## Computational Physics - PH3264

## Assignment 1

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Roll:20201017

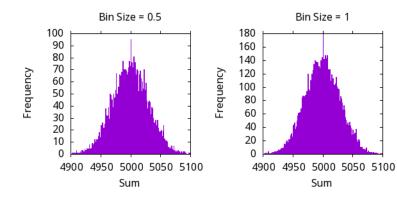
- a. For a-f, refer to respective .cpp and .out files for demonstration all involve printing random numbers with different seeds, and other simple tasks.
- g. The output from g.out is as follows:

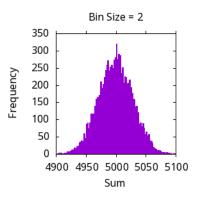
Absolute difference between 0.5 and average of random numbers

10 : 0.1838132364 100 : 0.02390399648 10000 : 0.0004469846813 1000000 : 5.272165292e-05

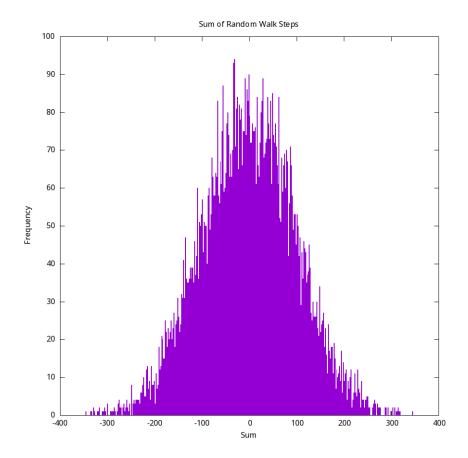
The expected value is 0 (as the number of random numbers sampled tends to infinity, the average approaces 0.5). As the number of sample here increases, the difference gets closer to 0 - verifying the law of large numbers.

h. The following plot shows the distribution of the sum of 10000 random numbers, computed 10000 times.

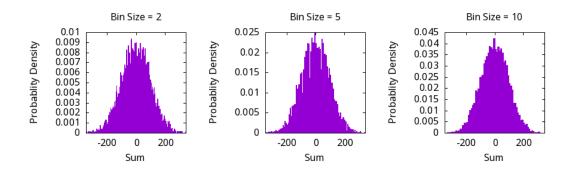




i. While it is not clear from the plot shown, zooming in shows that the bars alternate - this is because the sum of 10000 odd numbers (-1 and 1) is always even, causign the values for the bins (2n,2n+1) to be 0.



j. The plot below shows the same distribution with various bin sizes - Histograms with larger bin sizes are smoother.



Note: All plots hereafter are normalized such that the cumulative sum is 1.

- k. The plots for  $10^5$  samples of sum of  $10^4$  steps and  $10^5$  steps are shown below, using a bin width of 2.
- l. As can be seen in the plots below, with more samples at every step, the standard deviation increases. More samples indicates more steps with more steps in a walk, regions farther from the origin are more accessible, explaining this spread.

