vector<double> output(nfft);
180
181
       //
              // Allocate FFTW input/output
              fftw_complex* in =
183
           reinterpret_cast<fftw_complex*>(fftw_malloc(sizeof(fftw_complex) * (nfft/2 + 1)));
              double* out = reinterpret_cast<double*>(fftw_malloc(sizeof(double) * nfft));
185
       //
              // Copy input spectrum into FFTW buffer
186
       //
             for (std::size_t i = 0; i < nfft/2 + 1; ++i) {
187
       //
                 in[i][0] = input_vector[i].real();
188
       //
                 in[i][1] = input_vector[i].imag();
189
       11
              }
190
191
       //
              // Create inverse plan and execute
192
              fftw_plan plan = fftw_plan_dft_c2r_1d(static_cast<int>(nfft), in, out,
193
           FFTW_ESTIMATE);
       //
              fftw_execute(plan);
194
195
196
       //
              // Normalize by nfft (FFTW does unscaled IFFT)
       //
              for (std::size_t i = 0; i < nfft; ++i) {</pre>
197
       //
                 output[i] = out[i] / static_cast<double>(nfft);
198
       //
              }
200
       //
              // Cleanup
201
       //
             fftw_destroy_plan(plan);
202
       //
              fftw_free(in);
```

```
//
              fftw_free(out);
204
205
              return output;
206
       // }
2.07
208
       /*----
       x = ifft(std::vector<std::complex<double>> spectrum, nfft)
210
211
       #include <fftw3.h>
212
213
       #include <vector>
       #include <complex>
214
       #include <stdexcept>
215
216
       auto ifft(const std::vector<std::complex<double>>& input_vector,
217
                 const std::size_t
218
219
           if (nfft <= 0)</pre>
               throw std::runtime_error("nfft must be > 0");
221
           if (input_vector.size() != nfft)
222
               throw std::runtime_error("input spectrum must be of size nfft");
223
           // Output: real-valued time-domain sequence
225
           std::vector<double> output(nfft);
226
227
           // Allocate FFTW input/output
           fftw_complex* in = reinterpret_cast<fftw_complex*>(
229
               fftw_malloc(sizeof(fftw_complex) * (nfft/2 + 1)));
230
           double* out = reinterpret_cast<double*>(
231
               fftw_malloc(sizeof(double) * nfft));
232
233
           // Copy *only* the first nfft/2+1 bins (rest are redundant due to symmetry)
234
           for (std::size_t i = 0; i < nfft/2 + 1; ++i) {</pre>
               in[i][0] = input_vector[i].real();
               in[i][1] = input_vector[i].imag();
237
238
           // Create inverse FFTW plan
240
           fftw_plan plan = fftw_plan_dft_c2r_1d(
241
               static_cast<int>(nfft), in, out, FFTW_ESTIMATE);
           fftw_execute(plan);
244
245
           // Normalize by nfft (FFTW leaves IFFT unscaled)
246
           for (std::size_t i = 0; i < nfft; ++i) {</pre>
               output[i] = out[i] / static_cast<double>(nfft);
248
249
250
           // Cleanup
251
           fftw_destroy_plan(plan);
252
           fftw_free(in);
253
254
           fftw_free(out);
           return output;
256
257
258
259
260
   }
261
```

A.14 Flipping Containers

```
#pragma once
  namespace svr {
     /*-----
     Mirror image of a vector
     template <typename T>
     auto fliplr(const std::vector<T>& input_vector)
        // creating canvas
        auto
            canvas
                     {input_vector};
        // rewriting
        std::reverse(canvas.begin(), canvas.end());
        // returning
        return std::move(canvas);
17
  }
18
```

A.15 Indexing

```
#pragma once
  namespace svr {
      /*----
      y = index(vector, mask)
      template
                <typename T1,
                 typename T2,
                 typename = std::enable_if_t<std::is_arithmetic_v<T1>
                                         std::is_same_v<T1, std::complex<float> > ||
                                         std::is_same_v<T1, std::complex<double> >
10
11
      auto
             index(const
                          std::vector<T1>&
                                               input_vector,
                          std::vector<T2>&
                                               indices_to_sample)
14
         // creating canvas
         auto canvas {std::vector<T1>(indices_to_sample.size(), 0)};
         // copying the associated values
         for(int i = 0; i < indices_to_sample.size(); ++i){</pre>
                  source_index {indices_to_sample[i]};
             if(source_index < input_vector.size()){</pre>
                canvas[i] = input_vector[source_index];
             else
                cout << "svr::index | source_index !< input_vector.size()\n";</pre>
26
         }
         // returning
         return std::move(canvas);
      y = index(matrix, mask, dim)
```

```
-----*/
34
      template <typename T1, typename T2>
35
      auto index(const std::vector<std::vector<T1>>& input_matrix,
36
                         std::vector<T2>&
                const
                                                      indices_to_sample,
37
                const std::size_t&
                                                     dim)
38
          // fetching dimensions
40
          const auto& num_rows_matrix {input_matrix.size()};
          const auto& num_cols_matrix {input_matrix[0].size()};
43
          // creating canvas
44
                canvas {std::vector<std::vector<T1>>()};
          auto
45
          // if indices are row-indices
47
          if (dim == 0){
48
              // initializing canvas
              canvas = std::vector<std::vector<T1>>(
51
52
                 num_rows_matrix,
                 std::vector<T1>(indices_to_sample.size())
53
              );
55
              // filling the canvas
56
              auto destination_index {0};
              std::for_each(indices_to_sample.begin(), indices_to_sample.end(),
                          [&](const auto& col){
59
                            for(auto row = 0; row < num_rows_matrix; ++row)</pre>
60
                                canvas[row] [destination_index] = input_matrix[row][col];
61
                            ++destination_index;
63
                          });
          }
          else if(dim == 1){
              // initializing canvas
              canvas = std::vector<std::vector<T1>>(
67
                 indices_to_sample.size(),
68
                 std::vector<T1>(num_cols_matrix)
              );
70
              // filling the canvas
73
              #pragma omp parallel for
              for(auto row = 0; row < canvas.size(); ++row){</pre>
74
                 auto
                        destination_col {0};
75
                 std::for_each(indices_to_sample.begin(), indices_to_sample.end(),
76
                              [&row,
                               &input_matrix,
78
                               &destination_col,
79
                               &canvas](const auto& source_col){
                                    canvas[row] [destination_col++] =
                                        input_matrix[row] [source_col];
                              });
82
              }
83
          }
          else {
85
              std::cerr << "svr_index | this dim is not implemented \n";</pre>
88
          // moving it back
89
          return std::move(canvas);
90
      }
```

2 }

A.16 Linspace

```
/*----
  Dependencies
  #pragma once
  #include <vector>
  #include <complex>
  /*----
  -----*/
  template <typename T>
  auto linspace(auto&
13
                      input,
           const auto startvalue,
14
           const auto endvalue,
           const auto numpoints) -> void
  {
17
     auto stepsize = static_cast<T>(endvalue - startvalue)/static_cast<T>(numpoints-1);
    for(int i = 0; i<input.size(); ++i) {input[i] = startvalue + i*stepsize;}</pre>
20
  /*-----
21
22 in-place
  template <typename T>
  auto linspace(std::vector<std::complex<T>>& input,
25
           const auto
                                 startvalue,
26
27
           const
                 auto
                                 endvalue,
           const
                 auto
                                 numpoints) -> void
28
  {
29
     auto stepsize = static_cast<T>(endvalue - startvalue)/static_cast<T>(numpoints-1);
30
     for(int i = 0; i<input.size(); ++i) {</pre>
       input[i] = startvalue + static_cast<T>(i)*stepsize;
32
33
  };
  /*----
  template <typename T>
37
  auto linspace(const T
                           startvalue,
         const T
                           endvalue,
           const std::size_t numpoints)
40
 {
41
    std::vector<T> input(numpoints);
     auto stepsize = static_cast<T>(endvalue - startvalue)/static_cast<T>(numpoints-1);
    for(int i = 0; i<input.size(); ++i) {input[i] = startvalue +</pre>
       static_cast<T>(i)*stepsize;}
    return std::move(input);
45
 /*----
  template <typename T, typename U>
  auto linspace(const T
                            startvalue,
           const
51
                            endvalue,
```

```
const
                         std::size_t
                                         numpoints)
52
   {
53
       std::vector<double> input(numpoints);
54
       auto stepsize = static_cast<double>(endvalue -
55
           startvalue)/static_cast<double>(numpoints-1);
       for(int i = 0; i<input.size(); ++i) {input[i] = startvalue + i*stepsize;}</pre>
       return std::move(input);
57
 };
58
```

A.17 Max

```
#pragma once
   maximum along dimension 1
   template <std::size_t axis, typename T>
        max(const std::vector<std::vector<T>>& input_matrix) -> std::enable_if_t<axis</pre>
       == 1, std::vector<std::vector<T>> >
      // setting up canvas
      auto canvas
          {std::vector<std::vector<T>>(input_matrix.size(),std::vector<T>(1))};
      // filling up the canvas
      for(auto row = 0; row < input_matrix.size(); ++row)</pre>
          canvas[row][0] = *(std::max_element(input_matrix[row].begin(),
              input_matrix[row].end()));
      // returning
15
      return std::move(canvas);
16
   }
17
```

A.18 Meshgrid

```
______
  Dependencies
  #pragma once
  #include <vector> // for std::vector
6 #include <utility> // for std::pair
  #include <complex> // for std::complex
  /*----
10
  mesh-grid when working with 1-values
  template <typename T>
13
  auto meshgrid(const std::vector<T>& x,
14
       const std::vector<T>& y)
15
16
17
     // creating and filling x-grid
18
     std::vector<std::vector<T>> xcanvas(y.size(), std::vector<T>(x.size(), 0));
19
     for(auto row = 0; row < y.size(); ++row)</pre>
```

```
std::copy(x.begin(), x.end(), xcanvas[row].begin());
      // creating and filling y-grid
23
      std::vector<std::vector<T>> ycanvas(y.size(), std::vector<T>(x.size(), 0));
24
      for(auto col = 0; col < x.size(); ++col)</pre>
         for(auto row = 0; row < y.size(); ++row)</pre>
             ycanvas[row][col] = y[row];
      // returning
30
      return std::move(std::pair{xcanvas, ycanvas});
31
32 }
meshgrid when working with r-values
34
                       -----*/
35
  template <typename T>
  auto meshgrid(std::vector<T>&& x,
              std::vector<T>&& y)
38
39
40
      // creating and filling x-grid
41
      std::vector<std::vector<T>> xcanvas(y.size(), std::vector<T>(x.size(), 0));
42
      for(auto row = 0; row < y.size(); ++row)</pre>
43
         std::copy(x.begin(), x.end(), xcanvas[row].begin());
      // creating and filling y-grid
46
      std::vector<std::vector<T>> ycanvas(y.size(), std::vector<T>(x.size(), 0));
47
      for(auto col = 0; col < x.size(); ++col)</pre>
         for(auto row = 0; row < y.size(); ++row)</pre>
50
             ycanvas[row][col] = y[row];
51
      // returning
      return std::move(std::pair{xcanvas, ycanvas});
54
  }
```

A.19 Minimum

```
return std::move(canvas);
}
```

A.20 Norm

51

```
#pragma once
  /*-----
  calculating norm for vector
   -----*/
  template <typename T>
6 auto norm(const std::vector<T>& input_vector)
  {
      return std::sqrt(std::inner_product(input_vector.begin(), input_vector.end(),
8
                                    input_vector.begin(),
9
                                    (T)0));
10
11
12
13
  template <typename T>
  auto norm(const std::vector<std::vector<T>>& input_matrix,
             const std::size_t
16
  {
17
      // creating canvas
18
19
      auto canvas {std::vector<std::vector<T>>()};
      const auto& num_rows_matrix {input_matrix.size()};
20
      const auto& num_cols_matrix {input_matrix[0].size()};
21
22
23
      // along dim 0
      if(dim == 0)
24
25
         // allocate canvas
         canvas = std::vector<std::vector<T>>(
27
2.8
            std::vector<T>(input_matrix[0].size())
29
         );
31
         // performing norm
         auto accumulate_vector {std::vector<T>(input_matrix[0].size())};
         // going through each row
35
         for(auto row = 0; row < num_rows_matrix; ++row)</pre>
36
             std::transform(input_matrix[row].begin(), input_matrix[row].end(),
38
                         accumulate_vector.begin(),
39
                         accumulate_vector.begin(),
40
                         [](const auto& argx, auto& argy){
                             return argx*argx + argy;
                         });
43
         }
44
         // calculating element-wise square root
46
         std::for_each(accumulate_vector.begin(), accumulate_vector.end(),
                     [](auto& argx){
                          argx = std::sqrt(argx);
                     });
50
```

```
// moving to the canvas
           canvas[0] = std::move(accumulate_vector);
53
54
       else if (dim == 1)
55
           // allocating space in the canvas
                     = std::vector<std::vector<T>>(
58
               input_matrix[0].size(),
               std::vector<T>(1, 0)
           );
61
62
           // going through each column
63
           for(auto row = 0; row < num_cols_matrix; ++row){</pre>
               canvas[row][0] = norm(input_matrix[row]);
66
       }
       else
69
70
       {
           std::cerr << "norm(matrix, dim): dimension operation not defined \n";</pre>
71
73
       // returning
74
       return std::move(canvas);
75
   }
76
77
78
79
   /*
80
81
   Templates to create
       - matrix and norm-axis
82
           axis instantiated std::vector<T>
83
```

A.21 Division

```
#pragma once
  /*-----
  element-wise division with scalars
5 template <typename T>
  auto operator/(const std::vector<T>& input_vector,
              const T&
                                    input_scalar)
8
     // creating canvas
9
     auto canvas
                     {input_vector};
10
11
     // filling canvas
     std::transform(canvas.begin(), canvas.end(),
                 canvas.begin(),
                 [&input_scalar](const auto& argx){
                     return static_cast<double>(argx) /
                        static_cast<double>(input_scalar);
                 });
18
     // returning value
19
```

```
return std::move(canvas);
20
  }
21
  /*-----
22
  element-wise division with scalars
23
  template <typename T>
  auto operator/=(const std::vector<T>&
                                      input_vector,
26
                                      input_scalar)
               const
2.7
                      T&
28
29
      // creating canvas
     auto
          canvas
                     {input_vector};
30
31
     // filling canvas
32
      std::transform(canvas.begin(), canvas.end(),
33
                 canvas.begin(),
34
                  [&input_scalar](const auto& argx){
35
                     return static_cast<double>(argx) /
                         static_cast<double>(input_scalar);
                 });
37
38
      // returning value
      return std::move(canvas);
40
  }
41
  /*----
  element-wise with matrix
  -----*/
  template <typename T>
45
  auto operator/(const std::vector<std::vector<T>>& input_matrix,
                const T
                                              scalar)
47
48
     // fetching matrix-dimensions
49
      const auto& num_rows_matrix
                                {input_matrix.size()};
50
      const auto& num_cols_matrix
                                 {input_matrix[0].size()};
51
52
     // creating canvas
53
                     {std::vector<std::vector<T>>(
      auto canvas
        num_rows_matrix,
         std::vector<T>(num_cols_matrix)
     )};
      // dividing with values
59
              row = 0; row < num_rows_matrix; ++row){</pre>
      for(auto
60
         std::transform(input_matrix[row].begin(), input_matrix[row].end(),
61
                     canvas[row].begin(),
                     [&scalar](const auto& argx){
63
                         return argx/scalar;
64
                    });
     }
67
      // returning values
68
     return std::move(canvas);
69
  }
```

A.22 Addition

```
/*-----
  y = vector + vector
   -----*/
  template <typename T>
6 std::vector<T> operator+(const std::vector<T>& a,
                      const std::vector<T>& b)
8
      // Identify which is bigger
9
      const auto& big = (a.size() > b.size()) ? a : b;
10
      const auto& small = (a.size() > b.size()) ? b : a;
11
12
     std::vector<T> result = big; // copy the bigger one
13
     // Add elements from the smaller one
15
     for (size_t i = 0; i < small.size(); ++i) {</pre>
16
         result[i] += small[i];
17
19
20
     return result;
21 }
  /*-----
_{24} // y = vector + vector
25 template <typename T>
std::vector<T>& operator+=(std::vector<T>& a,
                       const std::vector<T>& b) {
2.8
      const auto& small = (a.size() < b.size()) ? a : b;</pre>
29
      const auto& big = (a.size() < b.size()) ? b : a;</pre>
30
31
     // If b is bigger, resize 'a' to match
     if (a.size() < b.size())</pre>
                                           {a.resize(b.size());}
     // Add elements
35
     for (size_t i = 0; i < small.size(); ++i) {a[i] += b[i];}</pre>
36
     // returning elements
38
     return a;
39
40 }
  41
42 // y = matrix + matrix
43 template <typename T>
std::vector<std::vector<T>> operator+(const std::vector<std::vector<T>>& a,
                                const std::vector<std::vector<T>>& b)
45
46
     // fetching dimensions
47
      const auto& num_rows_A {a.size()};
      const auto& num_cols_A
                              {a[0].size()};
                            {b.size()};
      const auto& num_rows_B
50
     const auto& num_cols_B {b[0].size()};
51
     // choosing the three different metrics
     if (num_rows_A != num_rows_B && num_cols_A != num_cols_B){
         cout << format("a.dimensions = [\{\},\{\}], b.shape = [\{\},\{\}]\n",
                     num_rows_A, num_cols_A,
                     num_rows_B, num_cols_B);
         std::cerr << "dimensions don't match\n";</pre>
58
      }
59
```

```
// creating canvas
61
        auto
              canvas
                          {std::vector<std::vector<T>>(
62
           std::max(num_rows_A, num_rows_B),
63
           std::vector<T>(std::max(num_cols_A, num_cols_B), (T)0.00)
64
       )};
65
       // performing addition
67
       if (num_rows_A == num_rows_B && num_cols_A == num_cols_B){
           for(auto row = 0; row < num_rows_A; ++row){</pre>
               std::transform(a[row].begin(), a[row].end(),
70
                             b[row].begin(),
                             canvas[row].begin(),
72
                             std::plus<T>());
73
           }
74
       }
75
       else if(num_rows_A == num_rows_B){
76
           // if number of columns are different, check if one of the cols are one
78
                          min_num_cols {std::min(num_cols_A, num_cols_B)};
79
                  auto
           if (min_num_cols != 1) {std::cerr<< "Operator+: unable to broadcast\n";}</pre>
                         max_num_cols {std::max(num_cols_A, num_cols_B)};
           const auto
           // using references to tag em differently
83
                                         {num_cols_A > num_cols_B ? a : b};
           const auto& big_matrix
           const
                  auto& small_matrix {num_cols_A < num_cols_B ? a : b};</pre>
86
           // Adding to canvas
87
           for(auto row = 0; row < canvas.size(); ++row){</pre>
               std::transform(big_matrix[row].begin(), big_matrix[row].end(),
                             canvas[row].begin(),
90
                             [&small_matrix,
                              &row](const auto& argx){
                                  return argx + small_matrix[row][0];
                             });
94
           }
95
       else if(num_cols_A == num_cols_B){
           // check if the smallest column-number is one
100
                        min_num_rows {std::min(num_rows_A, num_rows_B)};
           if(min_num_rows != 1)
                                     {std::cerr << "Operator+ : unable to broadcast\n";}
           const auto
                         max_num_rows {std::max(num_rows_A, num_rows_B)};
102
103
           // using references to differentiate the two matrices
                                         {num_rows_A > num_rows_B ? a : b};
           const auto& big_matrix
105
           const auto& small_matrix {num_rows_A < num_rows_B ? a : b};</pre>
106
           // adding to canvas
108
           for(auto row = 0; row < canvas.size(); ++row){</pre>
               std::transform(big_matrix[row].begin(), big_matrix[row].end(),
111
                             small_matrix[0].begin(),
                             canvas[row].begin(),
                             [](const auto& argx, const auto& argy){
113
                              return argx + argy;
114
                             });
           }
116
       }
       else {
118
           std::cerr << "operator+: yet to be implemented \n";</pre>
119
```

```
}
120
121
      // returning
122
      return std::move(canvas);
124
   }
   /*-----
   y = vector + scalar
126
   template <typename T>
129
   auto operator+(const std::vector<T>& input_vector,
               const
                                       scalar)
130
131
      // creating canvas
      auto canvas
                      {input_vector};
133
134
      // adding scalar to the canvas
      std::transform(canvas.begin(), canvas.end(),
136
                  canvas.begin(),
137
                   [&scalar](auto& argx){return argx + scalar;});
138
139
      // returning canvas
140
      return std::move(canvas);
141
   }
142
   /*-----
143
144
   y = scalar + vector
145
   template <typename T>
146
   auto operator+(const T
                                       scalar,
               const std::vector<T>& input_vector)
148
149
      // creating canvas
150
                      {input_vector};
151
      auto
           canvas
      // adding scalar to the canvas
      std::transform(canvas.begin(), canvas.end(),
154
                  canvas.begin(),
                   [&scalar](auto& argx){return argx + scalar;});
156
      // returning canvas
158
159
      return std::move(canvas);
160
   }
```

A.23 Multiplication (Element-wise)

```
[&scalar](auto& argx){argx = argx * scalar;});
     // returning
     return std::move(canvas);
15
16
  /*-----
  y = scalar * vector
  -----*/
19
  template <typename T1, typename T2,
20
     typename = std::enable_if_t<!std::is_same_v<std::decay_t<T1>, std::vector<T2>>>>
21
22
  auto operator*(const T1
                                   scalar,
             const
                    vector<T2>&
                                  input_vector)
23
24 {
     // fetching final-type
25
     using T3 = decltype(std::declval<T1>() * std::declval<T2>());
26
     // creating canvas
27
     auto
          canvas
                    {std::vector<T3>(input_vector.size())};
28
     // multiplying
     std::transform(input_vector.begin(), input_vector.end(),
30
                canvas.begin(),
31
                 [&scalar](auto& argx){
                 return static_cast<T3>(scalar) * static_cast<T3>(argx);
                });
34
     // returning
35
     return std::move(canvas);
36
37
  }
  /*-----
38
  y = vector * scalar
39
  template <typename T>
41
42
  auto operator*(const std::vector<T>& input_vector,
                const
                       Т
                                      scalar)
43
     // creating canvas
45
          canvas {input_vector};
     auto
46
     // multiplying
47
     std::for_each(canvas.begin(), canvas.end(),
                [&scalar](auto& argx){
49
                 argx = argx * scalar;
50
                });
51
     // returning
53
     return std::move(canvas);
  }
54
  /*----
55
 y = vector * vector
    -----*/
57
  template <typename T>
  auto operator*(const std::vector<T>& input_vector_A,
59
             const std::vector<T>& input_vector_B)
60
61
     // throwing error: size-desparity
62
     if (input_vector_A.size() != input_vector_B.size()) {std::cerr << "operator*: size</pre>
63
        disparity \n";}
     // creating canvas
65
     auto canvas {input_vector_A};
     // element-wise multiplying
68
     std::transform(input_vector_B.begin(), input_vector_B.end(),
69
                canvas.begin(),
```

```
canvas.begin(),
                [](const auto& argx, const auto& argy){
                    return argx * argy;
73
                }):
74
     // moving it back
     return std::move(canvas);
77
78 }
   /*-----
   -----*/
80
  template <typename T1, typename T2>
81
  auto operator*(const std::vector<T1>& input_vector_A,
82
               const std::vector<T2>& input_vector_B)
84
85
     // checking size disparity
86
     if (input_vector_A.size() != input_vector_B.size())
        std::cerr << "operator*: error, size-disparity \n";</pre>
88
89
     // figuring out resulting data type
90
     using T3 = decltype(std::declval<T1>() * std::declval<T2>());
92
     // creating canvas
93
          canvas
                    {std::vector<T3>(input_vector_A.size())};
     auto
     // performing multiplications
96
     std::transform(input_vector_A.begin(), input_vector_A.end(),
97
                input_vector_B.begin(),
98
                canvas.begin(),
                [](const auto&
                                  argx,
100
                  const auto&
                                 argy){
101
                    return static_cast<T3>(argx) * static_cast<T3>(argy);
102
                });
104
     // returning
105
     return std::move(canvas);
107
108
  109
111
  template <typename T>
112
  auto operator*(const T
                                        scalar,
113
            const std::vector<std::vector<T>>& inputMatrix)
114
115
     std::vector<std::vector<T>> temp {inputMatrix};
116
     for(int i = 0; i<inputMatrix.size(); ++i){</pre>
117
        std::transform(inputMatrix[i].begin(),
118
                   inputMatrix[i].end(),
119
                   temp[i].begin(),
120
                   [&scalar](T x){return scalar * x;});
121
     return std::move(temp);
123
124 }
  /*-----
126
  y = matrix * scalar
     -----*/
127
128 template <typename T>
129 auto operator*(const std::vector<std::vector<T>>& input_matrix,
```

```
Τ
                                                           scalar)
130
                    const
131
       // fetching matrix dimensions
              auto& num_rows_matrix
                                        {input_matrix.size()};
       const
       const auto& num_cols_matrix
                                        {input_matrix[0].size()};
134
135
       // creating canvas
136
             canvas
       auto
                          {std::vector<std::vector<T>>(
137
           num_rows_matrix,
           std::vector<T>(num_cols_matrix)
139
       )};
140
141
       // storing the values
142
       for(auto row = 0; row < num_rows_matrix; ++row)</pre>
143
           std::transform(input_matrix[row].begin(), input_matrix[row].end(),
144
                         canvas[row].begin(),
145
                         [&scalar](const auto& argx){
                             return argx * scalar;
147
                         });
148
149
       // returning
150
       return std::move(canvas);
151
   }
   /*-----
153
154
   y = matrix * matrix
      -----
155
   template <typename T>
156
   auto operator*(const std::vector<std::vector<T>>& A,
157
                 const std::vector<std::vector<T>>& B) -> std::vector<std::vector<T>>
158
159
       // Case 1: element-wise multiplication
160
       if (A.size() == B.size() && A[0].size() == B[0].size()) {
161
           std::vector<std::vector<T>> C(A.size(), std::vector<T>(A[0].size()));
162
           for (std::size_t row = 0; row < A.size(); ++row) {</pre>
163
               std::transform(A[row].begin(), A[row].end(),
164
                            B[row].begin(),
                            C[row].begin(),
166
                             [](const auto& x, const auto& y){ return x * y; });
167
           }
169
           return C;
170
171
       // Case 2: broadcast column vector
172
       else if (A.size() == B.size() && B[0].size() == 1) {
173
           std::vector<std::vector<T>> C(A.size(), std::vector<T>(A[0].size()));
174
           for (std::size_t row = 0; row < A.size(); ++row) {</pre>
175
               std::transform(A[row].begin(), A[row].end(),
                            C[row].begin(),
177
                             [&](const auto& x){ return x * B[row][0]; });
           }
179
180
           return C;
181
182
       // case 3: when second matrix contains just one row
183
       // case 4: when first matrix is just one column
       // case 5: when second matrix is just one column
185
186
       // Otherwise, invalid
187
       else {
```

```
throw std::runtime_error("operator* dimension mismatch");
189
190
191
   /*-----
192
   y = scalar * matrix
     template <typename T1, typename T2>
195
   auto operator*(const T1
196
                                            scalar,
               const std::vector<std::vector<T2>>& inputMatrix)
198
      std::vector<std::vector<T2>> temp {inputMatrix};
199
      for(int i = 0; i<inputMatrix.size(); ++i){</pre>
200
         std::transform(inputMatrix[i].begin(),
201
                     inputMatrix[i].end(),
202
                     temp[i].begin(),
203
                     [&scalar](T2 x){return static_cast<T2>(scalar) * x;});
204
      }
      return temp;
206
207
   /*-----
208
   matrix-multiplication
209
   -----*/
210
   template <typename T1, typename T2>
211
   auto matmul(const std::vector<std::vector<T1>>& matA,
212
            const std::vector<std::vector<T2>>& matB)
214
215
      // throwing error
216
      if (matA[0].size() != matB.size()) {std::cerr << "dimension-mismatch \n";}</pre>
217
218
      // getting result-type
219
      using ResultType = decltype(std::declval<T1>() * std::declval<T2>() + \
220
                               std::declval<T1>() * std::declval<T2>() );
221
222
      // creating aliasses
223
      auto finalnumrows {matA.size()};
224
      auto finalnumcols {matB[0].size()};
225
226
      // creating placeholder
228
      auto rowcolproduct = [&](auto rowA, auto colB){
         ResultType temp {0};
229
         for(int i = 0; i < matA.size(); ++i) {temp +=</pre>
230
             static_cast<ResultType>(matA[rowA][i]) +
             static_cast<ResultType>(matB[i][colB]);}
         return temp;
231
      };
232
      // producing row-column combinations
      std::vector<std::vector<ResultType>> finaloutput(finalnumrows,
235
          std::vector<ResultType>(finalnumcols));
      for(int row = 0; row < finalnumrows; ++row){for(int col = 0; col < finalnumcols;</pre>
236
          ++col){finaloutput[row][col] = rowcolproduct(row, col);}}
237
      // returning
238
      return finaloutput;
239
240
   /*-----
241
   y = matrix * vector
```

```
template
               <typename T>
    auto operator*(const std::vector<std::vector<T>>
                                                         input_matrix,
245
                           std::vector<T>
                                                         input_vector)
246
2.47
       // fetching dimensions
248
       const auto& num_rows_matrix
                                          {input_matrix.size()};
249
                                          {input_matrix[0].size()};
       const auto& num_cols_matrix
250
       const auto& num_rows_vector
                                          {1};
251
       const auto& num_cols_vector
                                          {input_vector.size()};
253
       const auto& max_num_rows
                                          {num_rows_matrix > num_rows_vector ?\
254
                                           num_rows_matrix : num_rows_vector};
255
                                          {num_cols_matrix > num_cols_vector ?\
       const auto& max_num_cols
256
                                           num_cols_matrix : num_cols_vector};
257
258
       // creating canvas
259
                           {std::vector<std::vector<T>>(
       auto
              canvas
260
           max_num_rows,
261
           std::vector<T>(max_num_cols, 0)
262
       )};
263
264
       //
265
       if (num_cols_matrix == 1 && num_rows_vector == 1){
266
267
           // writing to canvas
           for(auto row = 0; row < max_num_rows; ++row)</pre>
269
               for(auto col = 0; col < max_num_cols; ++col)</pre>
270
                   canvas[row][col] = input_matrix[row][0] *
                                                                     input_vector[col];
271
       }
272
273
       else{
           std::cerr << "Operator*: [matrix, vector] | not implemented \n";</pre>
274
275
276
       // returning
277
       return std::move(canvas);
278
280
281
282
   scalar operators
283
   auto operator*(const std::complex<double> complexscalar,
284
                  const double
                                             doublescalar){
285
       return complexscalar * static_cast<std::complex<double>>(doublescalar);
286
   }
287
   auto operator*(const double
                                              doublescalar,
288
                  const std::complex<double> complexscalar){
289
       return complexscalar * static_cast<std::complex<double>>(doublescalar);
290
   }
291
   auto operator*(const std::complex<double> complexscalar,
292
                  const int
                                              scalar){
293
       return complexscalar * static_cast<std::complex<double>>(scalar);
294
295
   }
   auto operator*(const int
296
                  const std::complex<double> complexscalar){
297
       return complexscalar * static_cast<std::complex<double>>(scalar);
298
   }
```

A.24 Subtraction

```
#pragma once
  /*-----
  y = vector - scalar
  -----*/
  template <typename T>
  auto operator-(const std::vector<T>& a,
             const T
                              scalar){
     std::vector<T> temp(a.size());
     std::transform(a.begin(),
                a.end(),
                temp.begin(),
                [scalar](T x){return (x - scalar);});
     return std::move(temp);
13
14 }
  /*-----
  y = vector - vector
   .-----*/
17
  template <typename T>
18
  auto operator-(const std::vector<T>& input_vector_A,
19
            const
                   std::vector<T>& input_vector_B)
21 {
     // throwing error
22
     if (input_vector_A.size() != input_vector_B.size())
23
        std::cerr << "operator-(vector, vector): size disparity\n";</pre>
25
     // creating canvas
26
     const auto& num_cols {input_vector_A.size()};
     auto
                canvas {std::vector<T>()};
29
     // peforming operations
     std::transform(input_vector_A.begin(), input_vector_A.begin(),
                input_vector_B.begin(),
32
                canvas.begin(),
33
                [](const auto& argx, const auto& argy){
34
                   return argx - argy;
                });
36
37
     // return
38
     return std::move(canvas);
40
  /*----
41
  y = matrix - matrix
                  template <typename T>
  auto operator-(const std::vector<std::vector<T>>& input_matrix_A,
45
                   std::vector<std::vector<T>>& input_matrix_B)
             const
     // fetching dimensions
48
     const auto& num_rows_A {input_matrix_A.size()};
49
     const auto& num_cols_A {input_matrix_A[0].size()};
     const auto& num_rows_B {input_matrix_B.size()};
51
     const auto& num_cols_B {input_matrix_B[0].size()};
52
     // creating canvas
     auto canvas {std::vector<std::vector<T>>()};
55
56
     // if both matrices are of equal dimensions
```

```
if (num_rows_A == num_rows_B && num_cols_A == num_cols_B)
          // copying one to the canvas
60
          canvas = input_matrix_A;
61
          // subtracting
          for(auto row = 0; row < num_rows_B; ++row)</pre>
              std::transform(canvas[row].begin(), canvas[row].end(),
                             input_matrix_B[row].begin(),
                             canvas[row].begin(),
                             [](auto& argx, const auto& argy){
68
                                 return argx - argy;
                             });
       // column broadcasting (case 1)
       else if(num_rows_A == num_rows_B && num_cols_B == 1)
          // copying canvas
75
          canvas = input_matrix_A;
76
          // substracting
          for(auto row = 0; row < num_rows_A; ++row){</pre>
              std::transform(canvas[row].begin(), canvas[row].end(),
                             canvas[row].begin(),
                             [&input_matrix_B,
                              &row](auto& argx){
                                 return argx - input_matrix_B[row][0];
                             });
          }
87
       else{
          std::cerr << "operator-: not implemented for this case \n";</pre>
91
       // returning
92
93
       return std::move(canvas);
   }
```

A.25 Operator Overloadings

A.26 Printing Containers

```
for(auto x: input) cout << x << ",";</pre>
     cout << endl;</pre>
13
14
15
17 template<typename T>
void fPrintMatrix(const std::vector<std::vector<T>> input_matrix){
     for(const auto& row: input_matrix)
19
       cout << format("{}\n", row);</pre>
20
21
22 /*-----
24 template <typename T>
void fPrintMatrix(const string&
                                     input_string,
              const std::vector<std::vector<T>> input_matrix){
     cout << format("{} = \n", input_string);</pre>
27
     for(const auto& row: input_matrix)
       cout << format("{}\n", row);</pre>
29
30 }
31 /*----
33 template<typename T, typename T1>
void fPrintHashmap(unordered_map<T, T1> input){
     for(auto x: input){
       cout << format("[{},{}] | ", x.first, x.second);</pre>
    cout <<endl;</pre>
38
39 }
 41 -----*/
  void fPrintBinaryTree(TreeNode* root){
    // sending it back
     if (root == nullptr) return;
45
    // printing
46
    PRINTLINE
     cout << "root->val = " << root->val << endl;</pre>
    // calling the children
     fPrintBinaryTree(root->left);
52
     fPrintBinaryTree(root->right);
53
    // returning
54
    return;
55
56
57 }
  /*----
     -----*/
  void fPrintLinkedList(ListNode* root){
60
     if (root == nullptr) return;
61
     cout << root->val << " -> ";
     fPrintLinkedList(root->next);
     return;
64
65 }
  /*-----
68 template<typename T>
69 void fPrintContainer(T input){
    for(auto x: input) cout << x << ", ";</pre>
```

```
cout << endl;</pre>
     return;
72
73
  /*-----
  template <typename T>
  auto size(std::vector<std::vector<T>> inputMatrix){
    cout << format("[{}, {}]\n",</pre>
               inputMatrix.size(),
80
               inputMatrix[0].size());
 }
81
 /*-----
82
 template <typename T>
84
 auto size(const std::string&
                                      inputstring,
85
    const std::vector<std::vector<T>>& inputMatrix){
     cout << format("{} = [{}, {}]\n",
               inputstring,
88
               inputMatrix.size(),
89
               inputMatrix[0].size());
90
```

A.27 Random Number Generation

```
#pragma once
  template <typename T>
5 auto rand(const T min,
       const T max) {
    static std::random_device rd; // Seed
    static std::mt19937 gen(rd()); // Mersenne Twister generator
    std::uniform_real_distribution<> dist(min, max);
    return dist(gen);
10
 }
  /*----
    -----*/
  template <typename T>
  auto rand(const T
                        min,
     const T
                        max,
16
       const std::size_t numelements)
17
18 {
    static std::random_device rd; // Seed
    static std::mt19937 gen(rd()); // Mersenne Twister generator
2.0
    std::uniform_real_distribution<> dist(min, max);
2.1
    // building the fianloutput
    vector<T> finaloutput(numelements);
24
    for(int i = 0; i<finaloutput.size(); ++i) {finaloutput[i] =</pre>
       static_cast<T>(dist(gen));}
    return finaloutput;
27
28 }
  /*-----
 template <typename T>
```

```
auto rand(const T
                                  argmin,
           const T
                                  argmax,
           const std::vector<int> dimensions)
34
  {
35
36
      // throwing an error if dimension is greater than two
      if (dimensions.size() > 2) {std::cerr << "dimensions are too high\n";}</pre>
38
39
      // creating random engine
      static std::random_device rd; // Seed
41
      static std::mt19937 gen(rd()); // Mersenne Twister generator
42
      std::uniform_real_distribution<> dist(argmin, argmax);
43
      // building the finaloutput
45
      vector<vector<T>> finaloutput;
46
      for(int i = 0; i<dimensions[0]; ++i){</pre>
          vector<T> temp;
          for(int j = 0; j<dimensions[1]; ++j) {temp.push_back(dist(gen));}</pre>
49
         // cout << format("\t\t temp = {}\n", temp);
50
51
         finaloutput.push_back(temp);
53
54
      // returning the finaloutput
      return finaloutput;
57
58 }
auto rand(const std::vector<int> dimensions)
   ₹
62
      using ReturnType = double;
63
      // throwing an error if dimension is greater than two
65
      if (dimensions.size() > 2) {std::cerr << "dimensions are too high\n";}</pre>
66
      // creating random engine
      static std::random_device rd; // Seed
      static std::mt19937 gen(rd()); // Mersenne Twister generator
70
      std::uniform_real_distribution<> dist(0.00, 1.00);
72
      // building the finaloutput
73
      vector<vector<ReturnType>> finaloutput;
74
      for(int i = 0; i<dimensions[0]; ++i){</pre>
          vector<ReturnType> temp;
76
          for(int j = 0; j<dimensions[1]; ++j) {temp.push_back(dist(gen));}</pre>
          finaloutput.push_back(std::move(temp));
80
      // returning the finaloutput
81
82
      return std::move(finaloutput);
83
84 }
85
   template <typename T>
87
  auto rand_complex_double(const T
                                                argmin,
88
                        const T
                                                argmax,
89
                        const std::vector<int>& dimensions)
```

```
{
91
        // throwing an error if dimension is greater than two
93
        if (dimensions.size() > 2) {std::cerr << "dimensions are too high\n";}</pre>
94
95
        // creating random engine
        static std::random_device rd; // Seed
97
        static std::mt19937 gen(rd()); // Mersenne Twister generator
        std::uniform_real_distribution<> dist(argmin, argmax);
100
        // building the finaloutput
101
        vector<vector<complex<double>>> finaloutput;
102
        for(int i = 0; i<dimensions[0]; ++i){</pre>
           vector<complex<double>> temp;
104
           for(int j = 0; j<dimensions[1]; ++j)</pre>
                {temp.push_back(static_cast<double>(dist(gen)));}
           finaloutput.push_back(std::move(temp));
        }
107
108
        // returning the finaloutput
109
        return finaloutput;
    }
111
```

A.28 Reshape

```
#pragma once
  /*-----
  reshaping a matrix into another matrix
  template <std::size_t M, std::size_t N, typename T>
   auto reshape(const std::vector<std::vector<T>>& input_matrix){
      // verifying size stuff
0
      if (M*N != input_matrix.size() * input_matrix[0].size())
         std::cerr << "Dimensions are quite different\n";</pre>
11
      // creating canvas
                      {std::vector<std::vector<T>>(
           canvas
         M, std::vector<T>(N, (T)0)
      )};
16
17
      // writing to canvas
18
      size_t tid
                            {0};
19
      size_t
              target_row
                            {0};
2.0
      size_t target_col
                            {0};
21
      for(auto row = 0; row<input_matrix.size(); ++row){</pre>
         for(auto col = 0; col < input_matrix[0].size(); ++col){</pre>
23
                          = row * input_matrix[0].size() + col;
             tid
24
                          = tid/N;
             target_row
             target_col
                          = tid%N;
             canvas[target_row][target_col] = input_matrix[row][col];
         }
30
      // moving it back
31
```

```
return std::move(canvas);
32
  }
33
  /*-----
34
  reshaping a matrix into a vector
35
  -----*/
36
  template<std::size_t M, typename T>
37
  auto reshape(const std::vector<std::vector<T>>& input_matrix){
38
39
     // checking element-count validity
41
     if (M != input_matrix.size() * input_matrix[0].size())
        std::cerr << "Number of elements differ\n";</pre>
42
43
     // creating canvas
     auto canvas {std::vector<T>(M, 0)};
45
46
     // filling canvas
47
     for(auto row = 0; row < input_matrix.size(); ++row)</pre>
        for(auto col = 0; col < input_matrix[0].size(); ++col)</pre>
49
            canvas[row * input_matrix.size() + col] = input_matrix[row][col];
50
51
     // moving it back
     return std::move(canvas);
53
54 }
  Matrix to matrix
57
  template<typename T>
58
  auto reshape(const std::vector<std::vector<T>>& input_matrix,
          const std::size_t
M,
61
            const std::size_t
                                       N){
62
     // checking element-count validity
63
     if ( M * N != input_matrix.size() * input_matrix[0].size())
        std::cerr << "Number of elements differ\n";</pre>
65
66
     // creating canvas
     auto canvas
                  {std::vector<std::vector<T>>(
        M, std::vector<T>(N, (T)0)
     )};
70
72
     // writing to canvas
     size_t tid
                         {0};
73
     size_t target_row {0};
74
     size_t target_col
                         {0};
     for(auto row = 0; row<input_matrix.size(); ++row){</pre>
76
        for(auto col = 0; col < input_matrix[0].size(); ++col){</pre>
77
                       = row * input_matrix[0].size() + col;
                       = tid/N;
           target_row
                       = tid%N;
           target_col
80
            canvas[target_row][target_col] = input_matrix[row][col];
81
        }
82
     }
     // moving it back
85
     return std::move(canvas);
86
  }
87
  89 converting a matrix into a vector
```

```
template<typename T>
   auto reshape(const std::vector<std::vector<T>>& input_matrix,
                const size_t
93
94
       // checking element-count validity
95
       if (M != input_matrix.size() * input_matrix[0].size())
           std::cerr << "Number of elements differ\n";</pre>
       // creating canvas
       auto canvas {std::vector<T>(M, 0)};
100
101
       // filling canvas
102
       for(auto row = 0; row < input_matrix.size(); ++row)</pre>
           for(auto col = 0; col < input_matrix[0].size(); ++col)</pre>
104
               canvas[row * input_matrix.size() + col] = input_matrix[row][col];
       // moving it back
       return std::move(canvas);
108
109
```

A.29 Summing with containers

```
#pragma once
    template <std::size_t axis, typename T>
  auto sum(const std::vector<T>& input_vector) -> std::enable_if_t<axis == 0,</pre>
     std::vector<T>>
     // returning the input as is
    return input_vector;
  }
  -----*/
  template <std::size_t axis, typename T>
  auto sum(const std::vector<std::vector<T>>& input_matrix) -> std::enable_if_t<axis == 0,</pre>
     std::vector<T>>
14
     // creating canvas
        canvas {std::vector<T>(input_matrix[0].size(), 0)};
16
17
     // filling up the canvas
     for(auto row = 0; row < input_matrix.size(); ++row)</pre>
       std::transform(input_matrix[row].begin(), input_matrix[row].end(),
                 canvas.begin(),
                 canvas.begin(),
                 [](auto& argx, auto& argy){return argx + argy;});
    // returning
    return std::move(canvas);
  /*-----
    -----*/
  template <std::size_t axis, typename T>
```

```
auto sum(const std::vector<std::vector<T>>& input_matrix) -> std::enable_if_t<axis == 1,</pre>
       std::vector<std::vector<T>>>
33
       // creating canvas
34
       auto canvas
                     {std::vector<std::vector<T>>(input_matrix.size(),
35
                                                 std::vector<T>(1, 0.00))};
37
       // filling up the canvas
38
       for(auto row = 0; row < input_matrix.size(); ++row)</pre>
           canvas[row][0] = std::accumulate(input_matrix[row].begin(),
                                              input_matrix[row].end(),
41
                                              static_cast<T>(0));
42
43
       // returning
       return std::move(canvas);
45
46
48
49
50
   template <std::size_t axis, typename T>
   auto sum(const std::vector<T>& input_vector_A,
51
           const std::vector<T>& input_vector_B) -> std::enable_if_t<axis == 0,</pre>
52
               std::vector<T> >
   {
53
       // setup
       const auto& num_cols_A
                                    {input_vector_A.size()};
55
       const auto& num_cols_B {input_vector_B.size()};
56
57
       // throwing errors
       if (num_cols_A != num_cols_B) {std::cerr << "sum: size disparity\n";}</pre>
59
60
       // creating canvas
       auto
             canvas {input_vector_A};
63
       // summing up
64
       std::transform(input_vector_B.begin(), input_vector_B.end(),
                     canvas.begin(),
                     canvas.begin(),
                     std::plus<T>());
70
       // returning
       return std::move(canvas);
71
   }
```

A.30 Tangent

```
if (input_vector_A.size() != input_vector_B.size())
           std::cerr << "atan2: size disparity\n";</pre>
        // create canvas
        auto canvas
                       {std::vector<T>(input_vector_A.size(), 0)};
        // performing element-wise atan2 calculation
        std::transform(input_vector_A.begin(), input_vector_A.end(),
                   input_vector_B.begin(),
                   canvas.begin(),
                   [](const auto& arg_a,
21
                     const auto& arg_b){
                       return std::atan2(arg_a, arg_b);
                   });
        // moving things back
        return std::move(canvas);
28
29
     /*----
     y = tan-inverse(a/b)
     -----*/
32
     template <typename T>
33
     auto atan2(T scalar_A,
             Т
                 scalar_B)
36
        return std::atan2(scalar_A, scalar_B);
37
38
  }
39
```

A.31 Tiling Operations

```
#pragma once
  namespace svr {
      /*-----
      tiling a vector
      template <typename T>
      auto tile(const std::vector<T>&
                                        input_vector,
                     std::vector<size_t>& mul_dimensions){
              const
         // creating canvas
         const std::size_t& num_rows
                                    {1 * mul_dimensions[0]};
11
         const std::size_t& num_cols {input_vector.size() * mul_dimensions[1]};
         auto
               canvas {std::vector<std::vector<T>>(
            num_rows,
            std::vector<T>(num_cols, 0)
         )};
16
         // writing
         std::size_t
                    source_row;
         std::size_t source_col;
20
         for(std::size_t row = 0; row < num_rows; ++row){</pre>
            for(std::size_t col = 0; col < num_cols; ++col){</pre>
               source_row = row % 1;
```

```
source_col = col % input_vector.size();
               canvas[row][col] = input_vector[source_col];
26
            }
2.7
         }
2.8
         // returning
         return std::move(canvas);
31
      /*-----
     tiling a matrix
      -----*/
35
      template <typename T>
36
      auto tile(const std::vector<std::vector<T>>& input_matrix,
37
              const
                     std::vector<size_t>&
                                              mul_dimensions){
38
39
         // creating canvas
                                     {input_matrix.size() * mul_dimensions[0]};
         const std::size_t& num_rows
                                    {input_matrix[0].size() * mul_dimensions[1]};
         const std::size_t& num_cols
42
               canvas {std::vector<std::vector<T>>(
43
            num_rows,
            std::vector<T>(num_cols, 0)
         )};
46
         // writing
         std::size_t
                      source_row;
         std::size_t
                    source_col;
50
51
         for(std::size_t row = 0; row < num_rows; ++row){</pre>
            for(std::size_t col = 0; col < num_cols; ++col){</pre>
               source_row = row % input_matrix.size();
               source_col = col % input_matrix[0].size();
               canvas[row][col] = input_matrix[source_row][source_col];
            }
         }
58
50
         // returning
         return std::move(canvas);
61
62
  }
63
```

A.32 Transpose

```
canvas[i][0] = input_vector[i];

// moving it back
return std::move(canvas);

}
```

A.33 Masking

```
#pragma once
  namespace svr {
      /*----
      y = input_vector[mask == 1]
      template <typename T,
              typename = std::enable_if_t< std::is_arithmetic_v<T>
                                      std::is_same_v<T, std::complex<double>> ||
                                      std::is_same_v<T, std::complex<float>>
      auto mask(const
                      std::vector<T>&
                                     input_vector,
                      std::vector<bool>& mask_vector)
              const
         // checking dimensionality issues
         if (input_vector.size() != mask_vector.size())
            std::cerr << "mask(vector, mask): incompatible size \n";</pre>
         // creating canas
               num_trues {std::count(mask_vector.begin(),
         auto
20
                                   mask_vector.end(),
                                   true)};
         auto
                canvas
                          {std::vector<T>(num_trues)};
         // copying values
         auto destination_index {0};
         for(auto i = 0; i <input_vector.size(); ++i)</pre>
            if (mask_vector[i] == true)
                canvas[destination_index++] = input_vector[i];
         // returning output
31
         return std::move(canvas);
32
33
      /*----
35
      template <typename T>
36
      auto mask(const std::vector<std::vector<T>>&
37
                                                   input_matrix,
              const
                      std::vector<bool>
                                                    mask_vector)
39
         // fetching dimensions
40
         const auto& num_rows_matrix {input_matrix.size()};
         const auto& num_cols_matrix {input_matrix[0].size()};
         const auto& num_cols_vector
                                           {mask_vector.size()};
         // error-checking
         if (num_cols_matrix != num_cols_vector)
46
            std::cerr << "mask(matrix, bool-vector): size disparity";</pre>
47
```

```
// building canvas
                 num_trues {std::count(mask_vector.begin(),
50
                                      mask_vector.end(),
51
                                      true)};
          auto
                 canvas
                            {std::vector<std::vector<T>>(
             num_rows_matrix,
             std::vector<T>(num_cols_vector, 0)
          )};
          // writing values
58
          #pragma omp parallel for
          for(auto row = 0; row < num_rows_matrix; ++row){</pre>
                    destination_index {0};
             for(auto col = 0; col < num_cols_vector; ++col)</pre>
                 if(mask_vector[col] == true)
                    canvas[row] [destination_index++] = input_matrix[row][col];
          }
65
          // returning
          return std::move(canvas);
69
      /*-----
70
      Fetch Indices corresponding to mask true's
      auto mask_indices(const std::vector<bool>& mask_vector)
73
74
          // creating canvas
                num_trues {std::count(mask_vector.begin(), mask_vector.end(),
                                      true)};
          auto
                 canvas
                            {std::vector<std::size_t>(num_trues)};
          // building canvas
                 destination_index {0};
81
          for(auto i = 0; i < mask_vector.size(); ++i)</pre>
             if (mask_vector[i] == true)
                 canvas[destination_index++] = i;
          // returning
          return std::move(canvas);
88
  }
89
```

A.34 Resetting Containers

```
if constexpr (sizeof...(rest_vectors) > 0) {
    reset(rest_vectors...);
}

}
```

A.35 Element-wise squaring

48

```
#pragma once
  namespace svr {
     /*-----
    Element-wise squaring vector
     -----*/
     template
            <typename T,
             typename = std::enable_if_t<std::is_arithmetic_v<T>>
          square(const std::vector<T>& input_vector)
     auto
       // creating canvas
       auto canvas
                    {std::vector<T>(input_vector.size())};
       // peforming calculations
       std::transform(input_vector.begin(), input_vector.end(),
                 canvas.begin(),
16
                  [](const auto& argx){
                       return argx * argx;
                  });
       // moving it back
21
       return std::move(canvas);
     /*-----
24
    Element-wise squaring vector (in-place)
25
     -----*/
26
     template
            <typename T,
             typename = std::enable_if_t<std::is_arithmetic_v<T>>
     void
          square_inplace(std::vector<T>& input_vector)
       // performing operations
32
       std::transform(input_vector.begin(), input_vector.end(),
33
                 input_vector.begin(),
                 [](auto& argx){
                    return argx * argx;
36
                 });
37
     /*----
     ELement-wise squaring a matrix
40
     -----*/
41
     template <typename T>
43
          square(const std::vector<std::vector<T>>& input_matrix)
       // fetching dimensions
       const auto& num_rows {input_matrix.size()};
       const auto& num_cols {input_matrix[0].size()};
```

```
// creating canvas
49
        auto canvas
                    {std::vector<std::vector<T>>(
50
           num_rows,
51
           std::vector<T>(num_cols, 0)
52
        )};
        // going through each row
55
        #pragma omp parallel for
        for(auto row = 0; row < num_rows; ++row)</pre>
           std::transform(input_matrix[row].begin(), input_matrix[row].end(),
58
                      canvas[row].begin(),
59
                      [](const auto& argx){
                          return argx * argx;
                      });
63
        // returning
        return std::move(canvas);
66
     /*----
67
     Squaring for scalars
68
     -----*/
     template <typename T>
70
     auto square(const T& scalar) {return scalar * scalar;}
71
  }
72
```

A.36 Thread-Pool

```
#pragma once
  namespace svr {
      class ThreadPool {
      public:
          // Members
          boost::asio::thread_pool
                                      thread_pool;
                                                      // the pool
          std::vector<std::future<void>> future_vector; // futures to wait on
          // Special-Members
          ThreadPool(std::size_t num_threads)
              : thread_pool(num_threads) {}
          ThreadPool(const ThreadPool& other)
                                                   = delete;
          ThreadPool& operator=(ThreadPool& other) = delete;
14
          // Member-functions
                                    converge();
          template <typename F> void push_back(F&& func);
17
          void
                                    shutdown();
18
19
      private:
20
          template<typename F>
21
          std::future<void> _wrap_task(F&& func) {
22
              std::promise<void> p;
              auto f = p.get_future();
25
              boost::asio::post(thread_pool,
                  [func = std::forward<F>(func), p = std::move(p)]() mutable {
                     func();
28
                     p.set_value();
29
```

```
});
31
           return f;
32
33
     };
34
     /*-----
36
     Member-Function: Add new task to the pool
     template <typename F>
     void ThreadPool::push_back(F&& func)
40
41
        future_vector.push_back(_wrap_task(std::forward<F>(func)));
42
43
     Member-Function: waiting until all the assigned work is done
     void ThreadPool::converge()
47
48
        for (auto &fut : future_vector) fut.get();
49
        future_vector.clear();
51
     /*-----
52
     Member-Function: Shutting things down
     void ThreadPool::shutdown()
55
56
        thread_pool.join();
59
  }
60
```

A.37 Flooring

```
namespace svr {
     element-wise flooring of a vector-contents
     template <typename T>
          floor(const
                        std::vector<T>& input_vector)
     auto
        // creating canvas
        auto canvas
                       {std::vector<T>(input_vector.size())};
10
        // filling the canvas
        std::transform(input_vector.begin(), input_vector.end(),
                    canvas.begin(),
                    [](const auto& argx){
                        return std::floor(argx);
                    });
        // returning
        return std::move(canvas);
     /*-----
21
     element-wise flooring of a vector-contents (in-place)
22
```

```
-----*/
23
      template <typename T>
24
      auto floor_inplace(std::vector<T>& input_vector)
25
26
         // rewriting the contents
         std::transform(input_vector.begin(), input_vector.end(),
                     input_vector.begin(),
                     [](auto& argx){
                         return std::floor(argx);
                     });
      }
33
      /*-----
34
      element-wise flooring of matrix-contents
35
      -----*/
36
      template <typename T>
37
           floor(const std::vector<std::vector<T>>& input_matrix)
      auto
38
         // fetching dimensions
40
         const auto& num_rows_matrix {input_matrix.size()};
41
         const auto& num_cols_matrix {input_matrix[0].size()};
         // creating canvas
         auto canvas
                         {std::vector<std::vector<T>>(
45
            num_rows_matrix,
            std::vector<T>(num_cols_matrix)
         )};
48
49
         // writing contents
         for(auto row = 0; row < num_rows_matrix; ++row)</pre>
51
            std::transform(input_matrix[row].begin(), input_matrix[row].end(),
                         canvas[row].begin(),
                         [](const auto& argx){
                             return std::floor(argx);
                         });
56
57
         // returning contents
         return std::move(canvas);
60
      }
      element-wise flooring of matrix-contents (in-place)
63
64
      template <typename T>
65
      auto floor_inplace(std::vector<std::vector<T>>& input_matrix)
67
         // performing operations
68
         for(auto row = 0; row < input_matrix.size(); ++row)</pre>
            std::transform(input_matrix[row].begin(), input_matrix[row].end(),
                         input_matrix[row].begin(),
71
                         [](auto& argx){
72
                             return std::floor(argx);
73
                         });
     }
75
  }
```

A.38 Squeeze

```
namespace svr {
      template
                 <typename T>
              squeeze(const std::vector<std::vector<T>>& input_matrix)
       {
          // fetching dimensions
          const auto& num_rows_matrix
                                            {input_matrix.size()};
          const auto& num_cols_matrix {input_matrix[0].size()};
          // check if any dimension is 1
          if (num_rows_matrix == 0 || num_cols_matrix == 0)
              std::cerr << "at least one dimension should be 1";</pre>
                 final_length {std::max(num_rows_matrix, num_cols_matrix)};
          auto
          // creating canvas
                 canvas
                                {std::vector<T>(final_length)};
          auto
          // building canvas
18
          if (num_rows_matrix == 1)
              // filling canvas
21
              std::copy(input_matrix[0].begin(), input_matrix[0].end(),
22
                       canvas.begin());
23
          else if(num_cols_matrix == 1)
              // filling canvas
              std::transform(input_matrix.begin(), input_matrix.end(),
                            canvas.begin(),
                            [](const auto& argx){
30
                                return argx[0];
31
                            });
          }
          // returning
35
          return std::move(canvas);
37
   }
38
```

A.39 Tensor Initializations

6 }

A.40 Real part

```
#pragma once
  namespace svr {
     /*-----
     For type-deductions
     template
            <typename T>
     struct real_result_type;
     template <> struct real_result_type<std::complex<double>>{
        using type = double;
     template <> struct real_result_type<std::complex<float>>{
       using type = float;
14
     template <> struct real_result_type<double> {
       using type = double;
     template <> struct real_result_type<float>{
        using type = float;
20
     };
21
22
     template
            <typename T>
     using real_result_t = typename real_result_type<T>::type;
25
     /*-----
     Element-wise real() of a vector
     -----*/
28
     template
            <typename T>
29
         real(const std::vector<T>& input_vector)
     auto
        // figure out base-type
        using TCanvas = real_result_t<T>;
        // creating canvas
            canvas
                     {std::vector<TCanvas>(
36
          input_vector.size()
       )};
       // storing values
40
        std::transform(input_vector.begin(), input_vector.end(),
                   canvas.begin(),
                   [](const auto&
                                 argx){
                      return std::real(argx);
                   });
       // returning
       return std::move(canvas);
     // Element-wise real() of a matrix
```

```
// template <typename T>
      // auto real(const std::vector<std::vector<T>>& input_matrix)
      // {
55
            // fetching dimensions
56
      //
            const auto& num_rows_matrix {input_matrix.size()};
            const auto& num_cols_matrix {input_matrix[0].size()};
      //
            // creating canvas
      //
      //
            auto canvas {std::vector<std::vector<T>>(
      11
              num_rows_matrix,
      //
                std::vector<T>(num_cols_matrix)
63
      //
            )};
      //
            // storing the values
      //
            for(auto row = 0; row < num_rows_matrix; ++row)</pre>
67
      //
                std::transform(input_matrix[row].begin(), input_matrix[row].end(),
      //
                              canvas[row].begin(),
                              [](const auto& argx){
70
      //
                                  return std::real(argx);
71
                              });
      //
            // returning
            return std::move(canvas);
      //
75
      // }
76
   }
```

A.41 Imaginary part

```
#pragma once
  namespace svr {
     /*-----
    For type-deductions
     -----*/
    template
            <typename T>
    struct imag_result_type;
    template <> struct imag_result_type<std::complex<double>>{
10
       using type = double;
11
     template <> struct imag_result_type<std::complex<float>>{
       using type = float;
     template <> struct imag_result_type<double> {
16
       using type = double;
17
     template <> struct imag_result_type<float>{
       using type = float;
20
    };
21
    template
            <typename T>
    using imag_result_t = typename imag_result_type<T>::type;
     /*-----
    template <typename T>
28
```

```
auto
              imag(const std::vector<T>& input_vector)
29
30
          // figure out base-type
31
          using TCanvas = imag_result_t<T>;
32
33
          // creating canvas
                            {std::vector<TCanvas>(
          auto canvas
35
              input_vector.size()
          )};
38
          // storing values
39
          std::transform(input_vector.begin(), input_vector.end(),
40
                         canvas.begin(),
41
                         [](const auto&
                                           argx){
42
                             return std::imag(argx);
43
                         });
          // returning
46
          return std::move(canvas);
47
      }
48
  }
```