

# DESIGN METHOD FOR LOCAL SCOUR AT BRIDGE PIERS

By B. W. Melville<sup>1</sup> and A. J. Sutherland<sup>2</sup>

**ABSTRACT:** A design method for the estimation of equilibrium depths of local scour at bridge piers is presented. The method is based upon envelope curves drawn to experimental data derived mostly from laboratory experiments. The laboratory data include wide variations in flow velocity and depth, sediment size and gradation, and pier size, shape, and alignment. Local scour depth estimation is based upon the largest possible scour depth that can occur at a cylindrical pier, which is  $2.4D$ , where  $D$  = the pier diameter. According to the method, this depth is reduced using multiplying factors where clear-water scour conditions exist, the flow depth is relatively shallow, and the sediment size is relatively coarse. In the case of nonrectangular piers, additional multiplying factors to account for pier shape and alignment are applied. The method of estimation of local scour depth is summarized in a flow chart.

## INTRODUCTION

Selection of an appropriate design method to estimate equilibrium depths of local scour at bridge piers has perplexed designers for many years. There is a wide variety of formulas available, and no obvious similarity in either their appearance or their predictions. A review of the more popular formulas has been given by Raudkivi and Sutherland (1981). The same publication presents a design method based on many laboratory studies. The method considered sediment gradation and size and flow depth effects but did not consider the possibility of live-bed scour.

Studies involving live-bed scour with uniform and nonuniform sediments have now been completed (Chee 1982; Chiew 1984; Baker 1986). These have explained the apparent conflicts arising from earlier studies, some of which showed live-bed scour exceeding clear-water scour (Garde 1961; Blench 1969; Jain and Fischer 1979) and others of which showed the reverse (Chabert and Engeldinger 1956; Laursen 1958, 1962; Hancu 1971; Breusers et al. 1977). These new data have made it possible to place all data within one framework. Clear-water scour becomes a special case, as does scour of uniform material, a rare event in practice.

Live-bed scour introduces two further processes. Threshold or critical flow conditions become of significance and are described herein by the mean flow velocity  $U_c$  appropriate for the stated sediment and channel slope. Of equal importance are the flow conditions beyond which armoring of the channel bed is impossible. There are also characterized by the mean flow velocity  $U_{ca}$ , which again depends on the sediment characteristics and channel slope.

Threshold and limiting armor conditions are discussed first. The general framework for scour estimation is then presented, and the effect of the

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significant parameters described. This leads directly to a design method, which is used on some illustrative examples.

### THRESHOLD CONDITIONS

The Shields diagram (Henderson 1966) remains the most effective way of determining threshold conditions for uniform sediments. For given fluid density and viscosity and sediment density, the Shields diagram can be used, as in Fig. 1, to obtain a plot of shear velocity  $u_{*c}$  against grain size,  $d_{50}$ . Water and sediment with densities of  $1,000 \text{ kg/m}^3$  and  $2,650 \text{ kg/m}^3$ , respectively, have been assumed in the preparation of Fig. 1. A useful relation for the coarser grain sizes  $d_{50} > 6 \text{ mm}$  is

$$u_{*c} = 0.03 d_{50}^{1/2} \dots\dots\dots (1)$$

where  $u_{*c}$  is in m/s, and  $d_{50}$  in mm. Threshold shear velocity is converted to threshold mean flow velocity  $U_c$  using, as an approximation, the logarithmic form of the velocity profile

$$\frac{U_c}{u_{*c}} = 5.75 \log \left( 5.53 \frac{y}{d_{50}} \right) \dots\dots\dots (2)$$

where  $y$  = flow depth. For uniform sediments,  $U_c$  marks the transition from clear-water to live-bed scour conditions.

Determination of threshold conditions for nonuniform sediments is not so clear-cut. The effects of particle size distribution may be important, and thus  $U_c$  would depend upon both the median grain size  $d_{50}$  and the geometric standard deviation  $\sigma_g = d_{84}/d_{50}$ . With nonuniform sediments, a flow can disturb the grains, removing some but simply rearranging others into a stable pattern that develops into an armored bed and stabilizes. Such flows are considered herein to be above threshold. Values of  $U_c$  are found using a suggestion first made by Neill (1968) that many of the intermediate sizes will move when flow conditions based on  $d_{50}$  exceed the Shields criterion. Neill claimed this to work well at least for  $\sigma_g < 2.5$ . Fig. 1 and

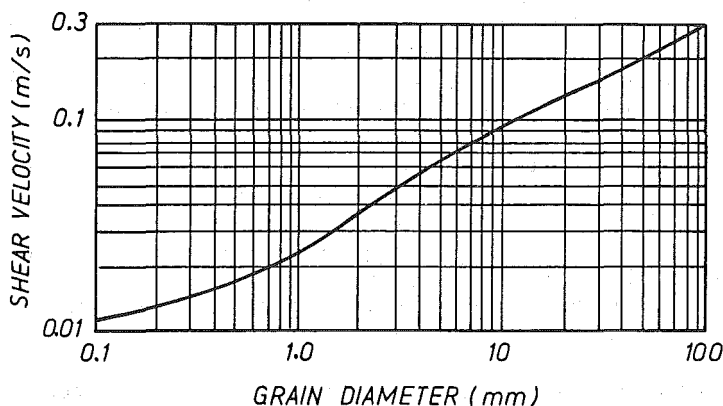


FIG. 1. Shields Chart for Threshold Condition of Uniform Sediments in Water

TABLE 1. Exponent  $m$ -Values for Eq. 3

Assumed value of $d_{\max}$ (1)	$m$ (2)
$d_{90}$	1.28
$d_{95}$	1.65
$d_{98}$	2.06
$d_{99}$	2.34

Eq. 2 based on  $d_{50}$  are used herein to determine  $U_c$  for nonuniform material.

### LIMITING ARMOR CONDITIONS

The flow condition beyond which armoring of a nonuniform channel bed is impossible is termed the limiting armor condition. This condition represents the coarsest or most stable armored bed for a given bed material and can be characterized by the mean velocity  $U_{ca}$ . At flows greater than  $U_{ca}$ , no armor layer can form, while at flows less than  $U_{ca}$ , the armored bed will be finer ( $d_{50a}$  smaller) or less stable than that formed at  $U_{ca}$ .

Each sediment has a unique value of  $U_{ca}$ , dependent on the sediment size and grading. For a given  $d_{50}$ ,  $U_{ca}$  increases with increasing  $\sigma_g$ . Chin (1985) showed that the value of  $U_{ca}$  for a given sediment is dependent on the maximum  $d_{\max}$  size and gives a method to determine  $U_{ca}$  using  $d_{\max}$ , which can be found from  $d_{50}$  and  $\sigma_g$  if a logarithmic normal distribution is assumed:

$$d_{\max} = \sigma_g^m d_{50} \quad \dots \dots \dots (3)$$

where  $m$  depends upon the size chosen for  $d_{\max}$  as shown in Table 1.

Chin (1985) showed that the  $d_{50}$  size of the coarsest possible armor,  $d_{50a}$ , is equal to  $d_{\max}/1.8$ . This value of  $d_{50a}$  is used to determine the critical shear velocity of the armored bed,  $u_{*ca}$  from Shields (Fig. 1). Calculation of  $U_{ca}$  then follows from Eq. 2, using  $d_{50a}$  as the grain size. Chin's (1985) laboratory experiments were conducted with no sediment replenishment from upstream of the test section. The test beds were allowed to degrade until erosion had effectively stopped. The more common condition for scouring at bridge sites involves sediment supply from upstream. Baker (1986) showed, using a sediment-recirculating flume, that in the latter case, the appropriate flow velocity  $U_a$  to characterize the limiting armor condition for scour determination is  $0.8U_{ca}$ . Baker explained that the bed armor layer for the condition of sediment supply from upstream is finer than the critical armor layer as determined by Chin (1985). This is because the sediment input from upstream limits erosion on the approach bed to the bridge site, effectively preventing the exposure of the number of coarse grains necessary to form the critical armor layer. For nonuniform sediments,  $U_a$  is considered to mark the transition from clear-water to live-bed scour conditions.

In practice, the value of  $U_a$ , determined using  $U_a = 0.8U_{ca}$ , needs to be checked against the physical constraint that  $U_a$  cannot be less than  $U_c$ . In the case of  $U_a < U_c$ , the proposed remedy is to set  $U_a = U_c$  and assume

# INPUT DATA:

GRAIN SIZE DISTRIBUTION,  $d_{50}$ ,  $\sigma_g$ ,  $d_{max}$   
FLOW DEPTH,  $y$

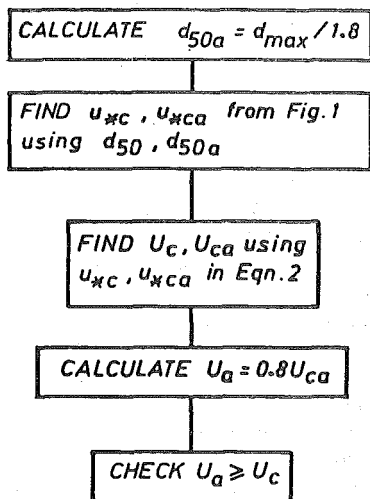


FIG. 2. Flow Chart to Calculate  $U_a$ , Limiting Armor Velocity

that the bed material is behaving as a uniform sediment. The method of evaluation of  $U_a$  is summarized in the flow chart (Fig. 2).

## FRAMEWORK FOR ANALYSIS OF LOCAL SCOUR

Equilibrium depth of local scour  $d_s$  at a pier can be written

$$d_s = f(\rho, \nu, U, y, \rho_s, d_{50}, \sigma_g, g, D, Sh, Al) \dots \dots \dots (4)$$

where  $\rho$  and  $\nu$  = fluid density and kinematic viscosity;  $U$  = mean flow velocity;  $y$  = flow depth;  $\rho_s$  = sediment density;  $g$  = gravitational acceleration;  $D$  = pier width normal to the flow;  $Sh$  and  $Al$  = parameters describing the shape and alignment of the pier; and  $f$  = "a function of." Eq. 4 can be written

$$\frac{d_s}{D} = f\left(\frac{UD}{\nu}, \frac{U^2}{gd_{50}}, \frac{y}{D}, \frac{\rho_s}{\rho}, \frac{d_{50}}{D}, \sigma_g, Sh, Al\right) \dots \dots \dots (5)$$

The density ratio is assumed constant, and the Reynolds number  $UD/\nu$  influences are assumed negligible for the highly turbulent flows envisaged. Thus

$$\frac{d_s}{D} = f\left(\frac{U^2}{gd_{50}}, \frac{y}{D}, \frac{d_{50}}{D}, \sigma_g, Sh, Al\right) \dots \dots \dots (6)$$

The functional relation has been evaluated using laboratory data by writing it in the form

$$\frac{d_s}{D} = K_I K_y K_d K_\sigma K_s K_\alpha \dots \dots \dots (7)$$

where the  $K$ s are expressions, presented in the following, describing the influence of each parameter in Eq. 6:  $K_I$  = flow intensity;  $K_y$  = flow depth;  $K_d$  = sediment size;  $K_\sigma$  = sediment gradation; and  $K_s$  and  $K_\alpha$  = pier shape and alignment, respectively. Each parameter is now considered individually.

### Flow Intensity

The Shields diagram defines a  $u_{*c}$  for a given  $d_{50}$ . A corresponding  $U_c$  can be found for the given flow depth, and thus the parameter  $U^2/gd_{50}$  can be written, using the given data as  $U/U_c$ . As such, this ratio is a measure of flow intensity and determines whether or not grain motion occurs. For  $U/U_c < 1$ , clear-water scour conditions pertain for both uniform and nonuniform sediments. If  $\sigma_g < 1.3$ , the sediment acts as a uniform sediment, and for  $U/U_c > 1$ , live-bed scour occurs. If  $\sigma_g > 1.3$  and  $1 < U/U_c < U_a/U_c$ , then armoring of the bed will occur as scouring proceeds, and it is considered that clear-water scour exists. For  $1 < U/U_a$ , there is no armoring, and live-bed scour occurs.

The flow intensity parameter thus determines the scouring processes that are important. It is shown later in the paper that a more appropriate form for this parameter is  $[U - (U_a - U_c)]/U_c$ , in which the difference  $(U_a - U_c)$  reflects the influence of sediment grading.

### Flow Depth Ratio

Ettema (1980), Chiew (1984), and others showed that scour depth increases with flow depth up to a limiting value of the flow depth ratio  $y/D$ , beyond which there is no influence of flow depth. Ettema explained that for shallow flows, the surface roller that forms ahead of the bridge pier interferes with the scour action of the horseshoe vortex because the two have opposite senses of rotation. With increasing flow depth, the interference reduces until there is no significant effect at  $y/D \sim 3$ . Data by Shen (1966), Ettema (1980), Chee (1982), and Chiew (1984) for uniform sediments under clear-water and live-bed conditions are shown in Fig. 3, in which  $K_y$ , the flow depth factor, is the ratio of  $d_s/D$  at a particular value of  $y/D$  to that at  $y/D \geq 4$ . These data all have  $D/d_{50} \geq 50$ . Ettema (1980) showed that the relationship between scour depth and flow depth is, in fact, a family of curves at different values of  $D/d_{50}$ . However, the effects of sediment size ratio will be considered separately in the following.

Also shown in Fig. 3 are data by Davoren (1985), obtained at a 1.5-m diameter pier in the Ohau River, New Zealand, during steady high flows. The bed material was nonuniform, with  $d_{50} = 20$  mm and  $\sigma_g = 5.3$ , such that  $D/d_{50} = 75$  and  $D/d_{\max} \sim 5$ .

For design purposes, the expression recommended for  $K_y$  is

$$K_y = 1.0, \quad \text{if } y/D > 2.6 \dots \dots \dots (8a)$$

$$K_y = 0.78 (y/D)^{0.255}, \quad \text{if } y/D < 2.6 \dots \dots \dots (8b)$$

This is shown in Fig. 3.

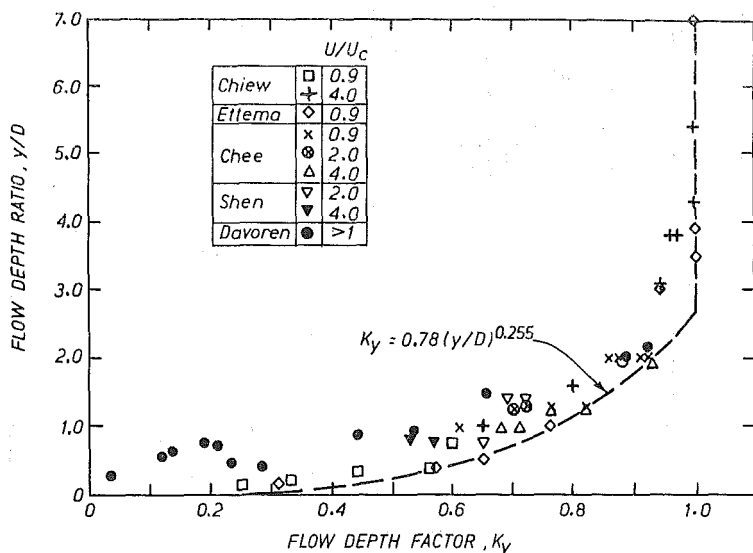


FIG. 3. Influence of Flow Depth on Scour Depth

### Sediment Size Ratio

Chiew's (1984) live-bed data for uniform sediments and those of Ettema (1980) derived from clear-water flows delineate the effects of the sediment size ratio  $D/d_{50}$  on scour depth as shown in Fig. 4.  $K_d$ , the sediment size factor, is the ratio of  $d_s/D$  at a particular value of  $D/d_{50}$  to that at  $D/d_{50} \geq 50$ , beyond which there is no effect of sediment size. The data show that sediment that is large relative to the pier size effectively limits the scour depth. Ettema (1980) identified two main causes for the reduction in scour depth at low values of  $D/d_{50}$ :

1. The erosion process can be impeded by particles that are large relative to the size of the groove that forms at the base of the scour hole in front of the pier. The groove has been identified as the principle erosion zone for bridge pier scour (Ettema 1980; Melville 1975; Shen et al. 1966) and forms under the action of the downflow that occurs in front of the pier. The downflow is recognized as the main scouring agent (Ettema 1980; Melville 1975; Shen et al. 1966).
2. Coarse particles in the groove may allow the downflow to penetrate the bed, thus dissipating some of the flow energy.

For design purposes the expression recommended for  $K_d$  is

$$K_d = 1.0, \quad \text{if } D/d_{50} > 25 \quad \dots\dots\dots (9a)$$

$$K_d = 0.57 \log (2.24 D/d_{50}), \quad \text{if } D/d_{50} < 25 \quad \dots\dots\dots (9b)$$

This is shown in Fig. 4.

### Sediment Gradation Effects

Work by Ettema (1976) showed that scour depths are reduced dramatically as  $\sigma_g$  increases. The tests were all clear-water tests. Live-bed tests

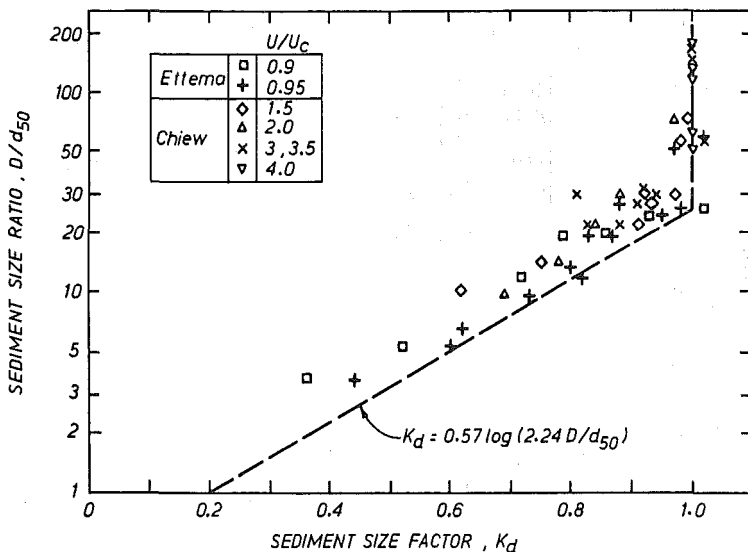


FIG. 4. Influence of Sediment Size on Scour Depth

by Baker (1986) have shown that under these conditions, the reductions are not so dramatic and that at very high flows ( $U/U_c > 4.0$ ), scour depths become almost independent of  $\sigma_g$ .

The results of Baker's (1986) study are shown in Fig. 5, in which all sediments have  $d_{50} = 0.6$  mm, and scour depths are temporal average values (i.e., scour depth due to the passage of bed features is excluded). In general, scour depths for a given  $U/U_c$  decrease as  $\sigma_g$  increases, and also the initial peak or armor peak occurs at higher values of  $U/U_c$  as  $\sigma_g$  increases. The reason for the reduction in scour depths is the presence of an armor layer on the approach bed and in the scour hole. At low flow velocities such that  $U_c < U < U_a$ , the approach bed is covered in an armor layer, and conditions resemble those of clear-water scour. With increasing flow velocity, the armor layer coarsens, and larger scour depths are recorded. The "coarsest possible" armored bed for a given sediment occurs at the velocity  $U_a$ , when conditions on the approach bed resemble the threshold condition for uniform bed material. The armor peak, or local maximum scour depth for a particular  $\sigma_g$ , occurs at  $U = U_a$ . As previously discussed, each sediment has a unique value of  $U_a$  (or  $U_c$ ) dependent on the sediment size and grading or  $d_{max}$  size. A larger  $d_{max}$  leads to a coarser armored bed (at the "coarsest possible" condition) and a correspondingly higher  $U_a$ .

Beyond  $U_a$ , live-bed conditions pertain, with armoring diminishing with increasing flow velocity until all bed particles are mobile at velocities supporting a transition flat bed. Dunes begin to form just above the armor peak velocity  $U_a$ , and the scour depth decreases because, on average, the supply of sediment from incoming bed features is greater than that removed by the scour mechanism. In effect, there is insufficient time between the passage of successive bed features and the consequent input

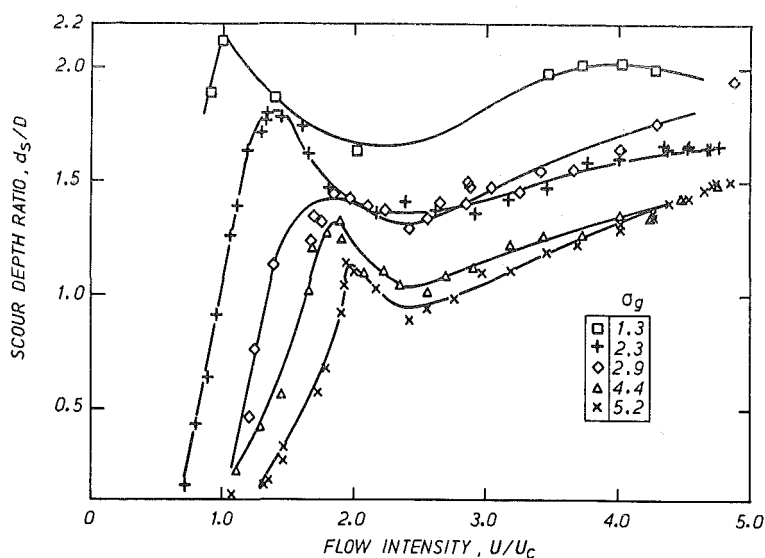


FIG. 5. Influence of  $\sigma_g$  on Scour Depth, Data by Baker (1986),  $d_{50} = 0.6$  mm

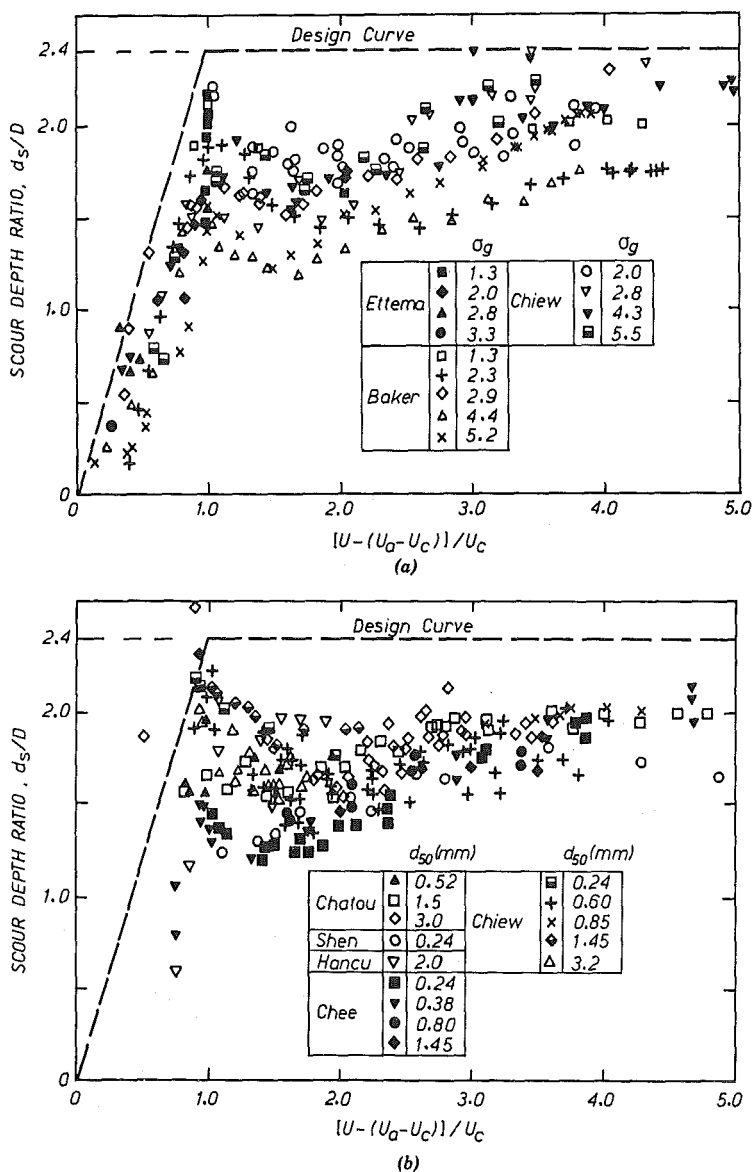
of sediment to the scour hole for the flow to remove the added bed material. The average scour depth attains a local minimum near the velocity producing the largest dunes, and then increases again, reaching a plateau at the transition flat bed condition.

The data in Fig. 5 include the effects of relative sediment size because the coarser particles do not satisfy the condition  $D/d_{50} > 50$ , as discussed previously. The sediment size factor  $K_d$  is used to adjust scour depths for the effects of relative sediment size and is based on the  $d_{50}$  size for uniform sediments. However, the  $d_{50}$  size does not adequately describe a nonuniform sediment. To adjust for the effect of sediment size, the  $d_{50}$  size of the coarsest possible armor layer  $d_{50a}$  is adopted for nonuniform sediments. There are two reasons for the choice of  $d_{50a}$  as the "effective size." First,  $d_{50a}$  is a quantity that can be determined using Chin's (1985) method as discussed previously, and second, the adjusted scour depths as shown in Fig. 6 are conservative (i.e., larger than if a smaller particle size had been used to estimate  $K_d$ ).

The velocity transformation in Fig. 6 has the effect of aligning the armor peaks for nonuniform sediments with the threshold peak for uniform sediment, i.e.,  $[U - (U_a - U_c)]/U_c = 1.0$  corresponds to  $U = U_a$  for nonuniform sediment, and  $U = U_a \equiv U_c$  for uniform sediment and is taken as the transition from clear-water to live-bed scour conditions for all sediments. Also shown in Fig. 6 are data by Ettema (1976), ( $d_{50} = 0.55$ –4.1 mm,  $\sigma_g = 1.3$ –4.6), Chiew (1984), ( $d_{50} = 0.24$ –3.2 mm,  $\sigma_g = 1.3$ –6.5), Chee (1982), ( $d_{50} = 0.24$ –1.45 mm,  $\sigma_g \sim 1.3$ ), Chabert and Engeldinger (1956), ( $d_{50} = 0.52$ –3.0 mm), Hancu (1971), ( $d_{50} = 2.0$  mm), and Shen et al. (1966), ( $d_{50} = 0.24$  mm). Where necessary, the data have been adjusted for relative sediment size.

The effects of  $\sigma_g$  have now been largely accounted for by the introduc-





**FIG. 6. Influence of Flow Intensity on Scour Depth: (a) Data by Baker (1986), Chiew (1984), and Ettema (1980); (b) Data for Uniform Sediments by Chabert and Engeldinger (1956) (Chatou Data), Chee (1982), Chiew (1984), Hancu (1971), and Shen et al. (1966)**

tion of  $U_a$  into the abscissa. The remaining effects are the smaller values of  $d_s/D$  at  $[U - (U_a - U_c)]/U_c = 1.0$  as  $\sigma_g$  increases, and a confused picture at higher values of  $[U - (U_a - U_c)]/U_c$ , where the  $\sigma_g$  value seems of little significance.

For design purposes, an envelope curve is recommended as shown in Fig. 6. It is unreasonable to reduce  $d_s/D$  below 2.4 for the larger flows in a design situation, as failure would then be possible at less than the design flood. Accordingly, it is recommended that, for all  $\sigma_g$  values

$$K_I = 2.4 \left| \frac{U - (U_a - U_c)}{U_c} \right|, \quad \text{if } \frac{U - (U_a - U_c)}{U_c} < 1 \dots \dots \dots (10a)$$

$$K_I = 2.4, \quad \text{if } \frac{U - (U_a - U_c)}{U_c} > 1 \dots \dots \dots (10b)$$

and, consequently,  $K_\sigma = 1.0$ .

### Shape and Alignment Effects

Factors to account for shape and alignment have been published by many researchers (Chabert and Engeldinger 1956; Laursen 1958; Laursen and Toch 1956; Tison 1940; Venkatadri 1965). A selection of shape factors  $K_s$  is given in Table 2. These apply to piers aligned with the flow and are based on  $K_s = 1.0$  for cylindrical piers. Streamlined shapes generally have  $K_s < 1.0$ , but for angles of attack greater than  $10^\circ$ – $15^\circ$ , any advantage of streamlining disappears. In such cases, it is recommended that  $K_s$  be not less than 1.0. Alignment factors  $K_\alpha$  taken from Laursen (1958) are shown in Fig. 7. It is recommended that Table 2 and Fig. 7 be used with the design method proposed herein, and that  $K_s$  be not less than 1.0.

### DESIGN METHOD

The method is shown in flow chart form in Fig. 8. Required input data are the flow conditions  $y$  and  $U$  for the design flood, the sediment properties expressed either as  $d_{50}$  and  $\sigma_g$  or  $d_{50}$  and  $d_{\max}$ , pier size  $D$ , and pier shape and alignment.

Preliminary calculations are required to determine  $u_{*c}$  for  $d_{50}$  using the Shields diagram or Fig. 1, and  $U_c$  from the velocity profile of Eq. 2. Next, the median grain size of the coarsest possible armor  $d_{50a}$  and the limiting armor velocity  $U_a$  are determined using the method that has been outlined. The parameter  $[U - (U_a - U_c)]/U_c$  is then found, and its magnitude indicates whether clear-water or live-bed scour is being considered, and thus the appropriate value of  $K_I$  can be found.

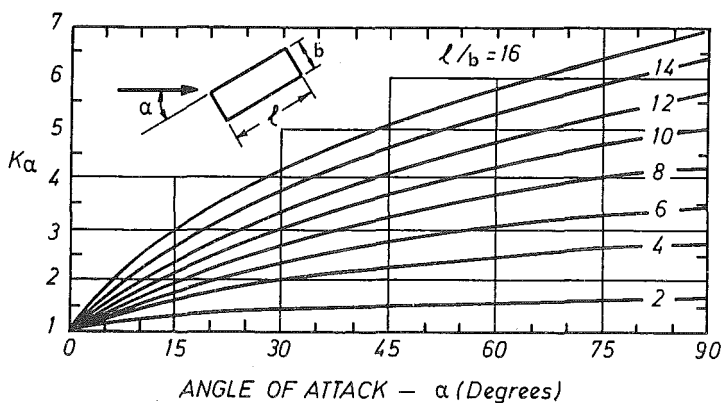
For clear-water scour, if  $\sigma_g > 1.3$ , the bed armors. In this case, the effective grain size is  $d_{50a}$ , and  $K_d$  must be found from Eq. 9, using  $d_{50a}$ . If  $\sigma_g < 1.3$ , armoring does not occur, and  $d_{50}$  is used in Eq. 9 to find  $K_d$ . For live-bed scour, it is not apparent which size fraction should be used to calculate  $K_d$ . Andrews and Parker (1985), drawing on both laboratory and field data, have suggested that with nonuniform sediments, a coarser surface layer is formed even during transport. To be conservative, it is recommended here that the  $d_{50}$  size, rather than something larger, be used to find  $K_d$  for live-bed scour.

TABLE 2. Pier Shape Factors,  $K_s$ 

Shape in plan (1)	Length/ width (2)	Reference			
		Tison (1940) (3)	Laursen and Toch (1956) (4)	Chabert and Engeldinger (1956) (5)	Venkatadri (1965) (6)
Circular	1.0	1.0	1.0	1.0	1.0
Lenticular	2.0	—	0.97	—	—
	3.0	—	0.76	—	—
	4.0	0.67	—	0.73	—
	7.0	0.41	—	—	—
Parabolic nose	—	—	—	—	0.56
Triangular nose, 60°	—	—	—	—	0.75
Triangular nose, 90°	—	—	—	—	1.25
Elliptic	2.0	—	0.91	—	—
	3.0	—	0.83	—	—
Ogival	4.0	0.86	—	0.92	—
Joukowski	4.0	—	—	0.86	—
	4.1	0.76	—	—	—
Rectangular	2.0	—	1.11	—	—
	4.0	1.40	—	1.11	—
	6.0	—	1.11	—	—

The remaining factors  $K_y$ ,  $K_\alpha$ , and  $K_s$  are then found, and local scour depth calculated from

$$d_s = K_T K_d K_y K_\alpha K_s D \dots \dots \dots (11)$$

FIG. 7. Alignment Factor  $K_\alpha$  for Piers Not Aligned with Flow

INPUT DATA:

FLOW -  $y, U$

SEDIMENT -  $d_{50}, d_{max}, \sigma_g$

PIER GEOMETRY  $D$ , Shape, Alignment

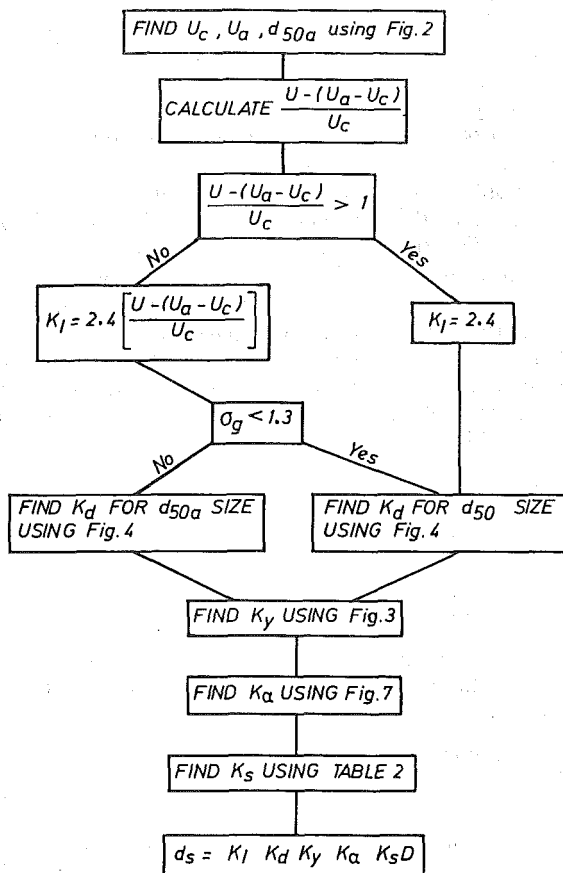


FIG. 8. Flow Chart for Determination of Design Local Scour Depth

For cylindrical piers,  $K_\alpha$  and  $K_s$  are always unity.

To demonstrate the method, two examples are considered. Find the local scour depth at a 1.2-m diameter pier under the following conditions: first,  $d_{50} = 0.5$  mm,  $\sigma_g = 2.5$ ,  $y = 1.5$  m, and  $U = 1.5$  m/s, and second,  $d_{50} = 100$  mm,  $\sigma_g = 2.0$ ,  $y = 1.8$  m, and  $U = 2.0$  m/s.

For  $d_{50} = 0.5$  mm:  $u_{*c} = 0.017$  m/s (Fig. 1), and  $U_c = 0.412$  m/s (Eq. 2). Equating  $d_{max}$  with  $d_{95}$ , we have  $d_{max} = \sigma_g^{1.65} d_{50} = 2.27$  mm, and  $d_{50a} = 1.26$  mm. Thus,  $u_{*c} = 0.0265$  m/s,  $U_{ca} = 0.582$  m/s, and  $U_a = 0.8U_{ca} = 0.466$  m/s. Now  $[U - (U_a - U_c)]/U_c = 3.51$ , and live-bed scour pertains. Thus,  $K_I = 2.4$ . To find  $K_y$ ,  $y/D = 1.25$ , and thus,  $K_y = 0.83$ . To find  $K_d$ ,  $D/d = 2,400$ , and thus,  $K_d = 1.0$ . Therefore,  $d_s = K_I K_d K_y D = 2.4 \times 1.0 \times 0.83 \times 1.2 = 2.38$  m.

For  $d_{50} = 100$  mm:  $u_{*c} = 0.3$  m/s, and  $U_c = 3.45$  m/s. We find  $d_{\max} = d_{95} = \sigma_g^{1.65} d_{50} = 314$  mm, and  $d_{50a} = 174$  mm. Thus,  $u_{*ca} = 0.03(174)^{1/2} = 0.396$  m/s, giving  $U_{ca} = 4.00$  m/s, and  $U_a = 3.20$  m/s. Because  $U_a < U_c$ , take  $U_a = U_c = 3.45$  m/s. Therefore,  $[U - (U_a - U_c)]/U_c = 0.580$ , and clear-water scour occurs. For clear-water scour,  $K_d$  should be based on  $d_{50a}$ . Thus  $K_I = 2.4 \times 0.580 = 1.39$ . To find  $K_y$ ,  $y/D = 1.5$ , and thus,  $K_y = 0.865$ . To find  $K_d$ ,  $D/d = 6.9$ , and thus  $K_d = 0.678$ . Therefore,  $d_s = K_I K_y K_d D = 0.98$  m.

In Figs. 9 and 10, several of the more widely recognized existing design methods are compared with the proposed method. Fig. 9 applies to uniform sediments and Fig. 10 to nonuniform sediments. The comparison is achieved by applying the various design methods to laboratory data for cylindrical piers selected from Chabert and Engeldinger (1956), Shen et al. (1966), Hancu (1971), Ettema (1976, 1980), Chiew (1984), and Baker (1986). The data were chosen to include a wide range of values of pier size, flow velocity, flow depth, sediment size, and sediment grading.

The design methods used for this comparison are those by Laursen and Toch (1956), Hancu (1971), Shen (1971), and Breusers et al. (1977). Each is quoted here in the correct form for application to cylindrical piers. Laursen and Toch (1956) proposed a design curve from their model studies, which Neill (1964) expressed as

$$d_s = 1.35 D^{0.7} y^{0.3} \dots\dots\dots (12)$$

Hancu (1971) proposed the equation

$$\frac{d_s}{D} = 2.42 \left( 2 \frac{U}{U_c} - 1 \right) \left( \frac{U_c^2}{gD} \right)^{1/3} \dots\dots\dots (13)$$

in which  $(2U/U_c - 1) = 1.0$  for live-bed scour. For clear-water scour, Shen (1971) suggested the use of the following equation which formed an envelope to all the known data:

$$d_s = 0.00022 \left( \frac{UD}{\nu} \right)^{0.619} \dots\dots\dots (14)$$

In the case of live-bed scour, Shen (1971) proposed that either the Larras (1963) equation

$$d_s = 1.05 D^{0.75} \dots\dots\dots (15)$$

or the Breusers (1965) equation

$$d_s = 1.4D \dots\dots\dots (16)$$

should be used. Breusers et al. (1977) concluded that scour depth is described by the following function

$$\frac{d_s}{D} = f \left( \frac{U}{U_c} \right) \left[ 2 \tanh \left( \frac{y}{D} \right) \right] \dots\dots\dots (17)$$

in which

$$f \left( \frac{U}{U_c} \right) = 0, \quad \text{for } \frac{U}{U_c} < 0.5 \dots\dots\dots (18a)$$

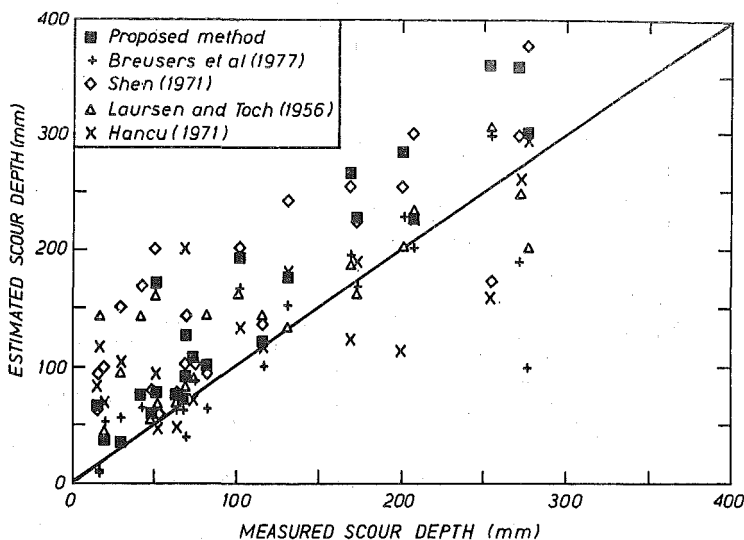


FIG. 9. Comparison for Uniform Sediments of Existing Design Methods with Proposed Method

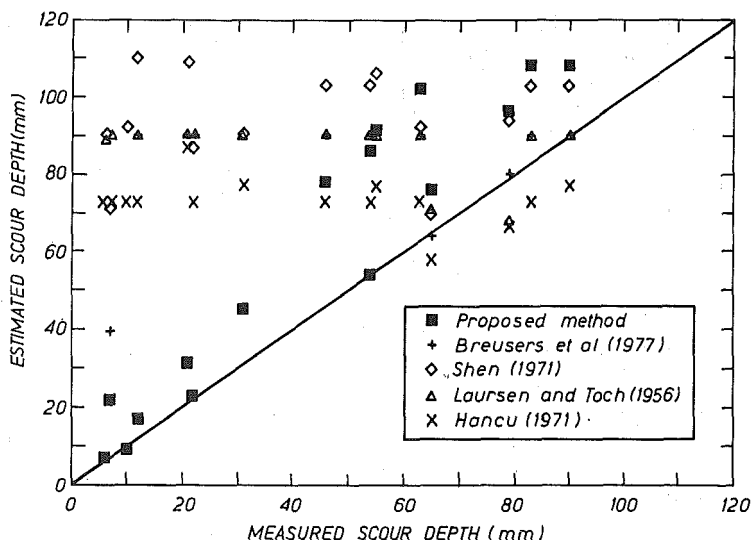
$$f\left(\frac{U}{U_c}\right) = \left(2 \frac{U}{U_c} - 1\right), \quad \text{for } 0.5 \leq \frac{U}{U_c} < 1.0 \dots\dots\dots (18b)$$

$$f\left(\frac{U}{U_c}\right) = 1, \quad \text{for } \frac{U}{U_c} \geq 1.0 \dots\dots\dots (18c)$$

In Figs. 9 and 10, the diagonal lines indicate perfect agreement. Points that plot above these lines represent conservative estimates of scour depth. The proposed method is everywhere conservative, as expected, because it is based on envelope curves to data. Being a design method, conservatism is a necessary feature. The existing methods all underestimate the scour depth in some instances, particularly for uniform sediments. For nonuniform sediments, the existing methods generally predict larger scour depths than the proposed method. This is also expected because the existing methods do not take into account the sediment grading.

## CONCLUSION

A design method is presented that enables prediction of local scour depths at bridge piers. The method is based on laboratory data, derived mainly from experiments with cylindrical piers, for which the largest possible local scour depth is  $2.4D$ . Multiplying factors, which have the effect of reducing this value, are applied where clear-water scour conditions exist ( $K_f$ ), the flow depth is relatively shallow ( $K_y$ ), and the sediment is relatively large ( $K_d$ ). In the case of noncylindrical piers, two additional multiplying factors are applied. These are  $K_s$ , the shape factor, which can



**FIG. 10. Comparison for Nonuniform Sediments of Existing Design Methods with Proposed Method**

have values up to 1.4, and  $K_\alpha$ , the alignment factor, which can be as large as 7.0. The design method is summarized in the flow chart (Fig. 8).

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## APPENDIX II. NOTATION

*The following symbols are used in this paper:*

- $Al$  = effect of pier alignment;  
 $D$  = pier width as shown in Fig. 7 (pier diameter for cylindrical piers);



- $d_{\max}$  = maximum particle size for a nonuniform sediment;  
 $d_s$  = equilibrium scour depth below mean bed level;  
 $d_{50}$  = median particle size;  
 $d_{84}$  = particle size for which 84% are finer;  
 $d_{50a}$  =  $d_{50}$  size of the coarsest armor layer;  
 $g$  = gravitational acceleration;  
 $K_d$  = sediment size factor;  
 $K_I$  = flow intensity factor;  
 $K_s$  = pier shape factor;  
 $K_y$  = flow depth factor;  
 $K_\alpha$  = pier alignment factor;  
 $K_\sigma$  = sediment gradation factor;  
 $m$  = exponent in Eq. 3;  
 $Sh$  = effect of pier shape;  
 $U$  = mean approach flow velocity;  
 $U_a$  = mean approach flow velocity at the armor peak =  $0.8 U_{ca}$ ;  
 $U_c$  = mean approach flow velocity at threshold condition;  
 $U_{ca}$  = mean approach flow velocity beyond which armoring of channel bed is impossible;  
 $u_{*c}$  = critical shear velocity defined by Shields function;  
 $u_{*ca}$  = critical shear velocity of armored bed;  
 $y$  = flow depth;  
 $\nu$  = kinematic viscosity;  
 $\rho$  = fluid density;  
 $\rho_s$  = sediment density; and  
 $\sigma_g$  = geometric standard deviation of particle size distribution =  $d_{84}/d_{50}$ .