from linearmodels import OLS from linearmodels import PanelOLS %matplotlib inline import warnings warnings.filterwarnings('ignore') **About Our Dataset** I compiled this dataset from sources such as the World Bank, the International Monetary Fund, and the Federal Reserve. It features various economic and social factors such as GDP, trade, corruption, literacy, etc. This data spans 131 countries over the course of 11 years, from 2006 to 2016. In this project, the focus will only be on 3 variables: First we have LN\_INCOMEPC: The natural log of income per capita. Traditionally, in econometrics, income per capita is logged to convert it into a psuedo growth rate. This is done to minimize the otherwise large differences across countries in income per capita, and in many ways, growth of income per capita is a better measure of prosperity. Data is taken from the World Bank and is in constant 2011 dollars. Next, we have **EIU** - our measure of democracy. EIU is the Economist's measure of democracy. It is not an unbiased measure of democratic institutions like the Polity IV index. EIU also includes cultural aspects like apathy toward government, trust, access to media, and contested elections (see <u>EIU methodology on pg 48</u>). This, however, has the drawback of capturing social and economic elements in addition to just democracy. Access to media and trust can be correlated with stability, hence our democracy measure captures more than just democracy. For instance, a country in which the people trust their government is likely to be one in which the government is doing a good job, which would likely be correlated with higher income per capita. Some things, like contested elections and apathy, we want to capture, but not stability. To control for this, we need a third variable. Our final variable is **LAW**. Rule of law attempts to capture the extent to which people obey laws and trust the government itself. Specifically, it looks at how well contracts are enforced, how honest the police and courts are, and how likely crime is. This captures the "trust in government" part of EIU which we do not want to count as democracy. Adding Law to our regression allows us to compare countries with different levels of democracy but similar levels of stability. The data is taken from the World Bank. It is important to note that the latter two are indices compiled from surveys or judged by so-called experts, and hence have a layer of subjectivity. However, the Economist and the World Bank are both experienced and well-respected in their fields, so we can have a strong degree of confidence in these measures. In [2]: import numpy as np import pandas as pd data = pd.read csv(r'C:\Users\Viral Shanker\Desktop\Combined2016new3.csv') data.head() j = (pd.get dummies(data["code"])) data1 = pd.concat([data, j], axis = 1) j = data1.columns j.drop("BOL") cs = j[97:]t = ['2', '3', '4', '5', '6', '7', '8', '9', '10', '11'] data["logInvestment"] = np.log(data["Investment"]) data["EIU"] = data["eiu"] We first do basic OLS regression. We regress LN\_INCOMEPC on LAW and EIU In [3]: mod = OLS(data.LN INCOMEPC, data[["eiu", "LAW", "constant"]]) res = mod.fit() res.summary Out[3]: **OLS Estimation Summary** Dep. Variable: LN\_INCOMEPC 0.6972 R-squared: OLS Estimator: Adj. R-squared: 0.6967 No. Observations: 1420 F-statistic: 5884.2 Date: Sat, Oct 19 2019 | P-value (F-stat) 0.0000 Time: 21:51:46 **Distribution:** chi2(2) Cov. Estimator: robust Parameter Estimates Std. Err. T-stat P-value Lower CI Upper CI Parameter 5.8356 0.0000 0.0808 eiu 0.1216 0.0208 0.1624 LAW 4.6173 0.1703 27.113 0.0000 4.2835 4.9510 constant 5.2779 0.0690 76.437 0.0000 5.1426 5.4132 LN\_INCOMEPC is positively correlated with LAW and EIU We have both LAW and EIU being positively correlated with income, LAW far more so with a large coefficient and massive tstatistic, but EIU is also positive and very significant. Now, we try without LAW and do a basic regression of income on democracy to get a point of reference. In [4]: mod = OLS(data.LN INCOMEPC, data[["eiu", "constant"]]) res = mod.fit() res.summary Out[4]: **OLS Estimation Summary** Dep. Variable: LN\_INCOMEPC 0.5359 R-squared: Estimator: OLS Adj. R-squared: 0.5355 No. Observations: 1420 F-statistic: 1558.8 Date: Sat, Oct 19 2019 | P-value (F-stat) 0.0000 Time: 21:51:46 **Distribution:** chi2(1) **Cov. Estimator:** robust Parameter Estimates Parameter Std. Err. T-stat P-value Lower CI Upper CI eiu 0.5247 0.0133 39.482 0.0000 0.4987 0.5508 constant 5.4002 0.0909 59.416 0.0000 5.2220 5.5783 EIU is much larger As expected, we get a strong positive correlation, and a very significant one at that. EIU's coefficient is around 5 times as big as it was in the previous regression, so clearly, LAW is doing its job and capturing part of EIU's effect. Now to visualize: In [5]: %matplotlib inline import seaborn as sns from matplotlib import pyplot as plt plt.style.use("fivethirtyeight") fig = plt.figure(figsize=(20,10)) sns.regplot(x = "eiu", y = "LN\_INCOMEPC", data=data) plt.title("Income vs Democracy") Out[5]: Text(0.5,1,'Income vs Democracy') Income vs Democracy We can do better Some issues are immediately obvious. First of all, we're treating every country/year combination as independent. For instance, 2006 Russia is bound to be very similar to 2007 Russia, so on the graph at least, one point per country is enough. It is misleading to treat each point as an independent entity. Regression-wise, we can try and account for the time-effects, and see what results we get. This means we have dummy variables for each year. Note that we drop the dummy variable of year 1 to avoid the dummy variable trap. In [6]: mod = OLS(data.LN INCOMEPC, data[["eiu", "constant",'2', '3', '4', '5', '6', '7', '8', '9', '10', '1 1']]) res = mod.fit() res.summary **OLS Estimation Summary** LN\_INCOMEPC | R-squared: 0.5375 Dep. Variable: Estimator: OLS **Adj. R-squared**: | 0.5339 No. Observations: 1420 F-statistic: 1571.4 Date: Sat, Oct 19 2019 | P-value (F-stat) 0.0000 Time: 21:51:47 **Distribution:** chi2(11) **Cov. Estimator:** robust Parameter Estimates Parameter | Std. Err. | T-stat | P-value | Lower CI | Upper CI 0.0000 0.5246 0.0133 39.493 0.4986 0.5506 eiu constant 5.2954 5.5415 0.1256 42.174 0.0000 5.0493 0.1308 0.2571 0.7971 -0.2227 0.2900 0.0336 0.0459 0.1303 0.3525 0.7245 -0.2095 0.3013 0.0517 0.1297 0.3983 0.6904 -0.2025 0.3058 0.1091 -0.1453 0.3635 0.1298 0.8407 0.4005 0.9009 | 0.3677 -0.1380 0.3727 0.1174 0.1303 0.1274 0.1297 0.9821 0.3260 -0.1268 0.3816 0.1419 0.1299 1.0920 0.2748 -0.1128 0.3966 0.1571 0.1292 1.2158 0.2241 -0.0962 0.4104 10 0.4221 0.1689 0.1292 1.3072 0.1911 -0.0843 11 0.2067 0.1287 1.6063 0.1082 -0.0455 0.4590 Almost no change in terms of our predictions. We try again with LAW In [7]: mod = OLS(data.LN INCOMEPC, data[["eiu", "LAW", "constant",'2', '3', '4', '5', '6', '7', '8', '9', '10', '11']]) res = mod.fit() res.summary **OLS Estimation Summary** Dep. Variable: LN\_INCOMEPC | R-squared: 0.6995 Adj. R-squared: OLS 0.6970 **Estimator:** 1420 No. Observations: F-statistic: 5896.7 Sat, Oct 19 2019 P-value (F-stat) Date: 0.0000 Time: 21:51:47 **Distribution:** chi2(12) Cov. Estimator: robust Parameter Estimates Parameter | Std. Err. | T-stat P-value Lower CI Upper CI 0.0208 5.7636 0.0000 0.0790 0.1605 eiu 0.1197 LAW 0.1702 0.0000 4.3032 4.9704 4.6368 27.244 5.2305 0.00005.0323 5.4288 0.1011 51.714 constant 0.0063 0.1092 0.0580 0.9537 -0.2077 0.2203 0.1152 -0.0974 0.1085 -0.8982 0.3691 -0.3101 -0.2731 0.7848 -0.0291 0.1064 -0.2376 0.1795 0.0208 0.1055 0.1972 0.8437 -0.1860 0.2276 0.0707 0.1060 0.6674 0.5045 -0.1370 0.2784 0.0469 0.1056 0.4438 0.6572 -0.1601 0.2538 0.0859 0.1052 0.8161 0.4144 -0.1204 0.2921 0.1222 0.1052 1.1611 0.2456 -0.0841 0.3285 10 1.5051 -0.0478 0.1583 0.1052 0.1323 0.3644 11 -0.0629 0.3435 0.1403 0.1037 1.3531 0.1760 Very similar results again While it is certainly correct to include the time dummies, they do not seem to be altering our estimates too much. We can leverage our cross-sectional data more, however. The Two-Way Panel As we had dummies for time, we now add dummies for each country using the PANELOLS method. These fixed effects capture all unique variation within each country as well as across countries each year. In [39]: data3 = data.set index(['code','TIME TREND']) mod = PanelOLS(data3.LN\_INCOMEPC, data3[["eiu", "LAW", "constant"]], time\_effects = True, entity\_eff ects = **True**) res = mod.fit() res.summary Out[39]: PanelOLS Estimation Summary Dep. Variable: LN\_INCOMEPC | R-squared: 0.1103 PanelOLS 0.2517 Estimator: R-squared (Between): 1420 No. Observations: R-squared (Within): 0.0676 Sat, Oct 19 2019 R-squared (Overall): Date: 0.2505 Time: 22:48:38 Log-likelihood 1808.0 **Cov. Estimator:** Unadjusted F-statistic: 79.182 P-value **Entities:** 130 0.0000 Avg Obs: 10.923 **Distribution:** F(2,1278) Min Obs: 1.0000 Max Obs: 11.000 F-statistic (robust): 79.182 0.0000 P-value 11 **Distribution:** F(2,1278) Time periods: Avg Obs: 129.09 Min Obs: 129.00 130.00 Max Obs: Parameter Estimates Parameter | Std. Err. | T-stat P-value Lower CI Upper CI 0.0319 0.0064 4.9619 0.0000 0.0193 0.0445 eiu LAW 0.8589 0.0796 10.790 0.0000 0.7028 1.0151 constant 7.7931 0.0524 148.64 0.0000 7.6903 7.8960 F-test for Poolability: 1393.9 P-value: 0.0000 Distribution: F(139,1278) Included effects: Entity, Time **Democracy is far less significant** Once we account for each country individually, we find that democracy has almost no effect on income per capita. Its coefficient is an order of magnitude smaller than it was in the normal OLS and time-effects regressions. Note however, that EIU is still significant. Two-Way Panel with only EIU In [9]: data3 = data.set\_index(['code','TIME\_TREND']) mod = PanelOLS(data3.LN\_INCOMEPC, data3[["eiu", "constant"]], time\_effects = True, entity\_effects = res = mod.fit() res.summary Out[9]: PanelOLS Estimation Summary Dep. Variable: LN\_INCOMEPC R-squared: 0.0292 PanelOLS Estimator: R-squared (Between): 0.0818 No. Observations: 1420 0.0227 R-squared (Within): Date: Sat, Oct 19 2019 | R-squared (Overall): 0.0809 Time: 21:51:47 Log-likelihood 1746.1 Cov. Estimator: Unadjusted F-statistic: 38.465 **Entities:** 130 P-value 0.0000 Avg Obs: 10.923 **Distribution:** F(1,1279) Min Obs: 1.0000 Max Obs: 11.000 F-statistic (robust): 38.465 P-value 0.0000 Time periods: **Distribution:** F(1,1279) 129.09 Avg Obs: Min Obs: 129.00 130.00 Max Obs: Parameter Estimates Std. Err. T-stat P-value Lower CI Upper CI **Parameter** 0.0412 0.0066 6.2020 0.0000 0.02820.0543 eiu 0.0385 212.90 0.0000 8.1199 8.2709 constant 8.1954 F-test for Poolability: 1963.2 P-value: 0.0000 Distribution: F(139,1279) Included effects: Entity, Time **Democracy is still very small** Democracy, even without LAW, remains small. Note that it is still very comparable to the regression with LAW in it. Most of the effects of LAW are captured by the time and country dummies. Let's visualize average LN\_INCOMEPC and average EIU to get an idea of where our countries fall It becomes difficult to capture PANEL data in a graph due to the number of dimensions. Hidden in the above regression are 130 country dummies and 10 time dummies. Still, visualization gives us a better sense of our data, far more so than our first plot. To prepare the data, we group by country name and get average values over 11 years for all our columns. We now have as many rows as countries - 131. In [10]: data2 = data data2 = data2.groupby("Country", as\_index = False).mean() **Drop Bosnia** We are actually missing EIU values for Bosnia, so we simply drop it. Previous graphs and regressions automatically drop missing values, but this time we need to manually do it. In [11]: data2 = data2[data2.Country != "Bosnia"] OLS regression again to get an idea of what to expect In [12]: mod = OLS(data2.LN\_INCOMEPC, data2[["eiu", "constant"]]) res = mod.fit() res.summary Out[12]: **OLS Estimation Summary** LN\_INCOMEPC | R-squared: 0.5484 Dep. Variable: OLS Estimator: Adj. R-squared: 0.5449 No. Observations: 130 F-statistic: 151.08 Date: Sat, Oct 19 2019 | P-value (F-stat) 0.0000 Distribution: Time: 21:51:47 chi2(1) Cov. Estimator: robust Parameter Estimates **Parameter** Std. Err. T-stat P-value Lower CI Upper CI eiu 0.5321 0.0433 12.291 0.0000 0.4473 0.6170 5.3603 0.2959 18.115 0.0000 4.7803 constant 5.9402 Similar to original OLS Again, very similar to our original OLS regression except for the lower t-stat, though still very significant. In [13]: | #Source of label\_point function: #https://stackoverflow.com/questions/46027653/adding-labels-in-x-y-scatter-plot-with-seaborn def label\_point(x, y, val, ax):  $a = pd.concat({'x': x, 'y': y, 'val': val}, axis=1)$ for i, point in a.iterrows(): ax.text(point['x']+.02, point['y'], str(point['val'])) In [14]: %matplotlib inline ax = sns.lmplot(x = "eiu", y = "LN\_INCOMEPC", data=data2, size = 15) label point(data2.eiu, data2.LN\_INCOMEPC, data2.Country, plt.gca()) plt.title("Average Income vs Average Democracy") Out[14]: Text(0.5,1,'Average Income vs Average Democracy') Average Income vs Average Democracy Saudi Arabia Kazakhstan Belarus Sierra Leone Mozambique Central African Republic A much clearer graph With the LN\_INCOMEPC and EIU values averaged, we can label each point and get a very real sense of our data distribution. There are some obvious outliers, which make sense with some geopolitical context. Saudi Arabia is not democratic at all yet is prosperous, and India, while democratic, struggles when it comes to income per capita. Adding LAW to the averages regression In [15]: mod = OLS(data2.LN INCOMEPC, data2[["eiu", "LAW", "constant"]]) res = mod.fit() res.summary Out[15]: **OLS Estimation Summary** LN\_INCOMEPC Dep. Variable: R-squared: 0.7058 Adj. R-squared: Estimator: OLS 0.7012 F-statistic: No. Observations: 130 569.40 Date: Sat, Oct 19 2019 | P-value (F-stat) 0.0000 Time: 21:51:48 **Distribution:** chi2(2) Cov. Estimator: robust Parameter Estimates P-value Lower CI Upper CI **Parameter** Std. Err. T-stat 0.1161 0.0695 1.6711 0.0947 -0.0201 0.2524 eiu LAW 4.7102 0.5716 8.2403 0.0000 3.5899 5.8306 constant 5.2595 0.2238 23.498 0.0000 4.8209 5.6982 **Democracy insignificant** It is interesting to note that EIU becomes close to insignificant here. That said, given our small sample, these results overall hold less value than our full-sample regressions since our samples are down to 131 as opposed to 1420. **Instrument Variable Regression** The above methodologies make no claim at causation. It could be that there exist confounding variables, that is, variables we have not included in our regression that affect both democracy and income per capita, which can give biased results. Or, we may have a reverse causality issue where income causes democracy to go up, which in turn causes income to go up, and so on. The only known way to empirically measure causation is to use some variation of the instrumental variable regression technique. We need an instrumental variable (IV) that satisfies two conditions: • Relevancy: The IV we choose must be relevant to the endogenous (in our case, EIU). This is easily tested with a simple regression of EIU on our instrument. This known as our "first stage." • Exclusion: (The tough one) The IV must be exogenous with respect to the y-variable (in our case, LN\_INCOMEPC). There is no real statistical way to test for this. One must be able to argue that this is the case for the chosen instrument. Our Instrument: demoWar demoWar is a simple dummy variable. demoWar is 1 if the country has gone to war with a democracy as defined by the Polity index, and a 0 otherwise. First Stage Regression In [16]: mod = OLS(data.eiu, data[["demoWar", "constant"]]) res = mod.fit() res.summary **OLS Estimation Summary** Dep. Variable: eiu R-squared: 0.0504 OLS Estimator: Adj. R-squared: 0.0498

**Democracy and Income** 

Importing needed libraries

from linearmodels import OLS import statsmodels.api as sm

from linearmodels import IV2SLS from linearmodels import IVGMM

from linearmodels import PanelOLS

In [1]: import numpy as np

import linearmodels

import numpy as np import linearmodels

we show that democracy in fact does not have a positive impact on income.

Democracy and economic prosperity go hand in hand. Countless studies have shown that in cross-sectional data (data across time and location) there exists a very siginificant correlation between income and democracy. However, whether democracy directly causes income growth is a more contentious matter. With a few exceptions, it is true that most rich countries are democracies, but this is likely due to imperfect models not accounting for issues like reverse causality and confounding

variables. Using the instrument variable tenchnique to establish causality and PANEL methods to control in-country variation,

In theory at least, we have satisfied the exclusion restriction. The IV regression We assume LAW is exogenous (this assumption is explored further on) and EIU is endogenous. Our instrument is demoWar. In [17]: sample = IVGMM(data.LN\_INCOMEPC, data[["constant", "LAW"]], data[["eiu"]], data["demoWar"]) sres = sample.fit() sres.summary **IV-GMM Estimation Summary** Dep. Variable: LN\_INCOMEPC R-squared: 0.4395 Estimator: IV-GMM Adj. R-squared: 0.4387

3217.7

0.0000

chi2(2)

7.0955

-0.1122

P-value Lower CI Upper CI

6.4014

-0.8968

**Democracy hurts income?** We see that democracy has flipped signs and turned negative! While EIU is still significant, it is less significant than it has been in previous regressions.

Distribution:

robust than OLS - the inclusion or exclusion of one variable can yield completely different results.

F-statistic:

**Distribution:** 

17.333 0.0000 5.6538

6.1915 0.0000

-2.5205 0.0117

Sat, Oct 19 2019 | P-value (F-stat)

No. Observations:

Cov. Estimator:

Parameter Estimates

demoWar -1.1959

constant 5.9988

It's Relevant

democratic.

reasoning

issue, like this.

No. Observations:

Cov. Estimator:

Parameter Estimates

constant 6.3747

Endogenous: eiu Instruments: demoWar **GMM Covariance** Debiased: False

including LAW.

sres.summary

Dep. Variable:

**Cov. Estimator:** 

Estimator:

Date:

Time:

constant

eiu

Out[18]:

Robust (Heteroskedastic)

Only democracy IV regression

21:51:48

robust

Flaws and Recourses:

9.3664

-0.5045

Date:

Time:

eiu

1420

21:51:48

Parameter | Std. Err. | T-stat

0.3678

1.5128

0.2002

robust

Out[17]:

**Parameter** 

Date:

Time:

1430

21:51:48

Std. Err.

0.1241

0.0632

robust

F-statistic:

**Distribution:** 

0.0000

0.0000

Sat, Oct 19 2019 P-value (F-stat)

T-stat

-9.6333

94.930

92.800

0.0000

chi2(1)

P-value Lower CI Upper CI

-1.4392

5.8750

-0.9526

6.1227

We get a t-statistic of -9.6, which is right around where we want it to be. Generally, a t-stat of 10 in the first stage is considered a strong instrument. This tells us that a country having gone to war with a democracy is correlated with that country being less

Exogneity: And now we must leave the safe abode of statistics behind, and rely on logic and

The <u>Democratic Peace Theory</u> alleges that democracies are far less likely to go to war with one another than they are to go to war with non-democracies. Here we have a channel which shows demoWar directly affecting democracy. It is important to note that this effect is independent of income and stability. According to the theory, the mere fact of being a democracy is enough to dissuade others from going to war with them. This instrument has also been used in several other papers exploring the same

In [18]: sample = IVGMM(data.LN\_INCOMEPC, data[["constant"]], data[["eiu"]], data["demoWar"]) sres = sample.fit() **IV-GMM Estimation Summary** LN\_INCOMEPC | R-squared: 0.4252 IV-GMM Adj. R-squared: 0.4248 No. Observations: 1420 F-statistic: 24.085 Sat, Oct 19 2019 | P-value (F-stat) 0.0000

Now we try IV with only EIU. Again, recall that democracy will capture some of the stability aspects we have tried to avoid by

chi2(1)

Parameter Estimates Parameter Std. Err. T-stat P-value Lower CI Upper CI 6.7789 0.3359 20.180 0.0000 6.1205 7.4373 0.2862 0.0583 4.9076 0.0000 0.1719 0.4006 Endogenous: eiu Instruments: demoWar **GMM Covariance** Debiased: False

Robust (Heteroskedastic) **Democracy stays positive** We retain a weaker but still significant coefficient for democracy in this case. Because the inclusion of LAW flips the sign, it is evident once again that democracy is capturing quite a lot of LAW's effect. This also serves as a warning in that IV is far less