## 10.5.3.9

## EE23BTECH11063 - Vemula Siddhartha

## **Question:**

If the sum of first 7 terms of an AP is 49 and that of 17 terms is 289, find the sum of first n terms.

## **Solution:**

$$s(n) = \frac{n+1}{2} (2x(0) + nd) u(n)$$
 (1)

From Table 0:

$$x(0) + 3d = 7 (2)$$

$$x(0) + 8d = 17 \tag{3}$$

From equations 2 and 3, the augmented matrix is:

$$s(n) = x(n) * u(n)$$
(10)

$$s(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} S(z)$$

$$\implies S(z) = X(z) \ U(z) \tag{11}$$

$$\implies S(z) = \left(\frac{1}{1 - z^{-1}} + \frac{2z^{-1}}{(1 - z^{-1})^2}\right) \left(\frac{1}{1 - z^{-1}}\right) (12)$$

$$S(z) = \frac{1}{(1-z^{-1})^2} + \frac{2z^{-1}}{(1-z^{-1})^3}$$

$$= z \frac{z^{-1}}{(1-z^{-1})^2} + \left(-z \frac{d}{dz} \left(z \frac{z^{-1}}{(1-z^{-1})^2}\right)\right)$$
(14)

$$x(n+1) \longleftrightarrow zX(z)$$

$$= (n+1) u(n) + n((n+1) u(n)) \qquad (15)$$

$$\implies s(n) = (n+1)^2 u(n) \tag{16}$$

$$\begin{pmatrix} 1 & 3 & 7 \\ 1 & 8 & 17 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - R_1} \begin{pmatrix} 1 & 3 & 7 \\ 0 & 5 & 10 \end{pmatrix}$$

$$\leftarrow \xrightarrow{R_1 \leftarrow R_1 - \frac{3}{5}R_2} \begin{pmatrix} 1 & 0 & 1 \\ 0 & 5 & 10 \end{pmatrix}$$

$$(5)$$

$$\stackrel{R_2 \leftarrow \frac{R_2}{5}}{\longleftrightarrow} \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \end{pmatrix} \tag{6}$$

$$\implies \begin{pmatrix} x(0) \\ d \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \tag{7}$$

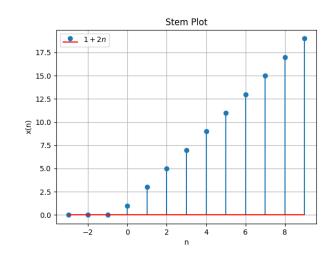


Fig. 0. Stem Plot of x(n)

From Table 0:

$$\implies x(n) = (1+2n)u(n)$$

$$x(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} X(z)$$
(8)

From Table 0:

$$\implies X(z) = \frac{1}{1 - z^{-1}} + \frac{2z^{-1}}{(1 - z^{-1})^2} \quad \{z \in \mathbb{C} : |z| > 1\}$$
(9)

Variable	Description	Value
x(0)	First term of the AP	?
d	Common difference of the AP	?
s(n)	Sum of <i>n</i> terms of the AP	?
s (6)	Sum of 7 terms of the AP	49
s(16)	Sum of 17 terms of the AP	289
x(n)	General term	?
TABLE 0		

Variables Used