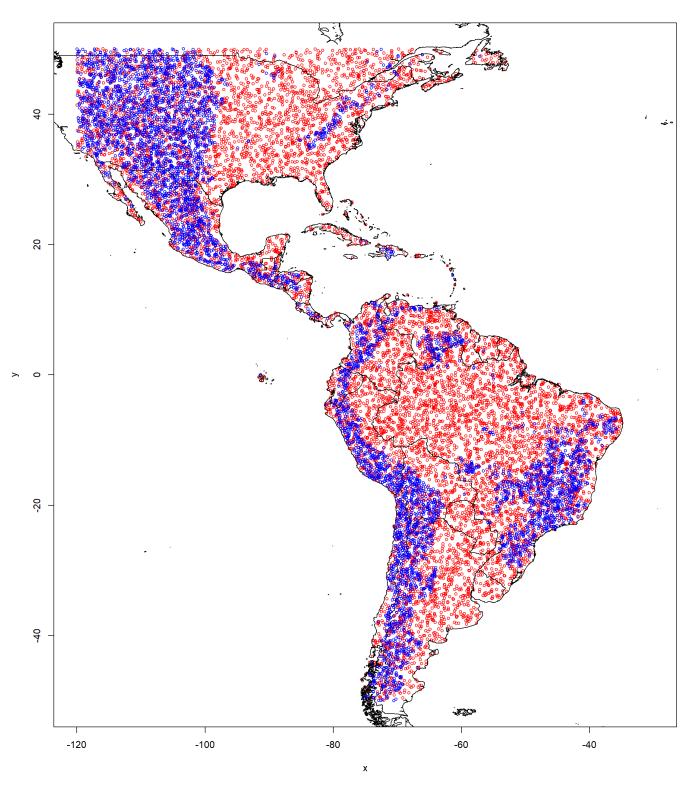
T downscaling TMax month 01 model

Viacheslav Shalisko 16 de abril de 2018

```
# random numbers seed
set.seed(1)
rpoints_mask1_number <- 10000
rpoints_mask2_number <- 10000
# month to be analysed (in current version the analysis is per month)
# dependent variable to be analysed
var_dependent <- "tmax"</pre>
var_dependent_name <- "Maximum temperature"</pre>
# geographic coordinate system string
mi_crs <- "+proj=longlat +ellps=WGS84 +datum=WGS84 +no_defs"</pre>
# map extent
# all data should be in geographic coodinates
ext_vector <- c(-120,-30,-50,50)
# output directory (relative to curretnt dir)
output_path <- 'C:/Users/vshal/Downloads/SDM_interpolations/models'</pre>
# name of low resolution source dependent variable
# name of high resolution predictor variable
r_predictor_name <- "C:/Users/vshal/Downloads/SDM_recortes/gmted_med075_Amer.tif"
# names of first and second high resolution masks
r_mask2_name <- "C:/Users/vshal/Downloads/SDM_recortes/Continents_Amer_S2a.tif"</pre>
knitr::opts_chunk$set(echo = TRUE)
knitr::opts_chunk$set(error = TRUE)
library(raster)
                    # raster processing
## Loading required package: sp
library(maptools)
                    # map processing
## Checking rgeos availability: FALSE
##
       Note: when rgeos is not available, polygon geometry
                                                           computations in maptools depend on gpclib,
##
       which has a restricted licence. It is disabled by default;
##
       to enable gpclib, type gpclibPermit()
library(rworldmap)
                    # worldmap datasets
## Warning: package 'rworldmap' was built under R version 3.4.2
## ### Welcome to rworldmap ###
## For a short introduction type : vignette('rworldmap')
library(rworldxtra)
                    # hires worldmap spatial dataframe
```

```
## Warning: package 'rworldxtra' was built under R version 3.4.2
library(dismo)
                       # SDM, here used to generate random points
library(mgcv)
                       # GAM models
## Loading required package: nlme
##
## Attaching package: 'nlme'
## The following object is masked from 'package:raster':
##
       getData
## This is mgcv 1.8-17. For overview type 'help("mgcv-package")'.
r_lores <- raster(r_lores_name)</pre>
r_predictor <- raster(r_predictor_name)</pre>
r_mask1 <- raster(r_mask1_name)</pre>
r_mask2 <- raster(r_mask2_name)</pre>
random\_points\_mask1 <- \ randomPoints(r\_mask1, \ n = rpoints\_mask1\_number, \ tryf = 3)
## Warning in randomPoints(r_mask1, n = rpoints_mask1_number, tryf = 3):
## generated random points = 0.8891 times requested number
random_points_mask2 <- randomPoints(r_mask2, n = rpoints_mask2_number, tryf = 5)</pre>
## Warning in randomPoints(r_mask2, n = rpoints_mask2_number, tryf = 5):
## generated random points = 0.5247 times requested number
dim(random_points_mask1)
## [1] 8891
               2
dim(random_points_mask2)
## [1] 5247
random_points_all <- rbind(random_points_mask1,random_points_mask2)</pre>
# background continents
plot(random_points_mask1, col='red',cex=0.7, xlim=ext_vector[1:2], ylim=ext_vector[3:4], axes=TRUE)
world_high <- getMap(resolution = "high")</pre>
plot(world_high, add=TRUE)
# render random points
points(random_points_mask2,col='blue',cex=0.7)
```

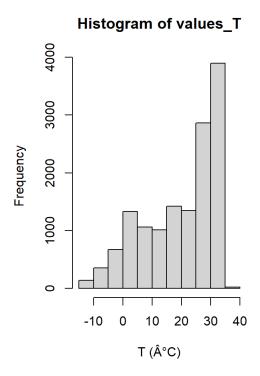


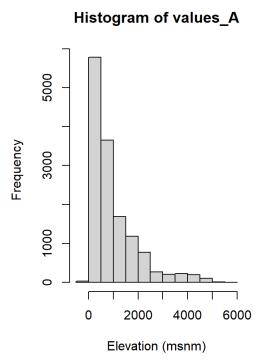
```
values_T <- extract(r_lores, random_points_all)
values_A <- extract(r_predictor, random_points_all)
values_Y <- random_points_all[,"y"]
values_X <- random_points_all[,"x"]

# remove NAs
intermediate_frame <- data.frame(values_X, values_Y, values_T, values_A)
intermediate_frame <- na.omit(intermediate_frame)

values_T <- as.vector(intermediate_frame[,3])
values_A <- as.vector(intermediate_frame[,4])
values_Y <- as.vector(intermediate_frame[,2])
values_X <- as.vector(intermediate_frame[,1])</pre>
```

```
par(mfrow=c(1, 2))
hist(values_T, col = "lightgray", xlab = "T (°C)")
hist(values_A, col = "lightgray", xlab = "Elevation (msnm)")
```





Simple models

```
mod_L1 <- lm(values_T ~ values_A)
summary(mod_L1)</pre>
```

```
##
## Call:
## lm(formula = values_T ~ values_A)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
  -35.109 -9.081
##
                    6.016
                            8.994 15.947
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                                             <2e-16 ***
## (Intercept) 22.8615215 0.1382272 165.39
                                             <2e-16 ***
## values_A
              -0.0033763 0.0001017 -33.21
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 11.83 on 14136 degrees of freedom
                                   Adjusted R-squared: 0.0723
## Multiple R-squared: 0.07236,
## F-statistic: 1103 on 1 and 14136 DF, p-value: < 2.2e-16
```

```
AIC(mod_L1)
```

```
## [1] 109976.9
```

```
mod_L2 <- lm(values_T ~ values_A + values_Y)
summary(mod_L2)</pre>
```

```
##
## Call:
## lm(formula = values_T ~ values_A + values_Y)
## Residuals:
##
     Min
               1Q Median
                              3Q
## -32.471 -3.423 1.494 5.058 14.867
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.519e+01 8.605e-02 292.68 <2e-16 ***
            -3.306e-03 6.231e-05 -53.05 <2e-16 ***
## values_A
              -3.348e-01 2.184e-03 -153.32 <2e-16 ***
## values_Y
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.247 on 14135 degrees of freedom
## Multiple R-squared: 0.6517, Adjusted R-squared: 0.6516
## F-statistic: 1.322e+04 on 2 and 14135 DF, p-value: < 2.2e-16
```

```
AIC(mod_L2)
```

```
## [1] 96131.49
```

```
mod_L3 <- lm(values_T ~ values_A + values_Y + I(values_Y^2))
summary(mod_L3)</pre>
```

```
##
## Call:
## lm(formula = values T ~ values A + values Y + I(values Y^2))
## Residuals:
##
      Min
                1Q Median
                                  3Q
                                          Max
## -11.5600 -1.8789 -0.0641 2.1755
                                       8.8632
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 3.221e+01 5.005e-02 643.5 <2e-16 ***
                -2.947e-03 2.871e-05 -102.6
## values_A
                                               <2e-16 ***
                                               <2e-16 ***
                -1.953e-01 1.175e-03 -166.3
## values_Y
## I(values_Y^2) -1.007e-02 4.389e-05 -229.4 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.335 on 14134 degrees of freedom
## Multiple R-squared: 0.9262, Adjusted R-squared: 0.9262
## F-statistic: 5.917e+04 on 3 and 14134 DF, p-value: < 2.2e-16
```

```
AIC(mod_L3)
```

```
## [1] 74184.97
```

```
mod_A1 <- gam(values_T ~ s(values_A))
summary(mod_A1)</pre>
```

```
##
## Family: gaussian
## Link function: identity
## Formula:
## values_T ~ s(values_A)
##
## Parametric coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 19.67396 0.09681 203.2 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
\hbox{\it \#\# Approximate significance of smooth terms:}
               edf Ref.df F p-value
##
## s(values_A) 8.703 8.973 217.7 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.121 Deviance explained = 12.2\%
## GCV = 132.59 Scale est. = 132.5
```

AIC(mod_A1)

```
## [1] 109220.2
```

```
gam.check(mod_A1)
```

-40

-30

-20

-10

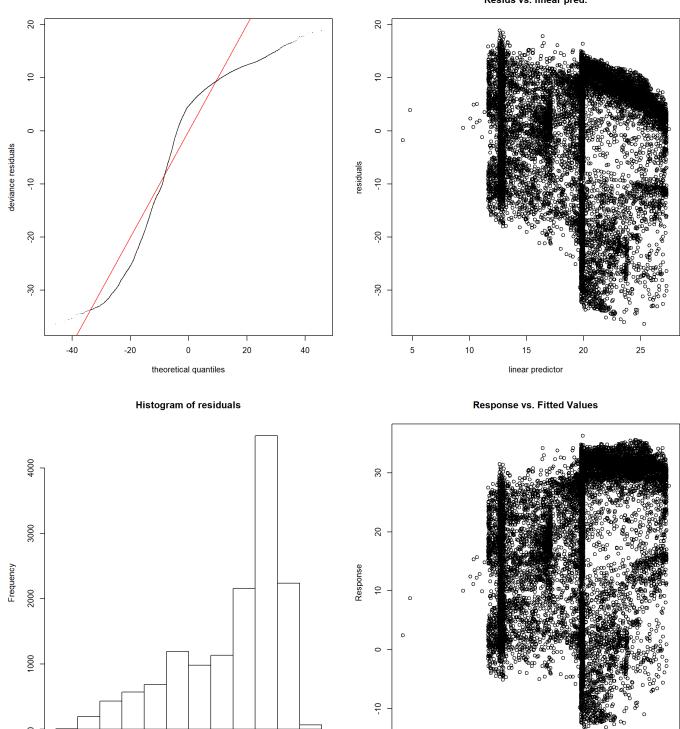
Residuals

0

10

20

Resids vs. linear pred.



```
##
## Method: GCV Optimizer: magic
## Smoothing parameter selection converged after 7 iterations.
## The RMS GCV score gradient at convergence was 9.729613e-05 .
## The Hessian was positive definite.
## Model rank = 10 / 10
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
## k' edf k-index p-value
## s(values_A) 9.0 8.7 0.97 0.015 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

10

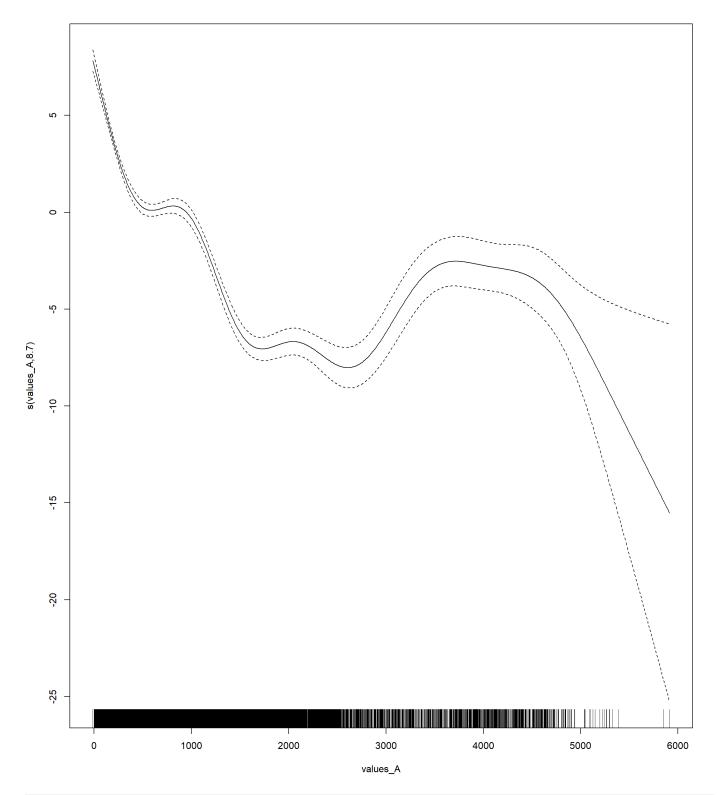
15

Fitted Values

20

25

plot(mod_A1, n=1000)



mod_A2 <- gam(values_T ~ s(values_A) + s(values_Y))
summary(mod_A2)</pre>

```
##
## Family: gaussian
## Link function: identity
## Formula:
## values_T ~ s(values_A) + s(values_Y)
##
## Parametric coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 19.6740 0.0234 840.6 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
\hbox{\it \#\# Approximate significance of smooth terms:}
              edf Ref.df F p-value
##
## s(values_A) 8.163 8.802 2037 <2e-16 ***
## s(values_Y) 8.897 8.997 25281 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.949 Deviance explained = 94.9%
## GCV = 7.7536 Scale est. = 7.7437
                                     n = 14138
```

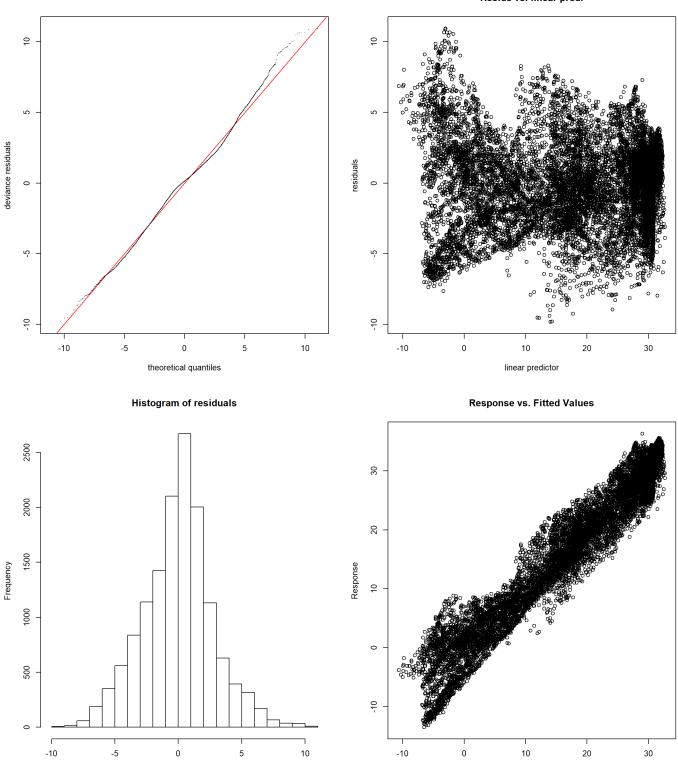
```
AIC(mod_A2)
```

```
## [1] 69080.8
```

```
gam.check(mod_A2)
```

Resids vs. linear pred.

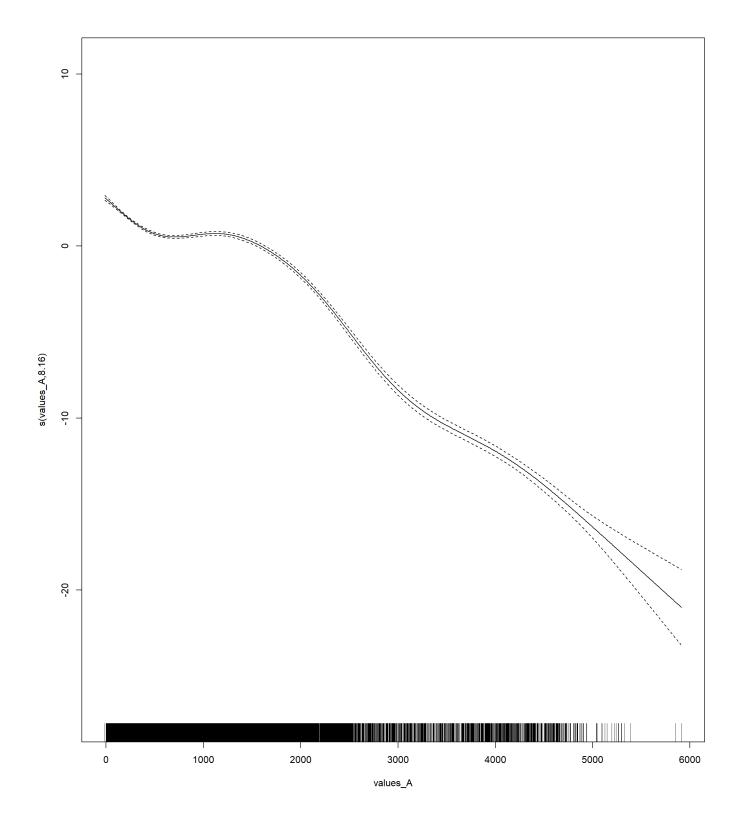
Fitted Values

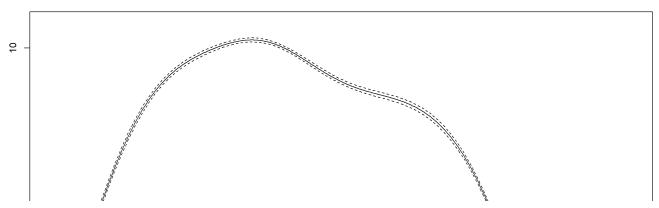


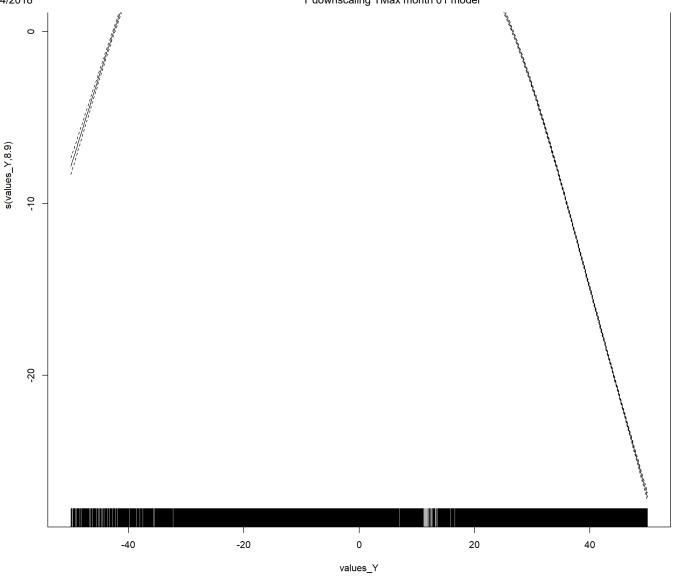
Residuals

```
##
## Method: GCV Optimizer: magic
## Smoothing parameter selection converged after 12 iterations.
## The RMS GCV score gradient at convergence was 7.260532e-06 .
## The Hessian was positive definite.
## Model rank = 19 / 19
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
##
## k' edf k-index p-value
## s(values_A) 9.00 8.16   1.01   0.71
## s(values_Y) 9.00 8.90   0.94   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1</pre>
```

```
plot(mod_A2,n=1000)
```







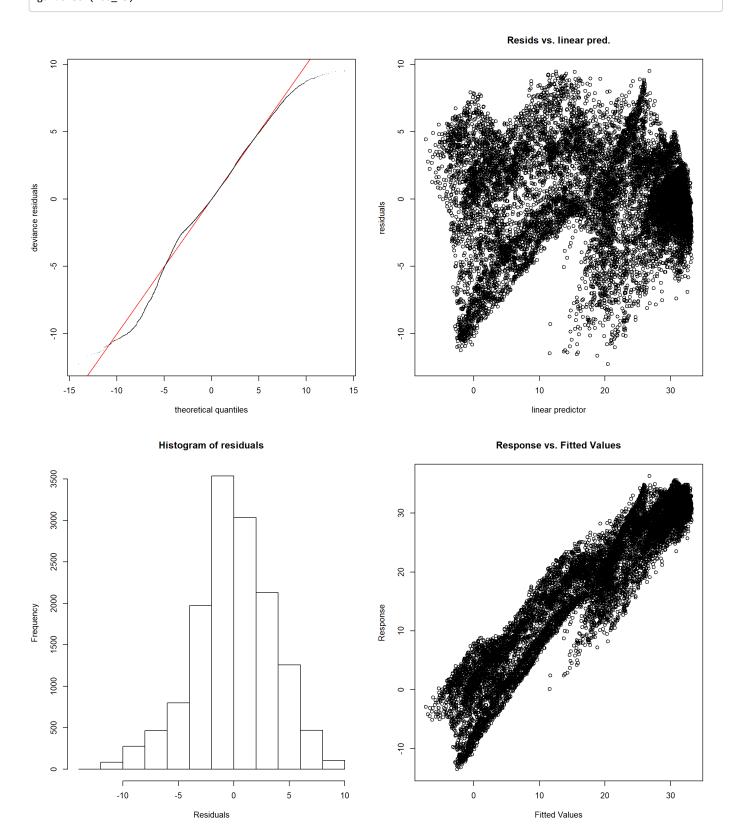
```
mod_A3 <- gam(values_T ~ values_A + s(values_Y,k=3))
summary(mod_A3)</pre>
```

```
## Family: gaussian
## Link function: identity
##
## Formula:
## values_T ~ values_A + s(values_Y, k = 3)
##
## Parametric coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.235e+01 4.144e-02 539.40 <2e-16 ***
## values_A -2.838e-03 3.052e-05 -92.98 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
              edf Ref.df F p-value
##
                     2 71767 <2e-16 ***
## s(values_Y) 2
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.917 Deviance explained = 91.7%
## GCV = 12.543 Scale est. = 12.54
```

```
AIC(mod_A3)
```

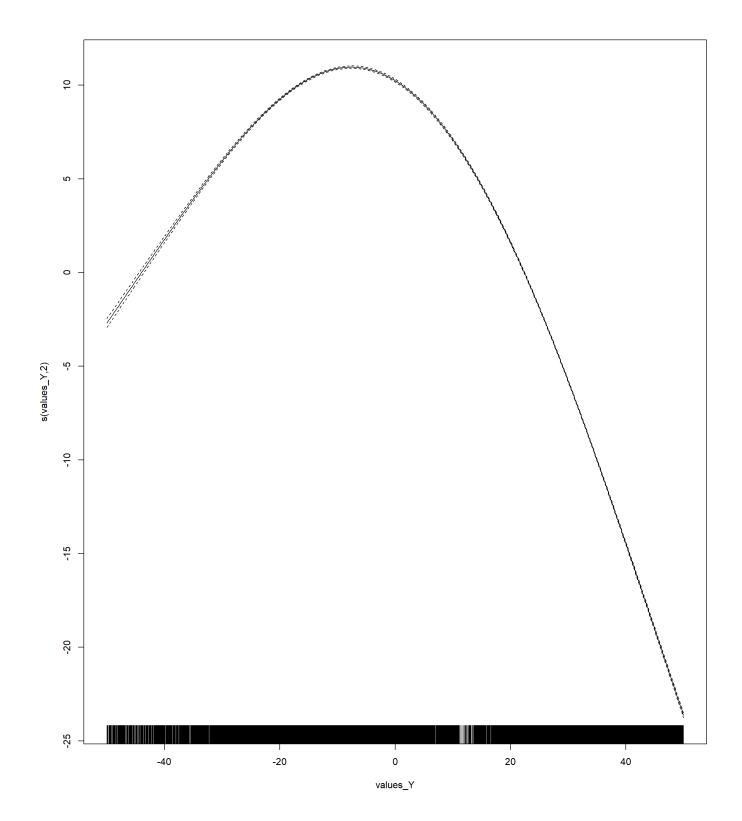
```
## [1] 75881.35
```

gam.check(mod_A3)



```
##
## Method: GCV Optimizer: magic
## Smoothing parameter selection converged after 15 iterations.
## The RMS GCV score gradient at convergence was 2.17802e-06 .
## The Hessian was positive definite.
## Model rank = 4 / 4
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
## k' edf k-index p-value
## s(values_Y) 2 2 0.68 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

```
plot(mod_A3,n=1000)
```



Spatial model

```
## Warning in te(values_A, values_X, values_Y, k = c(2, 10), d = c(1, 2)): one
## or more supplied k too small - reset to default
```

```
print(summary(mod_B1))
```

```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## values_T ~ values_A + te(values_A, values_X, values_Y, k = c(2,
      10), d = c(1, 2)) + s(values_Y, k = 3) + s(values_X, values_Y, k = 3)
##
##
      k = 600)
##
## Parametric coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.10674 11.98389 0.343 0.732
                        0.01269 1.299
                                            0.194
## values_A
               0.01649
##
## Approximate significance of smooth terms:
                                   edf Ref.df
                                                   F p-value
## te(values_A,values_Y,values_Y) 84.85 87.88 79.652 <2e-16 ***
                                  1.00 1.00 0.228 0.633
## s(values_Y)
                                 557.21 590.03 112.167 <2e-16 ***
## s(values_X,values_Y)
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.997 Deviance explained = 99.7%
## -REML = 15067 Scale est. = 0.40424 n = 14138
```

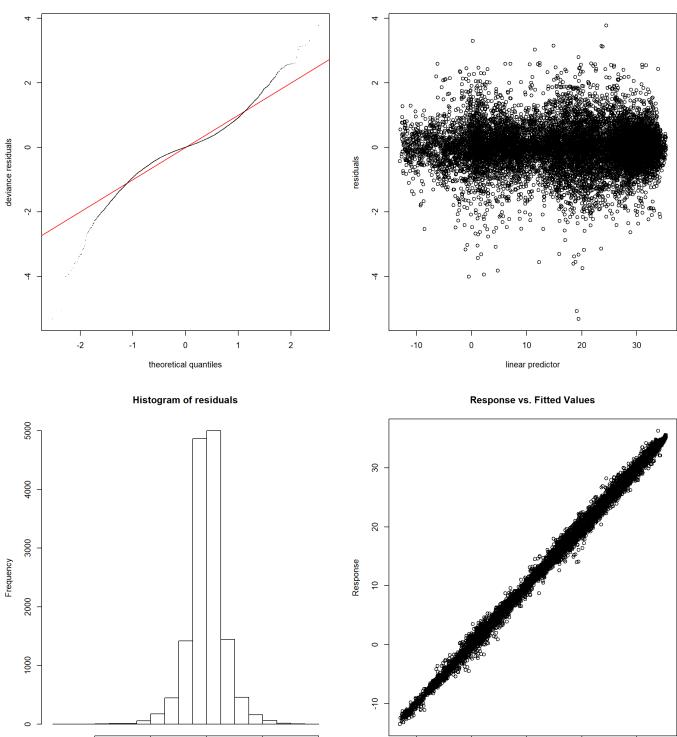
```
print(AIC(mod B1))
```

```
## [1] 27950.8
```

```
saveRDS(mod_B1, paste(output_path,"/","model_GAM_B1_",var_dependent,"_m",month,".rds",sep=""))
```

```
gam.check(mod_B1)
```





-10

0

10

Fitted Values

20

30

-2

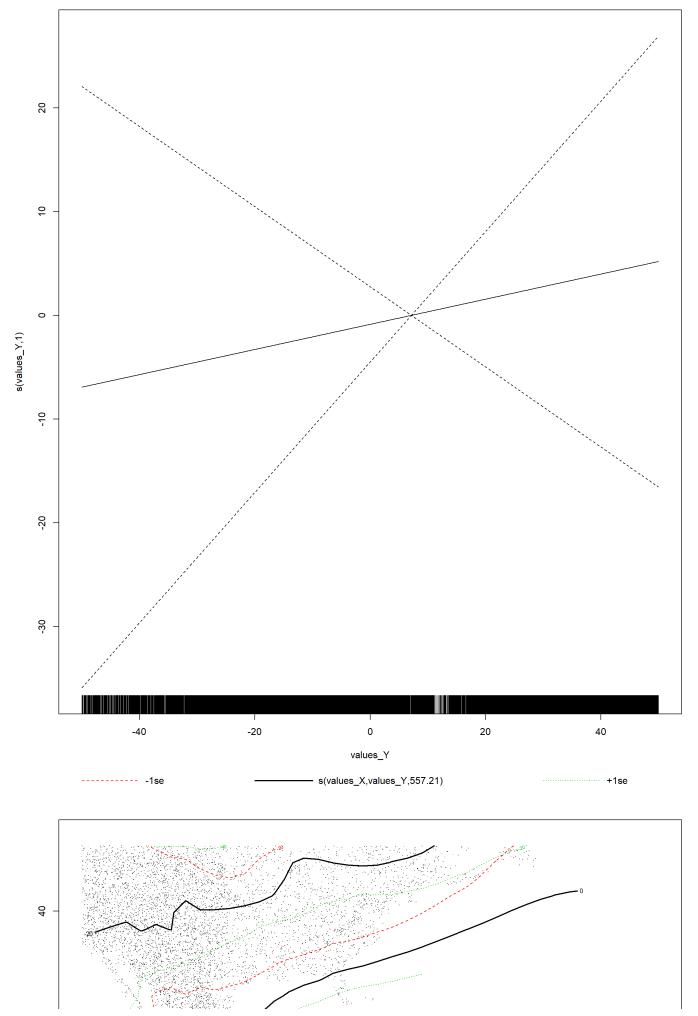
0

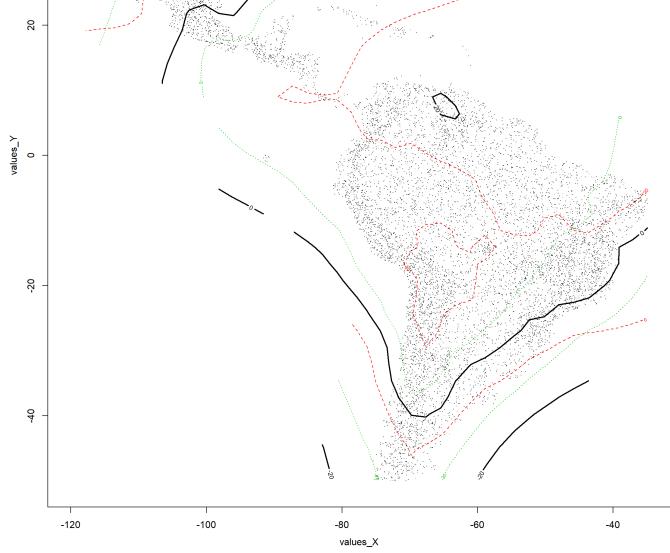
Residuals

2

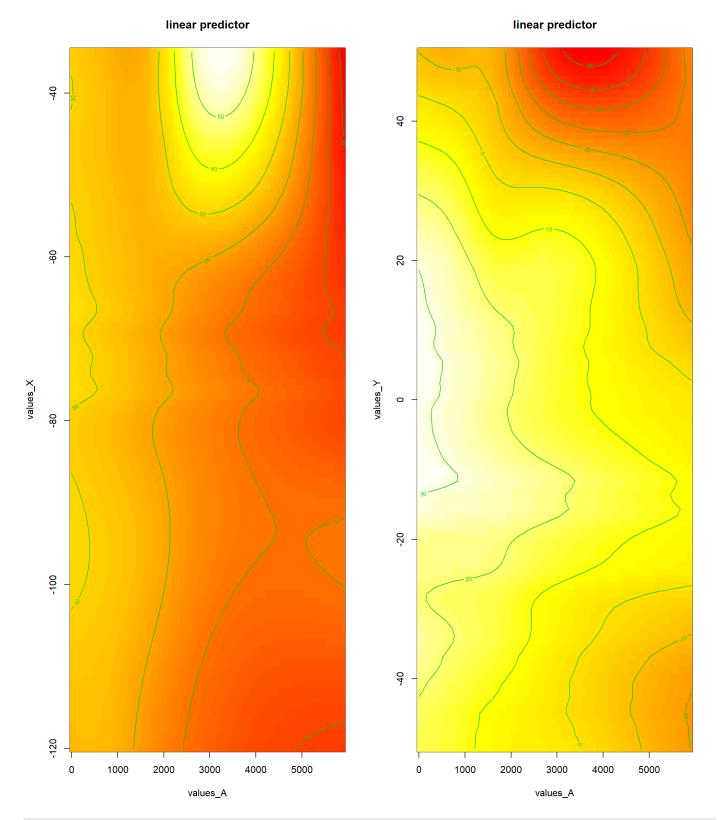
```
##
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-7.665426e-05,2.523688e-05]
## (score 15066.96 & scale 0.4042368).
## eigenvalue range [-6.629211e-07,7077.446].
## Model rank = 702 / 702
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k^{\prime}\text{.}
                                    k'
                                         edf k-index p-value
## te(values_A,values_X,values_Y) 100.0 84.8 0.72 <2e-16 ***</pre>
## s(values_Y)
                                   2.0 1.0
                                                0.99
                                                      0.14
                                 598.0 557.2
## s(values_X,values_Y)
                                               0.76 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
plot(mod_B1,n=1000)
```





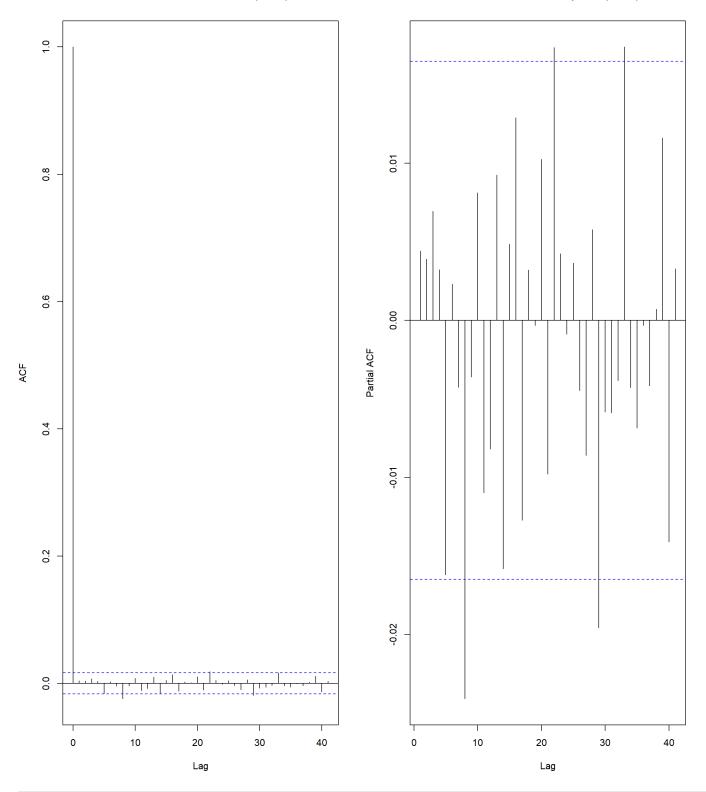
```
par(mfcol = c(1, 2))
vis.gam(mod_B1,view=c("values_A","values_X"),n.grid=100,plot.type = "contour")
vis.gam(mod_B1,view=c("values_A","values_Y"),n.grid=100,plot.type = "contour")
```



```
residuals_mod_B1 <- resid(mod_B1, type = "pearson")
par(mfcol = c(1, 2))
acf(residuals_mod_B1, main="Standarized residual ACF (GAM)")
pacf(residuals_mod_B1, main="Standarized residual pACF (GAM)")</pre>
```

Standarized residual ACF (GAM)

Standarized residual pACF (GAM)



Distribution of residuals (GAM)

