

# Written Exam for the M.Sc. in Economics 2010-1-R

International Trade and Investment

Final Exam, February 18th, 2010

4-hour closed book exam

- There are three pages in this exam paper, including this instruction page
- You need to answer all THREE questions, so manage your time accordingly.
- Make your math legible and easily followed, with the final answer boxed.
- Partial credit may be given.

Good Luck!

## 1. Exporters and non-exporters

Given the empirical research to date, identify whether these statements are true or false.

- (a) Exporting firms, on average, pay higher wages than firms that do not export.
- (b) Exporting firms, on average, sell less to the domestic market than firms that do not export.
- (c) Exporting firms, on average, pay higher wages than firms that both export and import.
- (d) The Extensive margin accounts for most of the trade expansion of French firms across markets
- (e) Firm-product-destination level export prices, on average, increase with distance.
- (f) Most firms that export continue exporting for at least 3 years.
- (g) Border effects are insignificant in free trade areas such as US-Canada.
- (h) In the 1980's, the relative wage of US production workers increased relative to the wage of nonproduction workers.

## 2. The Rybcynski Theorem.

We know that GDP is the sum of the value of the  $I$  good outputs:  $(GDP = \sum_{i=1}^I p_i y_i)$  and the sum of the value of the  $M$  factor inputs  $(GDP = \sum_{m=1}^M w_m V_m)$ . Suppose the GDP function of Denmark is translog in the  $I$  goods and  $M$  factors, i.e. it looks like:

$$\begin{aligned} \ln GDP = & \alpha_0 + \sum_{i=1}^I \alpha_i \ln p_i + \sum_{m=1}^M \beta_m \ln V_m \\ & + \frac{1}{2} \sum_{i=1}^I \sum_{j=1}^I \gamma_{ij} \ln p_i \ln p_j + \frac{1}{2} \sum_{m=1}^M \sum_{n=1}^M \delta_{mn} \ln V_m \ln V_n \\ & + \frac{1}{2} \sum_{i=1}^I \sum_{m=1}^M \varphi_{im} \ln p_i \ln V_m \end{aligned}$$

where  $p_i$  is the exogenous world price of good  $i$ ,  $V_m$  is the endowment of factor  $m$ , and the greek letters are unknown parameters.

- (a) What conditions do  $\alpha_i$  and  $\beta_m$  have to satisfy in order for the GDP to fit the duality conditions?
- (b) Given the translog GDP function, what is the expression for  $\frac{d(\ln GDP)}{d \ln V_m}$ ? How is  $\frac{d(\ln GDP)}{d \ln V_m}$  related to the value share of factor  $m$  in total  $GDP$ ?
- (c) Given the translog GDP function, what is the expression for  $\frac{d(\ln GDP)}{d \ln p_i}$ ? How is  $\frac{d(\ln GDP)}{d \ln p_i}$  related to the value share of good  $i$  in total  $GDP$ ?
- (d) Suppose you had data on  $s_m$  (the value share of factor  $m$  in total  $GDP$ ),  $s_i$  (the value shares of good  $i$  in total  $GDP$ ), world prices  $p_i$  and factor endowments  $V_m$  for all goods  $i$  and  $m$ . How would you estimate the Rybcynski coefficient, i.e. the change in the output of any good  $i$  to a change in endowment of any factor  $m$ ? (Hint: Deconstruct  $\frac{d \ln y_i}{d \ln V_m}$ ).
3. Consider a version of the Dornbusch, Fischer, Samuelson (1977) model:
- There are two countries, H and F (\* denotes F variables) producing a continuum of goods  $z \in (0, 1)$ .
  - The foreign country has 9 times the labor force of the home country.
  - The constant unit labor requirements are  $a(z) = z^2$  and  $a^*(z) = 1 - z^2$
  - The utility function is  $u = \int_0^1 b(z) \ln x(z) dz$ , where  $b(z) = 2z$  and  $x(z)$  denotes the quantity consumed of good  $z$ .
- (a) Verify that  $b(z) = 2z$  is a feasible Cobb-Douglas expenditure share.
- (b) Determine the range of goods that the home country produces. Determine the Home wage relative to the Foreign wage.
- (c) Draw the equilibrium graph relating the relative wage and set of goods produced in each country.