

# **QUANTITATIVE APTITUDE**



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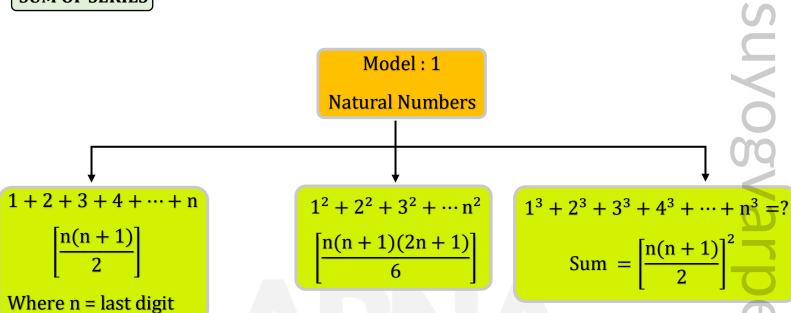


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### **NUMBER SYSTEM**

### **SUM OF SERIES**





 $1 + 3 + 5 + 7 \dots + 33$ 

 $(x^2)$ 

where  $\left[x = \frac{n+1}{2}\right]$ 

n = last digit

 $2 + 4 + 6 + 8 \dots + 50$ 

x(x+1)

where  $\left[x = \frac{n}{2}\right]$ 

n = last digit

51 + 53 + 55 ... + 65

Case: When series doesn't

Start from 1 or 2 and start

From in between

suyogvarpe939@gmail.com

Q.1 
$$1+2+3+\cdots+30=?$$

**Sol.** 
$$\frac{n(n+1)}{2} = \frac{30 \times 31}{2}$$
$$= 15 \times 31$$
$$= 45$$

$$\mathbf{Q.2} \quad \mathbf{1}^2 + \mathbf{2}^2 + \mathbf{3}^2 + \dots + \mathbf{12}^2 = ?$$

Sol. 
$$\frac{n(n+1)(2n+1)}{6} = \frac{12 \times 13 \times 25}{6}$$
$$= 50 \times 13$$
$$= 650$$

Q.3 
$$1^3 + 2^3 + 3^3 + \cdots + 9^3 = ?$$

Sol. 
$$\left[\frac{n(n+1)}{2}\right]^2 = \left(\frac{9 \times 10}{2}\right)^2$$
$$= 45^2$$
$$= 2025$$

Q.4 
$$1+3+5+\cdots+49=?$$

**Sol.** 
$$x^2$$

We know, 
$$x = \frac{n+1}{2}$$

$$=\frac{49+1}{2}$$

$$= 25$$

$$\therefore x^2 = (25)^2$$

$$= 625$$

**Q.5** 
$$2+4+6+\cdots+5+58=?$$

**Sol.** 
$$x(x + 1)$$

We Know, 
$$x = \frac{n}{2}$$

$$=\frac{58}{2}$$

$$= 29$$

$$x(x+1) = 29(29+1)$$

$$= 29 \times 30$$

39@gmall.com



$$= 870$$

$$Q.6 51 + 53 + 55.... + 99 = ?$$

**Sol.** 
$$(1+3+5+\cdots 99)-(1+3+5\cdots +49)$$

For 
$$1 + 3 + 5 + \dots 99$$

For 
$$1 + 3 + 5 + \cdots 99$$
  
by using formula:  $x^2$ 

Trick:  $x = \frac{n+1}{2}$ 

$$= \frac{99+1}{2}$$

$$x = 50$$

$$x^2 = (50)^2$$

$$= 2500$$
For  $1 + 3 + 5 \cdots + 49$ 

$$= 2500 - 625$$

$$= 1875$$
This method can be used when series starts from random number in between. That is series doesn't starts from 1, 2 etc.

Solving: 
$$(1+3+5+\cdots 99) - (1+3+5\cdots +49)$$

$$= 2500 - 625$$

$$= 1875$$

starts from 1, 2 etc.

Q.7 
$$10^2 + 11^2 + 12^2 + \cdots + 20^2 = ?$$





### FINDING THE SUM "UPTO N TERMS"

**Formula**: 
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

where  $a = 1^{st}$  Digit, d = difference,  $n = n^{th}$  term

### Q.8 Find the sum

$$1 + 3 + 5 + 7 + 9 \cdots$$
 upto 15 terms

Sol. 
$$S_n = \frac{n}{2}[2a + (n-1)d]$$
  
 $S_{15} = \frac{15}{2}[2(1) + (15-1)2]$   
 $= \frac{15}{2}[2 + 28]$ 

$$=\frac{15}{2}\times30$$

= 225 {d = difference, so difference between any 2 digits as per question is 2}

In this, we don't know what exactly us 15th term, so we used formula of Arithmetic Progression

### **Question to Practice**

Q.9 Find the sum of first 19 terms of the sequence 2, 7, 12, 17, ...?



### FINDING A NUMBER

### Q.10 What is two third of half of 369?

**Sol.** 
$$\frac{2}{3} \times \frac{1}{2} \times 369 = ?$$
 = 123

### Q.11 If one-third of one-fourth of a number is 15, then three-tenth of the number is?

Sol. 
$$\frac{1}{3} \times \frac{1}{4} \times x = 15$$
$$x = 15 \times 4 \times 3$$
$$x = 180$$

Now, three-tenth of this number

$$= \frac{3}{10} \times$$

$$= \frac{3}{10} \times 180$$

$$= 54$$

## Q.12 If the sum of two numbers, one of which is $\frac{2}{5}$ times the other is so, then the numbers are?

**Sol.** Let's take first no. 
$$= x$$

Then according to question, second no. =  $\frac{2}{5}x$ 

$$x + \frac{2}{5}x = 50$$

$$\frac{5x + 2x}{5} = 50$$

$$7x = 250$$

$$x = \frac{250}{7}$$

$$\therefore$$
 first no. = x

$$=\frac{250}{7}$$

Second no. = 
$$\frac{2}{5}$$
 x

$$=\frac{2}{5}\times\frac{250}{7}$$

$$=\frac{100}{7}$$



Q.13 If  $\frac{1}{2}$  is added to a number & the sum is multiple by 3, the result is 21 then the number is?

**Sol.** Let the no. be x

$$\left(\frac{1}{2} + x\right) \times 3 = 21$$

$$\frac{3}{2} + 3x = 21$$

$$3x = 21 - \frac{3}{2}$$

$$3x = \frac{42 - 3}{2}$$

$$3x = \frac{39}{2} \Rightarrow \boxed{x = \frac{13}{2}}$$

### **Question to Practice**

Q.14 If  $4/5^{th}$  of a number exceeds its  $3/4^{th}$  by 8, then the number is

Q.15 If 3/4 of a number is 7 more then 1/6 of the number, then 5/2 of the number is?



### **PROBLEMS ON AGES**

- Q.16 The present ages of A and B are in the ratio 4 : 5 and after 5 years they will be in the ratio 5 : 6. The present age A is?
- **Sol.** Let age be 'x'

Present after Future 5 years 5:6

4x:5x

After 5 years  $\Rightarrow 4x + 5:5x + 5 = 5:6$ 

 $\frac{4x+5}{5x+5} = \frac{5}{6}$   $\left\{ a: b = \frac{a}{b} \right\}$ 

By cross Multiplication 24x + 30 = 25x + 25

x = 5

∴ Present Age of A = 4x=  $4 \times 5$ = 20 years

Present Age of B = 5x

 $= 5 \times 5$ = 25 years

- Q.17 The ratio of present ages of two brothers is 1 : 2 and 5 years back, the ratio was 1 : 3 what will be the ratio of their ages after 5 years?
- Sol. Past -5 Present 1:3 1:2 x:2x

$$x - 5: 2x - 5 = 1:3$$

$$\frac{x-5}{2x-5} = \frac{1}{3}$$

$$3x - 15 = 2x - 5$$

$$x = 10$$

After 5 years, ratio of their ages

$$\Rightarrow$$
 x + 5: 2x + 5

$$\therefore x = 10$$

$$10 + 5:2(10) + 5$$

15:25



- Q.18 I am three times as old as my son. 15 years hence, 9 will be twice as old as my son. The sum of our ages is?
- **Sol.** Father Son

3x x

After 15 years

$$3x + 15$$
  $x + 15$ 

$$3x + 15 = 2(x + 15)$$

$$3x + 15 = 2x + 30$$

$$x = 15$$

Son age (x) = 15 years

Father age 
$$(3x) = 3 \times 15$$

$$= 45 \text{ years}$$

$$\therefore$$
 Sum of their ages = 45 + 15

$$= 60$$
 years

- Q.19 10 years ago daughter's age was two-fifth of her mother's age that time. while 10 years hence her age will be three-fifth of her mother's age then Find the difference in the ages of the two
- **Sol.** Let daughter's age = x

Let Mother's age = y

10 year <mark>ago</mark>

$$(x-10) = \frac{2}{5}(y-10) \rightarrow (1)$$

10 year hence

$$(x + 10) = \frac{3}{5}(y + 10) \rightarrow (2)$$

An solving equ. (1)

$$5x - 50 = 2y - 20$$

$$5x - 2y = 30 \rightarrow (3)$$

On solving equ. (2)

$$5x + 50 = 3y + 30$$

$$5x - 3y = 20 \rightarrow (4)$$

Solving equ. (3) & (4)



$$5x - 2y = 30$$

$$-5x + 3y = 20$$

$$y = 50$$

$$5x - 2y = 30$$

$$5x - 100 = 30$$

$$x = 26$$

Difference of ages = Mother age - daughter age = 50 - 26= 24

- Q.20 4 years ago, the ratio of the ages of A and B was 2: 3 and after 4 years, it will become 5: 7. Find their present ages
- Q.21 The present age of a father is 3 year more than three times the age of his son. 3 years hence, father's age will be lo year more than twice the age of son. The father's present age is?

### **TIME AND WORK**

### **Based On Chain Rule**

Formula 1:

$$P = No. of person$$

$$\frac{P_1 H_1 D_1}{P_2 H_2 D_2} = \frac{w_1}{w_2}$$

$$w = Work$$

$$P_1H_1D_1 = P_2H_2D_2$$

**Sol.** 
$$P_1 = 15$$
,  $W_1 = 3240$ ,  $H_1 = 2$ ,  $D_1 = 6$ 

$$P_2 = ?$$
,  $w_2 = 5400$ ,  $H_2 = 4$ ,  $D_2 = 3$ 

$$\frac{P_1 H_1 D_1}{P_2 H_2 D_2} = \frac{w_1}{w_2}$$

$$\frac{15\times2\times6}{\times\times4\times3} = \frac{3240}{5400}$$

$$\frac{15}{x} = \frac{81}{135}$$

$$x = \frac{135 \times 15}{81}$$

$$x = 25$$

$$\therefore$$
 No. of men required = 25

**Sol.** 
$$P_1 = 39$$
  $D_1 = 12$   $H_1 = 5$  hour

$$P_2 = 30$$
  $D_2 = ?$   $H_2 = 6$  ho

$$P_1H_1D_1 = P_2H_2D_2$$

$$39 \times 5 \times 12 = 30 \times x \times 6$$

$$x = 13$$

No. of days = 13 days

suyogvarpe939@gmail.com

Q.24 Ajay & Sunil together can complete a piece of work in 10 days, Sunil & Sanjay in 15 days & Sanjay and Ajay. They worked together for 6 days, and then Ajay leaves. Sunil and Ajay worked for 4 more days, and Sunil leaves How long will Sanjay take to complete the work?

**Sol.** Work done in 1 day:

Ajay + sunil = 
$$\frac{1}{10}$$

Sunil + Sanjay = 
$$\frac{1}{15}$$

Sanjay + Ajay = 
$$\frac{1}{20}$$

$$2 \text{ Sunil} + 2 \text{ Ajay} + 2 \text{ Sanjay} = \frac{1}{10} + \frac{1}{15} + \frac{1}{20}$$

Sunil + Ajay + Sanjay = 
$$\frac{1}{2} \left[ \frac{13}{60} \right]$$

Sunil + Ajay + Sanjay = 
$$\frac{13}{120}$$
 ... (1)

Work done in 6 days = 
$$\frac{13}{20} \times 6$$

$$=\frac{13}{20}$$

Work done in 4 days = 
$$\frac{1}{15} \times 4$$

By Sunil & Ajay = 
$$\frac{4}{15}$$

: Sunil left after 4 days, Ajay left after 6 days

Remaining work = 
$$1 - \begin{bmatrix} Work done \\ in 6 days \end{bmatrix} + \begin{bmatrix} Work done \\ in 4 days \end{bmatrix}$$

$$=1-\left[\frac{13}{20}+\frac{4}{15}\right]$$

$$=1-\frac{55}{60}$$

Remaining work =  $\frac{1}{2}$  [to be completed by Sanjay alone]

No. of days required, from equ. (1)



Sanjay + 
$$\underbrace{\text{Ajay + Sunil}}_{}$$
 =  $\frac{13}{120}$ 

$$Sanjay + \boxed{\frac{1}{10}} = \frac{13}{20}$$

(given in question)

That Ajay & Sunil take 10 days

Sanjay = 
$$\frac{13}{120} - \frac{1}{10}$$

Sanjay = 
$$\frac{1}{120}$$

⇒ Sanjay can complete yob in 120 days.

We know, Remaining work =  $\frac{1}{12}$ 

∴ Days req. to complete 
$$\frac{1}{12}$$
 work by Sanjay =  $120 \times \frac{1}{12}$ 

Sanjay will take 10 days to complete work

- Q.25 'A' can complete 2/3 of a work in 4 days & 'B' can complete 3/5 of the work in 6 days. In how many days can both A and B together complete the work?
- Q.26 If 72 men can build a wall of 280 m length in 21 days, how many men could take 18 days to build a similar type of wall of length 100 m?

ogvarpe939@

### **TIME AND DISTANCE**

- Q.27 Two friends started for a place one by motorcycle and other by car. The speed of motorcycle is 30 km/hr. and that of car is 24 km/hr. The first one takes 6hr.12 min to reach the destination. Find the time of reaching of second one.
  - (A) 8:00 hr.
- (B) 7.25 hr.
- (C) 7.50 hr.
- (D) 7.75 hr

**Sol.** Motorcycle: 30 km/hr.

6 hr./2min.

- $\Rightarrow$  1 hr. = 30 km
- $\therefore$  Distance for 6 hrs. =  $6 \times 30$  km

$$= 180 \text{ km}$$

1 hr. = 60 min

60 mins = 30 km

$$1 \min = \frac{3\emptyset}{6\emptyset} = \frac{1}{2} \text{ km}$$

$$\therefore \text{ Distance for } 12 \text{ min} = \frac{1}{2} \times 12$$

$$= 6 \text{ km}$$

Distance covered in 6 hrs. 12 min = 180 + 6

$$= 186 \text{ km}$$

Speed = 24 km/hr.

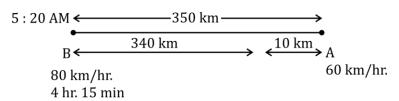
Time = DIstance/Speed

$$=\frac{186}{24}$$

$$\Rightarrow$$
 Time = 7.75 hr.

- Q.28 Kamal left for the City A from City B at 5:20 AM He travelled at a speed of 80Km/ hr. for 4 hrs. 1 min. After that, the speed was reduced to 60 km/hr. If the distance between two cities is 350 km, at what time did hamal reach City A
  - (A) 9: 20 AM
- (B) 9: 25 AM
- (C) 9:35 AM
- (D) 9:45 AM

Sol.



$$1 \text{ hr.} = 80 \text{ km}$$



Distance = Speed  $\times$  Time

 $= 80 \times 4 \text{ hr.}$ 

= 320 km

1 hr. = 80 km

60 min = 80 km

$$1 \min = \frac{8\emptyset}{6\emptyset}$$

$$15 \text{ mins} = \frac{8^4}{g_{z_1}} \times 15^5$$

=20 km

So Total distance travelled in 4 hr. 15 min = 320 + 20

= 340 km

Given, Total distance between A to B = 350 km

& distance travelled by B = 340 km From 4 hrs. 15 min

So remining distance = 350 - 340

= 10 km

Given speed = 60 km/hr.

$$\Rightarrow$$
 1 hr. = 60 km

$$\Rightarrow$$
 60 min = 60 km

$$\Rightarrow 1 \min = 1 \text{ km}$$

$$\therefore 10 \text{ km} = 10 \text{ min}$$

So  $10\ mins$  more to reach city A to travel  $350\ km$ 

So total time = 4 hrs. 15 mins

+ 10 mins

4 hrs. 25 mins

Journey started at 5: 20 AM

+ 4: 25

9:45 AM



- A man goes to his office by Scorer at a speed of 30 Km/hr. & reaches 6 min earlier. The goes Q.29 at a speed of 24 km/hr., he reaches 5 minutes late. The distance of his office is
  - (A) 20 Km

(B) 21 km

(C) 22 km

(D) 24 km

Sol.

$$T_1 \sim T_2 = 11 \text{ min}$$

$$\frac{D}{S} \sim \frac{D}{S} = 11 min$$

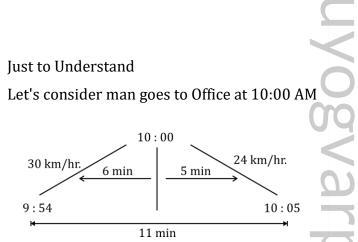
$$\frac{D}{30 \text{ km/hr.}} - \frac{D}{24 \text{ km/hr.}} = 11 \text{ min}$$

$$\frac{D}{30 \text{ km/hr.}} - \frac{D}{24 \text{ km/hr.}} = \frac{11}{60} \text{hr.}$$

$$\frac{4D-5D}{12\emptyset} = \frac{11}{6\emptyset}$$

$$D = \frac{11 \times 12}{6} \text{km}$$

$$D = 22 \text{ km}$$



### **Question to Practice**

Q.30 As car travelling at a speed of 40 km / hr. can complete a journey in 9 hr. How long will it take to travel the same distance at 60 km / hr.

# APNA

### **PROBLEMS ON TRAIN**

- A 100 m long train crossed a (rock/Pole/standing man) then, the distance travelled = Length of Train by train
- A 100 m long trains crossed a (Platform / Tunnel) of length 200 m, then: The distance travelled by Train = Length of Train + Platform Length
- Subtract Train 1 overtakes Train 2
  Speed Train 1 & Train 2 running in Parallel direction
- (+)
  Add
  Speed

  Train 1 crosses Train 2
  Train 1 Train 2 proceeds towards each other
- Q.31 A train 300 m long is running at a speed of as it will cross a bridge of 200 meters in?

**Sol.** Distance = 
$$300 + 200$$
, Speed =  $25 \text{ m/sec.}$  =  $500 \text{ m}$ 

$$T = \frac{D}{S}$$

$$T = \frac{500 \text{ m}}{25 \text{ m/sec.}}$$

$$T = 20 \text{ sec.}$$

Q.32 On train travelling at a speed of 30 m / sec crosses a platform, 600 m long in 30 seconds. The length (in meter) of train is?

**Sol.** 
$$S = 30 \text{ m/s}$$
  $P_L = 600 \text{ m}$   $T = 30 \text{ sec.}$ 

$$D = S \times T$$

$$\begin{cases} \text{If train crosses platform, D} = \frac{\text{Platform}}{\text{Length}} + \frac{\text{Platform}}{\text{Train}} \\ = 600 + x \end{cases}$$

$$600 + x = 30 \text{ m/sec.} \times 30 \text{ sec.}$$

$$600 + x = 900 \text{ m}$$

$$x = 300 \text{ m}$$

### **Question to Practice**

**Q.33** A train takes 18 seconds to pass through a platform 162 m long and 1 s seconds to pass through another platform 120 m long. The length of the train (in m) is:



### TRAINS MEETING

### Type - I:

Train speed,
distance between
stations, length
of both Train will be

To find at what distance & time both Trains meet

#### Formula:

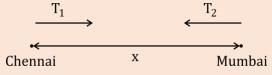
$$Distance = S_1 \left[ \frac{d + S_2 T}{S_1 + S_2} \right] km$$

Time = 
$$\left[\frac{d + S_2 T}{S_1 + S_2}\right]$$
 hours

where,  $S_1 = \text{speed of } 1^{\text{st}} \text{ Train}$ 

$$S_2 = speed of 2^{nd} Train$$

### Type – II:



To find distance between 2 stations

### Formula:

$$d\left[\frac{S_1 + S_2}{S_1 \sim S_2}\right] km$$

#### Type - III:

Chennai 
$$\bullet$$
  $T_1$   $\bullet$  Mumbai Chennai  $\bullet$   $T_2$ 

(Trains starting from same station but there will be a delay)

To find: Distance at which both trains meet

#### Formula:

$$\left[\frac{S_1 \times S_2 \times T}{S_1 \sim S_2}\right] km$$

To find: Time at which both Trains meet

Time = 
$$\left[\frac{S_1 T}{S_1 \sim S_2}\right]$$
 hours

- Q.34 Two trains start at the same time from A & B and proceeds towards B & A at 36 kmph & 42 kmph respectively. When they meet, it is found that one train has maned 48 km more than the other. What is the distance between A & B?
- Sol. Type II

$$d\left[\frac{s_1 + s_2}{s_1 \sim s_2}\right] km$$

$$=48\left[\frac{36+42}{36\sim42}\right]$$

$$=48\times\frac{78}{6}$$

$$= 48 \times 13$$

= 624 km

- Q.35 The distance between two stations A & B is 300 km. A train leaves Station 'A' at the speed of 30 km / hr. At the same time another train departs from Station B at speed of 45 km / hr. What will be the distance of the points Where both trains meet from point A?
- Q.36 A train leaves the station at 5 am at 60 km / hr. Another train leave the same station at 6:30 am at 75 km / hr. & travels in the direction of the first train. At What time and at what distance from the station will they meet?
- Sol. Type III

$$d = \left[\frac{S_1 \times S_2 \times T}{S_1 \sim S_2}\right] km$$

$$=\frac{60\times75\times\frac{3}{2}}{15}$$

$$= 450 \text{ km}$$

$$t = \left[\frac{S_1 T}{S_1 \sim S_2}\right] hours$$

$$= \left[ \frac{60 \times \frac{3}{2}}{15} \right] \text{ hours}$$

$$\left\{
\begin{array}{l}
T = 5 \text{ AM} \\
= 6:30 \text{ AM} \\
= 1\frac{1}{2} \\
= \frac{3}{2}
\end{array}
\right\}$$





 $\because 1^{st}$  Train starts at 5 am &  $2^{nd}$  Train starts at 6:30 am

So adding 6 hrs to 6:30

 $\Rightarrow$  Both Trains meet at = 6:30

+ 6 12:30

12:30 PM



## **CLOCK**

### To Find Angle between Hour & Minute Hand

#### Formula:

$$\theta = \left| 30H - \frac{11}{2}M \right|$$

H = Hour

M = Minutes

By using formula, If the angle between hour hand & minute hand is greater than 180°, then use:

360° – angle obtained by formula method

### Q.37 What is the angle between minute hand and hour hand at 1: 20?

**Sol.** Using Formula:

$$\theta = \left| 304 - \frac{11}{2} (M) \right|$$

$$\theta = \left| 30(1) - \frac{11}{2}(20) \right|$$

$$\theta = |-80|$$

$$\theta = 80^{\circ}$$

### Q.38 Find at what time between 1:00 and 2:00, the hands of clock will be together

**Sol.** 
$$\theta = 30H - \frac{11}{2}M$$

$$0 = 30 \times 1 - \frac{11}{2} M$$

$$-30 = -\frac{11}{2}M$$

$$30 = \frac{11}{2}M$$

$$M = \frac{30 \times 2}{11}$$

$$=\frac{60}{11}$$

$$=5\frac{5}{11}$$

$$\Rightarrow 1:05:\frac{5}{11}\sec$$

$$\begin{cases} \theta = 0^{\circ} \\ \text{as hands of clock} \\ \text{will be together} \end{cases}$$

For H consider lower value between which we have to find, eg – between 1 and 2 lower value is 1.



#### 0.39 Find at what time between 3:00 & 4:00, the hands of clock will be at a right angle

**Sol**. 
$$\theta = 30H - \frac{11}{2}M$$

If 
$$\theta = +90^{\circ}$$

$$90 = 30 \times 3 - \frac{11}{2} (M)$$
  $\{\theta = \pm 90^{\circ}\}$ 

$$\{\theta = \pm 90^{\circ}\}$$

$$90 - 90 = -\frac{11}{2}M$$

$$0 = -\frac{11}{2}M \Rightarrow M = 0$$

If 
$$\theta = -90^{\circ}$$

$$-90 = 30 \times 3 - \frac{11}{2}M$$

$$-90 - 90 = -\frac{11}{2}M$$

$$\neq 180 = \neq \frac{11}{2}M$$

$$M = \frac{180 \times 2}{11}$$

$$=\frac{360}{11}$$

$$=32\frac{8}{11}$$
 sec

### At what time between 4:00 & 5:00, the hands of Clock will be in opposite direction?

**Sol**. 
$$\theta = 30 \text{ H} - \frac{11}{2} \text{M}$$

$$\theta = \pm 180^{\circ}$$
 (Because opposite direction)

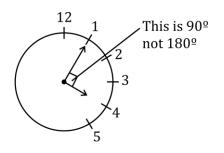
If 
$$\theta = +180^{\circ}$$

$$180 = 30 \times 4 - \frac{11}{2}M$$

$$180 = 120 - \frac{11}{2}M$$

$$60 = -\frac{11}{2}M$$

$$M = \frac{60 \times 2}{11}$$



$$\begin{cases} \text{therefore we} \\ \text{cannot consider} \\ \theta = +180^{\underline{o}} \end{cases}$$



$$M = \frac{120}{11}$$

If we observe 4:  $10: \frac{10}{11}$  sec.

$$=10\frac{10}{11}$$

$$\Rightarrow 4:10:\frac{10}{11} \text{ sec.}$$

— not Possible as it won't form 180º

If 
$$\theta = -180^{\circ}$$

$$-180 = 30 \times 4 - \frac{11}{2} \times M$$

$$-180 - 120 = -\frac{11}{2}M$$

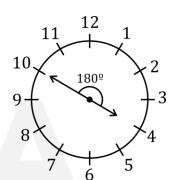
$$-300 = -\frac{11}{2}M$$

$$M = \frac{300 \times 2}{11}$$

$$=\frac{600}{11}$$

$$=54\frac{6}{11}$$

At 4: 54:  $\frac{6}{11}$  sec. the hands of clock will be in opposite direction.



- Q.41 What is the angle between minute hand and hour hand at 10:10
- Q.42 At what time between 3:00 & 4:00, will the hands of a clock be together?
- Q.43 Find at what time between 5:30 & 6:00, the hands of clock will be at right angle.

uyogva

## PERCENTAGE

- Q.44 If 50% of P = 25% of Q, then P = x% of Q Find x.
  - (A) 0.5

- (B) 20
- (C) 50
- (D) 30

{Total students Present = 1000 Boys + 800 Girls = 1800}

- Sol.  $50_2\%$  of P =  $25_1\%$  of Q
  - 2P = Q

To Find : P = x% of Q

- $\frac{Q}{2} = \frac{x}{100} \times Q$
- $x = \frac{100}{2}$
- x = 50
- In an examination, there were 1000 boys & 800 girls. 60 % of the boys and 50 % of girls passed Find the percent of Candidates failed?
- Sol. **1000** Boys

800 Girls

- 60 % Passed
- 50 % Passed
- 40 % Failed
- 50 % Failed
- $\Rightarrow \frac{40}{100} \times 1000$
- $=\frac{50}{100}\times800$
- = 400 Boys Failed
  - = 400 Girls Failed
- $\Rightarrow$  400 (Boys) + 400(girls) = 800 failed
- Total students who failed % of candidates =  $\frac{1}{\text{Total students paresent in exam}}$
- $=\frac{800}{1800}\times100$
- = 44.44 %
- Rath spends 40 % of her salary on food, 20 % on house rent and, 10 % on entertainment & 0.46 10 % on conveyance. If her savings at the end of a month are Rs 1500, then her salary per month (in Rs) is:
- Sol.

Savings: 100 % - expenditure

- = 100 % [40 % + 20 % + 10 % + 10 %]
- = 100% 80%
- = 20 %
- 20% = 1500



$$\therefore 100 \% = x$$

$$x = \frac{1500 \times 10\emptyset}{2\emptyset}$$

x = 7500

### **Question to Practice**

Q.47 If 20 % of (P + Q) = 50 % of (P: Q)

(A) 7:8

(B) 7:3

(C) 7:5

(D) 5:7

(A) 7: 8 (B) 7: 3 (C) 7: 5 (D) 5: 7

Q.48 For an examination, it in required its get 36 % of maximum marks to pass. A student got 113 marks for the examination are?

**Q.49 30** % of **2800** =?



### **PROFIT & LOSS**

### Formula:

$$\% \text{ gain} = \frac{\text{SP} - \text{CP}}{\text{CP}} \times 100$$

$$\{SP = Selling Price \}$$
  
 $\{CP = cost Rice \}$ 

$$CP = cost Rice$$

$$\% loss = \frac{CP - SP}{CP} \times 100$$

$$CP = \frac{100}{100 - loss \%} \times SP$$

$$CP = \frac{100}{100 + gain \%} \times SP$$

$$SP = \frac{100 + gain \%}{100} \times CP$$

$$SP = \frac{100 - \log \%}{100} \times CP$$

% change = 
$$a + b + \frac{ab}{100}$$

a = 1st Selling Price

b = 2<sup>nd</sup> Selling Price

By selling a cycle for Rs 4860, a student loses 19 % His cost Price is?

Sol. 
$$CP = \frac{100}{100 - Loss \%} \times SP$$

$$= \frac{100}{100 - 19} \times 4860$$

$$= \frac{100}{81} \times 4860$$

$$CP = 6000$$

Q.51 By selling a cell phone for Rs 2400, a shopkeeper makes a profit of 25%. Then, his profit percentage if he had sold it for Rs 2040, is?

Sol.  $CP = \frac{100}{100 + 25} \times 2400$   $\begin{cases} :: CP = \frac{100}{100} \times SP \end{cases}$ 

Sol. 
$$CP = \frac{100}{100 + 25} \times 2400$$
  
=  $\frac{100}{125} \times 2400$ 

$$CP = 1920$$

If 
$$SP = 2040$$
, gain  $\% = ?$ 

gain % = 
$$\frac{SP - CP}{CP} \times 10$$
  
=  $\frac{2040 - 1920}{1920} \times 100$   
=  $\frac{120}{1920} \times 100$   
gain % = 6.25%

- $-\times 100$   $\int_{J}^{20} \times 100$   $\int_{J}^{3} \times 100$   $\int_{J}^{3} \times 6.25\%$ .ehaan purchased a bike for Rs 54,000. He sold it a Loss of 8%. with that money purchased another bike & sold it at a profit of 10%. What is his overall loss/ Profit?  $\int_{J}^{3} \times 100$   $\int_{J}^{3}$ Q.52
- Sol.

$$a = -8$$
 (Loss)

$$b = +10$$
 (Profit)

% change 
$$= -8 + 10 - \frac{80}{100}$$

$$= 2 - 0.8$$

$$= 1.2\%$$

$$= 54000 \times \frac{1.2}{100}$$

$$= Rs 648$$

- Q.53 A Calculator is bought for Rs.350 and sold at a gain of 15% what will be the selling Price of Calculator?
- Q.54 By selling an article for Rs.720, a man loss 10% At what price should he sell at, to gain



## **RATIO AND PROPORTION**

Q. 55 If A: B = 
$$\frac{1}{2}$$
:  $\frac{1}{3}$ 

and B: 
$$C = \frac{1}{2} : \frac{1}{3}$$

then A: B: C = ?

**Sol.** A: B = 
$$\frac{1}{2}$$
:  $\frac{1}{3}$  B: C =  $\frac{1}{2}$ :  $\frac{1}{3}$ 

B: 
$$C = \frac{1}{2} : \frac{1}{3}$$

Taking L.C.M.

Taking L.C.M.

$$=\frac{3:2}{6}$$

$$=\frac{3:2}{6}$$

$$A: B = 3:2$$

$$B: C = 3:2$$

Put closest value 
$$\vdots$$
 B is 3  $\vdots$  Closest to C = 3  $\vdots$  A : B : C  $\vdots$  Put value which is closest  $\vdots$  B = 2  $\vdots$  closest value to C = 2 By multiplying both ratios  $\vdots$  By multiplying both ratios

Q.56 If a : b = 5 : 7

and c: d = 2a: 3b

then ac : bd = ?

a : b = 5 : 7, c : d = 2a : 3bSol.

$$\frac{a}{b} = \frac{5}{7} \qquad \qquad \frac{c}{d} = \frac{2a}{3b}$$

$$\frac{c}{d} = \frac{2a}{3b}$$

$$\frac{ac}{bd} = ?$$

Putting above values

$$\frac{ac}{bd} = \frac{5}{7} \times \frac{2a}{3b} \longrightarrow \left(\text{Substitute Value of } \frac{a}{b}\right)$$
$$= \frac{5}{7} \times \frac{2}{3} \times \frac{5}{7}$$
$$\frac{ac}{bd} = \frac{50}{147}$$

Divide Rs. 1250 among A, B, C, so that A gets 2/9 of B's share and C gets 3/4 of A' share Find the shares of A, B and C.

**Sol.** Given: 
$$A = \frac{2}{9}B$$
,  $C = \frac{3}{4}A$  (Substitute value of A)



$$\frac{A}{B} = \frac{2}{9}, \qquad C = \frac{3}{42} \times \frac{2}{93} B$$

$$\boxed{A: B = 2: 9} \qquad \frac{C}{B} = \frac{1}{6}$$

$$\frac{B}{C} = \frac{6}{1}$$

$$B: C = 6:1$$

Put nearest value  $\begin{array}{c|c}
A : B : C \\
\hline
2 : 9 : 9 \\
\hline
6 : 6 : 1
\end{array}$ Put nearest value  $\overline{12 : 54 : 9}$ 

On Simplifying

A: B: 
$$C = 12^4 : 54^{18} : 9^3$$
  
= 4 : 18 : 3

### **Question to Practice**

- Q.58 A mixture contains alcohol & water in the ratio 4: 3. If 5 litres of water is added to mixture the ratio becomes 4:5. find the quantity of alcohol in given mixture.
- Q.59 If A: B = 2:3

and B: C = 4:5 then

A: B: C = ?

Q.60 If 3A = 5B

and 4B = 6C then

A: C = ?



## SIMPLE INTEREST & COMPOUND INTEREST

### Simple interest

$$S \cdot I = \frac{PRT}{100}$$

$$A = P \left[ 1 + \frac{RT}{100} \right]$$

P = Principal T = Time Duration R = Rate of Interest A = Total amount

### **Compound Interest**

$$CI = P\left\{ \left[ 1 + \frac{R}{100} \right]^n - 1 \right\}$$

$$A = P\left(1 + \frac{R}{100}\right)^{n}$$
 where 
$$P = Principal$$
 Maturity Amount 
$$Total\ amount$$
 
$$Amount\ becomes$$
 
$$R = Rate\ of\ Interest$$
 
$$n = no\ of\ years$$

A = Total amount

### **Compound Interest**

(i) for half-yearly

### Formula:

$$A = P \left[ 1 + \frac{R/2}{100} \right]^{2n}$$

(ii) for Quarterly

#### Formula:

$$A = P \left[ 1 + \frac{R/4}{100} \right]^{4n}$$

Q.61 Dinesh deposit an amount of Rs 65800 to obtain simple Interest at 14% per annum for 4 years. What total amount will Dines get at the end of 4 years?

Sol. 
$$A = P \left[ 1 + \frac{RT}{100} \right]$$
  
 $A = 65800 \left[ 1 + \frac{(14 \times 4)}{100} \right]$ 

$$= 65800 \times \left[1 + \frac{56}{100}\right]$$

$$=\frac{658\emptyset\emptyset\times156}{1\emptyset\emptyset}$$

$$= 102648$$

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**Sol.** 
$$A = P \left[ 1 + \frac{P/2}{100} \right]^{21}$$

$$A = 16000 \left[ 1 + \frac{5}{100} \right]^2$$

$$= 16000 \left(\frac{105}{100}\right)^2$$

$$=16\emptyset\emptyset\emptyset\times\frac{105}{1\emptyset\emptyset}\times\frac{105}{1\emptyset\emptyset}$$

$$= 17,640$$

$$SI = 60 \sim 30$$

$$= 30$$

$$S. I_1 - S. I_2 = 30$$

$$\frac{PRT}{100} - \frac{PRT}{100} = 30$$

$$1500 \left[ \frac{4x}{100} - \frac{8x}{100} \right] = 30$$

$$1500 \times \frac{4x}{100} = 30$$

$$2x = 1$$

$$x = 0.5\%$$

Q.64 What will be the Compound Interest for sum of Rs. 8000 after 3 years at rate of 5% p.a.



### **AVERAGE**

Formula: Average = 
$$\frac{\text{Sum of Observation}}{\text{Total Number of Observation}}$$

- The average age of A, B and C is 26 years If the average age of A and C is 29 years. What is the Q.65 age of B in years?
- Sol.

age of B in years?
given:
$$\frac{A+B+C}{3}=26, \qquad \frac{A+C}{2}=29$$

$$A+B+C=26\times 3 \quad A+C=29\times 2$$

$$A+B+C=78 \quad A+C=54$$
Age of B = Total  $-(A+C)$ 

$$=78-54$$

$$=20 \text{ years.}$$
The average of 7 numbers is 5. If the average of first six of these numbers is 4, the seventh number is?

number is?

$$\begin{cases} Average = \frac{Total \text{ of } 7' \text{ no.}}{No. \text{ of terms}} \\ 5 = \frac{Total \text{ of '7' no.}}{7} \end{cases}$$

Total of '7' no.

$$= 7 \times 5$$

$$= 35$$

$$\begin{cases} \text{Average} &= \frac{\text{Total of 6 no.}}{\text{No. of Terms}} \\ 4 &= \frac{\text{Total of 6 no.}}{6} \end{cases}$$

Total of 6 no. =  $6 \times 4$ 

$$= 24$$

$$\therefore$$
 Seventh no. = 35 - 24

$$= 11$$

The average of marks obtained by 120 candidates was 35. If the average of marks of passed Q.67Candidates was 39 & that of failed candidates was 15, the number of candidates who passed the examination is?

**Sol.** Avg = 
$$\frac{\text{Total marks obtained}}{\text{No of Students}}$$



$$35 = \frac{\text{Total marks}}{120}$$

Total marks = 
$$120 \times 35$$
  
=  $4200$ 

Let's assume no of Passed candidates as 'x'

4200 = Marks obtained by passed candidate + Marks obtained by failed Candidate

$$4200 = (x \times 39) + [(120 - x) \times 15]$$

$$4200 = 39x + 1800 - 15x$$

$$2400 = 24x$$

$$x = 100$$

 $\therefore$  Passed candidates = 100

- Q.68 Of the three numbers, the first is twice the second and the second is thrice the third. If the average of the three numbers is 10. The number are?
- Q.69 The average expenditure of a man for the first 5 months is Rs 3600 and for the next 7 months it is Rs. 3900. If he saves Rs. 8700 during the year, his average income per month is?

### **AVERAGE SPEED**

**Note 1:** If the certain distance is covered at the speed of 'x' km/hr and the same distance is covered at 'y' Km/hr.then the average speed during entire journey is:

Where x, y = speed

**Note 2:** If the person covers 'A' Km at a speed of 'x' Km/hr., 'B' Km at a speed of 'y' km/hr. and 'C' km at a speed of 'z' km/hr. Find out average speed of entire journey

$$\left(\frac{A+B+C}{\frac{A}{x}+\frac{B}{y}+\frac{C}{z}}\right) \text{km/hr.}$$

where, A, B, C = distance

x, y, z = speed

Q.70 An person covers 9 km at a speed of 3 km/hr., 25 km at a speed of 5 km/hr and 30 km at a speed of 10 km/hr. Find out the average speed of the entire journey.

Sol. 
$$\left(\frac{A+B+C}{\frac{A}{x}+\frac{B}{y}+\frac{C}{z}}\right)$$
 km/hr.

Avg. speed = 
$$\left(\frac{9 + 25 + 30}{\frac{9}{3} + \frac{25}{5} + \frac{80}{10}}\right)$$

$$= \left(\frac{9+25+30}{3+5+3}\right)$$

$$=\frac{64}{11}$$

= 5.81 km/hr.

# uyogvarpe939@s



# **PROBABILITY**

$$Probability = \frac{Sum of Observation}{Possibility}$$

# "Coins"

# **Possibility**

- **1.** One Coin tossed :  $\{H, T\} = 2 \rightarrow Possibility$
- 2. Two Coins Tossed Simultaneously = {HH, HT, TH, TT} = 4

4. Four Coins Tossed = 
$$\begin{cases}
HHTH, THTT \\
HTHH, HTTT \\
THHH, HTTT \\
HTTT, THHT \\
HTTH, HTHT
\end{cases} = 16$$

Q.71 3 coins are tossed find the probability of exactly 2 heads.

Probability of exactly 2 heads =  $\frac{3}{8}$ 

### **Question to Practice**

Q.72 3 coins are tossed find the probability of no heads?



# DICE

# **Possible Outcomes**

(1) 1 Dice = 
$$6^n$$
 = (Where n = No. of Dice)  
=  $6^1$   
=  $6$ 

(2) 2 Dice = 
$$6^2$$
  
= 36

(3) 3 Dice = 
$$6^3$$
  
= 216

# Q.73 In a single throw of 2 dice, find the probability of getting a total of 3 or 5

**Sol.** Possible Outcomes

Probability = 
$$\frac{6}{36}$$

$$= \frac{1}{6}$$

# **Question to Practice**

Q.74 In a single throw of 2 dice, what is the probability of a doublet (same number)?

# Q.75 In a single throw of 3 dice, then find the probability of getting a total of 5

Sol. Possible Outcomes = 
$$6^n$$
  
=  $6^3$   
= 216  
Total of 5:  $\{(1,1,3) \quad (1,3,1) \quad (3,1,1)\}$   
 $(2,2,1) \quad (2,1,2) \quad (1,2,2)\}$   
Probability =  $\frac{6}{216}$ 



# **PERMUTATION**

# Q.76 How many ways the word can be arranged?

- (i) Non-Repeated Letters
  - (A) CAT
  - (B) MACHINE
  - (C) GAME
  - (D) CRYSTAL
  - (E) EDUCATION

Sol. (A) CAT 
$$= 3! - \text{Total No. of letter}$$
$$= 3 \times 2 \times 1$$
$$= 6$$

(B) MACHINE = 7!  
= 
$$7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$
  
=  $5040$ 

(C) GAME = 4!  
= 
$$4 \times 3 \times 2 \times 1$$
  
= 24

(D) CRYSTAL = 7!  

$$= 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$

$$= 5040$$

(E) EDUCATION = 9!  
= 
$$9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$
  
=  $362880$ 

- (ii) Repeated Letter
  - (A) SISTER
  - (B) PERCENTAGE

Sol. (A) SISTER = 
$$\frac{6!}{2!}$$
 Total No. of letter

No. of repeated letter

$$= \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{2 \times 1}$$

$$= 360$$



(B) PERCENTAGE = 
$$\frac{10!}{3!}$$
= 
$$\frac{10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 2 \times 2 \times 2}{2 \times 2 \times 2 \times 2}$$
= 
$$604800$$

- Q.77How many ways the word can be arranged?
- (i) **Vowel that comes together** 
  - (A) JUDGE
  - (B) MACHINE
- Sol. (A) JUDGE

Vowel: (UE)

JDG(UE)

we can place (UE) at following places

$$\frac{\downarrow}{J} \underbrace{J} \underbrace{D} \underbrace{\downarrow} G \underbrace{\downarrow}$$

$$= 4! \times 2!$$

No. of places

Vowels (UE)

where we can

[2 Letters]

place vowels

(No. of ways we can re-arrange vowel)

(B) MACHINE

Vowel: (AIE)

We can place (AIE) in following places  $\downarrow M \downarrow C \downarrow H \downarrow N \downarrow$ 

No. of places

(No. of ways (AIE) can

where we can

be re-arrange [3 Letters])

(AIE) place vowel

- (ii) Vowels always comes together
  - (A) SISTER
- Sol. Vowels: (IE)

We can place (IE) in following places

$$\frac{1}{\sqrt{S}} \underbrace{S} \underbrace{T} \underbrace{R} \underbrace{V}$$

$$= \underbrace{5! \times 2!}$$
No. of places
$$V = \underbrace{S} \underbrace{V}$$
No. of ways (IE) can be re-arranged [2] Letters

where we can

re-arranged [2 Letters, 2ways]

place (IE) No. of repeated

vowel Letters

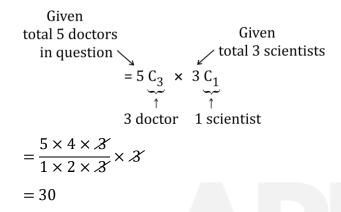
:uyogvarpe939@gm;

# **COMBINATION**

Q.78 Different committee's are to be made as per the requirement in each question. In how many ways can it be done?

8 students out of which 5 are doctors and 3 are scientist

- (i) A committee of 4 in while 3 are doctors & 1 is scientist
- **Sol.** 3 doctor & 1 scientists



- (ii) A committee of 5 in while which 3 are doctors
- **Sol.** To make committee of 5

3 are doctors (given)

 $\Rightarrow$  2 are scientists [5 - 3 = 2]

Committee doctor

Total
5 doctors
given 
$$\checkmark$$
 given
 $= 5 C_3 \times 3 C_2$ 

$$=\frac{5\times4\times\cancel{\mathcal{X}}}{1\times2\times\cancel{\mathcal{X}}}\times\frac{3\times\cancel{\mathcal{Z}}}{1\times\cancel{\mathcal{Z}}}$$

- = 30
- (iii) A committee of 2 in which there is no doctor
- **Sol.** (No doctor)

Committee of  $2 \Rightarrow$  only 2 scientists

Total
3 scientists
given
$$3 \underbrace{C_2}_{2} = \frac{3 \times 2}{1 \times 2} = 3$$
2 scientists





- (iv) Committee of 2 unit which either both are doctors or both are scientists
- **Sol.** 5 doctors 3 scientists (given)

Committee of 2

$$5 C_2 \oplus 3 C_2$$

either both doctor or scientist

$$=\frac{5\times4}{1\times2}+\frac{3\times2}{1\times2}$$

$$= 10 + 3$$



# **SQUARE AND CUBE ROOTS**

# Q.79 What least number should be multiplied with 384 to make it a perfect square?

**Sol.**  $384 \times ? = Perfect Square$ 

$$384 = 2 \times 3$$

$$=2^2\times 2^2\times 2^2\times 2^1\times 3^1$$

Perfect squares not perfect squares

To make  $2^1 \times 3^1$  perfect square,

we have to multiply it by  $2^1 \times 3^1$ 

$$\Rightarrow 2^1 \times 3^1 \times 2^1 \times 3^1$$

$$\Rightarrow \underbrace{2^2 \times 3^2}$$

(Perfect Square) (6)

 $\div$  6 is Least number to be multiplied with 384 to make it a perfect square.

# **Question to Practice**

- Q.80 What is the smallest number with which 5400 may be multiplied so that product is perfect cube?
- Q.81 Square of difference between two numbers is 9 while the sum of squares of those two number is 225 what is their product?

**Sol.** Given: 
$$(a - b)^2 = 9 \dots (1)$$

$$a^2 + b^2 = 225 \dots (2)$$

We know identity,

$$(a - b)^2 = a^2 + b^2 - 2ab$$

From (1) & (2)

$$9 = 225 - 2ab$$

$$ab = 116$$

$$ab = 58$$

$$∴$$
 Produce = 58

# APNA DLLEGE SU

# **LOGARITHM**

# Q.82 Find the value of:

(A) 
$$\log_5(25)$$

**Sol.** 
$$\log_5(5)^2 = 2 \times \log_5(5)$$
  
= 2 × 1  
= 2

(B) 
$$\log_{81} 3$$

**Sol.** 
$$81 = 3^4$$

$$\log_{3} 4(3) = \frac{1}{4} \times \log_{3}(3)$$
$$= \frac{1}{4} \times 1$$
$$= \frac{1}{4}$$

(C) 
$$\log_{\sqrt{7}} \left( \frac{1}{243} \right)$$

**Sol.** 
$$\frac{1}{243} = \frac{1}{(7)^3} = 7^{-3}$$
 (1)

$$\sqrt{7} = 7^{1/2}$$

$$\log_{7^{1/2}}(7^{-3}) = -3 \times \log_{7^{1/2}}(7)$$
$$= -3 \times \frac{1}{2}\log_{7} 7$$
$$= -3 \times 2 \times 1 = -6$$

**Sol.** 
$$1000 = 10^3$$

• 
$$0001 = \frac{1}{1000} = \frac{1}{10^4} = 10^{-4}$$

$$\log_{10} -410^{3} = 3 \times \frac{1}{(-4)} \log_{10} 10$$
$$= -\frac{3}{4} \times 1$$
$$= -\frac{3}{4}$$



$$(E) \qquad log_2 \bigg( \frac{512 \times 256}{32} \bigg)$$

**Sol.** 
$$32 = 2^5; 256 = 2^8$$

$$512 = 2^9$$

$$= \log_2 \frac{(2^9 \times 2^8)}{2^5}$$

$$= \log_2(2^9 \times 2^3)$$

$$= \log_2(2^{12})$$

$$= 12 \times \log_2(2)$$

$$= 12 \times 1 \Rightarrow 12$$

# Q.83 Find the value of y, if $log_y(25/9) = -2$

**Sol.** 
$$\log_{v}(25/9) = -2$$

$$a^m = x [log_a(x) = m]$$

$$y^{-2} = \frac{25}{9}$$

$$y^2 = \frac{9}{25}$$

$$y = \frac{3}{5}$$

# Q.84 Find the value of:

$$\log\left(\frac{15}{16}\right) - \log\left(\frac{27}{45}\right) + \log\left(\frac{48}{75}\right)$$

$$\log_a(xy) = \log_a(x) + \log_a(y)$$

# **Quotient Rule:**

$$log_a(x/y) = log_a(x) - log_a(y)$$

$$\log\left(\frac{15}{16}\right) - \underbrace{\log\left(\frac{27}{45}\right)}_{\downarrow} + \underbrace{\log\left(\frac{48}{75}\right)}_{\downarrow}$$

Quotient Rule Product Rule

$$\log \left( \frac{15^{1}}{16} \times \frac{45^{8}}{27_{g_{1}}} \times \frac{48^{3^{1}}}{75} \right)_{g_{1}}$$

$$= \log 1 = 0$$

**Sol. 7** 
$$(1^2 + 2^2 + \dots + 20^2) - (1^2 + \dots + 9^2)$$

$$=\frac{n(n+1)(2n+1)}{6}-\frac{n(n+1)(2n+1)}{6}$$

$$=\frac{20\times21\times41}{6}-\frac{9(10)(19)}{6}$$

$$= 2870 - (15 \times 19)$$

$$= 2585$$

**Sol. 9** 
$$a = 2$$

$$d = 7 - 2 = 5$$

$$n = 9$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{19} = \frac{19}{2} [2(2) + (19 - 1)5]$$

$$=\frac{19}{2}[4+(18\times5)]$$

$$=\frac{19}{2}\times 94=893$$

# **Sol. 14** Let the no. be x

$$\frac{4}{5}x - \frac{3}{4}x = 8$$

$$\frac{16x - 15x}{20} = 8$$

$$x = 160$$

# **Sol. 15** Let the no. be x

First no.-second no. = 7

$$\frac{3}{4}x - \frac{1}{6}x = 7$$

$$\frac{3x}{4} - \frac{x}{6} = 7$$

$$\frac{9x - 2x}{12} = 7$$

$$x = 12$$

 $\frac{5}{3}$  of the number

$$\Rightarrow \frac{5}{3}x$$

$$=\frac{5}{3}\times12$$

$$= 20$$

## Sol. 20

Past 4 years

Past age + 1

Past Present Future

2: 3 ? 5: 7

2x: 3x 5x: 7x

$$\frac{2x + 8}{3x + 8} = \frac{5}{7}$$

$$14x + 56 = 15x + 40$$

$$x = 6$$

Present ages, of A & B.

$$2x + 4 \Rightarrow 2(16) + 4$$

$$3x + 4 \Rightarrow 3(16) + 4$$

# **Sol. 21**

<u>Son</u>

**Father** 

Present age

X

3 + 3x

Future age

x + 3

3x + 6

After 10 years,

$$3x + 6 = 10 + 2(x + 3)$$

$$3x + 6 = 10 + 2x + 6$$

$$x = 10$$

 $\therefore$  Father Present age = 3 + 3x

$$= 3 + 3(10)$$

**Sol.25** 

'A': 
$$\frac{2}{3}$$
 of work = 4 days

1 work done by 'A' =  $4 \times \frac{3}{2}$ 

$$A = 6 \text{ days}$$

'B': 
$$\frac{3}{5}$$
 of work = 6 days

1 work done by 'B' =  $6 \times \frac{5}{3}$ 

$$B = 10 \text{ days}$$

$$A + B = ?$$

$$=\frac{1}{6}+\frac{1}{10}$$

$$=\frac{3^4}{30_{15}}\Rightarrow\frac{4}{15}$$

$$=\frac{4}{15}$$

Final answer will be reciprocal  $\Rightarrow \frac{15}{4}$  days

$$=3\frac{3}{4}$$
 days

$$P_1 = 72$$
  $D_1 = 21$   $w_1 = 280$ 

$$P_2 =$$

$$D_2 = 18$$

$$P_2 = ?$$
  $D_2 = 18$   $w_2 = 100$ 

We know, 
$$\frac{P_1 H_1 D_1}{P_2 H_2 D_2} = \frac{w_1}{w_2}$$

But in above question nothing is mentioned about no. of hours

$$\therefore \text{ we use } \frac{P_1 D_1}{P_2 D_2} = \frac{W_1}{W_2}$$

$$\frac{72 \times 21}{x \times 18} = \frac{280}{100}$$

$$\frac{6}{x} = \frac{1}{5}$$

$$x = 6 \times 5$$

$$x = 30$$

No. of men required = 30

### **Sol.30**

$$40 \text{ km/hr.} \times 9 = 360 \text{ km}$$

(: Distance = Speed 
$$\times$$
 Time)

$$60 \text{ km/hr.} \times ? = 360 \text{ km}$$

time = 
$$\frac{360}{60}$$

time = 6 hr.

### **Sol.33**



$$S_1 = S_2$$

$$\frac{D}{T} = \frac{D}{T}$$

(Length of Train + Platform Length) \_ Length of Train + Platform Length

Time

$$\frac{x+162}{18_6} = \frac{x+120}{15_5}$$

$$5x + 810 = 6x + 720$$

x = 90 m

### Type - I **Sol.35**

**Question to Practice** 

$$d = S_1 \left[ \frac{d + s_1 t}{s_1 + s_2} \right] km$$

t = Time difference

$$= T_1 \sim T_2$$

= 0 (: beth trains start at same time)

$$d = 30 \left[ \frac{300 + 30(0)}{30 + 45} \right]$$

$$=30\left[\frac{300}{75}\right]$$

$$=\frac{9000}{75}$$

= 120 km

**Sol. 41** 
$$\theta = \left| 30H - \frac{11}{2}(M) \right|$$

$$\theta = \left| 30(10) - \frac{11}{2}(10) \right|$$

$$\theta = |300 - 55|$$

$$\theta = 245^{\circ}$$

$$\because$$
 angle  $> 180^{\circ}$ 

$$= 115^{\circ}$$

**Sol. 42** 
$$\theta = \left| 30H - \frac{11}{2}(M) \right|$$

$$0^{\circ} = 30 \times 3 - \frac{11}{2} M$$

$$0 = 90 - \frac{11}{2}M$$

$$-90 = -\frac{11}{2}M$$

$$M = \frac{90 \times 2}{11}$$

$$=\frac{180}{11}$$

$$=16\frac{4}{11}$$

$$\Rightarrow$$
 3: 16:  $\frac{4}{11}$  sec.

**Sol. 43** 
$$\theta = 30H - \frac{11}{2}M$$

$$\theta = \pm 90^{\circ}$$

If 
$$\theta = -90^{\circ}$$

$$-90 = 30 \times 5 - \frac{11}{2}M$$

$$-90 - 150 = -\frac{11}{2}M$$

$$240 = \frac{11}{2} M$$

$$M = \frac{480}{11}$$

$$=43\frac{7}{11}$$

Between 5:30 & 6:00, the hands of clock will be at right angle at 5:43:7/11 sec.

**Sol.47** 20% of 
$$(P + Q) = 50\%$$
 of  $(P - Q)$ 

$$2(P+Q) = 5(P-Q)$$

$$2P + 2Q = 5Q - 5Q$$

$$2Q + 5Q = 5P - 2P$$

$$7Q = 3P$$

$$\frac{P}{Q} = \frac{7}{3}$$

**Sol.48** Pass Mark = 
$$113 + 85$$

$$= 198$$

$$100\% = x$$

$$36x = 198 \times 100$$

$$x = \frac{198 \times 100}{36}$$

$$x = 550$$

**Sol. 49** 
$$=\frac{30}{100} \times 2800$$

$$= 30 \times 28$$

$$= 840$$

Sol. 53 SP = 
$$\frac{100 + P\%}{100} \times CP$$
  
=  $\frac{100 + 15}{100} \times 350$   
=  $\frac{115}{100} \times 350$ 

$$SP = 402.5$$

Sol. 54 CP = 
$$\frac{100}{100 - \text{Loss\%}} \times \text{SP}$$
  
=  $\frac{100}{90} \times 720$   
=  $800$   
SP =  $\frac{100 + \text{gain \%}}{100} \times \text{CP}$   
=  $\frac{100 + 5}{100} \times 800$   
 $|\text{SP} = 840|$ 

**Sol. 58** Alcohol: Water 
$$= 4:3$$

$$= 4x: 3x$$

Alcohol = 4x, water = 3x

Given: 5 litres of water is added

$$\frac{4x}{3x+5} = \frac{4}{5}$$

$$4x \times 5 = 4(3x + 5)$$

$$20x = 12x + 20$$

$$8x = 20$$

$$x = 20/8$$

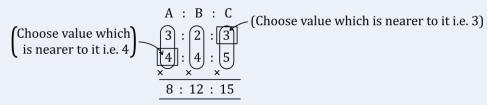
$$x = 5/2$$

 $Quantity \ of \ alcohol = 4x$ 

$$= 4^2 \times \frac{5}{2}$$

= 10 litres

**Sol.59** A: B = 2: 3, B: 
$$C = 4:5$$



A: B: 
$$C = 8: 12: 15$$

**Sol.60** 
$$3A = 5B$$
,

$$4B = 6C$$

$$\frac{A}{B} = \frac{5}{3} \qquad \qquad \frac{B}{C} = \frac{6}{4}$$

$$\frac{B}{C} = \frac{6}{4}$$

A: 
$$B = 5:3$$
 B:  $C = 6:4$ 

$$B: C = 6:4$$

A : B : C – Put nearest value Put nearest value -30 : 18 : 12

But we want A: C

On Simplifying  $\Rightarrow 30^5: 12^2$ 

$$\Rightarrow$$
 A: C = 5:2

**Sol. 64** 
$$A = P \left[ 1 + \frac{R}{100} \right]^n$$

$$=8000\left[1+\frac{5}{100}\right]^3$$

$$=8000 \left[ \frac{105}{100} \right]^3$$

$$=8000\times\frac{105}{100}\times\frac{105}{100}\times\frac{105}{100}$$

$$= 21 \times 21 \times 21$$

$$A = 9261$$

$$A = P + I$$

$$9261 = 8000 + I$$

$$I = 9261 - 8000$$

$$I = 1261$$

$$C. I. = Rs. 1261$$

**Sol.68** Third = 
$$x$$

$$Second = 3x$$

$$First = 2(3x)$$

$$= 6x$$

$$\frac{6x + 3x + x}{3} = 10$$

$$10x = 10 \times 3$$

$$10x = 30$$

$$x = 3$$

First number = 6x

$$=6\times3$$

Second number = 3x

$$= 3 \times 3$$

Third number = x

$$= 3$$

# **Sol.69** Total expenditure = $3600 \times 5$

$$= 18,000$$

Next 7 months =  $3900 \times 7$ 

$$= 27,300$$

Total Income for 12 months = 18,000 + 27,300 + 8,700

$$\therefore \text{ Arg. Income per month} = \frac{54000}{12}$$

$$= Rs. 4,500$$

Probability of no heads  $=\frac{1}{8}$ 

**Sol.74** Possible Outcomes

Probability = 
$$\frac{6}{36}$$
  
=  $\frac{1}{6}$ 

**Sol.80** 
$$5400 = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5$$

$$=2^3\times3^3 \times 5^2$$

Perfect cube not perfect cube

 $\therefore$  To make  $5^2$  a perfect cube, we have to multiply it by 5

$$=5^2\times(5)$$

$$= 5^3$$

 $\div$  Smallest number to be multiplied with 5400 to make it perfect cube.