

Written Exam for the B.Sc. or M.Sc. in Economics winter 2014-15

**Microeconomics B**

Final Exam

21/01/2015

(3-hour closed book exam)

Please note that the language used in your exam paper must correspond to the language of the title for which you registered during exam registration. I.e. if you registered for the English title of the course, you must write your exam paper in English. Likewise, if you registered for the Danish title of the course or if you registered for the English title which was followed by “eksamen på dansk” in brackets, you must write your exam paper in Danish.

**This exam question consists of 4 pages in total**

### Exercise 1

Consider the market for loanable funds. Denote by  $r$  the price of borrowing one dkk such that the demand for loans is  $D(r) = a - br$ , with  $a, b > 0$  and the financial sector can provide loans at a constant cost of  $c > 0$  per dkk.

The market for loanable funds is characterized by perfect competition and loans are always paid back by the borrower.

- a) Derive the market equilibrium for loanable funds: the price,  $r^*$ , and quantity of loans,  $q^*$ .

Consider imposing a tax of  $t$  per borrowed dkk which the financial sector must pay to the government.

- b) What is the new equilibrium price the borrowers pay and the sellers receive? Furthermore find the change in the amount of loans issued as a consequence of the tax.  
c) Comment on the following proposition from a politician:

“The financial sector must pay for their part in the financial crisis, therefore we should tax loanable funds.”

### Exercise 2

Consider a small town on the country side, in which a local farmer produce wheat and a paper mill produce paper.

The paper mill produces paper to a perfectly competitive market in which it can sell its output at a price  $p_x = 5$ , while the costs are  $c_p(x, e) = 4x + x^2 + e(e - 3)$  where  $e$  is the emission of waste water in the local river.

The river also provides water for irrigation for the farmer, but waste water increases the farmer's costs by lowering the wheat yields. The farmer can sell his output at the nearby city at a price  $p_y = 10$ , and the costs of the farmer is  $c_f(y, e) = 8y + y^2 + ey$ .

- a) Assume that each firm chooses his production to maximize his own profit, what will be the resulting production and profit levels.  
b) Are the production decisions efficient? Explain what generates the difference between your answer in a) and b).  
c) Can you offer a remedy that implemented the efficient production levels?

### Exercise 3

Consider an unemployment insurance policy provided by a governmental sponsored program, which is the sole provider of unemployment insurance. Each worker can voluntarily sign up for the program.

When employed there is a risk of being fired, and this risk depends on the effort the worker exerts in the daily working process. Thus, if the worker exerts a low effort there is a high risk of being fired,  $\pi_L$ , while there is a lower risk of being fired if she exerts a high effort,  $\pi_H < \pi_L$ .

If the worker is fired she has an income of  $w_1$ , while being on the job pays a wage of  $w_2$ . An insurance contract is characterized by the payment in each circumstance:  $(c_1, c_2)$  where  $c_1$  is the consumption of the insured if the worker is unemployed and  $c_2$  is the consumption if employed. The expected profit of an insurance contract where the effort is  $e$ , is  $\pi_e(w_1 - c_1) + (1 - \pi_e)(w_2 - c_2)$ .

The worker is risk adverse with a Bernoulli function  $v(c) - e$ , where  $c$  is the consumption and  $e$  the effort. The effort levels can be either low  $e = e_L = 0$  or high  $e = e_H > 0$ . If the worker does not get employment he or she can obtain a utility level of  $\bar{u}$ .

- a) Assume that the insurance program can observe the effort of each worker on the job. What contract will it offer if a high effort will be exerted? For a low effort?
- b) If the insurance program cannot observe the effort, will it be optimal to offer the contracts in a)?
- c) How should the insurance contract be designed to maximize expected profits?

#### Exercise 4

Consider an industry, producing microchips to PC's, consisting of two firms, Intel and AMD, with the total demand for microchips is given by  $D(p) = 200 - 2p$ . The marginal costs in each firm are constant, but different, as Intel has a cost advantage due to a patented production technology, such that  $MC_I = 10$  and  $MC_{AMD} = 15$ .

Each firm chooses its production levels, and then the price is determined when both firms output has been chosen.

- a) Find the Nash equilibrium when Intel and AMD simultaneously choose their production levels

When the patent right of Intel's production technology expires, AMD can adopt the new technology without costs, and the marginal costs reduces to  $MC_{AMD} = 10$ .

- b) Derive the new equilibrium. How does each firm react to this adoption of the new technology? Explain.
- c) If the adoption of the new technology had a (fixed) cost, how high should it be in order to prevent AMD from adopting the new technology?

#### Exercise 5

A local homeowner's association is considering if they should replace an old sewer system to reduce leaked water and prevent increased heavy rain fall from resulting in costly floods.

The homeowner's association has 15 members: 9 members each have a willingness to pay for the sewer system of 450dkk while 6 members each have a willingness to pay of 1000dkk.

The total cost of investing in a new sewer system is 7500dkk.

- a) Is it efficient for the homeowner's association to invest in the new sewer system?
- b) To choose if they should make the investment the board has decided to cast a majority vote in which they each pay an equal share of the costs. Would the vote implement the efficient decision?
- c) Could you design a mechanism that implements the efficient decision? Explain why the mechanism will implement the efficient decision.