

**Computational Physics - PH3264**  
Module 2 - Integration

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1. **Euler's Method:**  
Step Size 0.001: 7.24764  
Step Size 00.01: 28.0671
2. **Modified Euler's Method:**  
Step Size 0.001: 0.07706  
Step Size 00.01: 4.76803
3. **Improved Euler's Method:**  
Step Size 0.001: 0.05128  
Step Size 00.01: 3.59668
4. **Runge-Kutta RK-4 Method:**  
Step Size 0.001:  $3.54 \cdot 10^{-6}$   
Step Size 00.01: 0.02834
5. The value of  $x$  (starting with  $x_0 = 0.1$  and  $v_0 = 1.9$ ) at the end of 5000 iterations is -2.39932.
6. The value of  $x$  (starting with  $x_0 = 0$  and  $v_0 = 1.999$ ) at the end of 5000 iterations is -2.34132.
7. When  $v_0 > 2$ , the function  $x(t)$  becomes monotonously increasing. The corresponding graphs for Qn.5, Qn.6 and Qn.7 are shown in Figure 1.

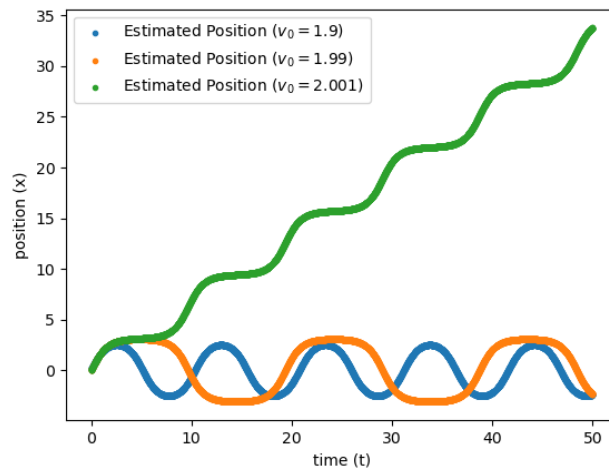


Figure 1: Solution for  $x$  with different initial values.

8. The final  $y$  value of particle 1 at  $t = 40$  is -0.11891. As the system is symmetric about the first and 26<sup>th</sup>. Therefore, we expect the graph for time evolution of particle 1 to be identical to that of particle 26. This has been shown in Figure 2.

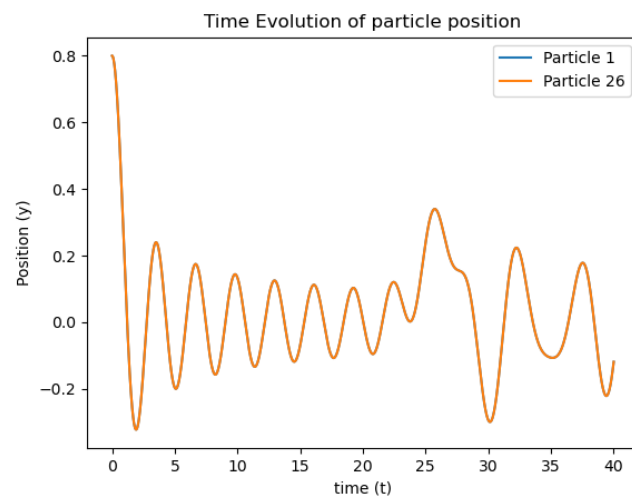


Figure 2: Solution for  $x$  with different initial values.

9. The value of the function at  $x = 0.8$  is 0.28147.